

# Exclusive channels in $pp$ collisions and the Odderon

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## Overview

Motivation

QCD calculation

Phenomenological improvements

Results and Discussion

Outlook

Based on results obtained with A. Bzdak, J-R. Cudell and L. Szymanowski

# The Odderon Conundrum

High energy scattering in QCD  $\longrightarrow$  2 color neutral reggeons with intercepts around 1:  
Pomeron ( $C = +1$ ) and Odderon ( $C = -1$ )

Pomeron: Total cross sections and diffraction

Odderon: Difference between cross sections for  $AB$  and  $A\bar{B}$  and exclusive processes

Searches for Odderon at HERA:  $\gamma p \rightarrow p\pi^0$ ,  $\gamma p \rightarrow \eta_c$ ,  $\gamma p \rightarrow \eta_c X$ ,  
asymmetries in diffractive charm and pion pair production  $\longrightarrow$  no signal found

Some weak evidence for Odderon in elastic  $pp$  and  $p\bar{p}$  scattering at CERN-ISR at  $\sqrt{s} = 53$  GeV in the dip region  $|t| \sim 1.5$  GeV<sup>2</sup>

Odderon is important element of the theory

The first reggeon beyond Pomeron that fulfills BKP equation; [J. Bartels, J. Kwieciński, M. Praszalowicz];  
relevant for considerations of integrability in QCD [L. Lipatov]

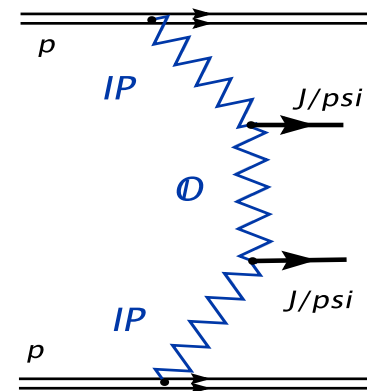
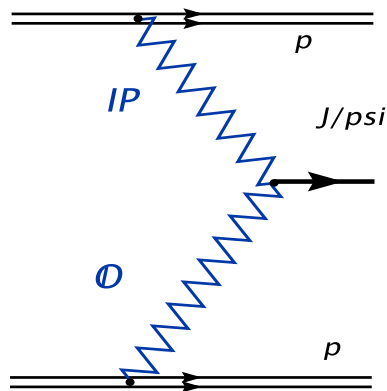
# Proposal of measurement

Exclusive production of vector mesons: [A. Schäfer, L. Mankiewicz, O. Nachtmann 1991], [V. Khoze, A. Martin, M. Ryskin, 2002], [C. Ewerz, 2003]

$pp \rightarrow pp V$  (or  $p\bar{p} \rightarrow p\bar{p} V$ ) with  $V = \phi, J/\Psi, \Upsilon$

$C$ -parity conservation requires the Odderon exchange (or the photon)

Alternatively:  $pp \rightarrow p \text{ gap } V \text{ gap } V \text{ gap } p$



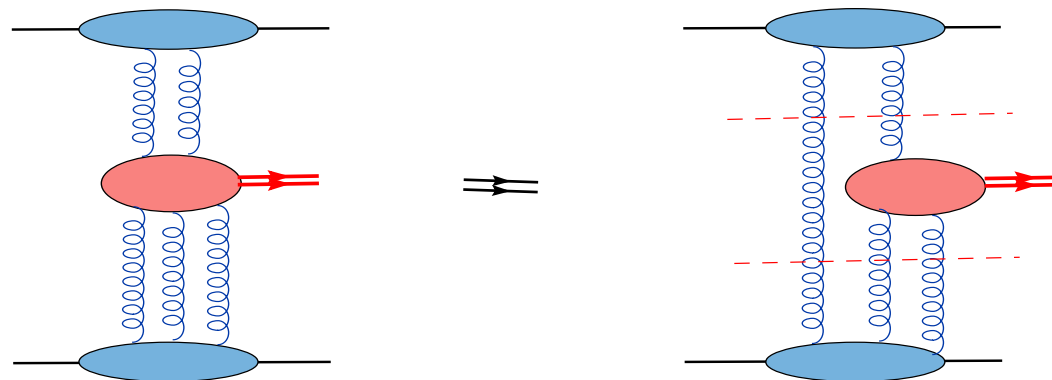
# Formalism

Basic tool – QCD at high energy  $\longrightarrow$  eikonal couplings, discontinuities

