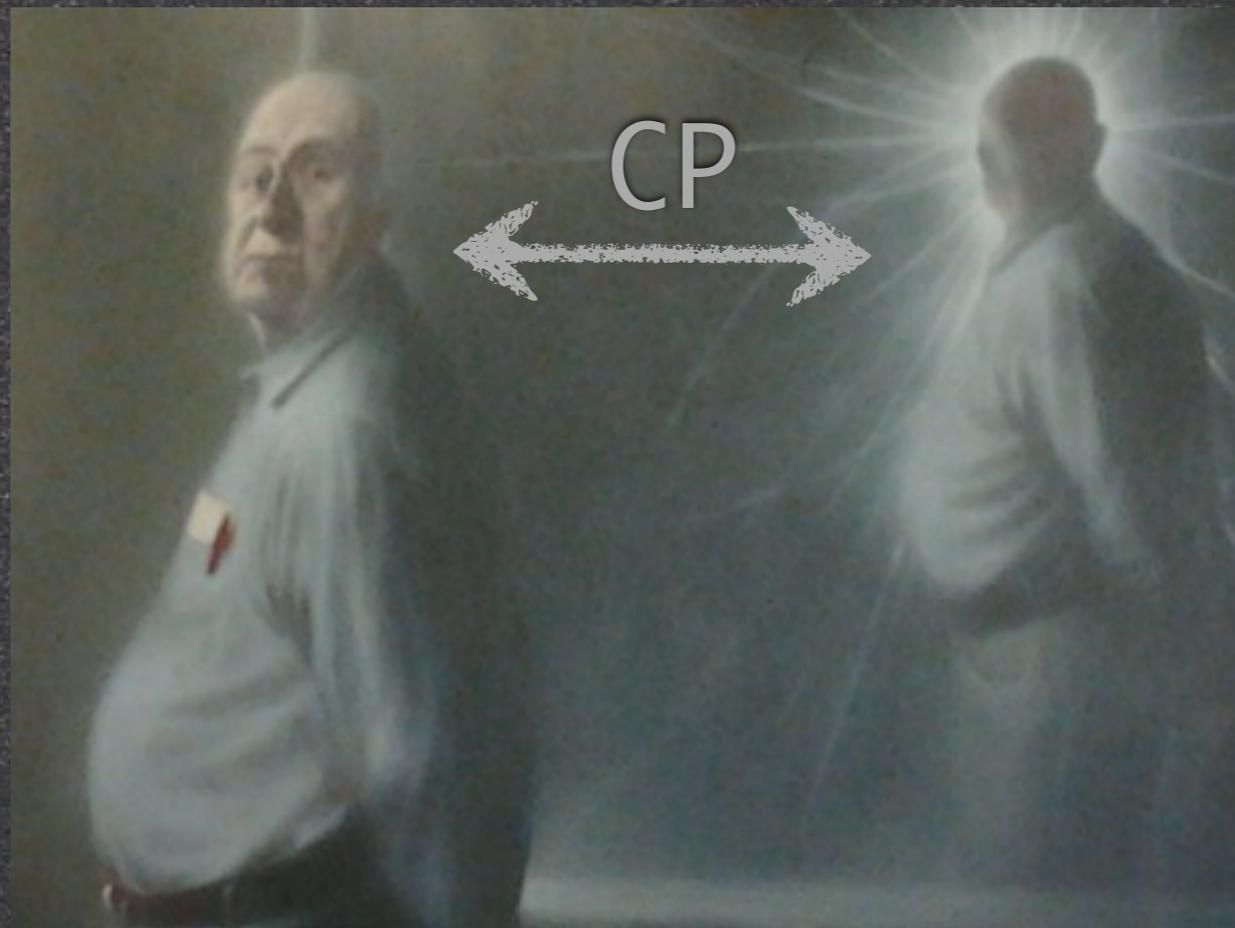


Adam Falkowski

LPT Orsay

CP Violation in 3-body Higgs Decays



Paris, 26 May 2014

Based on a paper with Yi Chen, Ian Low, Roberto Vega-Morales, 1405.xxxx

Plan

- CP violating Higgs couplings
- CP violating observables in Higgs physics
- New CP violating observable

Yi Chen, AA, Ian Low, Roberto Vega-Morales, 1405.xxxx

SM Higgs couplings

$$\mathcal{L}_{\text{SM}} = D_\mu H^\dagger D_\mu H + m_H^2 H^\dagger H - \lambda (H^\dagger H)^2 + \left(\frac{y_{ij}}{\sqrt{2}} H \bar{\psi}_i \psi_j + \text{h.c.} \right) + \dots$$

No Higgs

Couplings to
EW gauge
bosons

Self-
Couplings

Couplings to
fermions

$$H = \frac{1}{\sqrt{2}} \begin{pmatrix} \dots \\ v + h + \dots \end{pmatrix}$$

$$\left(\frac{h}{v} + \frac{h^2}{2v^2} \right) (2m_W^2 W_\mu^+ W_\mu^- + m_Z^2 Z_\mu Z_\mu)$$

$$-\frac{m_h^2}{2v} h^3 - \frac{m_h^2}{8v^2} h^4$$

$$-\frac{h}{v} \sum_f m_f \bar{f} f$$

Ensures unitarity of
VV→hh scattering

Ensures unitarity of
VV→VV scattering

Ensures unitarity of
VV→VVVV... scattering

Ensures unitarity of
VV→ff scattering

No CP violating couplings

~~$$-\frac{h}{4v} \tilde{C}_{V_1 V_2} \epsilon^{\mu\nu\rho\sigma} \partial_\mu V_\nu \partial_\rho V_\sigma$$~~

~~$$-i\tilde{y}_f h \bar{f} \gamma_5 f$$~~

BSM Higgs couplings

$$\mathcal{L} = \mathcal{L}_{\text{SM}} + \frac{1}{v} \mathcal{L}_{D=5} + \frac{1}{v^2} \mathcal{L}_{D=6} + \dots$$

Extending SM by higher dimensional operators modifies Higgs couplings existing in SM, and leads to new Higgs couplings with new tensor structures

X^3		φ^6 and $\varphi^4 D^2$		$\psi^2 \varphi^3$	
Q_G	$f^{ABC} G_\mu^{A\nu} G_\nu^{B\rho} G_\rho^{C\mu}$	Q_φ	$(\varphi^\dagger \varphi)^3$	$Q_{e\varphi}$	$(\varphi^\dagger \varphi)(\bar{l}_p e_r \varphi)$
$Q_{\tilde{G}}$	$f^{ABC} \tilde{G}_\mu^{A\nu} G_\nu^{B\rho} G_\rho^{C\mu}$	$Q_{\varphi\Box}$	$(\varphi^\dagger \varphi)\Box(\varphi^\dagger \varphi)$	$Q_{u\varphi}$	$(\varphi^\dagger \varphi)(\bar{q}_p u_r \tilde{\varphi})$
Q_W	$\varepsilon^{IJK} W_\mu^{I\nu} W_\nu^{J\rho} W_\rho^{K\mu}$	$Q_{\varphi D}$	$(\varphi^\dagger D^\mu \varphi)^* (\varphi^\dagger D_\mu \varphi)$	$Q_{d\varphi}$	$(\varphi^\dagger \varphi)(\bar{q}_p d_r \varphi)$
$Q_{\tilde{W}}$	$\varepsilon^{IJK} \tilde{W}_\mu^{I\nu} W_\nu^{J\rho} W_\rho^{K\mu}$				
$X^2 \varphi^2$		$\psi^2 X \varphi$		$\psi^2 \varphi^2 D$	
$Q_{\varphi G}$	$\varphi^\dagger \varphi G_{\mu\nu}^A G^{A\mu\nu}$	Q_{eW}	$(\bar{l}_p \sigma^{\mu\nu} e_r) \tau^I \varphi W_{\mu\nu}^I$	$Q_{\varphi l}^{(1)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{l}_p \gamma^\mu l_r)$
$Q_{\varphi \tilde{G}}$	$\varphi^\dagger \varphi \tilde{G}_{\mu\nu}^A G^{A\mu\nu}$	Q_{eB}	$(\bar{l}_p \sigma^{\mu\nu} e_r) \varphi B_{\mu\nu}$	$Q_{\varphi l}^{(3)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu^I \varphi)(\bar{l}_p \tau^I \gamma^\mu l_r)$
$Q_{\varphi W}$	$\varphi^\dagger \varphi W_{\mu\nu}^I W^{I\mu\nu}$	Q_{uG}	$(\bar{q}_p \sigma^{\mu\nu} T^A u_r) \tilde{\varphi} G_{\mu\nu}^A$	$Q_{\varphi e}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{e}_p \gamma^\mu e_r)$
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$Q_{\varphi \tilde{B}}$	$\varphi^\dagger \varphi \tilde{B}_{\mu\nu} B^{\mu\nu}$	Q_{dG}	$(\bar{q}_p \sigma^{\mu\nu} T^A d_r) \varphi G_{\mu\nu}^A$	$Q_{\varphi u}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{u}_p \gamma^\mu u_r)$
$Q_{\varphi WB}$	$\varphi^\dagger \tau^I \varphi W_{\mu\nu}^I B^{\mu\nu}$	Q_{dW}	$(\bar{q}_p \sigma^{\mu\nu} d_r) \tau^I \varphi W_{\mu\nu}^I$	$Q_{\varphi d}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{d}_p \gamma^\mu d_r)$
$Q_{\varphi \tilde{W}B}$	$\varphi^\dagger \tau^I \varphi \tilde{W}_{\mu\nu}^I B^{\mu\nu}$	Q_{dB}	$(\bar{q}_p \sigma^{\mu\nu} d_r) \varphi B_{\mu\nu}$	$Q_{\varphi ud}$	$i(\tilde{\varphi}^\dagger D_\mu \varphi)(\bar{u}_p \gamma^\mu d_r)$

