

# Dark Matter in Two Higgs doublet models with local $U(1)_H$ gauge symmetry

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Collaboration with P. Ko (KIAS) and Yuji Omura (Nagoya U.)

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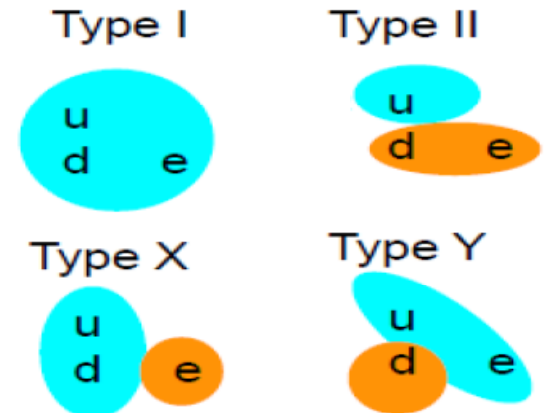
# Two Higgs doublet model

- Many high-energy models predict extra Higgs doublets.
  - SUSY, GUT, flavor symmetric models, etc.
- Two Higgs doublet model could be an effective theory of a high-energy theory.
- Two (or multi) Higgs doublet model itself is interesting.
  - Higgs physics (heavy Higgs, pseudoscalar, charged Higgs physics)
  - **dark matter physics** (one of Higgs scalar or extra fermions could be CDM.)  
Ma,PRD73;Barbieri,Hall,Rychkov,PRD74
  - baryon asymmetry of the Universe Shu,Zhang,PRL111
  - neutrino mass generation Kanemura,Matsui,Sugiyama,PLB727
  - can resolve experimental anomalies (top  $A_{FB}$  at Tevatron,  $B \rightarrow D^{(*)}TV$  at BABAR) Ko,Omura,Yu,EPJC73;JHEP1303

# 2HDM with $Z_2$ symmetry (2HDMw $Z_2$ )

- One of the simplest models to extend the SM Higgs sector.
- In general, flavor changing neutral currents (FCNCs) appear.
- A simple way to avoid the FCNC problem is to assign **ad hoc  $Z_2$  symmetry**.

Type	$H_1$	$H_2$	$U_R$	$D_R$	$E_R$	$N_R$	$Q_{L,L}$
I	+	-	+	+	+	+	+
II	+	-	+	-	-	+	+
X	+	-	+	+	-	-	+
Y	+	-	+	-	+	-	+



Fermions of same electric charges get their masses from one Higgs VEV.

$$\mathcal{L} = \bar{L}_i (y_{1ij}^E H_1 + \cancel{y_{2ij}^E H_2}) E_{Rj} + \text{H.c.} \quad \text{or vice versa}$$

NO FCNC at tree level.

# Generic problems of 2HDM

- It is well known that discrete symmetry could generate a domain wall problem when it is spontaneously broken.
- Usually the  $Z_2$  symmetry is assumed to be broken softly by a dim-2 operator,  $H_1^\dagger H_2$  term.

The softly broken  $Z_2$  symmetric 2HDM potential

$$V = m_1^2 H_1^\dagger H_1 + m_2^2 H_2^\dagger H_2 - (m_{12}^2 H_1^\dagger H_2 + h.c.) + \frac{1}{2} \lambda_1 (H_1^\dagger H_1)^2 + \frac{1}{2} \lambda_2 (H_2^\dagger H_2)^2 + \lambda_3 (H_1^\dagger H_1)(H_2^\dagger H_2) + \lambda_4 (H_1^\dagger H_2)(H_2^\dagger H_1) + \frac{1}{2} \lambda_5 [(H_1^\dagger H_2)^2 + h.c.]$$

- the origin of the softly breaking term?

$Z_2$  symmetry in 2HDM can be replaced by new  $U(1)_H$  symmetry associated with Higgs flavors.

# Type-I 2HDM

- Only one Higgs couples with fermions.

$$V_y = y_{ij}^U \bar{Q}_{Li} \tilde{H}_1 U_{Rj} + y_{ij}^D \bar{Q}_{Li} H_1 D_{Rj} + y_{ij}^E \bar{L}_i H_1 E_{Rj} + y_{ij}^N \bar{L}_i \tilde{H}_1 N_{Rj}$$

- anomaly free  $U(1)_H$  without extra fermions except RH neutrinos.

$U_R$	$D_R$	$Q_L$	$L$	$E_R$	$N_R$	$H_1$
$u$	$d$	$\frac{(u+d)}{2}$	$\frac{-3(u+d)}{2}$	$-(2u+d)$	$-(u+2d)$	$\frac{(u-d)}{2}$



2 parameters

- In general, extra fermions are required in order to cancel gauge anomaly.

→ one of extra fermions can be a candidate for the cold dark matter.

# Type-I 2HDM

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$$V_y = y_{ij}^U \bar{Q}_{Li} \tilde{H}_1 U_{Rj} + y_{ij}^D \bar{Q}_{Li} H_1 D_{Rj} + y_{ij}^E \bar{L}_i H_1 E_{Rj} + y_{ij}^N \bar{L}_i \tilde{H}_1 N_{Rj}$$

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$U_R$	$D_R$	$Q_R$	$L$	$E_R$	$N_R$	$H_1$	Type
$u$	$d$	$\frac{(u+d)}{2}$	$\frac{-3(u+d)}{2}$	$-(2u+d)$	$-(u+2d)$	$\frac{(u-d)}{2}$	
0	0	0	0	0	0	0	$h_2 \neq 0$
1/3	1/3	1/3	-1	-1	-1	0	$U(1)_{B-L}$
1	-1	0	0	-1	1	1	$U(1)_R$
2/3	-1/3	1/6	-1/2	-1	0	1/2	$U(1)_Y$

Ko, Omura, Yu, PLB717,202(2013)

- SM fermions are  $U(1)_H$  singlets.
- $Z_H$  is fermiophobic and Higgphilic.

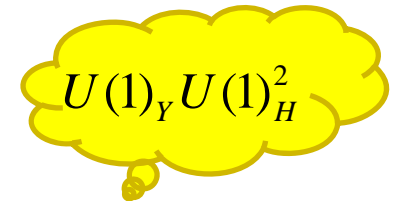
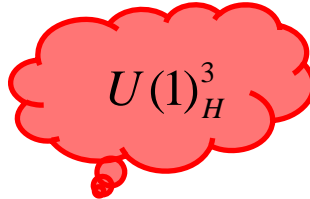
# Type-II 2HDM

- $H_1$  couples to the up-type fermions, while  $H_2$  couples to the down-type fermions.

$$V_y = y_{ij}^U \bar{Q}_{Li} \tilde{H}_1 U_{Rj} + y_{ij}^D \bar{Q}_{Li} H_2 D_{Rj} + y_{ij}^E \bar{L}_i H_2 E_{Rj} + y_{ij}^N \bar{L}_i \tilde{H}_1 N_{Rj}$$

$U_R$	$D_R$	$Q_L$	$L$	$E_R$	$N_R$	$H_1$	$H_2$
$u$	0	0	0	0	$u$	$u$	0

- Requires extra chiral fermions for cancellation of gauge anomaly.



	$SU(3)$	$SU(2)$	$U(1)_Y$	$U(1)_H$
$q_{Li}$	3	1	2/3	$\hat{Q}_L = u + \hat{Q}_R$
$q_{Ri}$	3	1	2/3	$\hat{Q}_R$
$n_{Li}$	1	1	0	$\hat{n}_L = u + \hat{n}_R$
$n_{Ri}$	1	1	0	$\hat{n}_R$



Two vector-like pairs of  $SU(2)_L$

Mixing between new chiral fermions and SM fermions is prohibited by  $U(1)_H$  charge assignment.

