# Protvino-2014 <br> Diffractive vector meson production in ultra-peripheral collisions at the LHC etc. <br> László Jenkovszky (BITP, Kiev) 

## Diffraction in:

- Elastic hadron scattering,
- Inelastic hadron scattering (SD, DD, CED),
- Exclusive ep collisions (HERA),
- Ultra-peripheral pp, Ap and AA collisions (LHC)
L.J. with R. Fiore, S. Fazio, A. Lengyel, R. Orava, F. Paccanoni, A. Papa, E. Predazzi, A. Papa et al.


## Elastic and total cross sections:

Anton Godizov: Current stage... , arXiv: 1404.7678;
S. Troshin and N. Tyurin: PR D 88(2013)077502;

Igor Dremin: Pomeranchuk centennial seminar, arXiv: 1311.4159 .

Elastic and DD
Roman Ryutin: arXiv: 1404.7678;
V.A. Petrov's School in Protvino;
L. J. + R.Fiore, S. Fazio, O, Kuprash, V. Magas, Risto Orava, A. Salii
(PR D \& Yad. Fizika, 2012-2014)


## Elastic Scattering

## $\sqrt{s}=14 \mathrm{TeV}$ prediction of BSW model



CNI region: $\left|f_{c}\right| \sim\left|f_{N}\right| \rightarrow$ LHC: - $\dagger \sim 6.510^{-4} \mathrm{GeV}^{2} ; \theta_{\text {min }} \sim 3.4 \mu \mathrm{rad}$

$$
\left(\theta_{\min } \sim 120 \mu \mathrm{rad} \text { @ SPS }\right)
$$

## Geometrical scaling (GS), saturation and unitarity

1. On-shell (hadronic) reactions (s,t, $Q^{\wedge} 2=\mathrm{m}^{\wedge} 2$ );
$t \leftrightarrow \rightarrow$ transformation: $h(s, b)=\int_{0}^{\infty} d \sqrt{-t} \sqrt{-t} A(s, t)$ and dictionary:


$\sigma_{t}(s)=\frac{4 \pi}{s} \operatorname{Im} A(s, t=0) ; \quad \frac{d \sigma}{d t}=\frac{\pi}{s^{2}}|A(s, t)|^{2} ; \quad n(s) ;$
$\sigma_{e l}=\int_{t_{m i n} \approx-s / 2 \approx \infty}^{t_{t h r} \approx 0} \frac{d \sigma}{d t} ; \quad \sigma_{i n}=\sigma_{t}-\sigma_{e l} ; \quad B(s, t)=\frac{d}{d t} \ln \left(\frac{d \sigma}{d t}\right) ;$
(and ratios: $\sigma / \mathrm{B}, \ldots . . .$. ).
$A_{p p}^{p \bar{p}}(s, t)=P(s, t) \pm O(s, t)+f(s, t) \pm \omega(s, t) \rightarrow_{L H C} \approx P(s, t) \pm O(s, t)$,
where $P, \quad O, \quad f . \omega$ are the Pomeron, odderon and non-leading Reggeon contributions.

| $\boldsymbol{\alpha}(\mathbf{0}) \backslash \mathbf{C}$ | + | - |
| :---: | :---: | :---: |
| $\mathbf{1}$ | $\mathbf{P}$ | $\mathbf{O}$ |
| $\mathbf{1} / \mathbf{2}$ | $\mathbf{f}$ | $\boldsymbol{\omega}$ |



Local slope, $\mathrm{Y}=\mathrm{B}(\mathrm{t})$ from the new TOTEM data (Jan Kašpar's talk): A. Lengyel et al. (Uzhgrorod, 1994), V. Ezhela (ISMD, Alushta, 2004), S. Denisov Protivno)


## Pomeron dominance at the LHC

Energy variation of the relative importance of the Pomeron with respect to contributions from the secondary trajectories and the Odderon:

$$
\begin{equation*}
R(s, t=0)=\frac{\Im m\left(A(s, t)-A_{P}(s, t)\right)}{\Im A(s, t)} \tag{1}
\end{equation*}
$$

where the total scattering amplitude $A$ includes the Pomeron contribution $A_{P}$ plus the contribution from the secondary Reggeons and the Odderon.

