



Doping Profile of Low-Gain Avalanche Diodes (LGAD) using C-V

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with

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Parts from 2 Runs of Low-Gain Avalanche Diodes

Pads 2012 (“Pablo”): 300 um FZ (W8, W7, W13)

Pads & Strips 2013 (“Marta”): 50 um epi, 300 um FZ



Charge Multiplication

W. MAES, K. DE MEYER* and R. VAN OVERSTRAETEN
Solid-State Electronics Vol. 33, No. 6, pp. 705-718, 1990

Charge multiplication in path length ℓ :

$$N(\ell) = N_0 * \exp(\alpha * \ell) = g * N_0$$

$$\alpha_{e,h}(E) = \alpha_{e,h}(\infty) * \exp\left(-\frac{b_{e,h}}{|E|}\right)$$

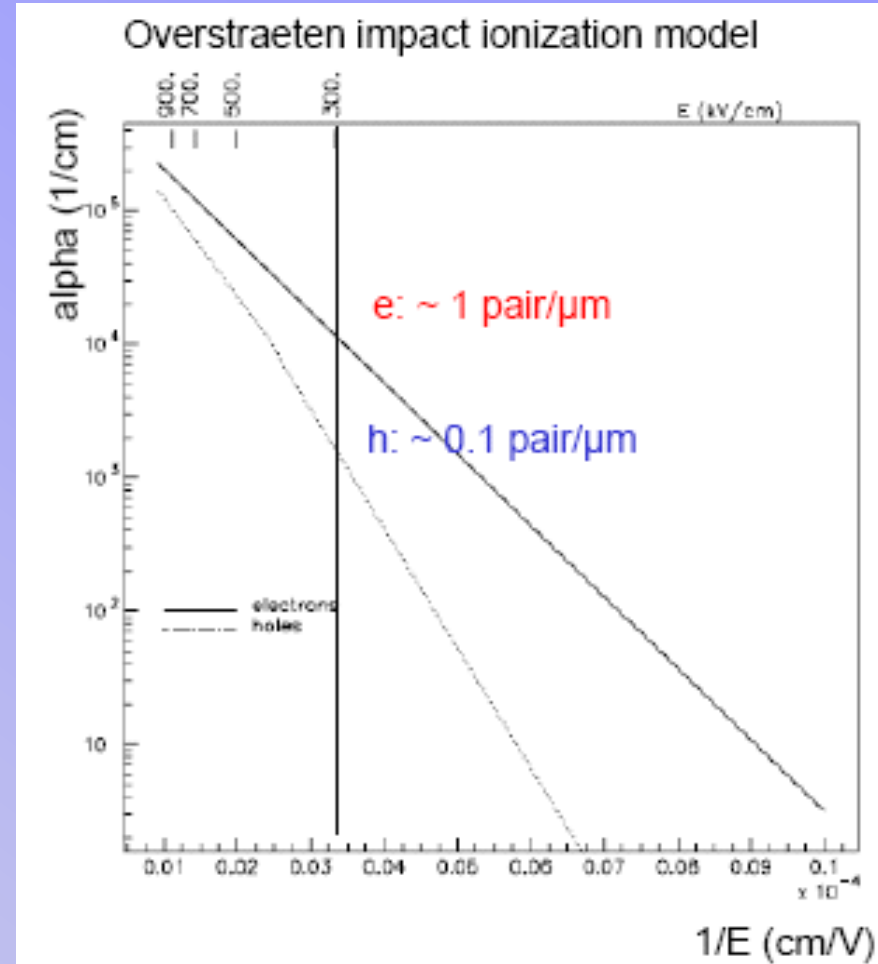
At the breakdown field in Si of 300kV/cm:

$$\alpha_e \approx 0.66 \text{ pair}/\mu\text{m}$$

$$\alpha_h \approx 0.17 \text{ pair}/\mu\text{m}$$

→ gain $g = 27$ possible in $l = 5 \mu\text{m}$.

→ In the linear mode (gain ~ 10), consider electrons only



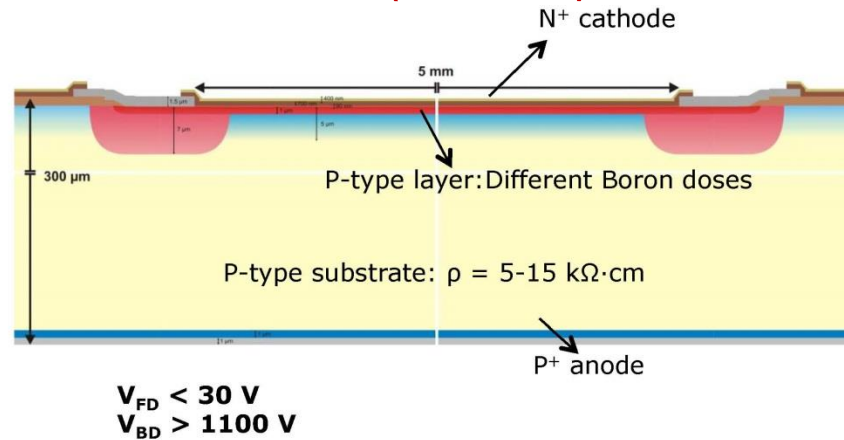
Need to raise E-field as close to breakdown field as possible for high gain but not too much to prevent breakdown!

Detailed realistic simulation of avalanche required.

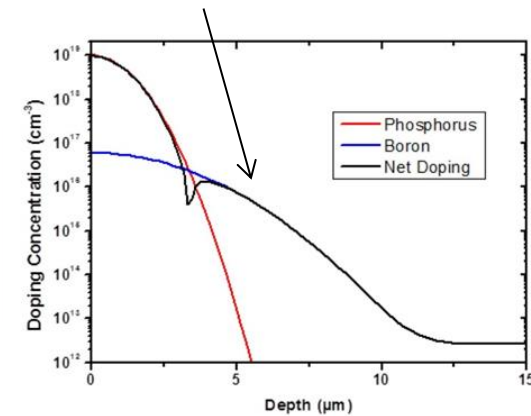
1. Thin p-type epitaxial substrates
2. Low gain avalanche detectors

Pads detectors with multiplication

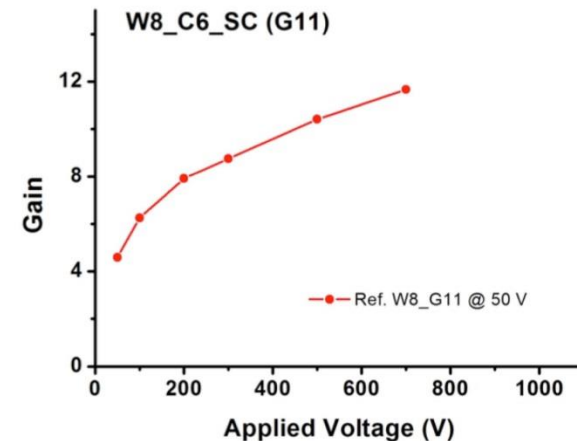
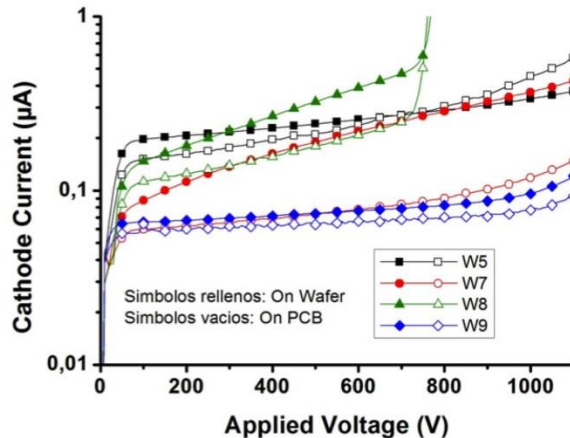
Low-Gain Avalanche Detector (LGAD)



