

Planck 2014

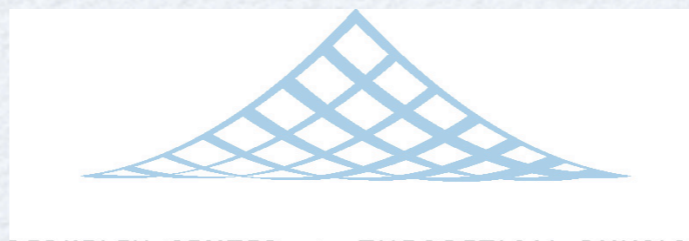
*Paris*

May 2014

# Dark Matter from The Multiverse: SUSY and Axions

Lawrence Hall

University of California, Berkeley



BERKELEY CENTER FOR THEORETICAL PHYSICS

# Two Surprises of Last 35 Years

- 1998      A Recent Cosmic Acceleration
- 2012      A Lonely Higgs Boson

Both are connected to fine-tuning

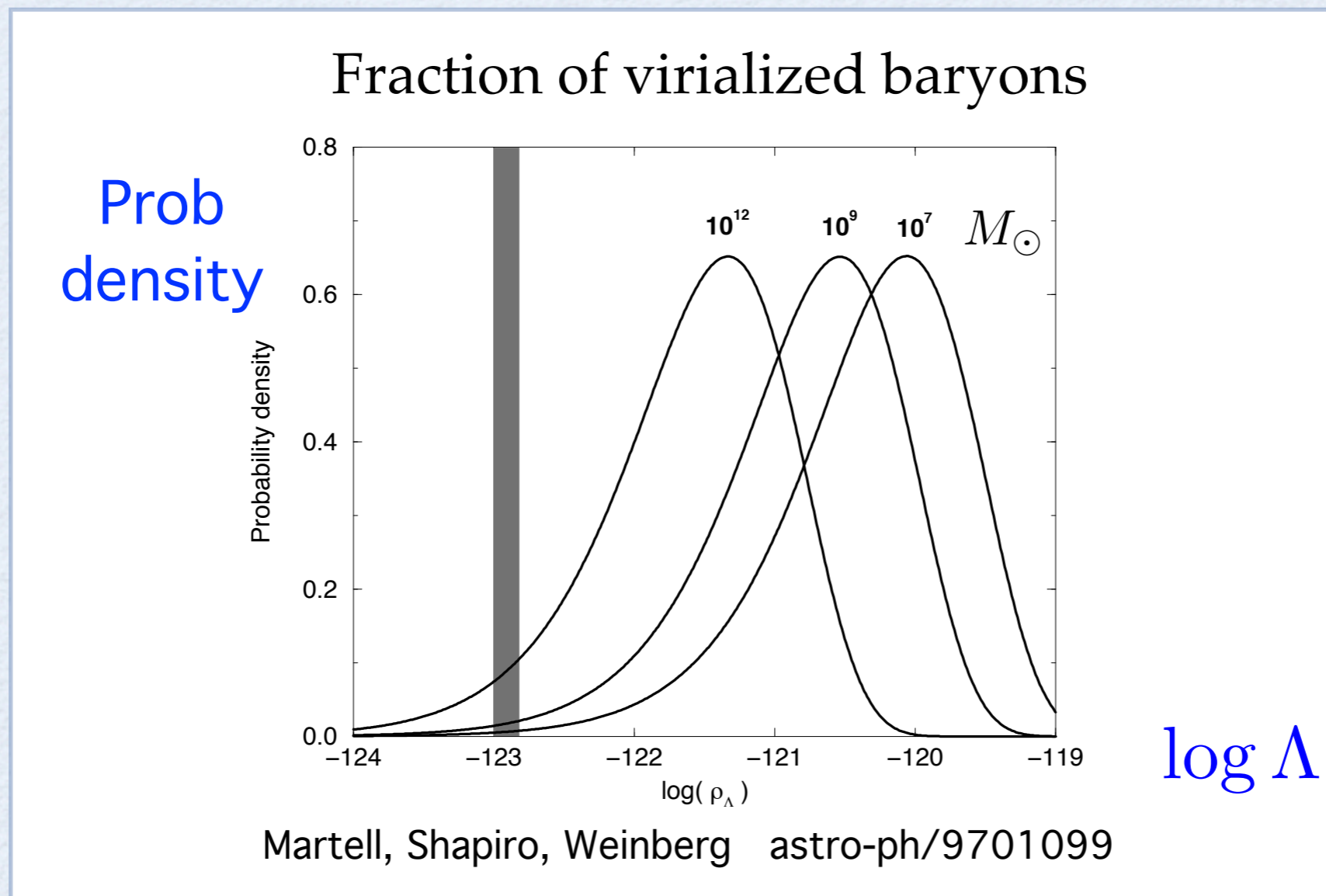
Both have a multiverse interpretation

Review the “Standard” Multiverse Interpretation

# 1. Dark Energy 1998

Predicted from multiverse view: Weinberg, 1987

Vary only the cosmological constant,  $\Lambda$



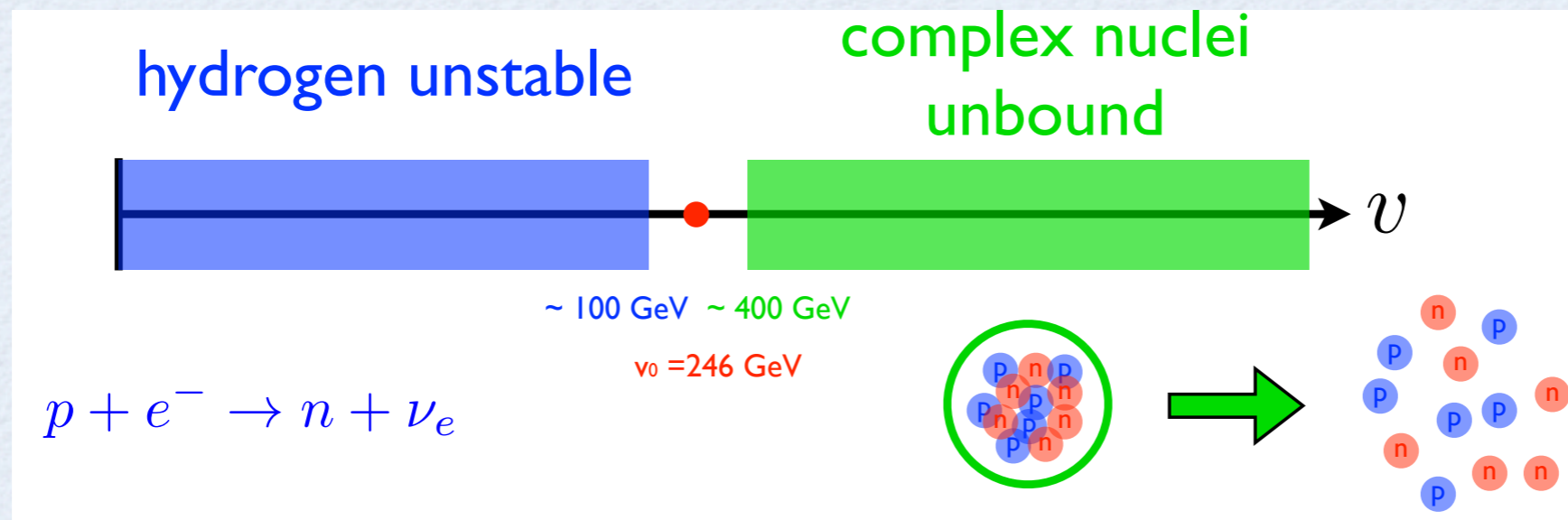
# 2. A Lonely Higgs Boson 2012

and nothing else for  
EWSB at TeV scale ??

Predicted

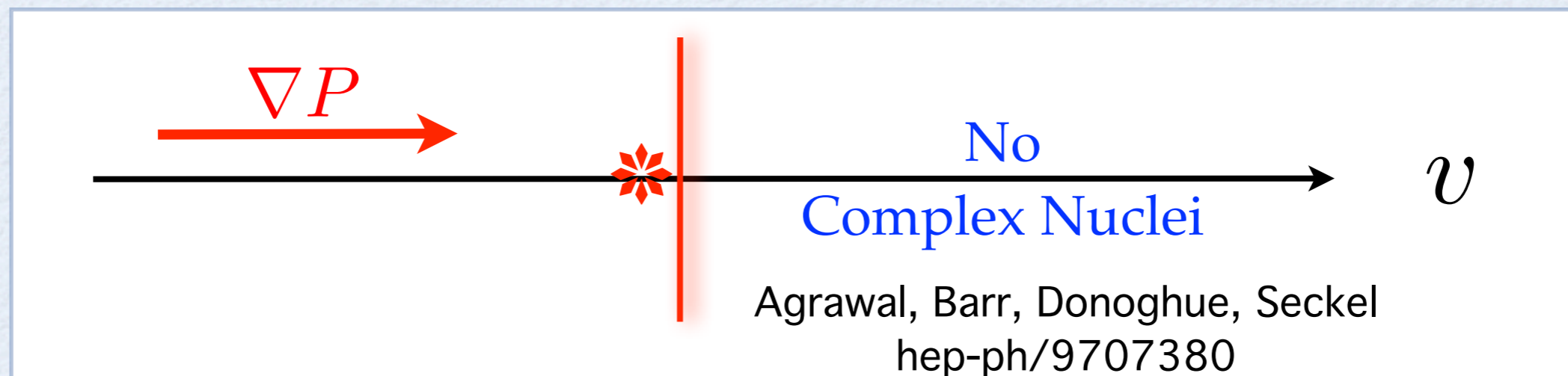
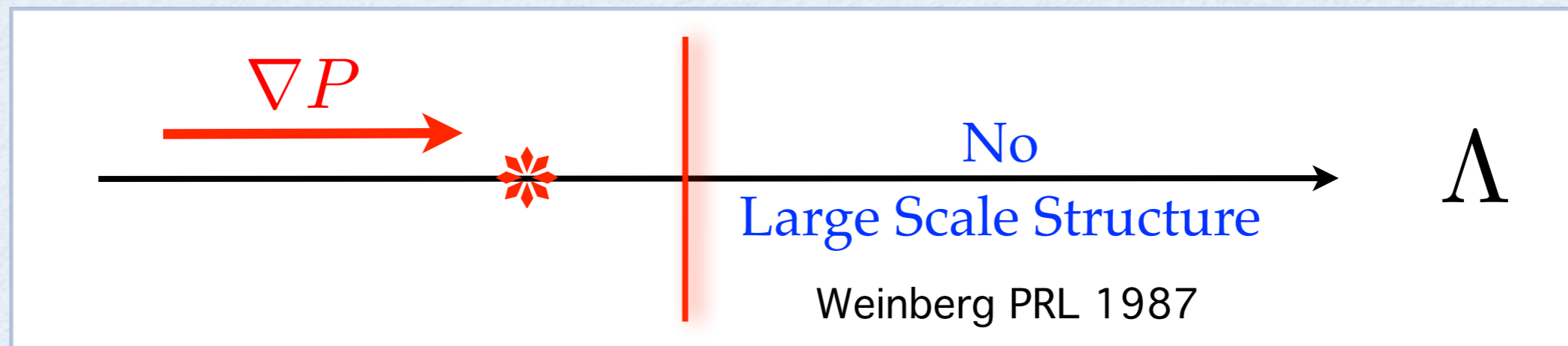
Agrawal, Barr, Donoghue, Seckel hep-ph/9707380

Damour, Donoghue arXiv:0712.2968



# Multiverse for $\Lambda$ and $\nu$

The two surprises have a common interpretation



# Just Imagine ...

1.  $\Omega_m = 0.99 \pm 0.02$

2.  $\pi_T, \rho_T, \dots$  at LEP, TeVatron, LHC

# Just Imagine ...

1.  $\Omega_m = 0.99 \pm 0.02$

2.  $\pi_T, \rho_T, \dots$  at LEP, TeVatron, LHC

- Data is telling us that Nature is fine-tuned
- The Multiverse provides a simple explanation

# Outline

1. An Alternative Multiverse explanation for  $(\Lambda, v)$
2. Scanning the Dark Matter Abundance
3. Implications: Susy  
Axions
4. A Model for the Axion and Higgs Mass



(I)

An Alternative Explanation for

$(\Lambda, v)$

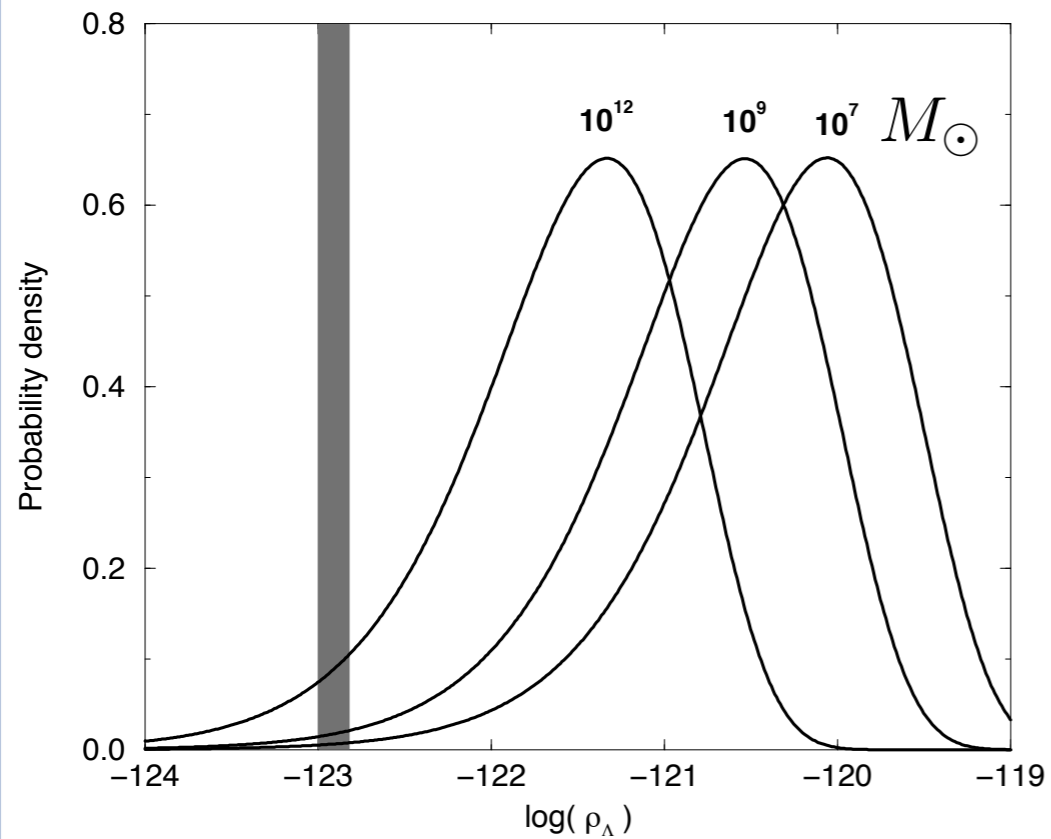
# $\Lambda$ from the Measure

## Stars in the Causal Patch

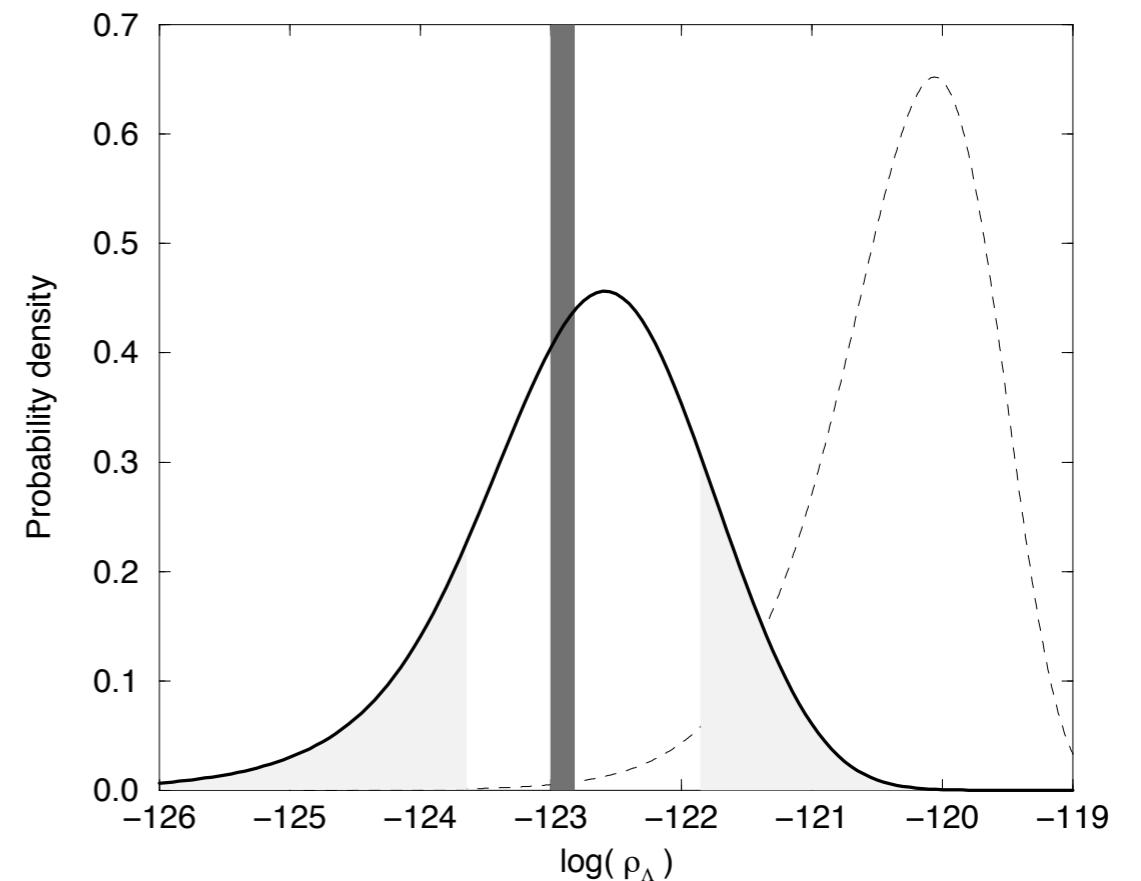
$$t_{\Lambda} \sim t_{obs}$$

$$\Lambda \sim \frac{1}{G t_{obs}^2}$$

## Fraction of virialized baryons



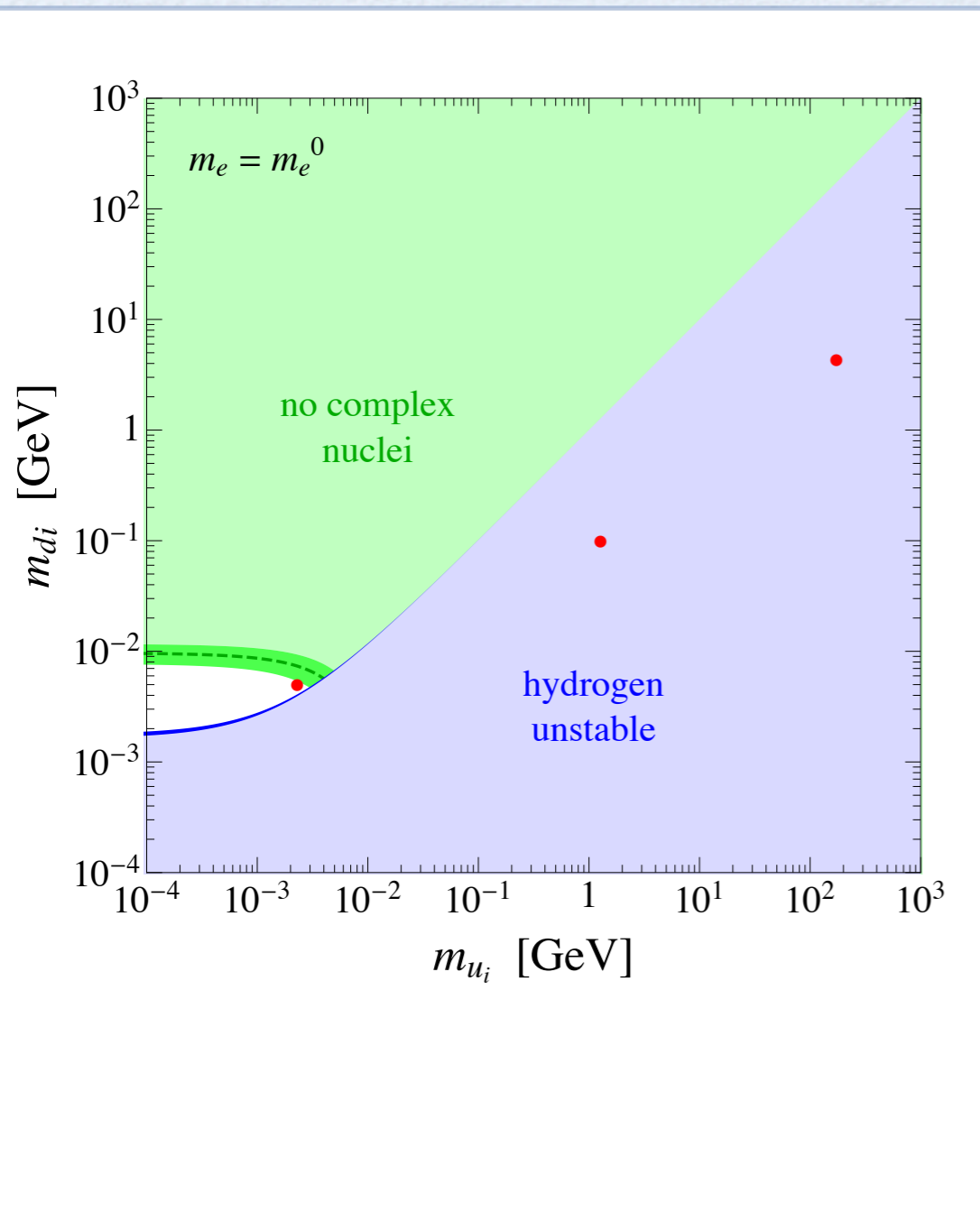
Martell, Shapiro, Weinberg [astro-ph/9701099](https://arxiv.org/abs/astro-ph/9701099)



Bousso, Harnik, Kribs, Perez [hep-th/0702115](https://arxiv.org/abs/hep-th/0702115)

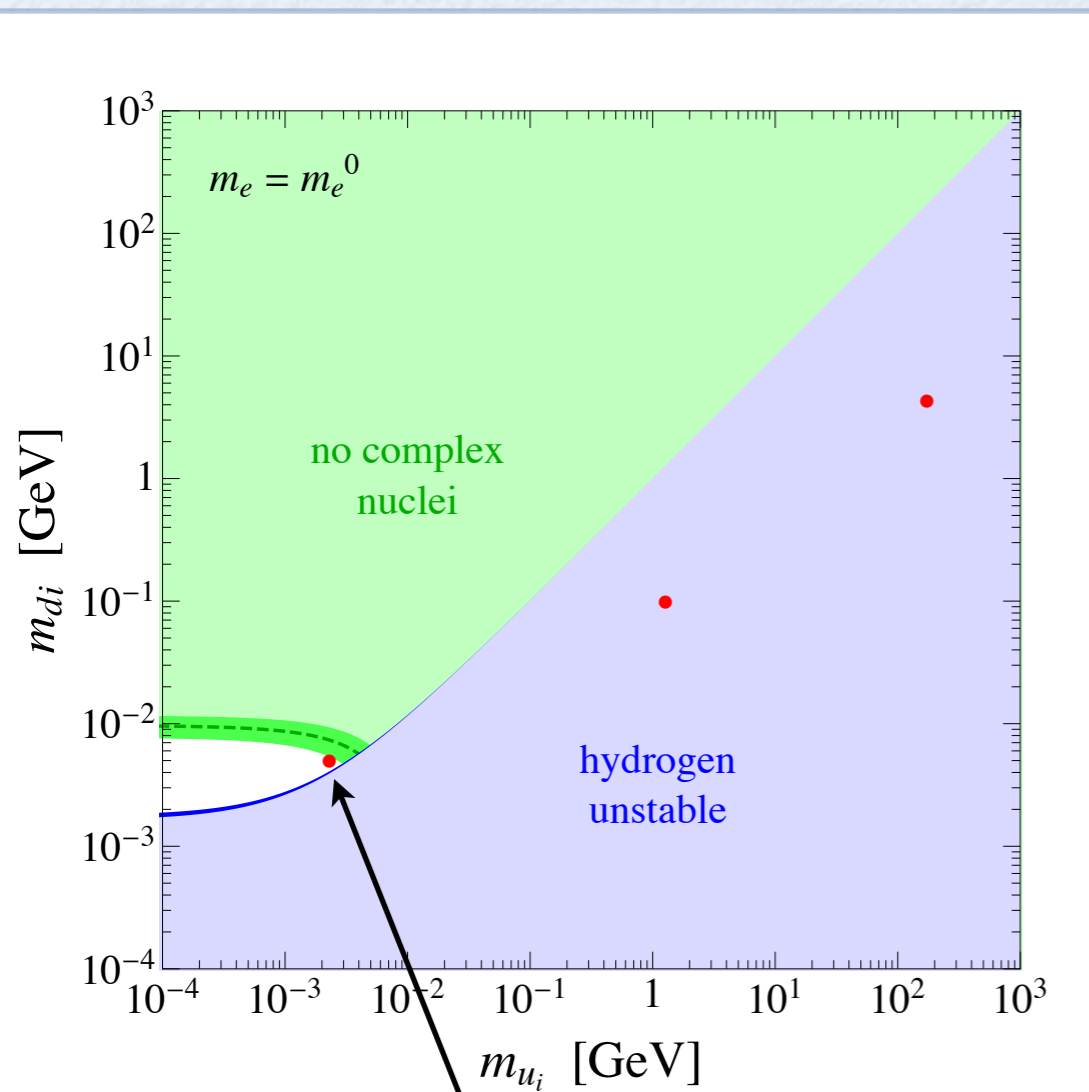
# Nuclear Boundaries: Determine $m_{u,d}$

