

# Systematic uncertainties from halo asphericity in dark matter searches

based on NB, Jaime Forero-Romero,  
Raghuveer Garani & Sergio Palomares-Ruiz

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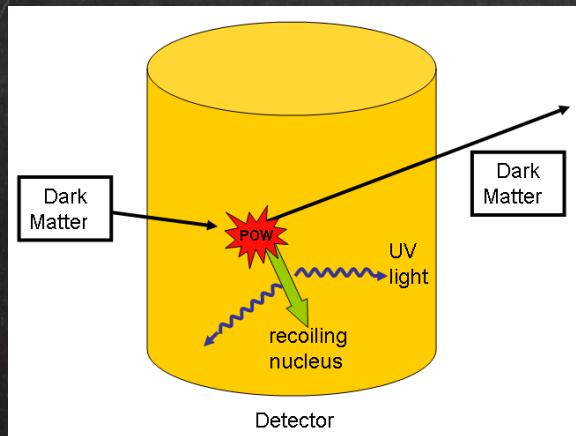
PLANCK à Paris, May 28<sup>th</sup>, 2014

# Direct and indirect DM searches

Several observations indicate existence of non-luminous Dark Matter (missing force) at very different scales! —» WIMPs

## \* Direct detection

DM particles streaming through the Earth could scatter with the nuclei of the detector



$$R \approx \frac{\rho_{\odot} \sigma \langle \nu \rangle}{m_{\chi} m_A}$$

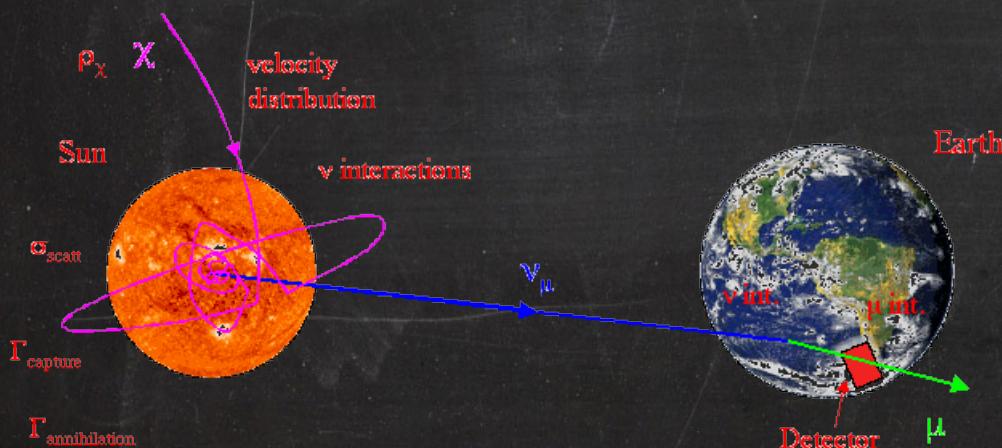
# Direct and indirect DM searches

Several observations indicate existence of non-luminous Dark Matter (missing force) at very different scales! —» WIMPs

\* Direct detection

\* Direct/Indirect detection

Flux of neutrinos  $\propto$  Sun's capture rate  
 $\propto$  DM particles through the Sun  $\propto$  local DM density



$$\dot{N}_\chi(t) = C_\odot - A_\odot N_\chi^2(t) - E_\odot N_\chi(t)$$

$$C^\odot \approx 1.3 \times 10^{21} \text{ sec}^{-1} \left( \frac{\rho_{\text{local}}}{0.3 \text{ GeV/cm}^3} \right) \left( \frac{270 \text{ km/s}}{\bar{v}_{\text{local}}} \right) \times \left( \frac{100 \text{ GeV}}{m_\chi} \right) \sum_i \left( \frac{A_i (\sigma_{\chi i, \text{SD}} + \sigma_{\chi i, \text{SI}}) S(m_\chi/m_i)}{10^{-6} \text{ pb}} \right),$$

# Direct and indirect DM searches

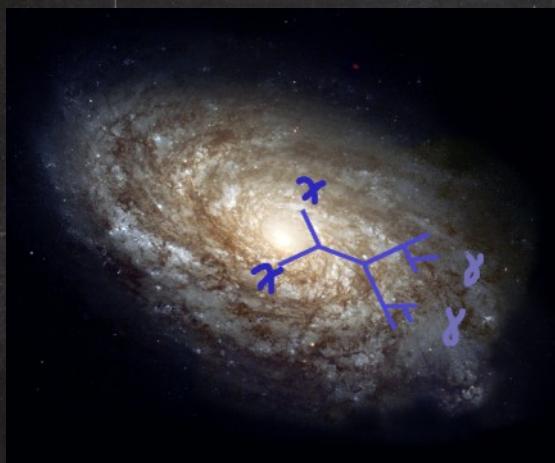
Several observations indicate existence of non-luminous Dark Matter (missing force) at very different scales! —» WIMPs

- \* Direct detection

- \* Direct/Indirect detection

- \* Indirect detection

Not only the local normalization is important but the also the shape of the halo!



$$\left( \frac{d\Phi_{\text{ann}}}{dE} \right) (E, \Delta\Omega) = \frac{\langle \sigma v \rangle}{2 m_\chi^2} \sum_i \text{BR}_i \frac{dN_{\text{ann}}^i}{dE} J_{\text{ann}}(\Omega) \frac{\Delta\Omega}{4\pi}$$
$$\left( \frac{d\Phi_{\text{dec}}}{dE} \right) (E, \Delta\Omega) = \frac{1}{m_\chi \tau_\chi} \sum_i \text{BR}_i \frac{dN_{\text{dec}}^i}{dE} J_{\text{dec}}(\Omega) \frac{\Delta\Omega}{4\pi}$$

$$J_{\text{ann}}(\Omega) \Delta\Omega = \int_{\Delta\Omega} d\Omega \int_{\text{los}} \rho(r(s, \Omega))^2 ds$$

$$J_{\text{dec}}(\Omega) \Delta\Omega = \int_{\Delta\Omega} d\Omega \int_{\text{los}} \rho(r(s, \Omega)) ds$$

# Direct and indirect DM searches

Several observations indicate existence of non-luminous  
Dark Matter (missing force) at very different scales! —» WIMPs

- \* Direct detection
- \* Direct/Indirect detection
- \* Indirect detection

In order to extract particle physics parameters ( $m_x$ ,  $\sigma$ ,  $\langle\sigma v\rangle$ ,  $\tau_{\text{dec}}$  ...) from DM experiments, the astrophysics ( $\rho_0$ ,  $J \cdot \Delta\Omega$ ) has to be under control —» DM halo

# DM: spherical halos?

N-body simulations favour Einasto and Navarro-Frenk-White profiles.

