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# CPT and QM tests using kaon Interferometry



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# CPT: introduction

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The three discrete symmetries of QM, C (charge conjugation), P (parity), and T (time reversal) are known to be violated in nature both singly and in pairs. Only CPT appears to be an exact symmetry of nature.

CPT theorem (Luders, Jost, Pauli, Bell 1955 -1957):

Exact CPT invariance holds for any quantum field theory which assumes:

(1) Lorentz invariance (2) Locality (3) Unitarity (i.e. conservation of probability).

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Extension of CPT theorem to a theory of quantum gravity far from obvious (e.g. CPT violation appears in some models with space-time foam backgrounds).

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The neutral kaon system offers unique possibilities to test CPT invariance e.g. :

$$\left| m_{K^0} - m_{\bar{K}^0} \right| / m_K < 10^{-18}, \quad \left| m_{B^0} - m_{\bar{B}^0} \right| / m_B < 10^{-14}, \quad \left| m_p - m_{\bar{p}} \right| / m_p < 10^{-8}$$

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# 1) “Standard” test of CPT symmetry in the neutral kaon system

# CPT test: the Bell-Steinberger relation

CPT violation in the mixing

$$|K_{S,L}\rangle = \frac{1}{\sqrt{2(1+|\varepsilon_{S,L}|)}} \left[ (1 + \varepsilon_{S,L}) |K^0\rangle + (1 - \varepsilon_{S,L}) |\bar{K}^0\rangle \right]$$

$$\varepsilon_{S,L} = \varepsilon \pm \delta$$

$$\delta = \frac{1}{2} \frac{(m_{\bar{K}^0} - m_{K^0}) - (i/2)(\Gamma_{\bar{K}^0} - \Gamma_{K^0})}{\Delta m + i\Delta\Gamma/2}$$

$$\Delta m = m_L - m_S$$

$$\Delta\Gamma = \Gamma_S - \Gamma_L$$

$$\phi_{SW} = \arctan(2\Delta m/\Delta\Gamma)$$

Unitarity constraint:  $|K\rangle = a_S |K_S\rangle + a_L |K_L\rangle$

$$\left( -\frac{d}{dt} \| |K(t)\rangle \|^2 \right)_{t=0} = \sum_f |a_S \langle f|T|K_S\rangle + a_L \langle f|T|K_L\rangle|^2$$

$$\left( \frac{\Re\varepsilon}{1+|\varepsilon|^2} - i\Im\varepsilon \right) = \frac{\frac{1}{\Gamma_S - \Gamma_L} \sum_f \langle f|T|K_S\rangle^* \langle f|T|K_L\rangle}{\left( \frac{\Gamma_S + \Gamma_L}{\Gamma_S - \Gamma_L} + i \tan \phi_{SW} \right)}$$

$K_S$   $K_L$  observables

# Experimental inputs to the Bell-Steinberger relation

	Value	Source
$\tau_{K_S}$	$0.08958 \pm 0.00005$ ns	PDG [14]
$\tau_{K_L}$	$50.84 \pm 0.23$ ns	KLOE average
$m_L - m_S$	$(5.290 \pm 0.016) \times 10^9$ s <sup>-1</sup>	PDG [14]
$\text{BR}(K_S \rightarrow \pi^+ \pi^-)$	$0.69186 \pm 0.00051$	KLOE average
$\text{BR}(K_S \rightarrow \pi^0 \pi^0)$	$0.30687 \pm 0.00051$	KLOE average
$\text{BR}(K_S \rightarrow \pi \ell \nu)$	$(11.77 \pm 0.15) \times 10^{-4}$	KLOE [6]
$\text{BR}(K_L \rightarrow \pi^+ \pi^-)$	$(1.933 \pm 0.021) \times 10^{-3}$	KLOE average
$\text{BR}(K_L \rightarrow \pi^0 \pi^0)$	$(0.848 \pm 0.010) \times 10^{-3}$	KLOE average
$\phi_{+-}$	$(43.4 \pm 0.7)^\circ$	PDG [14]
$\phi_{00}$	$(43.7 \pm 0.8)^\circ$	PDG [14]
$R_{S,\gamma} (E_\gamma > 20\text{MeV})$	$(0.710 \pm 0.016) \times 10^{-2}$	E731 [18]
$R_{S,\gamma}^{\text{th-IB}} (E_\gamma > 20\text{MeV})$	$(0.700 \pm 0.001) \times 10^{-2}$	KLOE MC [19]
$ \eta_{+-\gamma} $	$(2.359 \pm 0.074) \times 10^{-3}$	E773 [17]
$\phi_{+-\gamma}$	$(43.8 \pm 4.0)^\circ$	E773 [17]
$\text{BR}(K_L \rightarrow \pi^+ \pi^- \pi^0)$	$0.1262 \pm 0.0011$	KLOE average
$\eta_{+-0}$	$((-2 \pm 7) + i(-2 \pm 9)) \times 10^{-3}$	CPLEAR [10]
$\text{BR}(K_L \rightarrow 3\pi^0)$	$0.1996 \pm 0.0021$	KLOE average
$\text{BR}(K_S \rightarrow 3\pi^0)$	$< 1.5 \times 10^{-7}$ at 95% CL	KLOE [5]
$\phi_{000}$	uniform from 0 to $2\pi$	
$\text{BR}(K_L \rightarrow \pi \ell \nu)$	$0.6709 \pm 0.0017$	KLOE average
$A_L + A_S$	$(0.5 \pm 1.0) \times 10^{-2}$	$K_{\ell 3}$ average
$\text{Im}(x_+)$	$(0.8 \pm 0.7) \times 10^{-2}$	$K_{\ell 3}$ average

Main improvements done with KLOE measurements on  $K_S$  semileptonic and  $3\pi^0$  decays



# CPT test: the Bell-Steinberger relation

**KLOE result:** JHEP12(2006) 011

$$\text{Re } \varepsilon = (159.6 \pm 1.3) \times 10^{-5}$$

$$\text{Im } \delta = (0.4 \pm 2.1) \times 10^{-5}$$

CPLEAR: study of the time evolution of neutral kaons in semileptonic decays

$$\Re \delta = (0.30 \pm 0.33 \pm 0.06) \times 10^{-3}$$

PLB444 (1998) 52

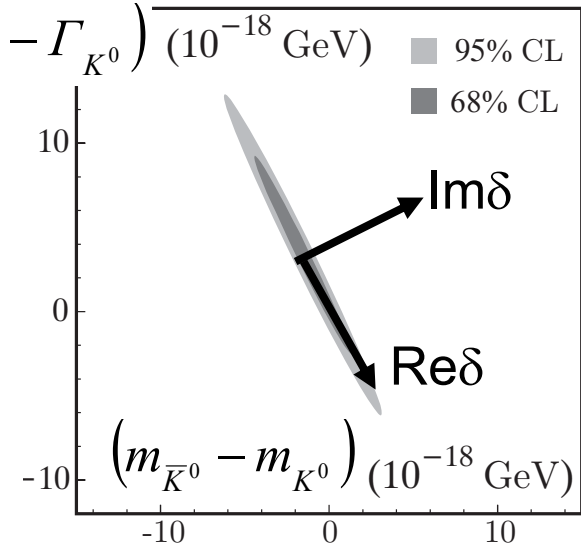
Combining  $\text{Re } \delta$  and  $\text{Im } \delta$  results:

$$\delta = \frac{1}{2} \frac{(m_{\bar{K}^0} - m_{K^0}) - (i/2)(\Gamma_{\bar{K}^0} - \Gamma_{K^0})}{\Delta m + i\Delta\Gamma/2} \quad (\Gamma_{\bar{K}^0} - \Gamma_{K^0}) (10^{-18} \text{ GeV})$$

Assuming  $(\Gamma_{\bar{K}^0} - \Gamma_{K^0}) = 0$ , i.e. no CPT viol. in decay:

$$-5.3 \times 10^{-19} < m_{\bar{K}^0} - m_{K^0} < 6.3 \times 10^{-19} \text{ GeV}$$

at 95% c.l.



# CPT test: the Bell-Steinberger relation

**PDG 2007 fit:**

$$\text{Re } \varepsilon = (161.2 \pm 0.6) \times 10^{-5}$$

$$\text{Im } \delta = (-0.6 \pm 1.9) \times 10^{-5}$$

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PLB444 (1998) 52

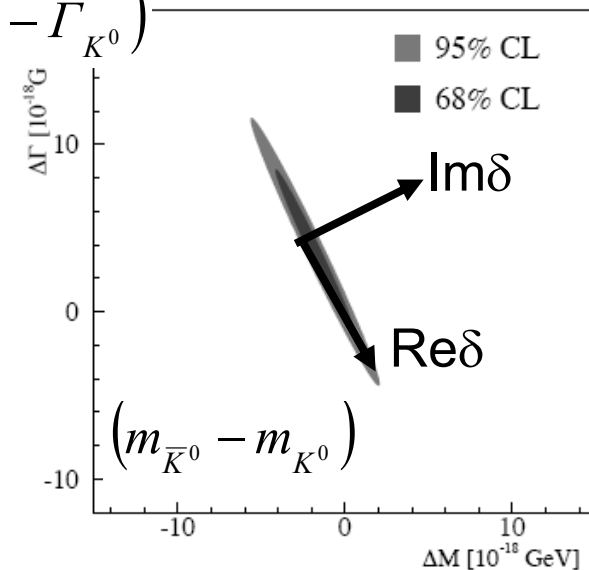
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Assuming  $(\Gamma_{\bar{K}^0} - \Gamma_{K^0}) = 0$ , i.e. no CPT viol. in decay:

$$-5.1 \times 10^{-19} < m_{\bar{K}^0} - m_{K^0} < 5.1 \times 10^{-19} \text{ GeV}$$

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Now main limitation comes from uncertainty on  $\phi_{+-}$   
(expected improvement using new KTeV results)

PLB444 (1998) 52

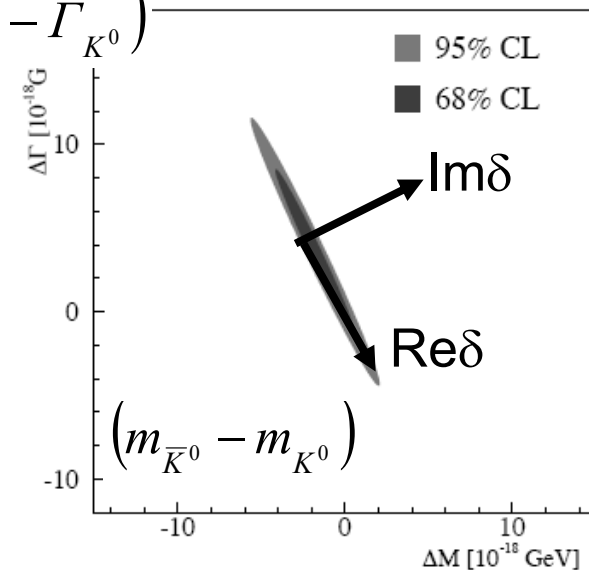
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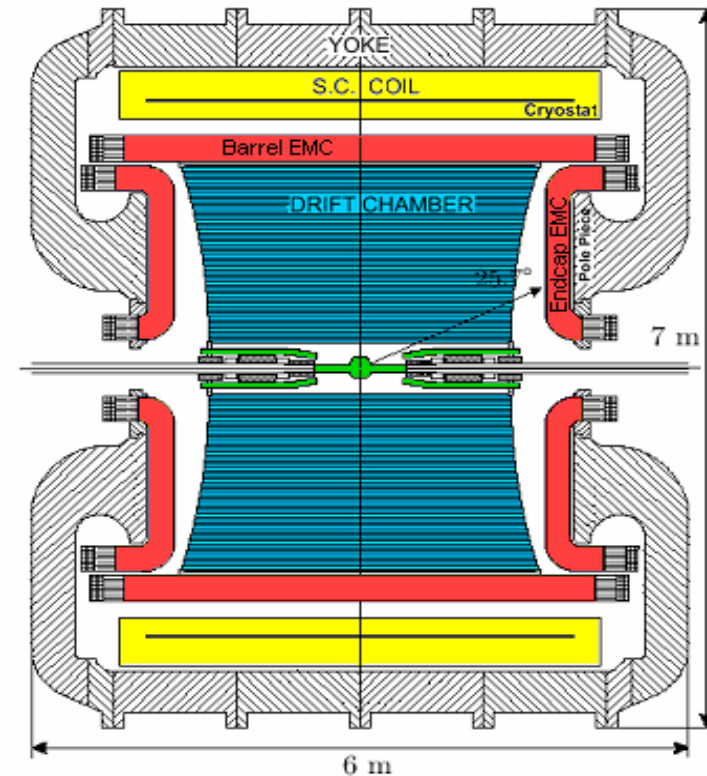


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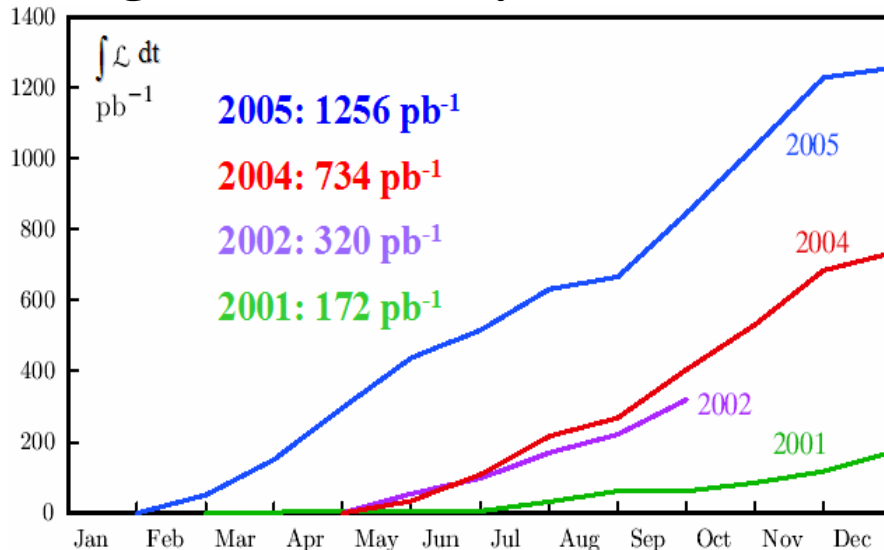
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## **2) Tests of QM and CPT symmetry in the neutral kaon system**

# The KLOE detector at the Frascati $\phi$ -factory DAΦNE



## Integrated luminosity (KLOE)



Lead/scintillating fiber calorimeter  
 drift chamber  
 4 m diameter × 3.3 m length  
 helium based gas mixture

Total KLOE  $\int \mathcal{L} dt \sim 2.5 \text{ fb}^{-1}$   
 (2001 - 05)

$\rightarrow \sim 2.5 \times 10^9 \text{ K}_S \text{K}_L \text{ pairs}$

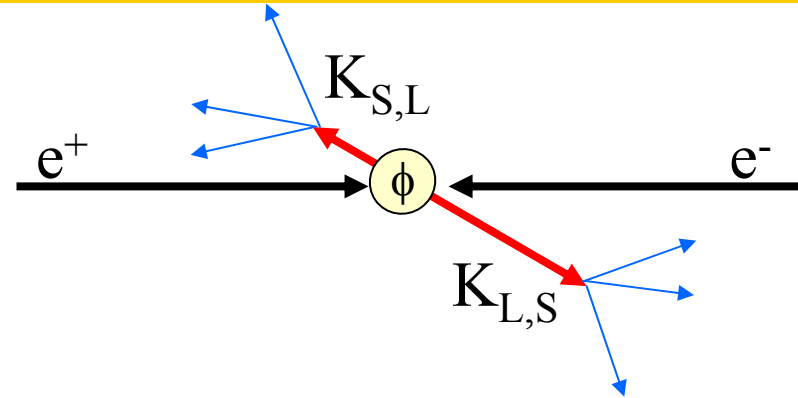
# Neutral kaons at a $\phi$ -factory

Production of the vector meson  $\phi$  in  $e^+e^-$  annihilations:

- $e^+e^- \rightarrow \phi$      $\sigma_\phi \sim 3 \mu\text{b}$   
 $W = m_\phi = 1019.4 \text{ MeV}$
- $\text{BR}(\phi \rightarrow K^0\bar{K}^0) \sim 34\%$
- $\sim 10^6$  neutral kaon pairs per  $\text{pb}^{-1}$  produced in an antisymmetric quantum state with  $J^{PC} = 1^-$  :

$$\mathbf{p}_K = 110 \text{ MeV}/c$$

$$\lambda_S = 6 \text{ mm} \quad \lambda_L = 3.5 \text{ m}$$



$$|i\rangle = \frac{1}{\sqrt{2}} \left[ |K^0(\vec{p})\rangle |\bar{K}^0(-\vec{p})\rangle - |\bar{K}^0(\vec{p})\rangle |K^0(-\vec{p})\rangle \right]$$

$$= \frac{N}{\sqrt{2}} \left[ |K_S(\vec{p})\rangle |K_L(-\vec{p})\rangle - |K_L(\vec{p})\rangle |K_S(-\vec{p})\rangle \right]$$

$$N = \sqrt{(1+|\varepsilon_S|^2)(1+|\varepsilon_L|^2)} / (1-\varepsilon_S\varepsilon_L) \cong 1$$

The detection of a kaon at large (small) times tags a  $K_S$  ( $K_L$ )  
 $\Rightarrow$  possibility to select a pure  $K_S$  beam (**unique** at a  $\phi$ -factory, not possible at fixed target experiments)

# Neutral kaon interferometry

$$|i\rangle = \frac{N}{\sqrt{2}} \left[ |K_S(\vec{p})\rangle |K_L(-\vec{p})\rangle - |K_L(\vec{p})\rangle |K_S(-\vec{p})\rangle \right]$$

Double differential time distribution:

$$I(f_1, t_1; f_2, t_2) = C_{12} \left\{ |\eta_1|^2 e^{-\Gamma_L t_1 - \Gamma_S t_2} + |\eta_2|^2 e^{-\Gamma_S t_1 - \Gamma_L t_2} - 2|\eta_1||\eta_2| e^{-(\Gamma_S + \Gamma_L)(t_1 + t_2)/2} \cos[\Delta m(t_2 - t_1) + \phi_1 - \phi_2] \right\}$$

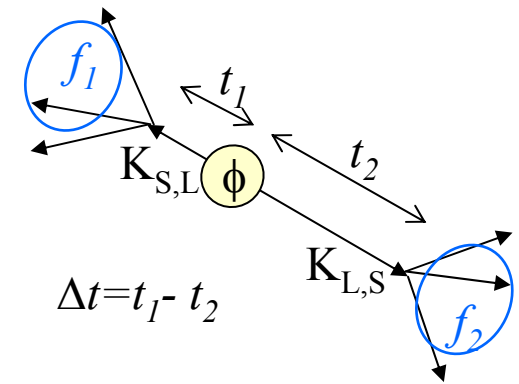
where  $t_1(t_2)$  is the proper time of one (the other) kaon decay into  $f_1$  ( $f_2$ ) final state and:

$$\eta_i = |\eta_i| e^{i\phi_i} = \langle f_i | T | K_L \rangle / \langle f_i | T | K_S \rangle$$

$$C_{12} = \frac{|N|^2}{2} \left| \langle f_1 | T | K_S \rangle \langle f_2 | T | K_S \rangle \right|^2$$

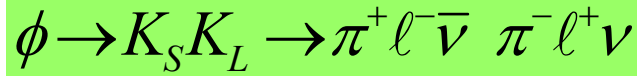
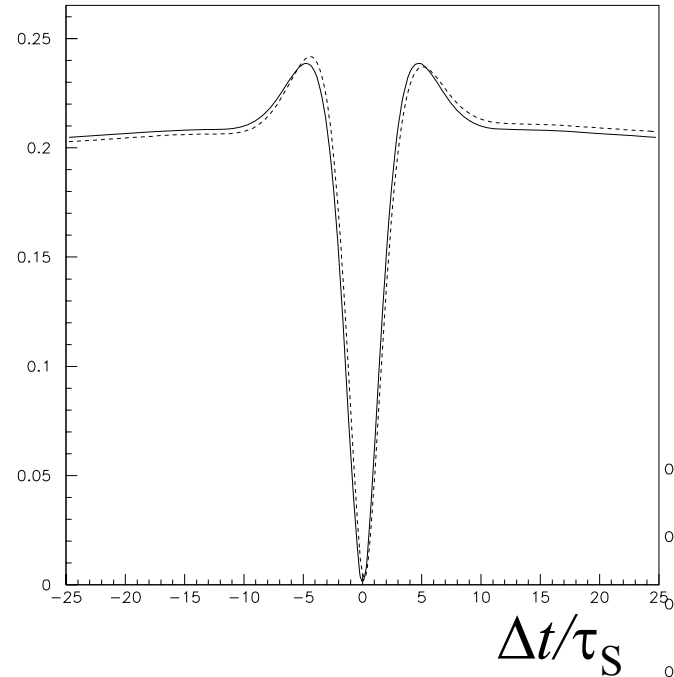
**characteristic interference term  
at a  $\phi$ -factory  $\Rightarrow$  interferometry**

From these distributions for various final states  $f_i$  one can measure the following quantities:  $\Gamma_S$ ,  $\Gamma_L$ ,  $\Delta m$ ,  $|\eta_i|$ ,  $\phi_i \equiv \arg(\eta_i)$

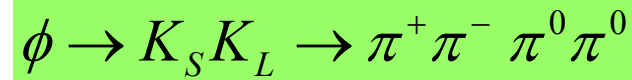
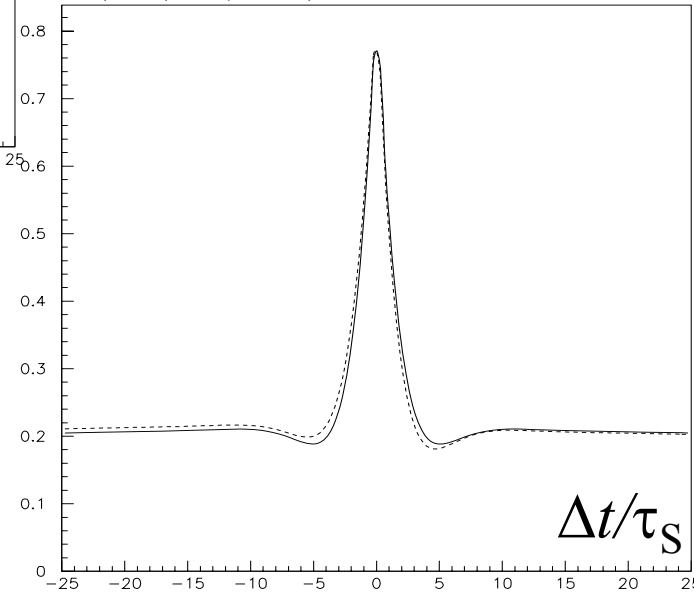


# Neutral kaon interferometry: main observables

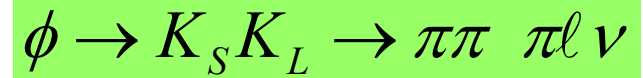
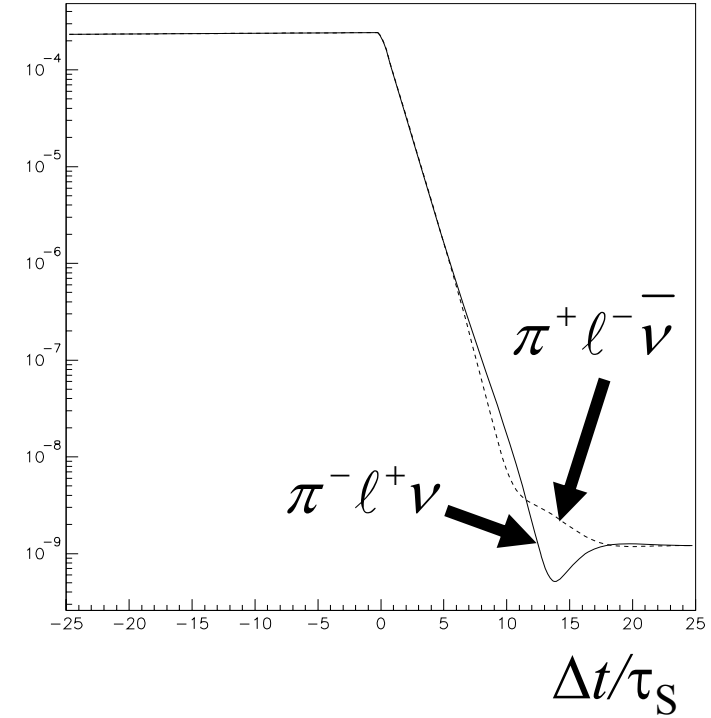
$I(\Delta t)$  (a.u)



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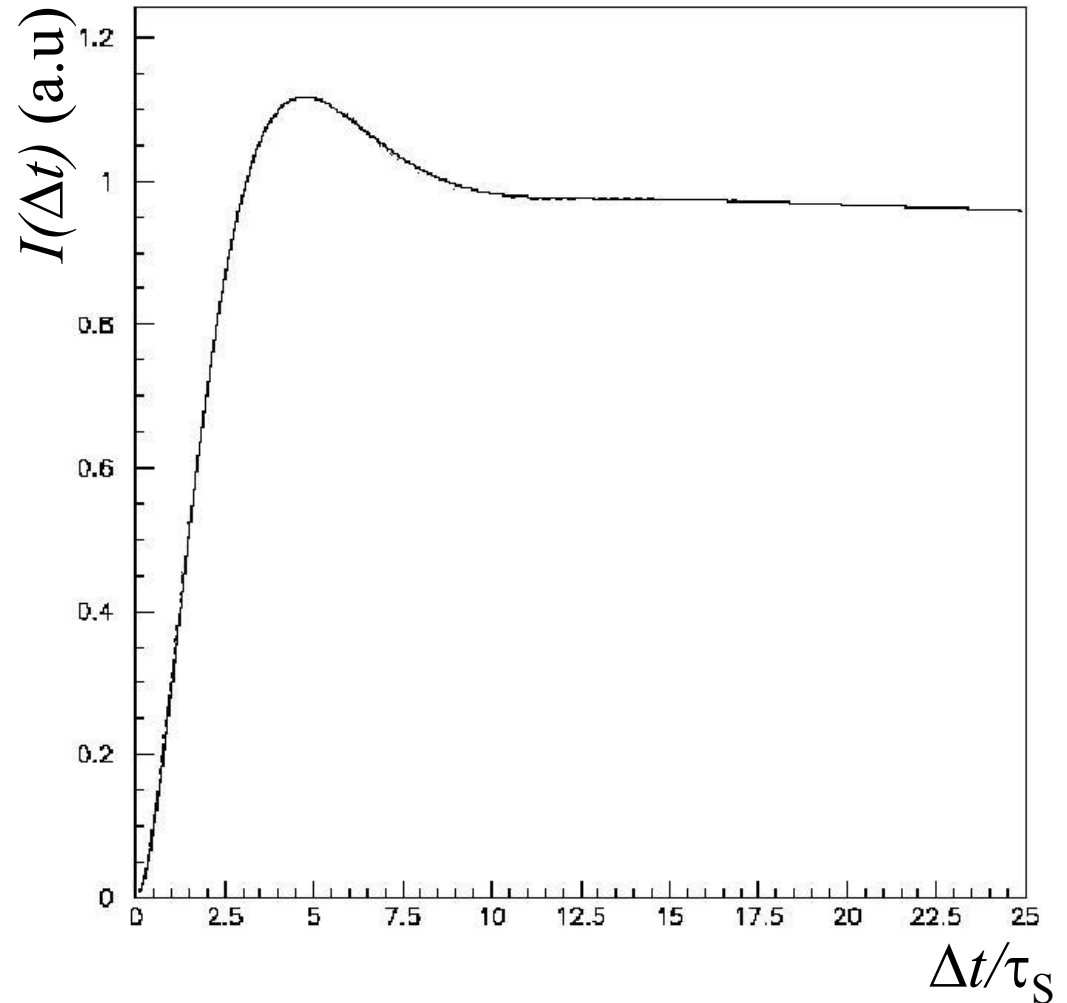
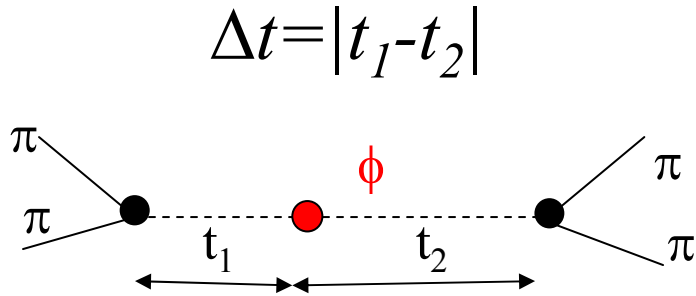




$$\phi \rightarrow K_S K_L \rightarrow \pi^+ \pi^- \quad \pi^+ \pi^-$$

$$|i\rangle = \frac{1}{\sqrt{2}} \left[ |K^0\rangle |\bar{K}^0\rangle - |\bar{K}^0\rangle |K^0\rangle \right]$$

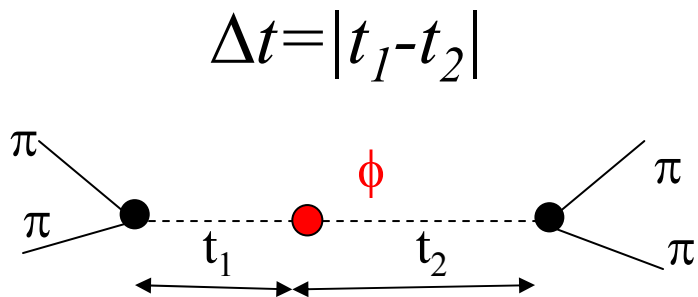
Same final state for both kaons:  $f_1 = f_2 = \pi^+ \pi^-$



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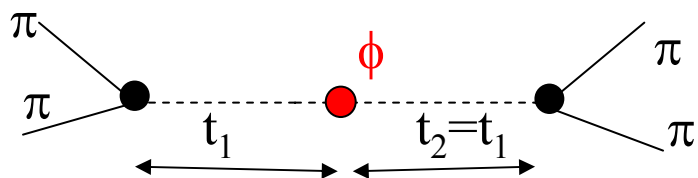
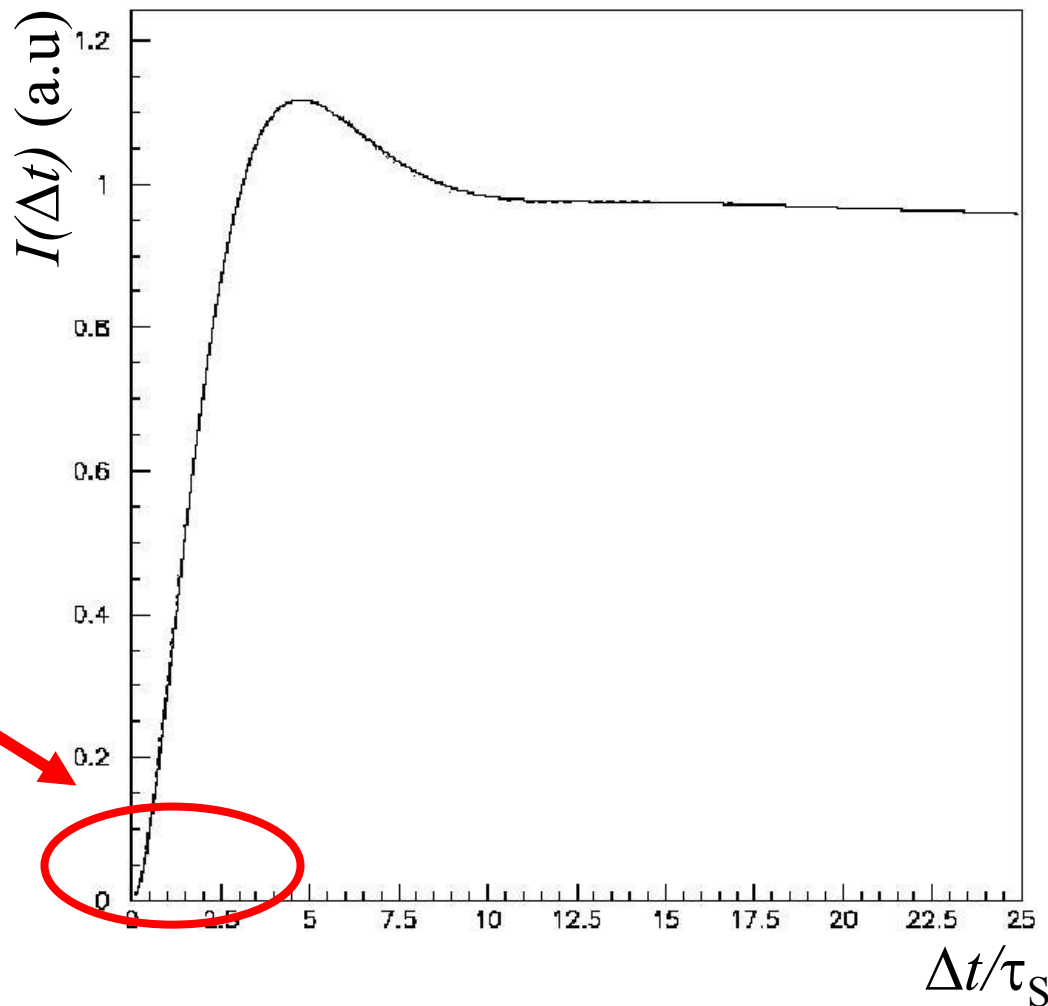
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EPR correlation:

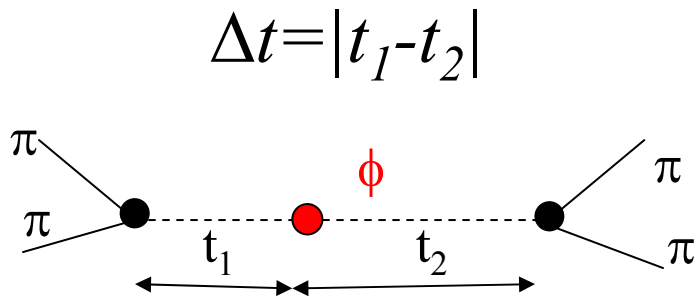
no simultaneous decays  
( $\Delta t=0$ ) in the same  
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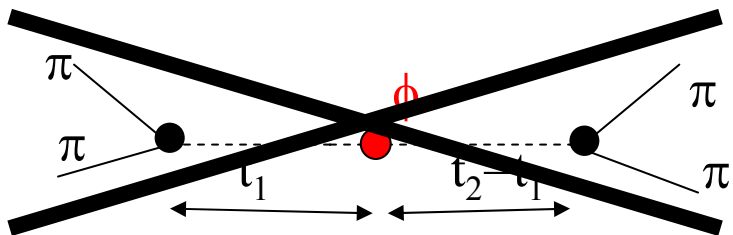
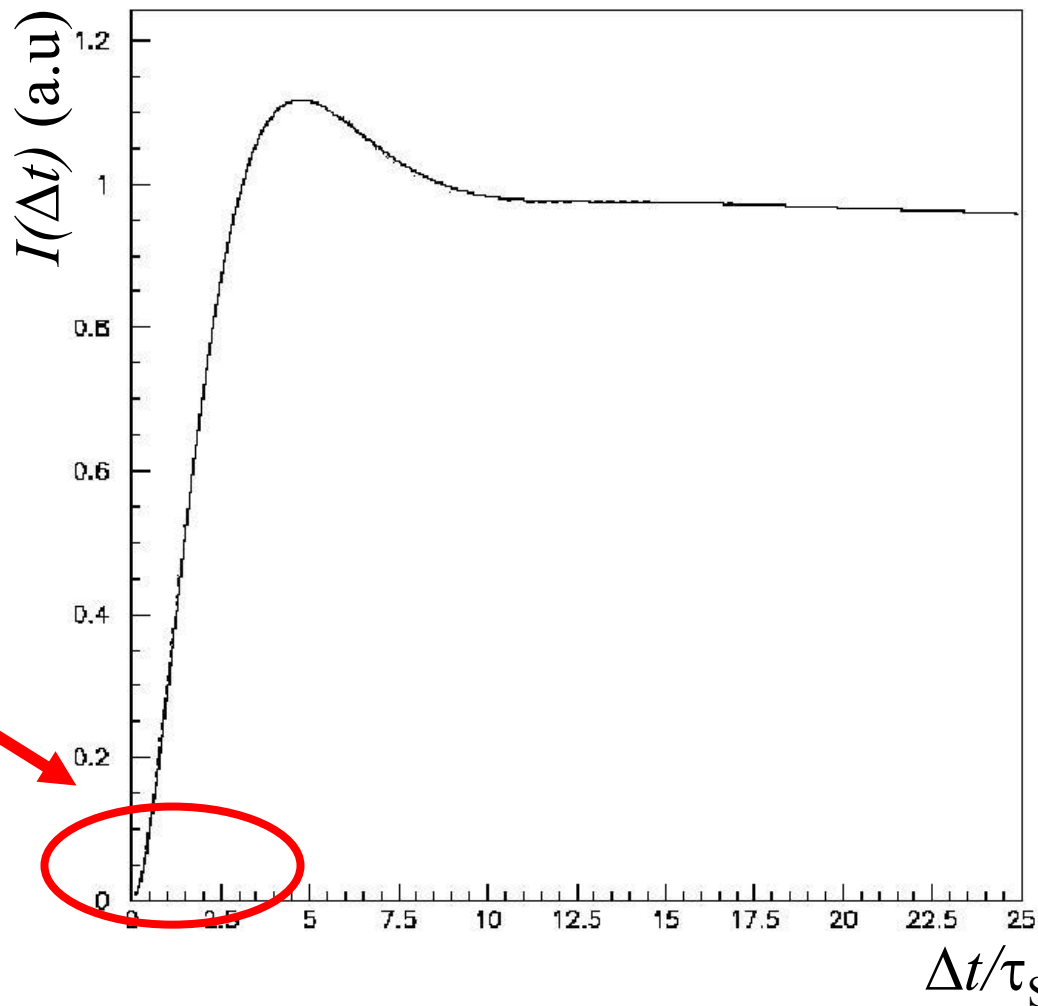
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# $\phi \rightarrow \mathbf{K}_S \mathbf{K}_L \rightarrow \pi^+ \pi^- \pi^+ \pi^-$ : test of quantum coherence

$$|i\rangle = \frac{1}{\sqrt{2}} \left[ |K^0\rangle |\bar{K}^0\rangle - |\bar{K}^0\rangle |K^0\rangle \right]$$

$$I(\pi^+ \pi^-, \pi^+ \pi^-; \Delta t) = \frac{N}{2} \left[ \left| \langle \pi^+ \pi^-, \pi^+ \pi^- | K^0 \bar{K}^0(\Delta t) \rangle \right|^2 + \left| \langle \pi^+ \pi^-, \pi^+ \pi^- | \bar{K}^0 K^0(\Delta t) \rangle \right|^2 - 2 \Re \left( \langle \pi^+ \pi^-, \pi^+ \pi^- | K^0 \bar{K}^0(\Delta t) \rangle \langle \pi^+ \pi^-, \pi^+ \pi^- | \bar{K}^0 K^0(\Delta t) \rangle^* \right) \right]$$

Feynman described the phenomenon of interference as containing “the only mystery” of quantum mechanics

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Decoherence parameter:

$$\zeta_{0\bar{0}} = 0 \rightarrow \text{QM}$$

$$\zeta_{0\bar{0}} = 1 \rightarrow \text{total decoherence} \\ \text{(also known as Furry's hypothesis} \\ \text{or spontaneous factorization)} \\ \text{[W.Furry, PR 49 (1936) 393]}$$

# $\phi \rightarrow \mathbf{K}_S \mathbf{K}_L \rightarrow \pi^+ \pi^- \pi^+ \pi^-$ : test of quantum coherence

- Analysed data:  $L=380 \text{ pb}^{-1}$
- Fit including  $\Delta t$  resolution and efficiency effects + regeneration
- $\Gamma_S, \Gamma_L, \Delta m$  fixed from PDG

**KLOE result:** [PLB 642\(2006\) 315](#)

$$\zeta_{0\bar{0}} = (1.0 \pm 2.1_{\text{STAT}} \pm 0.4_{\text{SYST}}) \times 10^{-6}$$

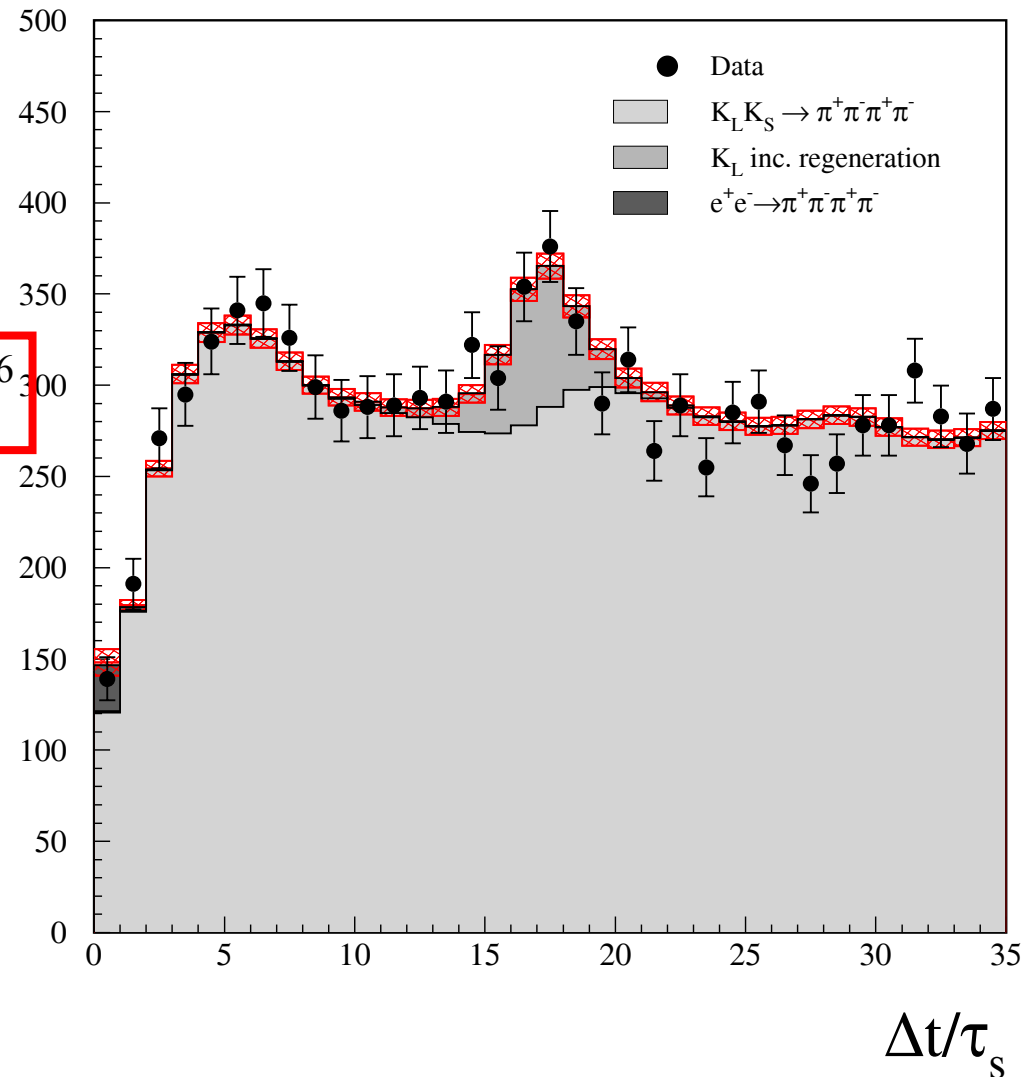
as CP viol.  $O(|\eta_{+-}|^2) \sim 10^{-6}$   
 $\Rightarrow$  high sensitivity to  $\zeta_{0\bar{0}}$

From CPLEAR data, Bertlmann et al.  
(PR D60 (1999) 114032) obtain:

$$\zeta_{0\bar{0}} = 0.4 \pm 0.7$$

In the B-meson system, BELLE coll.  
(PRL 99 (2007) 131802) obtains:

$$\zeta_{0\bar{0}}^B = 0.029 \pm 0.057$$



# $\phi \rightarrow K_S K_L \rightarrow \pi^+ \pi^- \pi^+ \pi^-$ : test of quantum coherence

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- Fit including  $\Delta t$  resolution and efficiency effects + regeneration
- $\Gamma_S, \Gamma_L, \Delta m$  fixed from PDG

**KLOE result:** [PLB 642\(2006\) 315](#)

$$\zeta_{00} = (1.0 \pm 2.1_{\text{STAT}} \pm 0.4_{\text{SYST}}) \times 10^{-6}$$

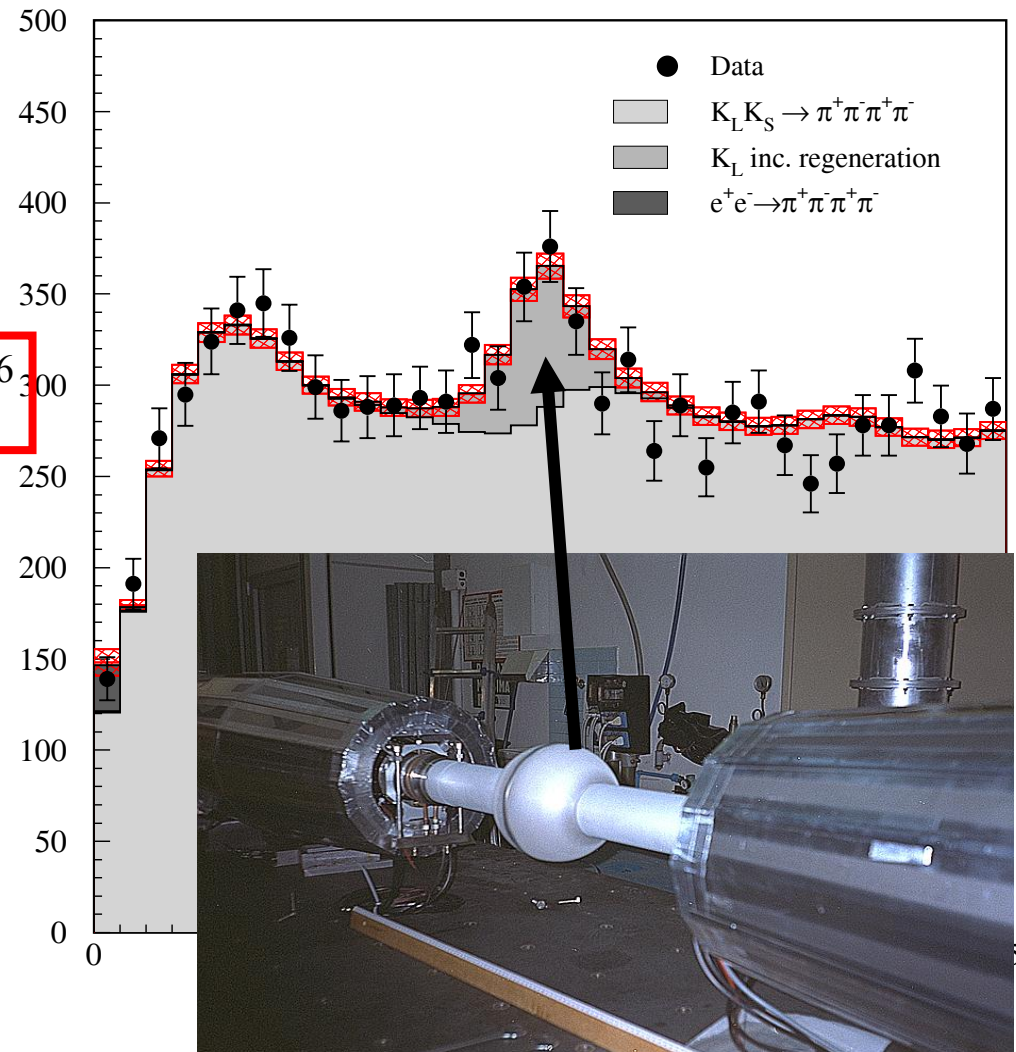
as CP viol.  $O(|\eta_{+-}|^2) \sim 10^{-6}$   
 $\Rightarrow$  high sensitivity to  $\zeta_{00}$