Table 2: Dimension-six operators other than the four-fermion ones.

Grzadkowski et al.
1008.4884

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Some of these operators violate CP, either via CP violating tensor structures, or via CP violating complex couplings

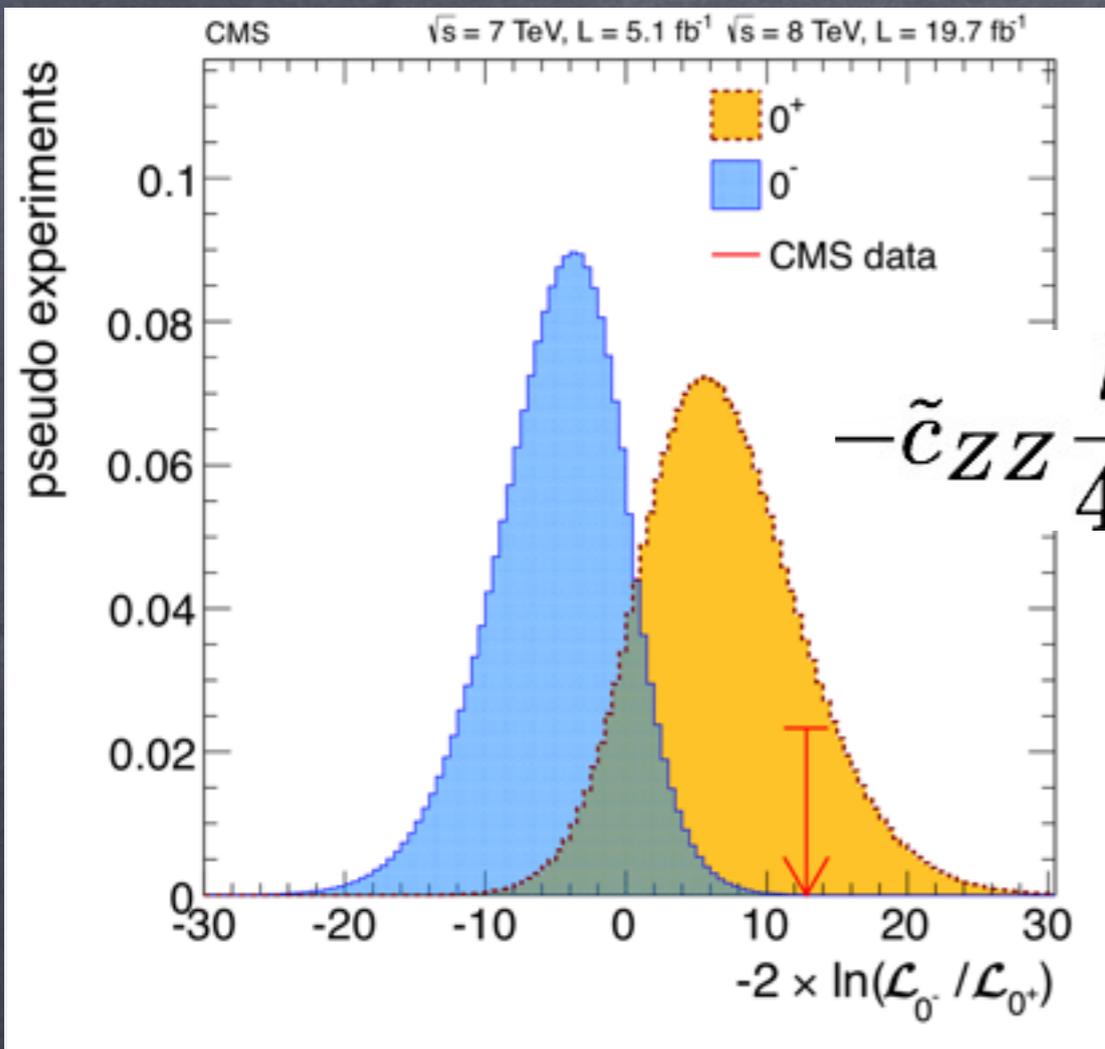
CP violating Higgs couplings to EW bosons

$$\mathcal{L}_{\text{CPV}} \supset -\frac{h}{4v} \epsilon^{\mu\nu\rho\sigma} [\tilde{c}_{\gamma\gamma} \partial_\mu A_\nu \partial_\rho A_\sigma + 2\tilde{c}_{Z\gamma} \partial_\mu Z_\nu \partial_\rho A_\sigma + \tilde{c}_{ZZ} \partial_\mu Z_\nu \partial_\rho Z_\sigma]$$

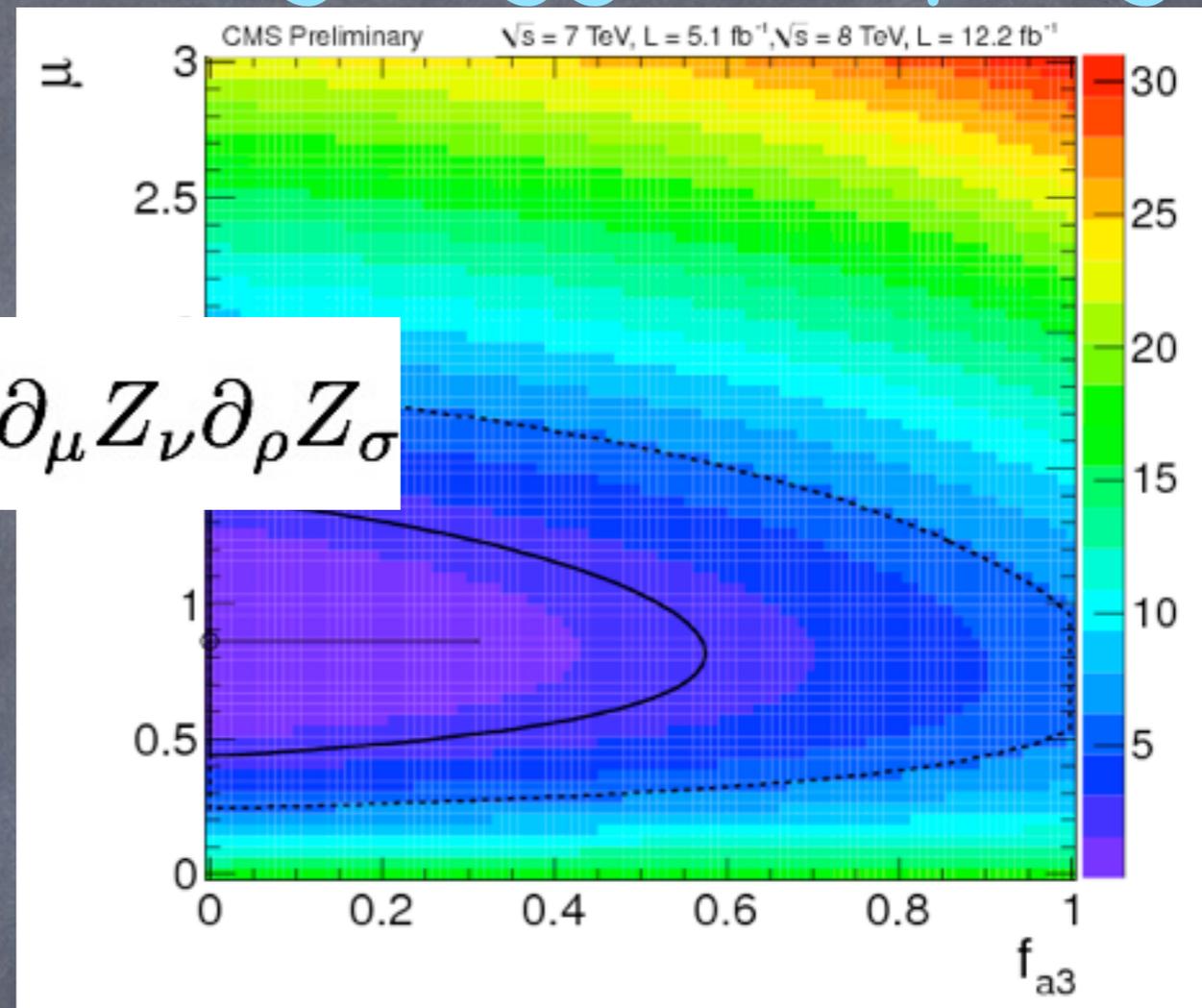
- Not present in SM at tree level; induced in effective action at 3-loop level, thus SM predicts they are zero for all practical purpose
- Very weak experimental constraints so far
- Higgs inclusive rates in given channel depends on squares of CP violating couplings, so corrections expected very small
- We should look at exclusive observables