Lowest order diagrams for the Odderon and Pomeron exchange

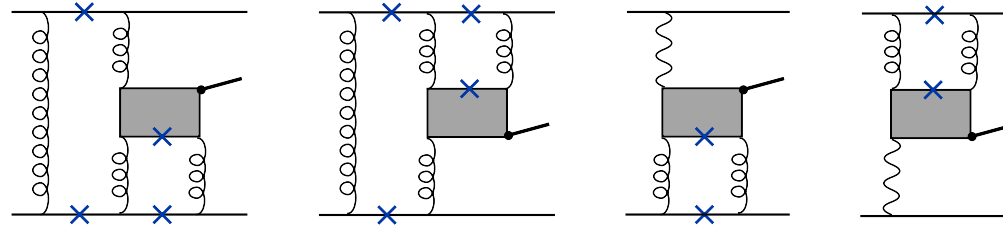


Amplitude and impact factors



# Derivation of the amplitude

Diagrams that contribute to exclusive production of  $C$ -odd meson



$$M = M_{PO}^{(1)} + M_{PO}^{(2)} + M_{\gamma P}^{(1)} + M_{\gamma P}^{(2)}$$

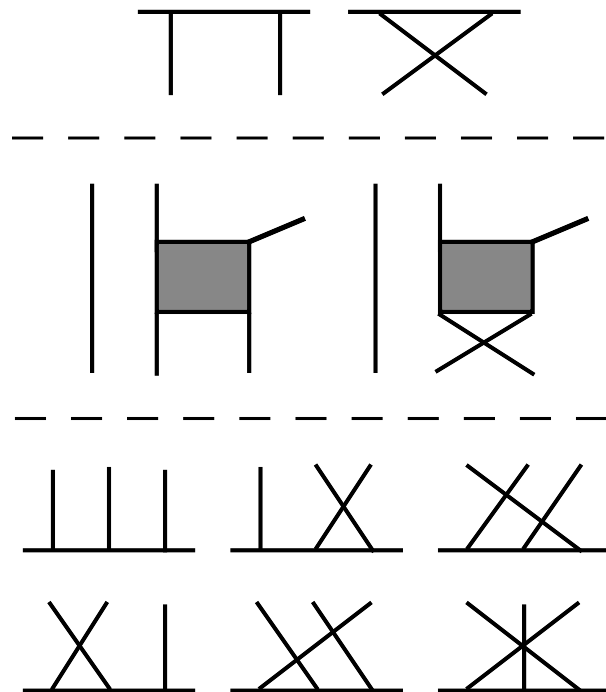
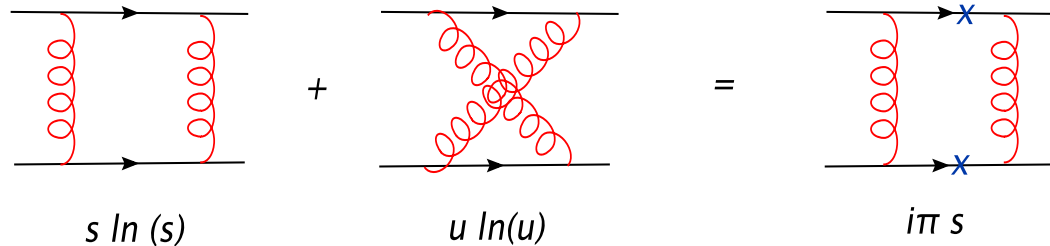
Diagrams evaluated using  $k_T$ -factorisation

$$M_{PO}^{(1)} = \frac{N}{sx'} \int \frac{d^2q_\perp d^2l_\perp}{Q_\perp^2 q_\perp^2 l_\perp^2 h_\perp^2} \Phi_{2g}(-Q_\perp, q_\perp) \Phi_{3g}^{J/\Psi}(q_\perp, h_\perp, l_\perp) \Phi_{3g}(Q_\perp, h_\perp, l_\perp).$$

$$M_{\gamma P}^{(1)} = \frac{N}{sx'} \int \frac{d^2l_\perp}{q_\perp^2 l_\perp^2 h_\perp^2} \Phi_\gamma(q_\perp) \Phi_{3g}^{J/\Psi}(q_\perp, h_\perp, l_\perp) \Phi_{2g}(h_\perp, l_\perp).$$

# Discontinuities and Combinatorics

In the high energy limit the amplitudes are dominated by discontinuities:



All crossings are needed to provide the impact factor with correct analytic properties

→ The definition of impact factors leads to overcounting of diagrams in the amplitude

→ To correct for multiple counting we multiply by  $1/2! \times 1/3!$

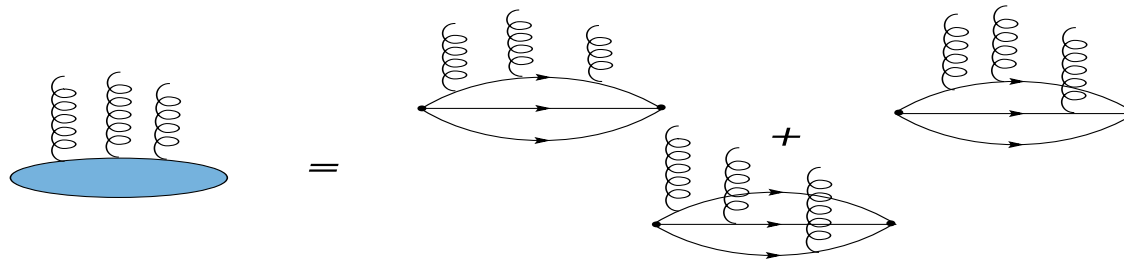
→ The intermediate diagram may be connected in  $2 \times 3$  ways

