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# Valence quarks and $k_T$ factorisation

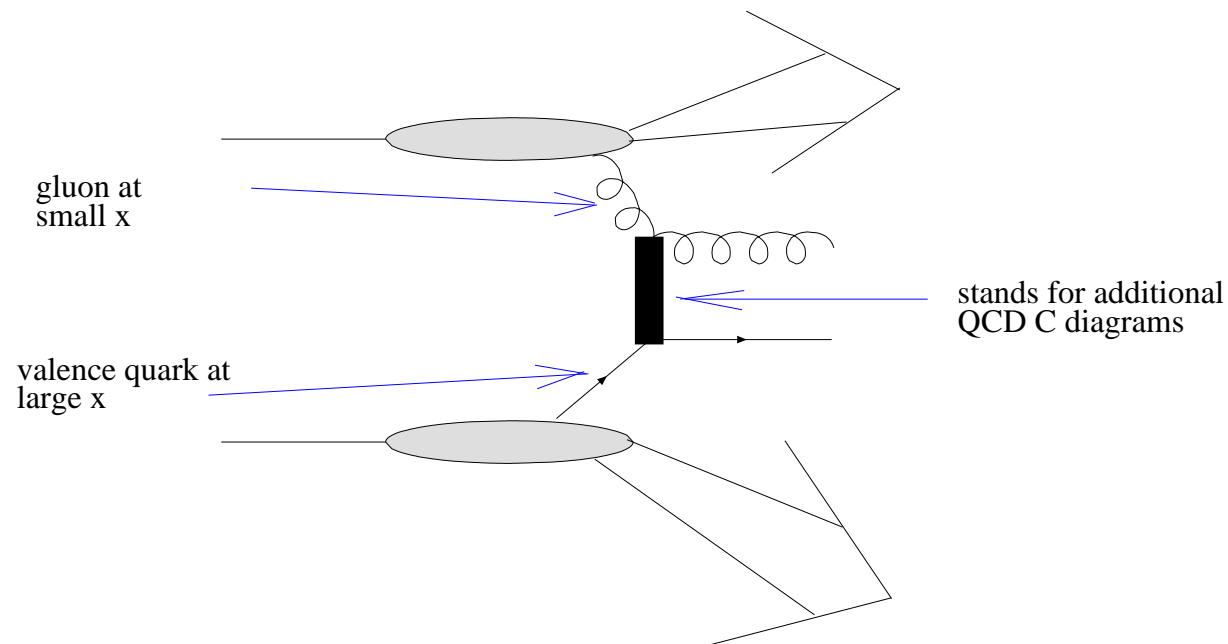
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DESY, Hamburg

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## Motivation

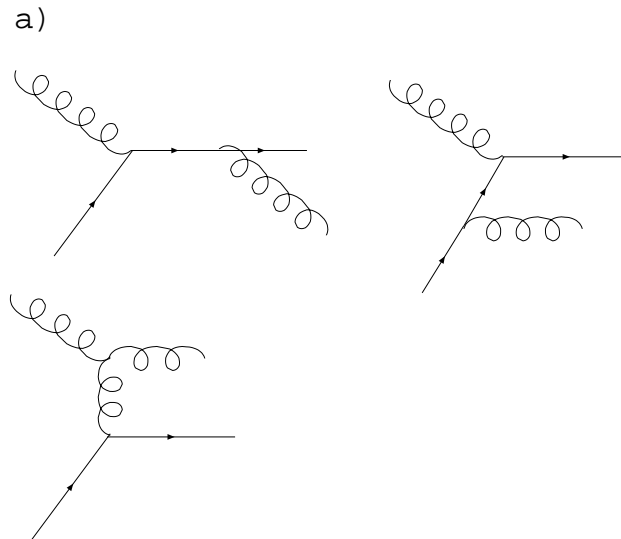
- HERA  $\rightarrow$  hints that at rapidities  $y > 3$  there can be new kind of dynamics  $\rightarrow$  BFKL, CCFM, BK. However, at HERA we cannot go to the more forward region.
- LHC will allow for this study. The interesting region can be studied if we consider QCD Compton scattering:



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## Jets at LHC - collinear approach

Jets are initiated by hard subprocesses QCD Compton. It is the relevant hard process if we want to study low  $x_g$  effects where  $x_g$  is a longitudinal momentum fraction carried by gluon.