see e.g.
Belusca-Maito
[1404.5343](#)

LHC constraints on CP violating Higgs couplings



$$-\tilde{c}_{ZZ} \frac{h}{4v} \epsilon^{\mu\nu\rho\sigma} \partial_\mu Z_\nu \partial_\rho Z_\sigma$$



- Only tells that pure SM coupling to ZZ preferred over pure CP violating coupling to ZZ

- Useless at this point

- A step in the right direction
- Should be marginalized over other Higgs couplings to give a useful bound

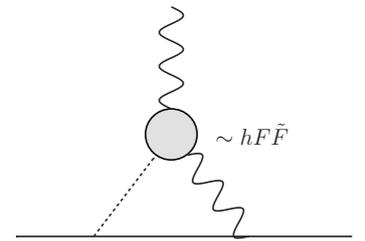
How to search for CP violating Higgs couplings

- Indirect: CP violating effects in low energy precision experiments
- Semi-direct: kinematic distributions sensitive to different momentum dependence of CP violating Higgs couplings
- Direct: genuinely CP violating observables in Higgs production and decay

Even here you need to close the circle, since EDM constraints assume 1st gen Higgs couplings that you can't measure

γ operator:
already severely constrained
by e and q EDMs

McKeen, Pospelov, Ritz '12

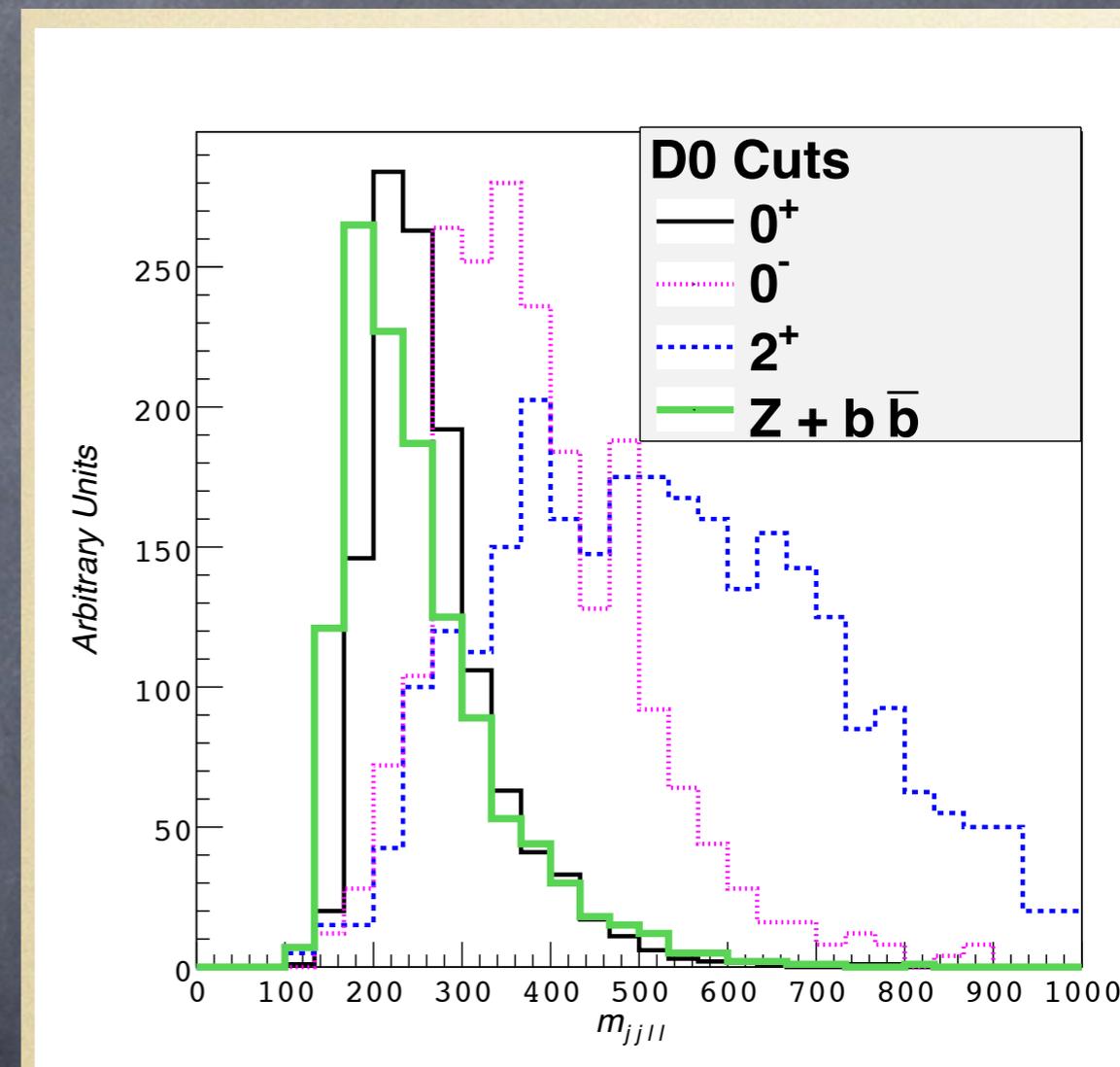


Christophe Grojean

Joseph Lykken

How to search for CP violating Higgs couplings

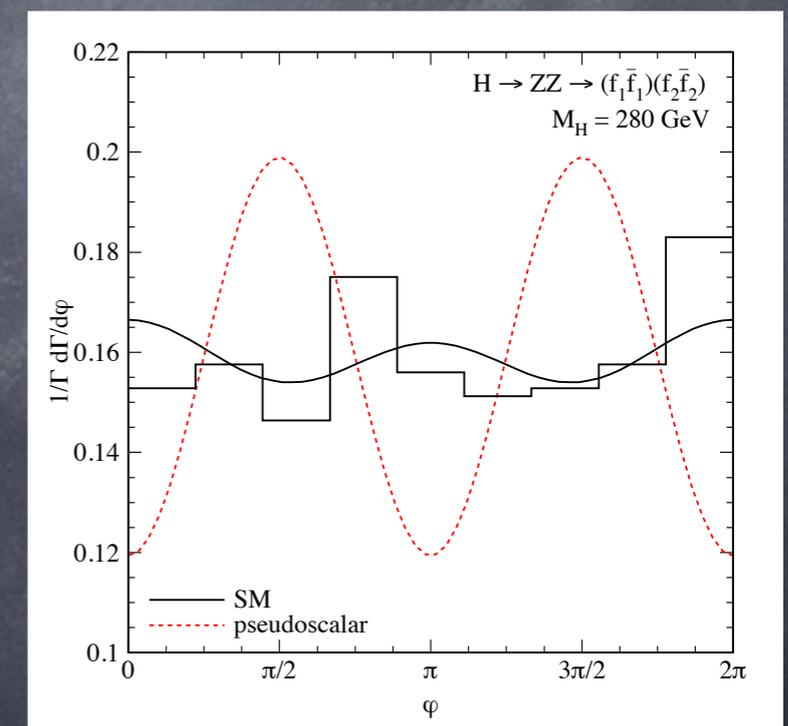
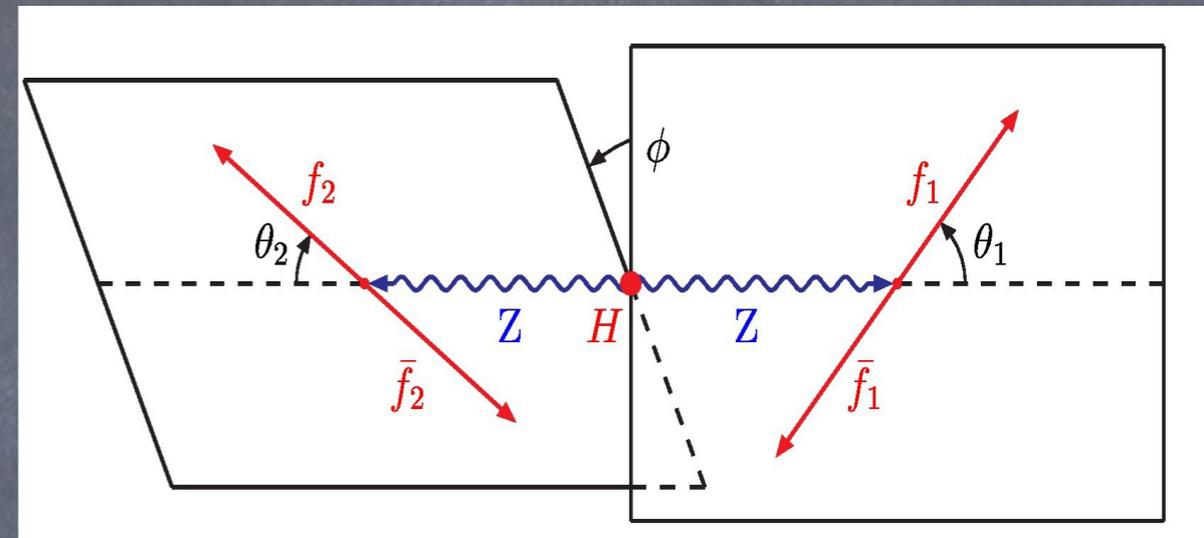
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Ellis, Hwang, VS, You. 1208.6002