Hall, Pinner, Ruderman; to appear



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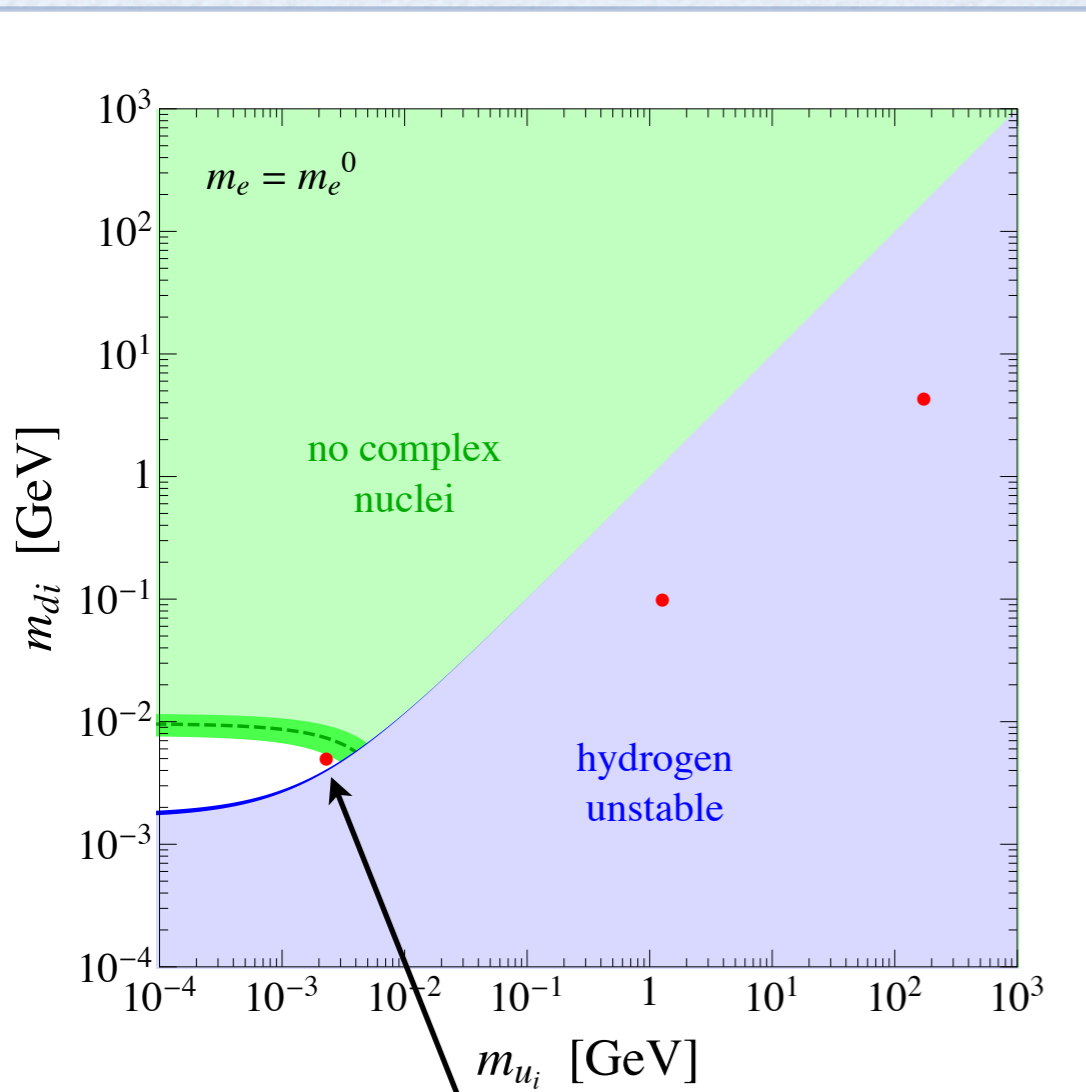
Hall, Pinner, Ruderman; to appear



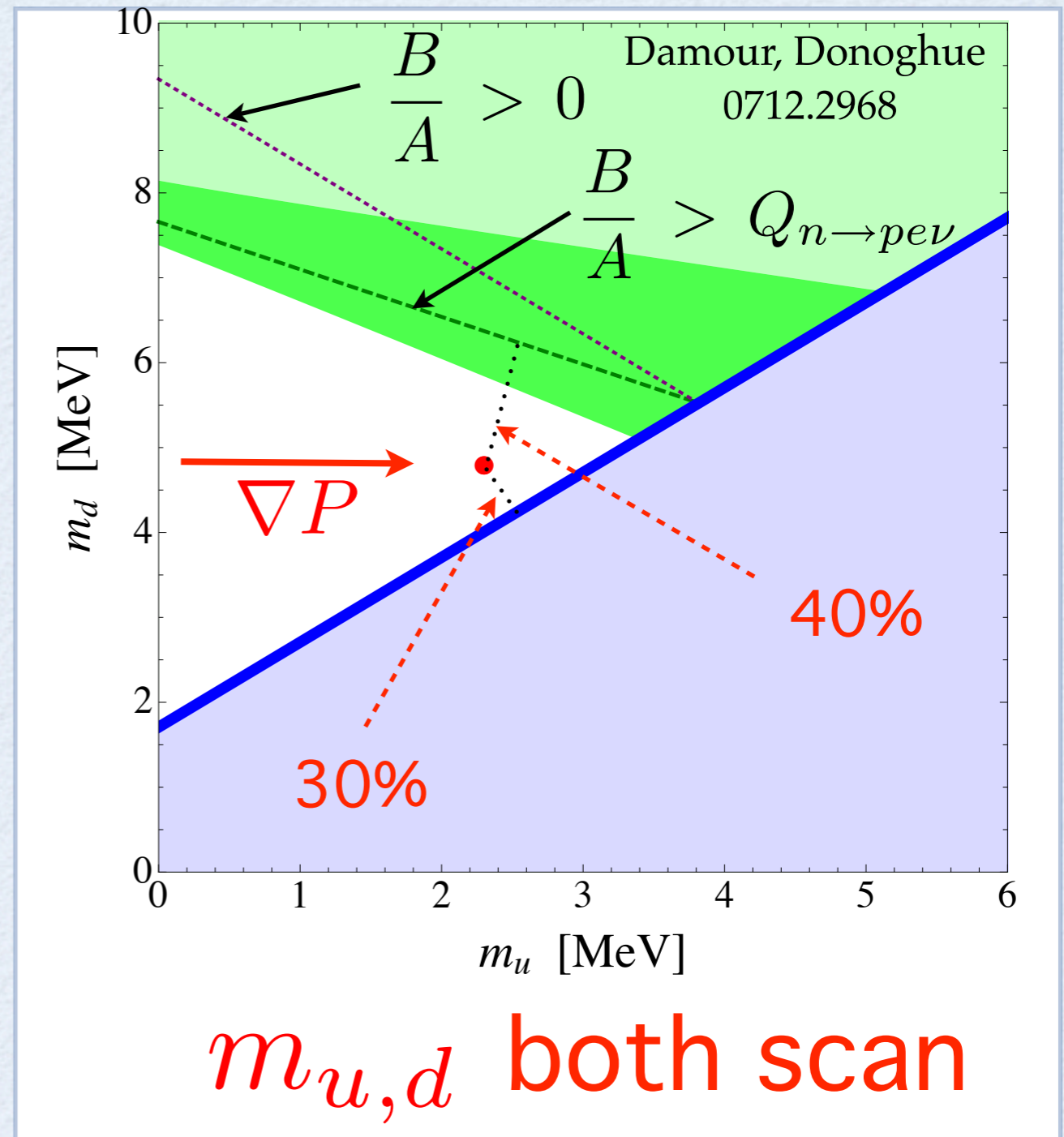
**Tip of the Cone!**

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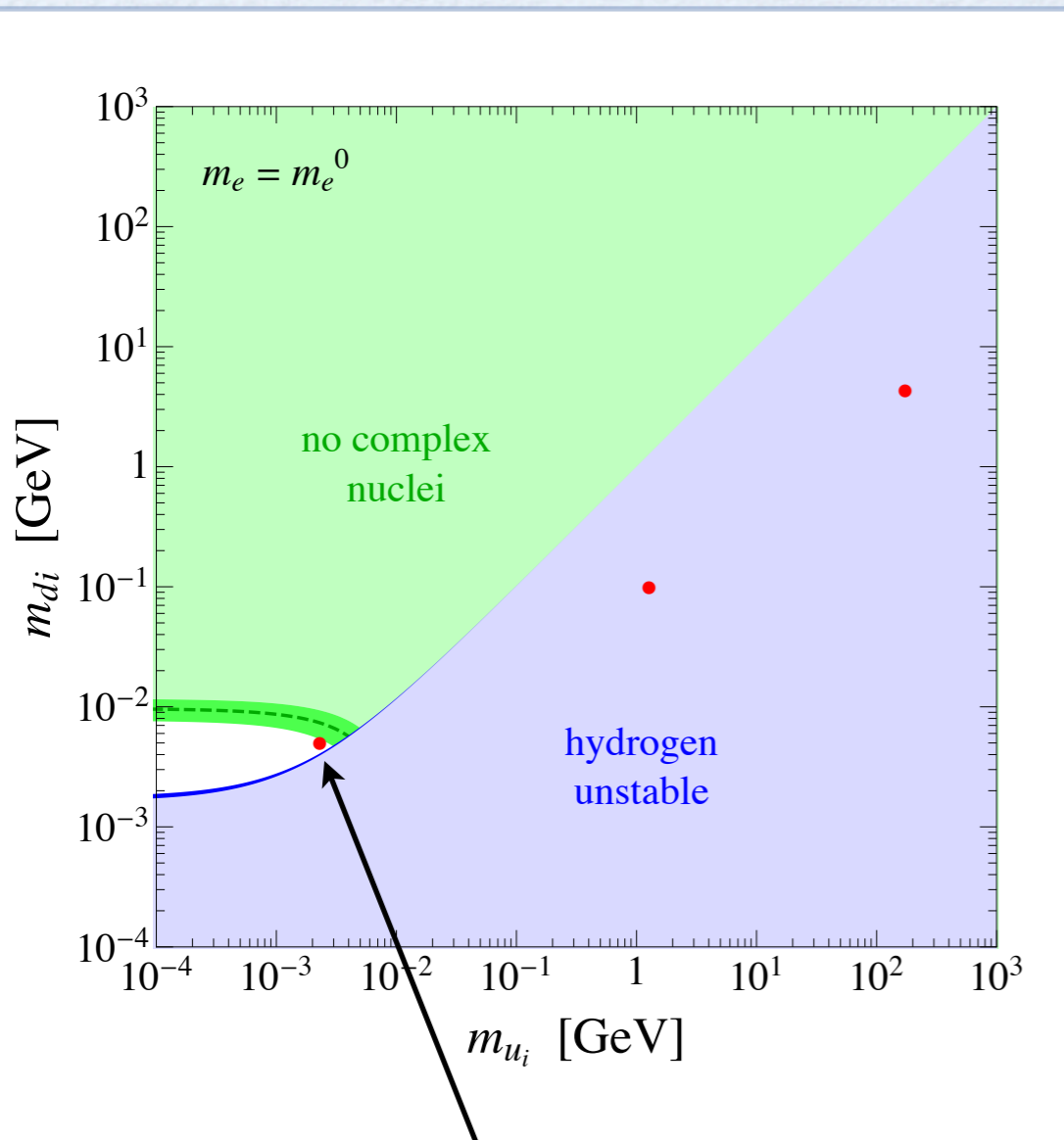


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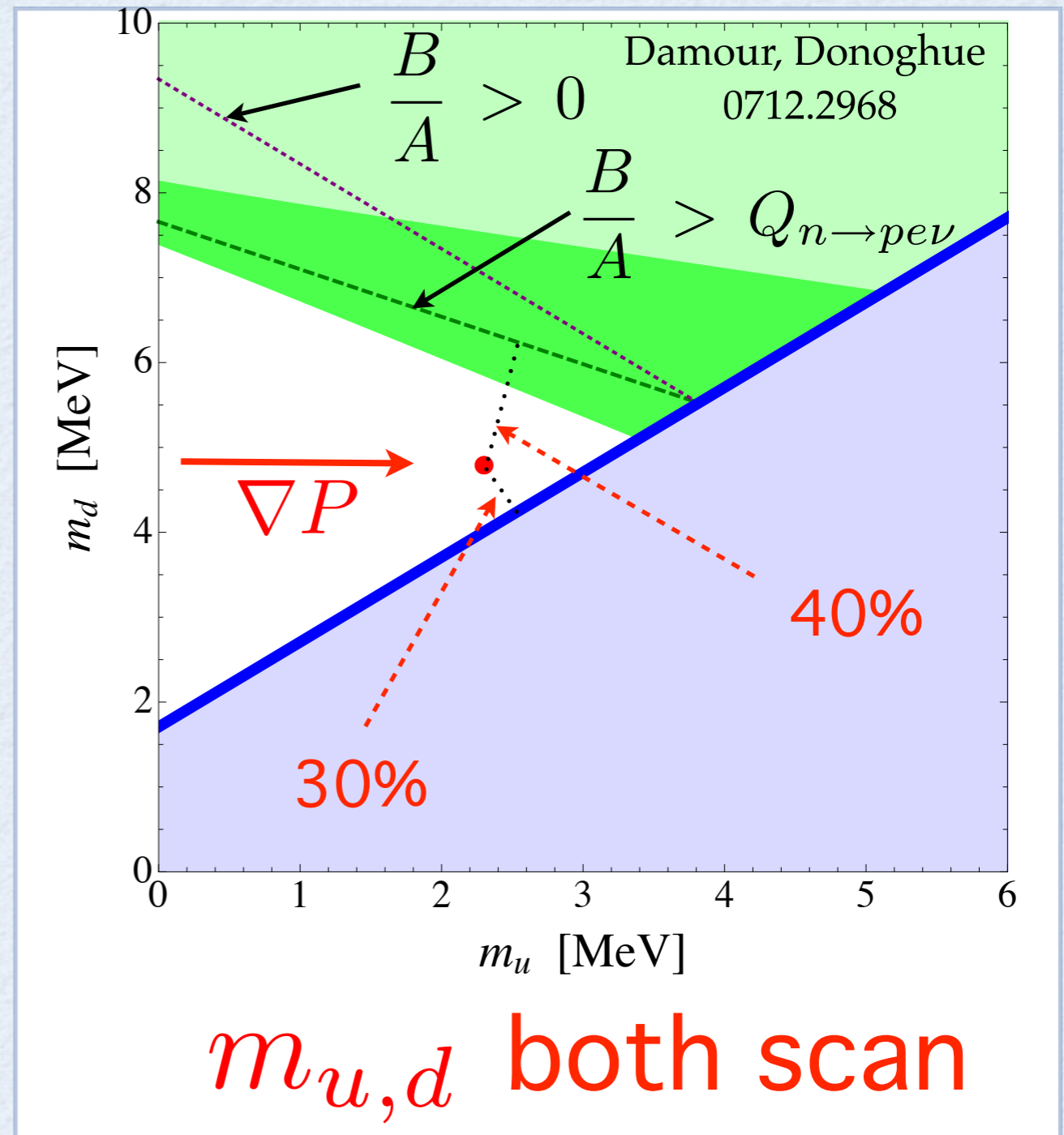


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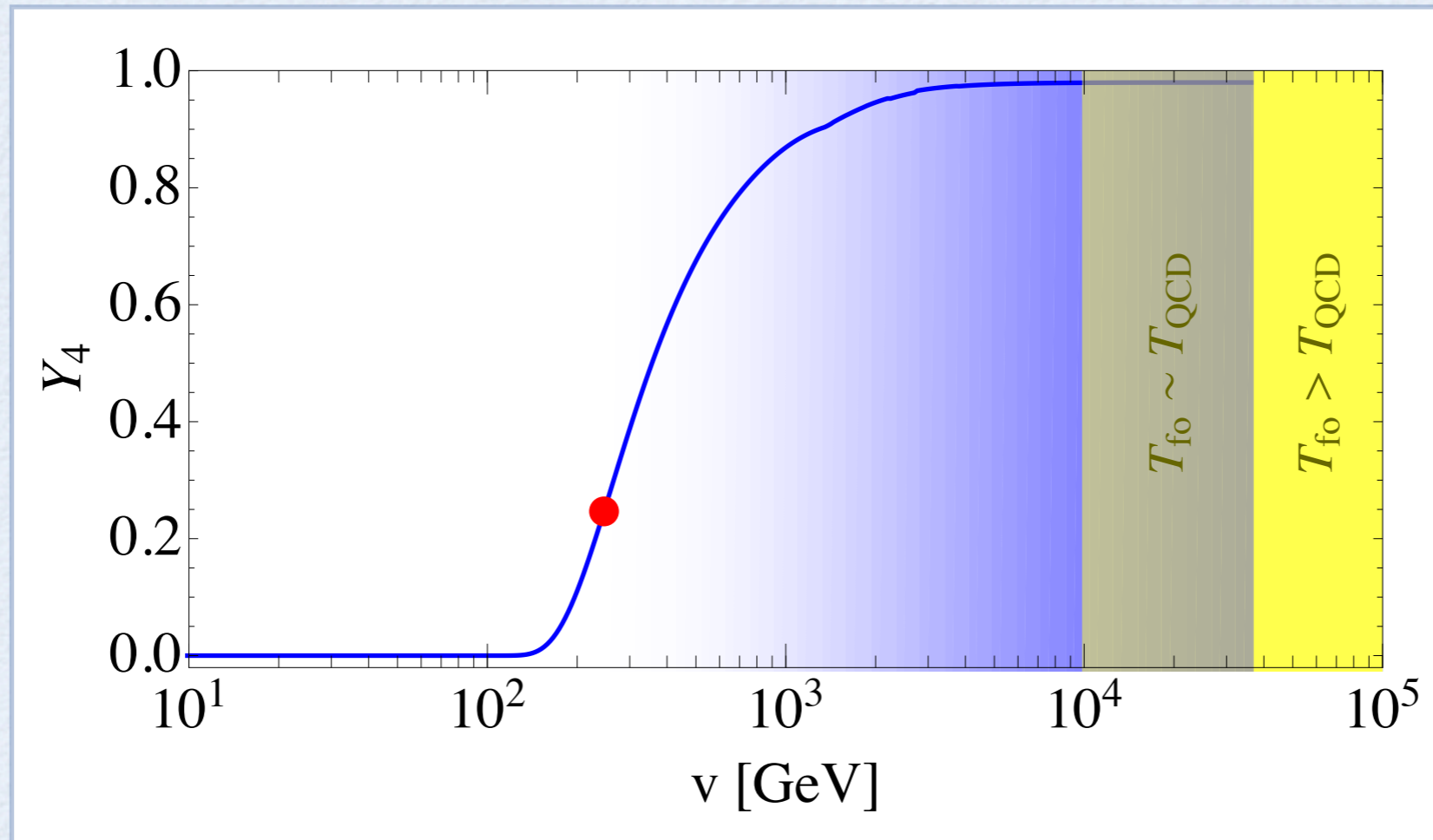
Tip of the Cone!



What determines  $\nu$  ?