One of extra fermions could be a candidate for CDM.

# Constraints

- experimental and theoretical constraints

$$m_h \sim 126 \text{ GeV}$$

$$|m_{H^+} - m_A|$$

$$|m_{H^+} - m_H|$$

$$\sin(\beta - \alpha)$$

$$\tan \beta$$

$$m_{H^+}$$

SM-like Higgs

$$m_H$$

EWPOs

small mass differences required

Exotic top decay

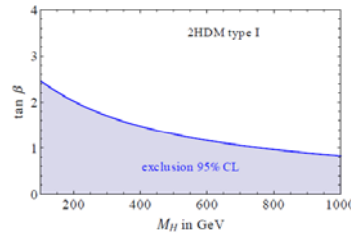
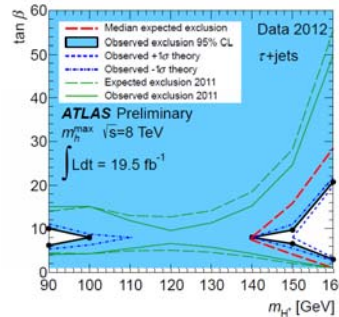
$$b \rightarrow s\gamma$$

Heavy Higgs search at LHC

Perturbativity

Unitarity

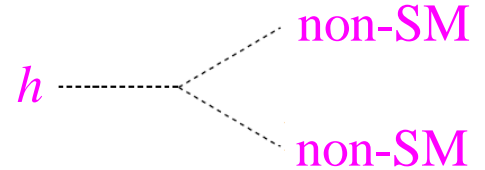
Vacuum stability



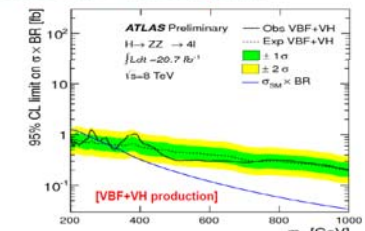
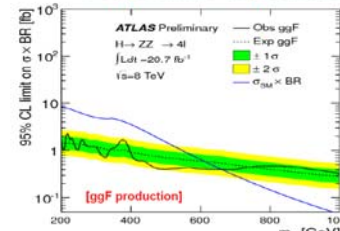
$$\tan \beta \gtrsim 1$$

Hermann, Misiak, Steinhauser, JHEP1211 (2012) 036

Invisible Higgs decay



→ Upper limits on production cross section × branching ratio



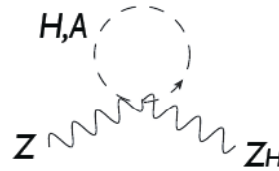


# Z-Z<sub>H</sub> mixing

- tree-level mixing ( $v_i \neq 0$ )

$$\Delta M_{ZZH}^2 = -\frac{\hat{M}_Z}{v} g_H \sum_{i=1}^2 q_{H_i} v_i^2 \quad \tan 2\xi = \frac{2\Delta M_{ZZH}^2}{\hat{M}_{ZH}^2 - \hat{M}_Z^2}$$

- loop-level mixing ( $v_1=0, v_2 \neq 0$ )



$$-\frac{\kappa_Z}{2} F_Z^{\mu\nu} F_{H\mu\nu} - \frac{\kappa_\gamma}{2} F_\gamma^{\mu\nu} F_{H\mu\nu} + \Delta M_{ZH}^2 \hat{Z}^\mu \hat{Z}_{H\mu}$$

$$\kappa_Z = \frac{q_H g_H e c_W}{16\pi^2 s_W} \left\{ \frac{1}{3} \ln \left( \frac{m_A^2}{m_{H^+}^2} \right) - \frac{1}{6} \frac{m_A^2 - m_H^2}{m_A^2} \right\},$$

$$\kappa_\gamma = \frac{q_H g_H e}{16\pi^2} \left\{ \frac{1}{3} \ln \left( \frac{m_A^2}{m_{H^+}^2} \right) - \frac{1}{6} \frac{m_A^2 - m_H^2}{m_A^2} \right\},$$

$$\Delta M_{ZH}^2 = -\frac{q_H g_H e}{32\pi^2 s_W c_W} (m_A^2 - m_H^2).$$

The mixing can appear because of  $SU(2)_L \times U(1)_Y$  breaking effects.

- collider bound depends on the  $U(1)_H$  charge assignment.
- In the fermiophobic  $Z_H$  case, the  $Z_H$  boson can be produced through the  $Z$ - $Z_H$  mixing and the bound for the mixing angle is

$$\sin \xi \lesssim O(10^{-2}) \sim O(10^{-3})$$

# Inert Doublet Model (IDMwZ<sub>2</sub>)

- a 2HDM ~ one of the simplest extension
- One of Higgs doublets does not develop VEV and exact Z<sub>2</sub> symmetry is imposed.
- The new Higgs doublet does not participate in the EW symmetry breaking.
- Under the Z<sub>2</sub> symmetry, SM particles are even, but the new Higgs doublet is odd.
- Viable DM candidate

$$H_1 = \begin{pmatrix} H^+ \\ \frac{1}{\sqrt{2}} (\underbrace{H}_{\text{DM candidates}} + i\underbrace{A}_{\text{DM candidates}}) \end{pmatrix}, \quad H_2 = \begin{pmatrix} G^+ \\ \frac{1}{\sqrt{2}} (v + \underbrace{h}_{\text{SM-like Higgs}} + iG^0) \end{pmatrix}$$

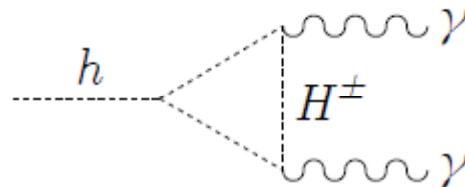
# Inert Doublet Model (IDMwZ<sub>2</sub>)

- CP-conserving potential

$$V = \mu_1 (H_1^\dagger H_1) + \mu_2 (H_2^\dagger H_2) - \mu_{12} (H_1^\dagger H_2 + h.c.) + \frac{\lambda_1}{2} (H_1^\dagger H_1)^2 + \frac{\lambda_2}{2} (H_2^\dagger H_2)^2 + \lambda_3 (H_1^\dagger H_1)(H_2^\dagger H_2) + \lambda_4 |H_1^\dagger H_2|^2 + \frac{\lambda_5}{2} \{ (H_1^\dagger H_2)^2 + h.c. \}.$$

forbidden by the Z<sub>2</sub> symmetry

- Type-I Yukawa interactions ~ only H<sub>2</sub> couples to the SM fermions.
- The h decay to two photons receives additional contribution through charged Higgs loop.



- H, A, H<sup>±</sup> ~ do not couple to SM fermions at tree level.

