## TESTING THE HIGGS BOSON THROUGH PAIR PRODUCTION

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#### What can we learn from double-Higgs production ?

1. Measure couplings not accessible through single-Higgs processes



2. (further) Test the Higgs as an  $SU(2)_{L}$  doublet

3. Probe the strength of EWSB dynamics at higher energies

General parametrization of Higgs couplings: non-linear Lagrangian

$$\begin{aligned} \mathcal{L} &= \frac{1}{2} \partial_{\mu} h \; \partial^{\mu} h - \frac{1}{2} m_{h}^{2} h^{2} - c_{3} \; \frac{1}{6} \left( \frac{3m_{h}^{2}}{v} \right) h^{3} + \dots \\ &- \sum_{\psi=u,d,l} m_{\psi^{(i)}} \; \bar{\psi}^{(i)} \psi^{(i)} \left( 1 + c_{\psi} \frac{h}{v} + c_{2\psi} \frac{h^{2}}{v^{2}} + \dots \right) \\ &+ \left( m_{W}^{2} W_{\mu}^{+} W^{-\mu} + \frac{1}{2} m_{Z}^{2} Z_{\mu} Z^{\mu} \right) \left( 1 + 2c_{V} \frac{h}{v} + c_{2V} \frac{h^{2}}{v^{2}} + \dots \right) \\ &+ \frac{\alpha_{s}}{\pi} \; G_{\mu\nu}^{a} G^{a\mu\nu} \left( c_{g} \frac{h}{v} + \frac{c_{gg}}{2} \frac{h^{2}}{v^{2}} + \dots \right) + \dots \end{aligned}$$

- Assumptions: 1) spin-0, custodial singlet Higgs; 2) New Physics is heavy
- All terms can be dressed up with EW Nambu-Goldstone bosons and made manifestly invariant under SU(2)<sub>L</sub>xU(1)<sub>Y</sub>

• Naively: 
$$\delta c_i \equiv (c_i - 1) \sim O\left(\frac{g_*^2 v^2}{m_*^2}\right)$$

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Current data constrain single-Higgs couplings to be close to the SM point

$$\delta c_i \lesssim O(20 - 30\%)$$

The SM point is special in that the theory stays weakly-coupled up to very high scales

How to live near the SM point:

1. The new boson is part of an  $SU(2)_L$  doublet

$$H = e^{i\pi/v} \begin{pmatrix} 0\\ v+h \end{pmatrix}$$

2. There is a gap between the NP scale and  $m_h$ 

#### Effective Lagrangian for a Higgs doublet

Buchmuller and Wyler NPB 268 (1986) 621 : Giudice et al. JHEP 0706 (2007) 045

Grzadkowski et al. JHEP 1010 (2010) 085

 $\mathcal{L} = \mathcal{L}_{SM} + \Delta \mathcal{L}_{(6)} + \Delta \mathcal{L}_{(8)} + \dots$ 

## Effective Lagrangian for a Higgs doublet

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EWSB sector 
$$= \{ \chi, h, \dots \}$$



$$A(s) = \frac{s}{v^2}(1 - c_V^2) - c_V^2 \frac{m_h^2}{v^2} \frac{s}{s - m_h^2 + i\Gamma_h m_h} \equiv g^2(\sqrt{s})$$

EWSB sector 
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• For an elementary Higgs boson

$$c_V = 1$$

$$g(E) \to \frac{m_h}{v} \quad \mbox{weak}$$

EWSB sector 
$$= \{ \chi, h, \dots \}$$



• For a composite Higgs

$$f^{2} \left| \partial_{\mu} e^{i\pi/f} \right|^{2} = |D_{\mu}H|^{2} + \frac{1}{2f^{2}} \left[ \partial_{\mu}(H^{\dagger}H) \right]^{2} + \dots$$

$$fy\,\bar{\psi}e^{i\pi/f}\psi = y\,\bar{\psi}H\psi + \frac{y}{f^2}(H^{\dagger}H)\bar{\psi}H\psi + \dots$$

$$\bar{c}_H, \bar{c}_u = O\left(\frac{v^2}{f^2}\right)$$

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• For a composite Higgs

 $(1 - c_V^2) \equiv \delta \neq 0$ 

coupling strength grows with energy:

$$g(E) \sim \frac{E}{v} \sqrt{\delta}$$

EWSB dynamics becomes fully non-perturbative at energies:

$$\Lambda_S = \frac{4\pi v}{\sqrt{\delta}}$$

EWSB sector 
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Energy cartoon







Energy cartoon



EWSB sector 
$$= \left\{ \, \chi \, , \, h \, , \dots \, \right\}$$



Energy cartoon







Higgs couplings from single-Higgs processes

$$g(E = m_h) = \frac{m_h}{v} \sqrt{\delta}$$
$$\delta = O\left(\frac{v^2}{f^2}\right)$$