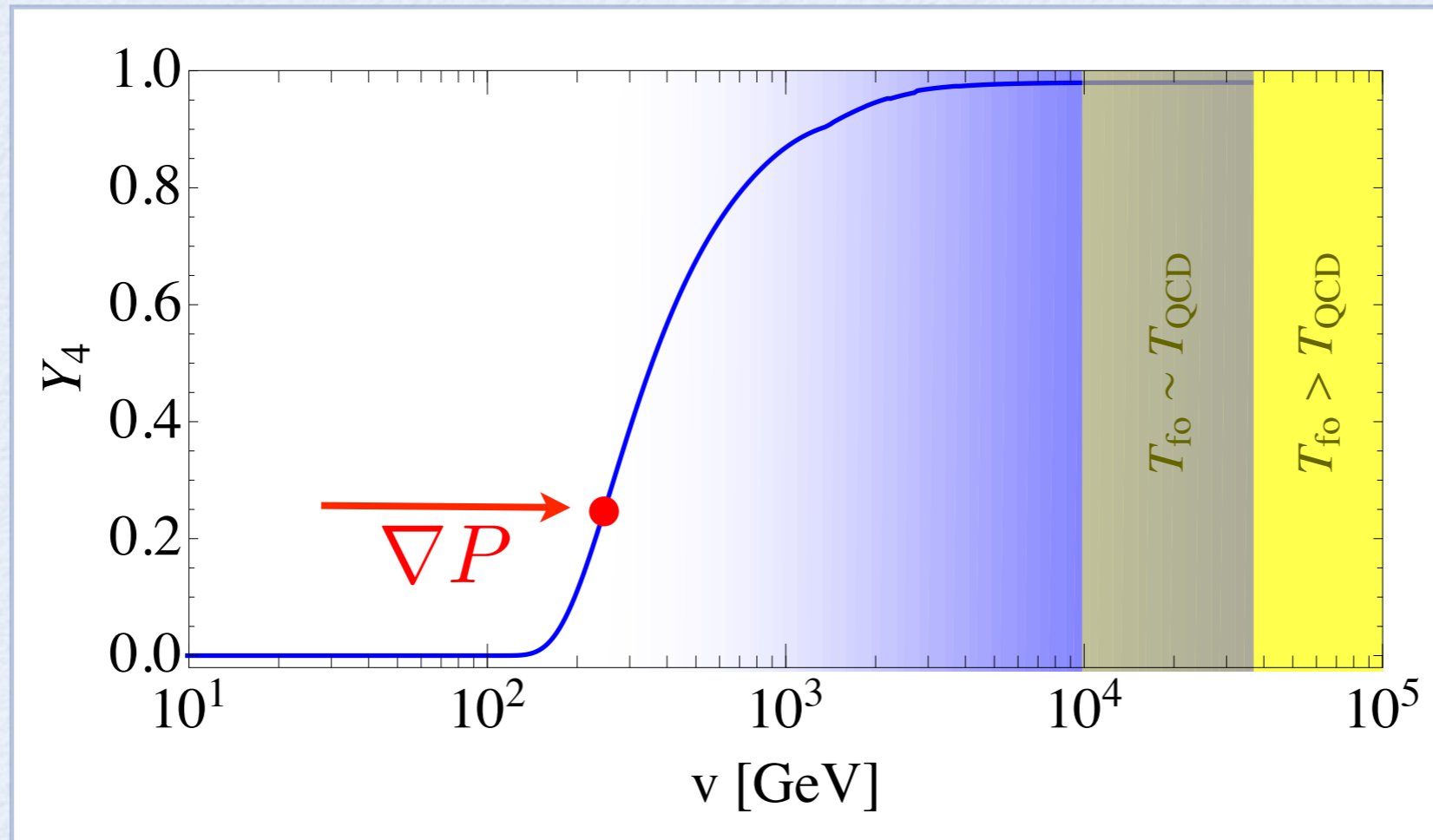
# $v$ from the Helium Boundary

Hall, Pinner, Ruderman; to appear



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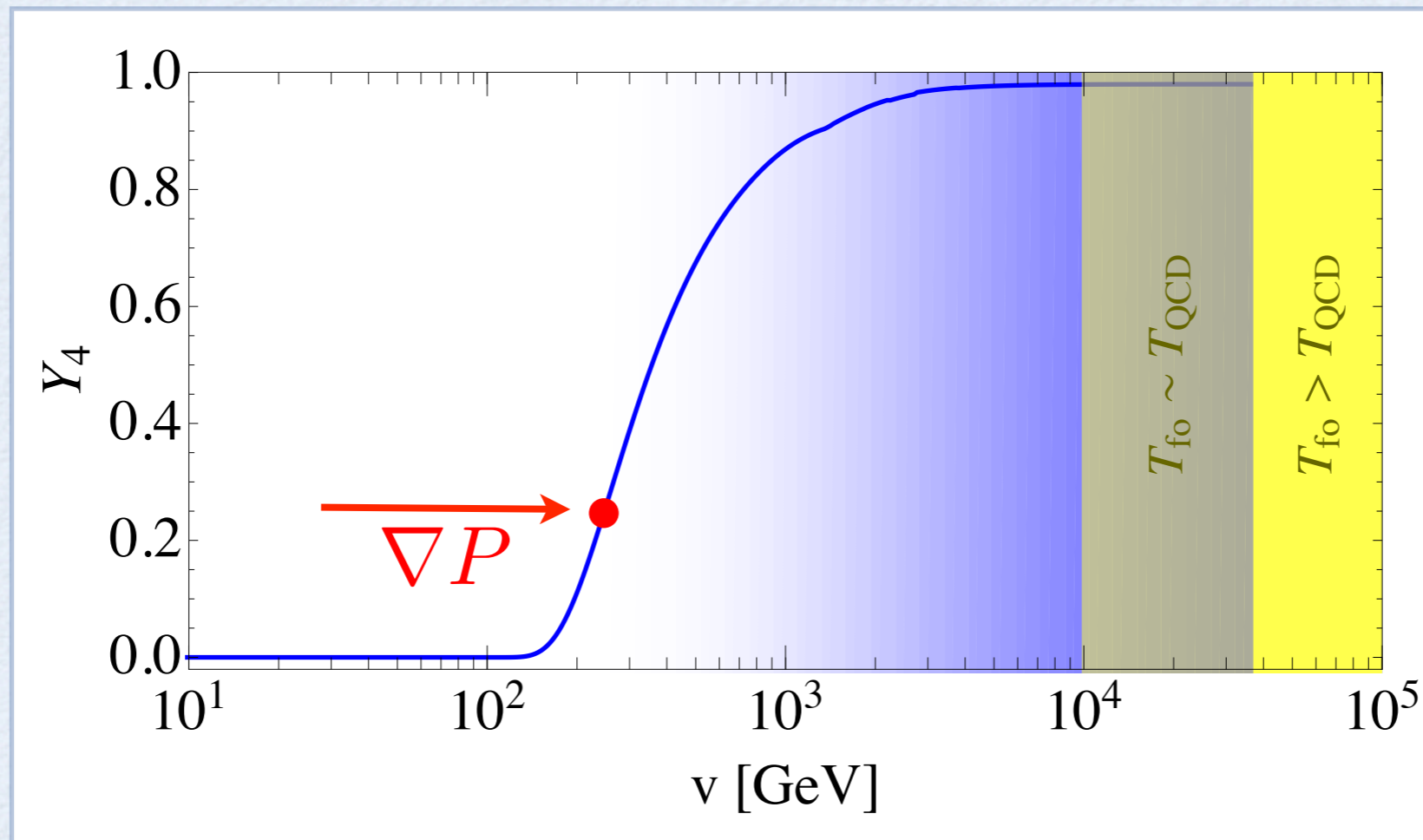
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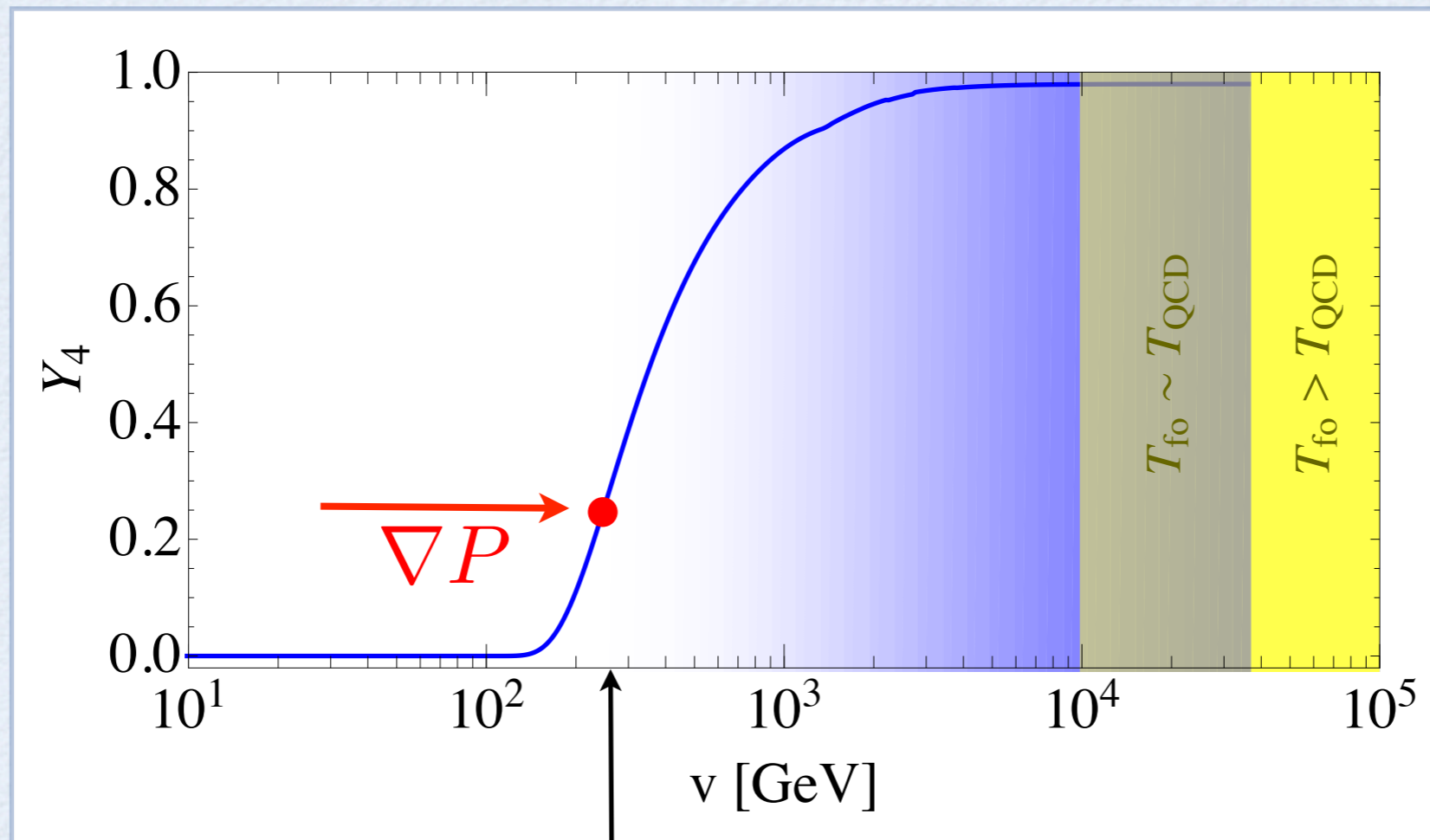


$$\left(\frac{n}{p}\right)_f \sim e^{-(m_n - m_p)/T_{np}}$$

$\swarrow$   $\frac{v^{4/3}}{M_{Pl}^{1/3}}$

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Hall, Pinner, Ruderman; to appear



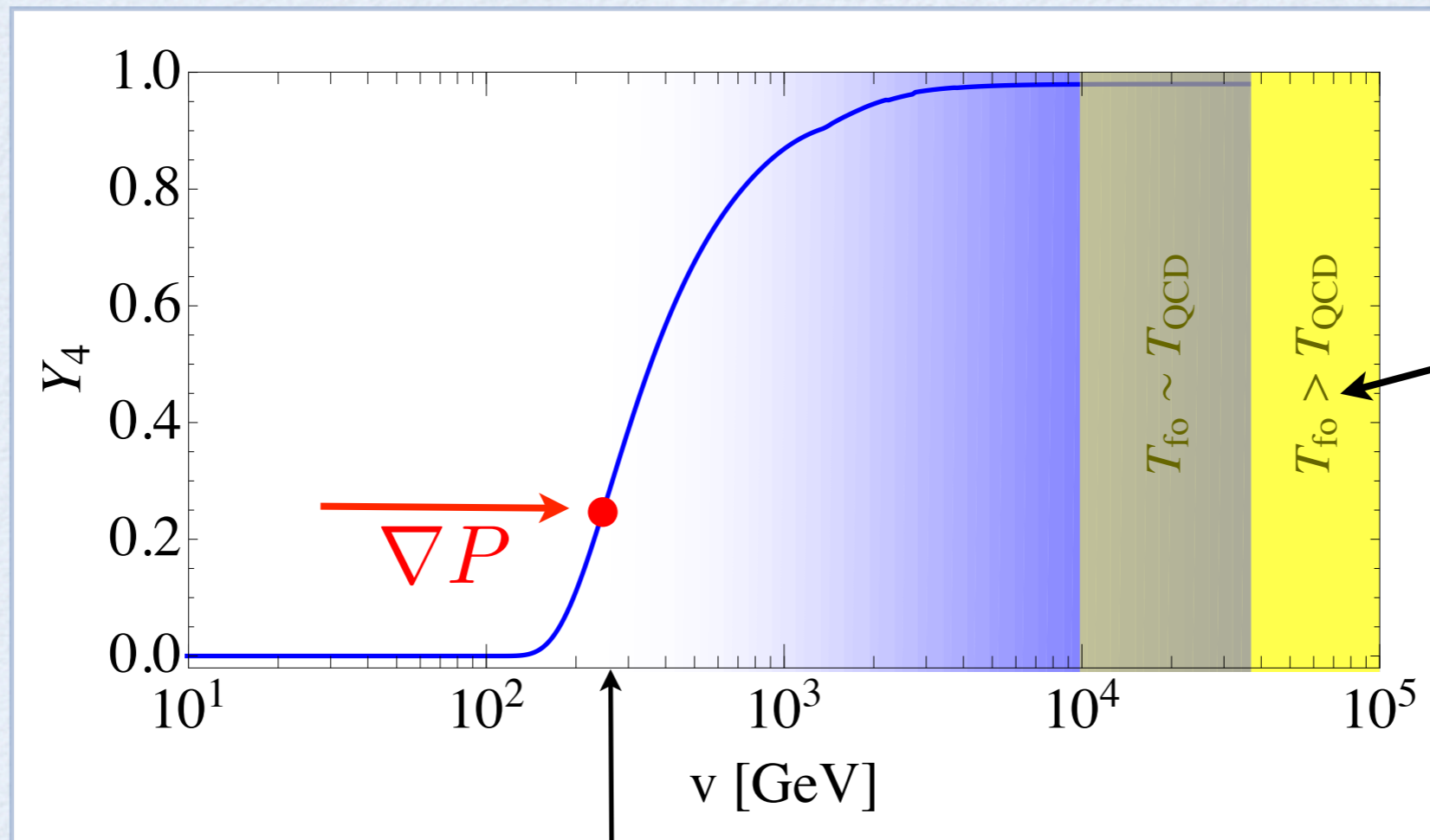
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$$\frac{v}{M_{Pl}} \sim 10^{-2} \left(\frac{\Lambda_{QCD}}{M_{Pl}}\right)^{3/4}$$

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(II)

Scanning the  
Dark Matter Abundance

Francesco D'Eramo, Lawrence Hall, Duccio Pappadopulo  
to appear

# Large Scale Structure: Varying DM

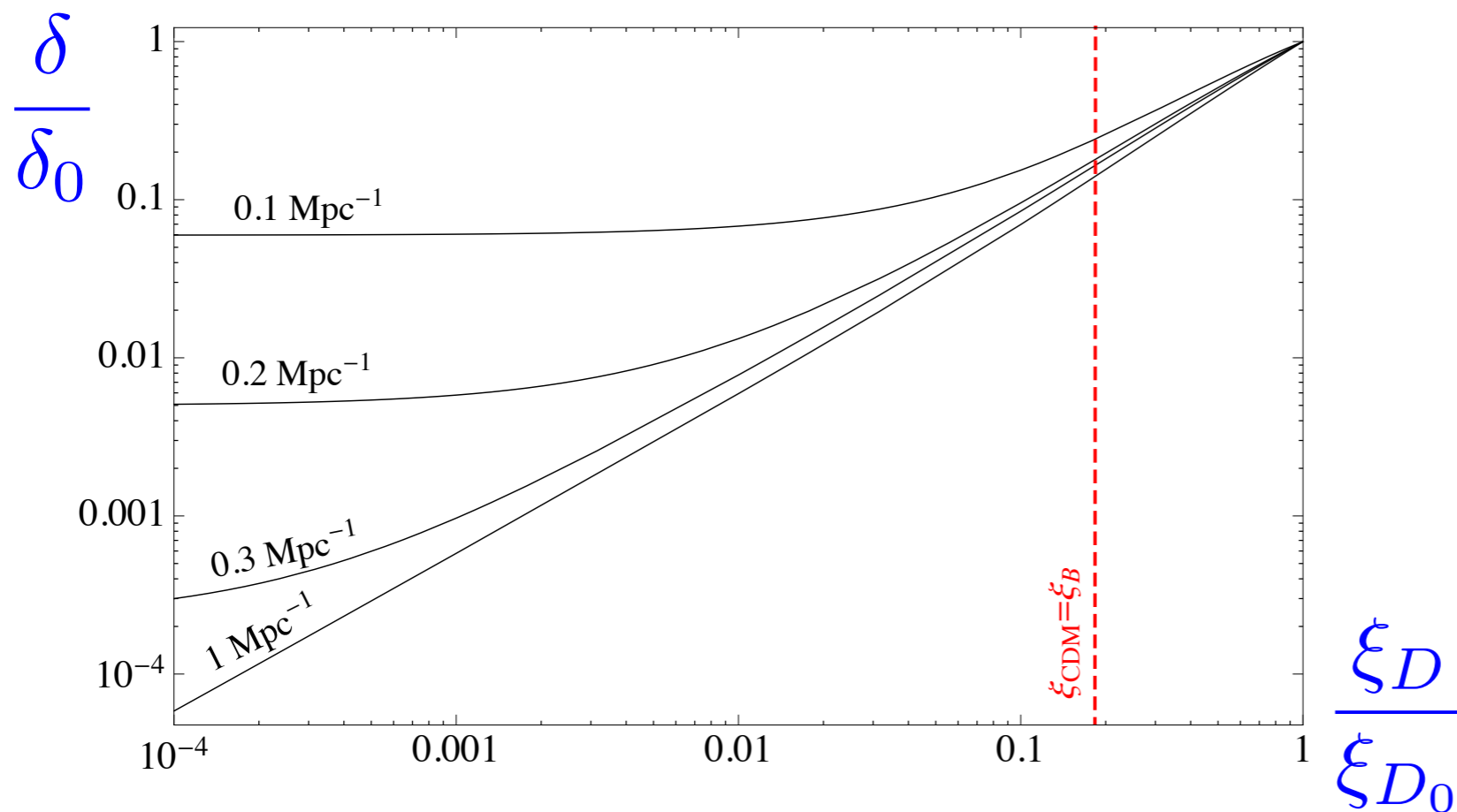
$$\rho \sim T^4 + (\xi_D + \xi_B)T^3 + \Lambda$$

$$\delta(\lambda) \sim \frac{T_e}{T_\Lambda} \left( \frac{\xi_D}{\xi_D + \xi_B} + \frac{\xi_B}{\xi_D + \xi_B} e^{-(\lambda_S/\lambda)^{1.4}} \right) Q_0$$

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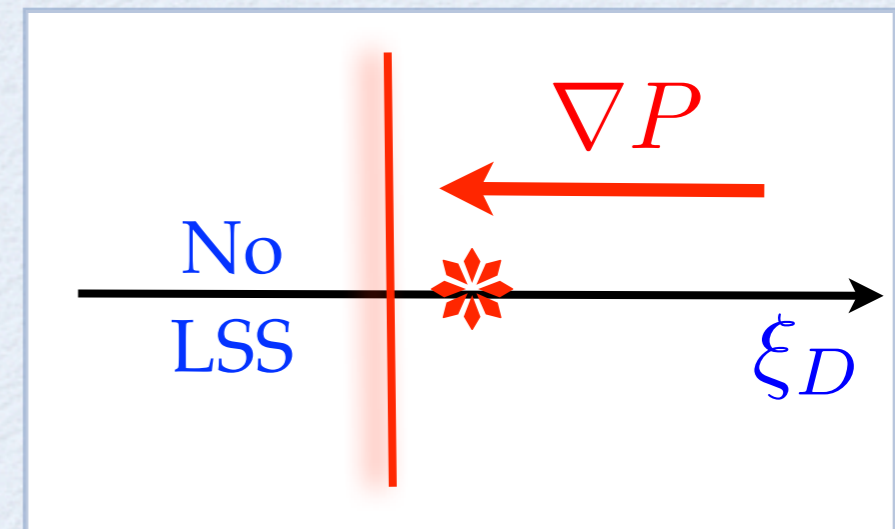
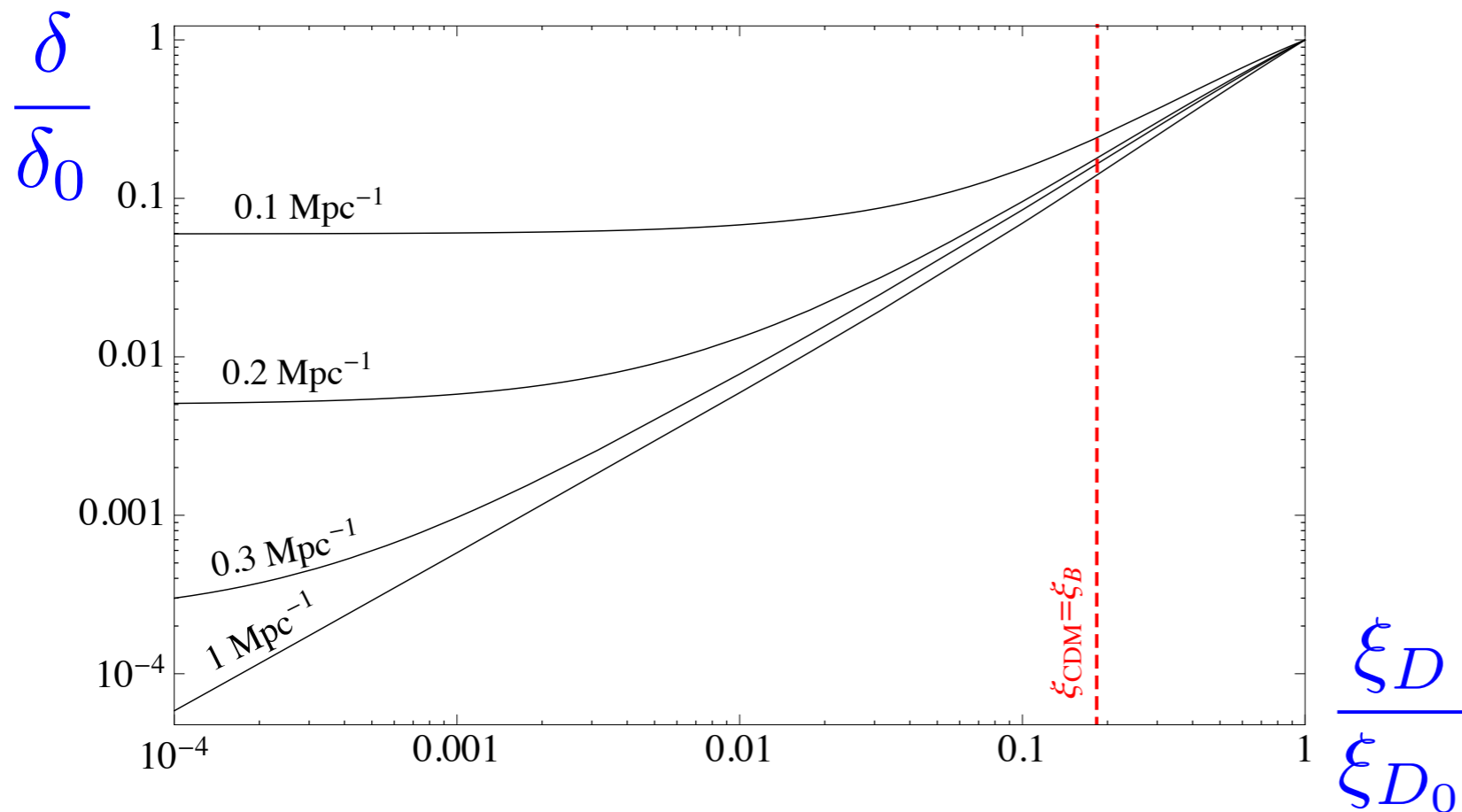


All relevant scales are Silk damped

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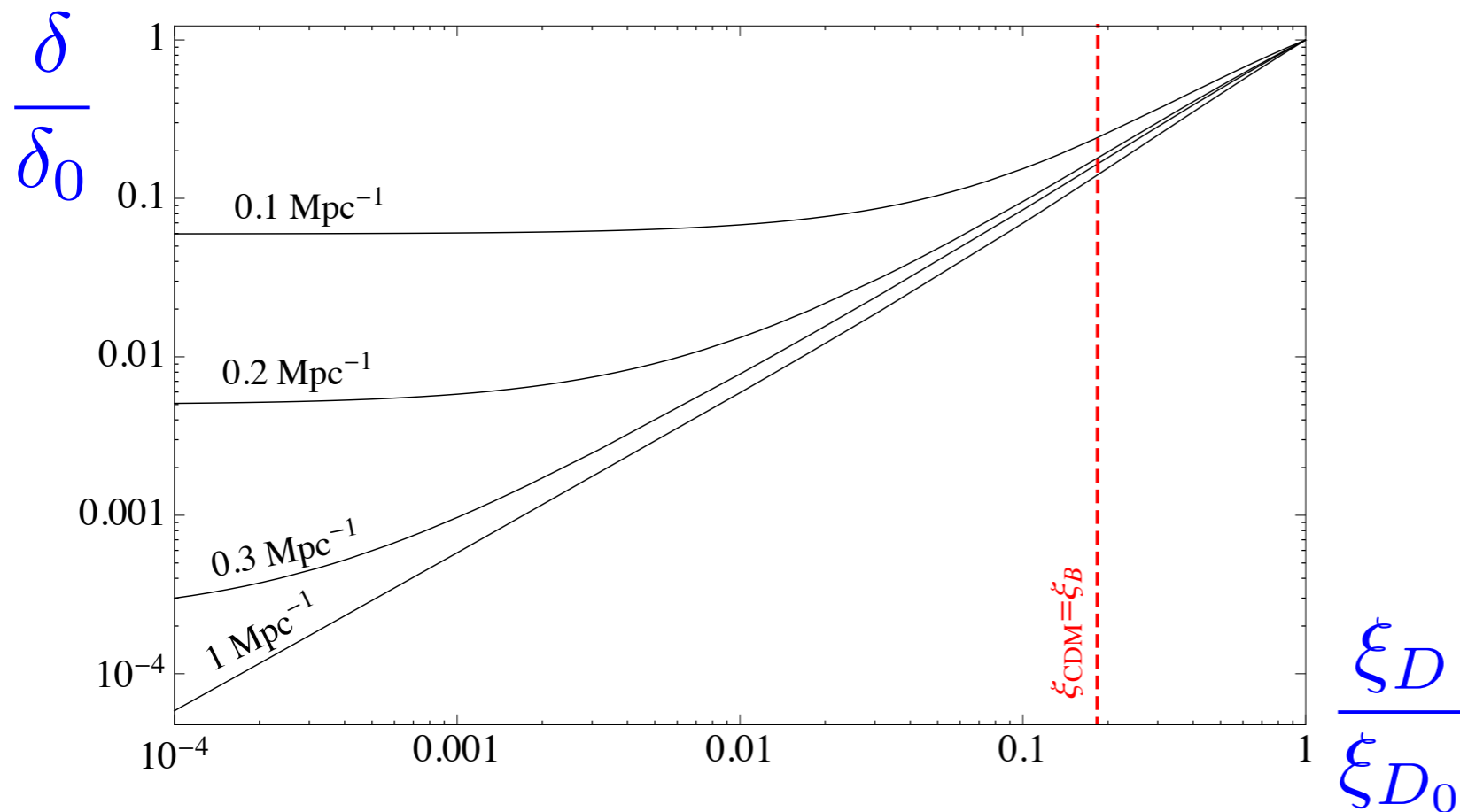