High-Field: Gain

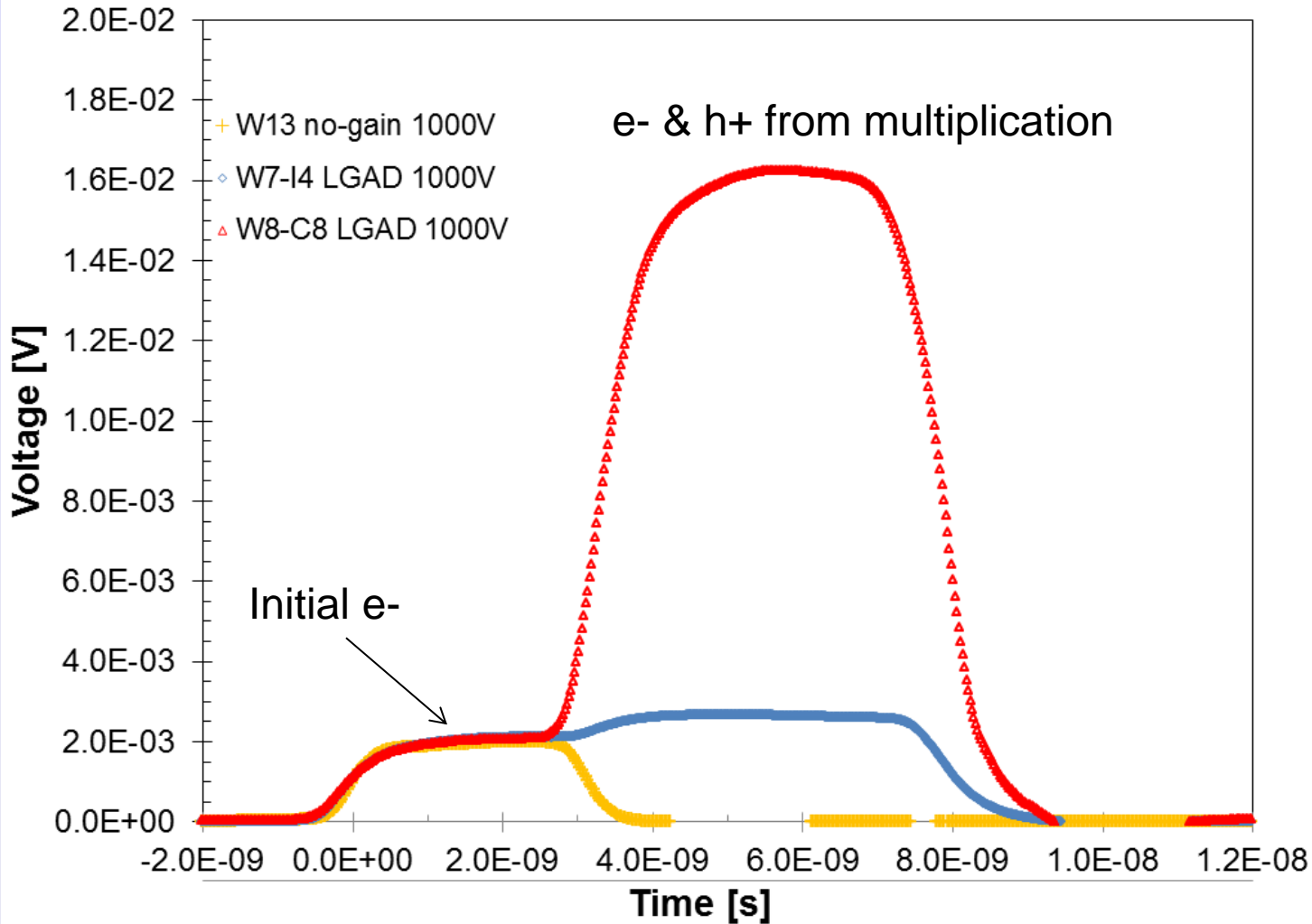


Marta Baselga,
Trento Workshop
Feb. 2013





Pulse – shape analysis with α TCT

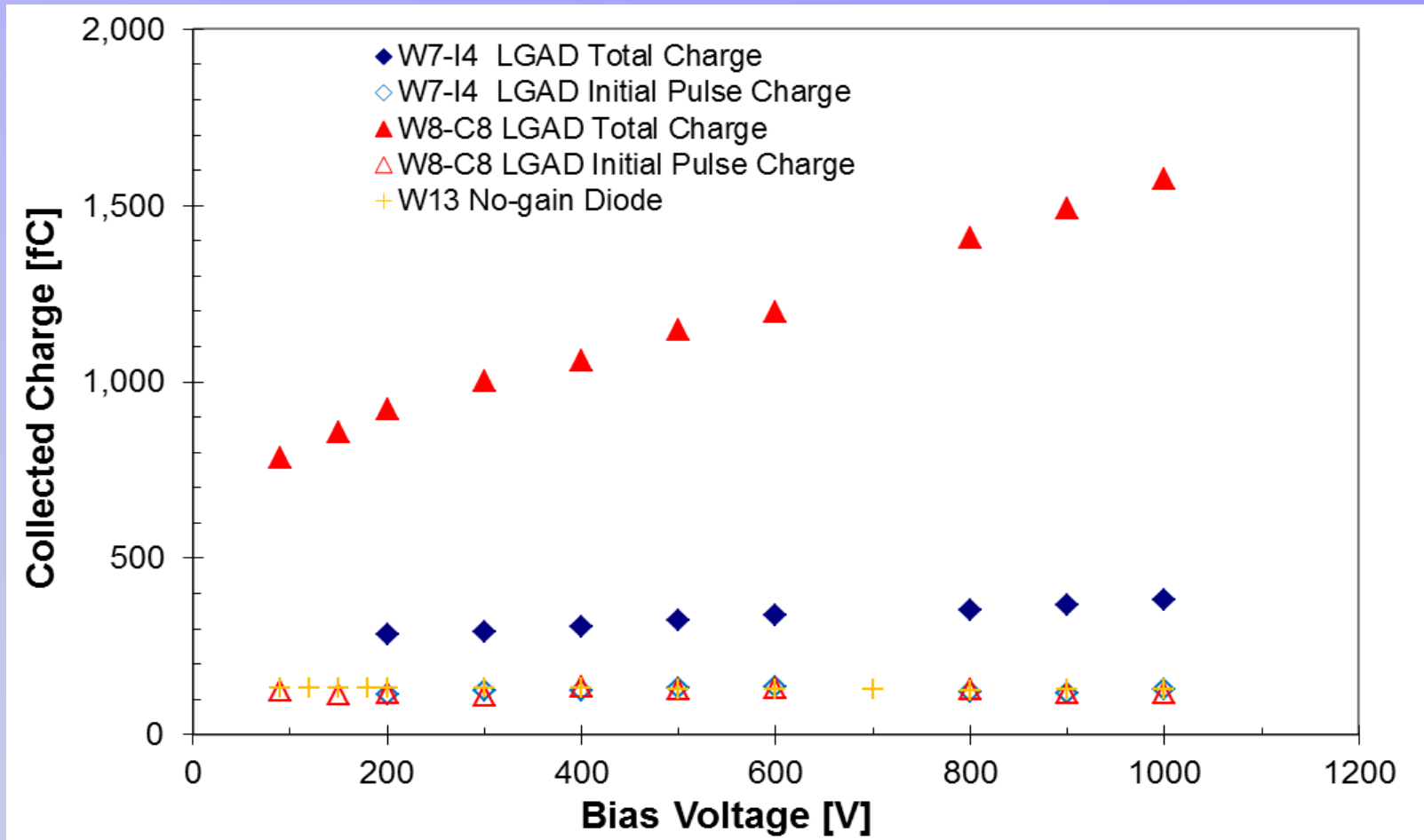


$$\text{Gain} = \text{Total pulse area} / \text{Initial Pulse Area}$$

Charge collection well described by simulations (Francesca's talk)



Total charge & initial Pulse charge



The initial pulse charge is identical for two different LGAD's (after correction) and a no-gain diode: Reflects the initial electron drift.

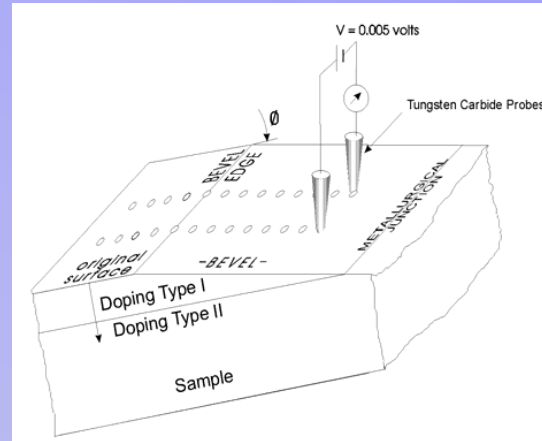
Large gain differences: $G(W8-C8)/G(W7-I4) \approx 4$ at 1000V bias.

Original idea: correlation with high leakage current, turns out to be wrong



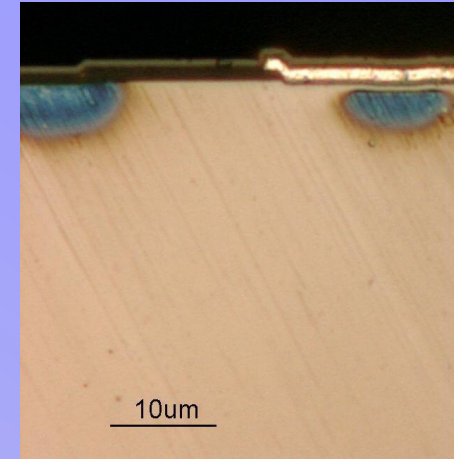
≥ 6 Methods for Extraction of Doping Profile

C-V
(used here)



SRP

Spreading Resistance Profiling
N. Dinu, Sept 2013 PPS



Micro-section + Etch
Salvador Hidalgo, 22nd RD50
see Marta's talk

SIM

Secondary Ion Mass Spectroscopy

XPS (ESCA)

X-ray photoelectron spectroscopy

Question: applicable for our range : $N = 10^{12} - 10^{17} \text{ cm}^{-3}$?

Terahertz Imaging

“Terahertz imaging of silicon wafers”

M. Herrmann et al, JAP 91,3, 1 (2002)

2 J. Appl. Phys., Vol. 91, No. 3, 1 February 2002

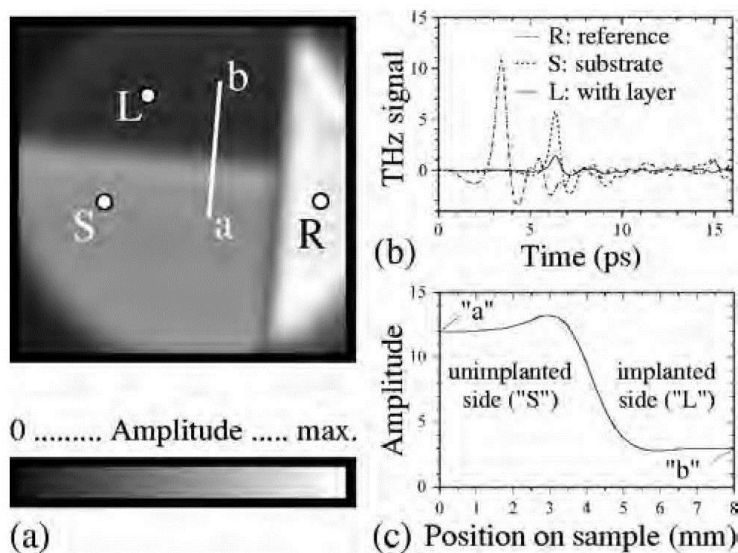


FIG. 1. (a) THz image of a Si sample with a $5 \times 10^{15} \text{ cm}^{-2}$ implanted layer: reference region (R, no sample), substrate region (S, not implanted) and layer region (L, implanted and strongly absorbing). The image size is $20 \text{ mm} \times 20 \text{ mm}$. The dark areas in the edges are shadows from the sample holder. (b) THz time-domain wave forms taken in the regions R, S, and L. (c) Pulse maxima along the line *a-b* in (a) (from a separate measurement). There are refraction effects resulting in a maximum and a minimum at the border between the implanted and unimplanted regions.

Exploits relationship between permittivity and refractive index:

$$\epsilon(\omega) = (n+ik)^2$$

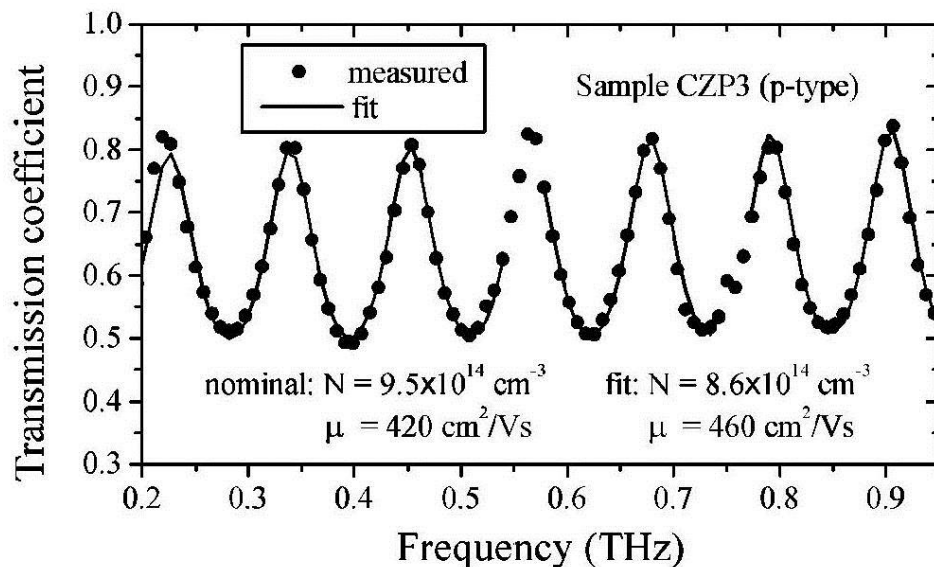


FIG. 2. Transmission spectrum of a *p*-type Si sample, and its best fit.