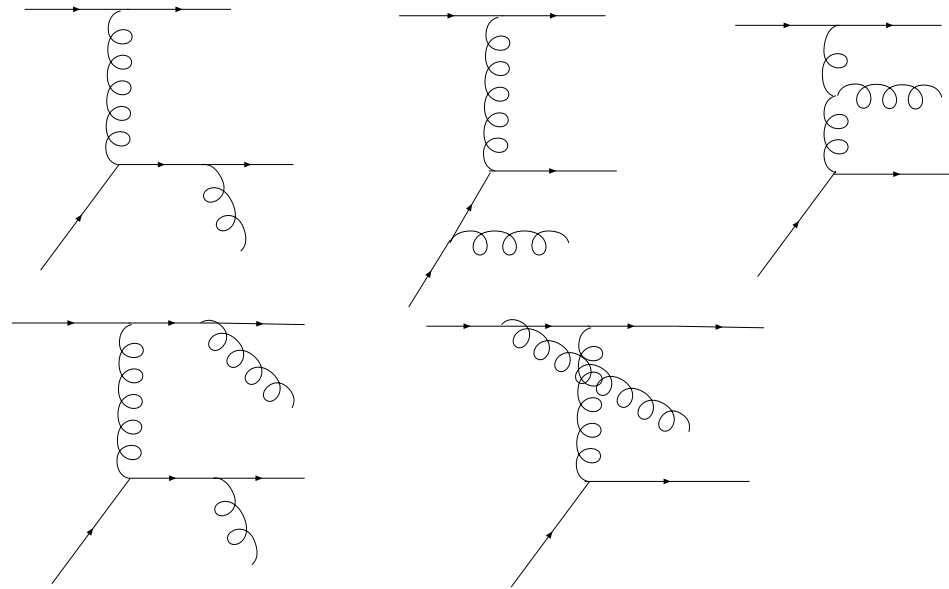


To go to low  $x_g$  safely we need to consider off-shell gluon...

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## QCD Compton in $k_T$ factorisation

Incoming gluon is not collinear to the proton it is off-shell. Valence quark is collinear to the proton. The upper quark line  $\rightarrow$  replaced by gluon distribution after matrix element is calculated



All five diagrams are required by gauge invariance.

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## Details of kinematics

The Sudakov decomposition is:

$$k = x_g p_A + z_g p_B + k_T$$

$$q = x_q$$

$$k' = x_{g'} p_A + z_{g'} p_B + k'_T$$

$$q' = z_{q'} p_A + x_{q'} p_B + q'_T$$

Mandelstam variables are:

$$s = (p_1 + p_2)^2$$

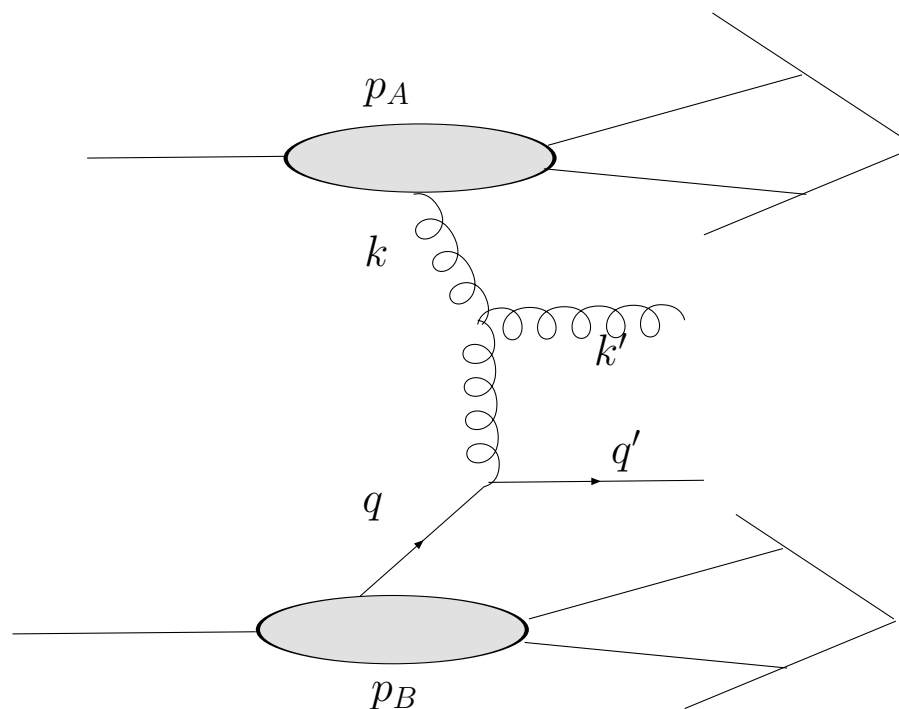
$$\hat{s} = (k + q)^2$$

$$\hat{u} = (k - q')^2$$

$$\hat{t} = (k - k')^2$$

We are interested in configuration where:

$$\hat{s}, \hat{t}, \hat{u} \ll s$$



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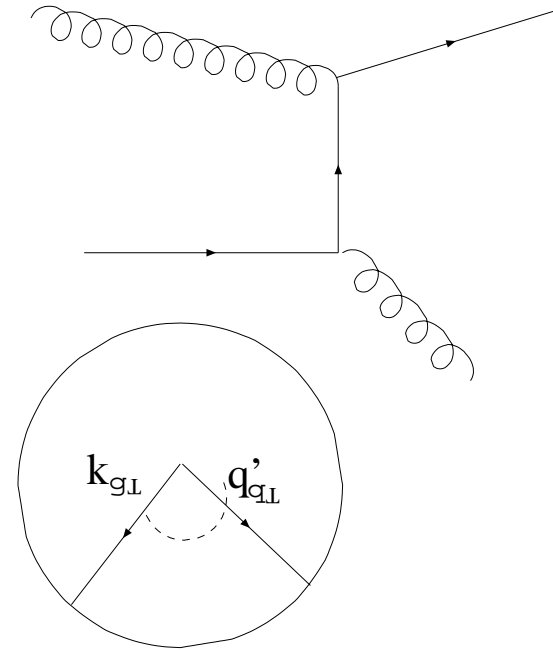
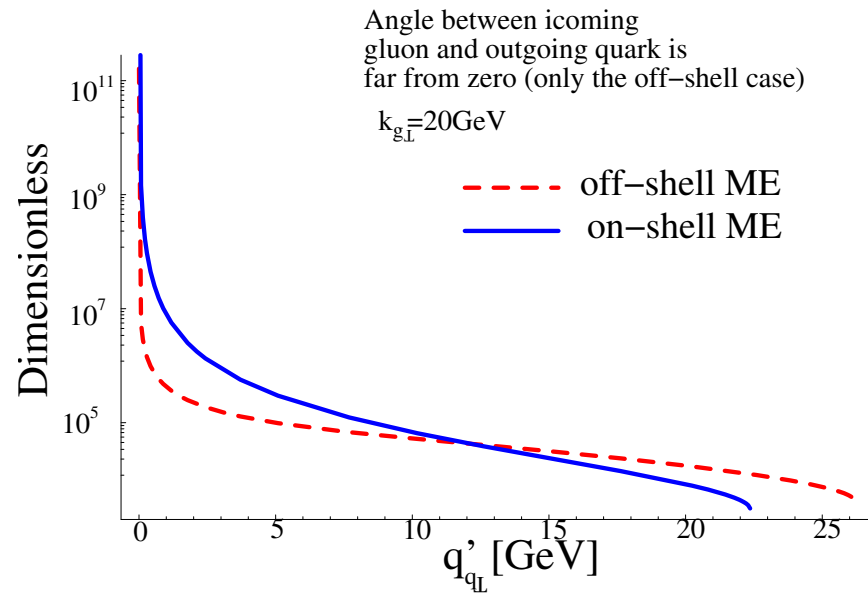
## Hard matrix element