How to search for CP violating Higgs couplings

- Indirect: CP violating effects in low energy precision experiments
- Semi-direct: kinematic distributions sensitive to different momentum dependence of CP violating Higgs couplings
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Miller et al.
hep-ph/0210077

CP violation and strong phases

- For Higgs decay, simple asymmetry for decays into CP conjugate states F and F bar requires interference of 2 amplitudes with different weak AND strong phases
- In absence of strong phases, one needs to resort to triple product asymmetries, which require 4 visible momenta in final state

$$\mathcal{M}_{h \rightarrow F} = |c_1| e^{i(\delta_1 + \phi_1)} + |c_2| e^{i(\delta_2 + \phi_2)}$$
$$\mathcal{M}_{h \rightarrow \bar{F}} = |c_1| e^{i(\delta_1 - \phi_1)} + |c_2| e^{i(\delta_2 - \phi_2)}$$

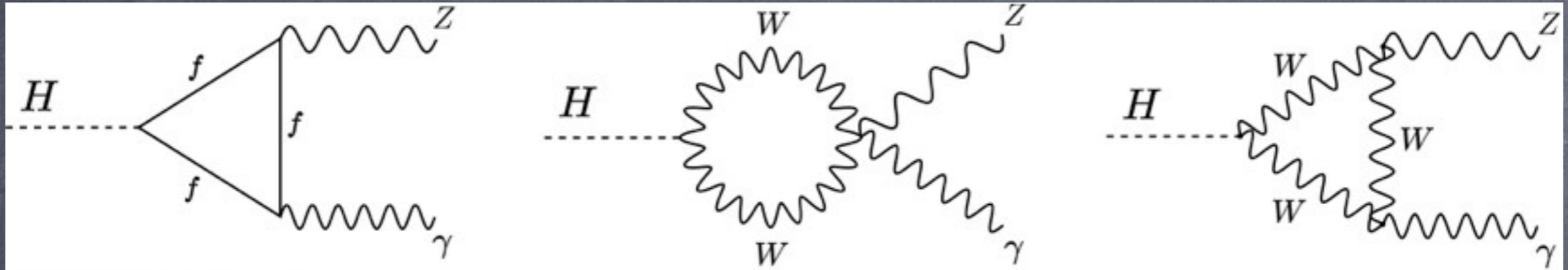
$$A_{\text{CP}} = \frac{d\Gamma_{h \rightarrow F} - d\Gamma_{h \rightarrow \bar{F}}}{d\Gamma_{h \rightarrow F} + d\Gamma_{h \rightarrow \bar{F}}}$$
$$\propto |c_1| |c_2| \sin(\delta_1 - \delta_2) \sin(\phi_1 - \phi_2)$$

$$\cos \phi = \frac{(\vec{p}_1 \times \vec{p}_2) \cdot (\vec{p}_3 \times \vec{p}_4)}{|\vec{p}_1 \times \vec{p}_2| |\vec{p}_3 \times \vec{p}_4|},$$