Like C-V, potentially not invasive?
Contact with Fraunhofer Institute



Deriving the Doping Profile from C-V

(strictly correct only for pad sensors and uniform doping density!!)

Bias Voltage V – Depleted Region x :
$$V = \frac{qN}{2\epsilon\epsilon_0} x^2$$

Resistivity ρ – Doping density N :
$$\rho = \frac{1}{q\mu N}$$

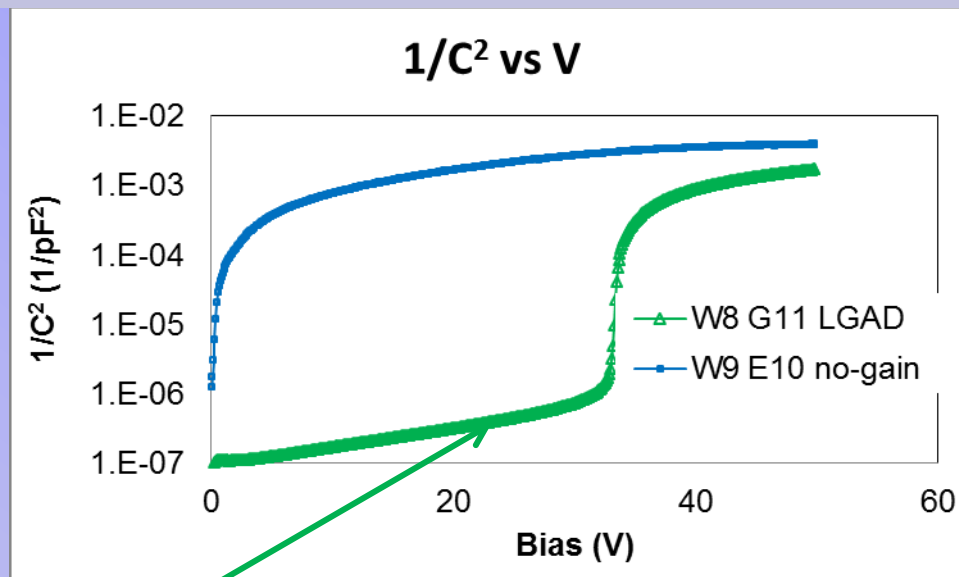
Capacitance C – Depl. Region x :
$$C(x) = \epsilon\epsilon_0 \frac{A}{x} = A\sqrt{\frac{\epsilon\epsilon_0 qN}{2V}}, \Rightarrow x = A / C$$

Doping Density:
$$N = \frac{2}{\frac{d(1/C^2)}{dV}} \cdot \frac{1}{\epsilon\epsilon_0 q A^2} = \frac{2}{\frac{d(1/C^2)}{dV}} \cdot \frac{1}{1.6 \cdot 10^{-7} A^2}$$

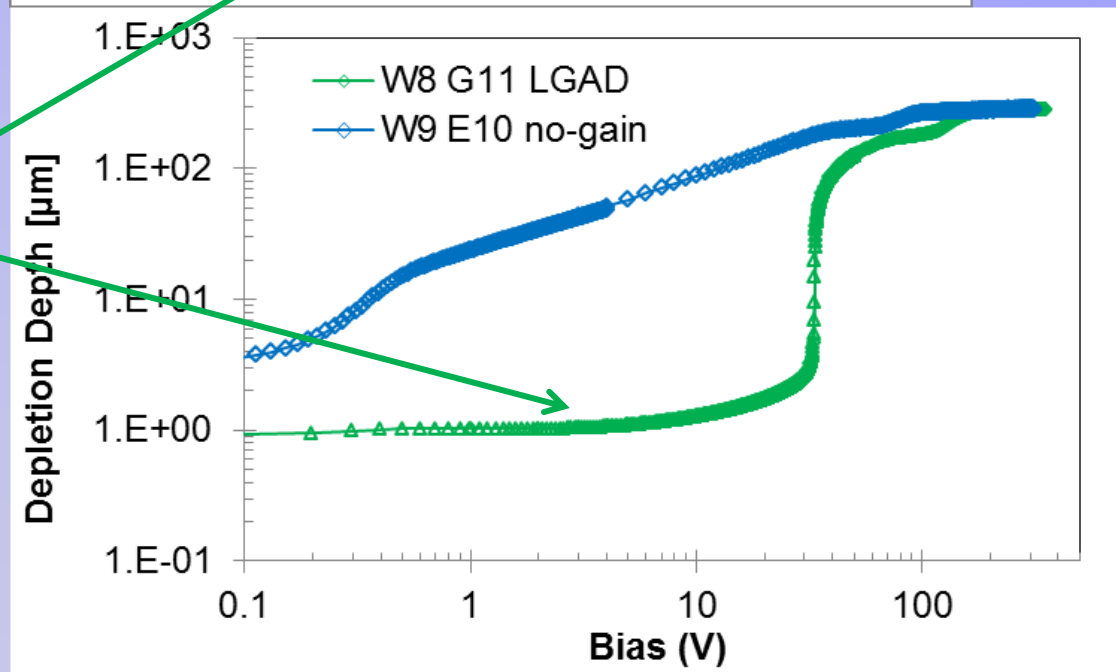


Large C-V Difference LGAD/no-gain at low Bias

Example on pads
W8G11: LGAD
W9E10 no gain



Important:
Take voltage steps
of 0.1V below 50 V
(below the “foot” / “lag”).

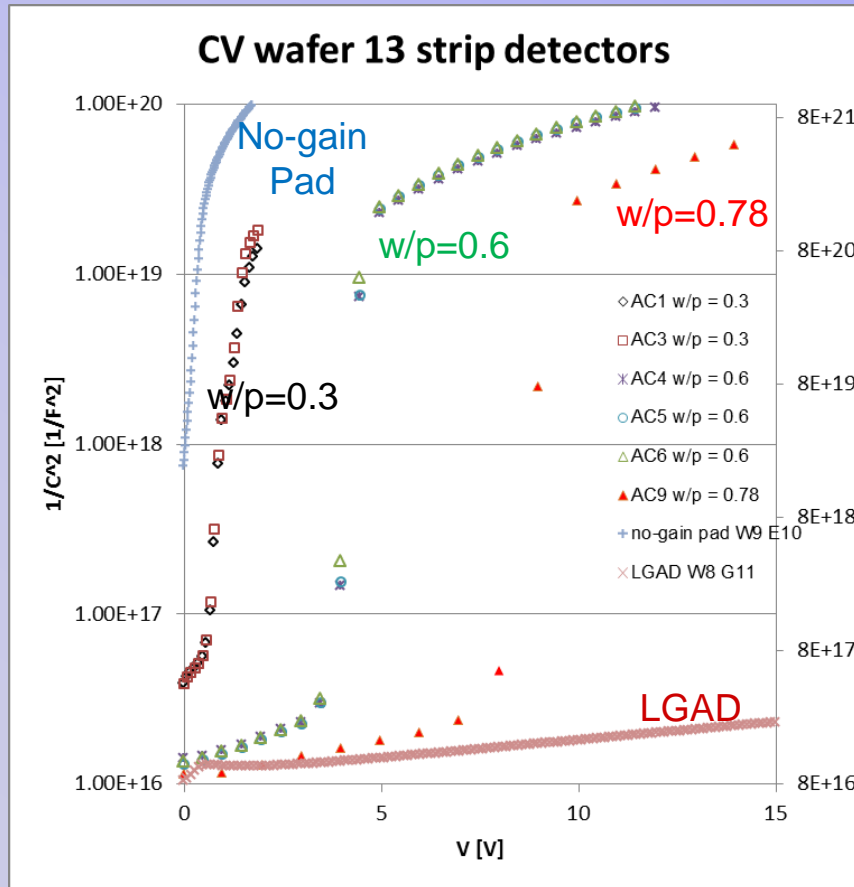
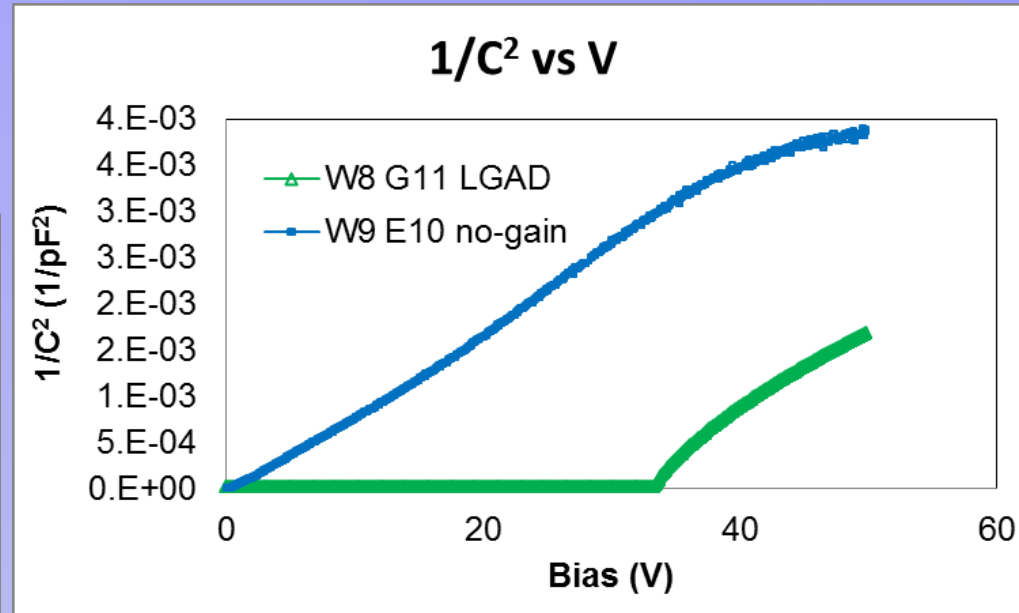




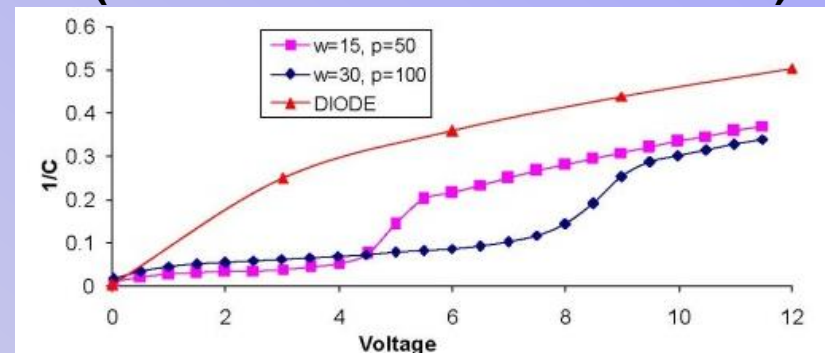
Large voltage “Lag” due to strip geometry

Example of “Foot” on pads

Careful: “foot” indicates gain only with pads!
 FZ **strips** gain?/no-gain?