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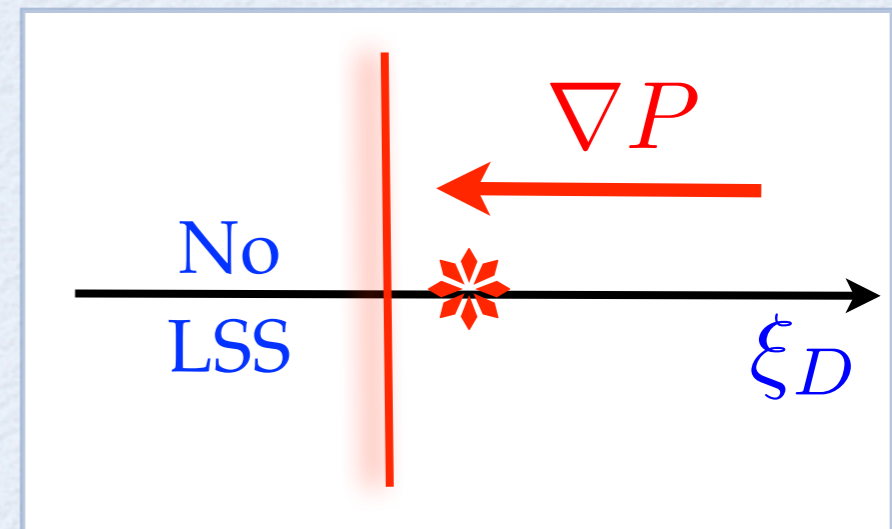
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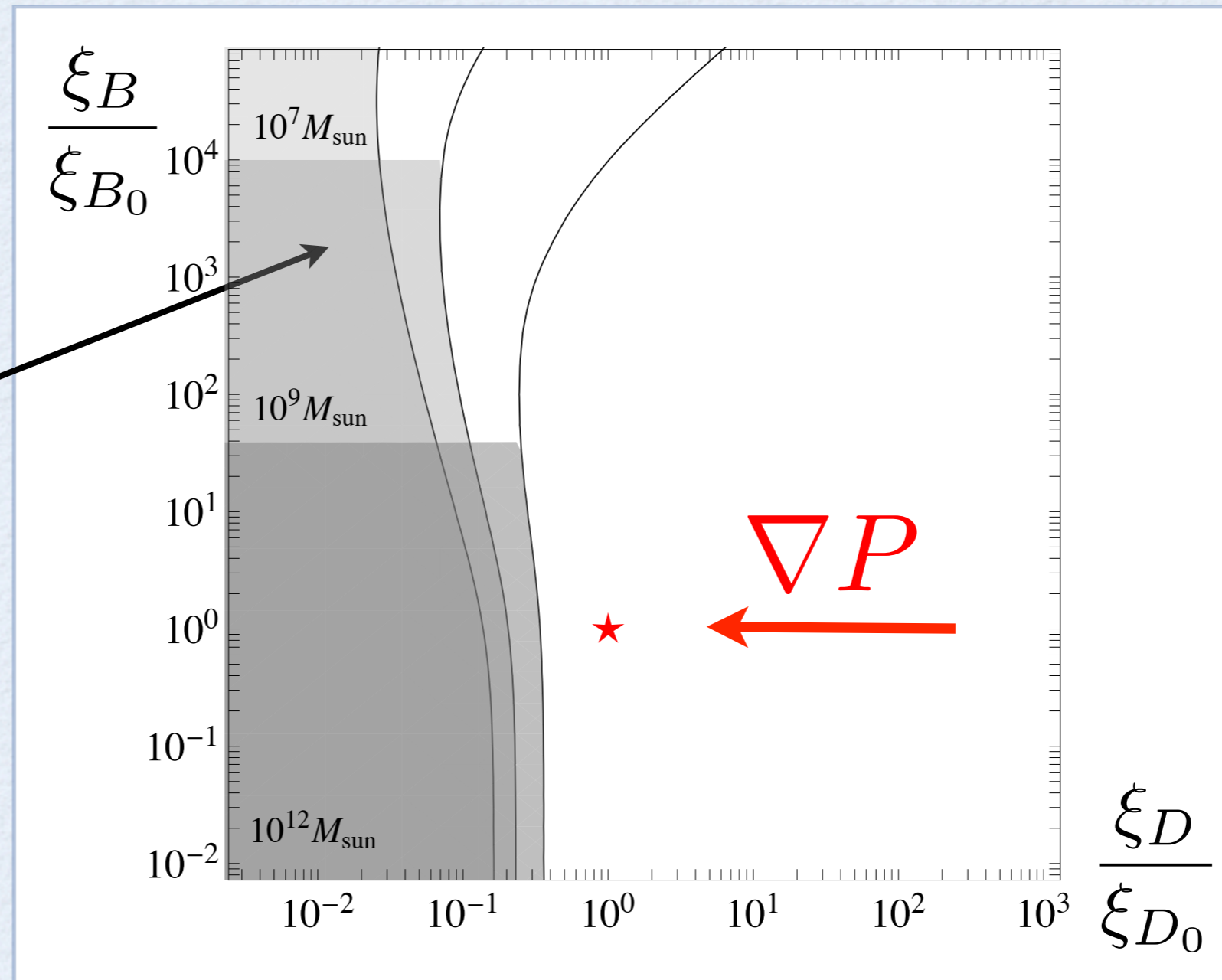
$$\frac{\xi_D^4}{\Lambda}$$

$10^2 - 10^3$  in  $\Lambda$   
 $3 - 5$  in  $\xi_D$



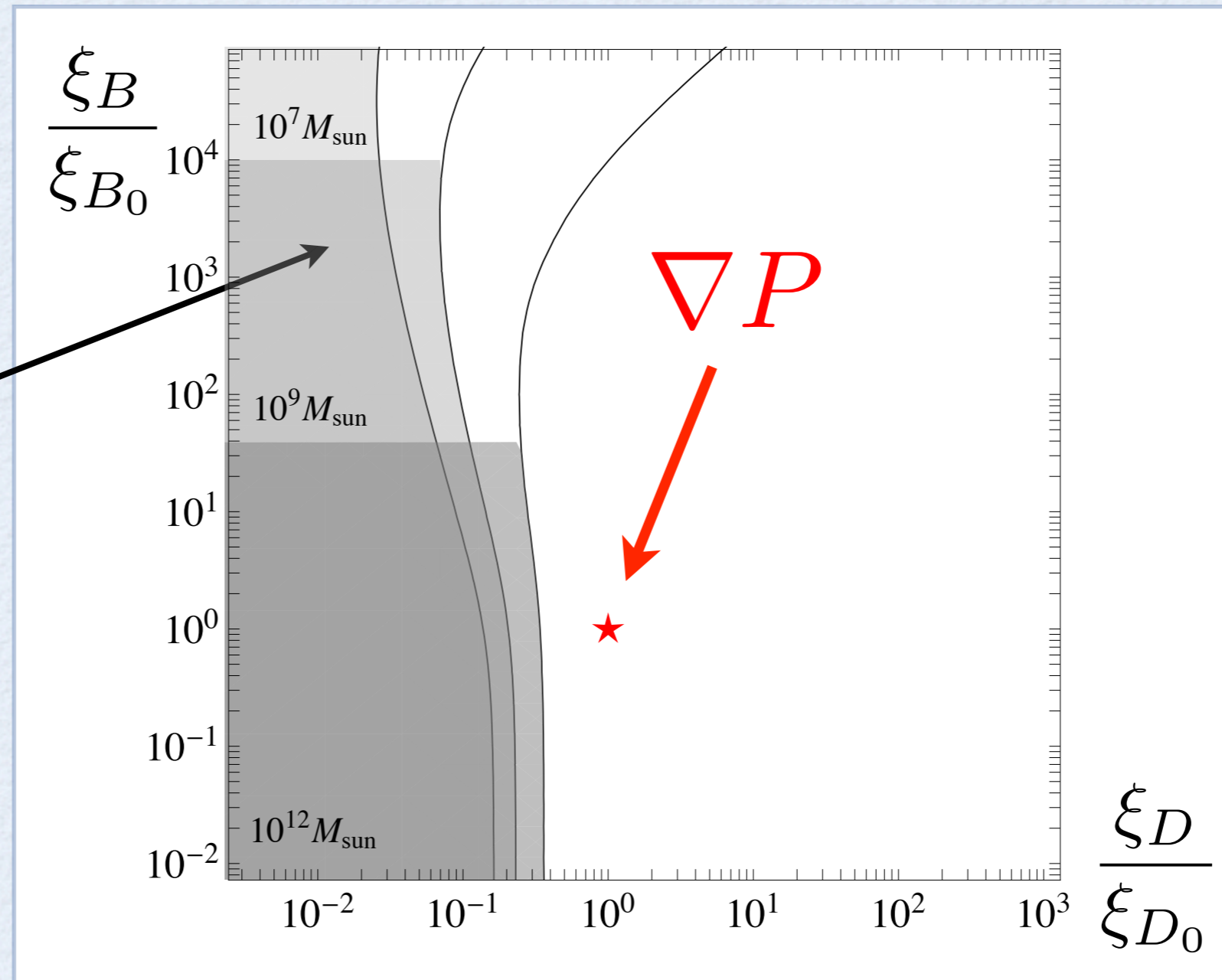
# Varying Baryons and Dark Matter

Could we live here?

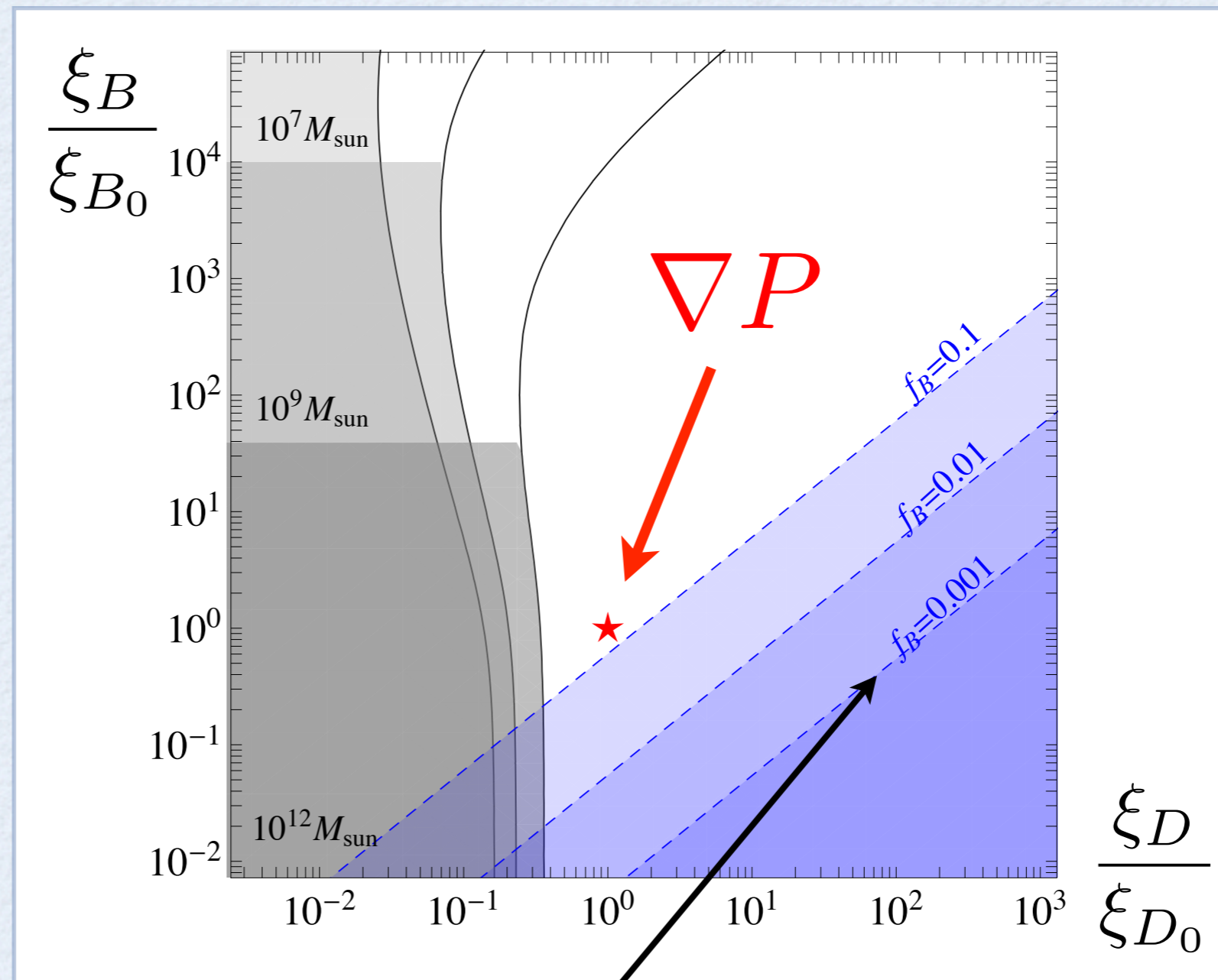


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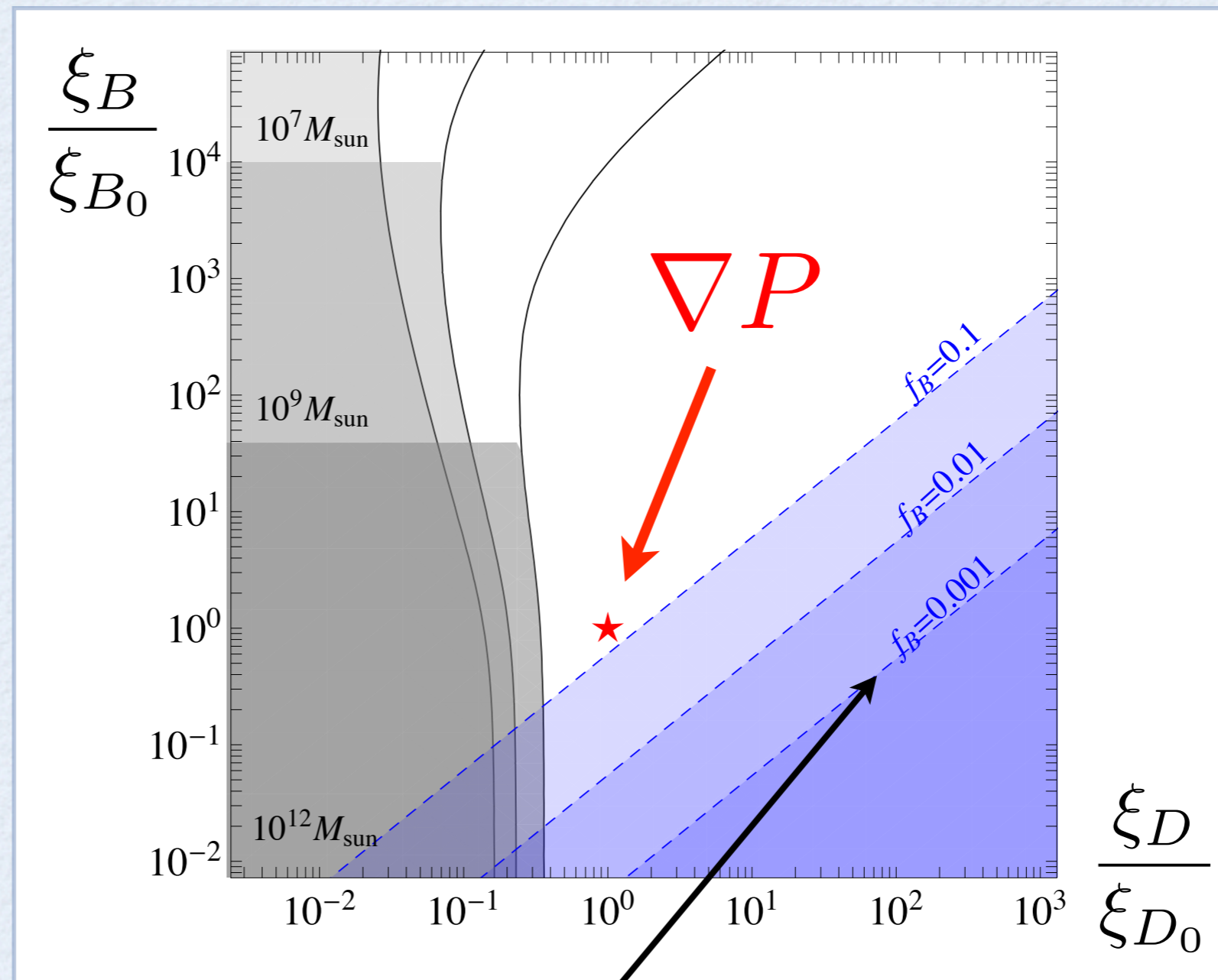


Probability cost  
from the measure

$$f_B = \frac{\xi_B}{\xi_D + \xi_B}$$

Freivogel 0810.0703  
Bousso, Hall 1304.6407

# Varying Baryons and Dark Matter



Explain both  
 $\xi_D, \xi_B$

Probability cost  
from the measure

$$f_B = \frac{\xi_B}{\xi_D + \xi_B}$$

Freivogel 0810.0703  
Bousso, Hall 1304.6407

# Towards a Larger Picture

Observable	Physical Origin
$\Lambda$	Observer dilution
$v$	Avoid ${}^4\text{He}$ universe
$m_{u,d,e}$	H, complex nuclei
$\xi_D$	Large Scale Structure
$\xi_B$	Observer dilution

- Tentative
- A beginning -- just “scatching the surface”
- Implications for Symmetries are Immense

(III)

Implications:  
SUSY

D'Eramo, Hall, Pappadopulo; to appear

# SUSY LSP Freeze-Out

Suppose the overall scale of SUSY breaking scans:

$$\xi_D \propto \frac{1}{\sigma_A} \propto \tilde{m}^2$$

$$dP \sim \tilde{m}^n \left( \frac{v^2}{\tilde{m}^2} \right) d \ln \tilde{m}$$

EWSB  
fine-tuning

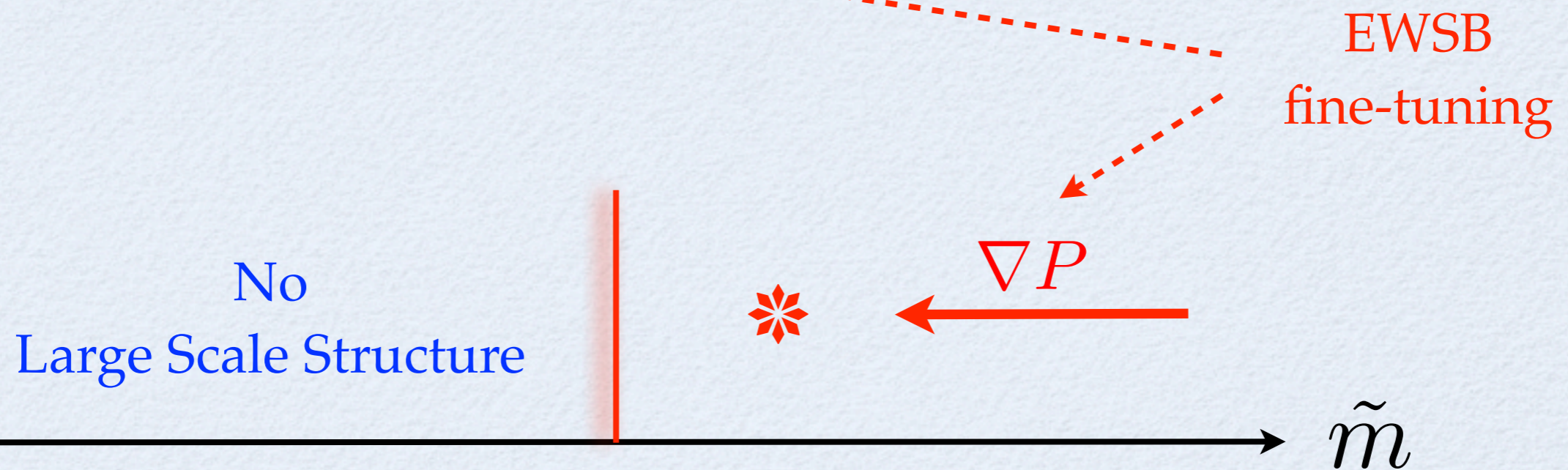


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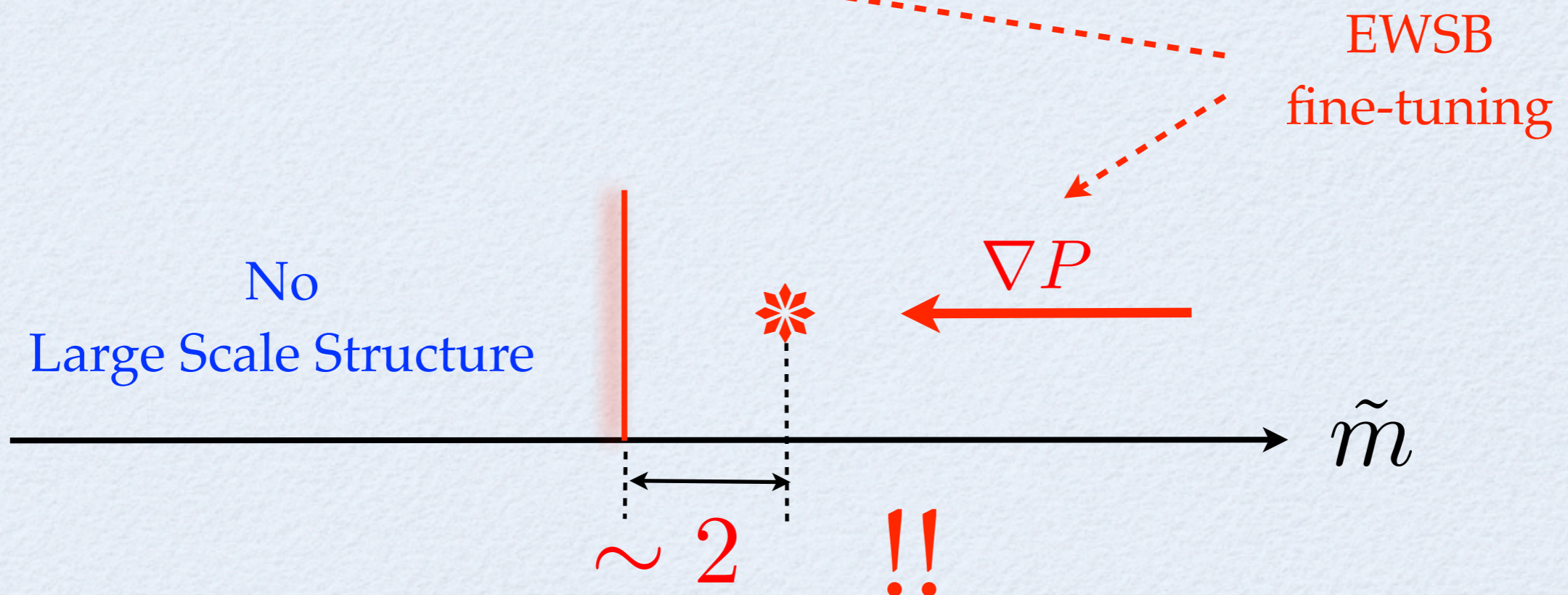