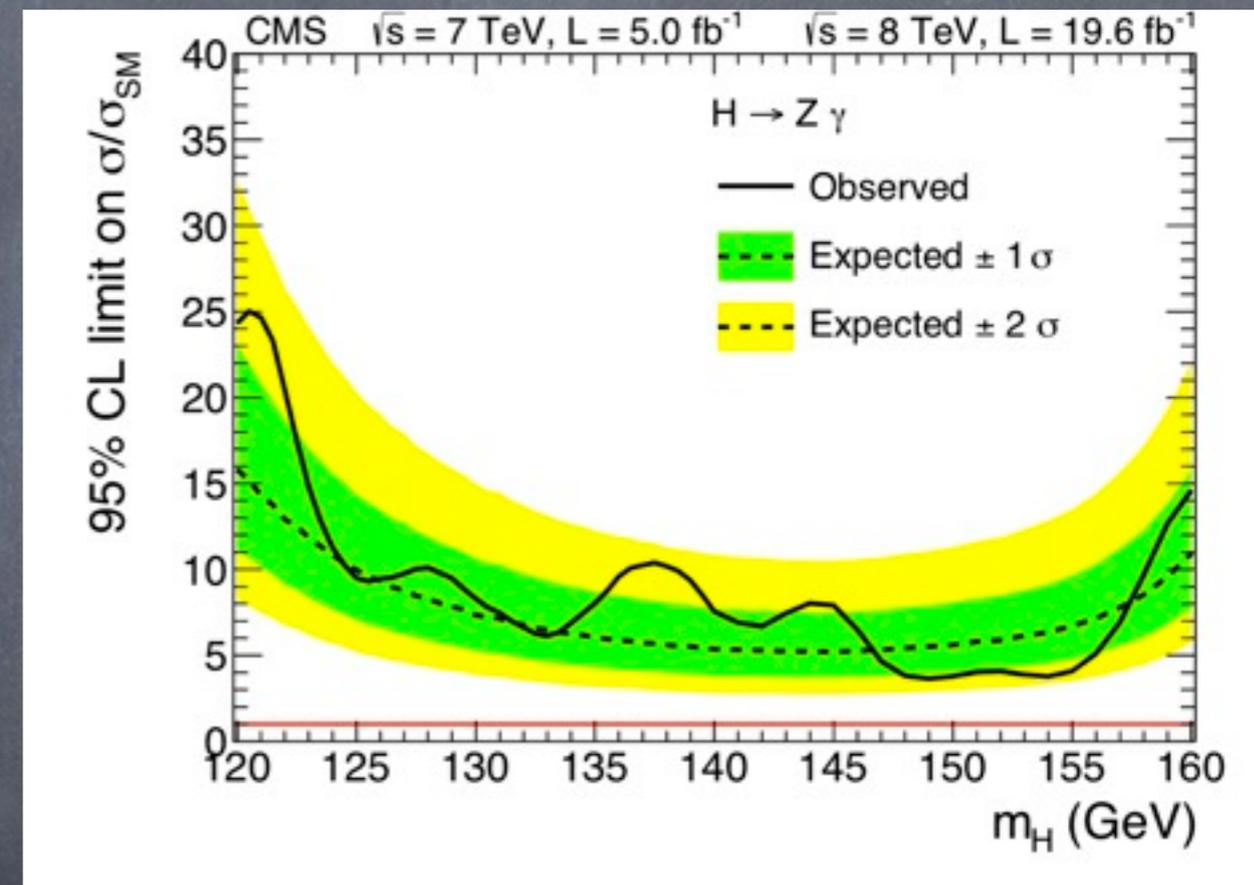
CP violation in 3-body Higgs decays

- New CP violating observable in certain 3-body Higgs decays that requires only 3 reconstructed momenta
- Analogous observables discussed to death in flavor physics, in context of BSM decay studied by Berger, Blanke, Grossman 1105.0672, but afaik no discussion in context of Higgs physics
- In Higgs decays, strong phase provided by the Breit-Wigner propagator of the Z boson, while weak phases may arise due to CP violating Higgs couplings
- Example: forward-backward asymmetry of lepton in $h \rightarrow (Z/\gamma)\gamma \rightarrow l-l+\gamma$ decays

Higgs decays to $Z\gamma$ in SM



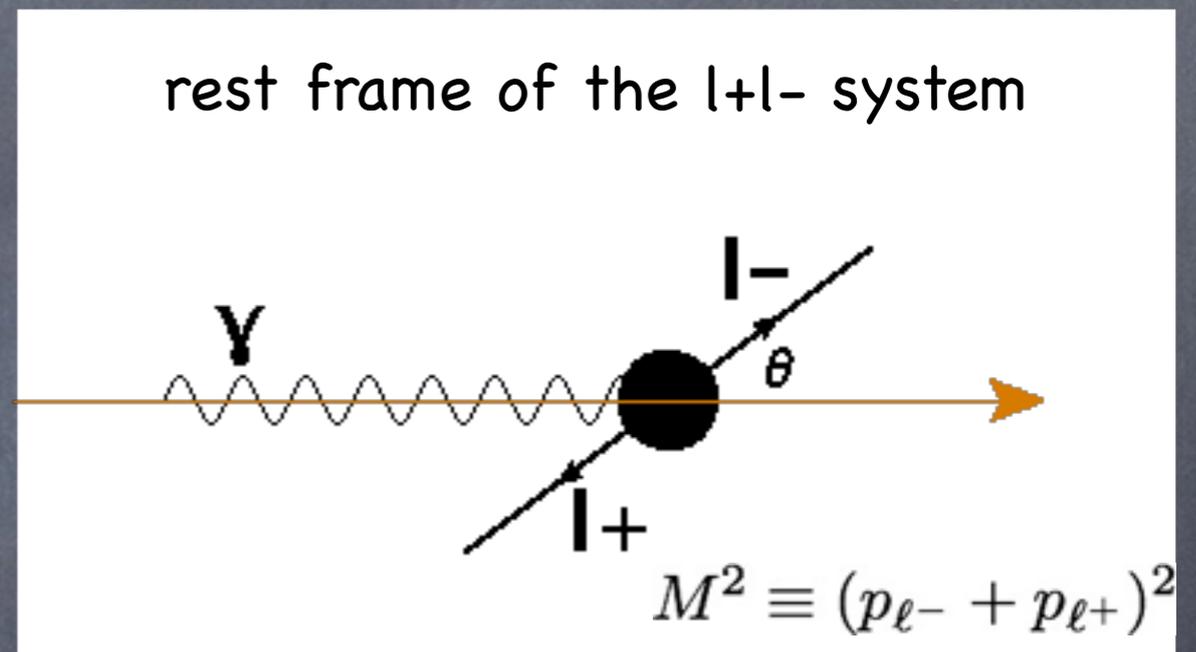
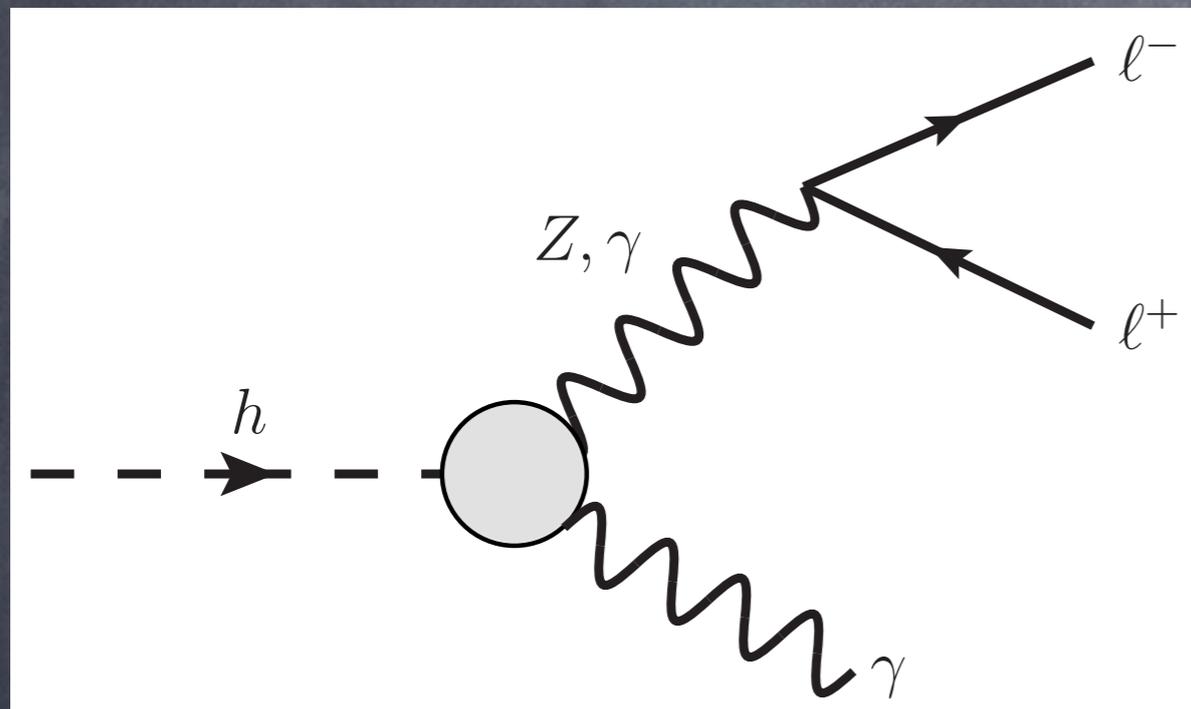
- In SM, loop level decays with branching fraction 0.16%
- Current limits order of magnitude larger
- Room for large CP violating Higgs coupling to $Z\gamma$ from BSM



Higgs decays to $Z\gamma$ in BSM

$$-\frac{h}{4v} \left(2c_{Z\gamma} A^{\mu\nu} Z_{\mu\nu} + 2\tilde{c}_{Z\gamma} A^{\mu\nu} \tilde{Z}_{\mu\nu} + c_{\gamma\gamma} A^{\mu\nu} A_{\mu\nu} + \tilde{c}_{\gamma\gamma} A^{\mu\nu} \tilde{A}_{\mu\nu} \right)$$