After squaring amplitude we obtain:

$$|M|^2 = -(4\pi)^2 \alpha_s^2 \frac{x_g^2 s^2 (x_q^2 + x_{q'}^2)}{18 \hat{s} \hat{u} \hat{t}} \left( \frac{\hat{s}(8x_q + x_{q'}) - \hat{u}(8x_{q'} + x_q)}{x_q - x_{q'}} + k^2 \right)$$

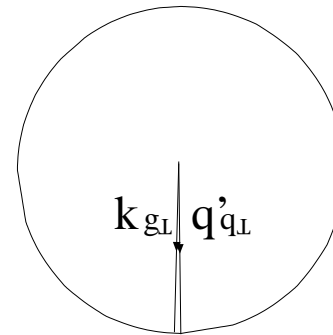
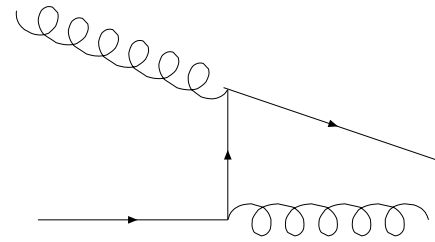
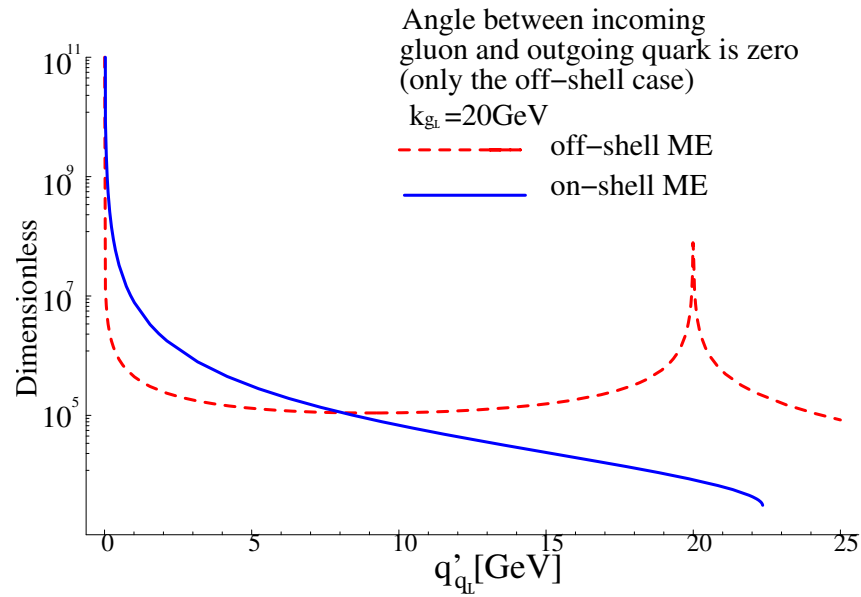
- In collinear limit  $k^2 \rightarrow 0$  one obtains QCD Compton
- Symmetry  $\hat{s} \rightarrow -\hat{u}$ ,  $x_{q'} \rightarrow x_q$
- This matrix element was calculated by M. Ciafaloni (Phys. Lett. B 429 (1998) 363-368) in different form and in different context

## Some properties of the off-shell ME



- off-shell ME allows for larger  $q'_{q,L}$

## Some properties of the off-shell ME



- at 0 angle there is a singularity at  $k'_q = k_g$



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## Cross-section for 2 jets

Cross-section for 2-jet production:

$$\sigma \sim f_g(x_g, k_T^2, \mu) \otimes |M|^2 \otimes f_q(x_q, k_{T2}^2, \mu)$$