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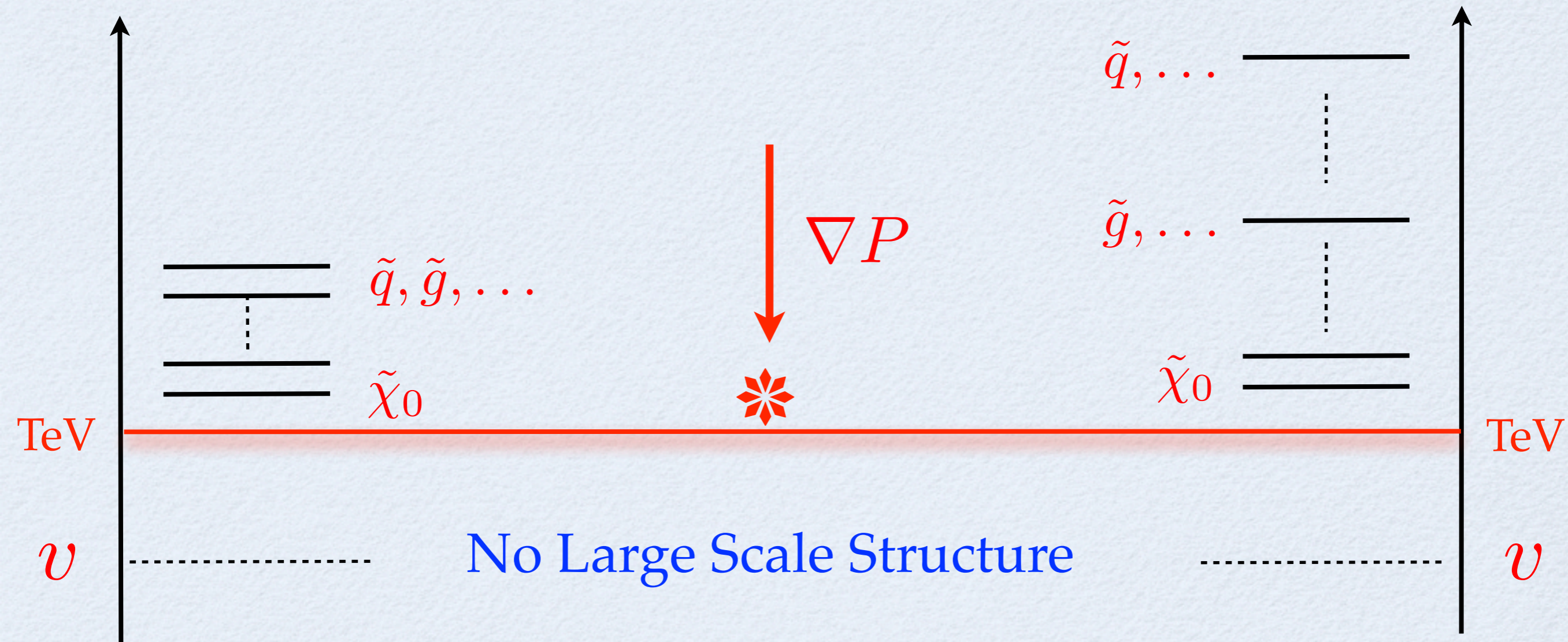
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# A Little SUSY Hierarchy

The SUSY spectrum may be the most natural consistent with Large Scale Structure

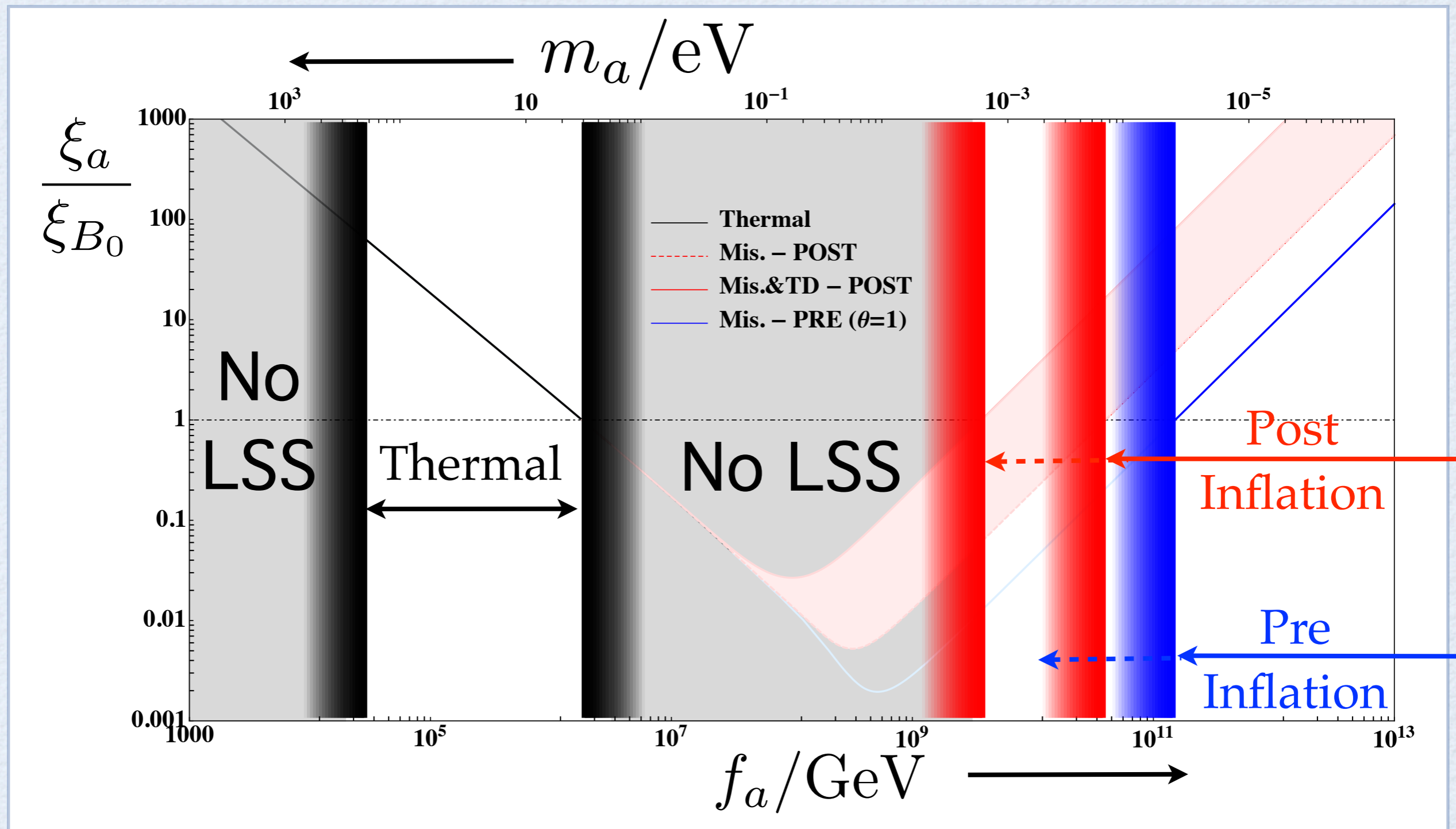


(III)

Implications:  
Axion with Low  $f$

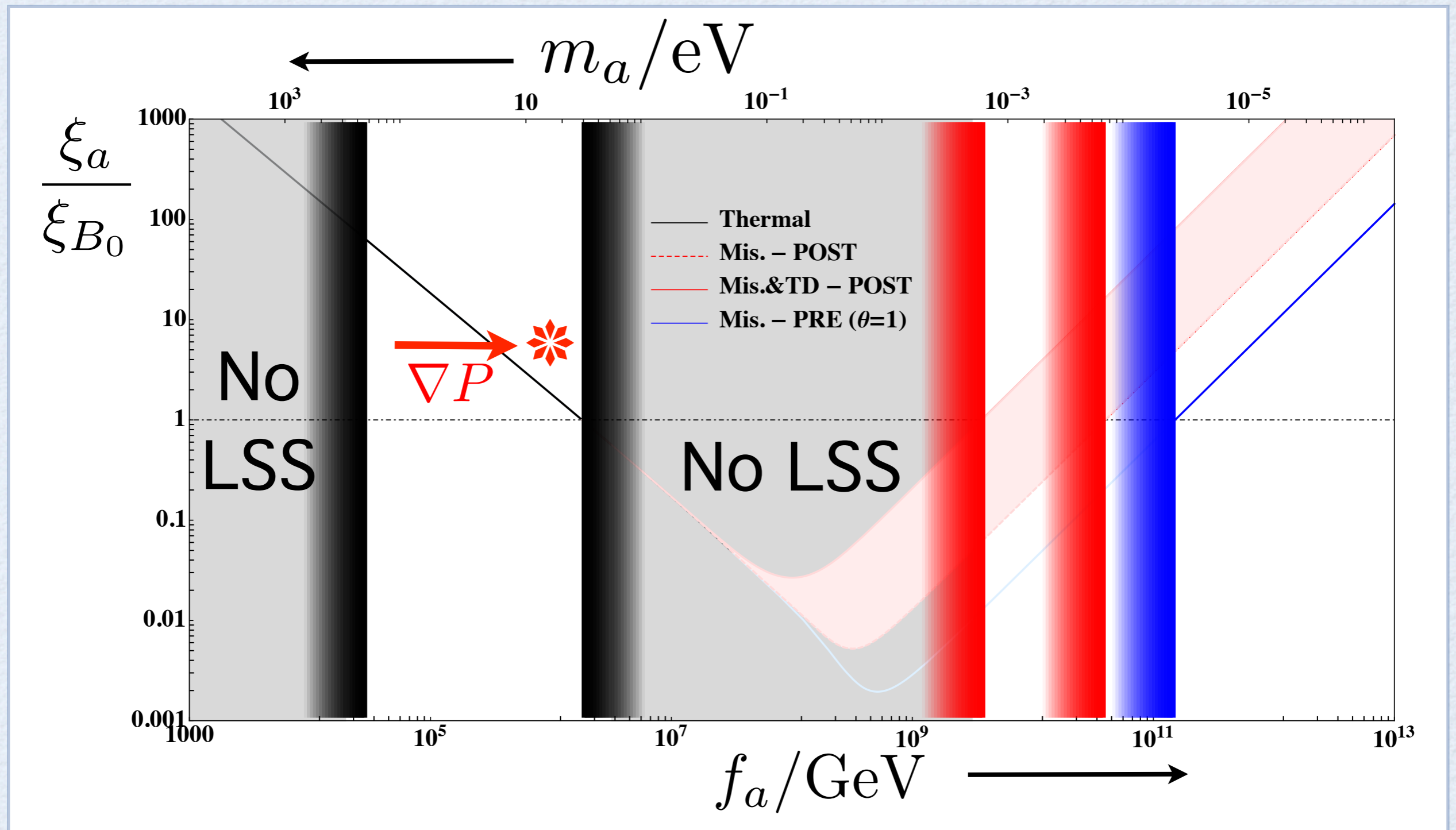
D'Eramo, Hall, Pappadopulo; to appear

# Axions and the LSS Boundary

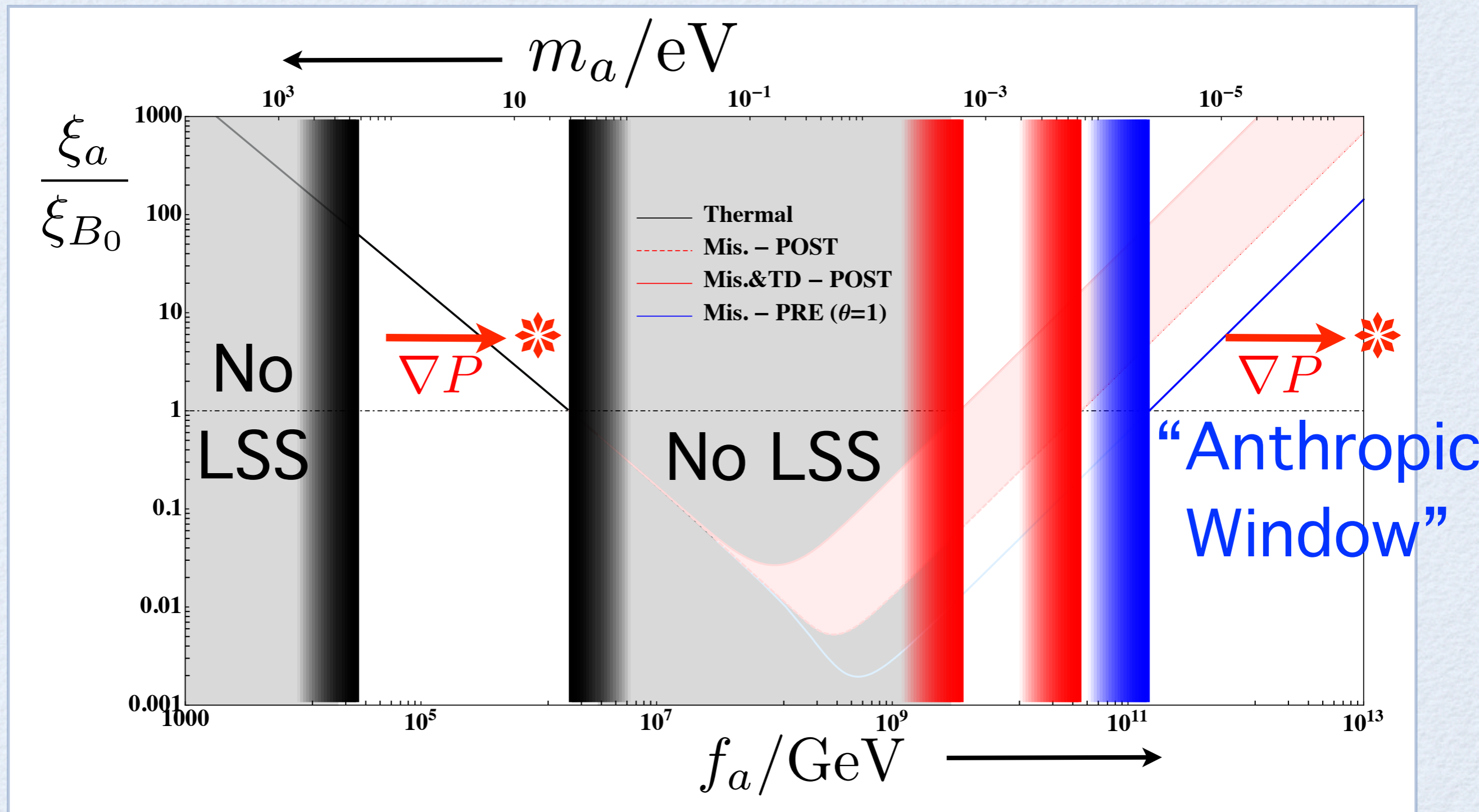


(using results from: Bae, Huh, Kim 0806.0497; Kawasaki, Nakayama 1301.1123)

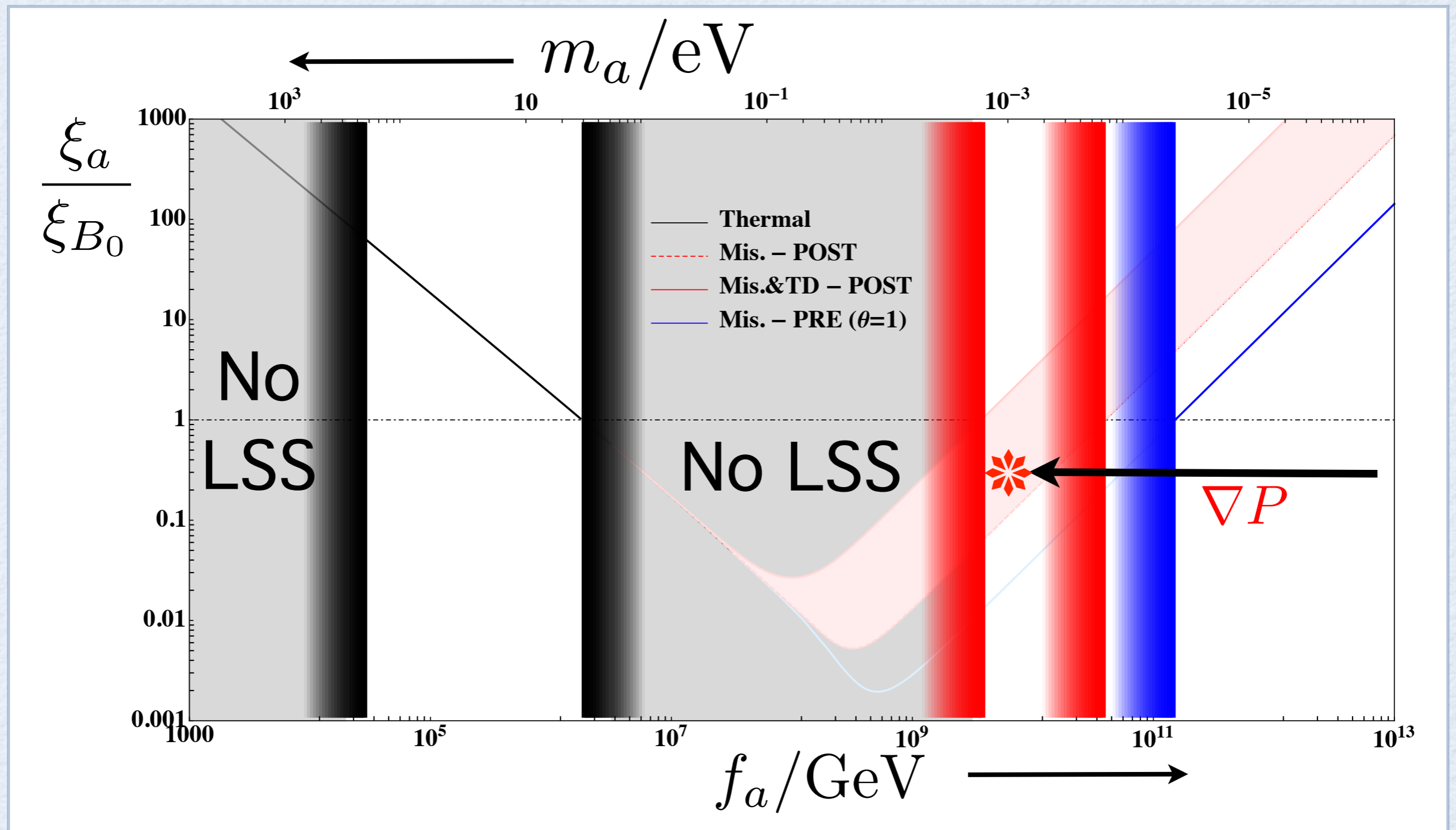
# Axions with High $f$



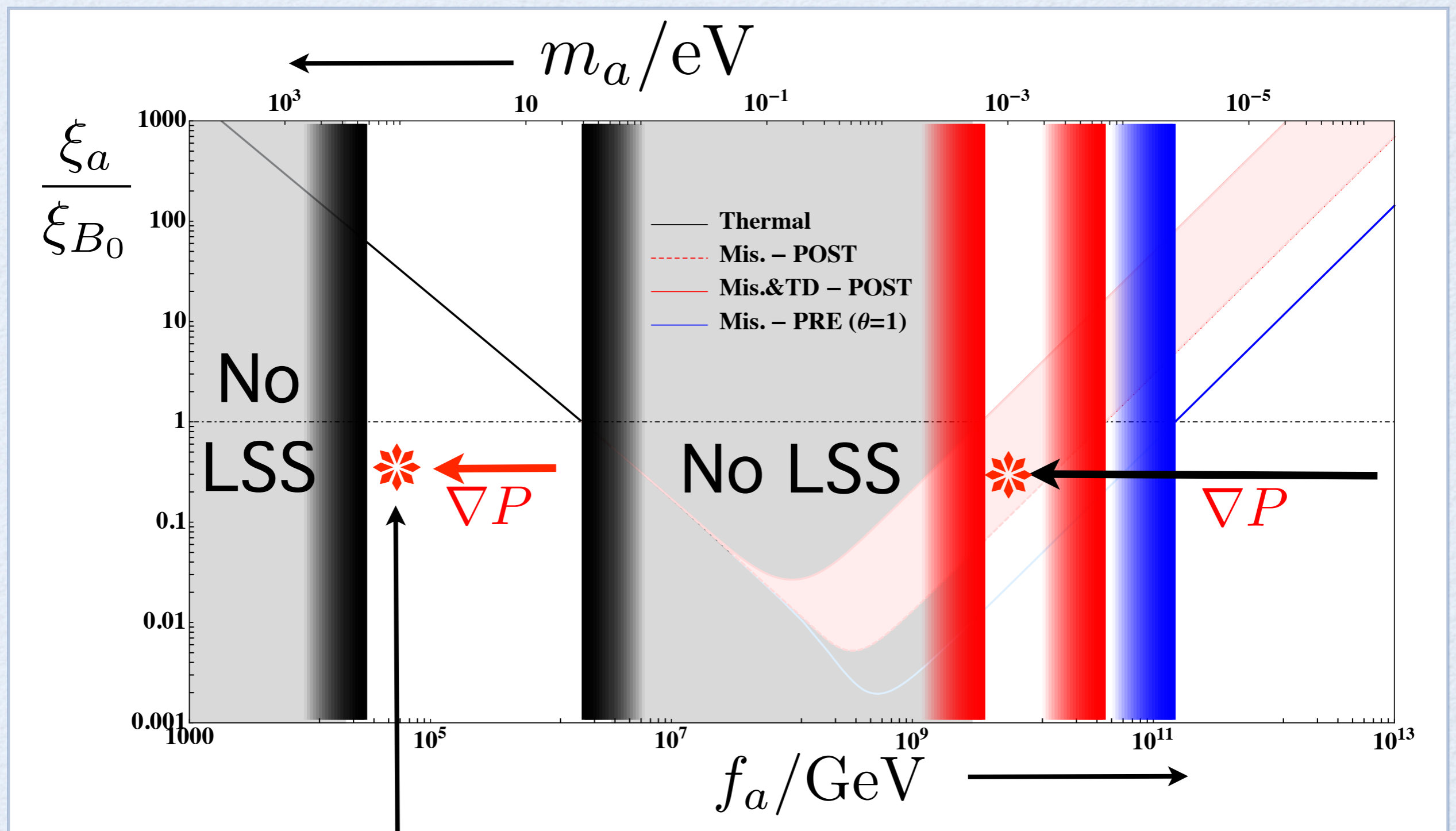
# Axions with High $f$



# Axions with High $f$



# Axions with High $f$



Likely Excluded: free streaming, decays, stars



# Axion Dark Matter Searches

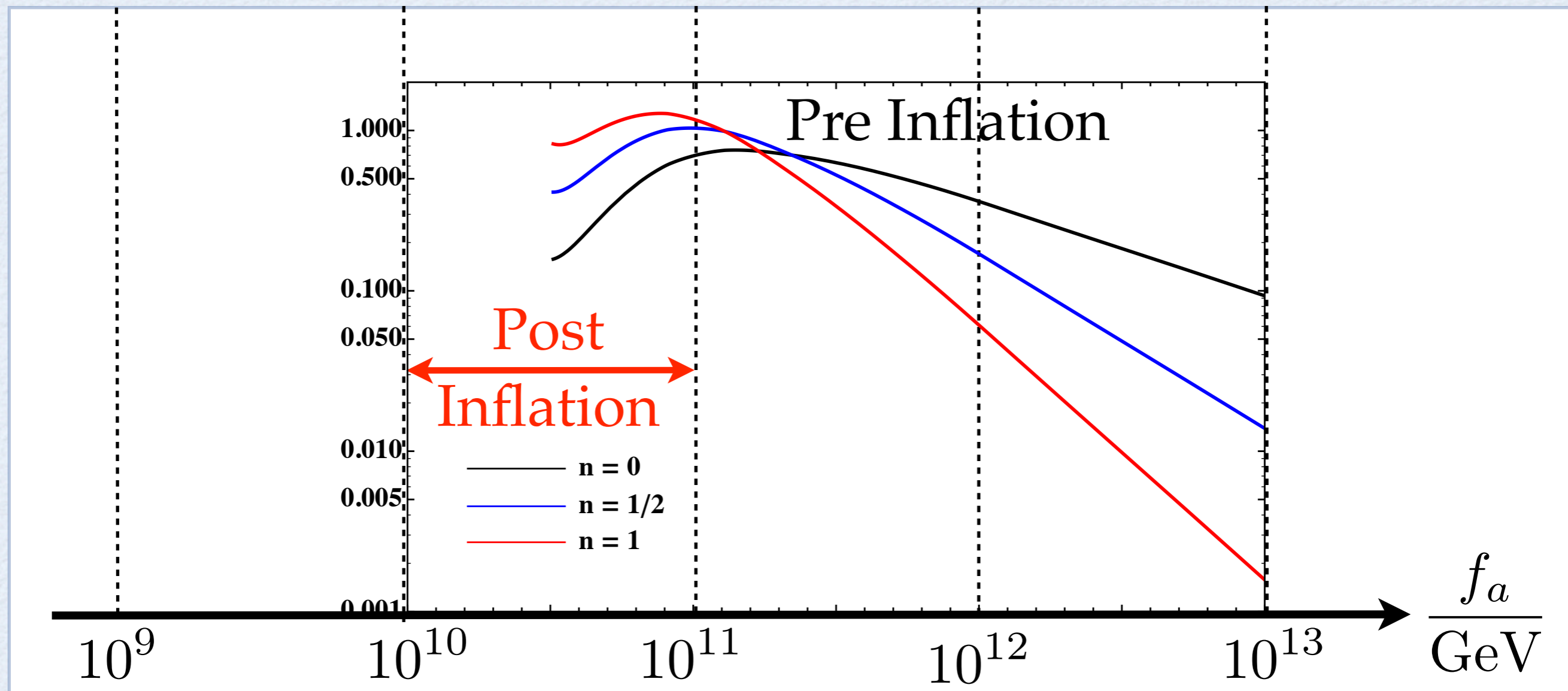
LSS boundary predicts single component dark matter