→ The combinatorial factor  $1/2$  is obtained

# Impact factors

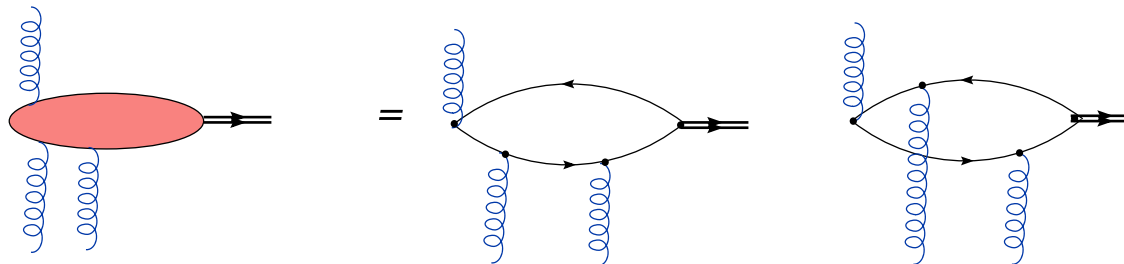
Proton impact factor – Fukugita-Kwieciński model

→ Antisymmetric wave function in color indices + scale  $m_\rho/2$



$3g \rightarrow J/\Psi$  impact factor

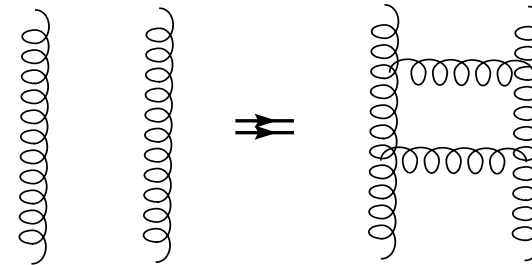
→ standard QCD calculation (with non-relativistic wave function)



# Evolution & gap survival

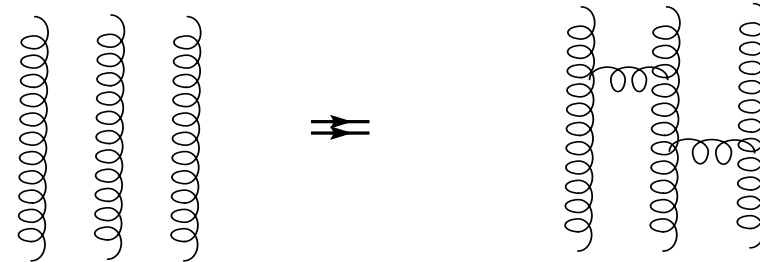
Higher order corrections  $\rightarrow$  ladder diagrams for the Pomeron

$\rightarrow$  enhancement  $\sim x^{-\lambda}$



Bartels-Kwieciński-Praszałowicz (BKP) equation for the Odderon

$\rightarrow$  broadening of the  $t$ -dependence, possible pre-asymptotic enhancement



Soft rescattering corrections: impact parameter profile of  $\mathbb{O} - \mathbb{P}$  fusion similar to  $\mathbb{P} - \mathbb{P}$  fusion. Khoze-Martin-Ryskin estimates of soft gap survival factor  $S^2$  for  $\chi_c$  may be used



# Photon exchange

Instead of the Odderon – the photon may be exchanged

Weizsäcker-Williams approximation:

[V. Khoze, A. Martin, M. Ryskin], [S. Klein, J. Nystrand], [G. Watt, LM]

$$dn_{\gamma/p} \propto \alpha_{em} \frac{dx}{x} \frac{dq^2}{q^2} F(q^2)$$

$$d\sigma(pp \rightarrow pp V) \simeq 2 dn_{\gamma/p} \sigma(\gamma p \rightarrow V p)$$

$\sigma(\gamma p \rightarrow V p) \sim W^{4\delta}$  was measured at HERA

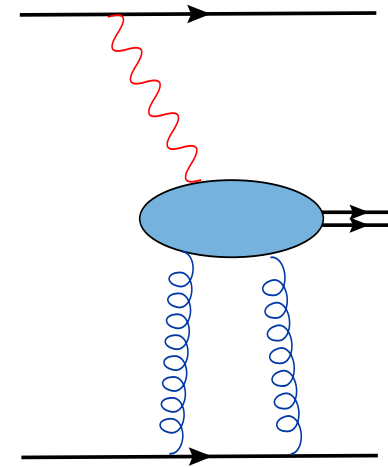
Weizsäcker-Williams spectrum and proton form-factor – upper cut-off:  $q_{max}^2 \sim 0.2 \text{ GeV}^2$

and lower cut-off  $q_{min}^2 \sim M_P^2 M_\Psi^2 / s \sim 2.5 \cdot 10^{-6} \text{ [Tevatron]} \text{ to } 5 \cdot 10^{-8} \text{ GeV}^2 \text{ [LHC]}$

→ dominated by small  $q^2$  → peripheral collisions → little rescattering

→ soft gap survival  $S^2 \sim 0.7 - 0.9$

Sudakov form-factor at  $3g \rightarrow V$  vertex – not important for  $J/\Psi$ , possibly relevant for  $\Upsilon$