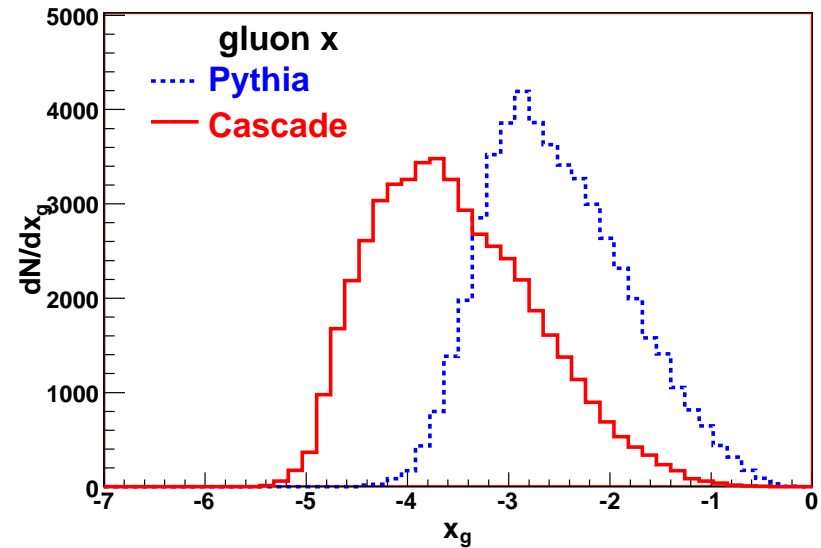
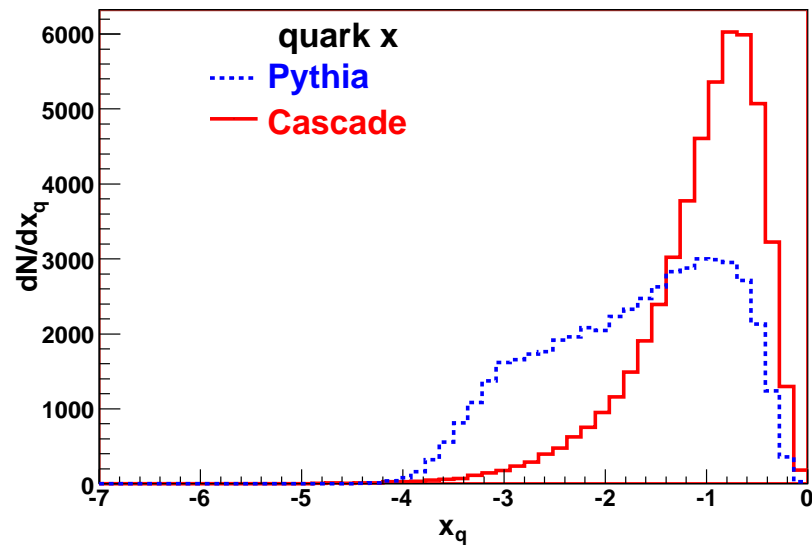
- $f_g(x_g, k_T^2, \mu)$  unintegrated gluon density ← CCFM
- $f_q(x_q, k_T^2, \mu)$  unintegrated valence quark density (needed for technical reasons) ← CCFM-like. Initial valence quark distribution is provided by CTEQ 6.1
- $\alpha_s \rightarrow \alpha_s(k_T^2)$
- cut on momenta of outgoing jets  $\rightarrow p_T > 10 \text{ GeV}$

The result for the total x-section is roughly:  $0.17 \text{ mb}$

For comparison total  $pp$  x-section at LHC energies is roughly  $80 \text{ mb}$