From observed abundance we can predict  $f_a$

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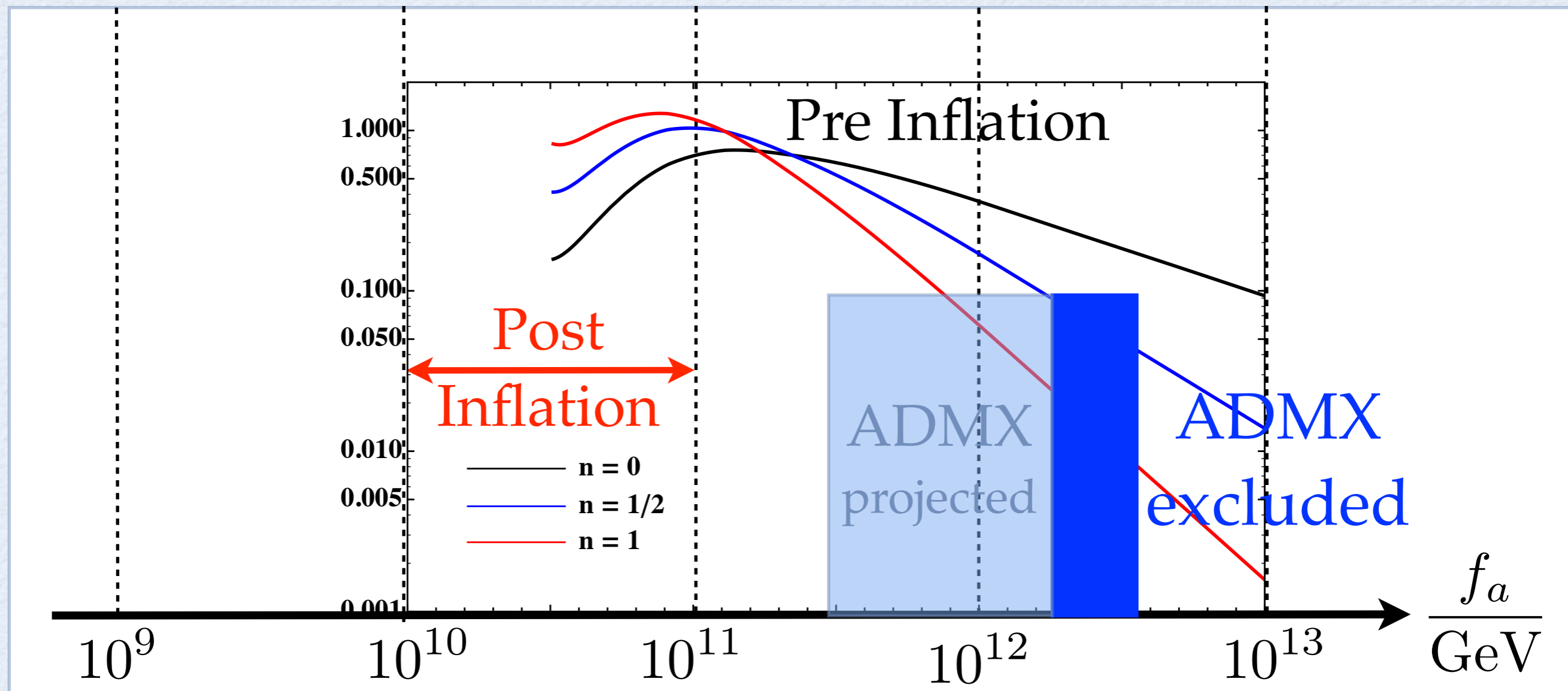
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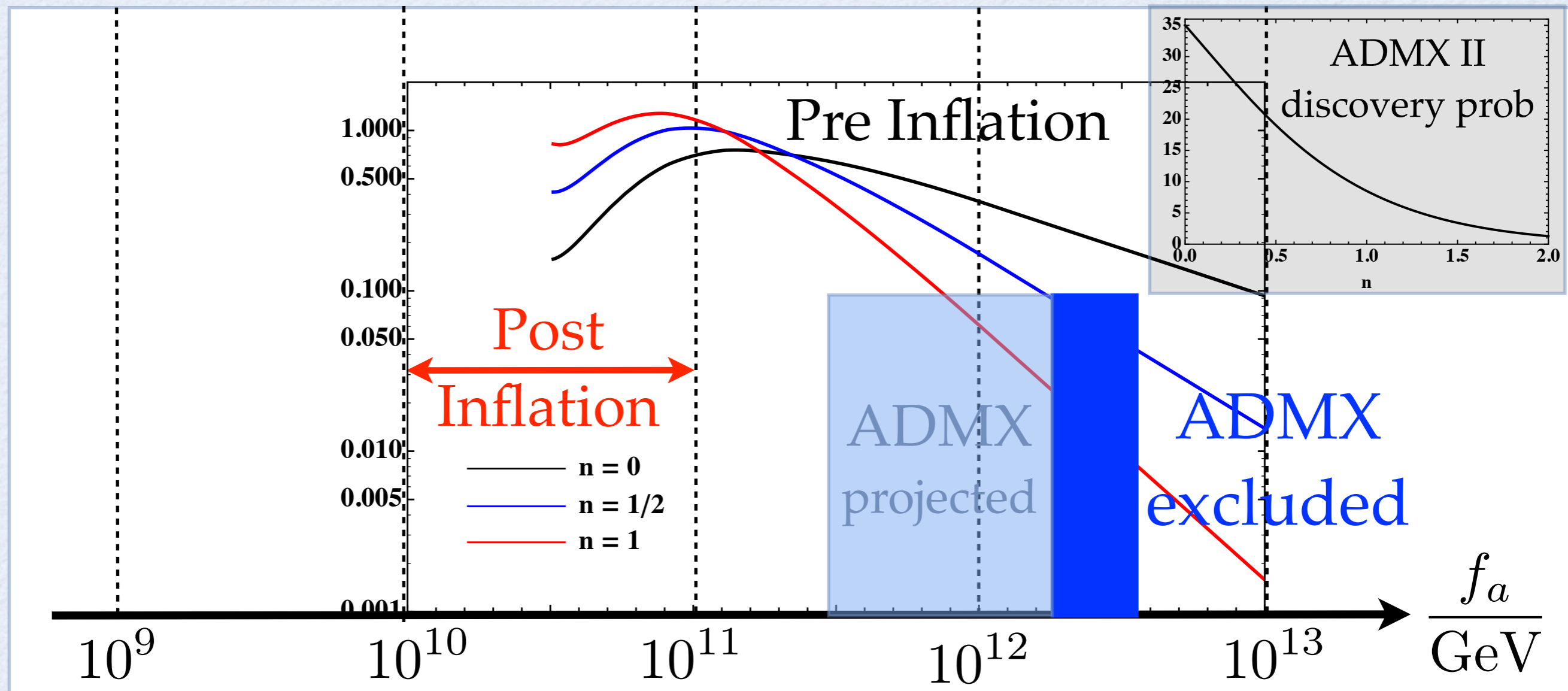
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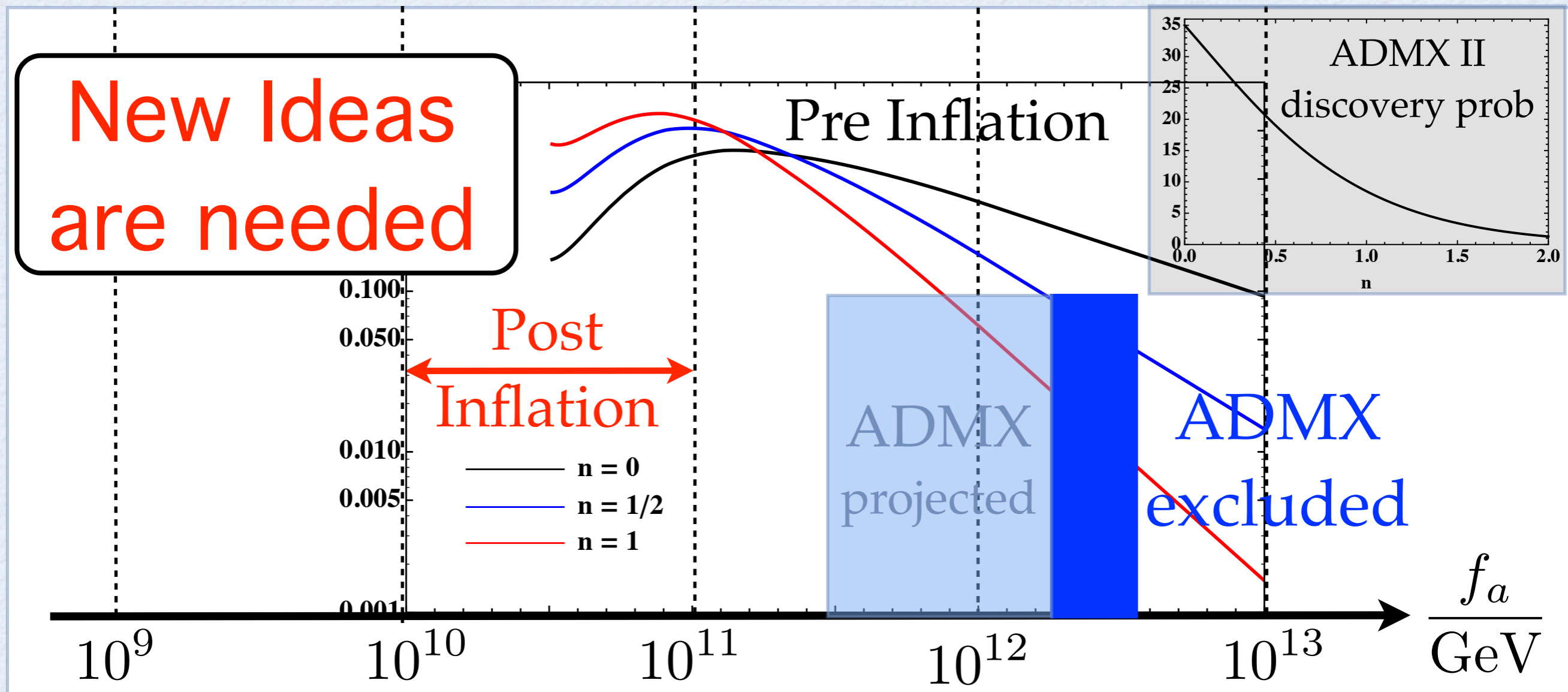
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# Axion Dark Matter Searches

LSS boundary predicts single component dark matter

From observed abundance we can predict  $f_a$



(IV)

A Model for the Multiverse Axion  
and the Higgs Mass

D'Eramo, Hall, Pappadopulo; to appear

# Minimal Supersymmetric PQ

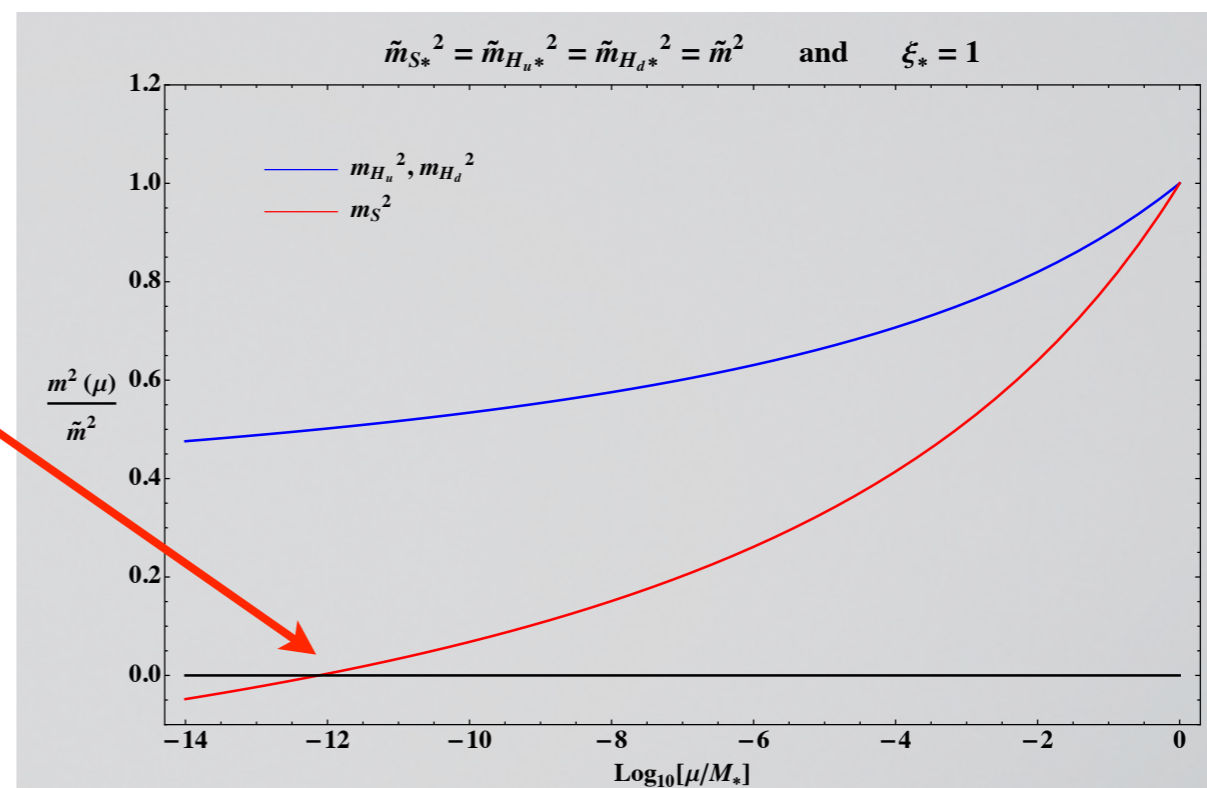
- MSSM:  $W = \mu H_u H_d$  Radiative EWSB
- MSPQ:  $W = \xi S H_u H_d$  Radiative PQB

# Minimal Supersymmetric PQ

- MSSM:  $W = \mu H_u H_d$  Radiative EWSB
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Dimensional  
Transmutation

$$f \sim e^{-\frac{16\pi^2}{\xi^2}} M_*$$



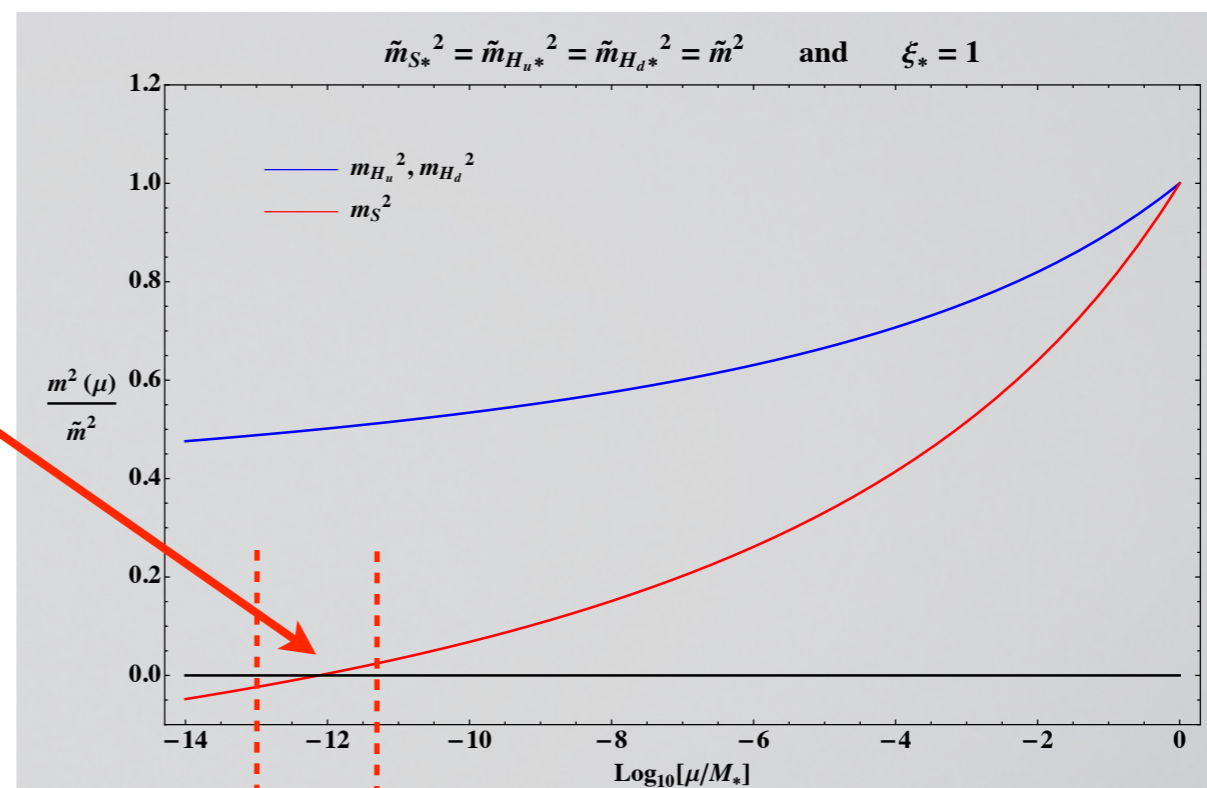


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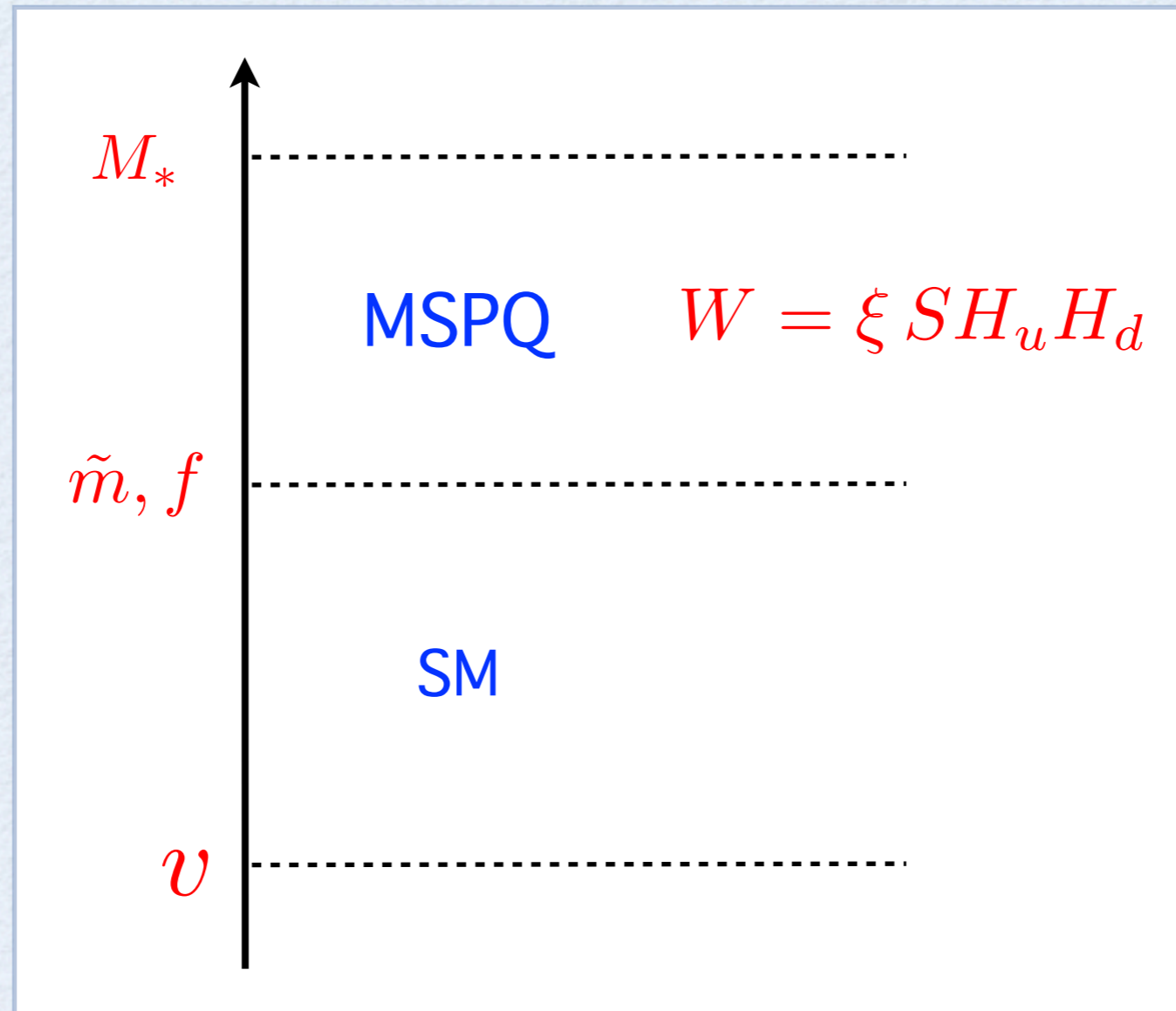


No  
EWSB

No  
EWSB

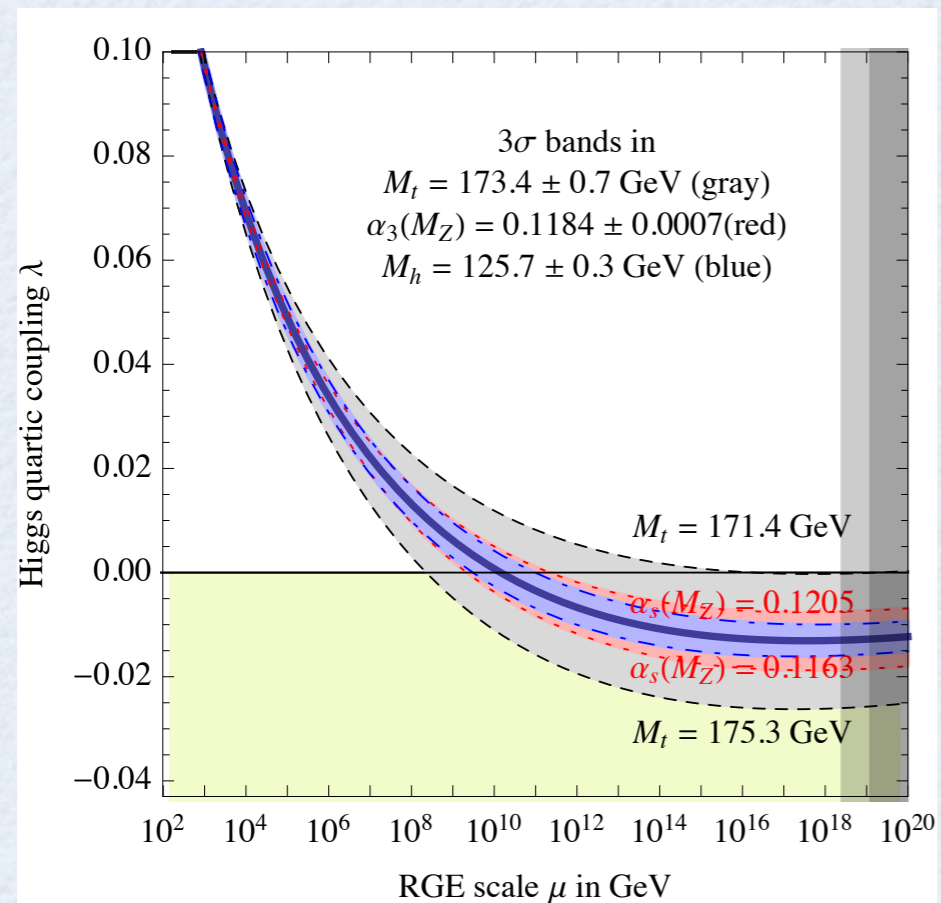
$\tilde{m}$

# Mass Scales



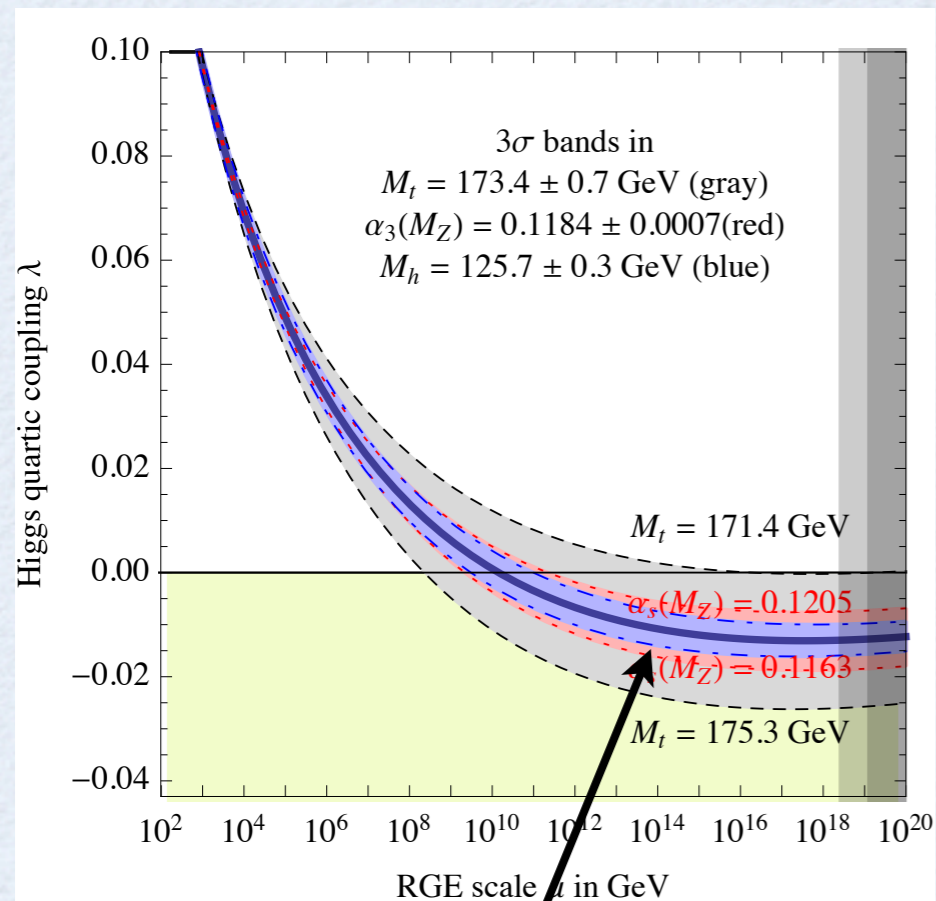
- The Multiverse allows a new Minimal SUSY
- It solves strong CP, and gives axion DM