$$g_{*}$$

$$m_{W,Z} v$$

$$f$$

$$m_{*} \Lambda_{S} = 4\pi f$$

$$M_{*}$$

Can put lower bound on coupling strength  $g_{st}$ 

$$g_*$$

$$m_{W,Z} v$$

$$f \quad m_* \quad \Lambda_S = 4\pi f$$

$$f \quad m_* \quad M_S = 4\pi f$$

$$g^2(\sqrt{\hat{s}}) = \frac{\hat{s}}{v^2} (c_V^2 - c_{2V}) \equiv \frac{\hat{s}}{v^2} \delta_{hh}$$

$$f \quad m_* \quad M_S = 4\pi f$$

$$g^2(\sqrt{\hat{s}}) \sim \frac{\alpha_S}{4\pi} y_t^2(1 + \delta_{C_i})$$

## Double Higgs production via VBF at pp colliders

work in progress with O. Bondu, A. Massironi, J. Rojo

	$14\mathrm{Tev}$	$100\mathrm{Tev}$
$\sigma(pp \to hhjj)$ [SM]	$1.5\mathrm{fb}$	$54\mathrm{fb}$
$BR(hh \rightarrow 4b) = 33\%$		
$BR(hh  ightarrow bb \tau$	$(\tau_h \tau_h) = 3$	.1%

#### Strategy of analysis:

- Final states included:  $hh \rightarrow 4b$  ,  $hh \rightarrow bb \tau_h \tau_h$
- Jets reconstructed using BDRS mass-drop tagger Butterworth et al. arXiv:0802.2470

#### Events classified by number of mass drops (fat jets)

$hh\! ightarrow\!4b$	boosted	2 MD
	semi-boosted	1 MD + 2 b-jets
	resolved	4 b-jets
$hh \rightarrow bb  \tau_h \tau_h$	boosted resolved	1 MD + 2 τ-jets 2 b-jets + 2 τ-jets

- Final events classified in bins of  $m_{hh}$  to enhance sensitivity on Higgs couplings



## Double Higgs production via VBF at pp colliders

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Cuts
 
$$p_{Tj} \ge 25 \text{ GeV}, \quad p_{Tb} \ge 25 \text{ GeV}, \quad p_{T\tau} \ge 25 \text{ GeV}$$
 $|\eta_j| \le 4.5, \quad |\eta_b| \le 2.5, \quad |\eta_\tau| \le 2.5$ 
 $\Delta R_{jb} \ge 0.4, \quad \Delta R_{bb} \ge 0.2, \quad \Delta R_{j\tau} \ge 0.4, \quad \Delta R_{b\tau} \ge 0.4, \quad \Delta R_{\tau\tau} \ge 0.2,$ 
 $m_{jj} \ge 800 \text{ GeV}, \quad \Delta R_{jj} \ge 4.0.$ 

- Efficiencies			
Efficiencies			
	$\epsilon_b = 0.7$	$\epsilon_{\tau} = 0.7$	
	$\zeta_b = 0.01$	$\zeta_{\tau} = 0.04$	

## Higgs reconstruction $|m( au au) - m_h| < 20 \,\text{GeV}$ $|m(bb) - m_h| < 0.15 \,m_h$

### Double Higgs production via VBF: results at the LHC

work in progress with O. Bondu, A. Massironi, J. Rojo

		Bin	s of $m$	$^{0}hh$	
	I	II	III	IV	V
$hh \rightarrow 4b \text{ [SM]}$ 4b2j	4.1 $3.5 \times 10^4$	3.7 $2.7 \times 10^3$	0.8 630	$1.2 \\ 225$	1.8 25
$hh \rightarrow 2b2\tau$ [SM]	0.3	0.3	0.06	0.09	0.09
ttjj	61	2.4	0.3	0.1	0.02

#### Number of events with 3ab<sup>-1</sup> after cuts

Bins [GeV]: 250, 500, 750, 1000, 1500

20% precision on  $\delta_2$  (  $f\sim 550\,{
m GeV}$  ), mostly from events with  $m_{hh}\!\sim\!1.5\,{
m TeV}$ 

Sensitive to trilinear Higgs couplings  $\sim 4$  times larger than in the SM

LHC 14TeV L=3ab<sup>-1</sup>



$$\delta_2 \equiv 1 - c_{2V}/c_V^2$$
$$\delta_3 \equiv 1 - c_3/c_V$$

R. Rattazzi, talk at "BSM physics opportunities at 100TeV", Cern 2014"



$$\mathcal{A}(VV \to hh) = g^2(E) \left( 1 + O\left(\frac{E^2}{m_*^2}\right) \right)$$

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negligible if  $g(E) \ll g_*$ 