SM: $|c_{Z\gamma}| \sim 0.015$, $|c_{\gamma\gamma}| \sim 0.0077$, $\tilde{c}_{Z\gamma} \approx \tilde{c}_{\gamma\gamma} \approx 0$



$$\frac{d\Gamma}{dM^2 d\cos\theta} = (1 + \cos^2\theta) \frac{d\Gamma_{\text{CPC}}}{dM^2} + \cos\theta \frac{d\Gamma_{\text{CPV}}}{dM^2}$$

$$\frac{d\Gamma_{\text{CPV}}}{dM^2} = (c_{Z\gamma}\tilde{c}_{\gamma\gamma} - c_{\gamma\gamma}\tilde{c}_{Z\gamma}) \times \frac{e(g_{Z,R} - g_{Z,L})m_Z\Gamma_Z(m_h^2 - M^2)^3}{512\pi^3 m_h^3 v^2 ((M^2 - m_Z^2)^2 + m_Z^2\Gamma_Z^2)}$$

Asymmetric part manifestly CP odd

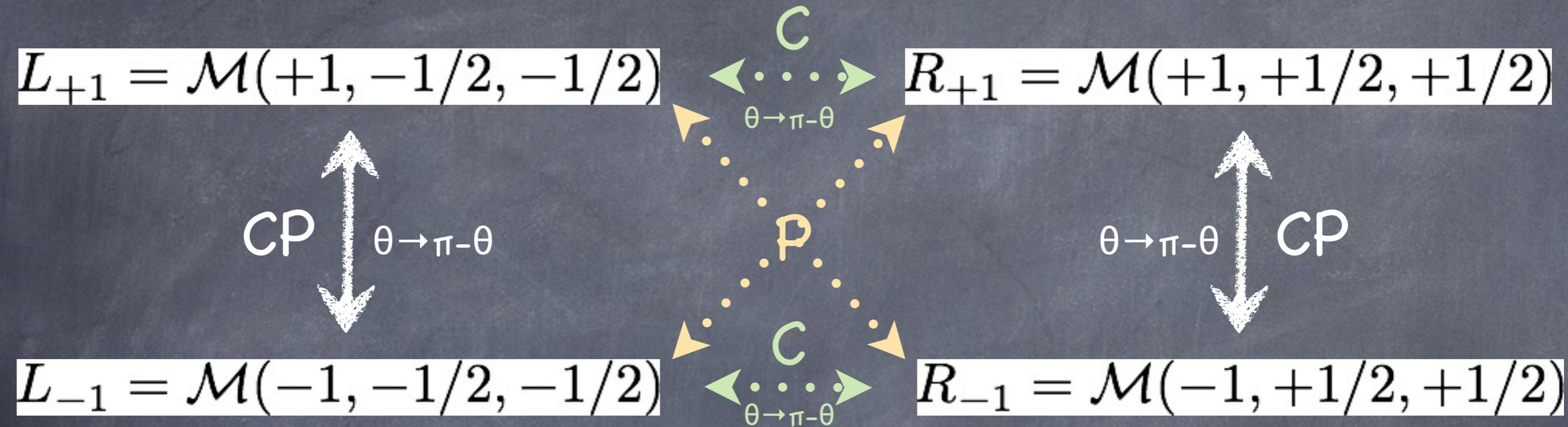
CP violation in $h \rightarrow l-l+\gamma$ decays

$$\frac{d\Gamma_{CPV}}{dM^2} = (c_{Z\gamma}\tilde{c}_{\gamma\gamma} - c_{\gamma\gamma}\tilde{c}_{Z\gamma}) \times \frac{e(g_{Z,R} - g_{Z,L})m_Z\Gamma_Z(m_h^2 - M^2)^3}{512\pi^3 m_h^3 v^2 ((M^2 - m_Z^2)^2 + m_Z^2\Gamma_Z^2)}$$

- CP violation is proportional to CP odd Higgs couplings to $Z\gamma$ or $\gamma\gamma$ who provide weak phases
- CP violation is proportional to the width of Z who provides the strong phase
- It leads to forward-backward asymmetry of lepton direction in rest frame of $l+l-$ system

$$A_{FB}(M) = \frac{\left(\int_0^1 - \int_{-1}^0\right) d\cos\theta \frac{d\Gamma}{dM^2 d\cos\theta}}{\left(\int_0^1 + \int_{-1}^0\right) d\cos\theta \frac{d\Gamma}{dM^2 d\cos\theta}} = \frac{3}{8} \frac{d\Gamma_{CPV}/dM^2}{d\Gamma_{CPC}/dM^2}$$

CP violation in $h \rightarrow l-l+\gamma$ decays



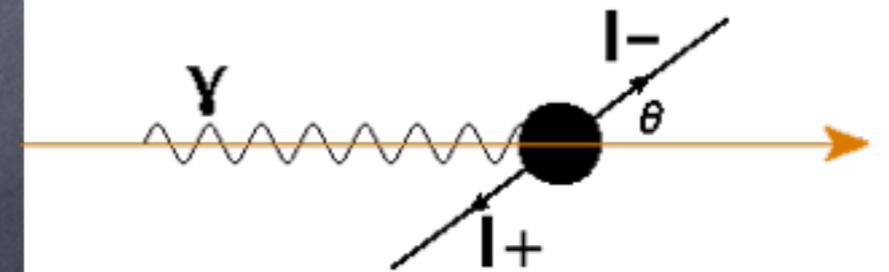
$$d\Gamma \sim |L_{+1}(\cos \theta)|^2 + |L_{-1}(\cos \theta)|^2 + |R_{+1}(\cos \theta)|^2 + |R_{-1}(\cos \theta)|^2$$

CP conserved \Rightarrow

$$L_{+1}(\cos \theta) = L_{-1}(-\cos \theta)$$

$$R_{+1}(\cos \theta) = R_{-1}(-\cos \theta)$$

rest frame of the $l+l-$



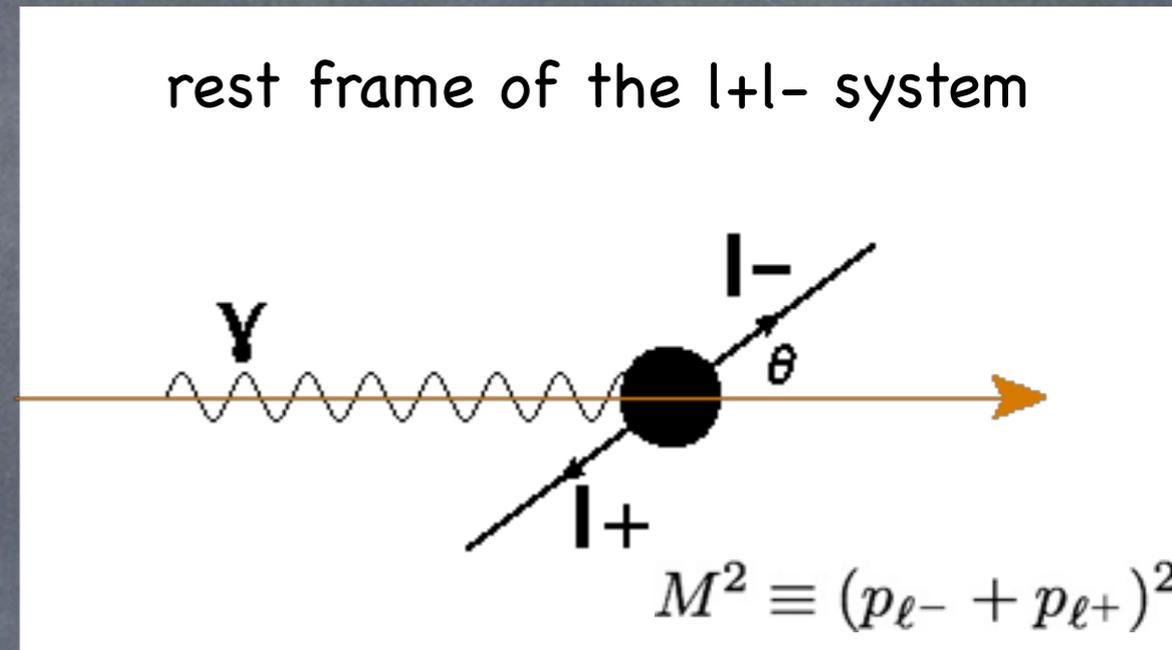
$$d\Gamma \sim |L_{+1}(\cos \theta)|^2 + |L_{+1}(-\cos \theta)|^2 + |R_{+1}(\cos \theta)|^2 + |R_{+1}(-\cos \theta)|^2$$