# Higgs Mass From Vacuum Stability



Buttazzo, Degrassi,  
Giardino, Giudice, Sala,  
Salvio, Strumia  
1307.3536

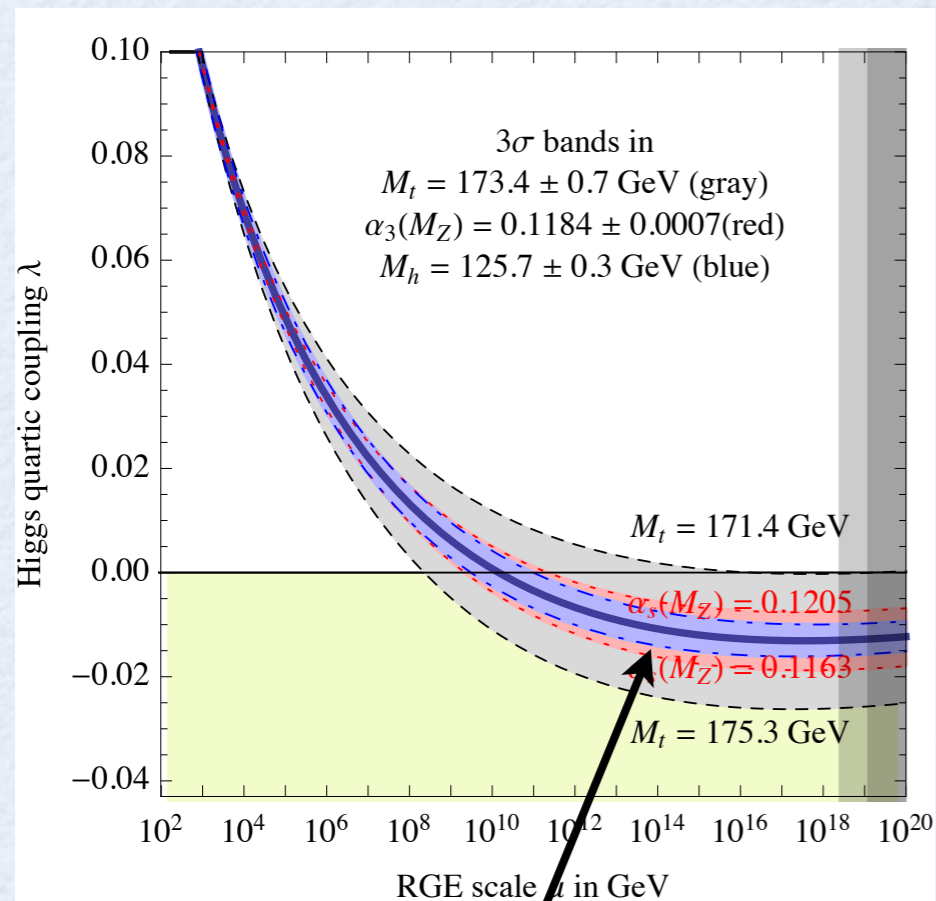
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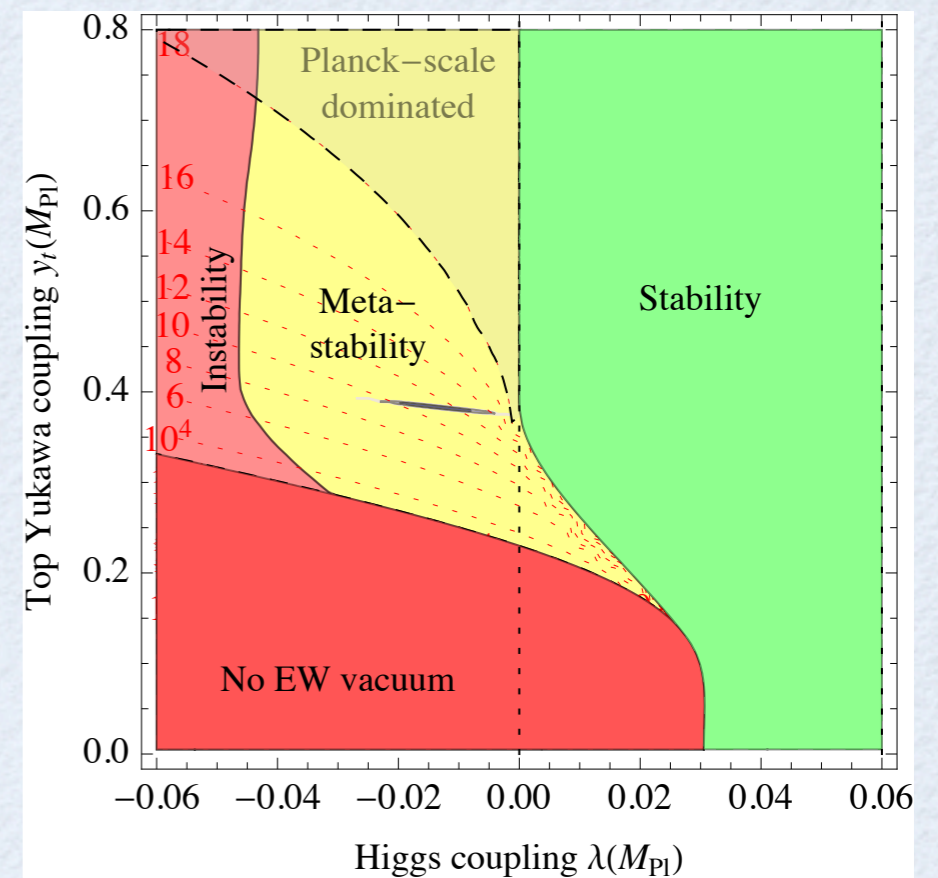
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Why is quartic  
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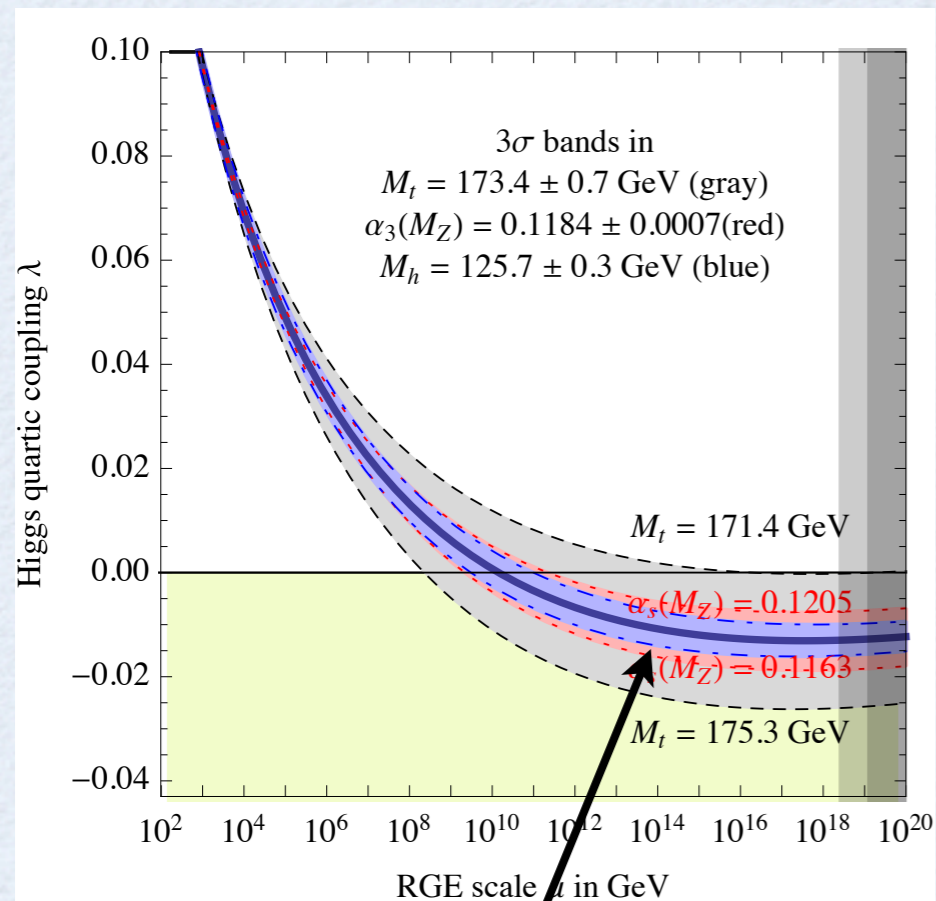


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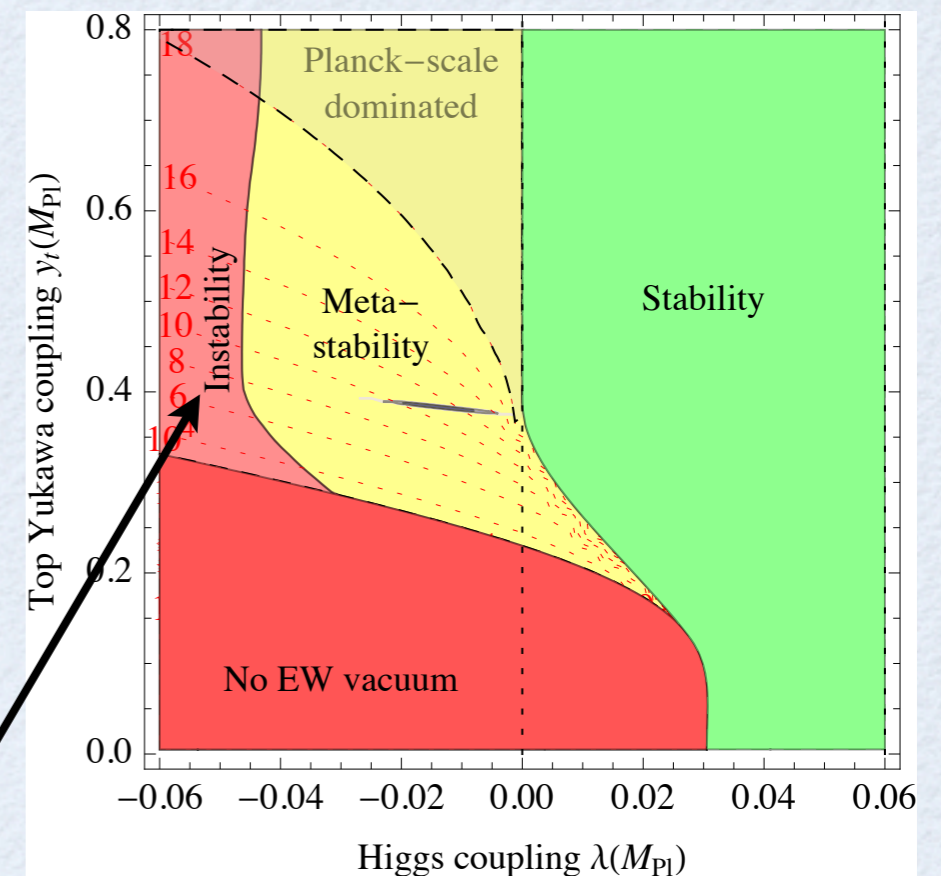
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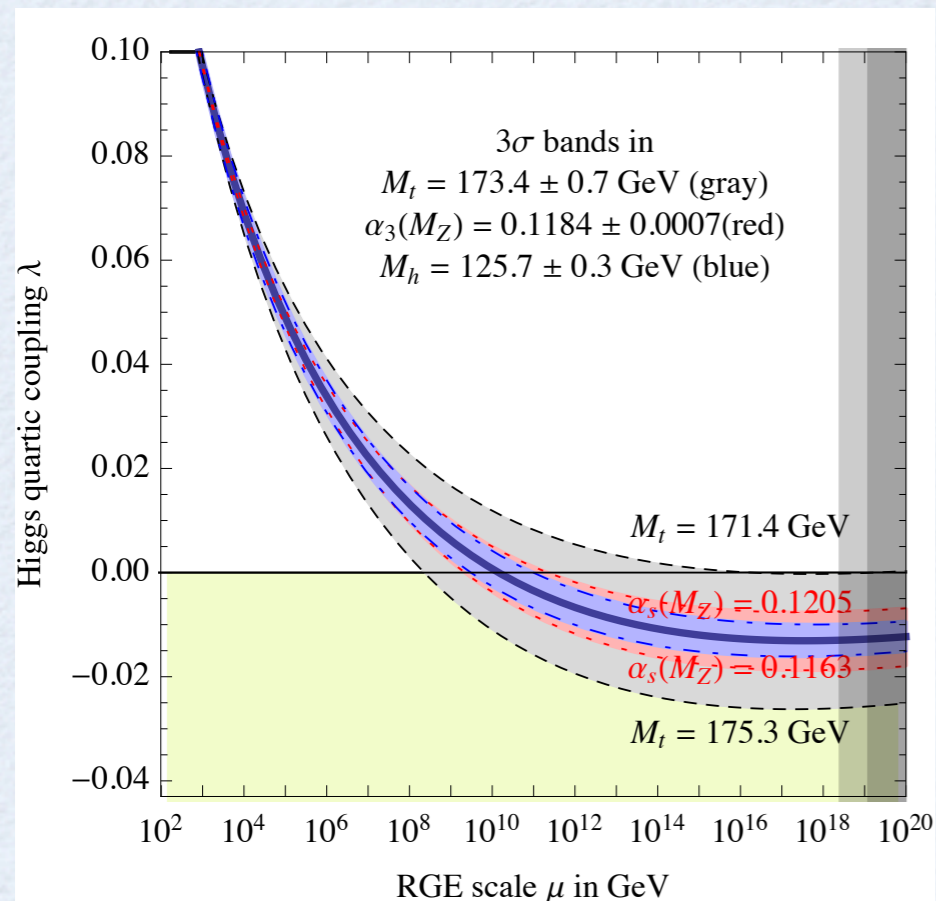
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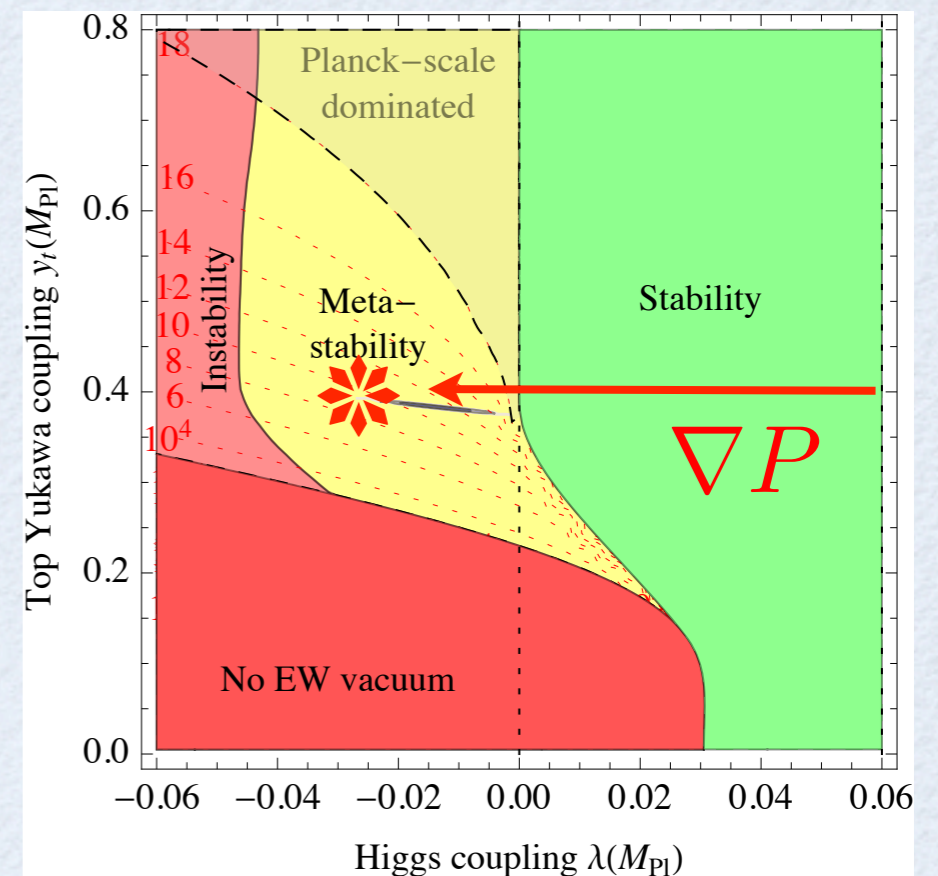


Close to vacuum instability!

# Higgs Mass From Vacuum Stability

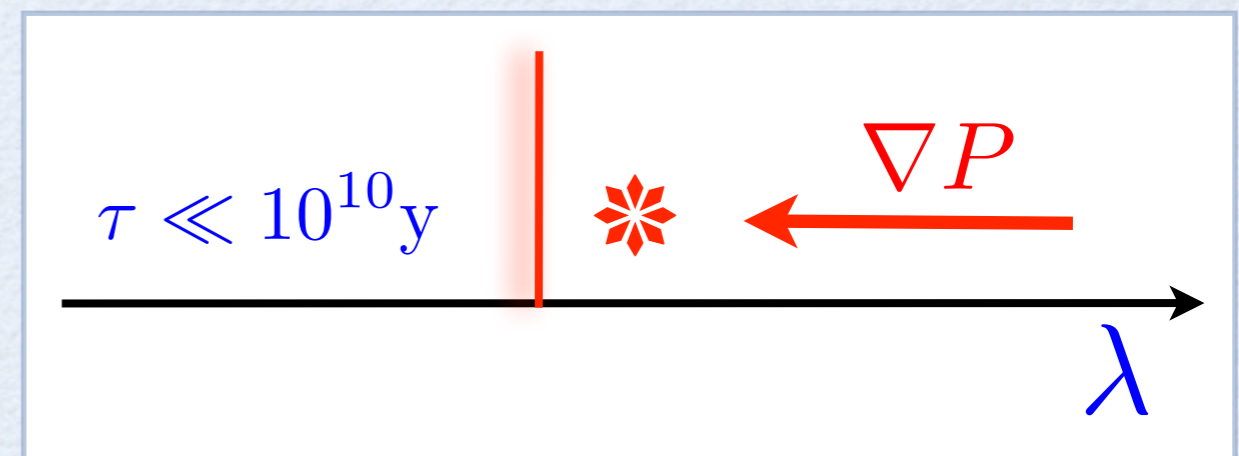


Buttazzo, Degrassi,  
 Giardino, Giudice, Sala,  
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 1307.3536

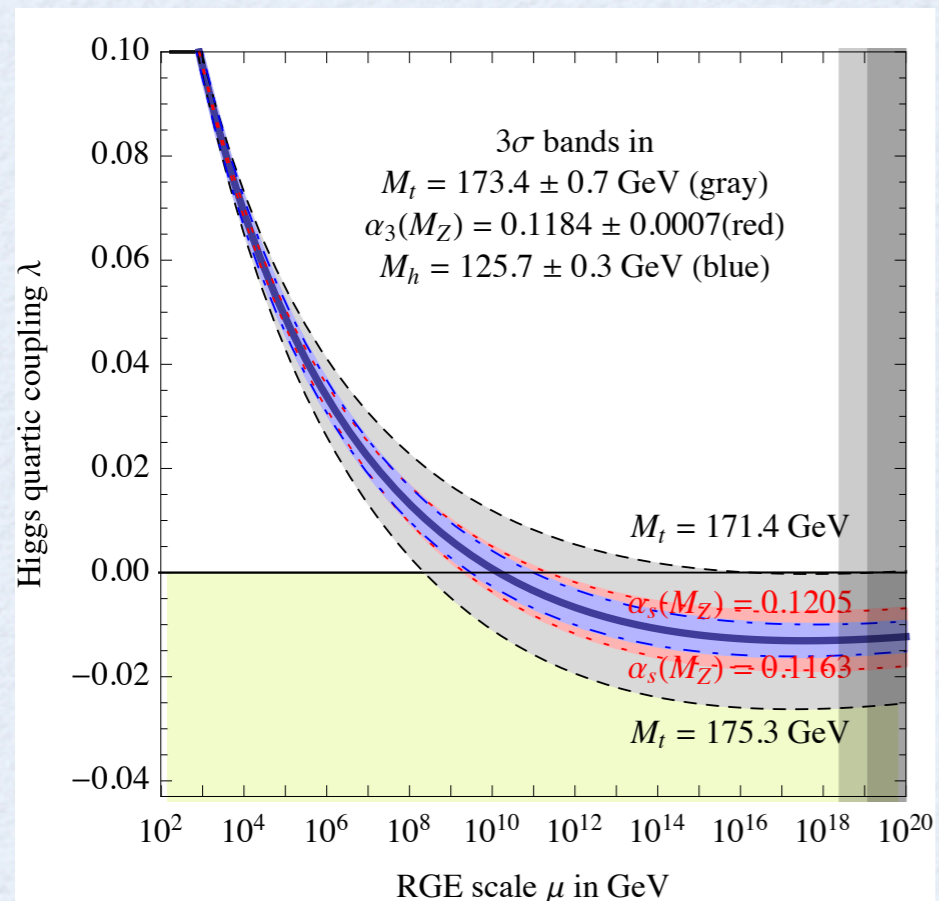


$$m_h = (112 \pm 8 + 25/n) \text{ GeV}$$

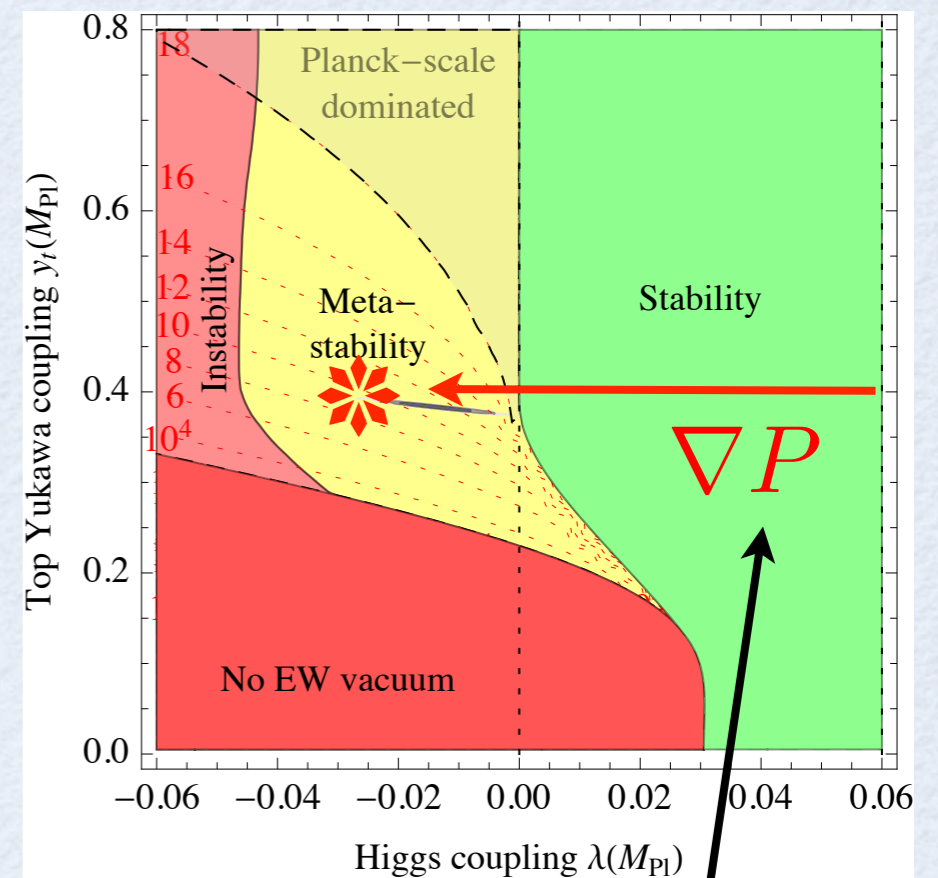
Feldstein, Hall, Watari  
 hep-ph/0608121