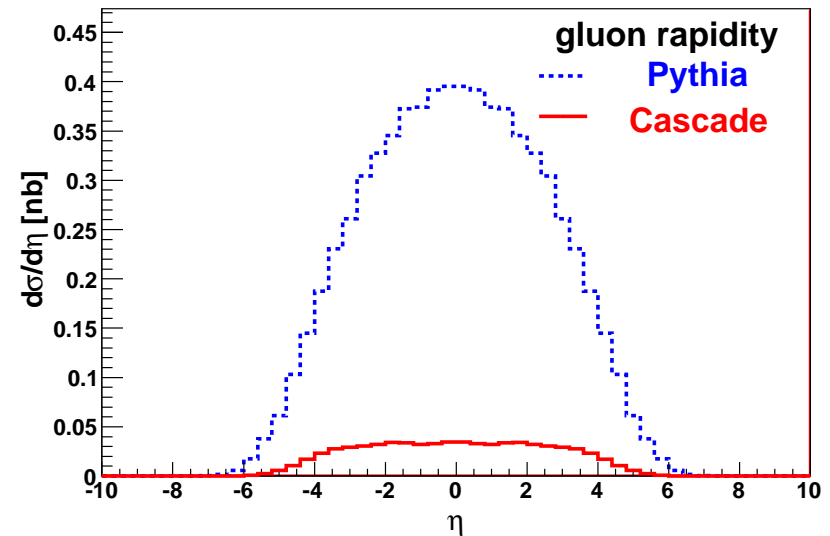
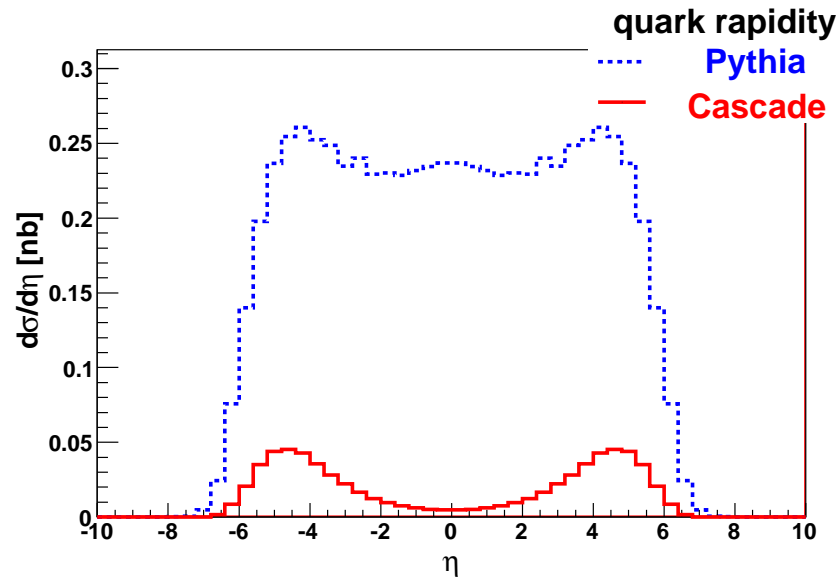
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## Results - x distribution before collision

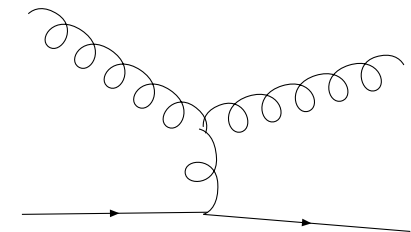


- difference in the distribution of gluon x because of  $k_T$  of gluon and quark
- difference in the distribution of quark x because of sea quarks

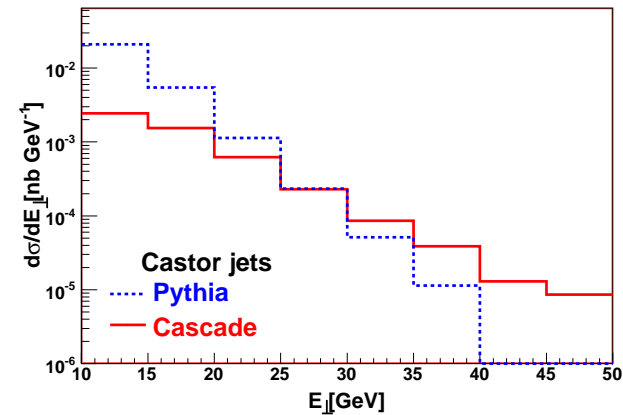
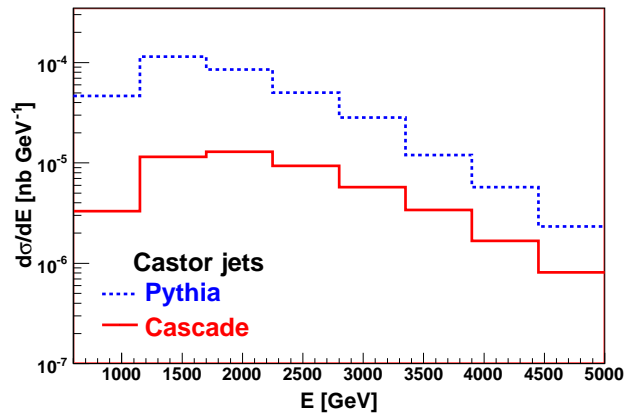
## Results - pseudo-rapidity distribution of produced jets