From CPLEAR data, Bertlmann et al.  
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$$\zeta_{00} = 0.4 \pm 0.7$$

In the B-meson system, BELLE coll.  
 (PRL 99 (2007) 131802) obtains:

$$\zeta_{00}^B = 0.029 \pm 0.057$$





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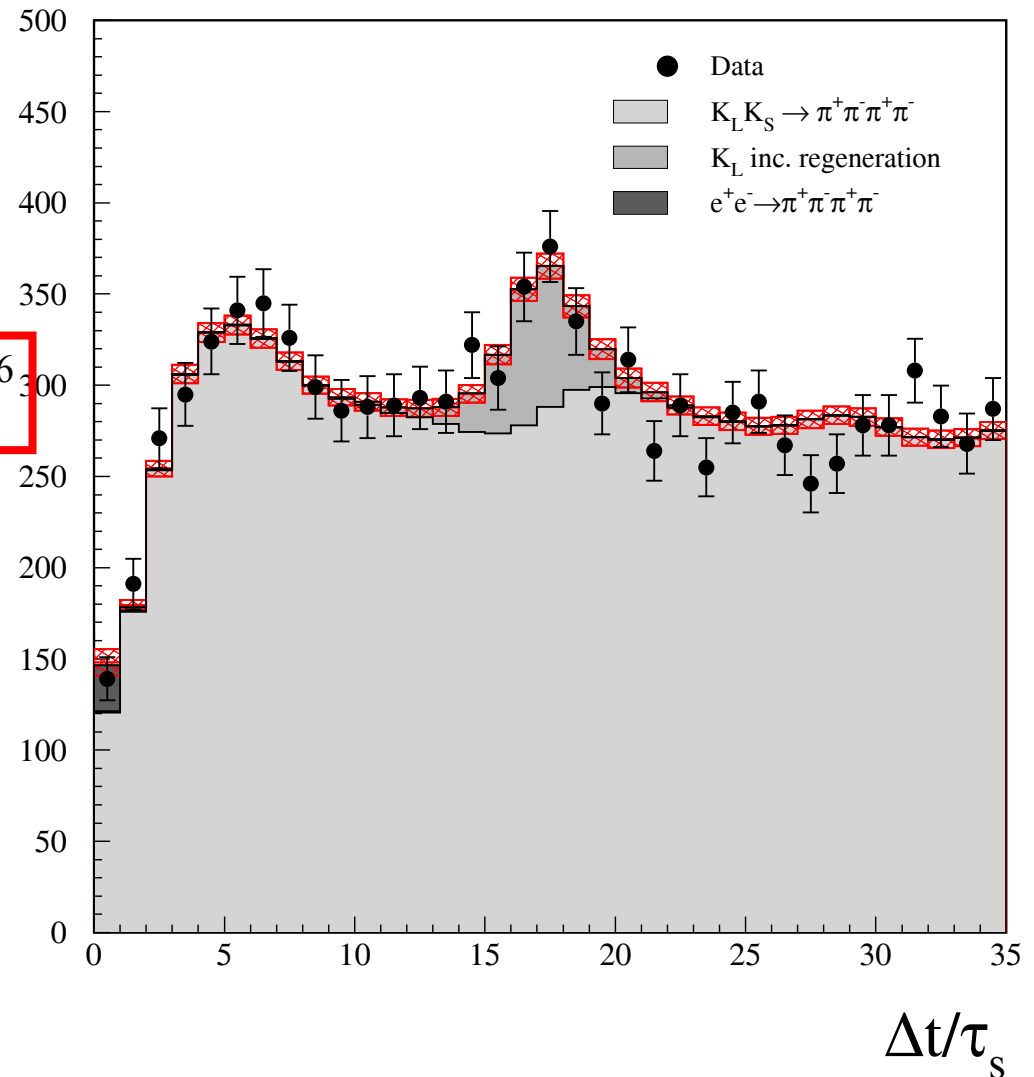
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# $\phi \rightarrow K_S K_L \rightarrow \pi^+ \pi^- \pi^+ \pi^-$ : test of quantum coherence

- Analysed data:  $L=1 \text{ fb}^{-1}$  (2005 data)
- Fit including  $\Delta t$  resolution and efficiency effects + regeneration
- $\Gamma_S, \Gamma_L, \Delta m$  fixed from PDG

**KLOE preliminary:**

$$\zeta_{0\bar{0}} = (0.3 \pm 1.2_{\text{STAT}}) \times 10^{-6}$$

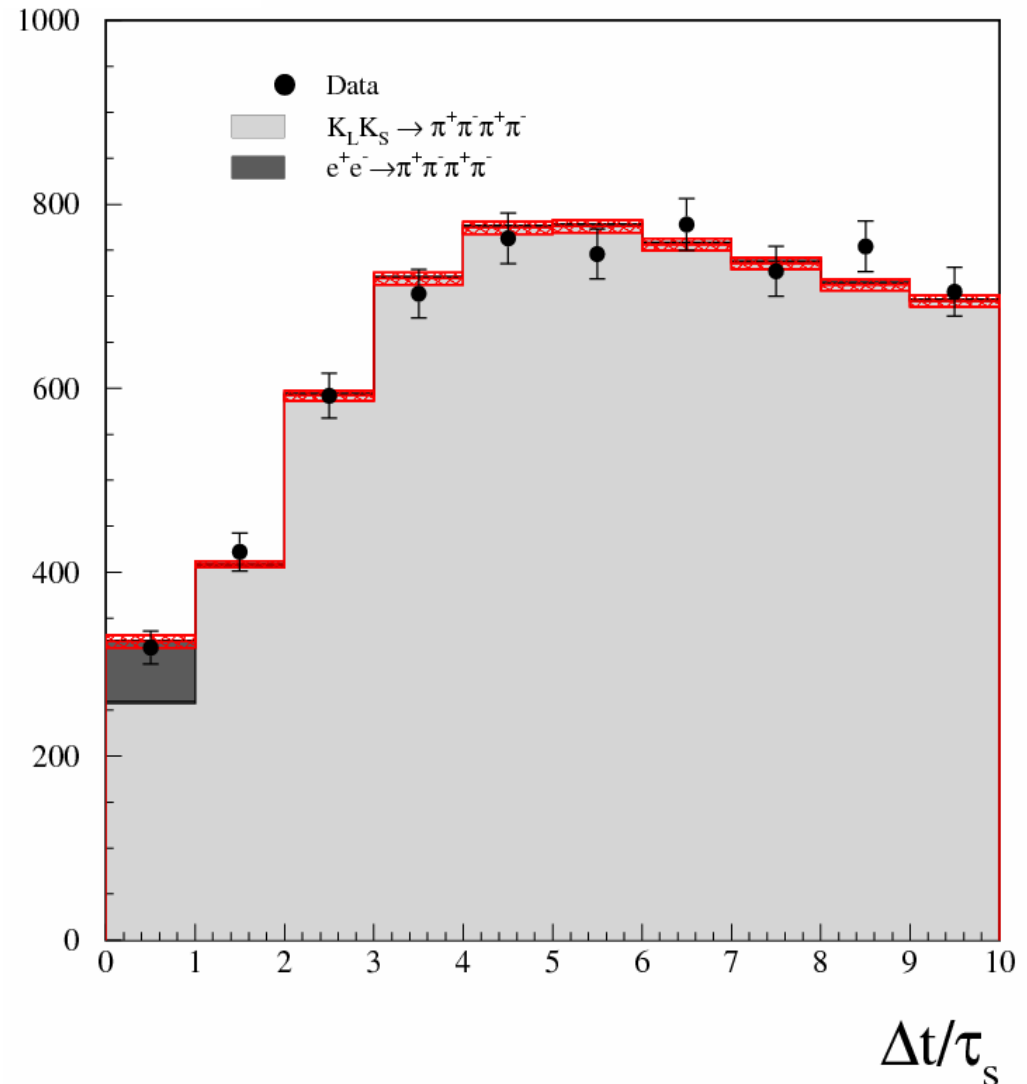
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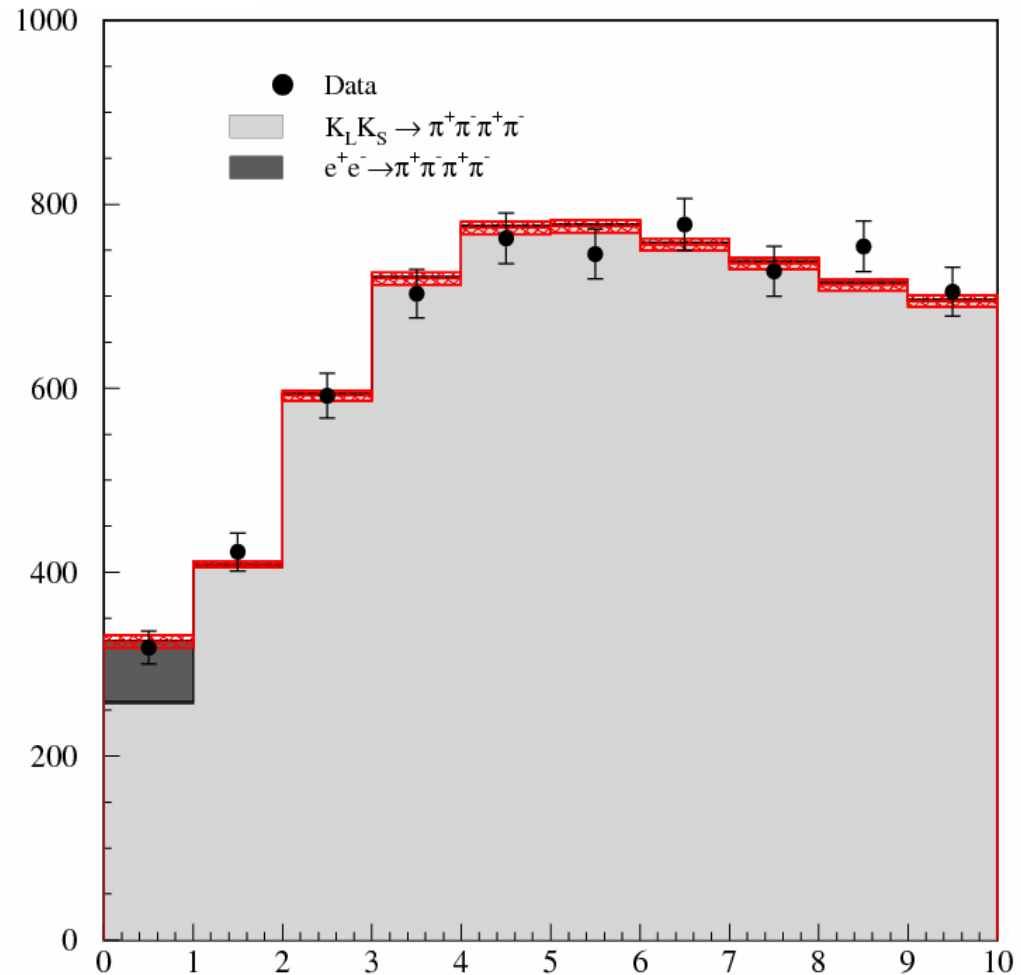
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Comparison with quantum optics test precisions

$\Delta t / \tau_S$



# Decoherence and CPT violation

Modified Liouville – von Neumann equation for the density matrix of the kaon system:

$$\dot{\rho}(t) = \underbrace{-iH\rho + i\rho H^\dagger}_{\text{QM}} + L(\rho)$$

← extra term inducing decoherence:  
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## Possible decoherence due quantum gravity effects:

**Black hole information loss paradox** => Possible decoherence near a black hole.

Hawking [1] suggested that at a microscopic level, in a quantum gravity picture, non-trivial space-time fluctuations (generically space-time foam) could give rise to decoherence effects, which would necessarily entail a violation of CPT [2].

J. Ellis et al.[3-6] => model of decoherence for neutral kaons => 3 new CPTV param.  $\alpha, \beta, \gamma$ :

$$L(\rho) = L(\rho; \alpha, \beta, \gamma)$$
$$\alpha, \gamma > 0, \quad \alpha\gamma > \beta^2$$

At most:  $\alpha, \beta, \gamma = O\left(\frac{M_K^2}{M_{\text{PLANCK}}}\right) \approx 2 \times 10^{-20} \text{ GeV}$

[1] Hawking, Comm.Math.Phys.87 (1982) 395; [2] Wald, PR D21 (1980) 2742; [3] Ellis et. al, NP B241 (1984) 381; PRD53 (1996)3846 [4] Huet, Peskin, NP B434 (1995) 3; [5] Benatti, Floreanini, NPB511 (1998) 550 [6] Bernabeu, Ellis, Mavromatos, Nanopoulos, Papavassiliou: Handbook on kaon interferometry [hep-ph/0607322]

# $\phi \rightarrow K_S K_L \rightarrow \pi^+ \pi^- \pi^+ \pi^-$ : decoherence & CPTV by QG

Study of time evolution of **single kaons**  
decaying in  $\pi^+ \pi^-$  and semileptonic final state

CPLEAR **PLB 364, 239 (1999)**

$$\alpha = (-0.5 \pm 2.8) \times 10^{-17} \text{ GeV}$$

$$\beta = (2.5 \pm 2.3) \times 10^{-19} \text{ GeV}$$

$$\gamma = (1.1 \pm 2.5) \times 10^{-21} \text{ GeV}$$

In the complete positivity hypothesis

$$\alpha = \gamma \quad , \quad \beta = 0$$

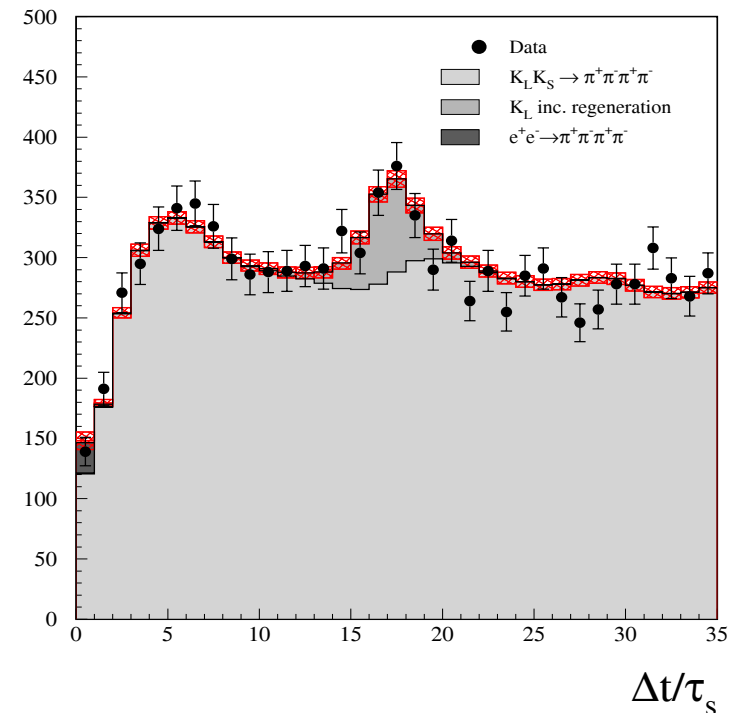
=> only one independent parameter:  $\gamma$

The fit with  $I(\pi^+ \pi^-, \pi^+ \pi^-; \Delta t, \gamma)$  gives:

**KLOE result**  $L=380 \text{ pb}^{-1}$  **PLB 642(2006) 315**

$$\gamma = \left( 1.1_{-2.4}^{+2.9} \text{STAT} \pm 0.4_{\text{SYST}} \right) \times 10^{-21} \text{ GeV}$$

Complete positivity guarantees the positivity of the eigenvalues of density matrices describing states of correlated kaons.