NFW

$$\rho(r) = \frac{4\rho_s}{r/r_s (1 + r/r_s)^2}$$

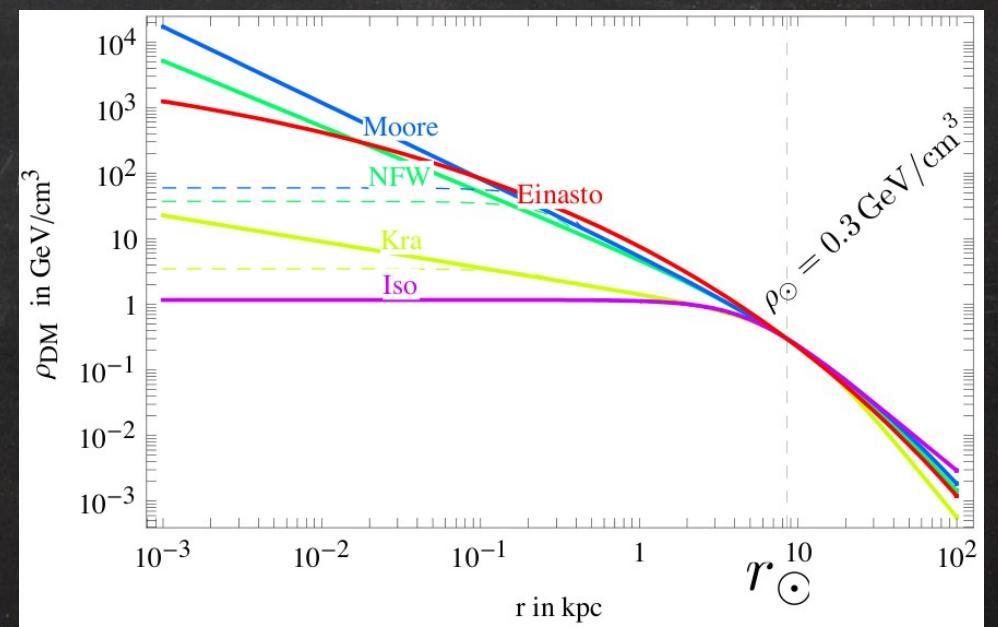
Einasto

$$\rho(r) = \rho_\odot \exp \left[ -\frac{2}{\alpha} \left( \left( \frac{r}{r_s} \right)^\alpha - \left( \frac{R_\odot}{r_s} \right)^\alpha \right) \right]$$

$$\rho_0 = 0.3 \text{ GeV / cm}^3$$

$$r_s = 20 \text{ kpc}$$

$$\alpha = 0.38$$



# DM: triaxial halos!

N-body simulations favour Einasto and Navarro-Frenk-White profiles.

Halos are found to be non-spherical.  
In fact, spherical halos are rare!

Baryons prefer to lay in one of  
the 3 symmetry planes

NFW

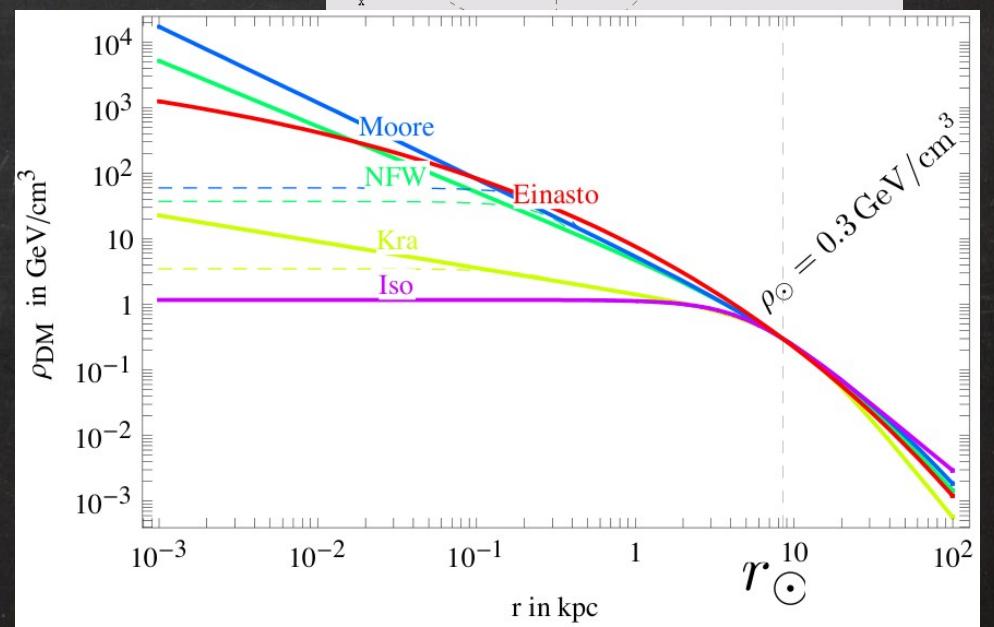
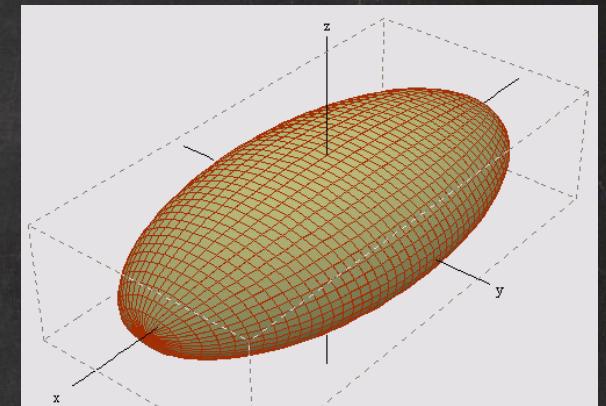
$$\rho(r) = \frac{4\rho_s}{r/r_s (1 + r/r_s)^2}$$

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$$\rho(r) = \rho_\odot \exp \left[ -\frac{2}{\alpha} \left( \left( \frac{r}{r_s} \right)^\alpha - \left( \frac{R_\odot}{r_s} \right)^\alpha \right) \right]$$

$$r_e^2 = x^2 + \left( \frac{y}{b/a} \right)^2 + \left( \frac{z}{c/a} \right)^2$$

$$a > b > c$$



# Bolshoi simulation

**Bolshoi** A. Klypin, S. Trujillo-Gómez & J. Primack '10

Publicly available through the MultiDark Database K. Riebe et al. '11

Cubic volume  $250 \text{ h}^{-1} \text{ Mpc}$ , sampled with  $2048^3$  particles