# Inert Double Model (IDMwU(1)<sub>H</sub>)

- We replace the  $Z_2$  symmetry by **U(1) gauge symmetry**.
- A SM-singlet  $\Phi$  has to be added.
- Without  $\Phi$ ,  $Z_H$  boson becomes massless.

$$\begin{aligned}
 V = & (m_1^2 + \tilde{\lambda}_1 |\Phi|^2)(H_1^\dagger H_1) + (m_2^2 + \tilde{\lambda}_2 |\Phi|^2)(H_2^\dagger H_2) - (m_{12}^2 H_1^\dagger H_2 + \text{h.c.}) \\
 & + \frac{\lambda_1}{2} (H_1^\dagger H_1)^2 + \frac{\lambda_2}{2} (H_2^\dagger H_2)^2 + \lambda_3 (H_1^\dagger H_1)(H_2^\dagger H_2) + \lambda_4 |H_1^\dagger H_2|^2 \\
 & + \frac{\lambda_5}{2} \{(H_1^\dagger H_2)^2 + \text{h.c.}\} + m_\Phi^2 |\Phi|^2 + \lambda_\Phi |\Phi|^4
 \end{aligned}$$

- $\Phi$  breaks the  $U(1)_H$  symmetry while  $H_2$  breaks the EW symmetry.
- The remnant symmetry of  $U(1)_H$  is the origin of the exact  $Z_2$  symmetry.

# Inert Double Model (IDMwU(1)<sub>H</sub>)

- We replace the Z<sub>2</sub> symmetry by **U(1) gauge symmetry**.
- A SM-singlet Φ has to be added.
- Without Φ, Z<sub>H</sub> boson becomes massless.

$$\begin{aligned}
 V = & (m_1^2 + \tilde{\lambda}_1 |\Phi|^2)(H_1^\dagger H_1) + (m_2^2 + \tilde{\lambda}_2 |\Phi|^2)(H_2^\dagger H_2) - \cancel{(m_{12}^2 H_1^\dagger H_2 + \text{h.c.})} \\
 & + \frac{\lambda_1}{2} (H_1^\dagger H_1)^2 + \frac{\lambda_2}{2} (H_2^\dagger H_2)^2 + \lambda_3 (H_1^\dagger H_1)(H_2^\dagger H_2) + \lambda_4 |H_1^\dagger H_2|^2 \\
 & + \frac{\lambda_5}{2} \{ \cancel{(H_1^\dagger H_2)^2} + \text{h.c.} \} + m_\Phi^2 |\Phi|^2 + \lambda_\Phi |\Phi|^4
 \end{aligned}$$

forbidden  
by the Z<sub>2</sub> symmetry

forbidden by the U(1)<sub>H</sub> symmetry (q<sub>H<sub>2</sub></sub>=0, q<sub>H<sub>1</sub></sub>≠0)

- Φ breaks the U(1)<sub>H</sub> symmetry while H<sub>2</sub> breaks the EW symmetry.
- The remnant symmetry of U(1)<sub>H</sub> is the origin of the exact Z<sub>2</sub> symmetry.

# Inert Double Model (IDMwU(1)<sub>H</sub>)

- IDM + SM-singlet  $\Phi$ .

$$\begin{aligned}
 V = & (m_1^2 + \tilde{\lambda}_1 |\Phi|^2)(H_1^\dagger H_1) + (m_2^2 + \tilde{\lambda}_2 |\Phi|^2)(H_2^\dagger H_2) - (m_{12}^2 H_1^\dagger H_2 + \text{h.c.}) \\
 & + \frac{\lambda_1}{2} (H_1^\dagger H_1)^2 + \frac{\lambda_2}{2} (H_2^\dagger H_2)^2 + \lambda_3 (H_1^\dagger H_1)(H_2^\dagger H_2) + \lambda_4 |H_1^\dagger H_2|^2 \\
 & + \frac{\lambda_5}{2} \{ (H_1^\dagger H_2)^2 + \text{h.c.} \} + m_\Phi^2 |\Phi|^2 + \lambda_\Phi |\Phi|^4
 \end{aligned}$$

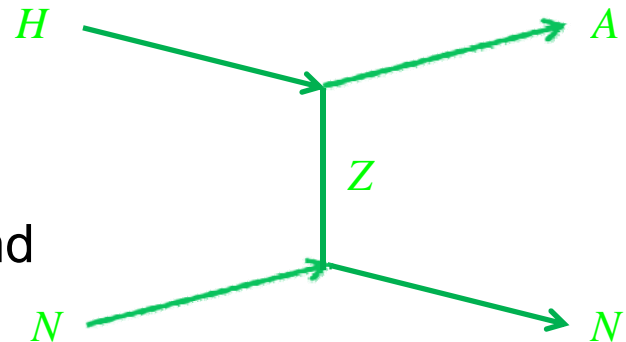
forbidden  
by the  $Z_2$  symmetry

forbidden by the  $U(1)_H$  symmetry ( $q_{H_2}=0, q_{H_1} \neq 0$ )

- Without  $\lambda_5$ , H and A are degenerate.

$$m_A = \sqrt{m_H^2 - \lambda_5 v^2}$$

- Direct searches for DM at XENON100 and LUX exclude this degenerate case.



# Inert Double Model (IDMwU(1)<sub>H</sub>)

- IDM + SM-singlet  $\Phi$ .

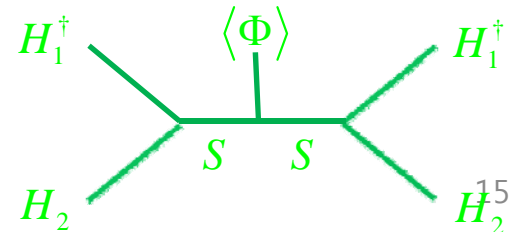
forbidden  
by the  $Z_2$  symmetry

$$\begin{aligned}
 V = & (m_1^2 + \tilde{\lambda}_1 |\Phi|^2)(H_1^\dagger H_1) + (m_2^2 + \tilde{\lambda}_2 |\Phi|^2)(H_2^\dagger H_2) - (m_{12}^2 H_1^\dagger H_2 + \text{h.c.}) \\
 & + \frac{\lambda_1}{2} (H_1^\dagger H_1)^2 + \frac{\lambda_2}{2} (H_2^\dagger H_2)^2 + \lambda_3 (H_1^\dagger H_1)(H_2^\dagger H_2) + \lambda_4 |H_1^\dagger H_2|^2 \\
 & + \left\{ c_l \left( \frac{\Phi}{\Lambda} \right)^l (H_1^\dagger H_2)^2 + \text{h.c.} \right\} + m_\Phi^2 |\Phi|^2 + \lambda_\Phi |\Phi|^4
 \end{aligned}$$

- The  $\lambda_5$  term can effectively be generated by a higher-dimensional operator.
- It could be realized by introducing a singlet  $S$  charged under  $U(1)_H$  with  $q_S = q_{H_1}$ .