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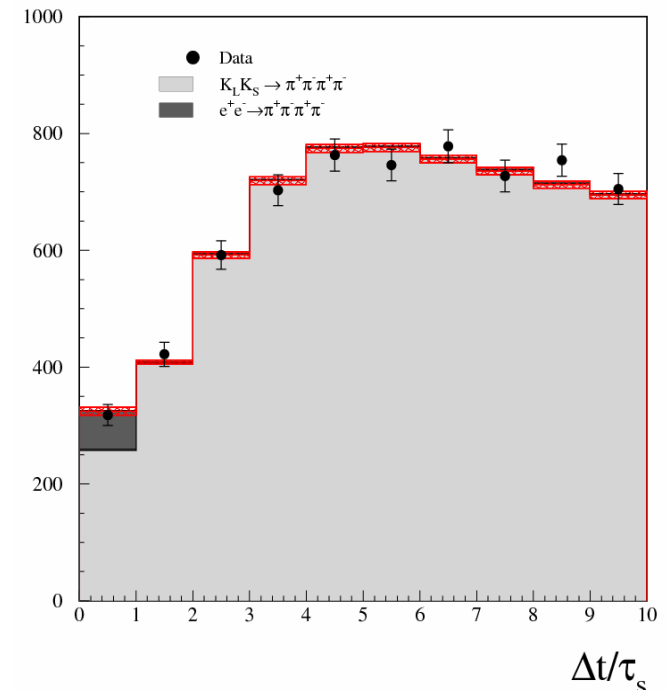
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The fit with  $I(\pi^+ \pi^-, \pi^+ \pi^-; \Delta t, \gamma)$  gives:

**KLOE preliminary**  $L=1 \text{ fb}^{-1}$

$$\gamma = \left( 0.8^{+1.5}_{-1.3 \text{ STAT}} \right) \times 10^{-21} \text{ GeV}$$

Complete positivity guarantees the positivity of the eigenvalues of density matrices describing states of correlated kaons.



# $\phi \rightarrow K_S K_L \rightarrow \pi^+ \pi^- \pi^+ \pi^- : \text{CPT violation in correlated K states}$

In presence of decoherence and CPT violation induced by quantum gravity (CPT operator “ill-defined”) the definition of the particle-antiparticle states could be modified. This in turn could induce a breakdown of the correlations imposed by Bose statistics (EPR correlations) to the kaon state [Bernabeu, et al. PRL 92 (2004) 131601, NPB744 (2006) 180]:

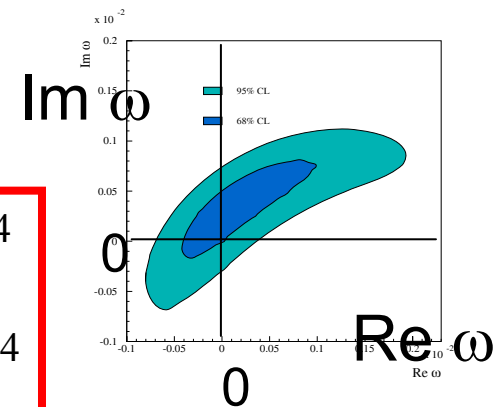
$$|i\rangle \propto (K^0 \bar{K}^0 - K^0 \bar{K}^0) + \omega (K^0 \bar{K}^0 + K^0 \bar{K}^0)$$

$|\omega|$  could be at most:  $|\omega|^2 = O\left(\frac{E^2/M_{PLANCK}}{\Delta\Gamma}\right) \approx 10^{-5} \Rightarrow |\omega| \sim 10^{-3}$

## KLOE result

Fit of  $I(\pi^+ \pi^-, \pi^+ \pi^-; \Delta t, \omega)$ :

**( $\omega$  measured for the first time)**



• Analysed data: 380 pb<sup>-1</sup>

$$\Re \omega = \left(1.1^{+8.7}_{-5.3 \text{ STAT}} \pm 0.9_{\text{SYST}}\right) \times 10^{-4}$$

$$\Im \omega = \left(3.4^{+4.8}_{-5.0 \text{ STAT}} \pm 0.6_{\text{SYST}}\right) \times 10^{-4}$$

$$|\omega| < 2.1 \times 10^{-3} \quad \text{at } 95\% \text{ C.L.}$$

**KLOE result :**

**PLB 642(2006) 315**



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## KLOE result

Fit of  $I(\pi^+ \pi^-, \pi^+ \pi^-; \Delta t, \omega)$ :

- Analysed data:  
1 fb<sup>-1</sup> (2005 data)

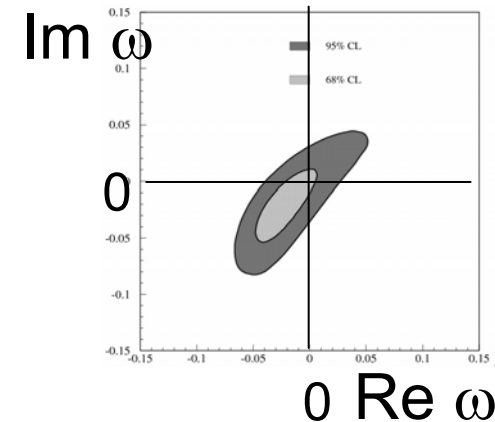
( $\omega$  measured for the first time)

$$\Re \omega = \left(-2.5^{+3.1}_{-2.3_{STAT}}\right) \times 10^{-4}$$

$$\Im \omega = \left(-2.2^{+3.4}_{-3.1_{STAT}}\right) \times 10^{-4}$$

**KLOE preliminary :**

$$|\omega| < 0.98 \times 10^{-3} \quad \text{at 95\% C.L.}$$



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### **3) Tests of Lorentz invariance and CPT symmetry in the neutral kaon system**

# CPT and Lorentz invariance violation (SME)

Kostelecky et al. developed a phenomenological effective model providing a framework for CPT and Lorentz violations, based on spontaneous breaking of CPT and Lorentz symmetry, which might happen in quantum gravity (e.g. in some models of string theory)

## Standard Model Extension (SME)

[Kostelecky PRD61 (1999) 016002, PRD 64 (2001) 076001]

CPT violation in SME manifests to lowest order only in  $\delta \Rightarrow$  **No CPT viol. in decays** and exhibits a kaon momentum dependence:

**$\delta$  cannot be a constant**

$$\delta = i \sin \phi_{SW} e^{i\phi_{SW}} \gamma_K \left( \Delta a_0 - \vec{\beta}_K \cdot \Delta \vec{a} \right) / \Delta m$$

where  $\Delta a_\mu$  are four parameters associated to SME lagrangian terms and related to CPT and Lorentz violation.

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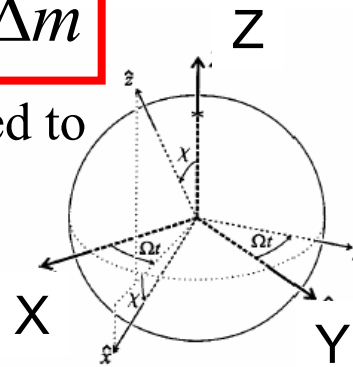
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$\delta$  depends on sidereal time  $t$  since laboratory frame rotates with Earth:

$$\bar{\delta}(|\vec{p}|, \theta, t) = \frac{i \sin \phi_{SW} e^{i\phi_{SW}}}{\Delta m} \gamma_K \left[ \Delta a_0 + \beta_K \Delta a_Z \cos \chi \cos \theta \right. \\ \left. + \beta_K \Delta a_Y \sin \chi \cos \theta \sin \Omega t + \beta_K \Delta a_X \sin \chi \cos \theta \cos \Omega t \right]$$

$\Omega$ : Earth's sidereal freq.  
 $\chi$ : angle bet. the z lab. axis and the Earth's rotat. axis  
 $\theta$ : kaon polar angle in the lab.

# Measurement of $\Delta a_\mu$ at KLOE

$\Delta a_0$  from  $K_{S,L}$  semileptonic asymmetries

$A_{S,L}$  (with symmetric polar angle  $\theta$  and sidereal time  $t$  integration)

$$A_S - A_L \cong \frac{4\Re(i \sin\phi_{SW} e^{i\phi_{SW}}) \gamma_K}{\Delta m} \Delta a_0$$

with  $L=400 \text{ pb}^{-1}$  (preliminary):

$$\Delta a_0 = (0.4 \pm 1.8) \times 10^{-17} \text{ GeV}$$

with  $L=2.5 \text{ fb}^{-1}$  :  $\sigma(\Delta a_0) \sim 7 \times 10^{-18} \text{ GeV}$  ( $\Delta a_0$  evaluated for the first time)

$\Delta a_{X,Y,Z}$  from  $\phi \rightarrow K_S K_L \rightarrow \pi^+ \pi^- \pi^+ \pi^-$   
(analysis vs polar angle  $\theta$  and sidereal time  $t$ )

Fit to:  $I[\pi^+ \pi^- (\cos\theta > 0), \pi^+ \pi^- (\cos\theta < 0); \Delta t]$

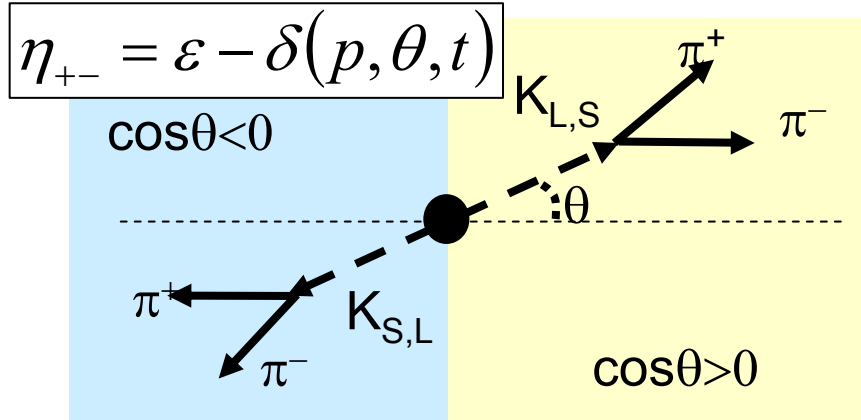
• at  $\Delta t \sim \tau_s$  sensitive to  $\text{Im}(\delta/\epsilon)$

With  $L=1 \text{ fb}^{-1}$  (preliminary):

$$\Delta a_X = (-6.3 \pm 6.0) \times 10^{-18} \text{ GeV}$$

$$\Delta a_Y = (2.8 \pm 5.9) \times 10^{-18} \text{ GeV}$$

$$\Delta a_Z = (2.4 \pm 9.7) \times 10^{-18} \text{ GeV}$$



KTeV :  $\Delta a_X, \Delta a_Y < 9.2 \times 10^{-22} \text{ GeV}$  @ 90% CL

BABAR  $\Delta a_{x,y}^B, (\Delta a_0^B - 0.30 \Delta a_Z^B) \sim O(10^{-13} \text{ GeV})$   
[PRL 100 (2008) 131802]

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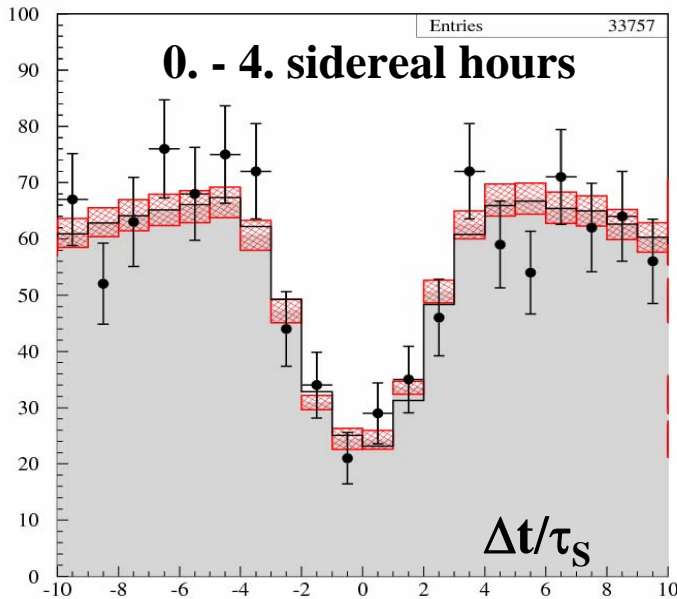
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## 4) Future plans

### Proposals to upgrade DAΦNE in luminosity (and energy):

Crabbed waist scheme at DAΦNE (proposal by P. Raimondi)

- increase L by a factor  $O(5)$
- requires minor modifications
- relatively low cost
- Experimental test at DAΦNE in progress

see talk of  
M. Moulson

### KLOE-2 Proposal:

#### Physics issues:

- Neutral kaon interferometry, CPT symmetry & QM tests
- Kaon physics, CKM, LFV, rare  $K_S$  decays
- $\eta, \eta'$  physics
- Light scalars,  $\gamma\gamma$  physics
- Hadron cross section at low energy, muon anomaly
- (baryon electromagnetic form factors,  $e^+e^- \rightarrow pp, nn, \Lambda\Lambda$ )

#### Detector upgrade issues:

- Inner tracker R&D
- $\gamma\gamma$  tagging system
- Calorimeter, increase of granularity
- FEE maintenance and upgrade
- Computing and networking update
- etc.. (Trigger, software, ...)



# Perspectives with KLOE-2 at upgraded DAΦNE

Mode	Test of	Param.	Present best published measurement	KLOE-2 L=50 fb <sup>-1</sup>
$K_S \rightarrow \pi e \nu$	CP, CPT	$A_S$	$(1.5 \pm 11) \times 10^{-3}$	$\pm 1 \times 10^{-3}$
$\pi^+ \pi^- \pi e \nu$	CP, CPT	$A_L$	$(3322 \pm 58 \pm 47) \times 10^{-6}$	$\pm 25 \times 10^{-6}$
$\pi^+ \pi^- \pi^0 \pi^0$	CP	$\text{Re}(\varepsilon'/\varepsilon)$	$(1.47 \pm 0.22) \times 10^{-3}$	$\pm 0.2 \times 10^{-3}$
$\pi^+ \pi^- \pi^0 \pi^0$	CP, CPT	$\text{Im}(\varepsilon'/\varepsilon)$	$(2.3 \pm 2.9) \times 10^{-3}$	$\pm 3 \times 10^{-3}$
$\pi e \nu \pi e \nu$	CPT	$\text{Re}(\delta) + \text{Re}(x_-)$	$\text{Re}(\delta) = (0.30 \pm 0.33) \times 10^{-3}$ $\text{Re}(x_-) = (-0.8 \pm 2.5) \times 10^{-3}$	$\pm 0.2 \times 10^{-3}$
$\pi e \nu \pi e \nu$	CPT	$\text{Im}(\delta) + \text{Im}(x_+)$	$\text{Im}(\delta) = (0.4 \pm 2.1) \times 10^{-5}$ $\text{Im}(x_+) = (0.8 \pm 0.7) \times 10^{-2}$	$\pm 3 \times 10^{-3}$
$\pi^+ \pi^- \pi^+ \pi^-$		$\Delta m$	$(5.288 \pm 0.043) \times 10^9 \text{ s}^{-1}$	$\pm 0.03 \times 10^9 \text{ s}^{-1}$