Asymmetry in $\cos \theta$ implies C and CP violation

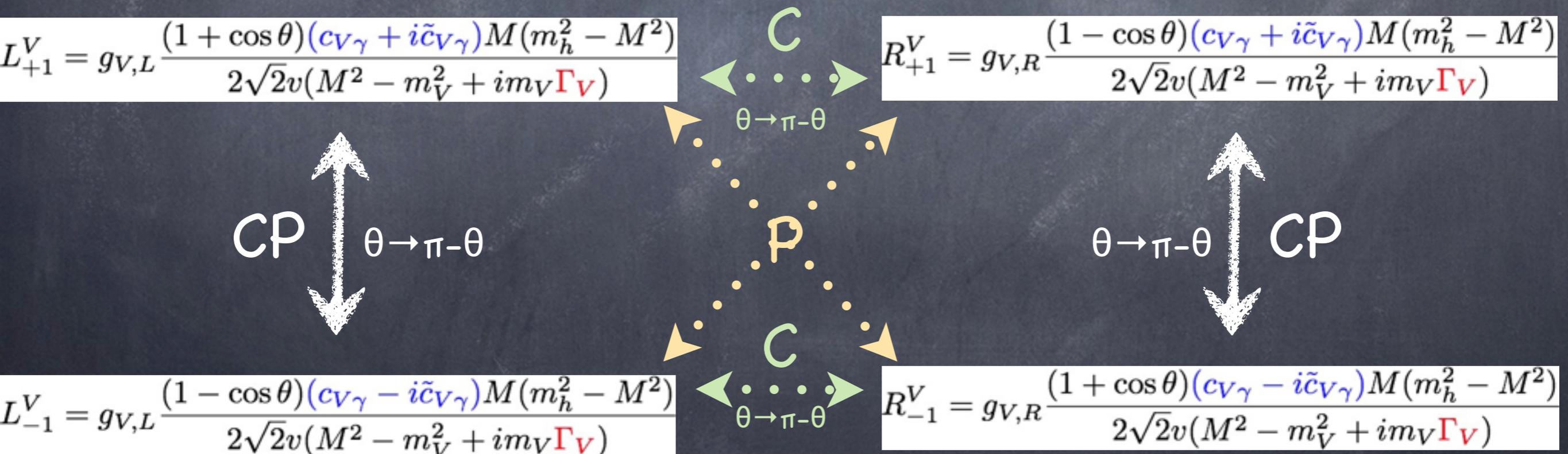
CP violation in $h \rightarrow l^- l^+ \gamma$ decays

Two interfering diagrams with intermediate Z or γ

$$\mathcal{M}(h \rightarrow l^- l^+ \gamma) = \mathcal{M}^Z + \mathcal{M}^\gamma$$



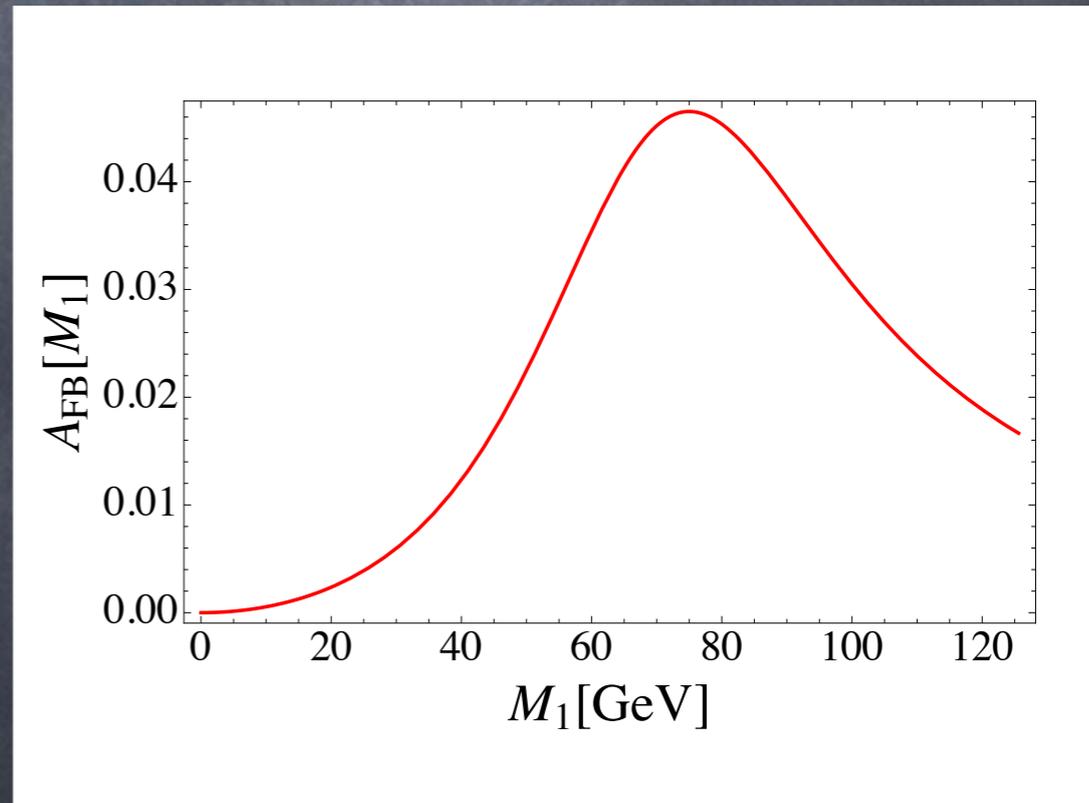
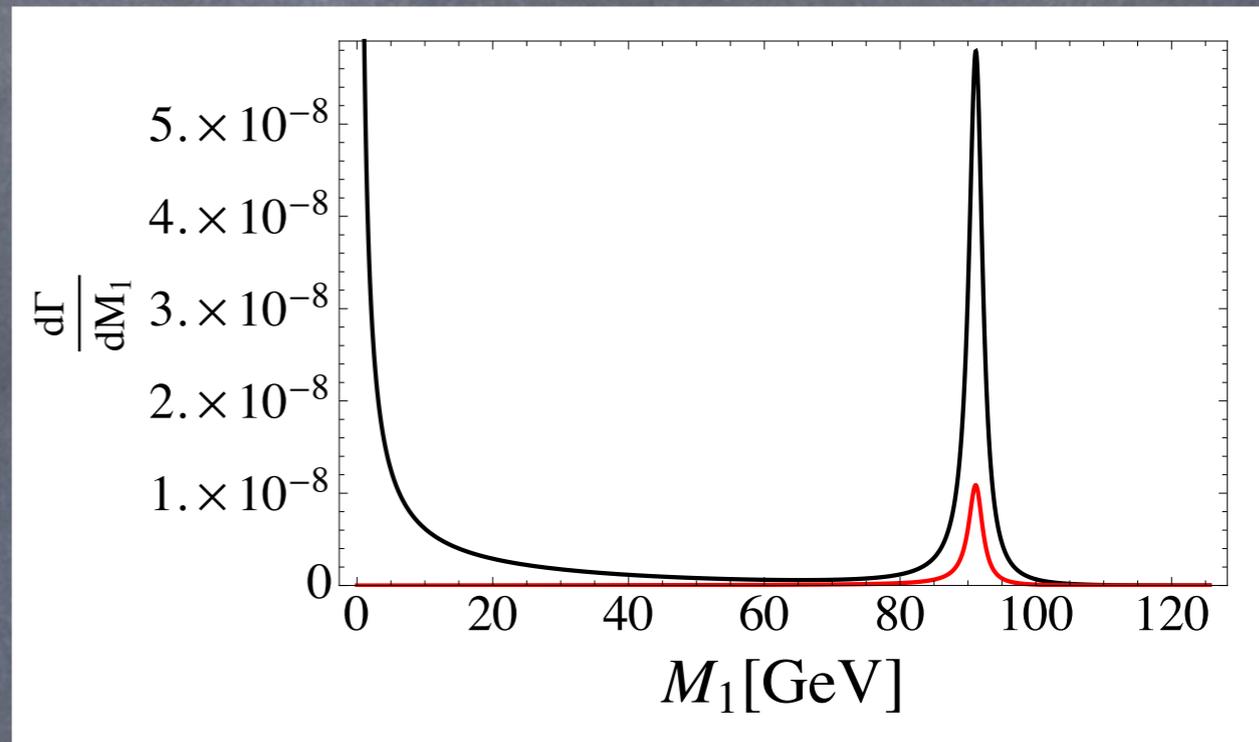
Each diagram has different strong and weak phase