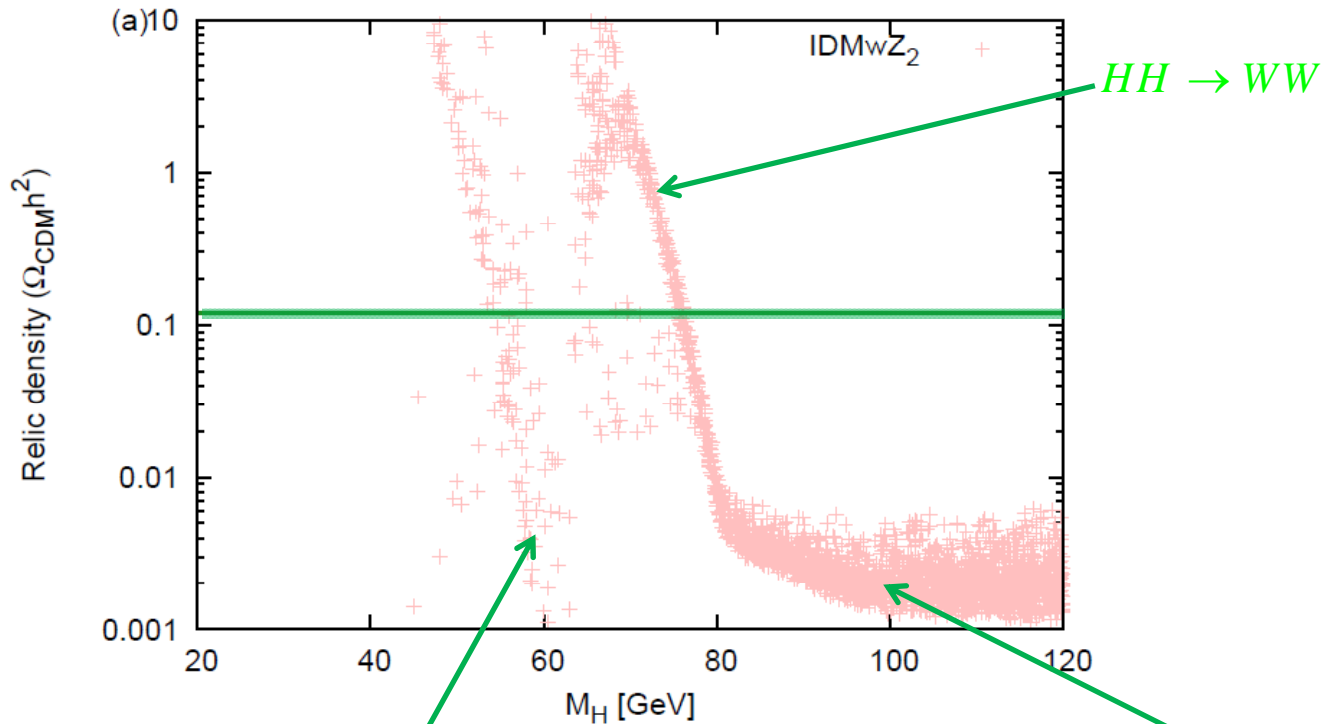
$$V_\Phi(|\Phi|^2, |S|^2) + V_H(H_i, H_i^\dagger) + \lambda_S(\Phi)S^2 + \lambda_H(S)H_1^\dagger H_2 + \text{h.c.}$$

$$\lambda_H = \lambda_H^0 S \quad \lambda_5 \sim \frac{(\lambda_H^0)^2}{2} \frac{\Delta m^2}{m_{\text{Re}(S)}^2 m_{\text{Im}(S)}^2},$$



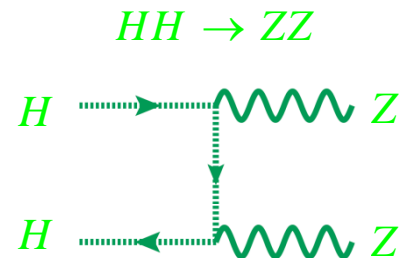
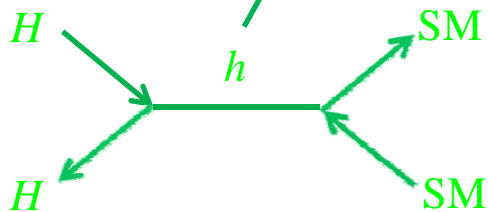
# Relic density (low mass)

$$\Omega_{\text{CDM}} h^2 = 0.1199 \pm 0.0027$$



+ IDMwZ<sub>2</sub>

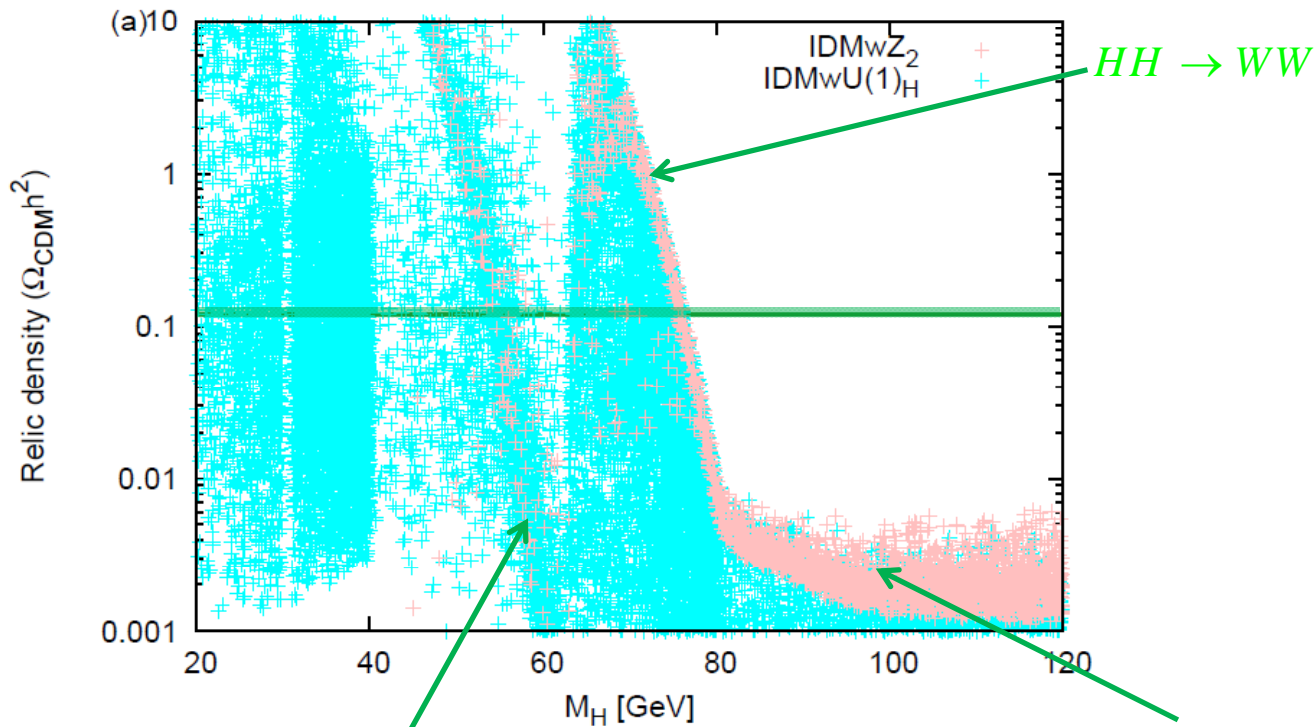
LUX bound is satisfied.





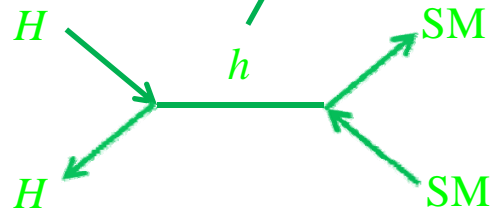
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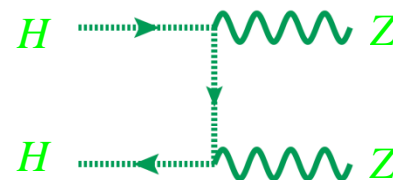


+  $\text{IDM}_{wZ_2}$   
+  $\text{IDM}_{wU(1)_H}$

LUX bound is satisfied.