The photon and the Odderon contributions do not interfere due to a phase shift

The  $\gamma P$  and  $P\gamma$  interference occurs at very low  $p_T$ -s of the outgoing protons

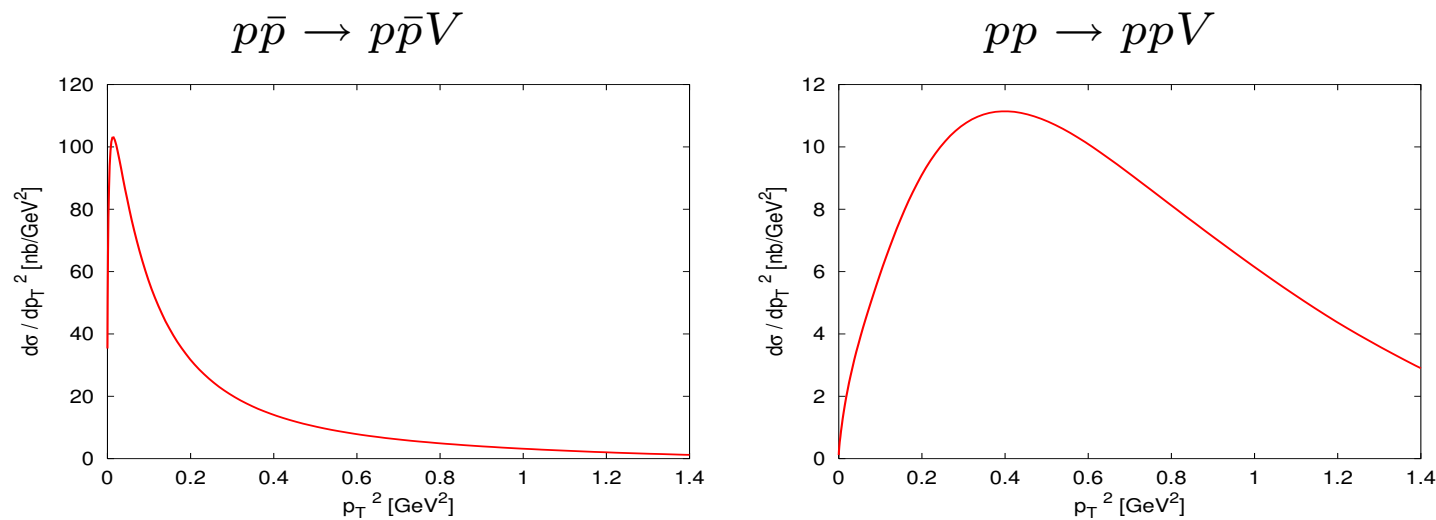
Photon emitter and the target are transformed into each other by a parity transformation

$P$ -parity of vector mesons is negative

→ the interference is destructive for  $pp$  collisions and constructive for  $p\bar{p}$  collisions

Similarly for Odderon – but broader  $p_T$  distribution

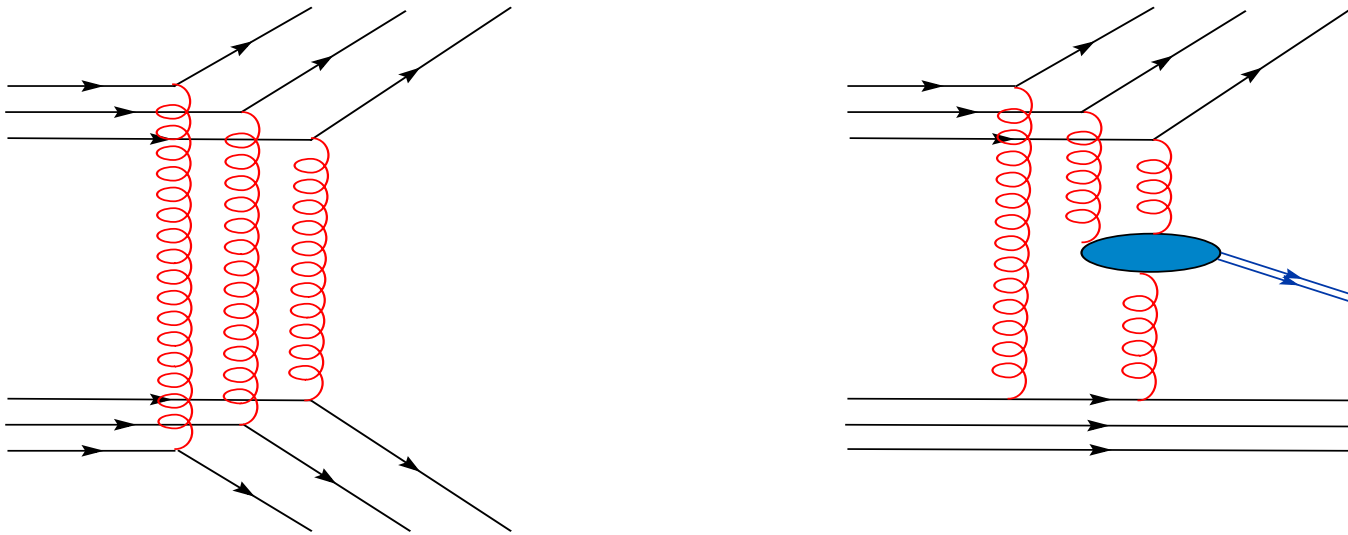
→ interference – quite important for the Odderon:



## Production at larger $p_T$ : Landshoff mechanism

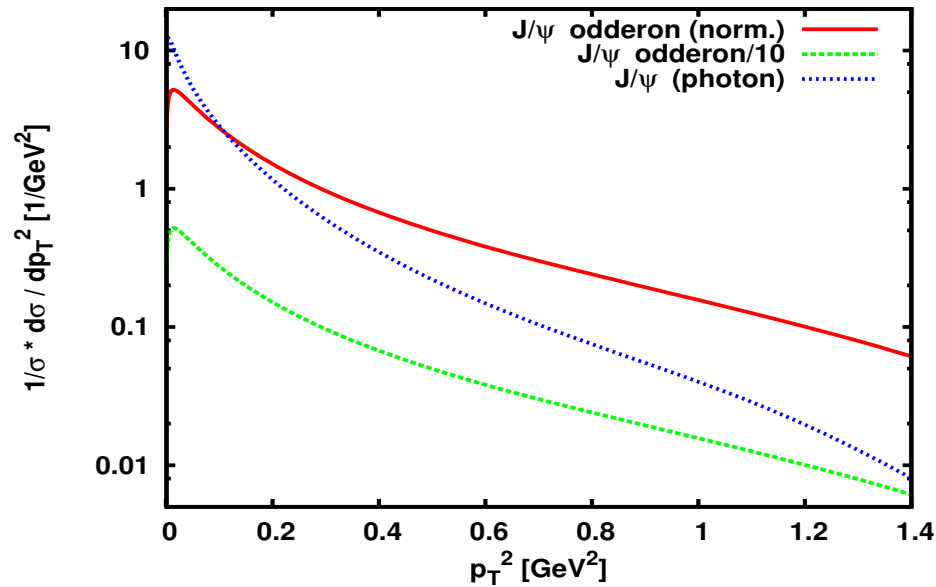
Photoproduction contribution is characterized by a Pomeron driven  $p_T$ -dependence  
 $d\sigma/dp_T^2 \sim \exp(-Bp_T^2)$  with  $B \simeq 4.5 \text{ GeV}^{-2}$

Tail of large  $p_T$  of vector mesons may emerge due to an analogue of the Landshoff mechanism for elastic  $pp$  scattering at large  $|t|$

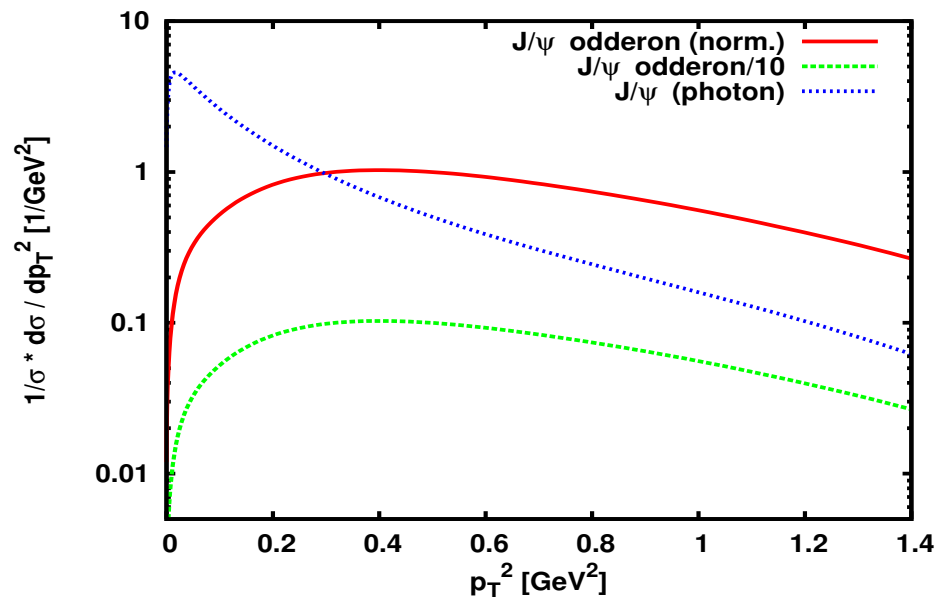


→ Enhanced sensitivity to the Odderon exchange at larger  $p_T$

# Meson $p_T$ distributions: photon / Odderon



Tevatron



LHC

→ Cut on meson  $p_T > 0.6$  GeV should enhance the relative Odderon contribution, especially in  $pp$  collisions