CP violation in $h \rightarrow l-l+\gamma$ decays

$$\frac{d\Gamma_{CPV}}{dM^2} = (c_{Z\gamma}\tilde{c}_{\gamma\gamma} - c_{\gamma\gamma}\tilde{c}_{Z\gamma}) \times \frac{e(g_{Z,R} - g_{Z,L})m_Z\Gamma_Z(m_h^2 - M^2)^3}{512\pi^3 m_h^3 v^2 ((M^2 - m_Z^2)^2 + m_Z^2\Gamma_Z^2)}$$

- Both symmetric and anti-symmetric peak at the Z pole \rightarrow one can use narrow width approximation for both
- Dependence on axial coupling to Z is because C needs to be violated as well

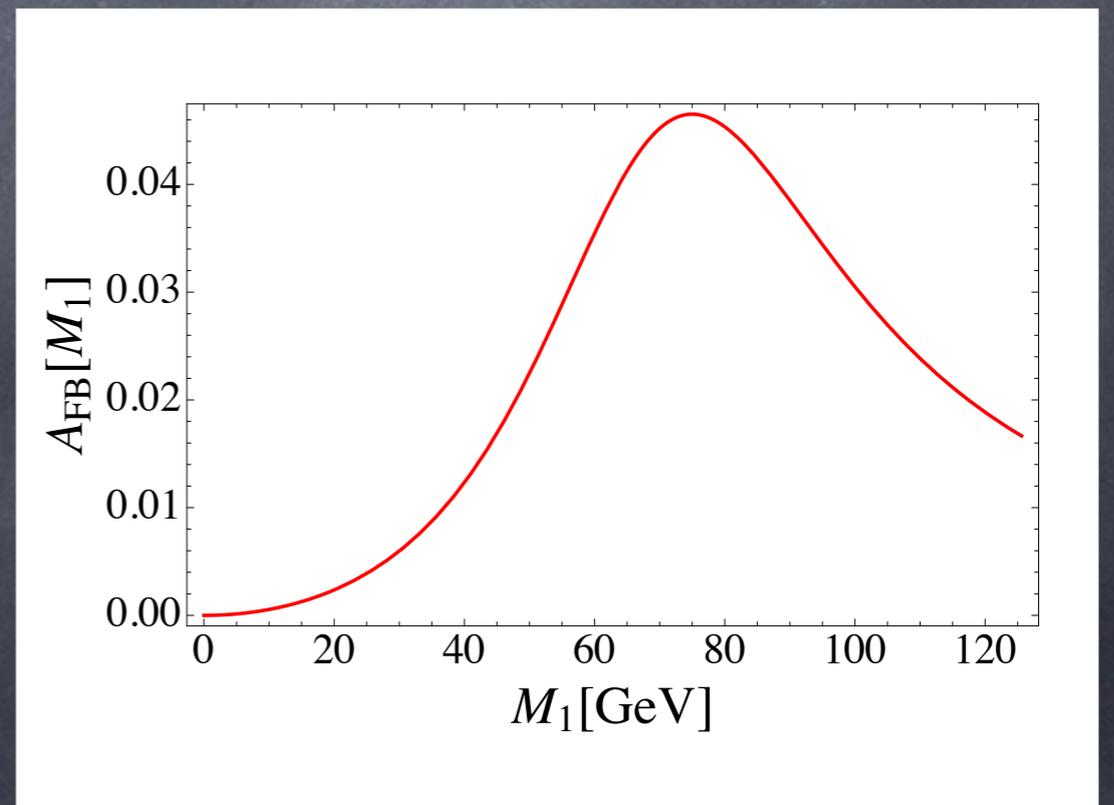


CP violation in $h \rightarrow l-l+\gamma$ decays

- Integrated asymmetry suppressed by Γ_Z/m_Z , but otherwise no parametric suppression
- 5% asymmetry possible if CP violating Higgs couplings of the same order as conserving ones
- Larger asymmetry possible if effective Higgs coupling to $Z\gamma$ smaller than in SM

$$\bar{A}_{\text{FB}} \sim \frac{\Gamma_Z}{m_Z} \frac{c_{Z\gamma} \tilde{c}_{\gamma\gamma} - c_{\gamma\gamma} \tilde{c}_{Z\gamma}}{c_{Z\gamma}^2 + \tilde{c}_{Z\gamma}^2}$$

$$\bar{A}_{\text{FB}} \approx 0.07 \frac{c_{Z\gamma} \tilde{c}_{\gamma\gamma} - c_{\gamma\gamma} \tilde{c}_{Z\gamma}}{c_{Z\gamma}^2 + \tilde{c}_{Z\gamma}^2}$$



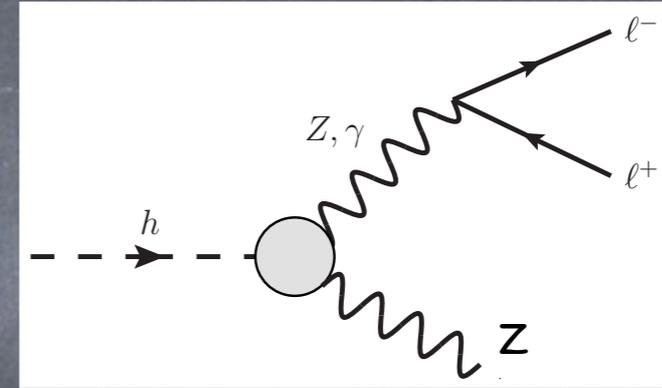
CP violation in $h \rightarrow l-l+\gamma$ decays in LHC

- $h \rightarrow Z\gamma$ with leptonic Z decay routinely searched for
- For CP violation, one has to fight not only symmetric Higgs background, but also symmetric non-Higgs SM background
- Standard cut-based analysis in $h \rightarrow Z\gamma$ channel has signal to background of order 1/100. Then sensitivity estimated as

$$\frac{S}{\sqrt{B}} \sim \left(\frac{A_{\text{FB}}}{0.1} \right) \sqrt{\frac{L}{3000 \text{ fb}^{-1}}}$$

Better signal to background using matrix element methods implies better sensitivity

Related CP violating Higgs processes



- $h \rightarrow l^- l^+ Z$: asymmetry more suppressed because of symmetric part profiting from tree-level hZZ coupling c_V

$$A_{\text{FB}}(h \rightarrow l^- l^+ Z) \sim \frac{\Gamma_Z}{m_Z} \frac{\tilde{c}_{Z\gamma}}{c_V} \lesssim 10^{-3}$$

- $e^- e^+ \rightarrow h Z$: asymmetry more suppressed in by additional m_Z/E

$$\bar{A}_{\text{FB}}(e^- e^+ \rightarrow h Z) \sim \frac{\Gamma_Z m_Z}{s} \frac{\tilde{c}_{Z\gamma}}{c_V} \lesssim 10^{-4}$$

- $e^- e^+ \rightarrow h \gamma$: large asymmetry but small rate

$$\bar{A}_{\text{FB}}(f \bar{f} \rightarrow h \gamma) \sim \frac{\Gamma_Z}{m_Z} \frac{c_{Z\gamma} \tilde{c}_{\gamma\gamma} - c_{\gamma\gamma} \tilde{c}_{Z\gamma}}{c_{Z\gamma}^2 + \tilde{c}_{Z\gamma}^2} \lesssim 10^{-1}$$

To take out

- A new class of CP violating observables in Higgs physics not relying on triple product asymmetries
- Can be applied to Higgs decay involving 3 observable particle: a pair of CP conjugate + 1 neutral particle
- Also relevant for 2-to-2 scattering processes with a pair of CP conjugate + Higgs + 1 other neutral particle
- Can be studied at hadron or lepton colliders
- New handle on CP violating Higgs couplings to Z and γ