

# *PDF uncertainties using Monte Carlo method*

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DESY

- ✦ Introduction
- ✦ Method
- ✦ Gaussian distribution of errors
- ✦ Log-normal, uniform distribution of errors
- ✦ Summary

# Introduction

The idea is to use a simple Monte Carlo technique to estimate PDF uncertainties which would provide:

- ✦ An independent cross check of the standard errors estimation
- ✦ Flexibility in testing various assumptions for the uncertainties distribution:

$$\sigma \sim \frac{N}{\mathcal{L}A}$$

- ✦ A detector acceptance,  $\mathcal{L}$  luminosity
- ✦ Systematic Uncertainties from  $A$  and  $\mathcal{L}$  are non-Gaussians ( $\mathcal{L}, A > 0$ )
  - ✦ Log-Normal distribution
- ✦ Some systematic uncertainties are “upper” limits:
  - ✦ Uniform distribution

# Method (1/2)

## ◆ Notations:

◆ Data point  $\rightarrow \sigma_i$

◆ Uncorrelated Uncertainty  $\rightarrow \delta_i^{uncorr}$

◆ Correlated systematic sources  $\alpha_j$  with their effect on data points  $\delta_{ij}^{corr}$

## ◆ Prepare a shifted data set:

◆ Shift the central value by taking into account the uncorr. and corr.errors:

### ◆ For Gauss Distribution of the errors:

◆ For only uncorrelated uncertainties:  $\sigma_i = \sigma_i(1 + \delta_i^{uncorr} RAND_i)$

◆ For correlated uncertainties: generate shifts for  $\alpha_j \rightarrow RAND_j$

$$\sigma_i = \sigma_i(1 + \delta_i^{uncorr} RAND_i + \sum_j^{N_{sys}} \delta_{ij}^{corr} RAND_j)$$

$RAND_i$  is Gauss Random Number Generator with mean 0



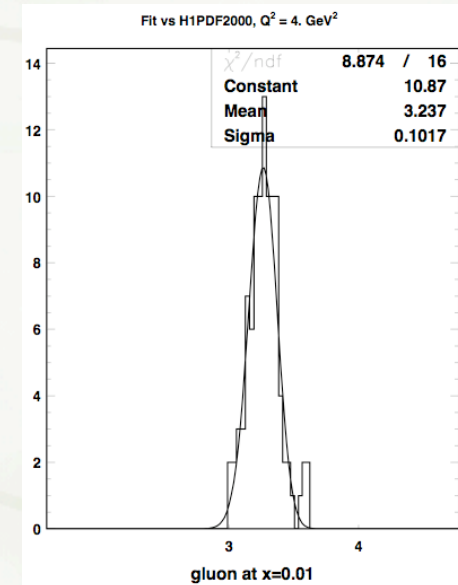
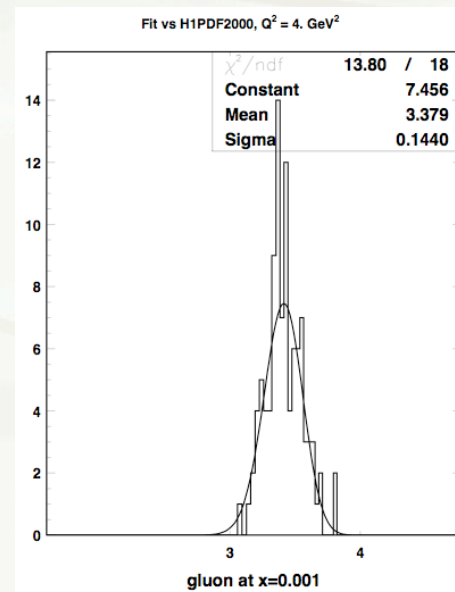
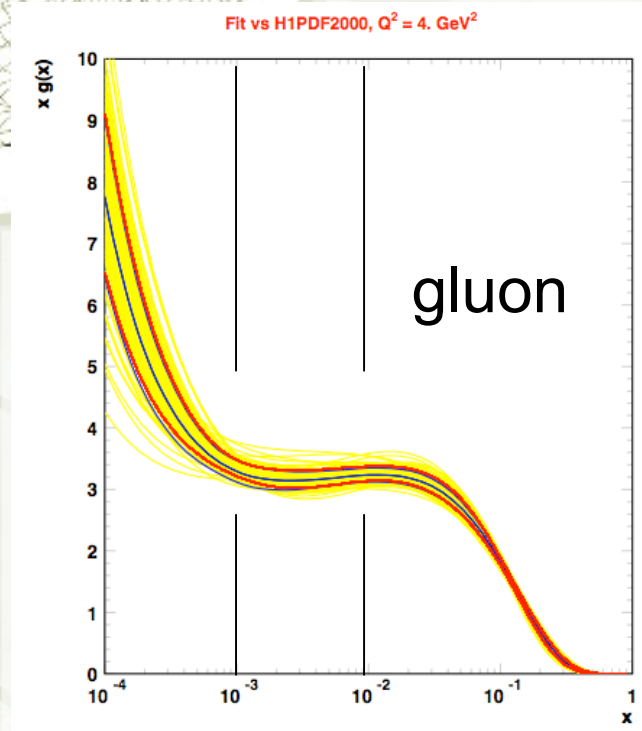
## Method (2/2)