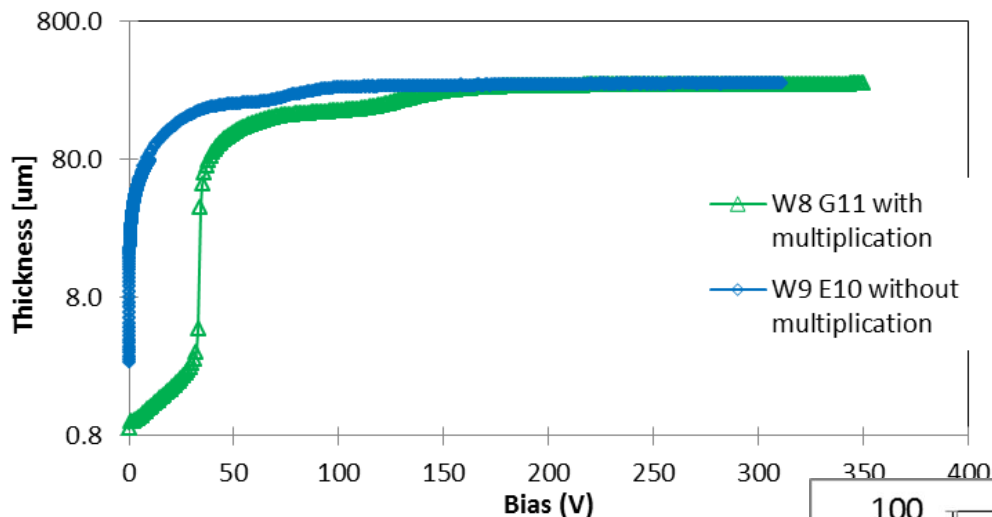
Lateral depletion in no-gain SMART FZ strips (Chris Betancourt M.S. Thesis)





Depleted thickness x vs. V

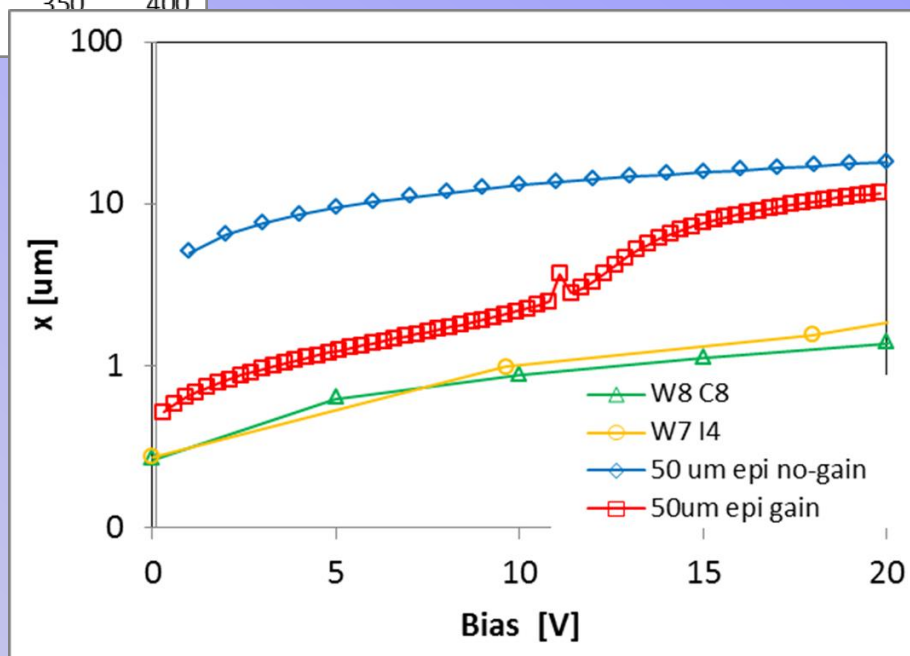
Depleted Thickness vs. V



$$x = A / C$$

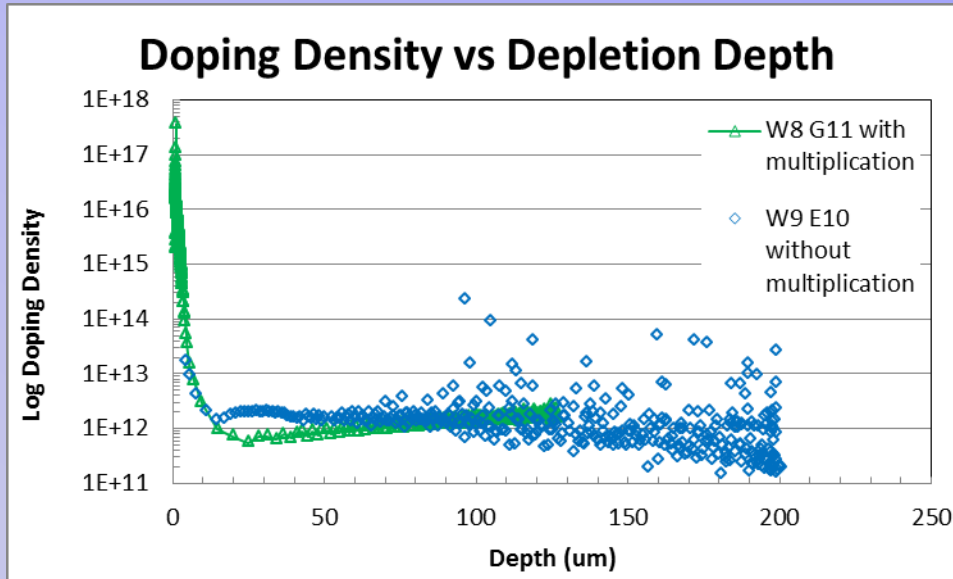
Conversion of
capacitance $C(V) \rightarrow C(x)$
doping density $N(V) \rightarrow N(x)$
resistivity $\rho(V) \rightarrow \rho(x)$

- Saturates at $x \approx 250\mu\text{m}$ as expected
- Shows large voltage lag for LGAD



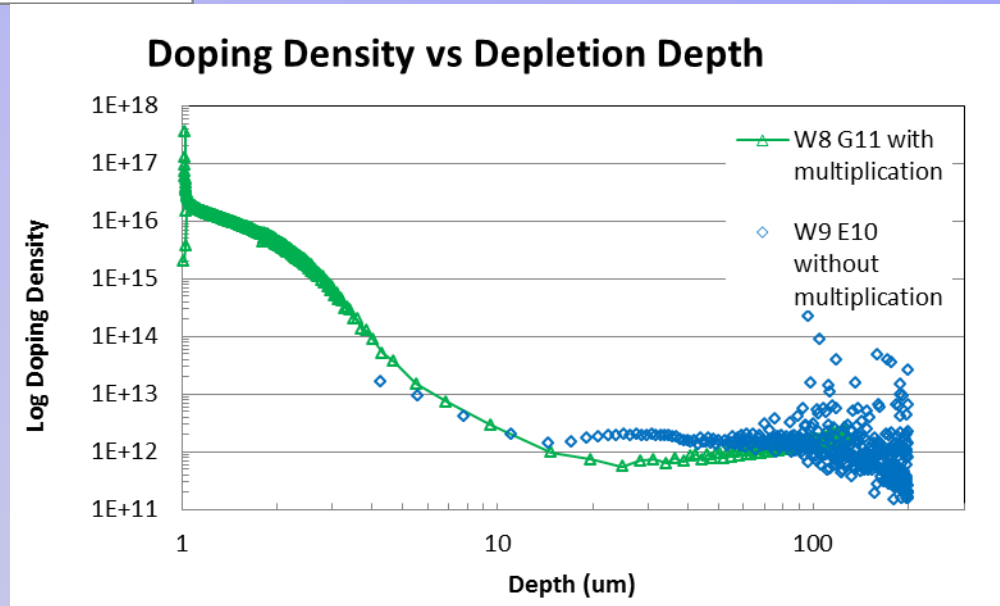


Doping Density Profile N(x)



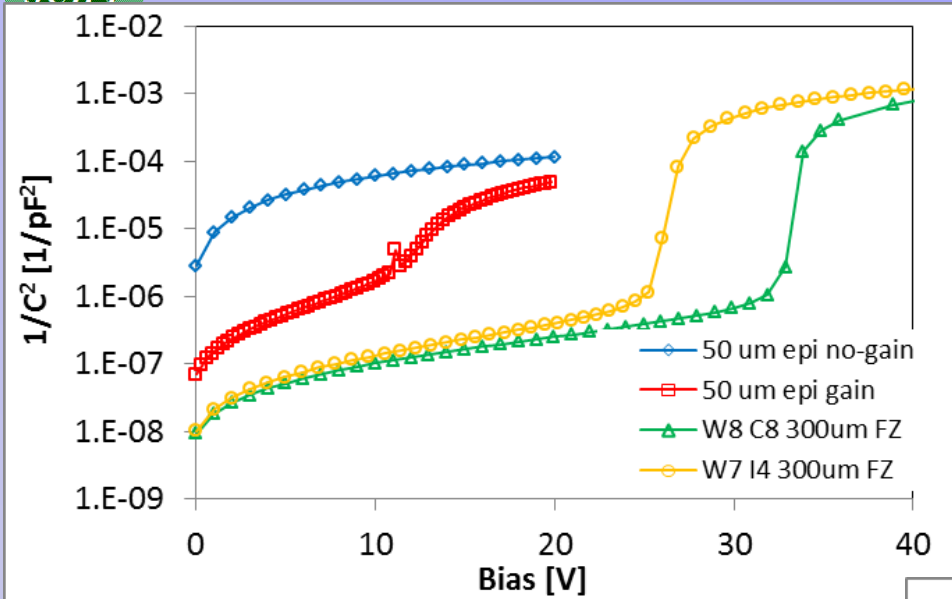
$$N = \frac{2}{\frac{d(1/C^2)}{dV}} \cdot \frac{1}{\epsilon q A^2}$$

LGAD and no-gain diode have same doping profile far away from gain region!