# Higgs Mass in MSPQ



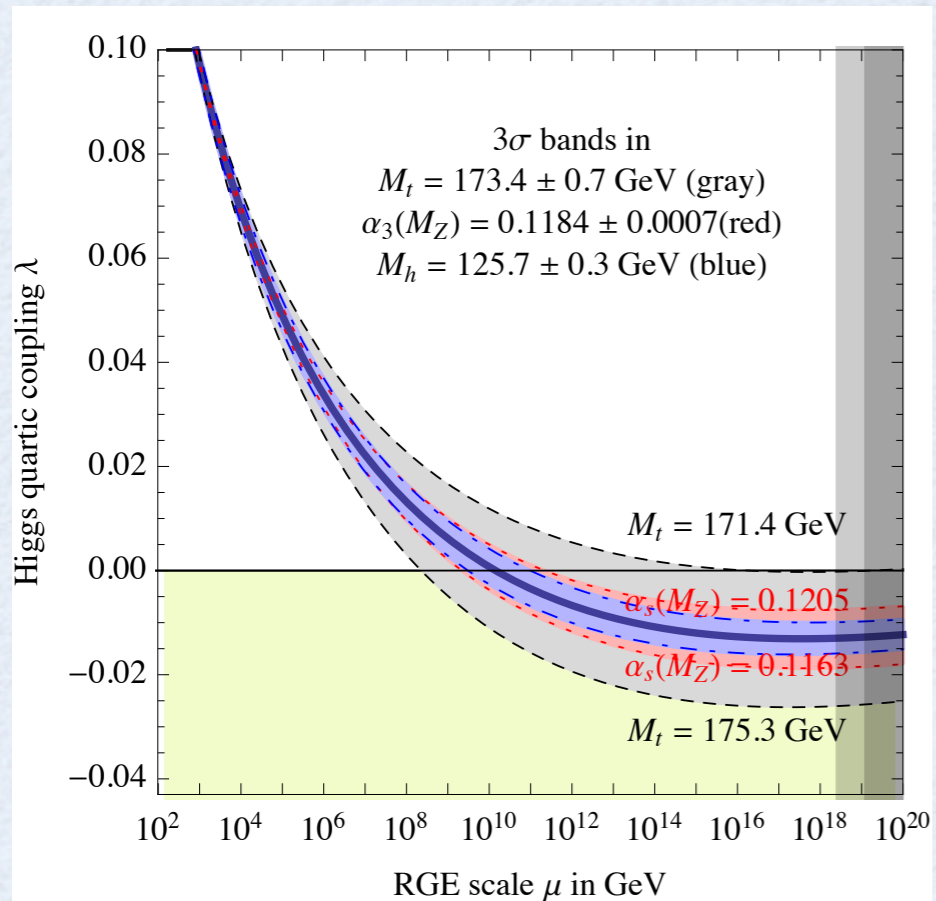
Buttazzo, Degrassi,  
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 1307.3536



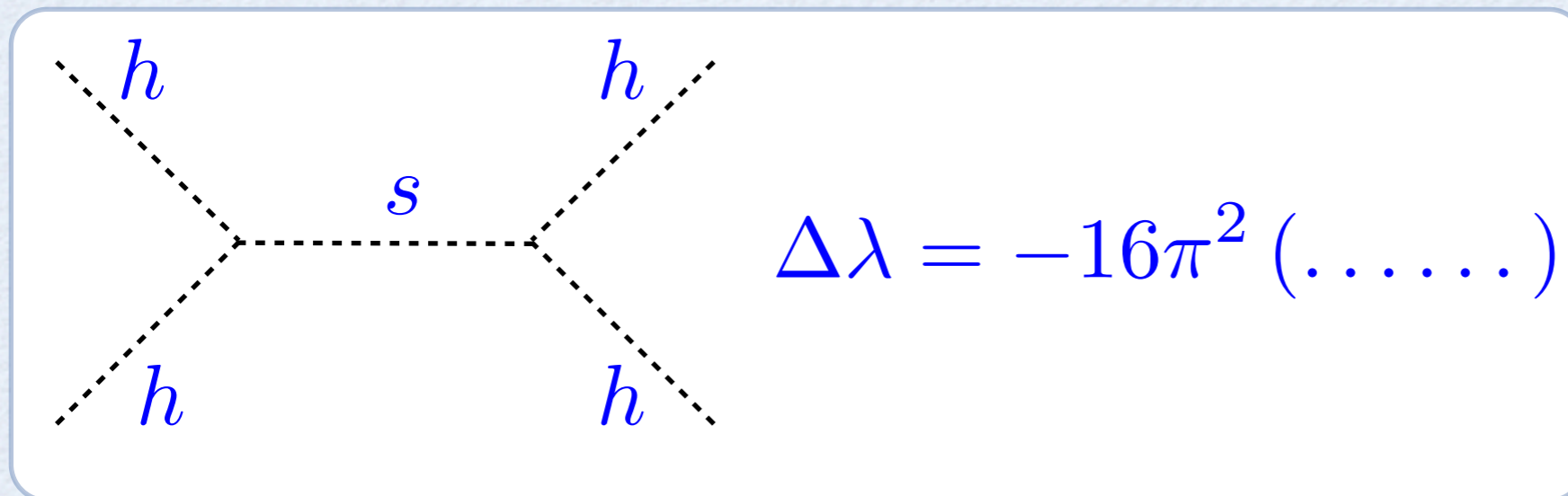
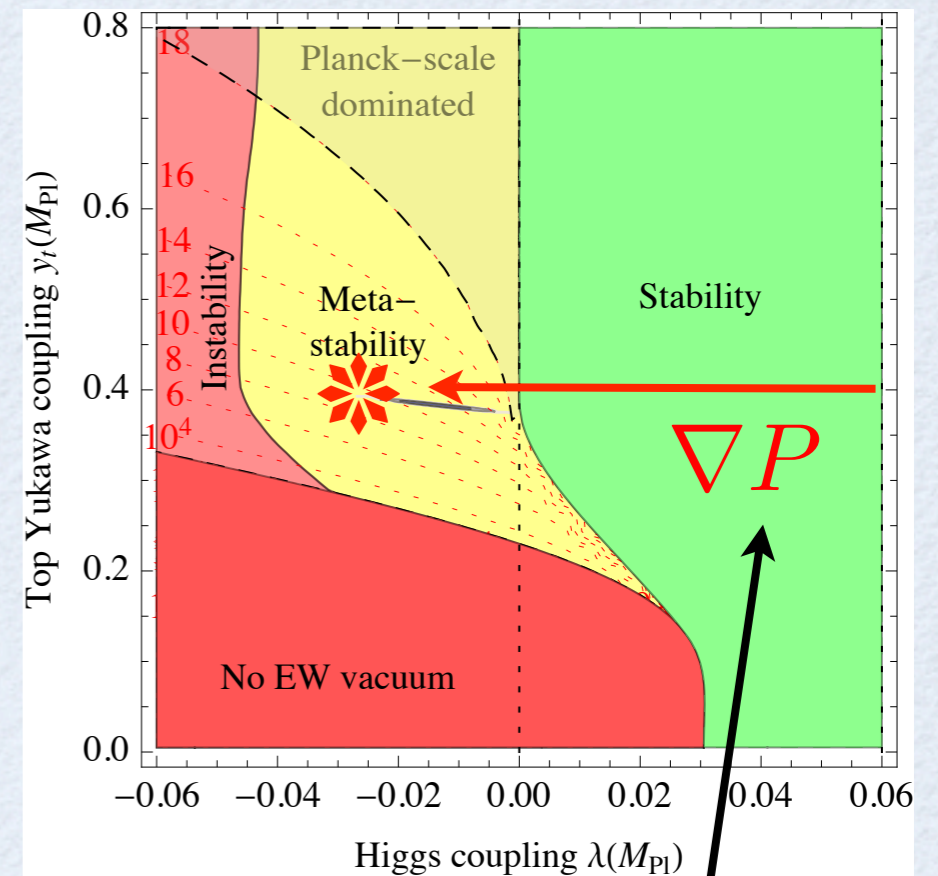
Origin?



# Higgs Mass in MSPQ



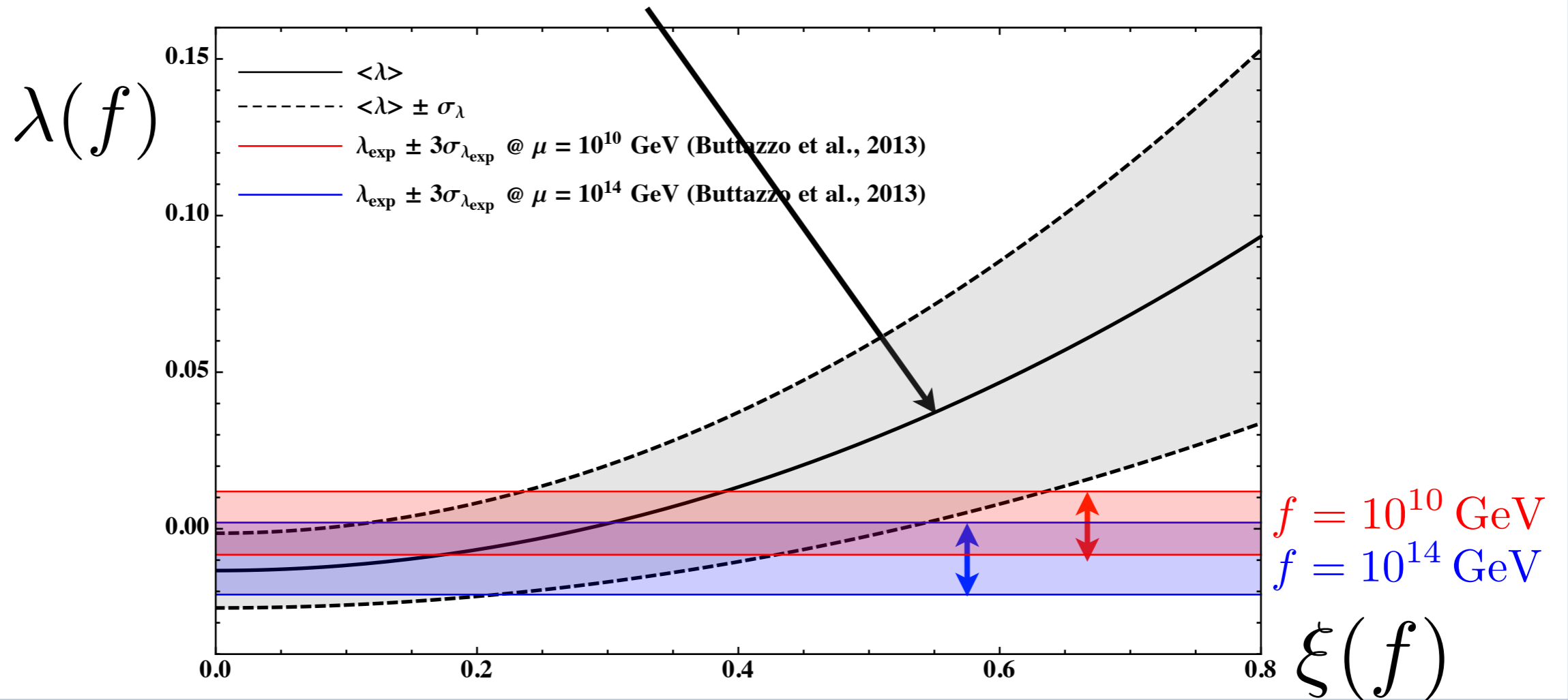
Buttazzo, Degrassi,  
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 1307.3536



Origin?

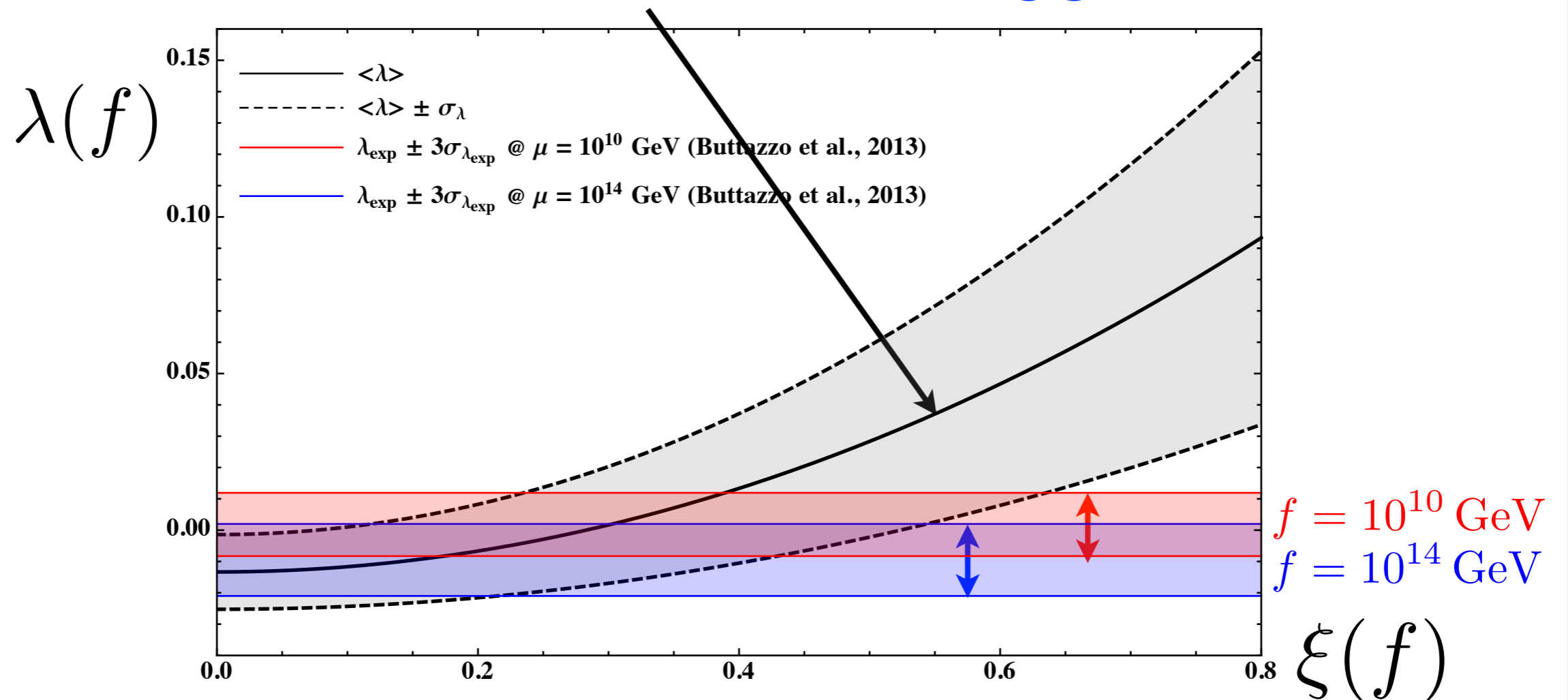
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● Statistical prediction of Higgs mass



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- Radiative PQB:  $f$  from dim. trans.
- Environmental selection:  $v \ll \tilde{m} \sim f$
- DM and Strong CP: Axions

# Conclude: A Multiverse View

Two  
surprises

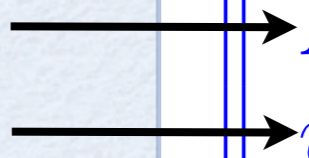
Observable	Physical Origin
$\Lambda$	Observer dilution
$\nu$	Avoid ${}^4\text{He}$ universe
$m_{u,d,e}$	H, complex nuclei
$\xi_D$	Large Scale Structure
$\xi_B$	Observer dilution
$m_H$	EW vacuum stability

Non  
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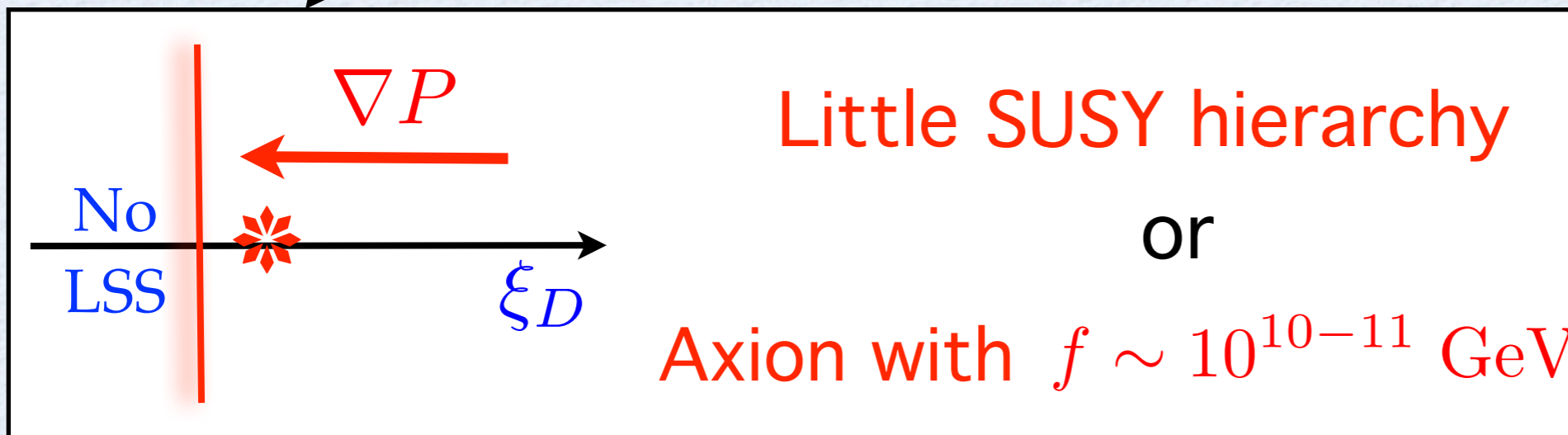
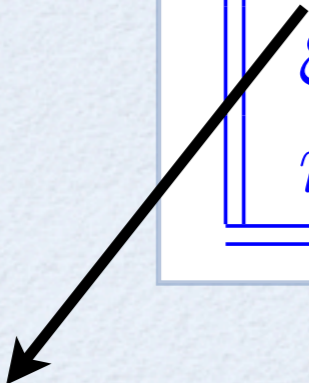
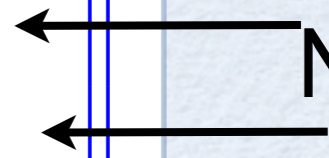
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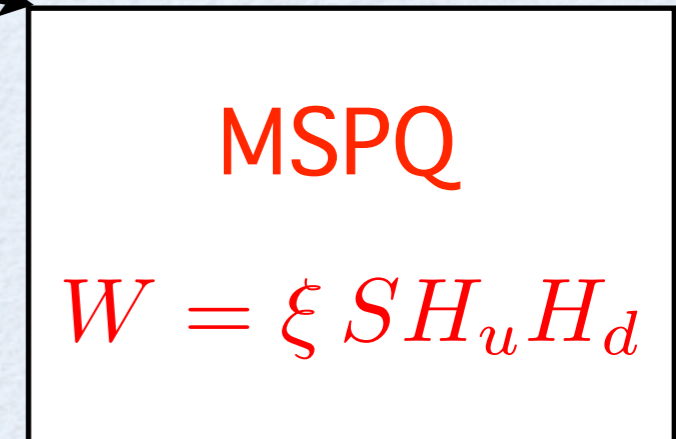
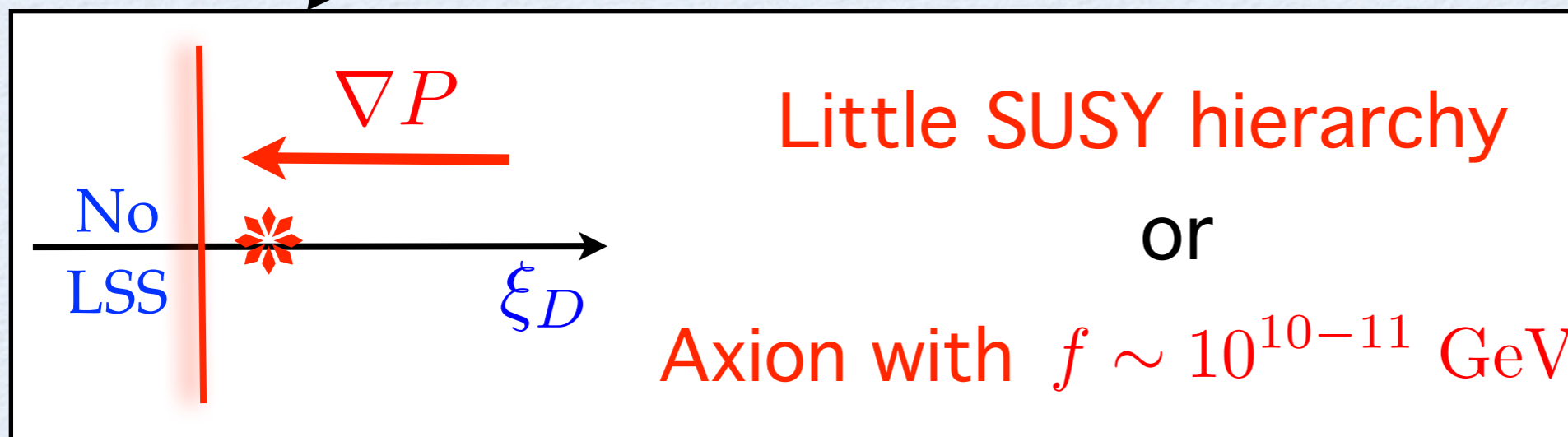


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# The Troubling Question

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How will we ever be sure?

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## How will we ever be sure?

- We may never have a high level of certainty
- The situation is similar to other great ideas  
(inflation, grand unification, string theory; seesaw neutrinos/leptogenesis)
- I aim not to convince you, but to challenge you
- We should seek evidence wherever we can



# The MeV Scale

*Several aspects of our Universe*

*-- some of which seem to be prerequisites for the evolution of any form of life--  
depend rather delicately on apparent coincidences among the physical constants*

Carr, Rees  
Nature (1979)

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$m_e$	$(m_n - m_p)_{EM}$	$(m_n - m_p)_q$	$T_{n \leftrightarrow p}$
$\uparrow$	$\uparrow$	$\uparrow$	$\uparrow$
$y_e v$	$\alpha \Lambda_{QCD}$	$(y_d - y_u)v$	$\frac{v^{4/3}}{M_{Pl}^{1/3}}$

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All four are within a factor 2 of 1 MeV