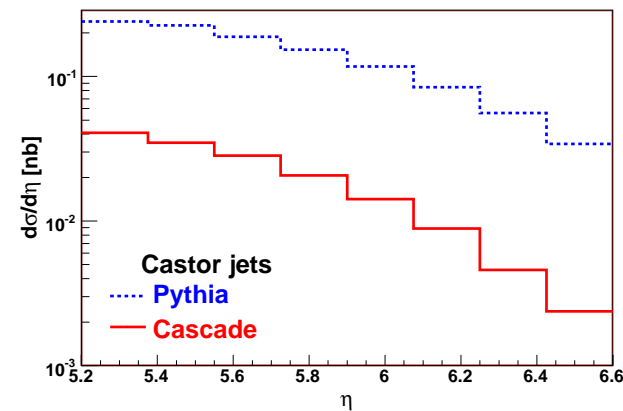
- valence quark ( $m_q = 0$ ) is slightly deflected
- produced jets are well separated in rapidity



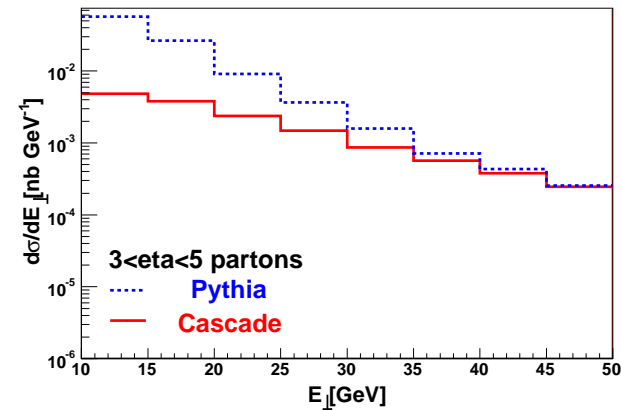
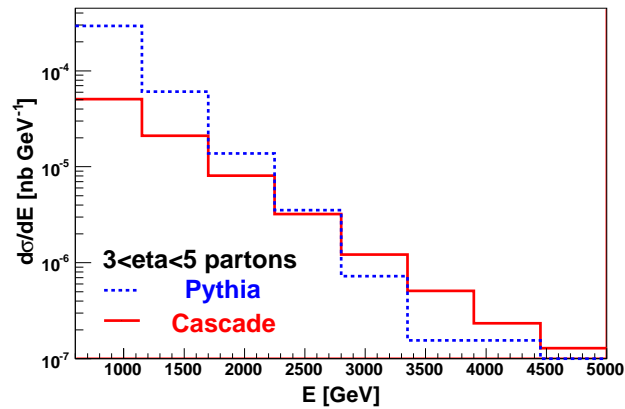
# Energy, transversal energy and $\eta$ of jets in Castor calorimeter



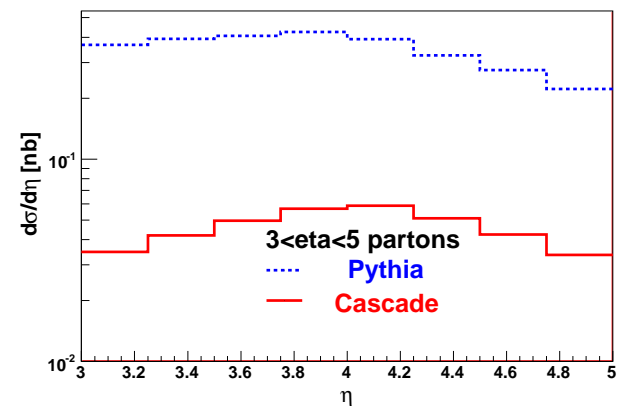
- Castor – pseudo-rapidity region  $5.2 < \eta < 6.6$



## Energy, transversal energy and $\eta$ of jets in $3 < \eta < 5$ region



- A detector in pseudo-rapidity region  $3 < \eta < 5$
- Difference could come from sea-quarks