Voltage Lag (“Foot”) in $1/C^2$ vs V



lag of depletion in gain diodes:

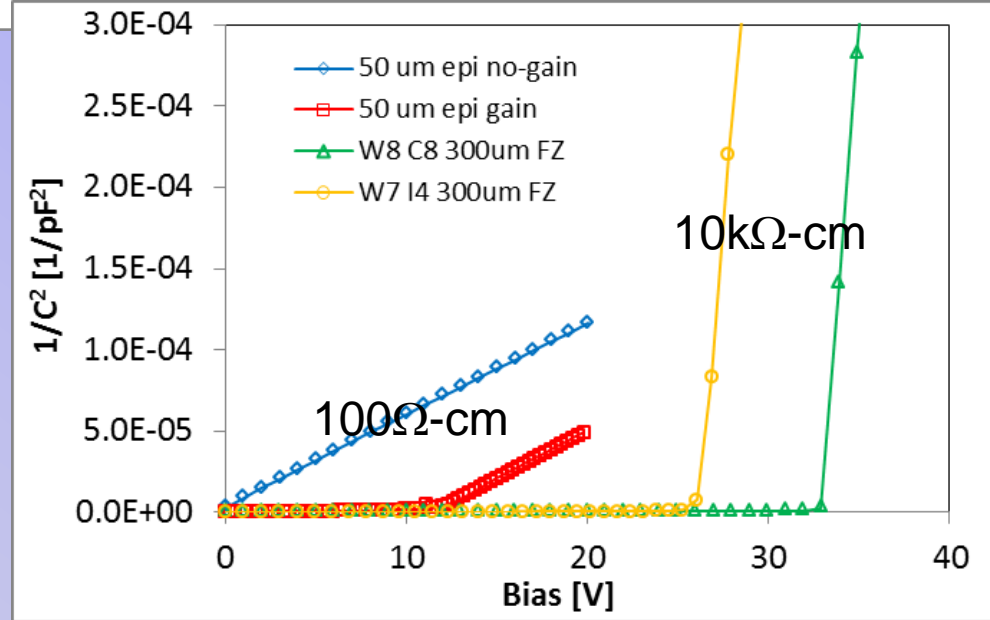
W8 C8 : 33V,

W7 I4 : 26V,

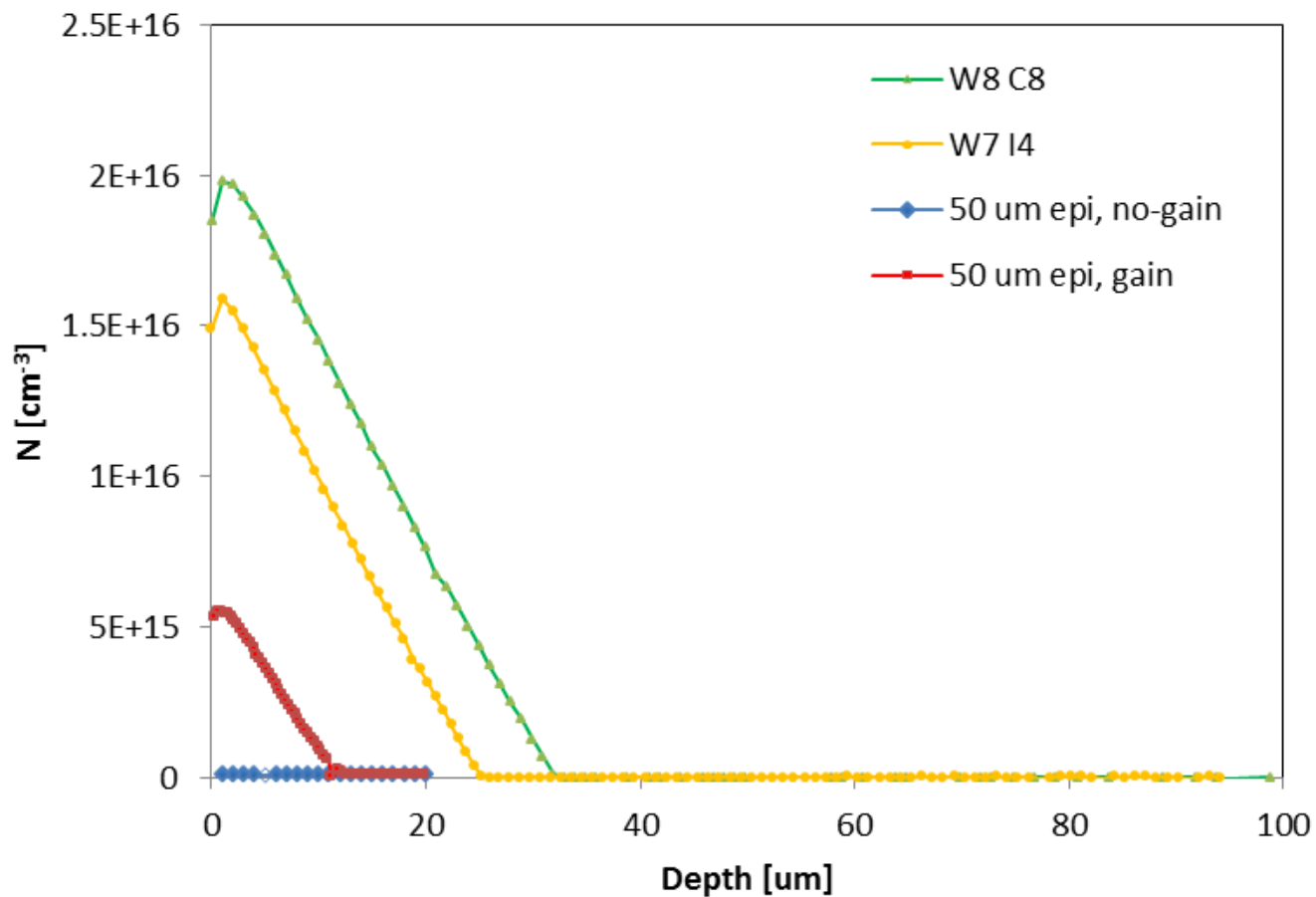
(W13, W9 : < 1V)

50um epi (gain): 12V

50um epi (no-gain): < 1V



Estimate of Doping Density Profile



Nmax :

W8 C8 : 2.0×10^{16}

W7 I4: 1.6×10^{16}

50 μm epi

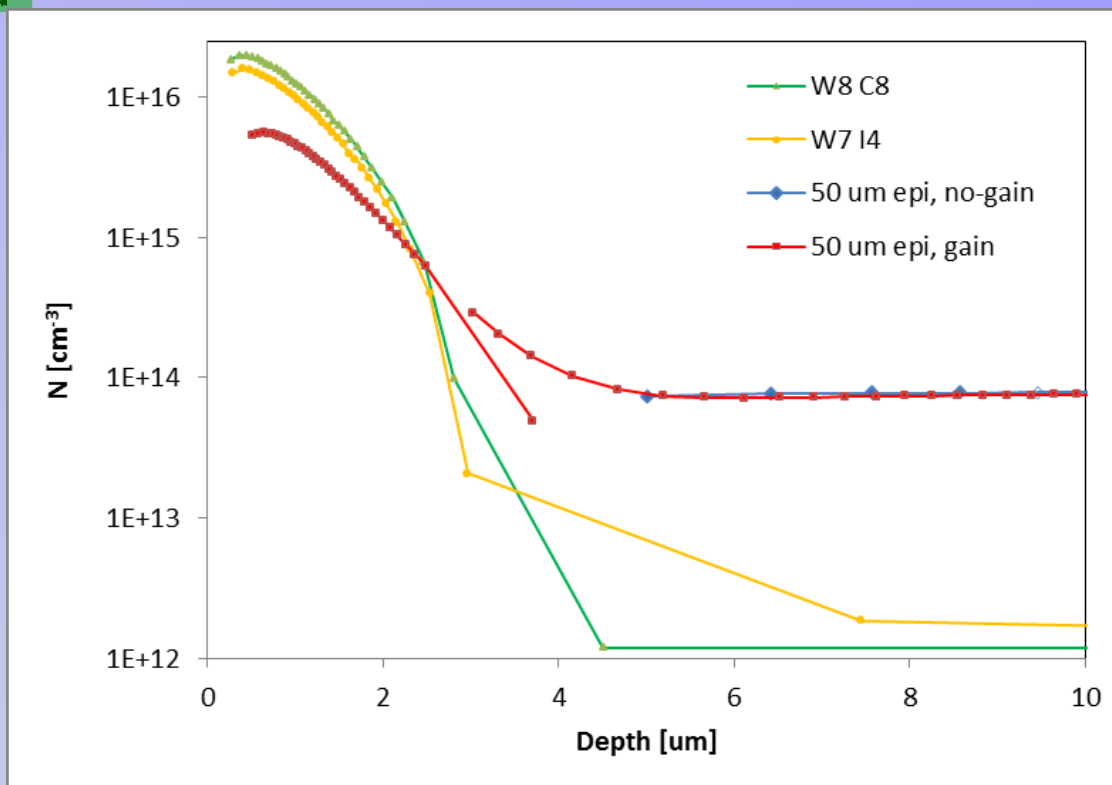
(gain): 0.6×10^{16}

50 μm epi

(no-gain): 7×10^{13}



Doping Density Profile



Device	Voltage Lag [V]	N_{max} [cm^{-3}]	N_{Bulk} [cm^{-3}]	Gain (400V)
W8 C8 FZ	35	$2.0\text{e}16$	$1.6\text{e}12$	8
W7 i4 FZ	29	$1.6\text{e}16$	$1.6\text{e}12$	2.5
50um epi (gain)	14	$0.6\text{e}16$	$7\text{e}13$	~ 1
50um epi (no-gain)	< 1	$7\text{e}13$	$7\text{e}13$	~ 1