- ★ Repeat the preparations for N times (here  $N \geq 100$ )
- ★ Perform the fit N times to extract PDFs
- ★ PDF uncertainties => from the RMS of the spread
- ★ This study is performed using:
  - ★ published H1-HERA I data of NC and CC  $e_{\pm}p$  scattering cross sections [ref: *Eur. Phys. J. C* 30, 1-32 (2003)]
  - ★ Fit program H1 QCDNUM implementation at NLO:
    - ★  $\overline{\text{MS}}$  renormalisation scheme, DGLAP evolution at NLO, massless quarks, polynomial form for PDF parametrisation a la H1PDF2000

# Gaussian Errors

- ★ To test the method, assume all errors follow Gauss distribution and compare the results to standard error estimation

[PDF4LHC, April 2008]



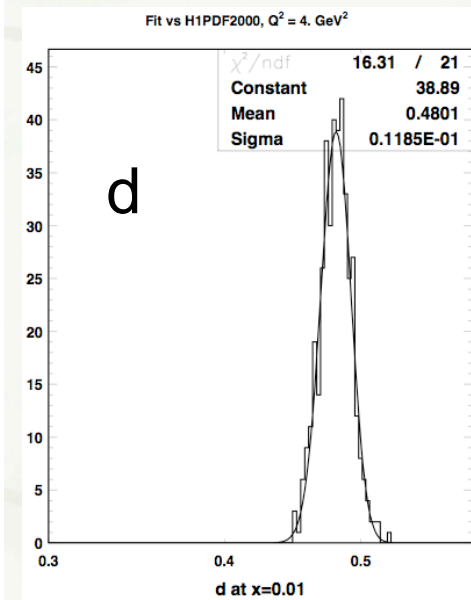
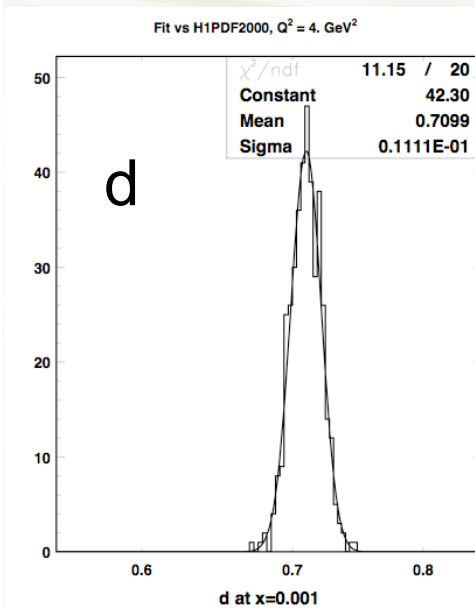
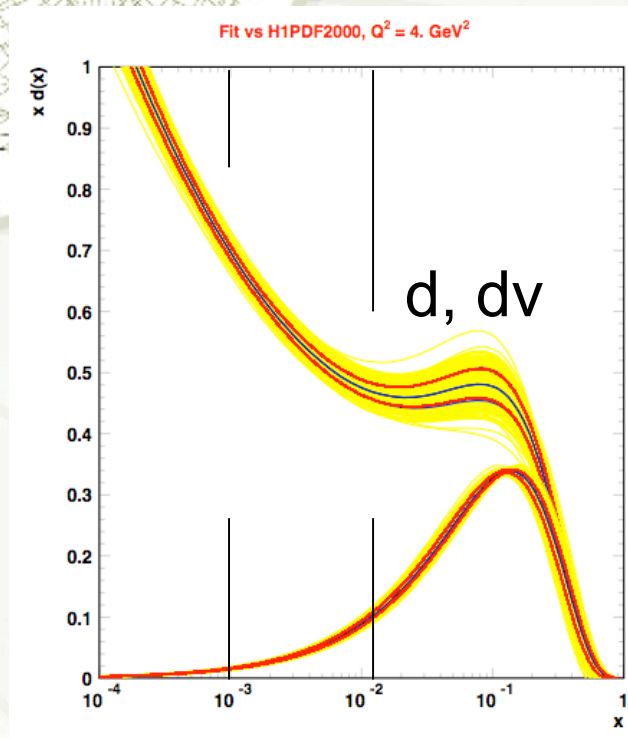
- ★ 400 Yellow lines
- ★ Red lines: PDF uncertainties from RMS
- ★ Blue lines: Hessian errors