Starting from the Tevatron energy region, the relative contribution of the non-Pomeron terms to the total cross-section becomes smaller than the experimental uncertainty and hence at higher energies they may be completely neglected, irrespective of the model used.

$$
\begin{equation*}
R(s, t)=\frac{\mid\left(A(s, t)-\left.A_{P}(s, t)\right|^{2}\right.}{|A(s, t)|^{2}} . \tag{2}
\end{equation*}
$$




L. Jenkovszky, A. Lengyel, D. Lontkovskyi, The Pomeron and Odderon in elastic, inelastic and total cross sections at the LHC, Int. J. Mod. Phys. A 26, \# 26 \& 27 (2011) 4755-4771, arXiv:1105.1202

## Phenomenology

## R.J.J. Phillips and V. Barger, Model independent analysis

 of the structure in pp scattering, Phys. Lett. B 46 (1973) 412.Phillips and Barger in 1973 [ ], right after its first observation at the ISR. Their formula reads

$$
\begin{equation*}
\frac{d \sigma}{d t}=|\sqrt{A} \exp (B t / 2)+\sqrt{C} \exp (D t / 2+i \phi)|^{2} \tag{1}
\end{equation*}
$$

where $A, B, C, D$ and $\phi$ are determined independently at each energy.



- Some open questions:
- 0) Definition of diffraction: rapidity gap vs. P exchange;
- 1) The ratio between SD, DD and CD?
- 2) Integrated cross section require the knowledge of the M- dependence for all M! Low- and high M:

3) Duality in M (FMSR);
4) Structures in $t$ : a dip in $t \sim 1 \mathrm{GeV}^{\wedge} 2, \ldots$

- 5) The background (in s and in M);
- 6) Exclusive-inclusive relation;
- 7) From elastic to inelastic diffraction (dis)continuity.


## Simple (but approximate) factorization relations

$$
\begin{equation*}
\frac{d^{3} \sigma_{D D}}{d t d M_{1}^{2} d M_{2}^{2}}=\frac{d^{2} \sigma_{S D 1}}{d t d M_{1}^{2}} \frac{d^{2} \sigma_{S D 2}}{d t d M_{2}^{2}} / \frac{d \sigma_{e l}}{d t} . \tag{1}
\end{equation*}
$$

Assuming $e^{b t}$ dependence for both SD and elastic scattering, integration over $t$ yields

$$
\begin{equation*}
\frac{d^{3} \sigma_{D D}}{d M_{1}^{2} d M_{2}^{2}}=k \frac{d^{2} \sigma_{S D 1}}{d M_{1}^{2}} \frac{d^{2} \sigma_{S D 2}}{d M_{2}^{2}} / \sigma_{e l} . \tag{2}
\end{equation*}
$$

where $k=r^{2} /(2 r-1), \quad r=b_{S D} / b_{e l}$.


## TriTriple Regge (Pomeron) limit::



FNAL


## Alternative (to the triple Regge) approach: Diffraction dissociation and DIS :


G.A. Jaroszkiewicz and P.V. Landshoff, Phys. Rev. 10 (1974) 170; A. Donnachie, P.V. Landshoff, Nucl. Phys. B 244 (1984) 322.

R. Fiore \{lit et al.\} EPJ A 15 (2002) 505,hep-ph/0206027;
R. Fiore \{lit et al.\} Phys. Rev. D 68 (2004) 014004, hep-ph/0308178.

## Dual properties of the inelastic SF (transition amplitude)


L. Jenkovszky, V.K. Magas, and E. Predazzi, EPJA 12 (2001) 36; hep-ph/0110374.


The $p p$ scattering amplitude

$$
\begin{align*}
& A(s, t)_{P}= \\
& -\beta^{2}\left[f^{u}(t)+f^{d}(t)\right]^{2}\left(\frac{s}{s_{0}}\right)^{\alpha_{P}(t)-1} \frac{1+e^{-i \pi \alpha_{P}(t)}}{\sin \pi \alpha_{P}(t)} \tag{1}
\end{align*}
$$

where $f^{u}(t)$ and $f^{d}(t)$ are the amplitudes for the emission of $u$ and $d$ valence quarks by the nucleon, $\beta$ is the quark-Pomeron coupling, to be determined below; $\alpha_{P}(t)$ is a vacuum Regge trajectory. It is assumed that the Pomeron couples to the proton via quarks like a scalar photon.

A single-Pomeron exchange is valid at the LHC energies, however at lower energies (e.g. those of the ISR or the SPS) the contribution of non-leading Regge exchanges should be accounted for as well.