# Perspectives with KLOE-2 at upgraded DAΦNE

Mode	Test of	Param.	Present best published measurement	KLOE-2 L=50 fb <sup>-1</sup>
$\pi^+\pi^- \quad \pi^+\pi^-$	QM	$\zeta_{00}$	$(1.0 \pm 2.1) \times 10^{-6}$	$\pm 0.1 \times 10^{-6}$
$\pi^+\pi^- \quad \pi^+\pi^-$	QM	$\zeta_{SL}$	$(1.8 \pm 4.1) \times 10^{-2}$	$\pm 0.2 \times 10^{-2}$
$\pi^+\pi^- \quad \pi^+\pi^-$	CPT & QM	$\alpha$	$(-0.5 \pm 2.8) \times 10^{-17} \text{ GeV}$	$\pm 2 \times 10^{-17} \text{ GeV}$
$\pi^+\pi^- \quad \pi^+\pi^-$	CPT & QM	$\beta$	$(2.5 \pm 2.3) \times 10^{-19} \text{ GeV}$	$\pm 0.1 \times 10^{-19} \text{ GeV}$
$\pi^+\pi^- \quad \pi^+\pi^-$	CPT & QM	$\gamma$	$(1.1 \pm 2.5) \times 10^{-21} \text{ GeV}$	$\pm 0.2 \times 10^{-21} \text{ GeV}$ compl. pos. hyp. $\pm 0.1 \times 10^{-21} \text{ GeV}$
$\pi^+\pi^- \quad \pi^+\pi^-$	CPT & EPR corr.	Re( $\omega$ )	$(1.1 \pm 7.0) \times 10^{-4}$	$\pm 2 \times 10^{-5}$
$\pi^+\pi^- \quad \pi^+\pi^-$	CPT & EPR corr.	Im( $\omega$ )	$(3.4 \pm 4.9) \times 10^{-4}$	$\pm 2 \times 10^{-5}$
$K_{S,L} \rightarrow \pi e \nu$	CPT & Lorentz	$\Delta a_0$	$[(0.4 \pm 1.8) \times 10^{-17} \text{ GeV}]$	$\pm 2 \times 10^{-18} \text{ GeV}$
$\pi^+\pi^- \quad \pi^+\pi^-$	CPT & Lorentz	$\Delta a_Z$	$[(2.4 \pm 9.7) \times 10^{-18} \text{ GeV}]$	$\pm 7 \times 10^{-19} \text{ GeV}$
$\pi^+\pi^- \quad \pi e \nu$	CPT & Lorentz	$\Delta a_{X,Y}$	$[<10^{-21} \text{ GeV}]$	$O(10^{-19}) \text{ GeV}$

[....] = preliminary

# Conclusions

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- The neutral kaon system is an excellent laboratory for the study of CPT symmetry and the basic principles of Quantum Mechanics;
- Several parameters related to possible
  - CPT violation (within QM)
  - CPT violation and decoherence
  - CPT violation and Lorentz symmetry breakinghave been measured, in some cases with a precision reaching the interesting Planck's scale region;
- All results are consistent with no CPT violation
- The analysis of the full KLOE data sample ( $2.5 \text{ fb}^{-1}$ ) is in progress;
- KLOE and DAΦNE are going to be upgraded;
- Neutral kaon interferometry, CPT symmetry and QM tests are one of the main issues of the KLOE-2 physics program

More detailed information can be found in:

## Handbook on neutral kaon interferometry at a $\phi$ -factory

G. Amelino-Camelia, M. Arzano, F. Benatti,  
J. Bernabeu, R. Bertlmann, A. Bramon,  
A. Di Domenico, R. Floreanini, A. Go,  
B. Hiesmayr, G. Isidori, R. Lehnert, N. Mavromatos  
J. Ellis, G. Garbarino, A. Marcianò, D. Nanopoulos,  
J. Papavassiliou, S. Sarkar

(editor A. D. D.)

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Frascati Physics Series, Vol. 43, 2007

also available at:

<http://www.roma1.infn.it/people/didomenico/roadmap/handbook.html>



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Laboratori Nazionali di Frascati

FRASCATI PHYSICS SERIES



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INTERFEROMETRY AT A  $\Phi$ -FACTORY

Editor  
A. Di Domenico

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PHYSICS SERIES

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HANDBOOK ON NEUTRAL KAON  
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43  
2007

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**Spare**

**A. Di Domenico**

**Neutral kaon interferometry at a phi-factory**

**J. Bernabeu, J. Ellis, N. Mavromatos, D. Nanopoulos, J. Papavassiliou**

**CPT and quantum mechanics tests with kaons**

**S. Sarkar**

**Methods and models for the study of decoherence**

**F. Benatti, R. Floreanini**

**Open quantum dynamics: complete positivity and correlated kaons**

**R. Lehnert**

**CPT and Lorentz symmetry breaking: a review**

**G. Amelino-Camelia, M. Arzano, A. Marciano'**

**On the quantum gravity phenomenology of multiparticle states**

**G. Isidori**

**Testing CPT in the neutral kaon system by means of the Bell-Steinberger relation**

**R. Bertlmann, B. Hiesmayr**

**Strangeness measurements of kaon pairs, CP violation and Bell inequalities**

**A. Bramon, R. Escribano, G. Garbarino**

**A review of Bell inequality tests with neutral kaons**

**A. Bramon, G. Garbarino, B. Hiesmayr**

**Kaonic quantum erasers at a phi-factory: "erasing the present, changing the past"**

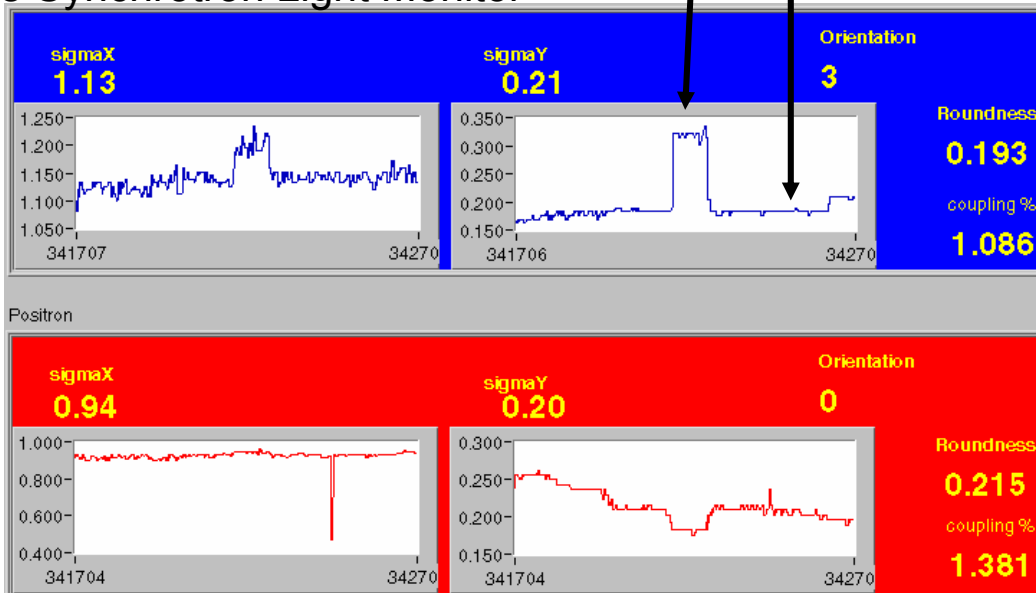
**A. Go**

**Kaon interferometry at CPLEAR**

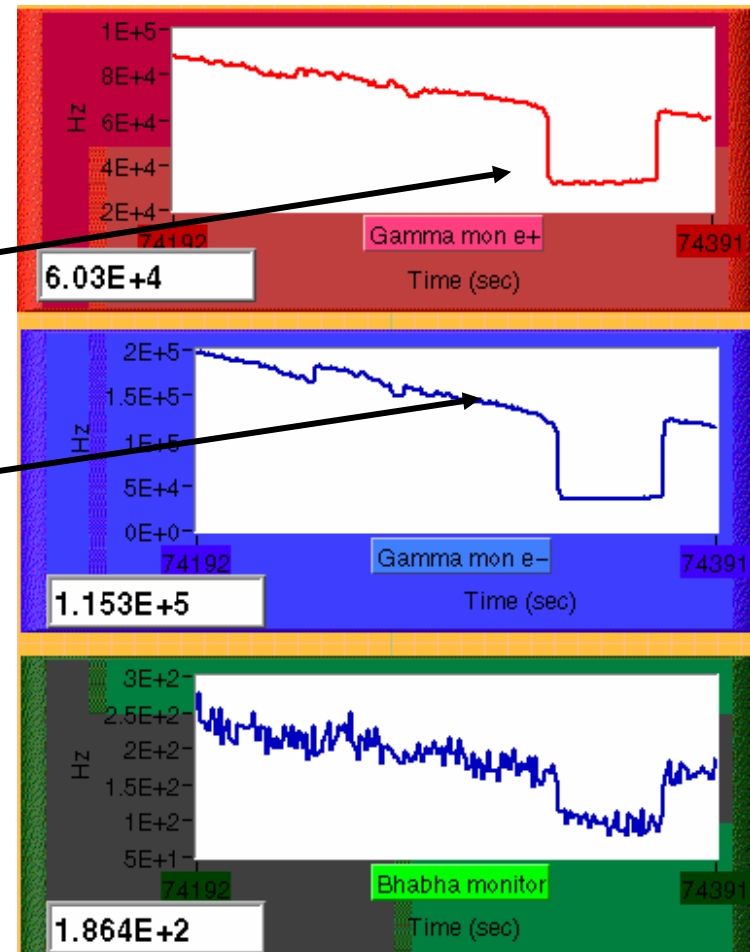
# EFFECTS OF CRAB SEXTUPOLES ON LUMINOSITY

A huge work on machine optimization has been done and is still in progress in term of feedbacks systems tuning, background minimization and tuning of the machine luminosity...

Transverse beam dimensions at the Synchrotron Light Monitor



## LUMINOMETERS

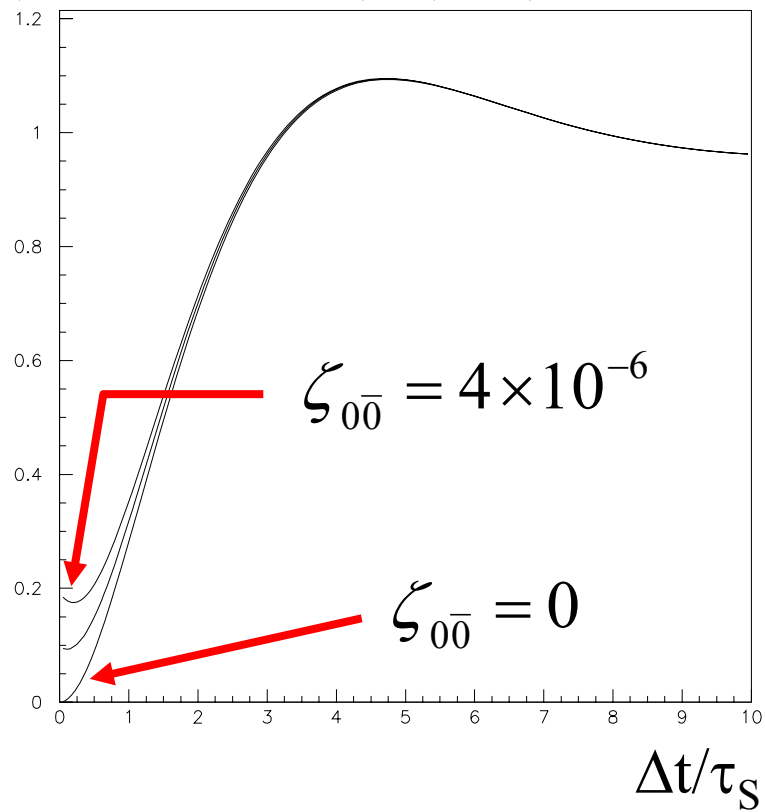


*P. Raimondi May 6, 2008*

# Example of interferometry at KLOE-2: $\phi \rightarrow K_S K_L \rightarrow \pi^+ \pi^- \pi^+ \pi^-$

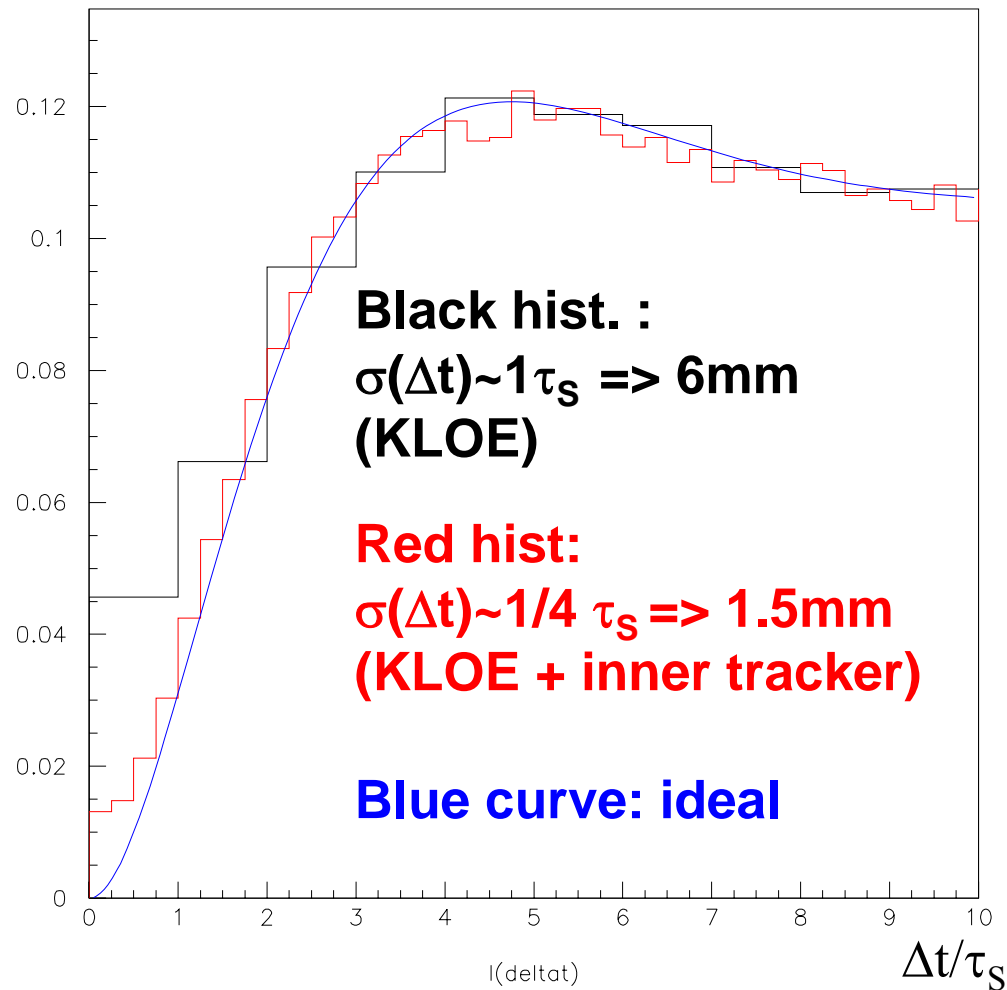
Possible signal of decoherence concentrated at very small  $\Delta t$

$I(\pi^+ \pi^-, \pi^+ \pi^-; \Delta t)$  (a.u.)



Theoretical distribution

$I(\pi^+ \pi^-, \pi^+ \pi^-; \Delta t)$  (a.u.)



Reconstructed distribution (MC)

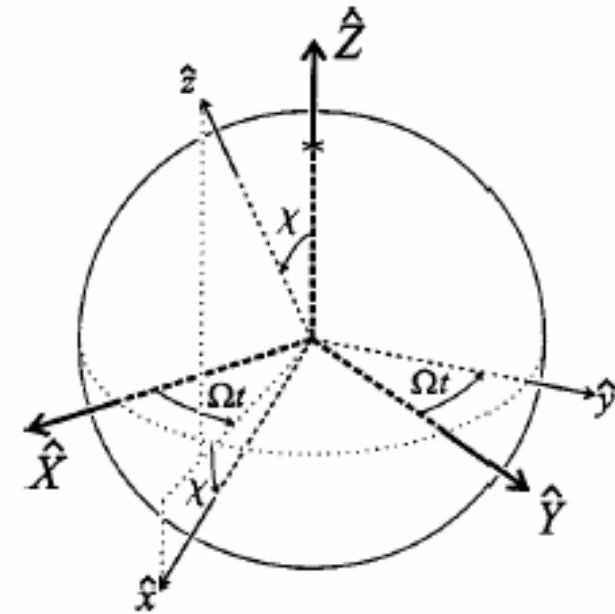


# CPT and Lorentz invariance violation (SME)

For a fixed target experiment (fixed momentum direction)  $\delta$  depends on sidereal time  $t$  since laboratory frame rotates with Earth.