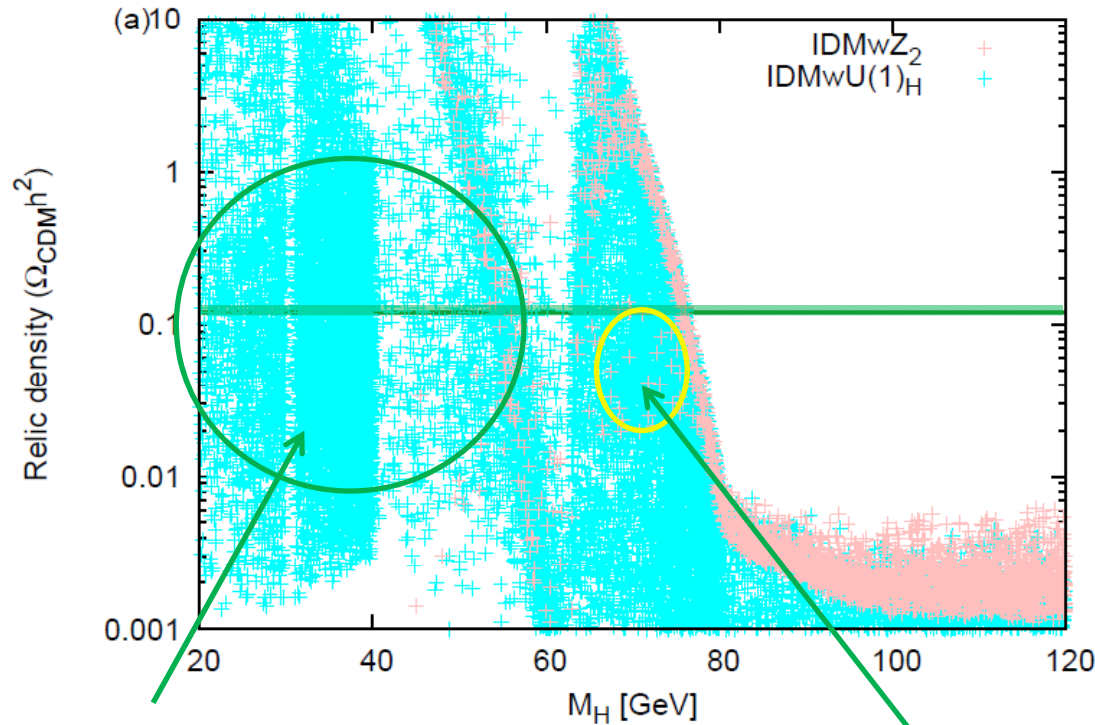


$HH \rightarrow ZZ$



# Relic density (low mass)

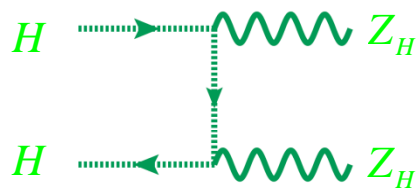
$$\Omega_{\text{CDM}} h^2 = 0.1199 \pm 0.0027$$



+ IDMwZ<sub>2</sub>  
+ IDMwU(1)<sub>H</sub>

LUX bound is satisfied.

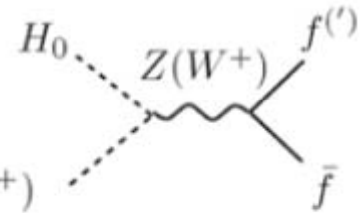
$$HH \rightarrow Z_H Z_H, ZZ_H$$



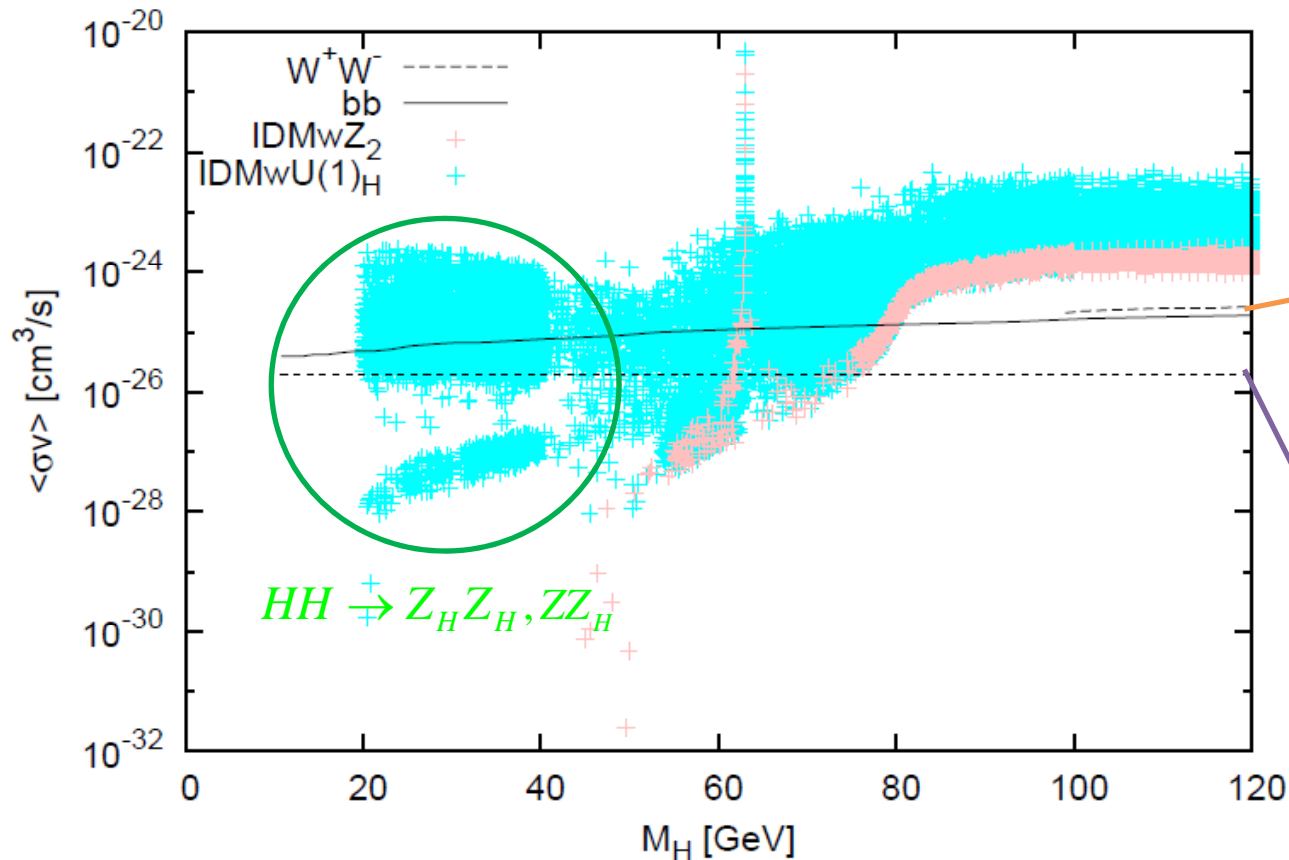
$$HA, HH^\pm \rightarrow \text{SM} + \text{SM}^{(\prime)}$$