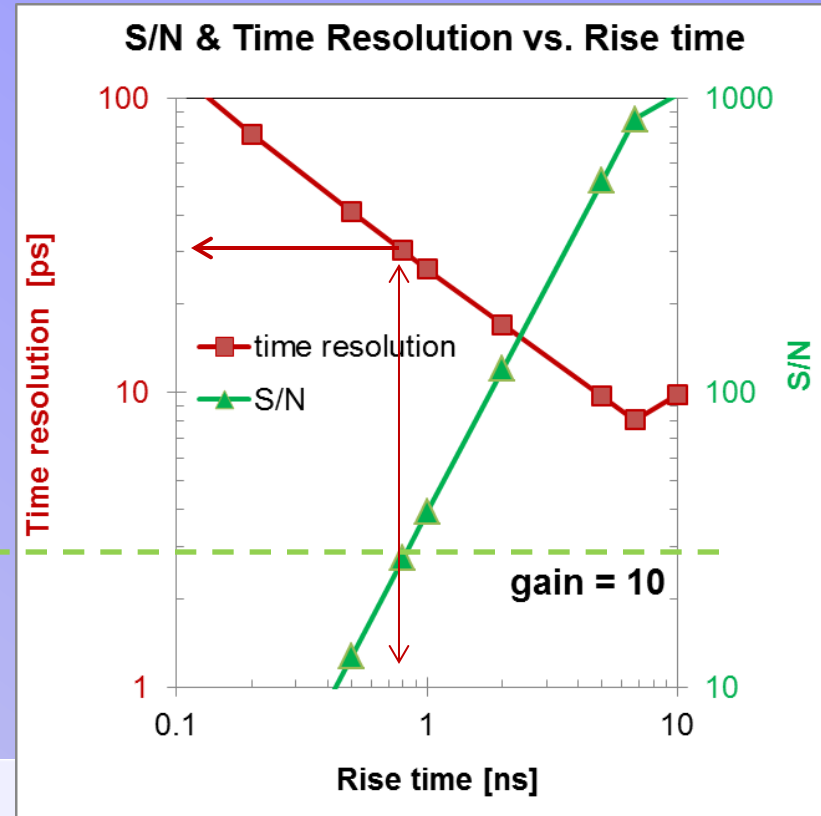


Rise Time, Thickness, S/N, Time Resolution

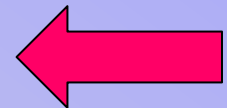
$$\sigma_t(CFD) = \tau_R \frac{1}{(S/N)} \left[1 + \left(CFD \cdot 10 \frac{\Delta S}{S} \right)^2 \right]^{1/2}$$

Rise rime \approx Collection time
(\sim Thickness)

Need S/N > 30



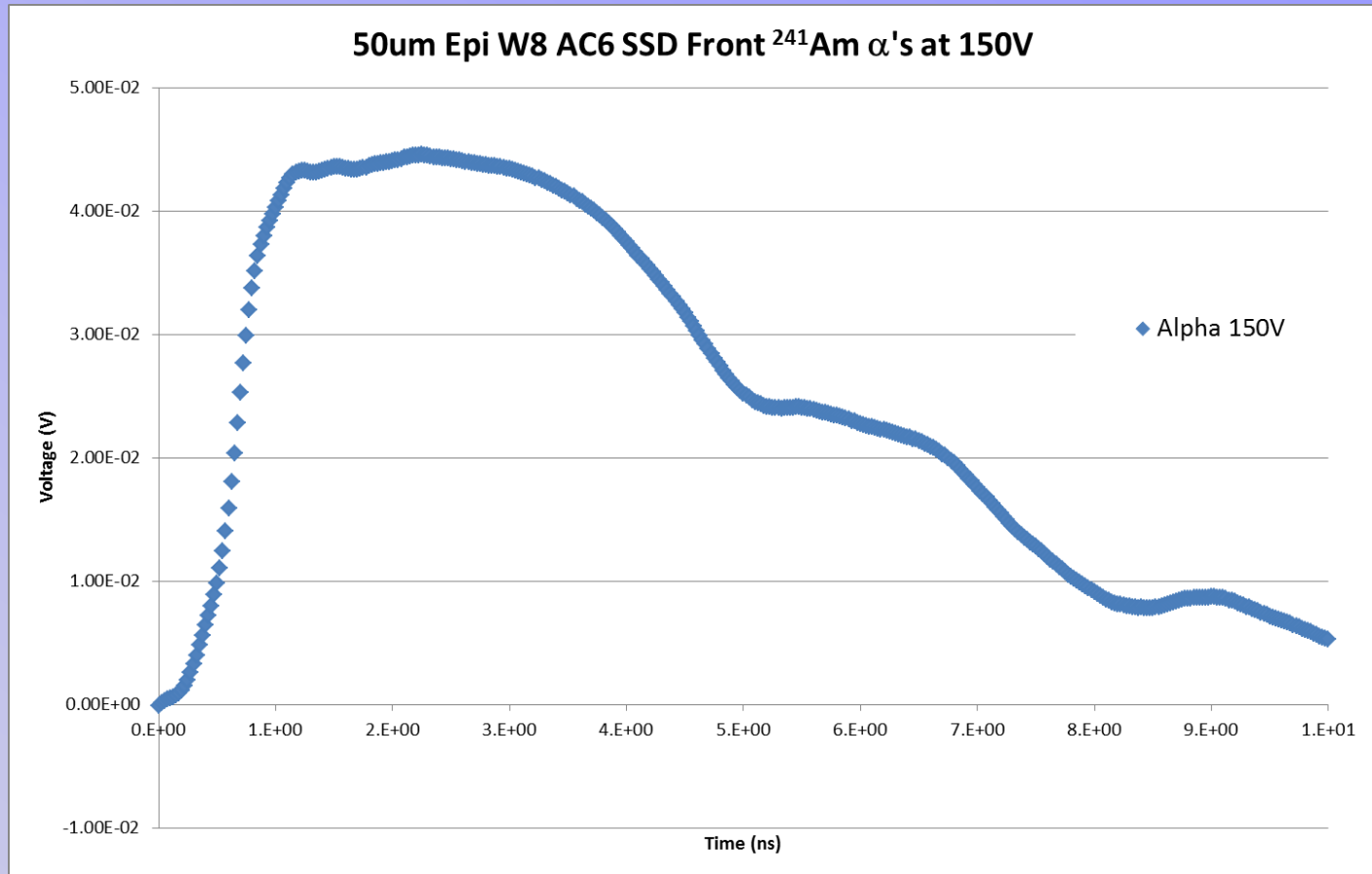
Gain G	τ_R [ps]	Thickness [μm]	Time resolution [ps]			
			no CDF	CFD=1/10	CFD=1/5	CFD=1/3
1	3000	130	282	132	139	154
10	800	36	85	30	33	40
100	200	9	29	7.5	9.0	11.6



(like \sim 50 μm thick sensors..but see Nicolo's talk)



Front-side α TCT on 50um epi strip sensors



**Limited by early breakdown at $\frac{1}{2}$ of VFD = 270 V (100 Ω -cm!)
Need high resistivity bulk and high breakdown voltage on thin sensors**



Excess Noise in Sensors with Gain

Charge multiplication in silicon sensors allows increasing the signal-to-noise ratio S/N as long as the excess noise due to the multiplication process is small.

$$ENC = \sqrt{2 \cdot e \cdot i_{gen} \cdot \tau} \cdot \sqrt{F} \cdot G$$

(M. Mikuz, HSTD9, Sept. 2013)

$F(G=1) = 1$, $F(G \gg 1) = 2$ (R. J. McIntyre, IEEE TED13(1966)164)

For LGAD:

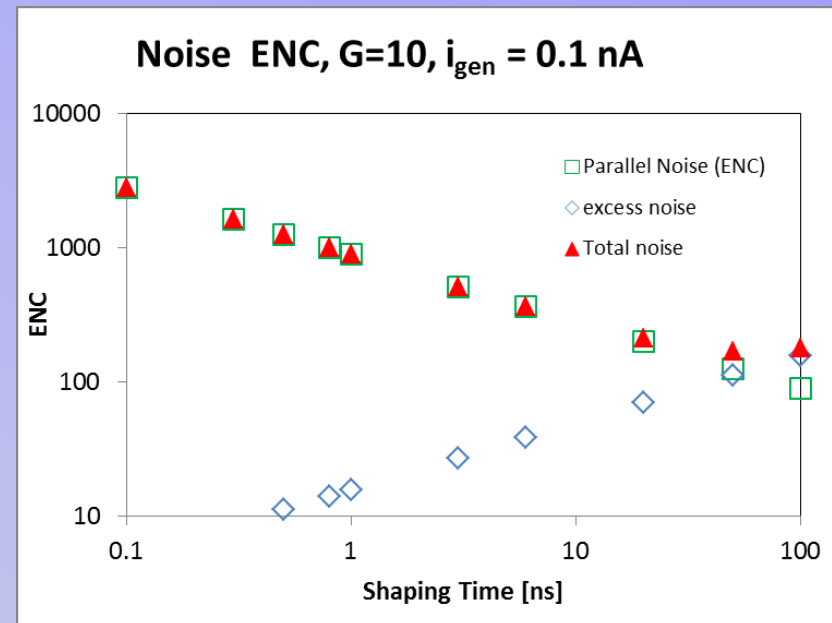
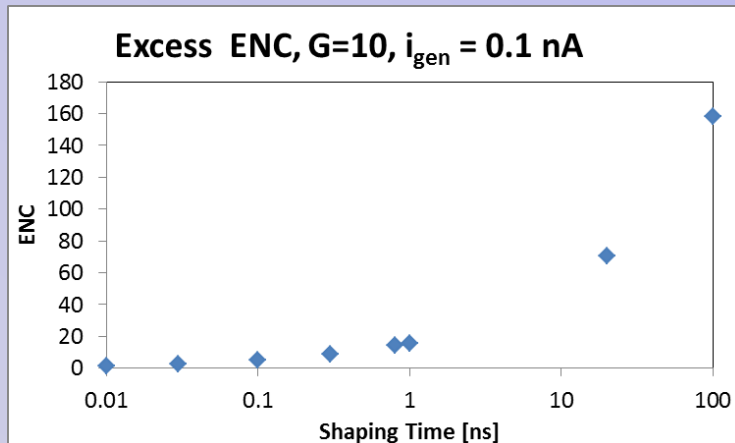
Current $i_{gen} = 10 \mu A/cm^2$