Good agreement

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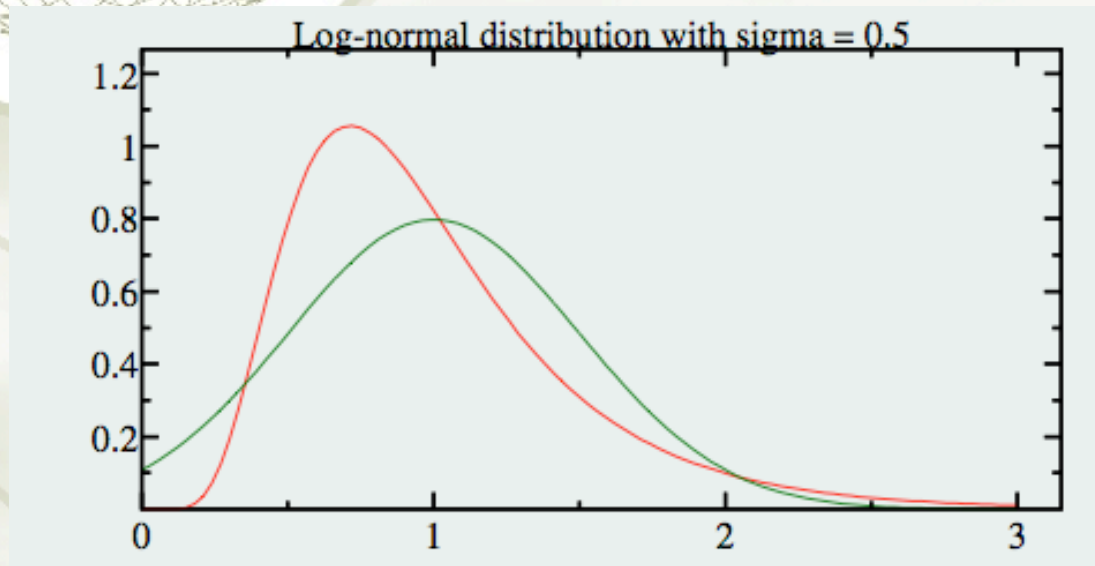


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# Log-normal Distribution

- ★ Normalisation error follows a log-normal distribution
  - ★ product of random variables [V. Blobel]