$$H^+ H^- \rightarrow A + Z_H, Z + Z_H, \dots$$

Co-annihilation



# Indirect searches (low mass)



+  $IDMwZ_2$   
+  $IDMwU(1)_H$

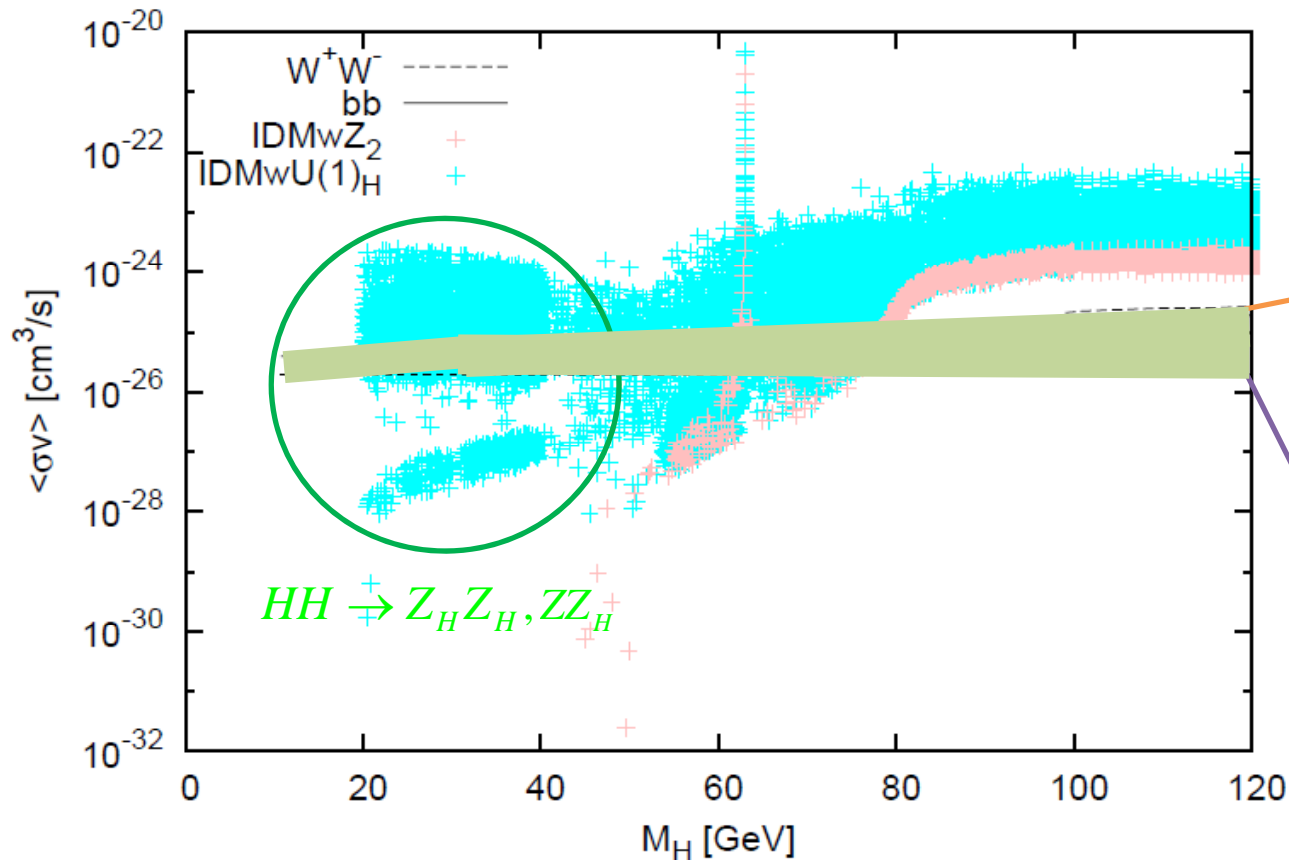
Constraints on the DM annihilation cross section from Fermi-LAT's analysis of 15 dwarf spheroidal galaxies.

Fermi-LAT, arXiv:1310.0828

Constraint on the S-wave DM annihilation from the relic density observation

- All points satisfy constraints from the relic density observation and LUX experiments.

# Indirect searches (low mass)



+  $IDMwZ_2$   
+  $IDMwU(1)_H$

Constraints on the DM annihilation cross section from Fermi-LAT's analysis of 15 dwarf spheroidal galaxies.

Fermi-LAT, arXiv:1310.0828

Constraint on the S-wave DM annihilation from the relic density observation

- But, indirect DM signals depend on the decay patterns of produced particles from annihilation or decay of DMs.

# Gamma ray flux from DM annihilation

- Dwarf spheroidal galaxies are excellent targets to search for annihilating DM signatures because of DM-dominant nature without astrophysical backgrounds like hot gas.

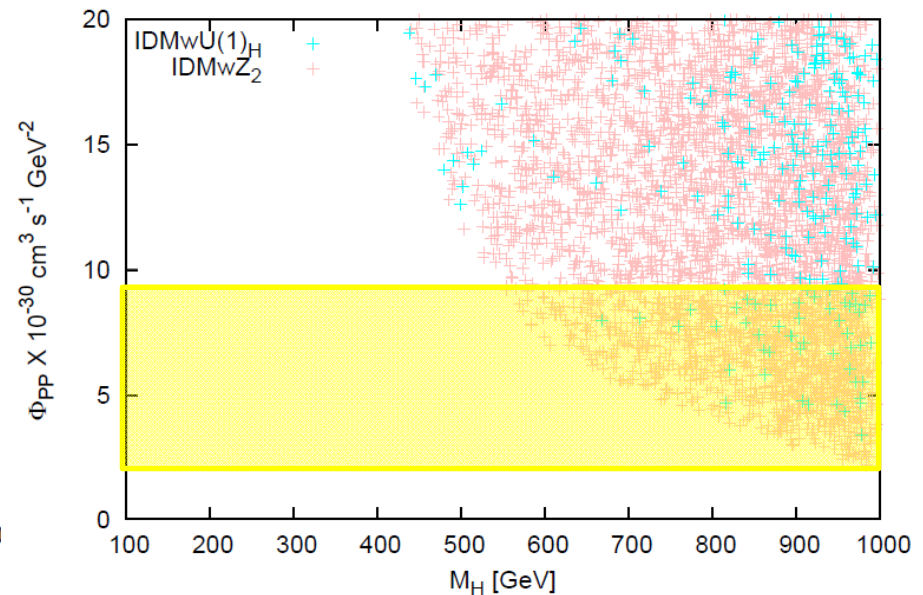
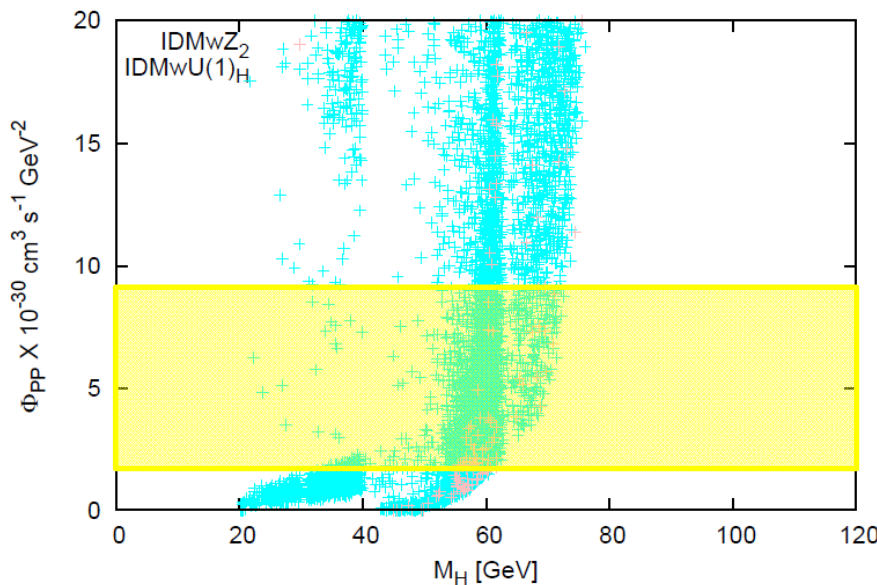
$$\phi_s(\Delta\Omega) = \underbrace{\frac{1}{4\pi} \frac{\langle\sigma v\rangle}{2m_{\text{DM}}^2} \int_{E_{\text{min}}}^{E_{\text{max}}} \left(\frac{dN_\gamma}{dE_\gamma}\right) dE_\gamma}_{\Phi_{\text{PP}}} \cdot \underbrace{\int_{\Delta\Omega} \left\{ \int_{\text{l.o.s.}} \rho^2(\mathbf{r}) dl \right\} d\Omega'}_{\text{J-factor}} .$$

The final  $\gamma$ -ray spectrum.