# Improvements & Uncertainties

Photon contribution is well understood  $\sim 30\%$  of uncertainty

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Cross-section mediated by Odderon exchange beyond the lowest order:

$$\sigma(pp \rightarrow ppV) \simeq \bar{\alpha}_s^5 \times \left( \frac{\sqrt{s}x_0}{M_V} \right)^{2\lambda(M_V^2)} \times S^2 \times \sigma_0(pp \rightarrow ppV)$$

High power of **coupling constant**  $\sigma \sim \bar{\alpha}_s^5 \alpha_s^3(M_Q)$

Evolution of the Pomeron (DGLAP/BFKL): standard and well understood

$$\longrightarrow \lambda(M_{J/\Psi}^2) \simeq 0.2, \quad \lambda(M_{\Upsilon}^2) \simeq 0.35 - 0.4$$

Evolution and absorption of the Odderon – not taken into account yet

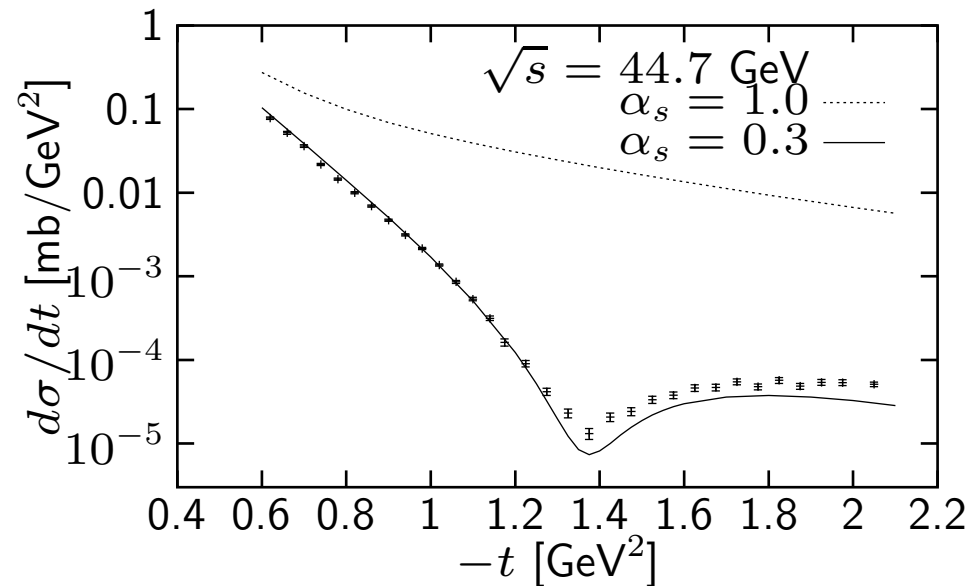
**Soft gap survival factor**  $S^2 \simeq 0.05$  for Tevatron and  $S^2 \simeq 0.025$  for LHC [Khoze, Martin, Ryskin]

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# Constraining Odderon coupling to proton

[G. Dosch, C. Ewerz, V. Schatz]

$\bar{\alpha}_s$  in Fukugita-Kwieciński impact factor for 3 gluons was constrained by fitting elastic  $pp$  and  $p\bar{p}$  cross sections:  $\bar{\alpha}_s \sim 0.3$  was found



Alternatively: total cross section and  $J/\Psi$  photoproduction data indicate  $\bar{\alpha}_s \sim 0.7 - 0.9$

Possible explanations of discrepancy could be e.g. rescattering or absorption of the Odderon

Pessimistic scenario:  $\bar{\alpha}_s = 0.3, S^2 = 1$

Optimistic scenario:  $\bar{\alpha}_s = 1, S^2 = 0.05 - 0.025$

## Results

Photon:  $t$ -integrated  $\frac{d\sigma}{dy}|_{y=0}$ :

[talk by G. Watt]

$p\bar{p} \rightarrow p\bar{p} J/\Psi$  at Tevatron:  $\sim 3$  nb

$pp \rightarrow pp J/\Psi$  at LHC:  $\sim 10$  nb

$pp \rightarrow pp \Upsilon$  at LHC\* (NLO effects!): 0.03—0.07 nb

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Odderon:  $t$ -integrated  $\frac{d\sigma}{dy}|_{y=0}$ :

$p\bar{p} \rightarrow p\bar{p} J/\Psi$  at Tevatron: 0.2 — 3 nb

$pp \rightarrow pp J/\Psi$  at LHC: 0.3 — 3 nb

$pp \rightarrow pp \Upsilon$  at LHC\*: 0.002 — 0.02 nb

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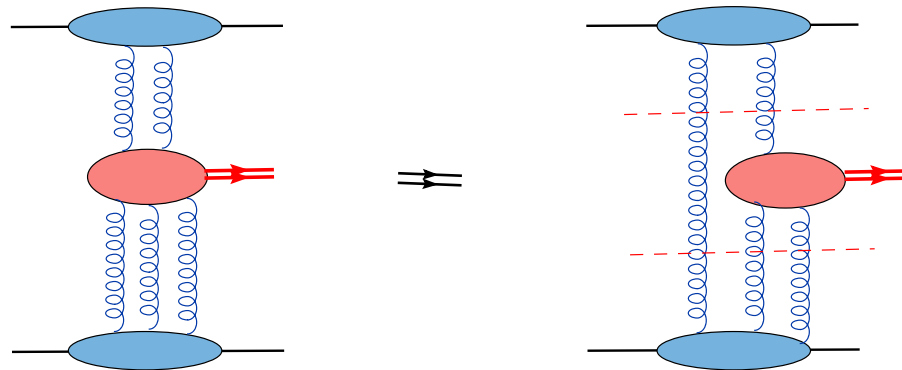
# Comparing with KMR estimates