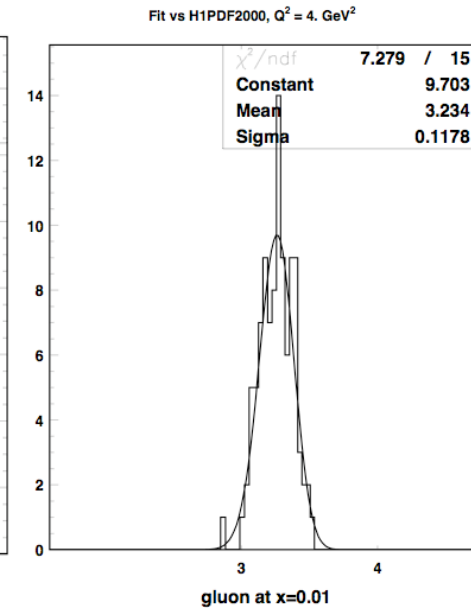
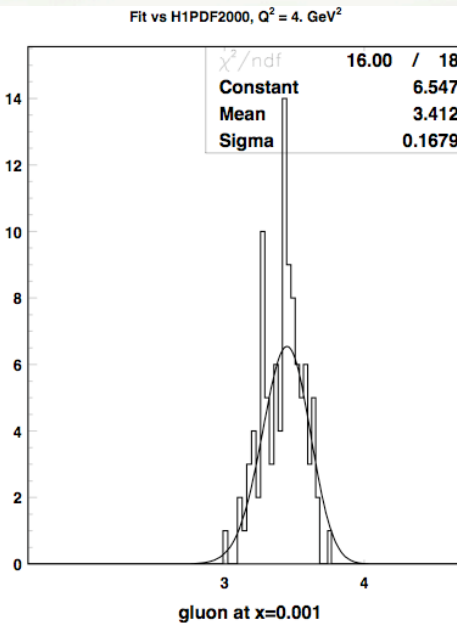
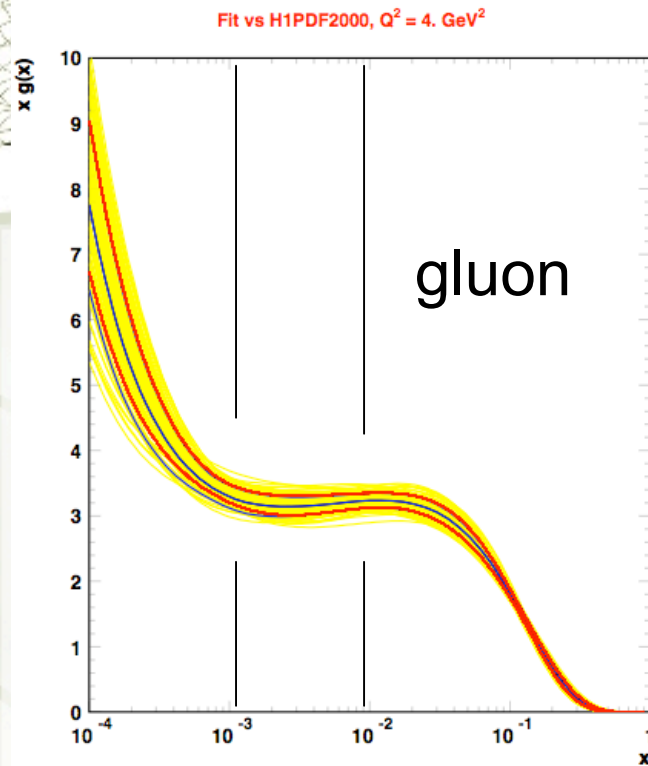
- Comparison between Log-normal and Gauss Distribution:
  - same mean (here 1)
  - shifted peaks

Hence, it is interesting to test the effect on PDFs!

→ use Log-Normal Random Number Generator in the data preparation to extract PDFs from the fits

# 1. Log-normal dist. for Lumi

- ◆ Assume that all errors, apart from Lumi uncertainty follow Gauss
- ◆ Distribution for lumi uncertainty is assumed Log-normal here



Similar effect to pure gaussian case!