-> current per pixel $i = 1 nA$, $i_{gen} = 0.1 nA$

Gain = 10, $F=2$



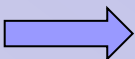


-> excess Noise at $\tau = 800 ps$: $14 e^-$

-> excess Noise at $\tau = 20 ns$: $70 e^-$





Conclusions

- Extraction of doping density value for the bulk agrees with expected value for both FZ and epi.
- Comparing values for the doping density N of the gain region of LGAD's shows the sensitivity of the gain:
Factor 3 in gain for 20% difference in N !
- "Marta's" gain diodes have $\sim 30\%$ of N of the "Pablo's" diodes:
  Marta
- Have a run with higher doping density and higher resistivity bulk  Virginia
- Simulations describe observed pulse shapes reliably
  Francesca
- Simulation of time resolution including e-h statistics in thin sensors  Nicolo
- Always worry about radiation damage  Gregor



Pulse shapes on LGAD using α 's and lasers

Hartmut Sadrozinski, Vitaliy Fadeyev, Abe Seiden,, Zac
Galloway, Jeff Ngo

SCIPP, UC Santa Cruz

Nicolo Cartiglia, Francesca Cenna

INFN Torino

Marta Baselga

CNM Barcelona

α 's : 5.5 MeV Am(241) (we detect about $\frac{1}{2}$ of that)

“ps” Laser 850 and 1064

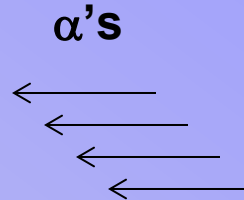
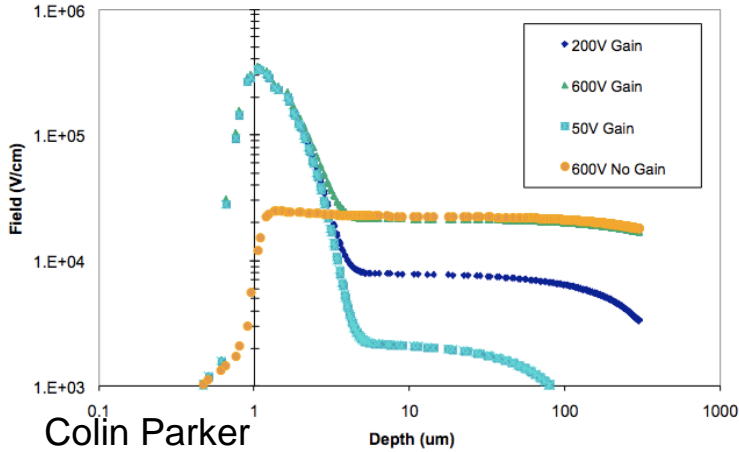
Both front and back illumination



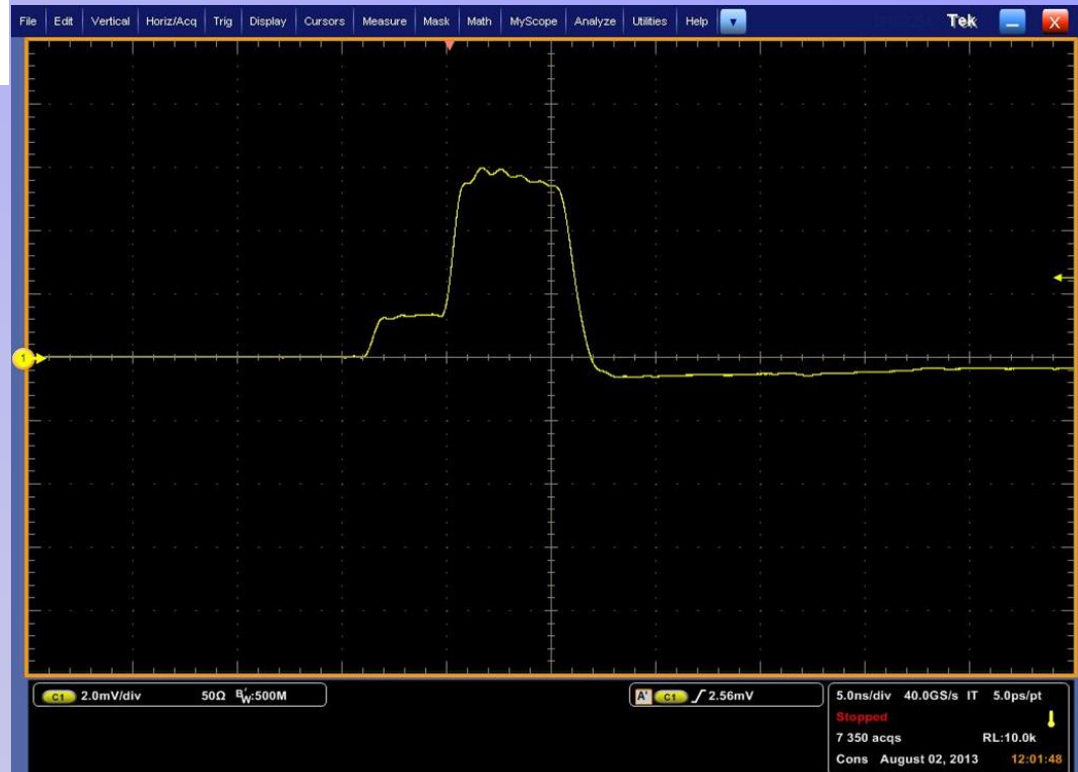
SCIPP

Charge Collection with α 's from Am(241)

Electric Field vs. Depth



Am(241)
 illuminating the back side,
 range ~ few um's
 "electron injection"
 signal drifts and is then
 amplified in high field



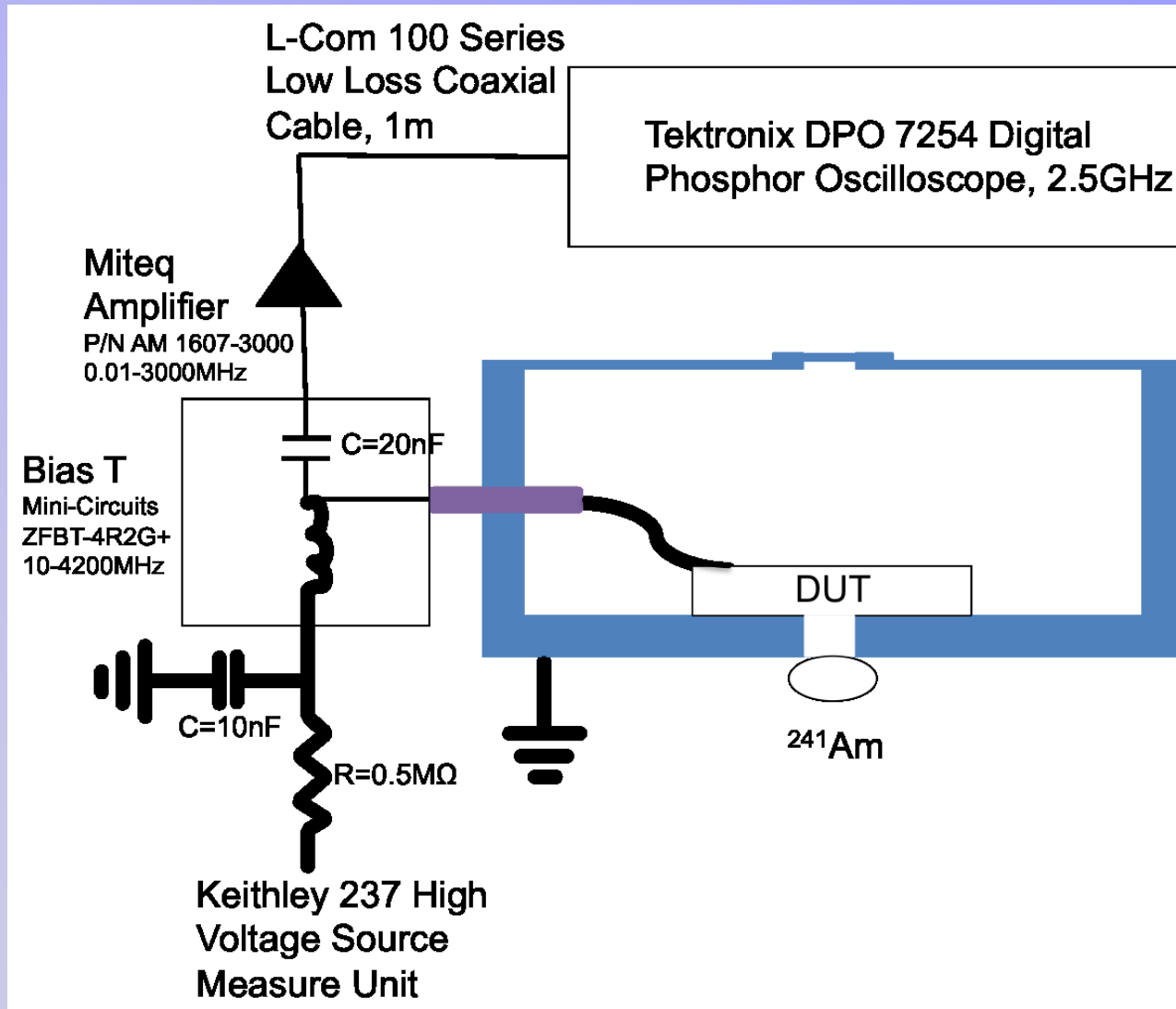
Fast signals!

Observed rise times \approx 400 ps
allowing time-resolved current
transient (TCT) analysis .

Don't know yet where the
lower limit is, since we are still
improving the BW of the
system.