Mass of a simulation particle  $1.4 \cdot 10^8 \text{ h}^{-1} \text{ M}_\odot$

Cosmological parameters compatible with WMAP9

$$\Omega_m = 0.27, \Omega_\Lambda = 0.73, n_s = 0.95, h = 0.70, \sigma_8 = 0.82$$

DM only

DM halos fitted using NFW profile

Effects due to substructure (clumps) captured

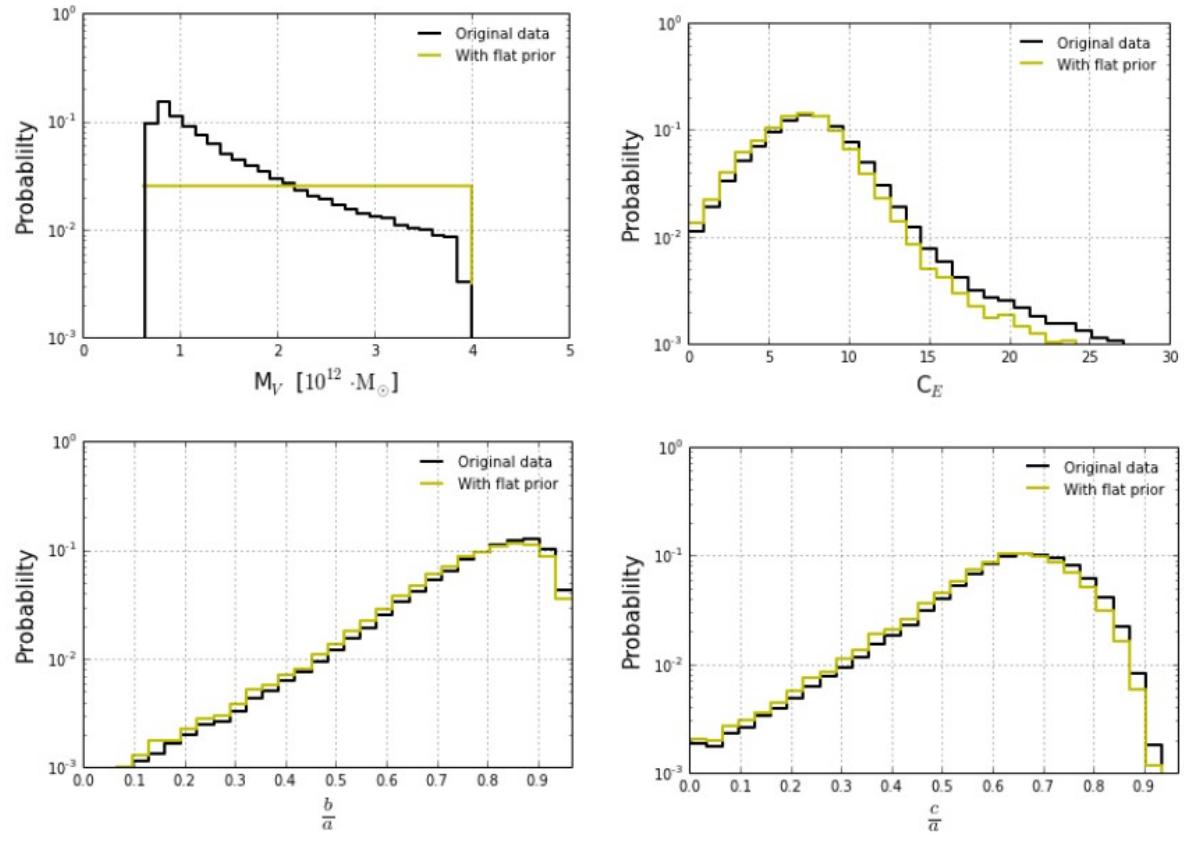
Collection of  $O(10^5)$  halos characterised by

Virial mass  $M_v$  (and/or virial radius)

Triaxial parameters  $b/a$  &  $c/a$

Concentration parameter  $C_E$

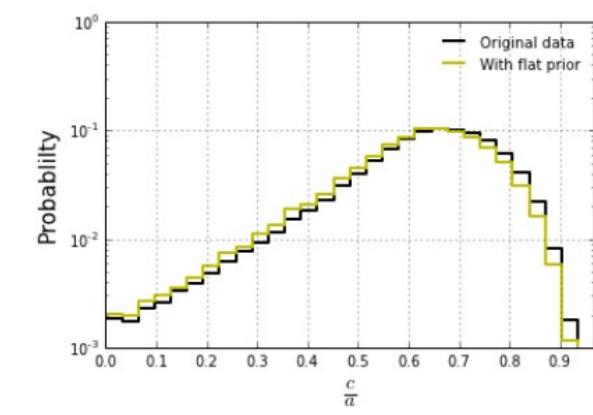
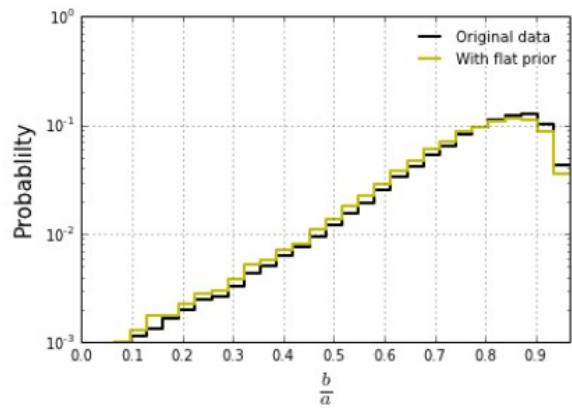
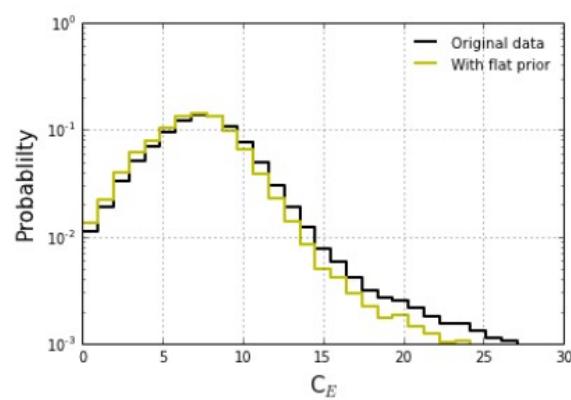
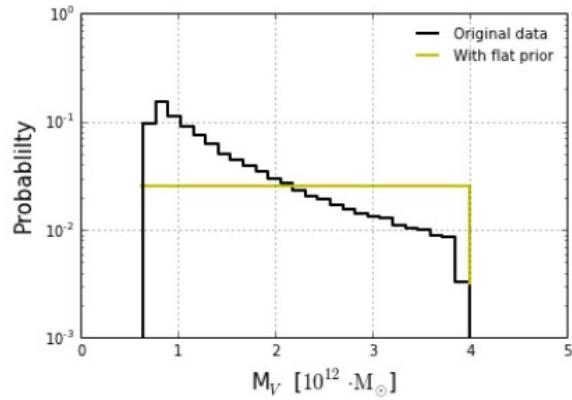
# Data set