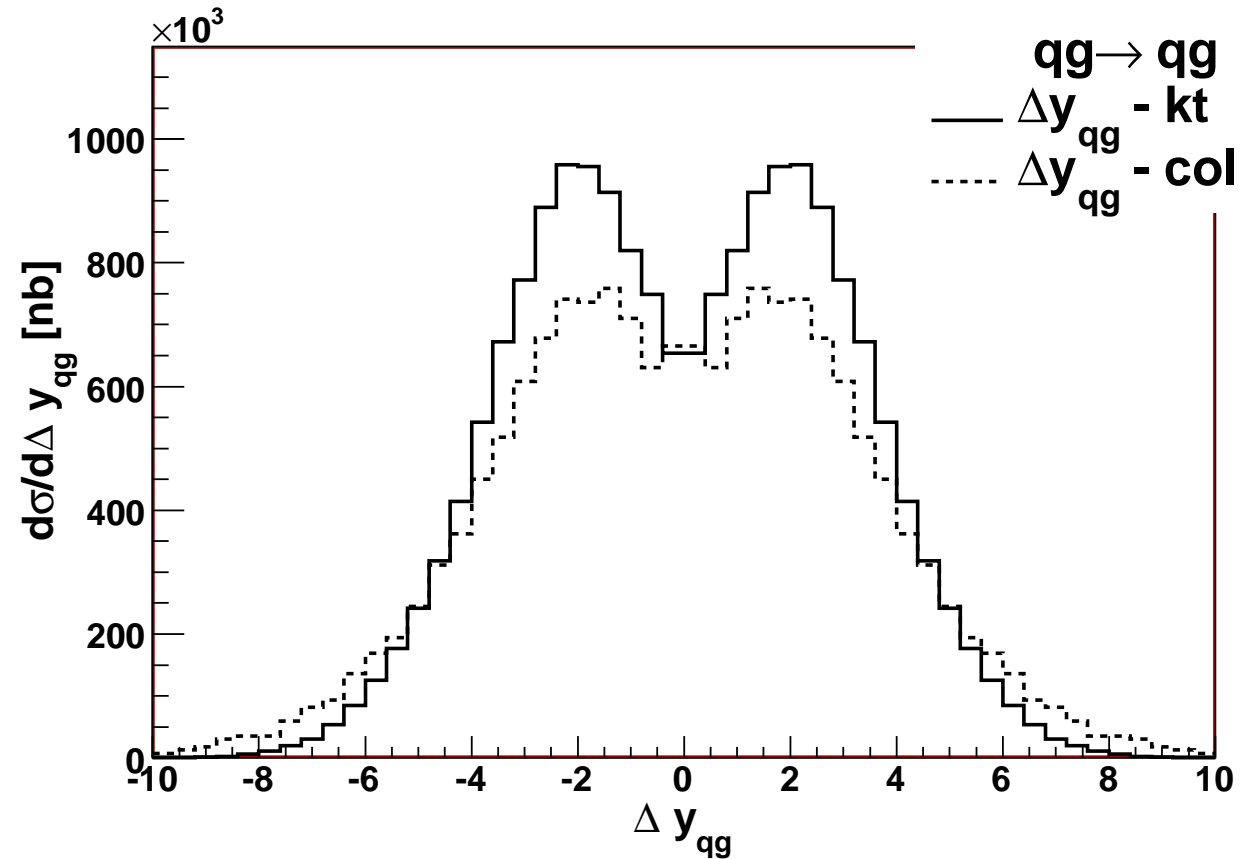


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## Conclusions and outlook

- We obtained matrix element in  $k_T$  factorisation which allow for studies of low  $x_g$  effects at the LHC
- CCFM-like equation for unintegrated quark distribution has been incorporated in Monte Carlo framework → CASCADE
- $p_T$  and rapidity spectra of produced jets have been calculated
  
- Next step: including parton showers
- Step towards including multiple interactions for MC generator in  $k_T$  factorisation framework
- Since gluon is probed at low momentum fraction we are going to include nonlinear evolution equation to parametrize unintegrated gluon distribution
- Inclusion of sea-quarks initiated process

## Back up slides



- Rapidity difference between produced jets