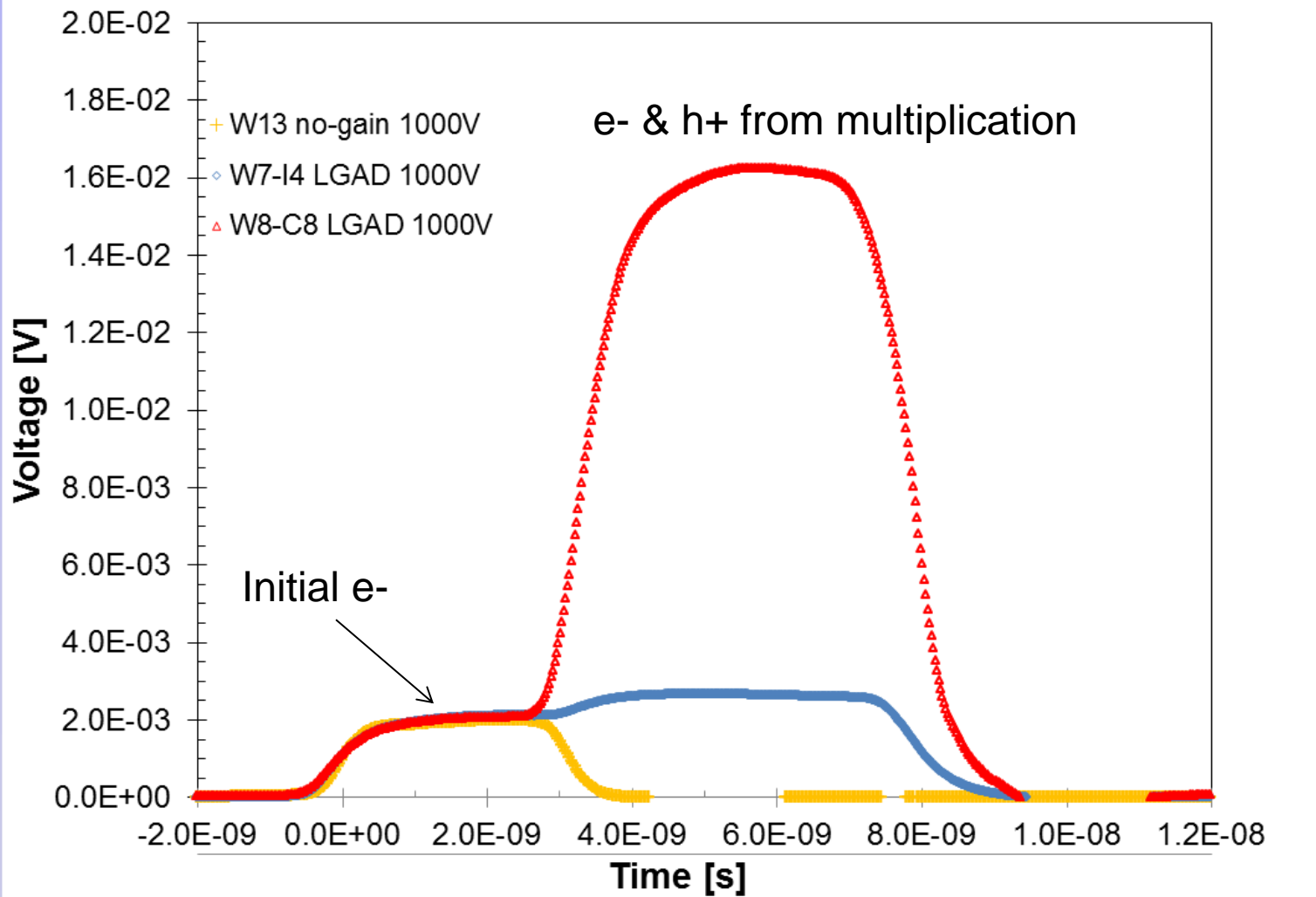


High BW α TCT Set-up





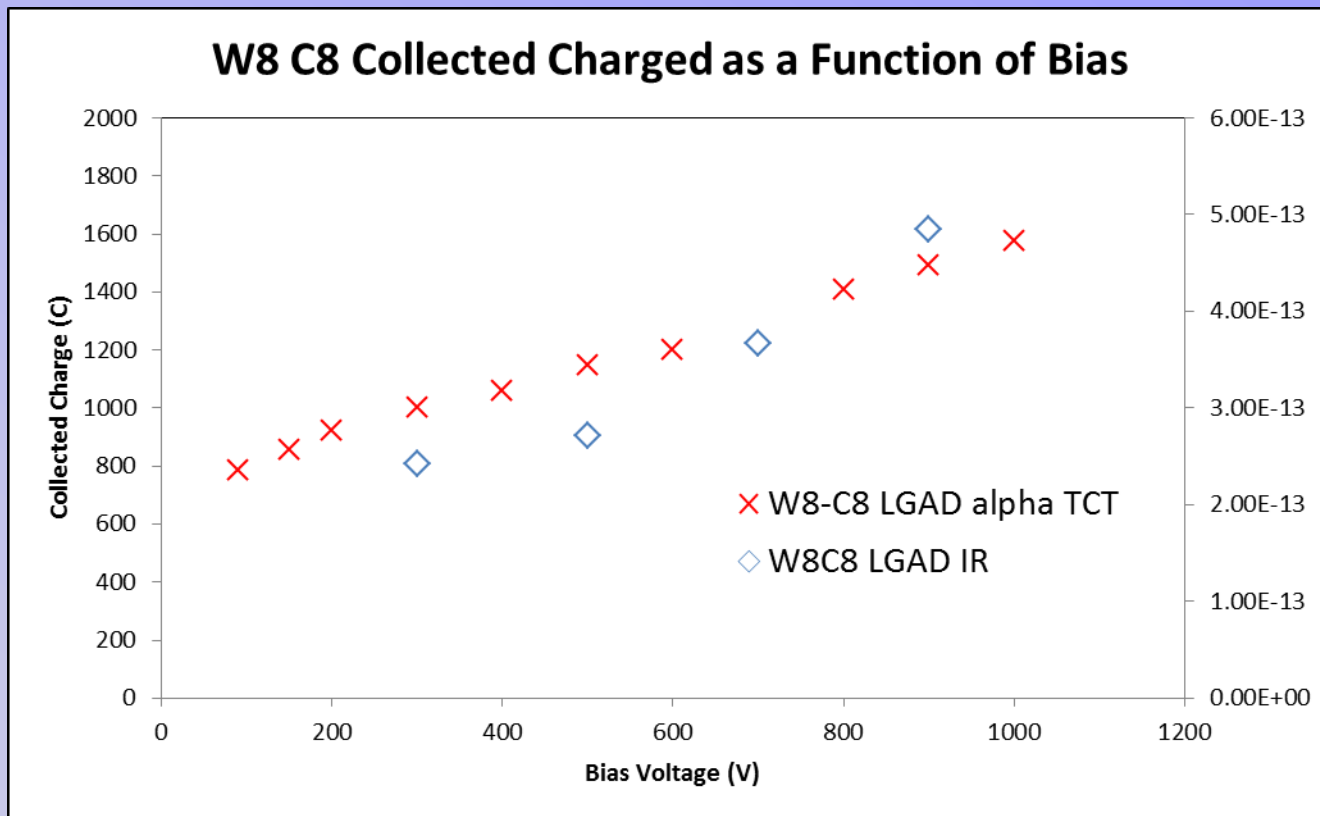
Pulse – shape analysis with α TCT



$$\text{Gain} = \text{Total pulse area} / \text{Initial Pulse Area}$$



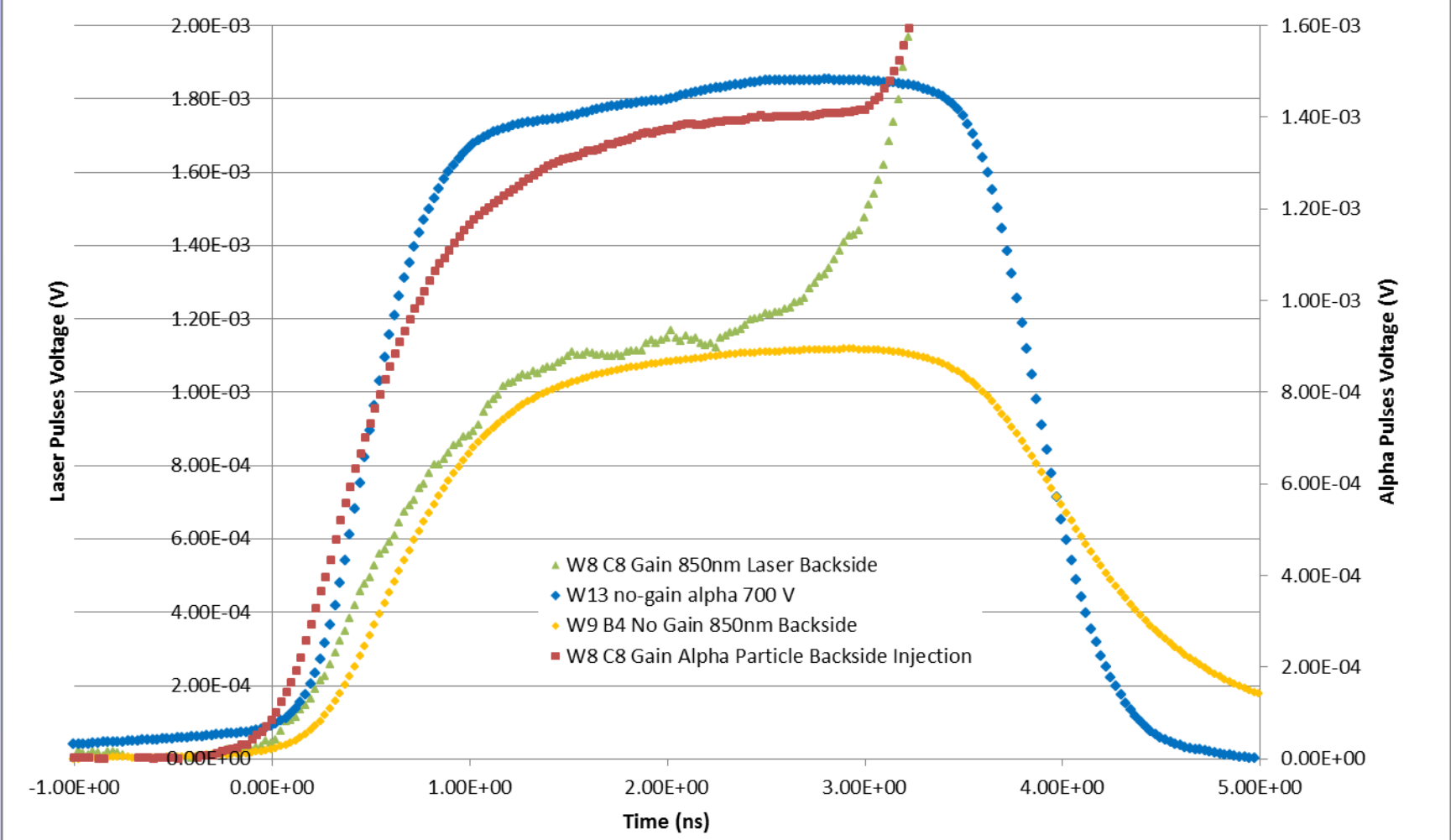
TCT: more gain with IR laser than with α ?





TCT: red laser ~ same speed as α

850nm Laser vs. Am241 Alpha: Backside Injection





TCT: more gain with red laser than with α ?