Thus, the unpolarized elastic $p p$ differential cross section is

$$
\begin{equation*}
\frac{d \sigma}{d t}=\frac{\left[3 \beta F^{p}(t)\right]^{4}}{4 \pi \sin ^{2}\left[\pi \alpha_{P}(t) / 2\right]}\left(s / s_{0}\right)^{2 \alpha_{P}(t)-2} \tag{2}
\end{equation*}
$$

Similar to the case of elastic scattering, the double differential cross section for the SDD reaction, by Regge factorization, can be written as

$$
\begin{align*}
& \frac{d^{2} \sigma}{d t d M_{X}^{2}}=\frac{9 \beta^{4}\left[F^{p}(t)\right]^{2}}{4 \pi \sin ^{2}\left[\pi \alpha_{P}(t) / 2\right]}\left(s / M_{X}^{2}\right)^{2 \alpha_{P}(t)-2} \times  \tag{1}\\
& {\left[\frac{W_{2}}{2 m}\left(1-M_{X}^{2} / s\right)-m W_{1}\left(t+2 m^{2}\right) / s^{2}\right]}
\end{align*}
$$

where $W_{i}, \quad i=1,2$ are related to the structure functions of the nucleon and $W_{2} \gg W_{1}$. For high $M_{X}^{2}$, the $W_{1,2}$ are Regge-behaved, while for small $M_{X}^{2}$ their behavior is dominated by nucleon resonances. The knowledge of the inelastic form factors (or transition amplitudes) is crucial for the calculation of low-mass diffraction dissociation.

At the lower vertex, the inelastic FF (transition amplitude) is the structure function

$$
W_{2}\left(M_{X}^{2}, t\right)=\frac{-t(1-x)}{4 \pi \alpha_{s}\left(1+4 m^{2} x^{2} /(-t)\right)} \operatorname{Im} A\left(M_{X}^{2}, t\right)
$$

(here the Briorken variable $x \sim-t / M_{X}^{2}$ ), where the imaginary part of the transition amplitude is

$$
\operatorname{Im} A\left(M_{X}^{2}, t\right)=a \sum_{n=0,1, \ldots} \frac{[f(t)]^{2(n+1)} \operatorname{Im} \alpha\left(M_{x}^{2}\right)}{\left(2 n+0.5-\operatorname{Re} \alpha\left(M_{X}^{2}\right)\right)^{2}+\left(\operatorname{Im} \alpha\left(M_{X}^{2}\right)\right)^{2}}
$$




The imaginary part of the trajectory can be written in the following way:

$$
\begin{equation*}
\mathcal{I} m \alpha(s)=s^{\delta} \sum_{n} c_{n}\left(\frac{s-s_{n}}{s}\right)^{\lambda_{n}} \cdot \theta\left(s-s_{n}\right) \tag{1}
\end{equation*}
$$

where $\lambda_{n}=\mathcal{R e} \alpha\left(s_{n}\right)$.

The real part of the proton trajectory is given by

$$
\begin{equation*}
\mathcal{R} e \alpha(s)=\alpha(0)+\frac{s}{\pi} \sum_{n} c_{n} \mathcal{A}_{n}(s), \tag{1}
\end{equation*}
$$

where

$$
\begin{aligned}
& \mathcal{A}_{n}(s)=\frac{\Gamma(1-\delta) \Gamma\left(\lambda_{n}+1\right)}{\Gamma\left(\lambda_{n}-\delta+2\right) s_{n}^{1-\delta}}{ }^{2} F_{1}\left(1,1-\delta ; \lambda_{n}-\delta+2 ; \frac{s}{s_{n}}\right) \theta\left(s_{n}-s\right)+ \\
& \left\{\pi s^{\delta-1}\left(\frac{s-s_{n}}{s}\right)^{\lambda_{n}} \cot [\pi(1-\delta)]-\right. \\
& \left.\frac{\Gamma(-\delta) \Gamma\left(\lambda_{n}+1\right) s_{n}^{\delta}}{s \Gamma\left(\lambda_{n}-\delta+1\right)}{ }_{2} F_{1}\left(\delta-\lambda_{n}, 1 ; \delta+1 ; \frac{s_{n}}{s}\right)\right\} \theta\left(s-s_{n}\right) .
\end{aligned}
$$

