Jets and resummation

Mrinal Dasgupta

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Motivation.

- Issues and challenges in jet resummations.
- The dijet azimuthal decorrelation.
- Future developments.

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Motivation



Striking success of event shapes – general lessons or a one off Pokshitzer, Lucenti, Marchesini, Salam 1998

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A history of surprises



 Apply e⁺e⁻ ideas blindly to e.g. single hemisphere DIS event shapes – breakdown of techniques , need for non-global logarithms , large N_c approximation.

Salam and MD 2002

• Look for non-global logarithms in gaps between jet studies in hadron -collisions using "well-known standard techniques" – find breakdown of naive coherence (super leading logarithm $\alpha_s^4 \ln^5 Q/Q_0$).

Forshaw Kyrieleis an<u>d</u> Se<u>y</u>mou<u>r</u> 200

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 Use well accepted resummation formulae in situations involving running of a jet algorithm – find extra logarithms that depend on algorithm parameters. Banfi and M.D. 2004, Banfi Delenda and M.D. 2006

Lesson – Important to keep testing "established" ideas in different contexts. Helps design better observables for future phenomenology - e.g. event shapes at hadron colliders. Banfi, Salam, Zanderighi 2005



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Include

Dijet rates with symmetric E_t cuts.

• Dijet invariant mass near threshold x = -Kidonakis, Oderda, Sterman 1998

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$$x = \frac{M_{jj}^2}{\sqrt{\hat{s}}} \to 1.$$

- Inclusive jet spectra $x_t = \frac{2p_t}{\sqrt{s}} \rightarrow 1$. Kidonakis Oderda and Sterman 1998, De Florian and Vogelsang 2007
- Dijet azimuthal decorrelations $\Delta \phi_{jj} \rightarrow \pi$.
- Energy flow between jets with a clustered or jet defined final state. Appleby and Seymour 2002, Banfi and MD 2005 Banfi, Delenda and MD 2006

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Making the *Ap* global

Kinematics in the transverse plane :

$$\begin{aligned} \vec{p}_{t,1} &= p_{t,1}(1,0), \\ \vec{p}_{t,2} &= p_{t,2}(\cos(\pi-\epsilon),\sin(\pi-\epsilon)), \\ &= p_{t,2}(-\cos\epsilon,\sin\epsilon), \\ \vec{k}_{t,i} &= k_{t,i}(\cos\phi_i,\sin\phi_i) \end{aligned}$$

From momentum conservation $\epsilon = -\sum_{i} \frac{\kappa_{t,i}}{p_t} \sin \phi_i$ Use an E_t weighted recombination scheme (H1 collaboration)

$$\phi_j = \frac{\sum_{i \in j} E_{t,i} \phi_i}{\sum_{i \in j} E_{t,i}}$$

Then

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Then

$$\phi_{j1} = \frac{\sum_{i \in j1} k_{t,i} \phi_i}{p_{t,1} + \sum_{i \in j1} k_{t,i}} \approx \frac{\sum_{i \in j1} k_{t,i} \phi_i}{p_t},$$

Jets and resummation

$$\phi_{j2} = \frac{\sum_{i \in j2} k_{t,i} \phi_i + p_{t,2}(\pi - \epsilon)}{p_{t,2} + \sum_{i \in j2} k_{t,i}} \approx (\pi - \epsilon) + \frac{\sum_{i \in j2} k_{t,i}(\phi_i - \pi)}{p_t},$$

Finally we have

$$|\pi - \Delta \phi| = \left| \sum_{i} \frac{k_{t,i}}{p_t} \left(\sin \phi_i - \theta_{i1} \phi_i - \theta_{i2} (\pi - \phi_i) \right) \right| + \mathcal{O} \left(k_t^2 \right),$$

Both gluons inside and out of jets contribute. Observable in fact continuously global and resummable to NLL accuracy.

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$$\tan \phi_j = \frac{p_{t,y}}{p_{t,x}}$$

with
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Resummation in b space leads to (for dijets in DIS)

$$\Sigma_a(\{p\},\Delta) = \frac{1}{\pi} \int_{-\infty}^{\infty} \frac{db}{b} \sin(b\Delta) e^{-R_a(b)} f_a(x,\mu_f^2/b^2).$$

 $\Delta \equiv |\pi - \Delta \phi|$ Similar result with two pdfs for hadron collisions $\sin(b\Delta)$ function reflects phase space constraint while R(b) contains the QCD dynamics. Result of their convolution - no Sudakov peak. Distribution in Δ goes smoothly to non-zero value as $\Delta \rightarrow 0$.

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DIS dijets

In

$$\begin{aligned} R_{\text{out}}^{a}(\bar{b}) &= (C_{1}^{a} + C_{2}^{a})\frac{\alpha_{s}}{2\pi} \left(\frac{2}{3}L^{2} + \frac{4}{3}L\left(-\ln 3 - 4\ln 2 + 3\ln \frac{Q}{p_{t}}\right)\right) \\ &+ \frac{4}{3}\frac{\alpha_{s}}{2\pi} \left(C_{1}^{a}B_{1}^{a} + C_{2}^{a}B_{2}^{a}\right)L, \\ R_{\text{in}}^{a} &= C_{i}^{a}\frac{\alpha_{s}}{2\pi} \left(2L^{2} + 4L\left(-\ln 2 + \ln \frac{Q}{p_{t}}\right)\right) + 4C_{i}^{a}\frac{\alpha_{s}}{2\pi}B_{i}^{a}L, \\ \ln S(\bar{b}, \{p\}) &= -4L \left(2C_{F}\frac{\alpha_{s}}{2\pi}\ln \frac{Q_{qq'}}{Q} + C_{A}\frac{\alpha_{s}}{2\pi}\ln \frac{Q_{qg}Q_{gq'}}{Q_{qq'}Q}\right), \end{aligned}$$
with $L = \ln \bar{b}$

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Results(Hadron Collisions)

$$\begin{aligned} \mathsf{R}_{\text{out}}(\bar{b}) &= (C_1 + C_2) \frac{\alpha_s}{2\pi} \left(\frac{2}{3} L^2 + \frac{4}{3} L \left(-\ln 3 - 4\ln 2 + 3\ln \frac{Q_{12}}{p_t} \right) \right) + \\ &+ \frac{4}{3} (C_1 B_1 + C_2 B_2) \frac{\alpha_s}{2\pi} L, \\ R_{\text{in}} &= (C_{i1} + C_{i2}) \frac{\alpha_s}{2\pi} \left(2L^2 + 4L \left(-\ln 2 + \ln \frac{Q_{12}}{p_t} \right) \right) + \\ &+ 4 (C_{i1} B_{i1} + C_{i2} B_{i2}) \frac{\alpha_s}{2\pi} L, \\ \ln S &= \ln \frac{\text{Tr} \left(H e^{-t\Gamma^{\dagger}/2} M e^{-t\Gamma/2} \right)}{\text{Tr} (HM)} \end{aligned}$$



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- Need to account for NP effects "intrinsic" k_i
- Comparisons with data from HERA and Tevatron



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