For a  $\phi$ -factory there is an additional dependence on the polar and azimuthal angle  $\theta, \phi$  of the kaon momentum in the laboratory frame:

$$\begin{aligned} \bar{\delta}(|\vec{p}|, \theta, t) &= \frac{1}{2\pi} \int_0^{2\pi} \delta(\vec{p}, t) d\phi \\ &= \frac{i \sin \phi_{SW} e^{i\phi_{SW}}}{\Delta m} \gamma_K \left[ \Delta a_0 + \beta_K \Delta a_Z \cos \chi \cos \theta \right. \\ &\quad \left. + \beta_K \Delta a_Y \sin \chi \cos \theta \sin \Omega t \right. \\ &\quad \left. + \beta_K \Delta a_X \sin \chi \cos \theta \cos \Omega t \right] \end{aligned}$$



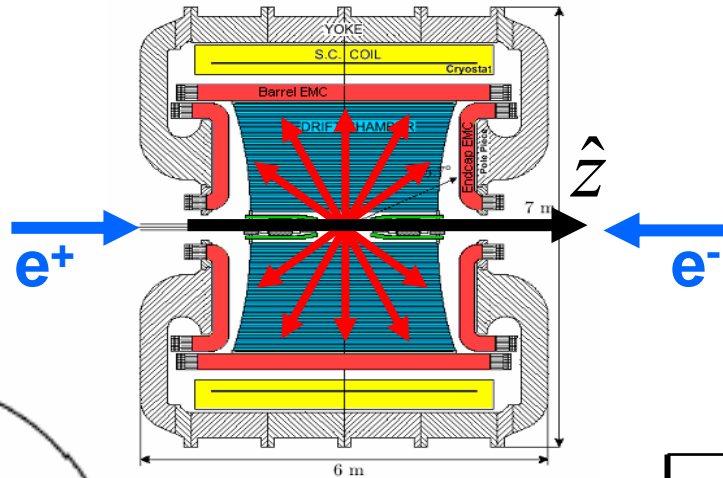
(in general z axis is non-normal to Earth's surface)

$\Omega$ : Earth's sidereal frequency  
 $\chi$ : angle between the z lab. axis and the Earth's rotation axis

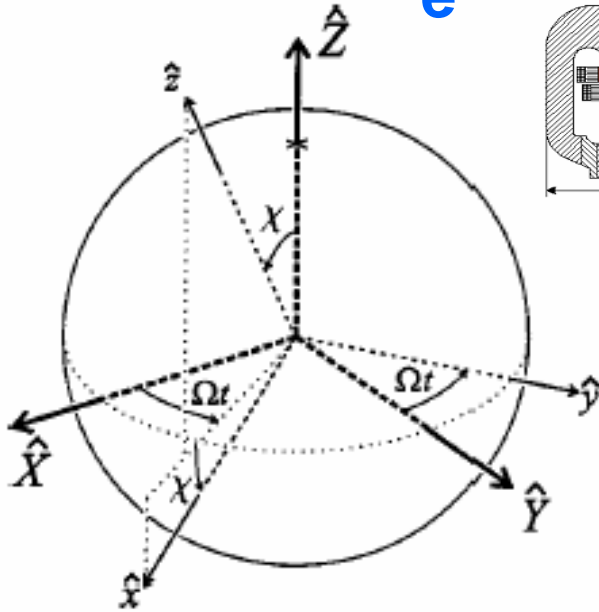
# CPT and Lorentz invariance violation (SME)

At DAΦNE K mesons are produced with angular distribution  $dN/d\Omega \propto \sin^2\theta$

KLOE is a kind of telescope, able to explore with a kaon beam almost any direction in space



KLOE latitude	$\sim 41.8^\circ$
KLOE longitude	$\sim 12.7^\circ$
$e^+$ beam axis	$\sim S57.8^\circ W$
$\gamma_K \beta_K$	$\sim 0.22$



(in general z axis is non-normal to Earth's surface)

term	coefficient	value
$\Delta a_0$	$\gamma_K$	1.02
$\Delta a_z$	$\gamma_K \beta_K \cos \chi$	-0.09
$\Delta a_x$	$\gamma_K \beta_K \sin \chi$	0.20
$\Delta a_y$	$\gamma_K \beta_K \sin \chi$	0.20

# $\phi \rightarrow K_S K_L \rightarrow \pi^+ \pi^- \pi^+ \pi^-$ : decoherence & CPTV by QG

The fit with  $I(\pi^+ \pi^-, \pi^+ \pi^-; \Delta t, \alpha, \beta, \gamma)$  gives:

**KLOE preliminary**

$$\alpha = \left( -10^{+41}_{-31 \text{ STAT}} \pm 9_{\text{SYST}} \right) \times 10^{-17} \text{ GeV}$$

$$\beta = \left( 3.7^{+6.9}_{-9.2 \text{ STAT}} \pm 1.8_{\text{SYST}} \right) \times 10^{-19} \text{ GeV}$$

$$\gamma = \left( -0.4^{+5.8}_{-5.1 \text{ STAT}} \pm 1.2_{\text{SYST}} \right) \times 10^{-21} \text{ GeV}$$

In the complete positivity hypothesis

$$\alpha = \gamma, \quad \beta = 0$$

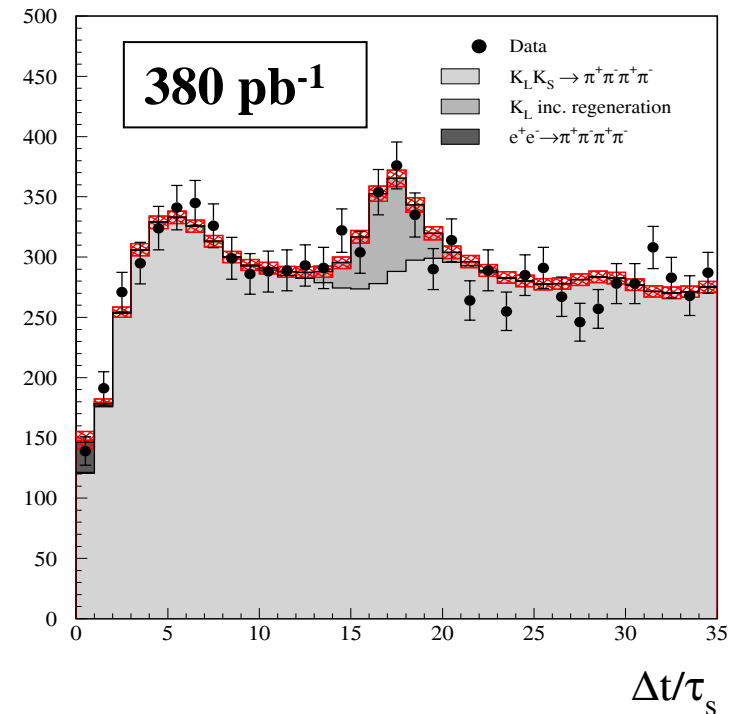
=> only one independent parameter:  $\gamma$

**KLOE result**

**PLB 642(2006) 315**

$$\gamma = \left( 1.1^{+2.9}_{-2.4 \text{ STAT}} \pm 0.4_{\text{SYST}} \right) \times 10^{-21} \text{ GeV}$$

$$\gamma < 6.4 \times 10^{-21} \text{ GeV} \quad \text{at 95\% C.L.}$$



Complete positivity guarantees the positivity of the eigenvalues of density matrices describing states of correlated kaons.

→  $\pm 1.1_{\text{STAT}} \times 10^{-21} \text{ GeV}$   
with  $L=2.5 \text{ fb}^{-1}$ :

# CPT violation in the neutral kaon system: “standard” picture

## CPT violation in the mixing

$$|K_{S,L}\rangle = \frac{1}{\sqrt{2(1+|\varepsilon_{S,L}|)}} \left[ (1 + \varepsilon_{S,L}) |K^0\rangle + (1 - \varepsilon_{S,L}) |\bar{K}^0\rangle \right]$$

$$\varepsilon_{S,L} = \varepsilon \pm \delta$$

$$\delta = \frac{1}{2} \frac{(m_{\bar{K}^0} - m_{K^0}) - (i/2)(\Gamma_{\bar{K}^0} - \Gamma_{K^0})}{\Delta m + i\Delta\Gamma/2}$$

$$\Delta m = m_L - m_S$$

$$\Delta\Gamma = \Gamma_S - \Gamma_L$$

$$\phi_{SW} = \arctan(2\Delta m/\Delta\Gamma)$$

## CPT violation in semileptonic decays

$$\langle \pi^- \ell^+ \nu | T | K^0 \rangle = a + b \quad \langle \pi^+ \ell^- \bar{\nu} | T | K^0 \rangle = c + d$$

$$\langle \pi^+ \ell^- \bar{\nu} | T | \bar{K}^0 \rangle = a^* - b^* \quad \langle \pi^- \ell^+ \nu | T | \bar{K}^0 \rangle = c^* - d^*$$

CPT viol.	CPT & $\Delta S = \Delta Q$ viol.	$\Delta S = \Delta Q$ Viol.
$y = -\frac{b}{a}$	$x_- = -\frac{d^*}{a}$	$x_+ = \frac{c^*}{a}$

Semileptonic charge asymmetry:

$$A_{S,L} = \frac{\Gamma(K_{S,L} \rightarrow \pi^- e^+ \nu) - \Gamma(K_{S,L} \rightarrow \pi^+ e^- \bar{\nu})}{\Gamma(K_{S,L} \rightarrow \pi^- e^+ \nu) + \Gamma(K_{S,L} \rightarrow \pi^+ e^- \bar{\nu})}$$

$$= 2\Re\varepsilon \pm 2\Re\delta - 2\Re y \pm 2\Re x_{\pm}$$

Standard Model prediction of  $\Delta S = \Delta Q$  rule violation is  $x \sim O(10^{-7})$

$$A_S - A_L = 4(\Re\delta + \Re x_-)$$

# CPT violation in the neutral kaon system: “standard” picture

## CPT violation in $\pi\pi$ decays

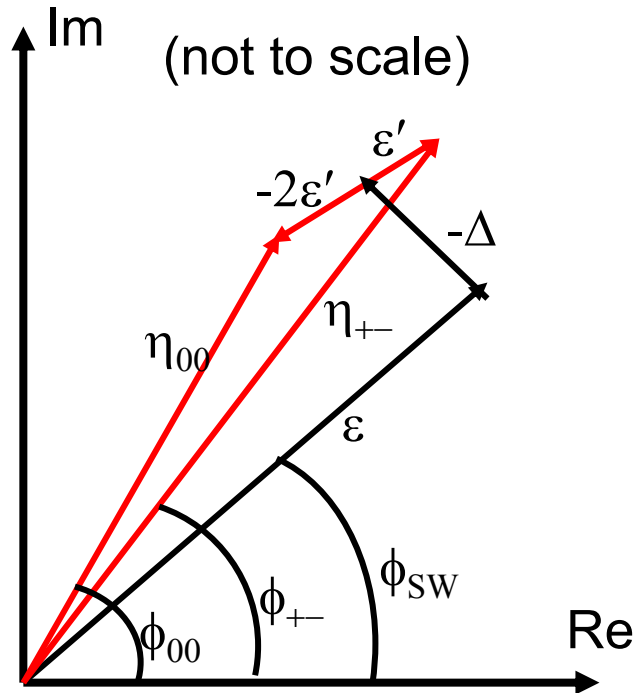
$$\langle \pi\pi; I | T | K^0 \rangle = (A_I + B_I) e^{i\delta_I}$$

$$\langle \pi\pi; I | T | \bar{K}^0 \rangle = (A_I^* - B_I^*) e^{i\delta_I}$$

$A_I(B_I)$  CPT conserving (violating)

$K \rightarrow \pi\pi$  amplitudes for  $I=0,2$

( $\delta_I$  strong phase shift for  $I=0,2$ )



$$\eta_{+-} = |\eta_{+-}| e^{i\phi_{+-}} = \frac{\langle \pi^+ \pi^- | T | K_L \rangle}{\langle \pi^+ \pi^- | T | K_S \rangle} = \varepsilon - \Delta + \varepsilon'$$

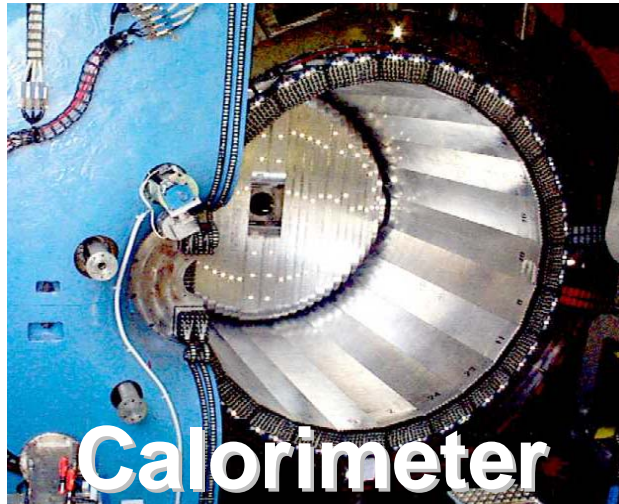
$$\eta_{00} = |\eta_{00}| e^{i\phi_{00}} = \frac{\langle \pi^0 \pi^0 | T | K_L \rangle}{\langle \pi^0 \pi^0 | T | K_S \rangle} = \varepsilon - \Delta - 2\varepsilon'$$

$$\Delta = \delta - \frac{\Re B_0}{\Re A_0} \quad \phi_{SW} = \arctan(2\Delta m / \Delta\Gamma)$$

$$\phi_{00} - \phi_{+-} \approx \frac{3}{\sqrt{2}} \frac{1}{|\eta_{+-}|} \frac{\Re A_2}{\Re A_0} \left( \frac{\Re B_2}{\Re A_2} - \frac{\Re B_0}{\Re A_0} \right) \approx -3\Im \left( \frac{\varepsilon'}{\varepsilon} \right)$$

$$\phi_{+-} - \phi_{SW} \approx \frac{-1}{\sqrt{2} |\eta_{+-}|} \left[ \frac{m_{11} - m_{22}}{2\Delta m} + \frac{\Re B_0}{\Re A_0} \right]$$

# The KLOE detector



Lead/scintillating fiber  
4880 PMTs  
98% coverage of solid angle

$$\sigma_E/E \cong 5.7\% / \sqrt{E(\text{GeV})}$$

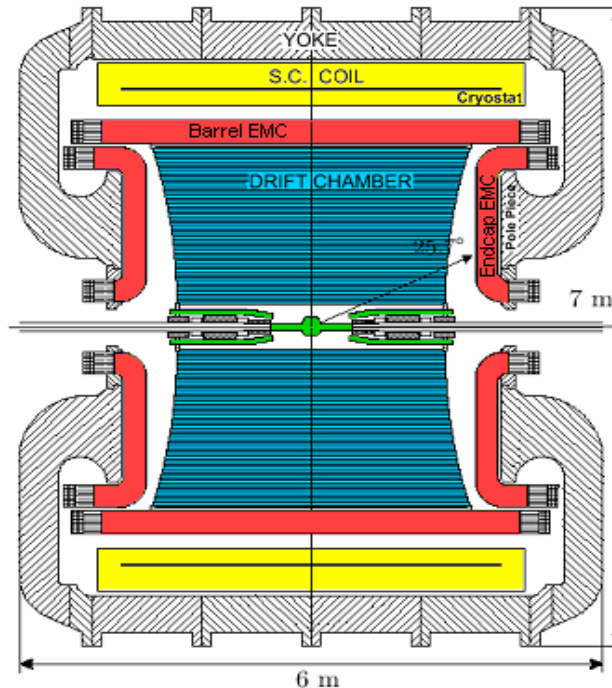
$$\sigma_t \cong 54 \text{ ps} / \sqrt{E(\text{GeV})} \oplus 50 \text{ ps}$$

(relative time between clusters)

$$\sigma_{\gamma\gamma} \sim 2 \text{ cm} (\pi^0 \text{ from } K_L \rightarrow \pi^+\pi^-\pi^0)$$

## Superconducting coil

$$B = 0.52 \text{ T}$$



4 m diameter  $\times$  3.3 m length  
90% helium, 10% isobutane  
12582/52140 sense/total wires  
All-stereo geometry

$$\sigma_p/p \cong 0.4\% \text{ (tracks with } \theta > 45^\circ)$$

$$\sigma_x^{\text{hit}} \cong 150 \mu\text{m (xy), 2 mm (z)}$$

$$\sigma_x^{\text{vertex}} \sim 1 \text{ mm}$$

# CPT: introduction

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The three discrete symmetries of QM, C (charge conjugation), P (parity), and T (time reversal) are known to be violated in nature both singly and in pairs. Only CPT appears to be an exact symmetry of nature.