- ◆ 100 Yellow lines
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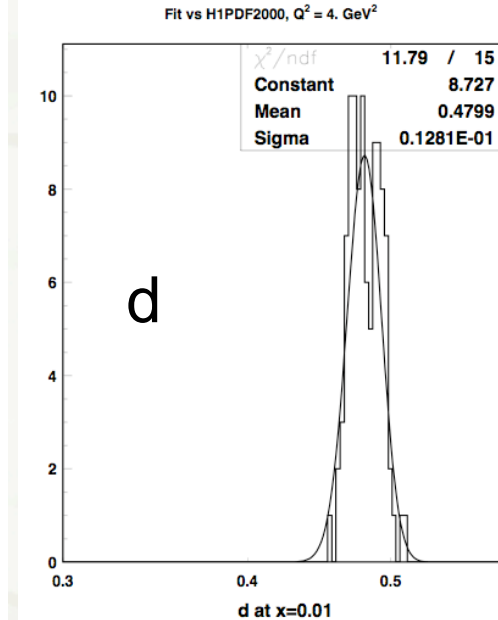
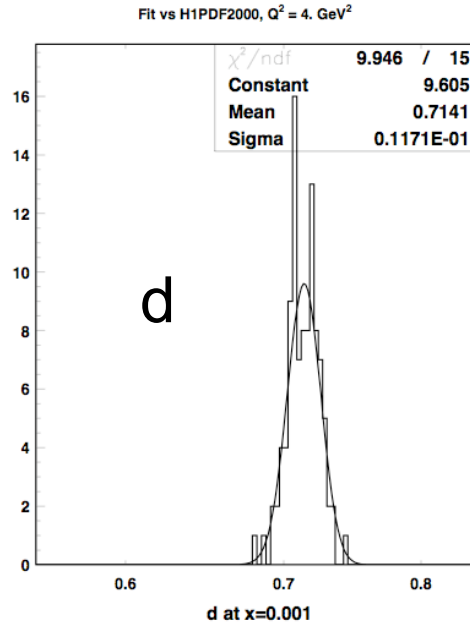
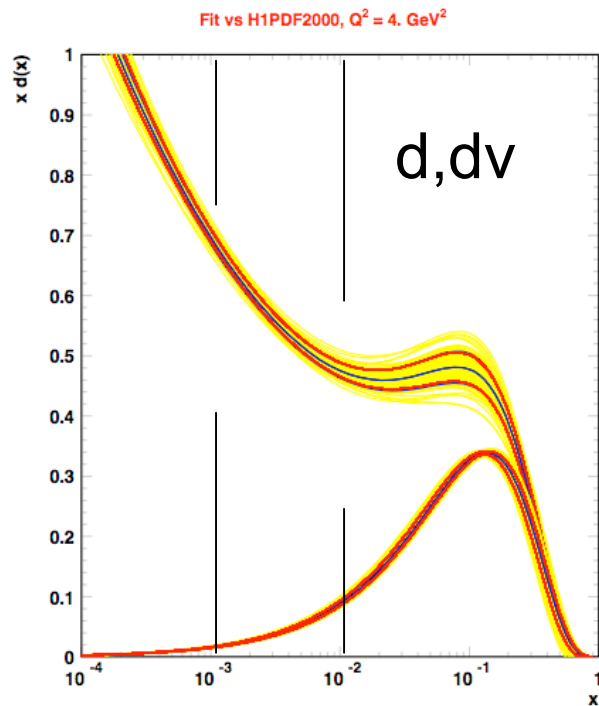
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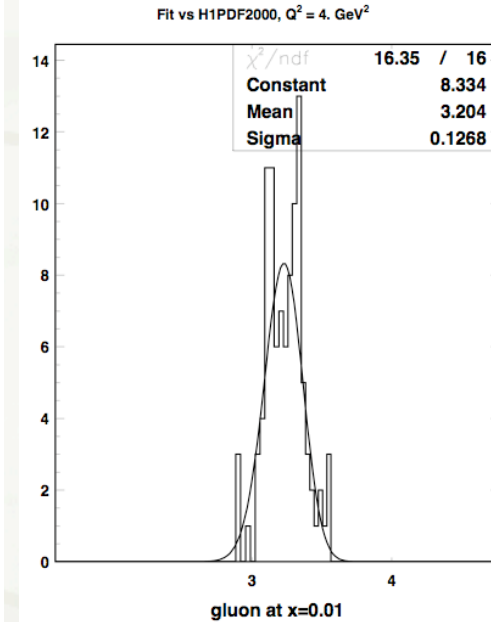
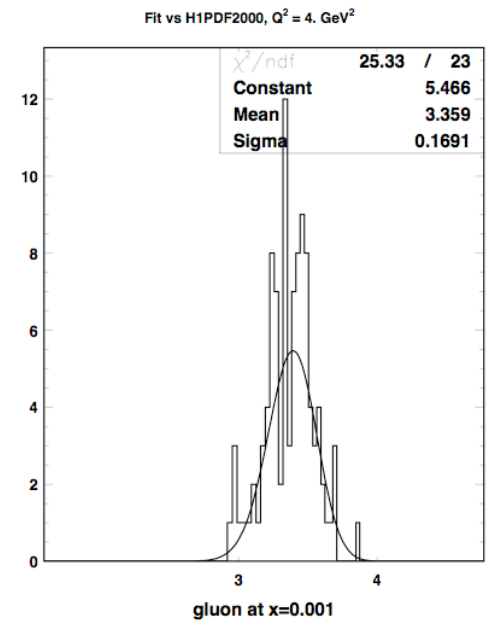
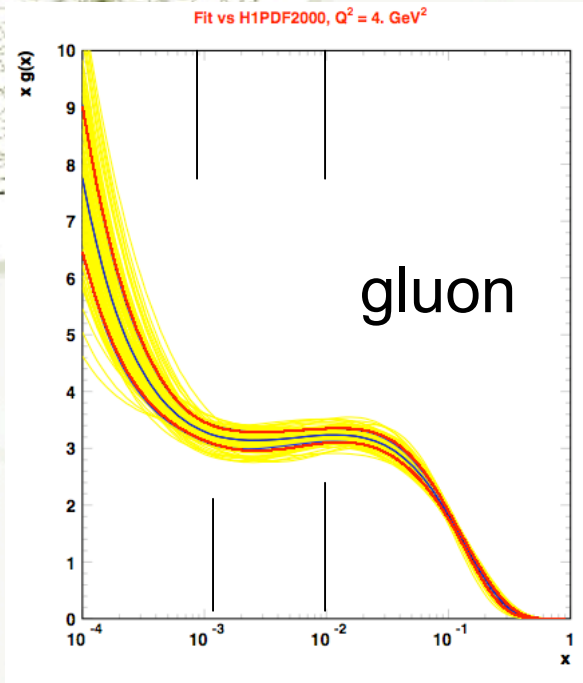