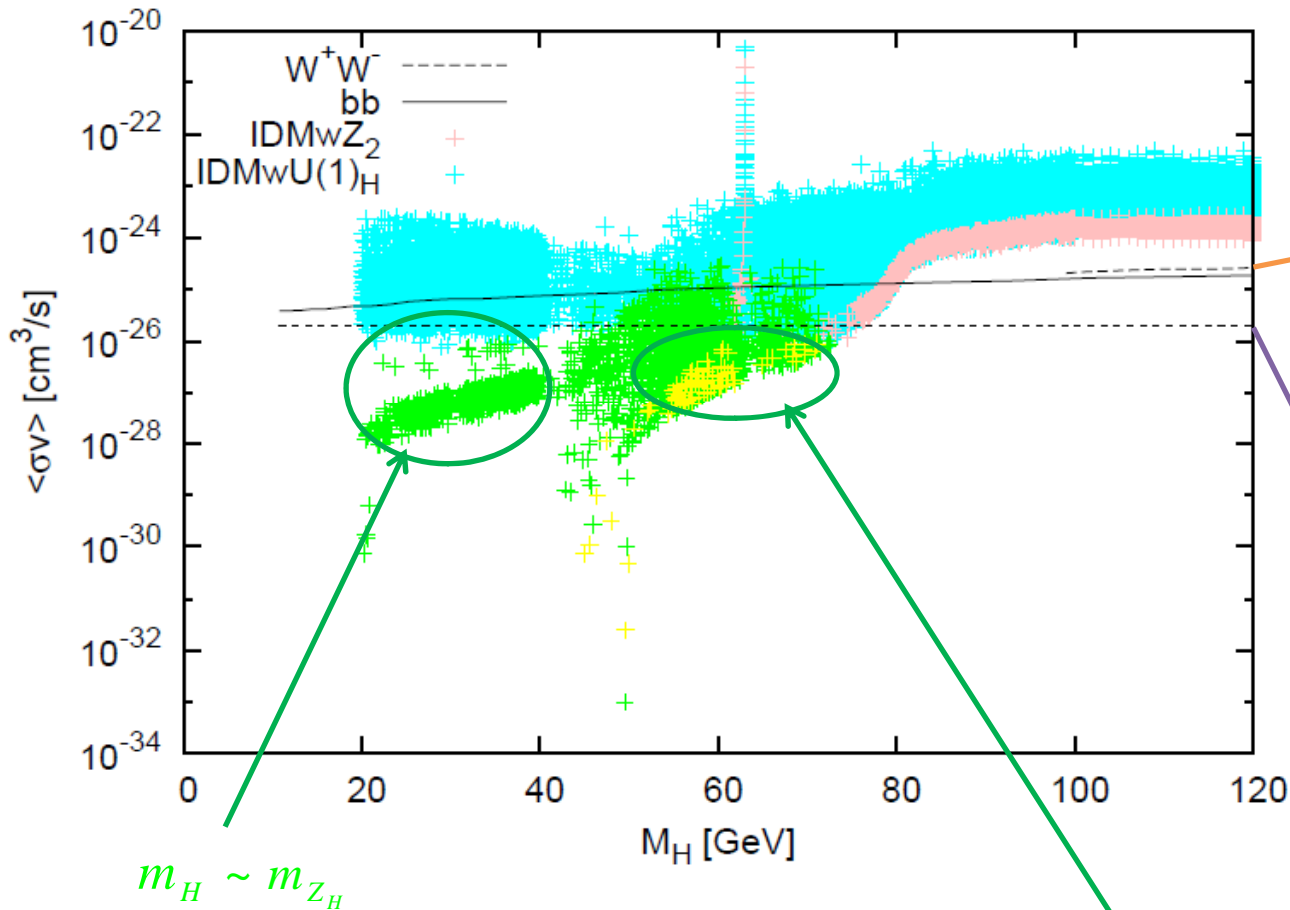
contains information about the distribution of DM.

A 95% upper bound is  $\Phi_{\text{PP}} = 5.0_{-4.5}^{+4.3} \times 10^{-30} \text{ cm}^3 \text{ s}^{-1} \text{ GeV}^{-2}$

Geringer-Sameth, Koushiappas, PRL107



# Indirect searches (low mass)



+  $IDMwZ_2$   
 +  $IDMwU(1)_H$

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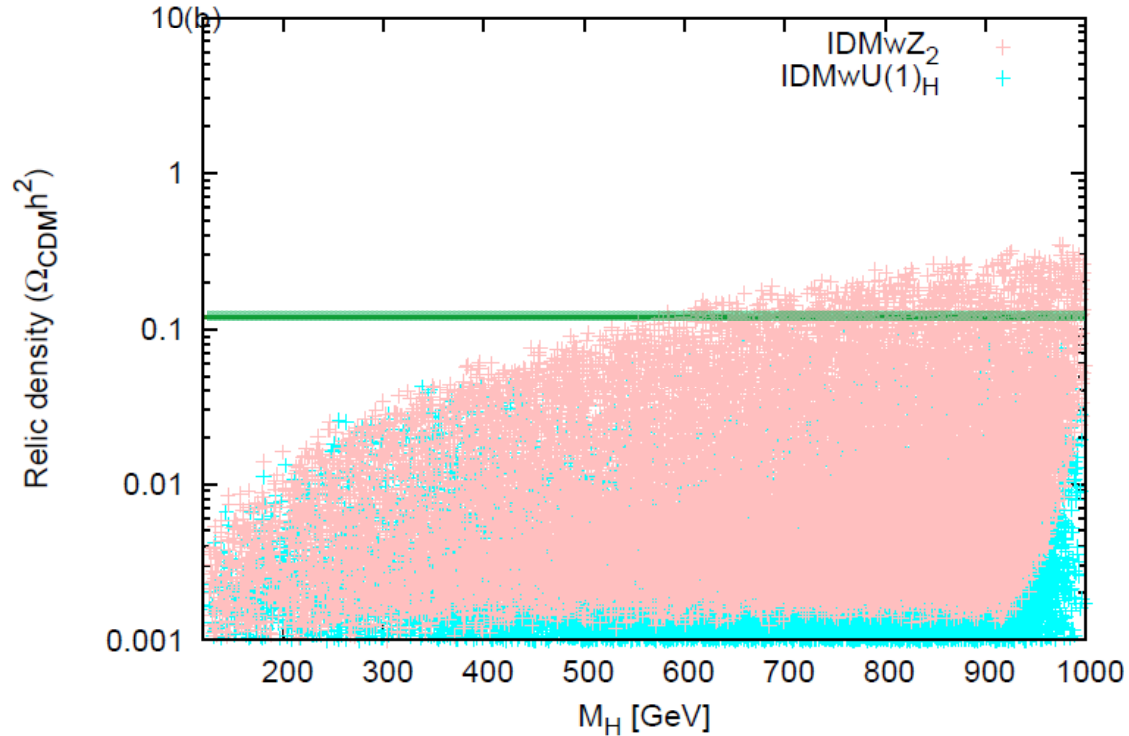
[Fermi-LAT, arXiv:1310.0828](#)

