

# HP-PS circumference

The aim is to optimize the HP-PS circumference in order to improve synchronization in case of injection into SPS.

The present ratio between SPS and HP-PS is 5.88.

If we assume 25 ns beam the present harmonic number of SPS is 924. The idea is to find a ratio which is an integer or a ratio of integers.

25 ns beam leads to a revolution period of  $3.85\mu\text{s}$  then circumference of 1152m.

FT beam assuming MTE extraction.

In this case the SPS extraction kicker gap ( $1.1\mu\text{s}$ ) must be taken into account in the HPPS beam structure which will be, at HPPS extraction :  $3.85\mu\text{s} = 2.75\mu\text{s} + 1.1\mu\text{s}$ .

$2.75\mu\text{s}$  corresponds to 70% of HPPS circumference, so  $h_{\text{HPPS}}=110$  and  $2.5*10^{14}/110 = 2.27*10^{12}\text{ppb}$  in the HPPS.

If we assume 5-turn MTE extraction we obtain :  $2.27*10^{12}/5 = 4.54*10^{11}\text{ppb}$  in the SPS.

This is already higher than the maximum intensity which can be accepted by the SPS ( $2.5*10^{11}\text{ppb}$ ) so it must be decreased.

$5*2.75\mu\text{s} = 13.75\mu\text{s} = 59.5\%$  of SPS full of beam.

25 ns beam leads to a revolution period of  $4.19\mu\text{s}$  then circumference of 1256.63m.

FT beam assuming MTE extraction.

In this case the SPS extraction kicker gap ( $1.1\mu\text{s}$ ) must be taken into account in the HPPS beam structure which will be, at HPPS extraction :  $4.19\mu\text{s} = 3.09\mu\text{s} + 1.1\mu\text{s}$ .

$3.09\mu\text{s}$  corresponds to 70% of HPPS circumference, so  $h_{\text{HPPS}} = 124$  and  $2.5 \cdot 10^{14} / 124 = 2.1 \cdot 10^{12} \text{ppb}$  in the HPPS.

If we assume 5-turn MTE extraction we obtain :  $2.1 \cdot 10^{12} / 5 = 4.03 \cdot 10^{11} \text{ppb}$  in the SPS.

This is already higher than the maximum intensity which can be accepted by the SPS ( $2.5 \cdot 10^{11} \text{ppb}$ ) so it must be decreased.

$5 \cdot 3.09\mu\text{s} = 15.45\mu\text{s} = 67\%$  of SPS full of beam.