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## 2. Uniform dist. for all errors

- Assume that all errors follow Uniform Distribution

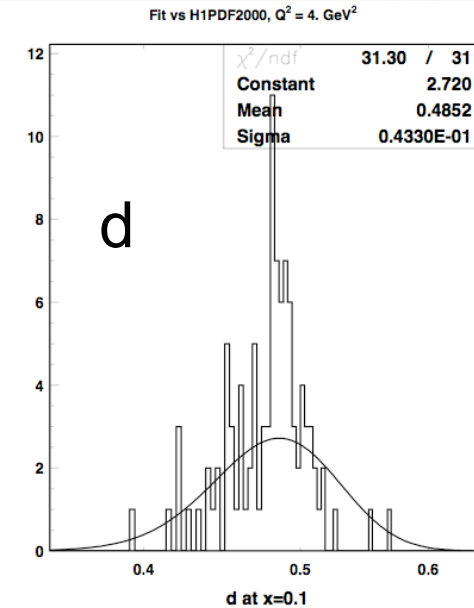
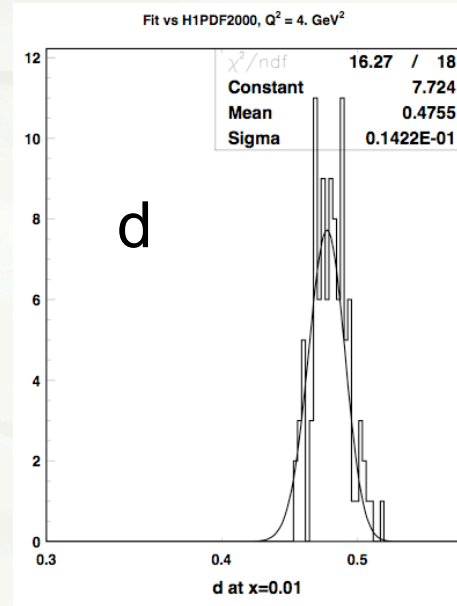
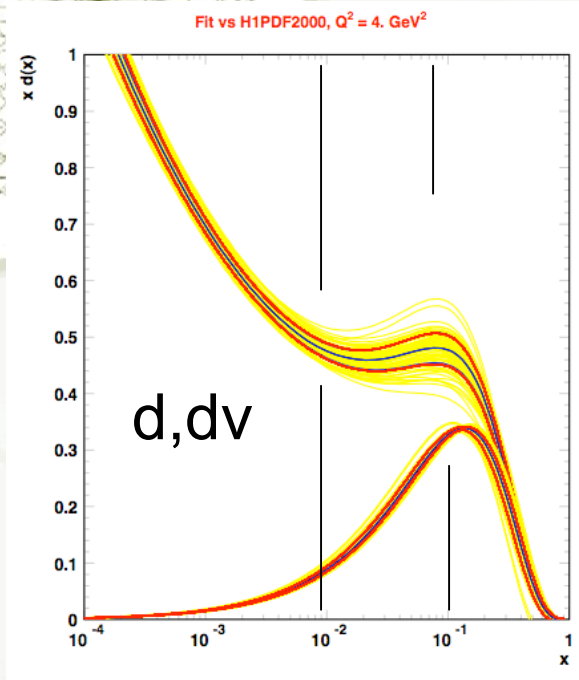


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# Summary

- ★ A simple method to estimate PDF uncertainties built within QCD Fit framework:
  - ★ Assuming only Gaussian distribution of the errors agrees well with the standard error estimation
- ★ Allows to check non-Gaussian distributions for the experimental uncertainties:
  - ★ Results are similar to Gaussian case when using log-normal and uniform distributions of the uncertainties
- ★ Method could be extended for other variables (i.e. cross sections) for cross checks with standard error evaluation