Constraint on the S-wave DM annihilation from the relic density observation

Co-annihilation

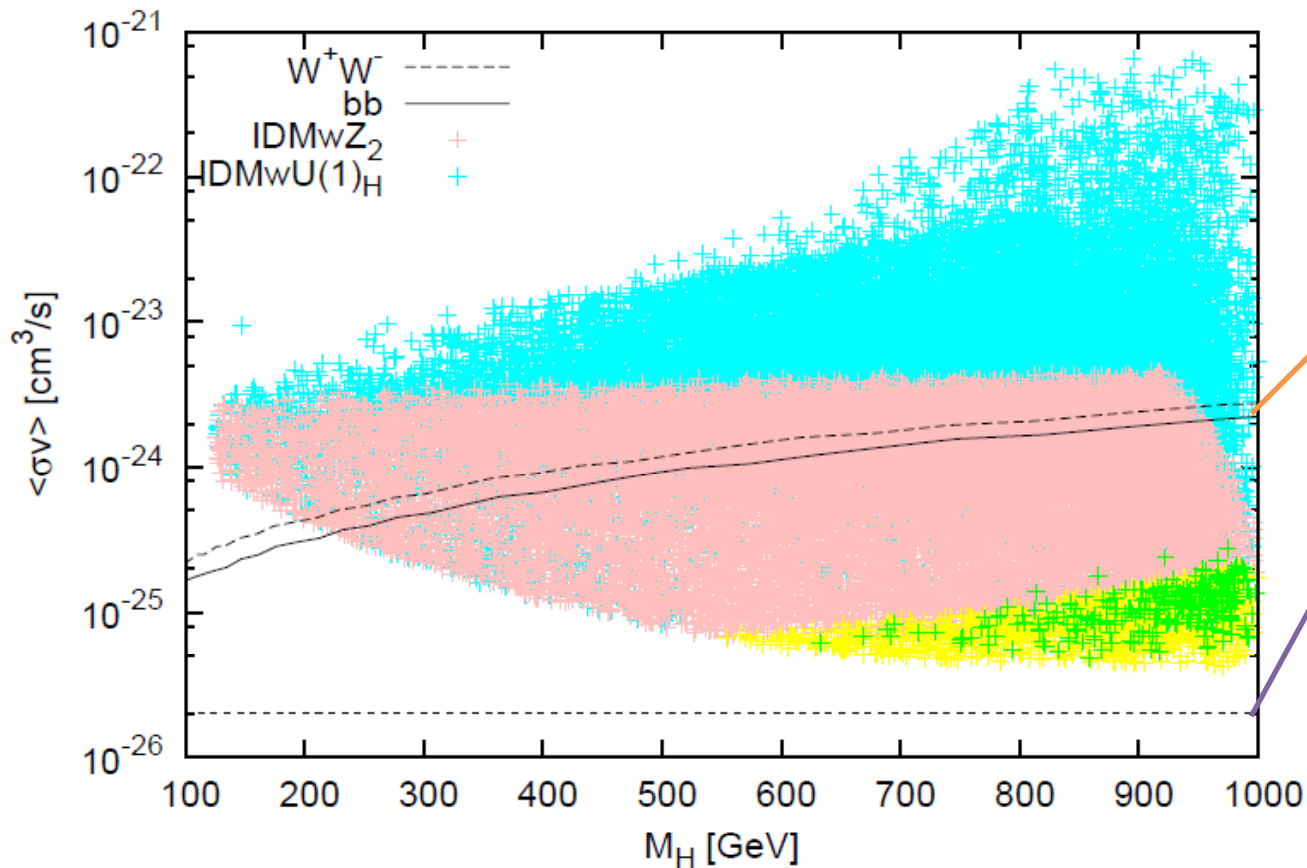
# Relic density (high mass)

$$\Omega_{\text{CDM}} h^2 = 0.1199 \pm 0.0027$$



+ IDMwZ<sub>2</sub>  
+ IDMwU(1)<sub>H</sub>

# Indirect searches (high mass)



Constraints on the DM annihilation cross section from Fermi-LAT's analysis of 15 dwarf spheroidal galaxies.

Fermi-LAT, arXiv:1310.0828

Constraint on the S-wave DM annihilation from the relic density observation



# Conclusions

- 2HDM may be an effective theory of a high-energy theory and useful to test the underlying theory.
- 2HDM can easily be extended to a gauged model and the  $U(1)$  gauge symmetry could be the origin of  $Z_2$  symmetry.
- The  $U(1)$  extension to inert doublet model could introduce dark matter candidates whose stability are guaranteed by the remnant symmetry of  $U(1)_H$ .
- In type-I, a light CDM scenario is possible in the  $IDMwU(1)_H$ .

Back up

# Higgs Potential

- in the ordinary 2HDM with  $Z_2$  symmetry

$$V = m_1^2 H_1^\dagger H_1 + m_2^2 H_2^\dagger H_2 - (m_{12}^2 H_1^\dagger H_2 + h.c.) + \frac{1}{2} \lambda_1 (H_1^\dagger H_1)^2 + \frac{1}{2} \lambda_2 (H_2^\dagger H_2)^2 + \lambda_3 (H_1^\dagger H_1)(H_2^\dagger H_2) + \lambda_4 (H_1^\dagger H_2)(H_2^\dagger H_1) + \frac{1}{2} \lambda_5 [(H_1^\dagger H_2)^2 + h.c.]$$

not invariant under  $U(1)_H$

- in the 2HDM with  $U(1)_H$ , we include an extra singlet scalar  $\Phi$ , which makes  $Z_H$  heavy.

$$V = \hat{m}_1^2 (|\Phi|^2) H_1^\dagger H_1 + \hat{m}_2^2 (|\Phi|^2) H_2^\dagger H_2 - (m_3^2 (\Phi) H_1^\dagger H_2 + h.c.) + \frac{\lambda_1}{2} (H_1^\dagger H_1)^2 + \frac{\lambda_2}{2} (H_2^\dagger H_2)^2 + \lambda_3 (H_1^\dagger H_1)(H_2^\dagger H_2) + \lambda_4 |H_1^\dagger H_2|^2 + m_\Phi^2 |\Phi|^2 + \lambda_\Phi |\Phi|^4$$

$$H_1^\dagger H_2 \Phi$$

invariant under  $U(1)_H$

no  $\lambda_5$  terms!

- neutral Higgs

$$\begin{pmatrix} h_\Phi \\ h_1 \\ h_2 \end{pmatrix} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & \cos \alpha & -\sin \alpha \\ 0 & \sin \alpha & \cos \alpha \end{pmatrix} \begin{pmatrix} \cos \alpha_1 & 0 & -\sin \alpha_1 \\ 0 & 1 & 0 \\ \sin \alpha_1 & 0 & \cos \alpha_1 \end{pmatrix} \begin{pmatrix} \cos \alpha_2 & -\sin \alpha_2 & 0 \\ \sin \alpha_2 & \cos \alpha_2 & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} \tilde{h} \\ H \\ h \end{pmatrix}$$

- a pair of charged Higgs + 1 pseudoscalar Higgs + 3 neutral Higgs bosons