## SD and DD cross sections

$$
\begin{aligned}
& \frac{d^{2} \sigma_{S D}}{d t d M_{x}^{2}}=F_{p}^{2}(t) F\left(x_{B}, t\right) \frac{\sigma_{T}^{P p}\left(M_{x}^{2}, t\right)}{2 m_{p}}\left(\frac{s}{M_{x}^{2}}\right)^{2(\alpha(t)-1)} \ln \left(\frac{s}{M_{x}^{2}}\right) \\
& \frac{d^{3} \sigma_{D D}}{d t d M_{1}^{2} d M_{2}^{2}}=C_{n} F^{2}\left(x_{B}, t\right) \frac{\sigma_{T}^{P p}\left(M_{1}^{2}, t\right)}{2 m_{p}} \frac{\sigma_{T}^{P p}\left(M_{2}^{2}, t\right)}{2 m_{p}} \\
& \times\left(\frac{s}{\left(M_{1}+M_{2}\right)^{2}}\right)^{2(\alpha(t)-1)} \ln \left(\frac{s}{\left(M_{1}+M_{2}\right)^{2}}\right)
\end{aligned}
$$

## "Reggeized (dual) Breit-Wigner" formula:

$$
\begin{gathered}
\sigma_{T}^{P p}\left(M_{x}^{2}, t\right)=\operatorname{Im} A\left(M_{x}^{2}, t\right)=\frac{A_{N^{*}}}{\sum_{n} n-\alpha_{N^{*}}\left(M_{x}^{2}\right)}+B g\left(t, M_{x}^{2}\right)= \\
=A_{n} \sum_{n=0,1, \ldots} \frac{[f(t)]^{2(n+1)} \operatorname{Im} \alpha\left(M_{x}^{2}\right)}{\left(2 n+0.5-\operatorname{Re} \alpha\left(M_{x}^{2}\right)\right)^{2}+\left(\operatorname{Im} \alpha\left(M_{x}^{2}\right)\right)^{2}}+B_{n} e^{b_{i n}^{b g}}\left(M_{x}^{2}-M_{p+\pi}^{2}\right)^{\epsilon} \\
F\left(x_{B}, t\right)=\frac{x_{B}\left(1-x_{B}\right)}{\left(M_{x}^{2}-m_{p}^{2}\right)\left(1+4 m_{p}^{2} x_{B}^{2} /(-t)\right)^{3 / 2}}, \quad x_{B}=\frac{-t}{M_{x}^{2}-m_{p}^{2}-t} \\
F_{p}(t)=\frac{1}{1-\frac{t}{0.71}}, \quad f(t)=e^{b_{i n} t} \\
\alpha(t)=\alpha(0)+\alpha^{\prime} t=1.04+0.25 t
\end{gathered}
$$

## SDD cross sections vs. energy.




## Approximation of background to reference points ( $\mathrm{t}=-0.05$ )




## Approximation of background to reference points ( $\mathrm{t}=-0.5$ )




## B-slopes for SD



## Double differential SD cross sections




## DDD cross sections vs. energy.




## Triple differential DD cross sections



## Prospects (future plans): central diffractive meson production (double Pomeron exchange)



## Open problems:

1. Interpolation in energy: from the Fermilab and ISR to the LHC; (Inclusion of non-leading contributions);
2. Deviation from a simple Pomeron pole model and breakdown of Regge-factorization;
3. Experimental studies of the exclusive channels ( $p+\pi, \ldots$ ) produced from the decay of resonances (N*, Roper?,,,) in the nearly forward direction.
4. Turn down of the cross section towards $t=0$ ?!

(a)

(b)

(c)

Diagrams of DVCS (a) and VMP (b) amplitudes and their Reggefactorized form (c)

## Regge-type DVCS amplitude

M. Capua, S. F., R. Fiore, L. L. Jenkovszky, and F Paccanoni

Published in: Physics Letters B645 (Feb. 2007) 161-166


Applications for the model can be:

- Study of various regimes of the scattering amplitude vs Q2, W, t (perturbative $\rightarrow$ unperturbative QCD)
- Study of GPD

DVCS amplitude: $\quad A\left(s, t, Q^{2}\right)_{\gamma^{*} p \rightarrow p}=-A_{0} V_{1}\left(t, Q^{2}\right) V_{2}(t)\left(-i s / s_{0}\right)^{\alpha(t)}$ the $t$ dependence at the vertex $p I P p$ is introduced by: $\quad \alpha(t)=\alpha(0)-\alpha_{1} \ln \left(1-\alpha_{2} t\right)$ the vertex $\gamma^{* I P \gamma}$ is introduced by the trajectory:

$$
\beta(z)=\beta(0)-\beta \ln \left(1-\beta_{2} z\right)
$$

indicating with: $L=\ln \left(-i s / s_{0}\right)$ the DVCS amplitude can be written as:

$$
A\left(s, t, Q^{2}\right)_{\gamma^{*} p \rightarrow p}=-A_{0} e^{b \alpha(t)} e^{b \beta(z)}\left(-i s / s_{0}\right)^{\alpha(t)}=-A_{0} e^{(b+L) \alpha(t)+b \beta(z)}
$$