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If max sensitivity on  $\delta_2$  comes from events with invariant mass  $\sim E$ 

$$m_* > E \quad \Longrightarrow \quad \delta_2 < \left(\frac{g_*^2 v^2}{E^2}\right) = 0.54 \left(\frac{g_*}{3}\right)^2 \left(\frac{1 \text{ TeV}}{E}\right)^2 \qquad 4\pi \gtrsim g_* > \frac{E}{v} \sqrt{(\delta_2)_{min}} \equiv g_{min}$$

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For our analysis at the LHC L=3ab<sup>-1</sup>:

$$E \sim 1.5 \,\mathrm{TeV}$$
  
 $(\delta_2)_{min} \sim 0.2$   $\Longrightarrow$   
 $(f > 550 \,\mathrm{GeV})$ 

$$\delta_2 < 0.24 \left(\frac{g_*}{3}\right)^2$$
$$4\pi \gtrsim g_* > g_{min} = 2.7$$

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#### In general: Study

Study of Higgs properties via EFT in double Higgs production better justified at high-precision machines (such as e<sup>+</sup>e<sup>-</sup> colliders)

## Double Higgs via VBF at CLIC 3TeV

#### **Process:** $e^+e^- \rightarrow \nu\bar{\nu} hh \rightarrow \nu\bar{\nu} 4b$

- Background negligible (req. good mass res. h vs Z) (largest processes:  $hZ\nu\bar{\nu}, ZZ\nu\bar{\nu}, ZZe^+e^-$ )
- Final events classified in 4 categories of  $m_{hh}$  ,  $H_T$  to enhance sensitivity on Higgs couplings

Results with 1ab<sup>-1</sup>-

5% precision on  $\delta_2$  (  $f \sim 1.1\,{
m TeV}$  )

30% precision on  $\delta_3$ 

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### Double Higgs-strahlung at the ILC

Assuming 
$$\sqrt{s} = 500 \text{ GeV} + 1 \text{ TeV}$$
  
 $L = 1 \text{ ab}^{-1}$   
 $c_V^2 (BR(b\bar{b})/BR(b\bar{b})_{SM}) = 1$ 



RC, Grojean, Pappadopulo, Rattazzi, Thamm JHEP 1402 (2014) 006



#### Double Higgs production via gluon fusion





RC, Ghezzi, Moretti, Panico, Piccinini, Wulzer JHEP 1208 (2012) 154

Suppression of SM triangle diagram at high-energy implies:

much stronger sensitivity on c<sub>2t</sub> than on c<sub>3</sub>

[ First noticed by:

Dib, Rosenfeld, Zerwekh, JHEP 0605 (2006) 074 Grober and Muhlleitner, JHEP 1106 (2011) 020 ]

$$\sigma(pp \to hh + X)_{SM} = 28.7 \,\mathrm{fb}$$

(NLO K = 2 incl.)



-  $hh \rightarrow b\overline{b}\gamma\gamma$  may be the best channel Baur, Plehn, Rainwater, PRD 69 (2004) 053004 ATLAS: ATL-PHYS-PUB-2012-004

#### - $hh \rightarrow b \overline{b} \tau \tau$ promising in the boosted regime

Dolan, Englert, Spannowsky JHEP 1210 (2012) 112 Barr, Dolan, Englert, Spannowsky PLB 728 (2014) 308

## - $hh \rightarrow b\overline{b}b\overline{b}$ difficult but maybe observable at the HL-LHC

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We reconsidered the channel  $hh 
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Q: how does double-Higgs compare to single-Higgs in constraining  $\bar{c}_u$  ?

Azatov, DelRe, RC, Meridiani, Micheli, Panico, Son work in progress

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  - Best machine is  $e^+e^-$  CLIC with  $\sqrt{s} = 3 \,\mathrm{TeV}$  and L=3ab<sup>-1</sup>

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Double Higgs-strahlung at the ILC with 500GeV+1TeV:

Precision: Whh at 20%; hhh at 100%

# Conclusions (continued)

- Double Higgs production gives the opportunity to:
  - i) measure Higgs couplings not accessible in single production;
  - ii) probe the strength of EWSB dynamics
- Double Higgs production via gluon fusion:
  - Best process to extract trilinear coupling at the LHC
  - Extremely sensitive to Whh coupling, competes with single-Higgs in constraining  $\bar{c}_u$

68% probability intervals on *hhh* from  $hh \rightarrow b\bar{b}\gamma\gamma$ :

LHC 300fb <sup>-1</sup> :	$\bar{c}_3 \in [-1.5, 6.0]$

- LHC 3ab<sup>-1</sup>:  $\bar{c}_3 \in [-0.98, 1.8] \cup [3.4, 5.3]$
- **100TeV 3ab**<sup>-1</sup>:  $\bar{c}_3 \in [-0.27, 0.24]$