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CPT theorem (Luders, Jost, Pauli, Bell 1955 -1957):

Exact CPT invariance holds for any quantum field theory which assumes:

(1) Lorentz invariance (2) Locality (3) Unitarity (i.e. conservation of probability).



# CPT: introduction

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Exact CPT invariance holds for any quantum field theory which assumes:

(1) Lorentz invariance (2) Locality (3) Unitarity (i.e. conservation of probability).

Testing the validity of the CPT symmetry probes the most fundamental assumptions of our present understanding of particles and their interactions.

Extension of CPT theorem to a theory of quantum gravity far from obvious (e.g. CPT violation appears in some models with space-time foam backgrounds).

# Measurement of $\Delta a_{X,Y,Z}$ at KLOE

$\Delta a_{X,Y,Z}$  from  $\phi \rightarrow K_S K_L \rightarrow \pi^+ \pi^- \pi^+ \pi^-$   
(analysis vs polar angle  $\theta$  and sidereal time  $t$ )

$$\eta_{+-} = \varepsilon - \delta(p, \theta, t)$$

$I[\pi^+ \pi^- (\cos \theta > 0), \pi^+ \pi^- (\cos \theta < 0); \Delta t]$

- at  $\Delta t \gg \tau_s$  sensitive to  $\text{Re}(\delta/\varepsilon) = 0$
- at  $\Delta t \sim \tau_s$  sensitive to  $\text{Im}(\delta/\varepsilon)$

With  $L = 1 \text{ fb}^{-1}$  (**preliminary**):  $\chi^2/\text{dof} = 131/117$

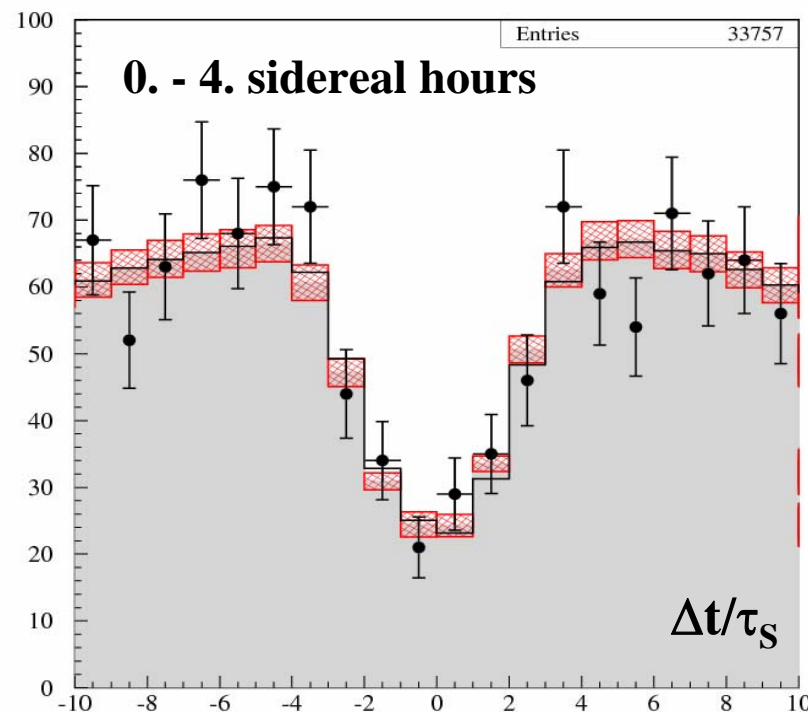
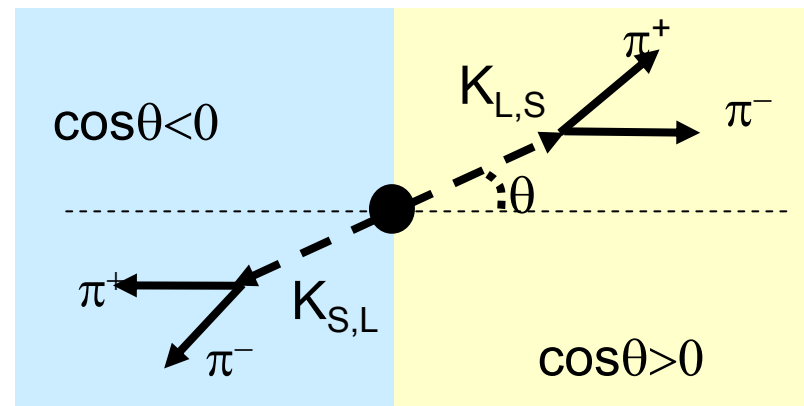
$$\Delta a_X = (-6.3 \pm 6.0) \times 10^{-18} \text{ GeV}$$

$$\Delta a_Y = (2.8 \pm 5.9) \times 10^{-18} \text{ GeV}$$

$$\Delta a_Z = (2.4 \pm 9.7) \times 10^{-18} \text{ GeV}$$

KTeV :  $\Delta a_X, \Delta a_Y < 9.2 \times 10^{-22} \text{ GeV}$  @ 90% CL

BABAR  $\Delta a_{X,Y}^B, (\Delta a_0^B - 0.30 \Delta a_Z^B) \sim O(10^{-13} \text{ GeV})$   
[PRL 100 (2008) 131802]



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$$\eta_{\pi\pi} = |\eta_{\pi\pi}| e^{i\phi_{\pi\pi}} = \frac{\langle \pi\pi | T | K_L \rangle}{\langle \pi\pi | T | K_S \rangle}$$

$$\phi_{00} - \phi_{+-} \approx \frac{3}{\sqrt{2}} \frac{1}{|\eta_{+-}|} \frac{\Re A_2}{\Re A_0} \left( \frac{\Re B_2}{\Re A_2} - \frac{\Re B_0}{\Re A_0} \right) \approx -3 \Im \left( \frac{\varepsilon'}{\varepsilon} \right)$$

$$\phi_{+-} - \phi_{SW} \approx \frac{-1}{\sqrt{2} |\eta_{+-}|} \left[ \frac{m_{11} - m_{22}}{2\Delta m} + \frac{\Re B_0}{\Re A_0} \right]$$

# Some results of CPT tests

CLEAR

$$\Re\delta = (0.30 \pm 0.33 \pm 0.06) \times 10^{-3}$$

PLB444 (1998) 52

KTeV

$$\begin{aligned} \phi_{+-} - \phi_{SW} &= 0.61^\circ \pm 0.62^\circ \pm 1.01^\circ \\ \phi_{00} - \phi_{+-} &= 0.39^\circ \pm 0.22^\circ \pm 0.45^\circ \end{aligned}$$

PRL88, 181601 (2002)

$$A_{S,L} = \frac{\Gamma(K_{S,L} \rightarrow \pi^- e^+ \nu) - \Gamma(K_{S,L} \rightarrow \pi^+ e^- \bar{\nu})}{\Gamma(K_{S,L} \rightarrow \pi^- e^+ \nu) + \Gamma(K_{S,L} \rightarrow \pi^+ e^- \bar{\nu})} = 2\Re\epsilon \pm 2\Re\delta - 2\Re\gamma \pm 2\Re x_-$$

$$A_L = (3322 \pm 58 \pm 47) \times 10^{-6}$$

PRD67, 012005 (2003)

KLOE

$$A_S = (1.5 \pm 9.6 \pm 2.9) \times 10^{-3}$$

PLB 636(2006) 173

input from other experiments

$$A_S - A_L = 4(\Re\delta + \Re x_-)$$

$$\Re x_- = (-0.8 \pm 2.4 \pm 0.7) \times 10^{-3}$$

CPT &  $\Delta S = \Delta Q$  viol.

$$A_S + A_L = 4(\Re\epsilon - \Re\gamma)$$

$$\Re\gamma = (0.4 \pm 2.4 \pm 0.7) \times 10^{-3}$$

CPT viol.

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CLEAR

$$\Re\delta = (0.30 \pm 0.33 \pm 0.06) \times 10^{-3}$$

PLB444 (1998) 52

KTeV

$$\begin{aligned} \phi(\varepsilon) - \phi_{SW} &= [0.40 \pm 0.56]^\circ \\ \phi_{00} - \phi_{+-} &= [0.30 \pm 0.35]^\circ \end{aligned}$$

UPDATE  
2008

$$A_{S,L} = \frac{\Gamma(K_{S,L} \rightarrow \pi^- e^+ \nu) - \Gamma(K_{S,L} \rightarrow \pi^+ e^- \bar{\nu})}{\Gamma(K_{S,L} \rightarrow \pi^- e^+ \nu) + \Gamma(K_{S,L} \rightarrow \pi^+ e^- \bar{\nu})} = 2\Re\varepsilon \pm 2\Re\delta - 2\Re y \pm 2\Re x_-$$

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CPT &  $\Delta S = \Delta Q$  viol.

$$A_S + A_L = 4(\Re\varepsilon - \Re y)$$

$$\Re y = (0.4 \pm 2.4 \pm 0.7) \times 10^{-3}$$

CPT viol.

# CPT test: the Bell-Steinberger relation

Unitarity constraint:

Experimental inputs:

$$\left( \frac{\Re \varepsilon}{1 + |\varepsilon|^2} - i \Im \delta \right) = \frac{1}{\Gamma_S - \Gamma_L} \sum_f \langle f | T | K_S \rangle^* \langle f | T | K_L \rangle = \frac{\left( \frac{\Gamma_S + \Gamma_L}{\Gamma_S - \Gamma_L} + i \tan \phi_{SW} \right)}{\Gamma_S - \Gamma_L}$$

$K_S$   $K_L$  observables

Main improvements done with KLOE measurements of  $K_S$  semileptonic and  $3\pi^0$  decays

	Value	Source
$\tau_{K_S}$	$0.08958 \pm 0.00005$ ns	PDG [14]
$\tau_{K_L}$	$50.84 \pm 0.23$ ns	KLOE average
$m_L - m_S$	$(5.290 \pm 0.016) \times 10^9$ s <sup>-1</sup>	PDG [14]
$\text{BR}(K_S \rightarrow \pi^+ \pi^-)$	$0.69186 \pm 0.00051$	KLOE average
$\text{BR}(K_S \rightarrow \pi^0 \pi^0)$	$0.30687 \pm 0.00051$	KLOE average
$\text{BR}(K_S \rightarrow \pi \ell \nu)$	$(11.77 \pm 0.15) \times 10^{-4}$	KLOE [6]
$\text{BR}(K_L \rightarrow \pi^+ \pi^-)$	$(1.933 \pm 0.021) \times 10^{-3}$	KLOE average
$\text{BR}(K_L \rightarrow \pi^0 \pi^0)$	$(0.848 \pm 0.010) \times 10^{-3}$	KLOE average
$\phi_{+-}$	$(43.4 \pm 0.7)^\circ$	PDG [14]
$\phi_{00}$	$(43.7 \pm 0.8)^\circ$	PDG [14]
$R_{S,\gamma} (E_\gamma > 20\text{MeV})$	$(0.710 \pm 0.016) \times 10^{-2}$	E731 [18]
$R_{S,\gamma}^{\text{th-IB}} (E_\gamma > 20\text{MeV})$	$(0.700 \pm 0.001) \times 10^{-2}$	KLOE MC [19]
$ \eta_{+-\gamma} $	$(2.359 \pm 0.074) \times 10^{-3}$	E773 [17]
$\phi_{+-\gamma}$	$(43.8 \pm 4.0)^\circ$	E773 [17]
$\text{BR}(K_L \rightarrow \pi^+ \pi^- \pi^0)$	$0.1262 \pm 0.0011$	KLOE average
$\eta_{+-0}$	$((-2 \pm 7) + i(-2 \pm 9)) \times 10^{-3}$	CPLEAR [10]
$\text{BR}(K_L \rightarrow 3\pi^0)$	$0.1996 \pm 0.0021$	KLOE average
$\text{BR}(K_S \rightarrow 3\pi^0)$	$< 1.5 \times 10^{-7}$ at 95% CL	KLOE [5]
$\phi_{000}$	uniform from 0 to $2\pi$	
$\text{BR}(K_L \rightarrow \pi \ell \nu)$	$0.6709 \pm 0.0017$	KLOE average
$A_L + A_S$	$(0.5 \pm 1.0) \times 10^{-2}$	$K_{\ell 3}$ average
$\text{Im}(x_+)$	$(0.8 \pm 0.7) \times 10^{-2}$	$K_{\ell 3}$ average



# Perspectives with KLOE-2 at upgraded DAΦNE

Param.	Present best published measurement	KLOE-2 L=50 fb <sup>-1</sup>
A <sub>S</sub>	$(1.5 \pm 11) \times 10^{-3}$	$\pm 1 \times 10^{-3}$
A <sub>L</sub>	$(3322 \pm 58 \pm 47) \times 10^{-6}$	$\pm 25 \times 10^{-6}$
Re(ε'/ε)	$(1.47 \pm 0.22) \times 10^{-3}$	$\pm 0.2 \times 10^{-3}$
Im(ε'/ε)	$(2.3 \pm 2.9) \times 10^{-3}$	$\pm 3 \times 10^{-3}$
Re(δ) +Re(x <sub>-</sub> )	Re(δ) = $(0.30 \pm 0.33) \times 10^{-3}$ Re(x <sub>-</sub> ) = $(-0.8 \pm 2.5) \times 10^{-3}$	$\pm 0.2 \times 10^{-3}$
Im(δ) +Im(x <sub>+</sub> )	Im(δ) = $(0.4 \pm 2.1) \times 10^{-5}$ Im(x <sub>+</sub> ) = $(0.8 \pm 0.7) \times 10^{-2}$	$\pm 3 \times 10^{-3}$
Δm	$(5.288 \pm 0.043) \times 10^9 \text{ s}^{-1}$	$\pm 0.03 \times 10^9 \text{ s}^{-1}$

Param.	Present best published measurement	KLOE-2 L=50 fb <sup>-1</sup>
ζ <sub>00</sub>	$(1.0 \pm 2.1) \times 10^{-6}$	$\pm 0.1 \times 10^{-6}$
ζ <sub>SL</sub>	$(1.8 \pm 4.1) \times 10^{-2}$	$\pm 0.2 \times 10^{-2}$
α	$(-0.5 \pm 2.8) \times 10^{-17} \text{ GeV}$	$\pm 2 \times 10^{-17} \text{ GeV}$
β	$(2.5 \pm 2.3) \times 10^{-19} \text{ GeV}$	$\pm 0.1 \times 10^{-19} \text{ GeV}$
γ	$(1.1 \pm 2.5) \times 10^{-21} \text{ GeV}$	$\pm 0.2 \times 10^{-21} \text{ GeV}$ compl. pos. hyp. $\pm 0.1 \times 10^{-21} \text{ GeV}$
Re(ω)	$(1.1 \pm 7.0) \times 10^{-4}$	$\pm 2 \times 10^{-5}$
Im(ω)	$(3.4 \pm 4.9) \times 10^{-4}$	$\pm 2 \times 10^{-5}$
Δa <sub>0</sub>	$[(0.4 \pm 1.8) \times 10^{-17} \text{ GeV}]$	$\pm 2 \times 10^{-18} \text{ GeV}$
Δa <sub>Z</sub>	$[(2.4 \pm 9.7) \times 10^{-18} \text{ GeV}]$	$\pm 7 \times 10^{-19} \text{ GeV}$
Δa <sub>X,Y</sub>	$[<10^{-21} \text{ GeV}]$	$O(10^{-19})\text{GeV}$