Pioneering estimate in QCD by [V. Khoze, A. Martin, M. Ryskin, 2002]

Explicit evaluation of quark diagrams:



Many differences: diagram selection,  $\alpha_s$ , gap survival



Final results similar



## Enhancing the Odderon by $p_T$ -cut

Photon Weizsäcker-Williams spectrum:  $\sim \frac{dp_T^2}{p_T^2}$  — dominated by  $p_T^2 \ll 0.1 \text{ GeV}^2$

Odderon contribution tends to be much broader in  $p_T$  — characteristic  $p_T^2 \sim 0.25 \text{ GeV}^2$  and a power-like tail due to Landshoff mechanism

Pomeron–Odderon fusion gives  $p_T$ -distributions of **both** outgoing proton transverse momenta characterised by a scale  $t_0 \sim 0.25 \text{ GeV}^2$

Pomeron-Photon fusion gives one proton with very small  $p_T$

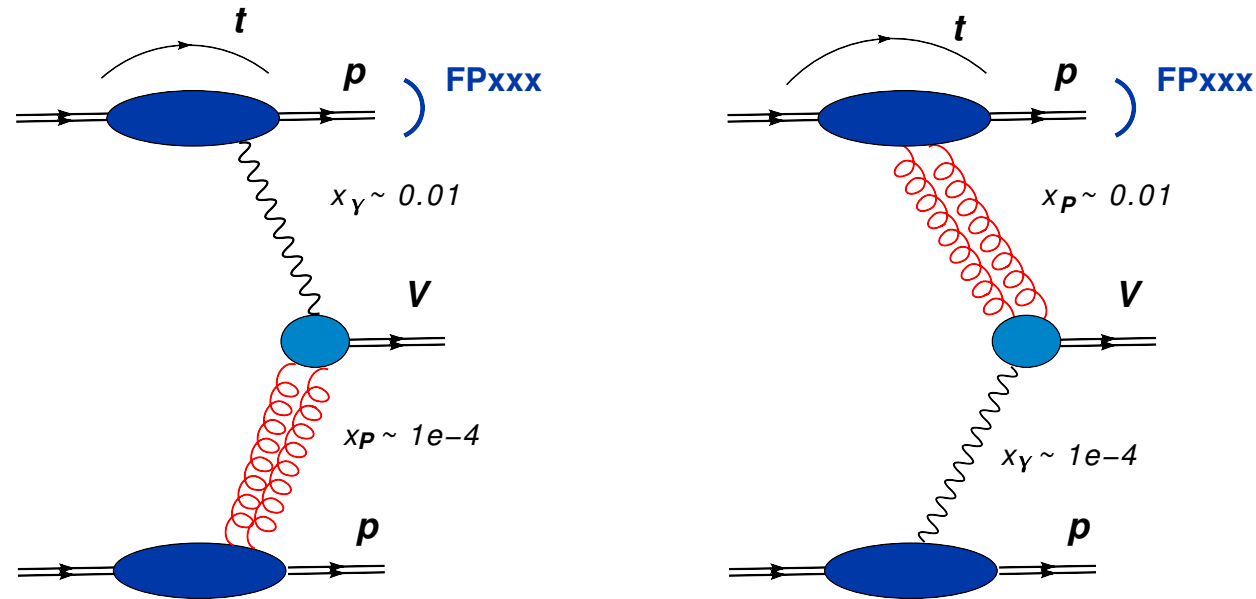
Sensitivity to Odderon may be improved by measuring protons'  $p_T$ :

with both  $|t_1| > 0.25 \text{ GeV}^2$  and  $|t_2| > 0.25 \text{ GeV}^2$ :

photon contribution decreases  $\sim 200$  times and Odderon – only  $\sim 10$  times

## Employing Forward Detectors

In production of  $\Upsilon$  at LHC — impossible to observe both protons... but maybe one is enough?