## Exclusive diffraction



## Main kinematic variables

electron-proton centre-of-mass energy:

$$
s=(k+p)^{2} \approx 4 E_{e} E_{p}
$$

photon virtuality:

$$
Q^{2}=-q^{2}=-\left(k-k^{\prime}\right)^{2} \approx 4 E_{e} E_{e}^{\prime} \sin ^{2} \frac{\theta}{2}
$$

photon-proton centre-of-mass energy:

$$
W^{2}=(q+p)^{2}, \text { where : } m_{p}<W<\sqrt{s}
$$

$$
\text { square 4-momentum at the } p \text { vertex: }
$$

$$
t=\left(p^{\prime}-p\right)^{2}
$$

$>$ Vector Mesons production in diffraction
$>$ Deeply Virtual Compton Scattering

## Deeply Virtual Compton Scattering



## DVCS properties:

- Similar to VM production, but $\gamma$ instead of VM in the final state
- No VM wave-function involved
- Important to determine Generalized Parton Distributions sensible to the correlations in the proton
- GPD ${ }_{\mathrm{s}}$ are an ingredient for estimating diffractive cross sections
 at the LHC


## $b\left(Q^{2}+M^{2}\right)-V M$



## Basic ideas

Reggeometry=Regge+geometry (play on words, or pun)
How to combine $s, t$ and $Q^{\wedge} 2$ dependencies in a binary reaction?

1. The $t$ and $\tilde{Q}^{2}$ depedences are combined by "geometry":

A rough estimates (to be fine-tuned!) yields

$$
\beta\left(t, M, Q^{2}\right)=\exp \left[4\left(\frac{1}{M_{V}^{2}+Q^{2}}+\frac{1}{2 m_{N}^{2}}\right) t\right] .
$$

2. The $s$ and $t$ behavior are related by the Regge-pole model;
3. There is only one, universal, Pomeron, but it has two components - soft and hard, their relative weights depending on $\tilde{Q}^{2}$.


$$
\begin{gathered}
A\left(s, t, Q^{2}, M_{v}^{2}\right)=\frac{\tilde{A}_{s}}{\left(1+\frac{\widetilde{Q^{2}}}{\widetilde{Q_{s}^{2}}}\right)^{n_{s}}} e^{-i \frac{\pi}{2} \alpha_{s}(t)}\left(\frac{s}{s_{0 s}}\right)^{\alpha_{s}(t)} e^{2\left(\frac{a_{s}}{Q^{2}}+\frac{b_{s}}{2 m_{p}^{2}}\right) t} \\
+\frac{\tilde{A_{h}}\left(\frac{\widetilde{Q^{2}}}{\widetilde{Q_{h}^{2}}}\right)}{\left(1+\frac{\widetilde{Q^{2}}}{\widetilde{Q}_{h}^{2}}\right)^{n_{h}+1}} e^{-i \frac{\pi}{2} \alpha_{h}(t)}\left(\frac{s}{s_{0 h}}\right)^{\alpha_{h}(t)} e^{2\left(\frac{a_{h}}{Q^{2}}+\frac{b_{h}}{2 m_{p}^{2}}\right) t}
\end{gathered}
$$

|  | $A_{s}$ | $\widetilde{Q}_{s}^{2}$ | $n_{s}$ | $\alpha_{0 s}$ | $\alpha_{s}^{\prime}$ | $a_{s}$ | $b_{s}$ | $\tilde{\chi}^{2}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $p p$ | $5.9 \pm 5.7$ | $* * *$ | 0.00 | $1.05 \pm 0.14$ | $0.276 \pm 0.474$ | $2.877 \pm 2.837$ | 0.00 | 1.52 |
| $\rho^{0}$ | $59.5 \pm 29.3$ | 1.33 | $1.35 \pm 0.05$ | $1.15 \pm 0.06$ | 0.15 | -0.22 | 1.69 | 6.56 |
| $\phi$ | $31.8 \pm 35.3$ | 1.30 | $1.32 \pm 0.10$ | $1.14 \pm 0.12$ | 0.15 | $-0.85 \pm 1.60$ | $2.51 \pm 2.67$ | 3.81 |
| $J / \psi$ | $34.2 \pm 19.0$ | $1.4 \pm 0.7$ | $1.39 \pm 0.13$ | $1.21 \pm 0.05$ | 0.09 | 1.90 | 1.03 | 4.50 |
| $\Upsilon(1 S)$ | $37 \pm 101$ | $0.9 \pm 1.7$ | $1.53 \pm 0.55$ | $1.29 \pm 0.26$ | $0.01 \pm 0.6$ | 1.90 | 1.03 | 1.28 |
| $D V C S$ | $9.7 \pm 9.0$ | $0.45 \pm 0.5$ | $0.94 \pm 0.24$ | $1.19 \pm 0.09$ | $-0.007 \pm 0.3$ | $1.94 \pm 4.65$ | $1.74 \pm 2.28$ | 1.75 |