$\sim 10^5$  DM only halos  
 $\langle M_V \rangle \sim 1.5 \cdot 10^{12} M_*$   
 $\langle C \rangle \sim 8.9$   
 $\langle b/a \rangle \sim 0.81$   
 $\langle c/a \rangle \sim 0.66$

Flat prior on  $M_V$  in order to avoid cosmological bias

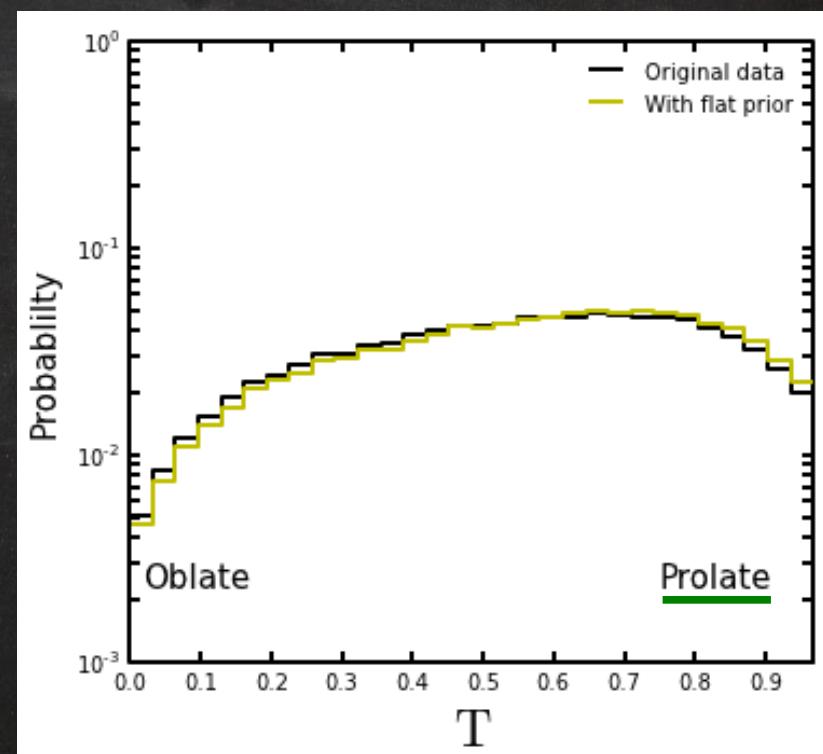
# Data set



Triaxiality parameter

$$T = \frac{1 - (b/a)^2}{1 - (c/a)^2} \quad \langle T \rangle \sim 0.58$$

$\sim 10^5$  DM only halos  
 $\langle M_V \rangle \sim 1.5 \cdot 10^{12} M_\ast$   
 $\langle C \rangle \sim 8.9$   
 $\langle b/a \rangle \sim 0.81$   
 $\langle c/a \rangle \sim 0.66$