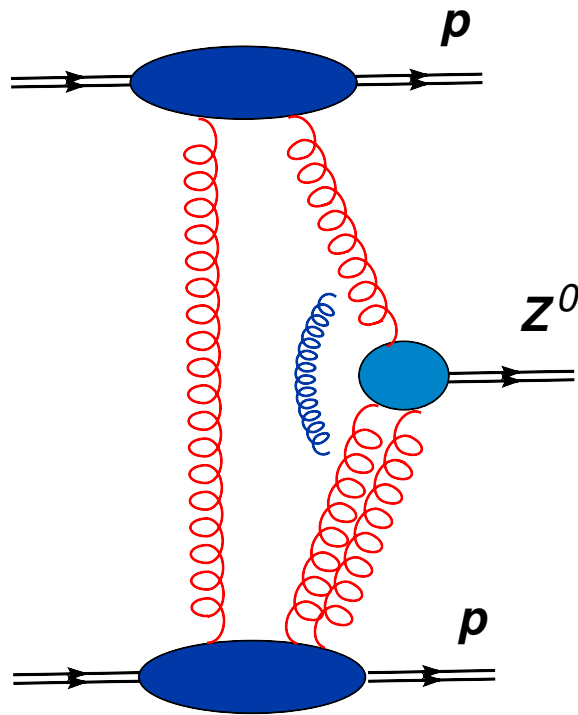


For  $\Upsilon$  production and  $x_1 \sim 0.01$ :  $M(\gamma P) \sim 7 M(P\gamma)$  [gluon evolution]

- Cut:  $|t| > 0.25 \text{ GeV}^2$  — leading contribution severely reduced
- total  $\gamma P$  cross section reduced by more factor  $\sim 20$
- Odderon contribution — reduced by factor of  $\sim 2$

## Comment: exclusive $Z^0$

Odderon may compete with photon in exclusive  $Z^0$  production [talk by G. Watt]



→ Odderon contribution negligible

[Odderon : photon] ratio  
expected to be small

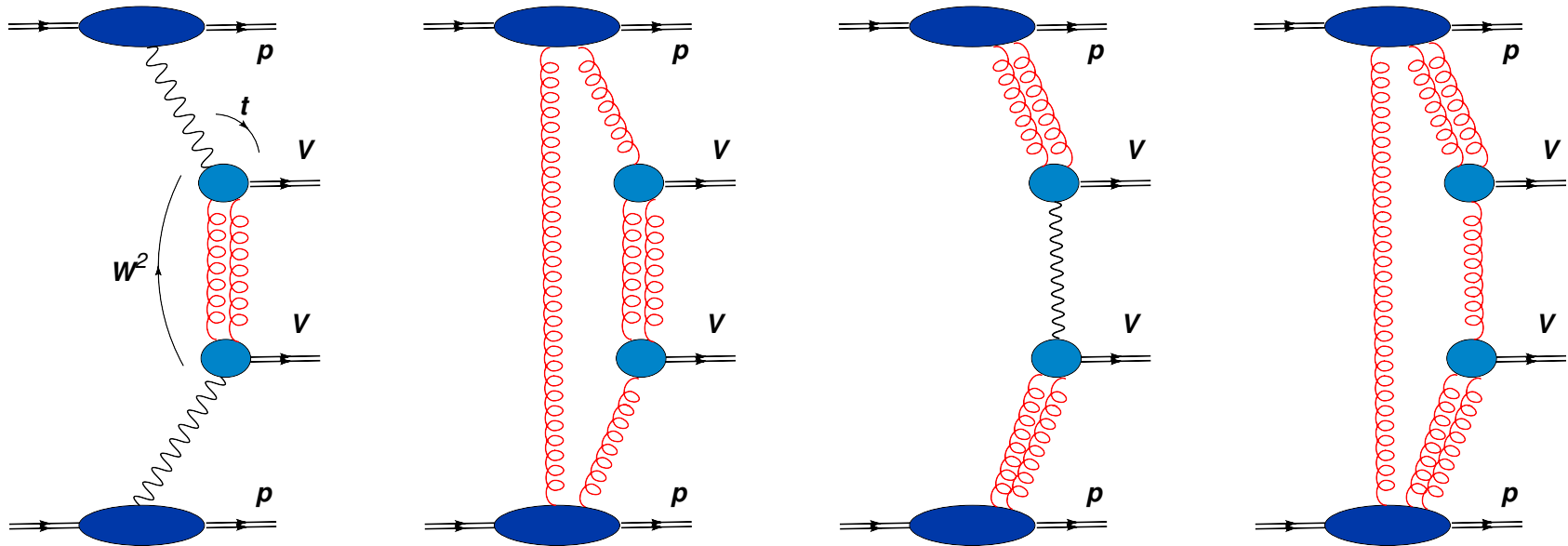
→ small  $\alpha_s(M_Z) <$   
 $\alpha_s(M_V)$

→ generalized Sudakov  
effects are important

# Outlook: double (twin?) exclusive vector meson production

Exclusive two vector meson production with large separation in rapidity

Various subprocesses contribute:



Good chance that P–O–P contribution is dominant

Relatively precise estimates can be made

Very preliminary estimates for  $J/\Psi$  are promising

Also interesting and calculable is double  $\rho^0$  production at high  $t$

## How to find the Odderon?

1. Measure exclusive  $pp \rightarrow pp J/\Psi$  or  $pp \rightarrow pp \Upsilon$  and compare to photon contribution
2. Cut on transverse momentum of VM and compare to photon
3. Cut on transverse momenta of two outgoing protons and compare to photon
4. If (3) impossible: cut on one outgoing proton in forward meson production
5. Try to find the excess
6. If nothing works with single meson — try to double it