Table 1. Fitting results

|  | $\delta$ | $\alpha_{0 s}$ | $\alpha_{0 s}($ fit $)$ | $\alpha_{s}^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: |
| $p p$ |  | $1.08(\mathrm{DL})$ | $1.05 \pm 0.14$ | $0.276 \pm 0.474$ |
| $\rho^{0}$ | 0.22 | 1.055 | $1.15 \pm 0.06$ | 0.15 |
| $\phi$ | 0.22 | 1.055 | $1.14 \pm 0.12$ | 0.15 |
| $J / \psi$ | 0.8 | 1.2 | $1.21 \pm 0.05$ | 0.09 |
| $\Upsilon(1 S)$ | 1.6 | 1.4 | $1.29 \pm 0.26$ | $0.01 \pm 0.6$ |
| $D V C S$ | 0.54 | 1.135 | $1.19 \pm 0.09$ | $-0.007 \pm 0.3$ |

Table 2. $\alpha(0), \alpha^{\prime}$

Parameter $s_{0 s}$ for simplicity is also fixed $s_{0 s}=1$.
(a) The $W$ dependence of the cross section for exclusive VM photoproduction together with the total photoproduction cross section. Lines are the result of a $W^{\delta}$ fit to the data at high $W$-energy values.

* Parameters that doesn't have errors in table[1] were fixed at fitting stage.


## rho0(1)



## phi (1)







## J/psi (1)



## DVCS (1)




The differential cross section reads:

$$
\begin{gathered}
\frac{d \sigma\left(h_{1}+h_{2} \rightarrow h_{1}+V+h_{2}\right)}{d Y} \\
\omega_{+} \frac{d N_{\gamma / h_{1}}\left(\omega_{+}\right)}{d \omega} \sigma_{\gamma h_{2} \rightarrow V h_{2}}\left(\omega_{+}\right)+\omega_{-} \frac{d N_{\gamma / h_{2}}\left(\omega_{-}\right)}{d \omega} \sigma_{\gamma h_{1} \rightarrow V h_{1}}\left(\omega_{-}\right),
\end{gathered}
$$

where $\frac{d N_{\gamma / h}(\omega)}{d \omega}$ is the "equivalent" photon flux $\frac{d N_{\gamma / h}(\omega)}{d \omega}=\frac{\alpha_{e m}}{2 \pi \omega}\left[1+\left(1-\frac{2 \omega}{\sqrt{s}}\right)^{2}\right](\ln \Omega-$ $\left.\frac{11}{6}+\frac{3}{\Omega}-\frac{3}{2 \Omega^{2}}+\frac{1}{3 \Omega^{3}}\right)$ and $\sigma_{\gamma p \rightarrow V p}(\omega)$ is the total cross section of the vector meson photoproduction subprocess. $\omega$ is the photon energy, $\omega=W_{\gamma p}^{2} / 2 \sqrt{s}_{p p}$ with $\omega_{\text {min }}=M_{V}^{2} /\left(4 \gamma_{L} m_{p}\right)$, where $\gamma_{L}=\sqrt{s} /\left(2 m_{p}\right)$ is the Lorentz factor, e.g., for pp at the LHC for $\sqrt{s}=7 \mathrm{TeV}, \gamma_{L}=3731$.

## Power law vs geometric model at LHC




Generally similar behaviour
Power law is somewhat steeper in $\mathrm{W} \rightarrow$ a more distinct bell-like structure in y

## Adding LHCb rapidity cross section




Both power law and geometric model are much flatter than the data

By fitting the power (and normalization) a much better description of data can be obtained (green curve)
However, power tends to be very small ( $\delta=0.37$ ) which contradicts HERA (page 4)

## Grand comparison

Here all available curves are summarized, also the result using the logarithmic growth of the photc


Logarithm describes data best

## үp cross section




## Спасибо!