# Impact of halo asphericity

~spherical

$$b/a = 0.96$$

$$c/a = 0.92$$

prolate

$$b/a = 0.58$$

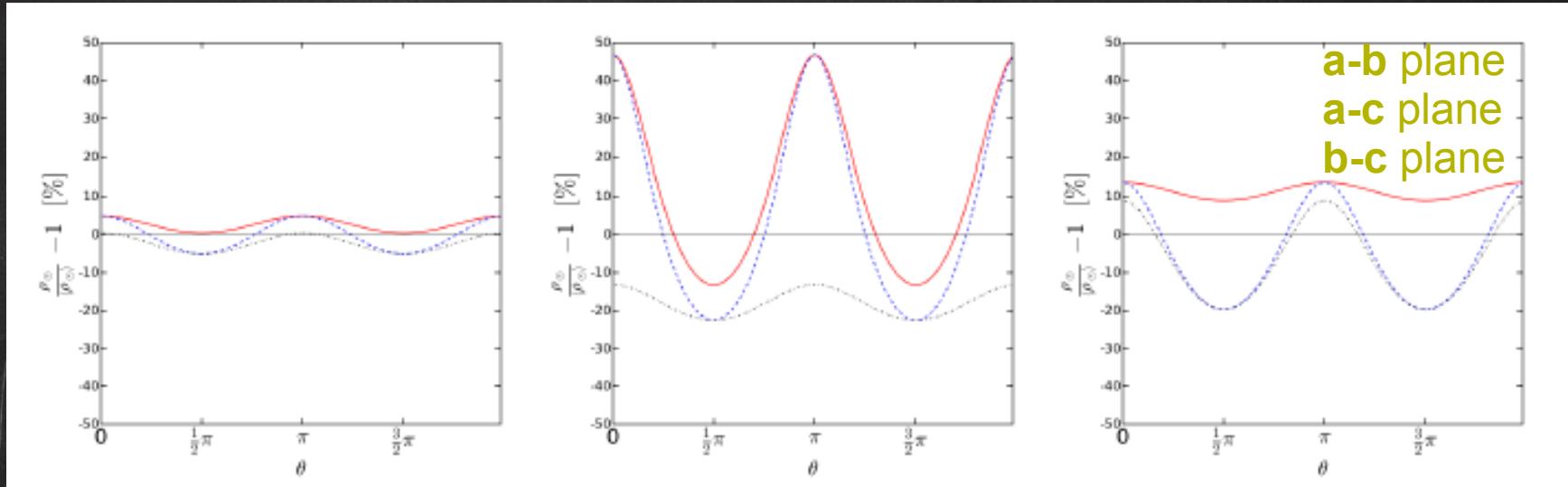
$$c/a = 0.48$$

oblate

$$b/a = 0.97$$

$$c/a = 0.77$$

$$\rho / \langle \rho \rangle - 1 \quad [\%]$$



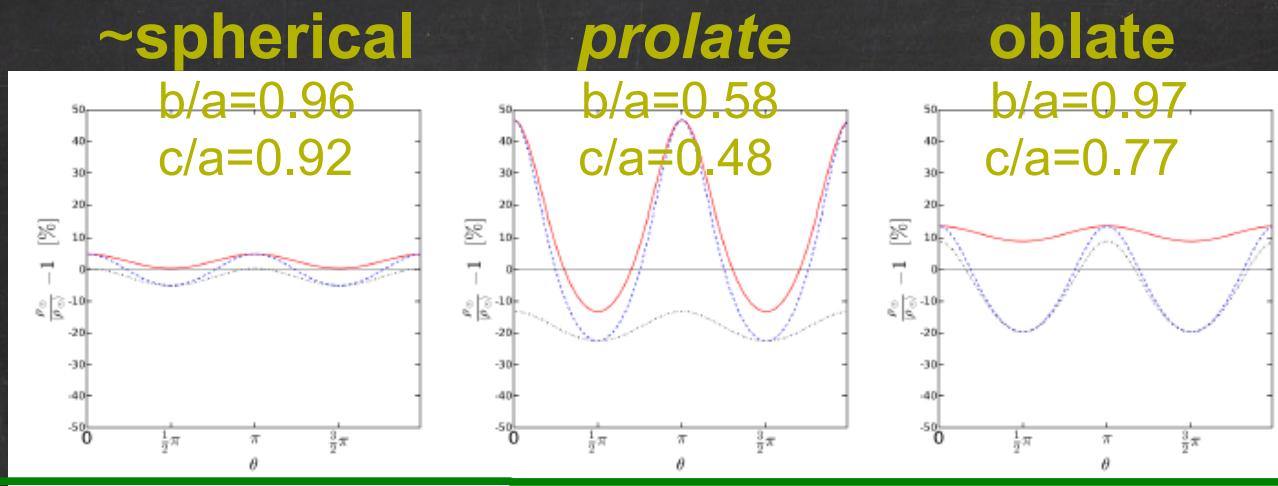
$\rho_0(\theta)$ : Local DM density at a given angle  $\theta$

$\langle \rho_0 \rangle$ : Spherically averaged local DM density

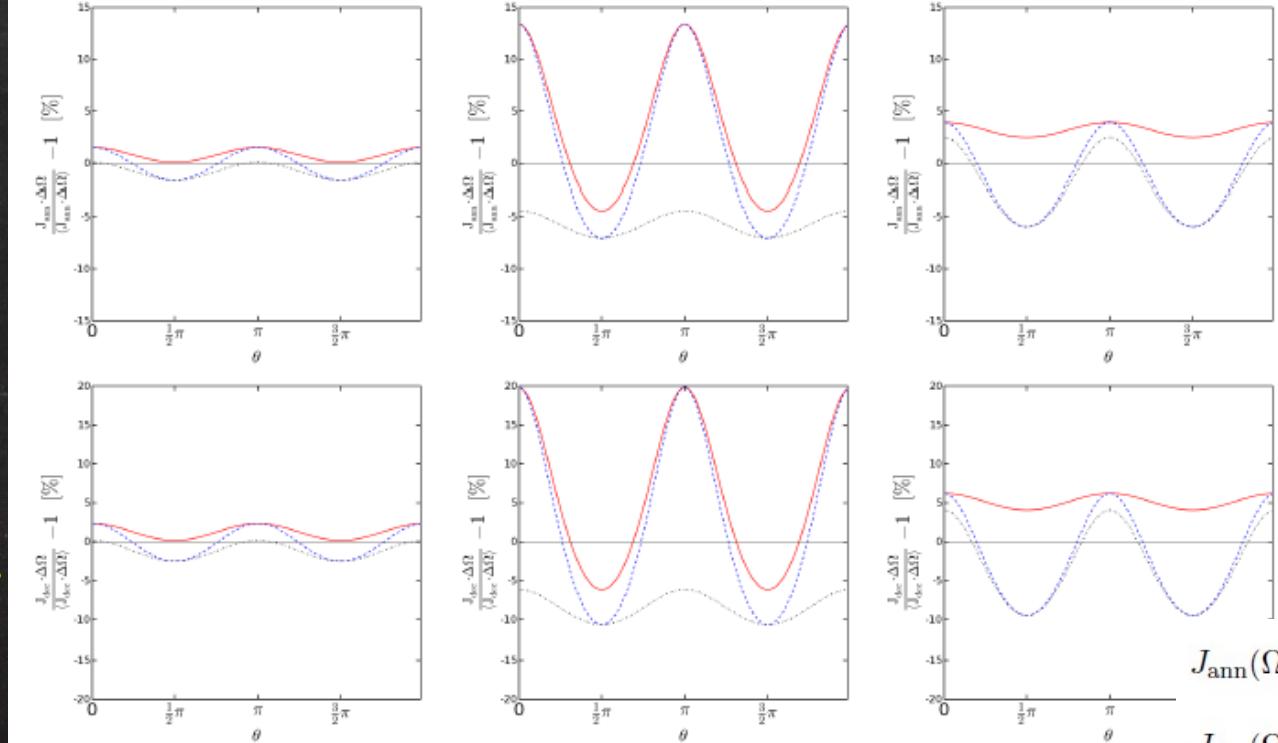
$\rho_0 / \langle \rho_0 \rangle - 1$ : Uncertainty induced by **triaxiality**

# Impact of halo asphericity

$\rho/\langle \rho \rangle - 1$   
[%]



$J/\langle J \rangle - 1$   
[%]



ROI =  $20^\circ \times 20^\circ$

$$J_{\text{ann}}(\Omega)\Delta\Omega = \int_{\Delta\Omega} d\Omega \int_{\text{los}} \rho(r(s, \Omega))^2 ds$$

$$J_{\text{dec}}(\Omega)\Delta\Omega = \int_{\Delta\Omega} d\Omega \int_{\text{los}} \rho(r(s, \Omega)) ds$$

# Observational priors

## Virial mass

Different methods like gravitational lensing, rotation curves, escape velocity, velocity dispersion profiles of some tracers...

Estimates based on stellar kinematics tend to yield  $\leq 10^{12} M_*$

distant tracers tend to yield  $\geq 10^{12} M_*$

$M_v$  is expected to lie within  $0.7 \cdot 10^{12} M_* < M_v < 4 \cdot 10^{12} M_*$

# Observational priors

## Virial mass

### Mass at 60 kpc

Total mass in the innermost 60 kpc  
Sloan Digital Sky Survey '08

$$M(<60 \text{ kpc}) = (4.0 \pm 0.7) \cdot 10^{11} M_{\odot}$$

# Observational priors

**Virial mass**

**Mass at 60 kpc**

**Local DM surface density**

$$\Sigma_{z_0}(R_\odot) \equiv \Sigma(R_\odot, |z| < z_0) = \int_{-z_0}^{+z_0} \rho(R_\odot, z) dz$$

$\Sigma(|z| < 1.1 \text{ kpc}) = (17 \pm 6) \text{ M}_* \text{ pc}^{-2}$  J. Bovy & HW. Rix '13

# Observational priors

**Virial mass**

**Mass at 60 kpc**

**Local DM surface density**

**Sun's galactocentric distance**

$$R_* = [7.5, 8.7] \text{ kpc}$$

# Observational priors

Virial mass

Mass at 60 kpc

Local DM surface density

Sun's galactocentric distance

Other dynamical constraints for the Milky Way:

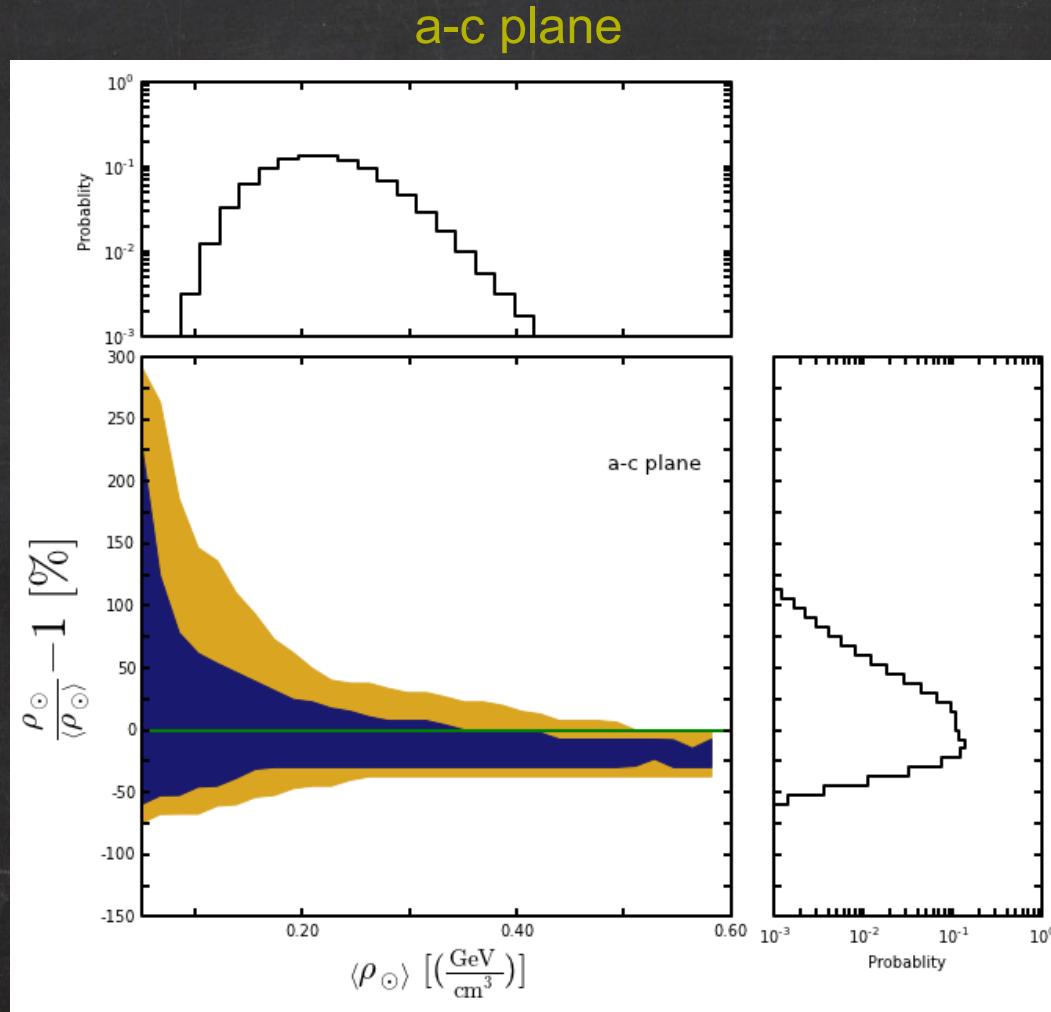
Terminal velocities,

velocity dispersions in a tracer population,

local circular velocities...

need a detailed **mass model for baryons** in the MW

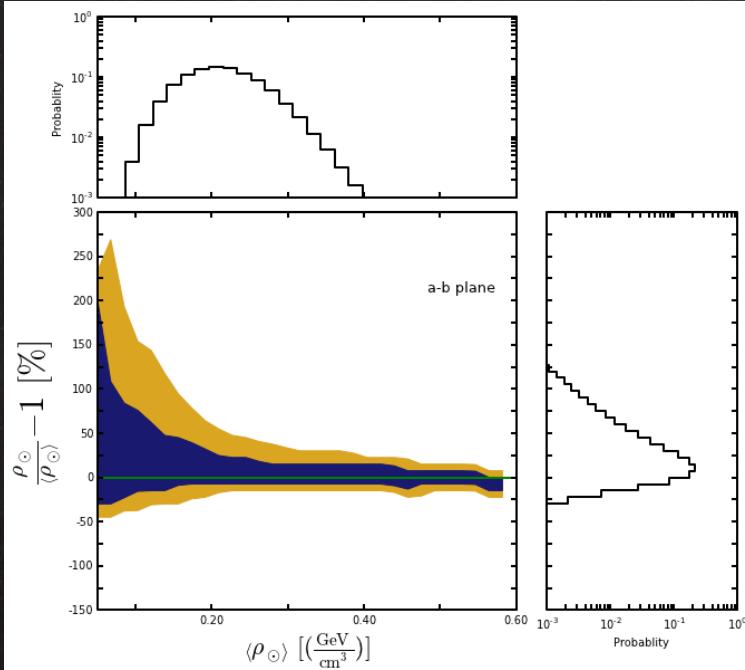
# Systematic uncertainties in $\rho_0$



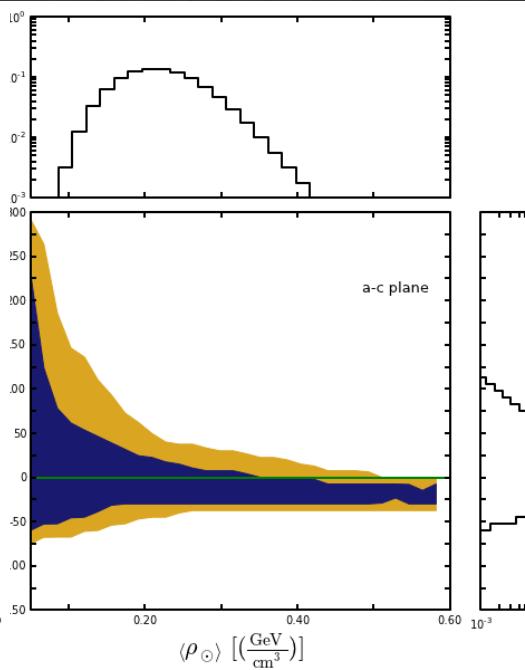
$\langle \rho_0 \rangle$ : Spherically averaged DM local density  
 $\rho_0 / \langle \rho_0 \rangle - 1$ : Uncertainty induced by triaxiality

# Systematic uncertainties in $\rho_0$

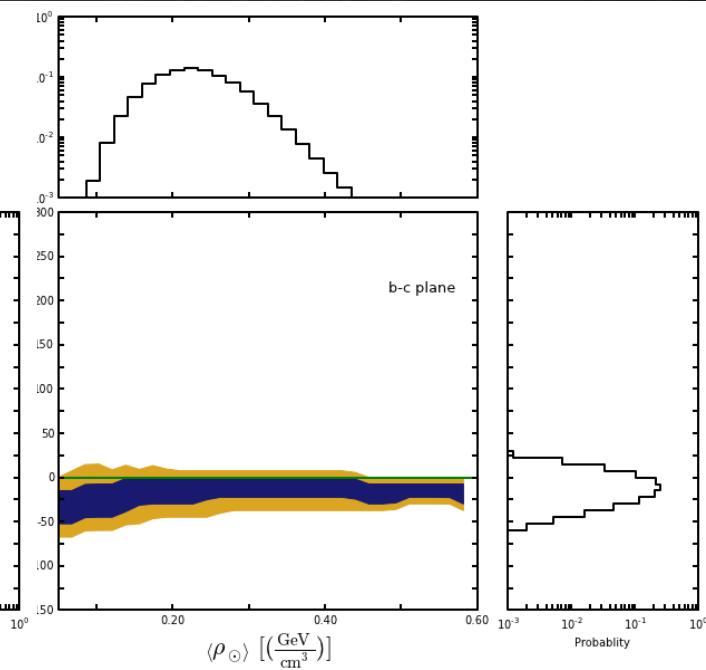
a-b plane



a-c plane



b-c plane

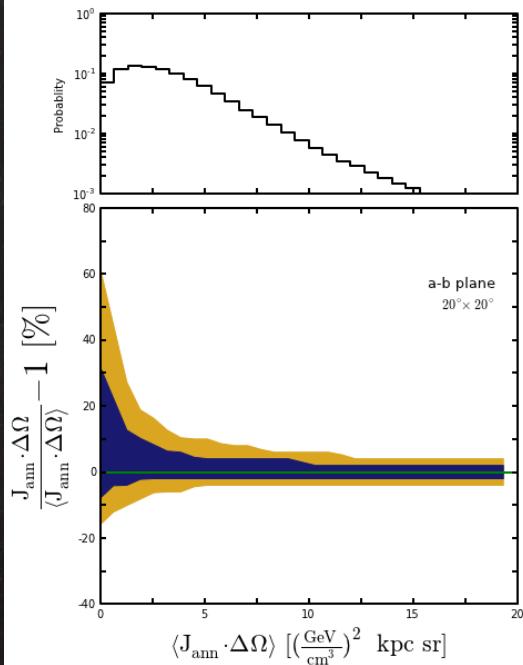


If  $\langle \rho_0 \rangle \sim 0.3 \text{ GeV/cm}^3$

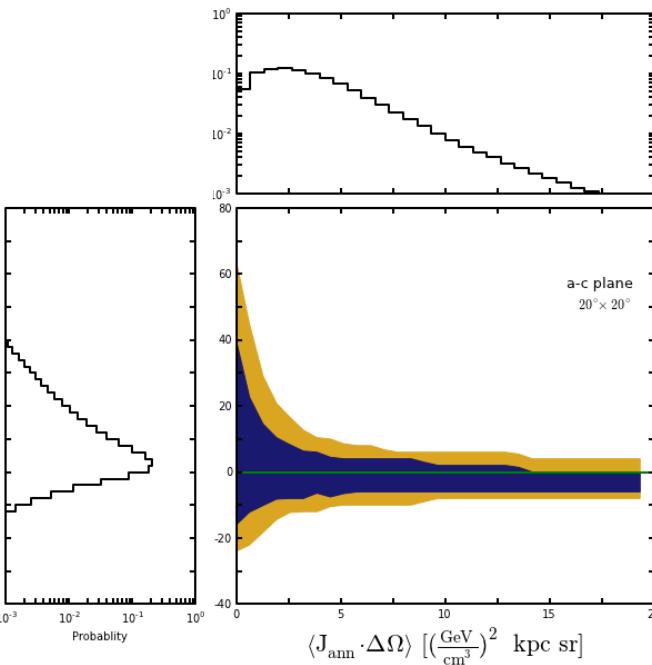
the uncertainty  $\sim 40\%$  @ 95% CL

# Systematic uncertainties in $\mathbf{J} \cdot \Delta\Omega$ Annihilation

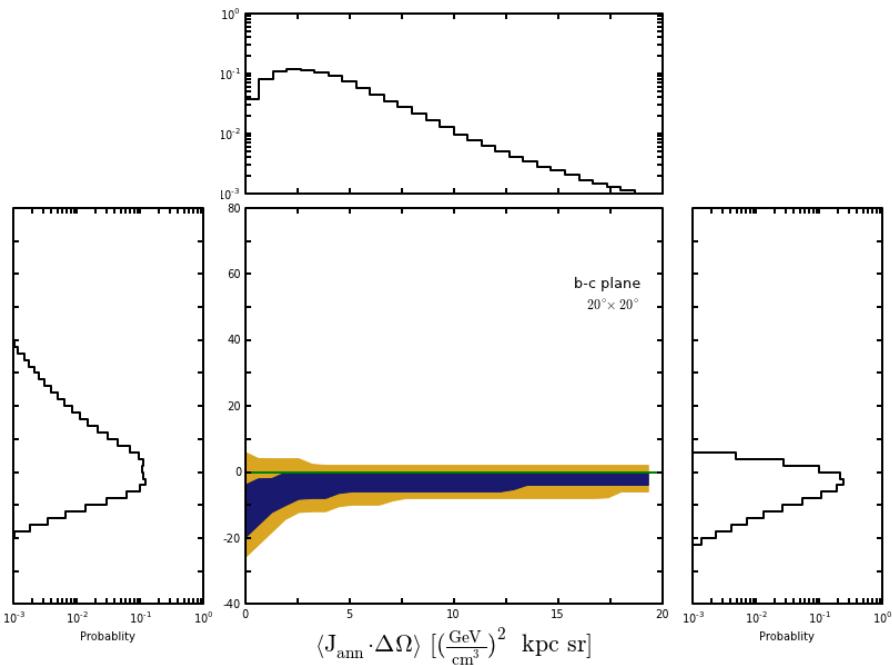
a-b plane



a-c plane



b-c plane

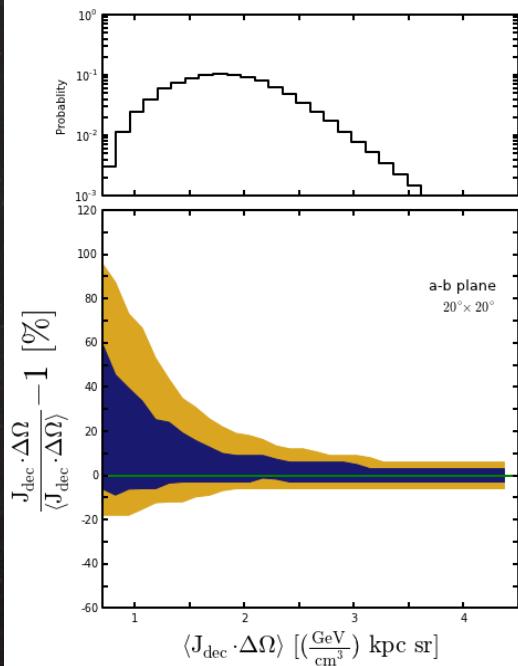


$\langle \mathbf{J}_{\text{ann}} \cdot \Delta\Omega \rangle \sim 14 \text{ (GeV/cm}^3)^2 \text{ kpc sr}$   
 ROI =  $20^\circ \times 20^\circ$  around the GC

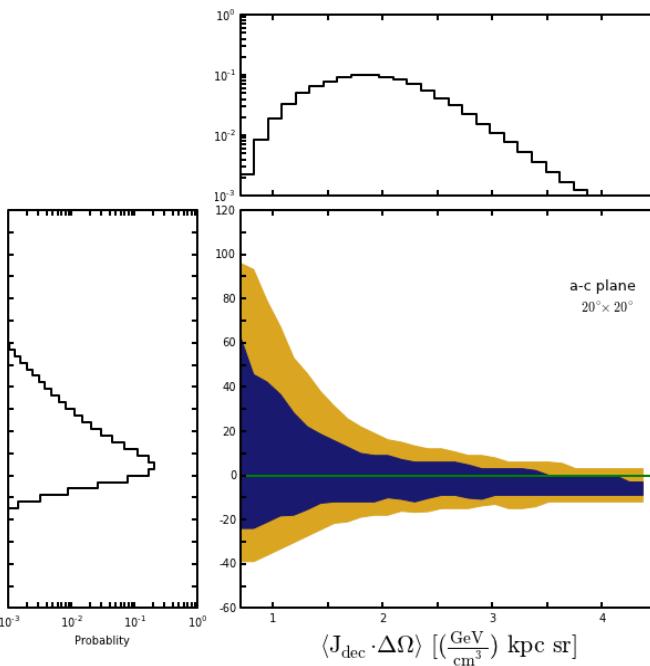
uncertainty  $\sim 9\%$  @ 95% CL

# Systematic uncertainties in $\mathbf{J} \cdot \Delta\Omega$ Decay

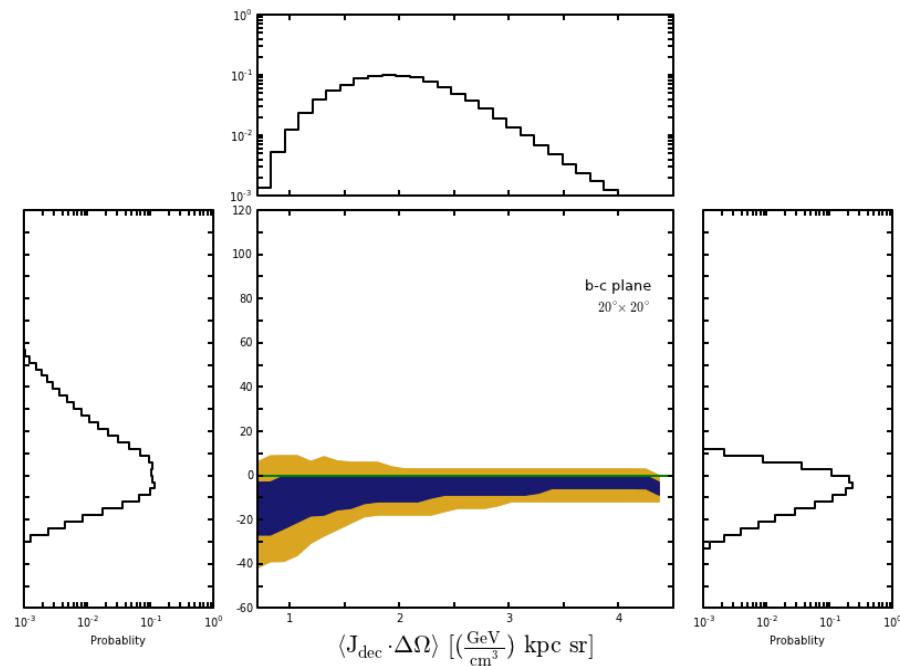
a-b plane



a-c plane



b-c plane



$\langle \mathbf{J}_{\text{dec}} \cdot \Delta\Omega \rangle \sim 3.5 \text{ GeV/cm}^3 \text{ kpc sr}$

uncertainty  $\sim 15\% @ 95\% \text{ CL}$

ROI =  $20^\circ \times 20^\circ$  around the GC

# Conclusions

- \* In order to extract particle physics parameters ( $m_x$ ,  $\sigma$ ,  $\langle \sigma v \rangle$ ) from DM experiments, the astrophysics has to be under control.
- \* N-body simulations predicts triaxial DM halos. Spherical halos are rare!
- \* Using the DM only N-body simulation *Bolshoi* we studied the systematic uncertainties in  $\rho_0$  and  $J \cdot \Delta\Omega$  due to the halo asphericity.
- \* We took into account observational priors ( $M_v$ ,  $M_{60}$ , SD...) in order to make the halos more Milky way like.
- \* **For a standard NFW, deviations for  $\rho_0 \sim 0.3\text{-}0.4 \text{ GeV/cm}^3$ : ~40%.**  
 $J_{\text{ann}} \cdot \Delta\Omega \sim 9\% \text{ (annihilation)}$   
 $J_{\text{dec}} \cdot \Delta\Omega \sim 15\% \text{ (decay)} @ 95\% \text{ CL}$  ROI =  $20^\circ \times 20^\circ$  around the GC
- \* Non negligible effect for DM detection!
- \* For J-factors, uncertainty on the different profiles!