

# APFEL

A PDF Evolution Library with QED Corrections

**arXiv:1310.1394**

Valerio Bertone

CERN



**HERAFitter User's meeting**

16.10.2013

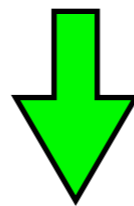
In collaboration with Stefano Carrazza and Juan Rojo

# SUMMARY

- 🍏 Motivations
- 🍏 Strategy
- 🍏 Validation and Benchmark
- 🍏 Conclusions and Outlook

# Motivations

- 🍏 Need for **precision physics** at the LHC:
  - 🍏 present PDF determination accuracy reaches NNLO in QCD.
- 🍏 At this level of accuracy **QED corrections** become relevant.
  - 🍏 Naive argument:  $\frac{\alpha_s^2(M_Z)}{\alpha(M_Z)} \sim 1.8$
  - 🍏 inclusion of QED corrections to **PDF evolution**,
  - 🍏 extraction of a **photon PDF** from data.
- 🍏 Need for an **accurate, flexible** and **public** code to perform PDF evolution that includes QED corrections.



**APFEL**

A PDF Evolution Library: **arXiv:1310.1394**

# Motivations

## *Main Features of APFEL 1.0.0*

### 🍏 Accuracy:

- 🍏 PDF evolution up to NNLO in QCD and LO in QED,
- 🍏 FFNS and VFNS,
- 🍏 Pole and  $\overline{\text{MS}}$  heavy quark masses.

### 🍏 Flexibility:

- 🍏 Fortran, C/C++ and Python interfaces,
- 🍏 interface to LHAPDF (input/output).

### 🍏 Publicly available from the HepForge webpage:

<http://apfel.hepforge.org/>

# Strategy

## *Solution of QCD and QED DGLAP Equations*

- 🍏 APFEL adopts a **decoupled** approach:

*Different scales*

$$\mu^2 \frac{\partial}{\partial \mu^2} \mathbf{q}(x, \mu, \nu) = \mathbf{P}^{\text{QCD}}(x, \alpha_s(\mu)) \otimes \mathbf{q}(x, \mu, \nu),$$
$$\nu^2 \frac{\partial}{\partial \nu^2} \mathbf{q}(x, \mu, \nu) = \mathbf{P}^{\text{QED}}(x, \alpha(\nu)) \otimes \mathbf{q}(x, \mu, \nu),$$

- 🍏 whose **independent** solutions are:

$$\mathbf{q}(x, \mu_1, \nu) = \mathbf{\Gamma}^{\text{QCD}}(x|\mu_1, \mu_0) \otimes \mathbf{q}(x, \mu_0, \nu),$$

$$\mathbf{q}(x, \mu, \nu_1) = \mathbf{\Gamma}^{\text{QED}}(x|\nu_1, \nu_0) \otimes \mathbf{q}(x, \mu, \nu_0).$$

- 🍏 Combination of  $\mathbf{\Gamma}^{\text{QCD}}$  and  $\mathbf{\Gamma}^{\text{QED}}$  to obtain the QCD+QED **combined evolution...** but how?

# Strategy

## *Combining QCD and QED Evolutions*

- 🍏 QCD and QED evolutions **do not commute**:

$$[\Gamma^{\text{QCD}}, \Gamma^{\text{QED}}] \neq 0$$

- 🍏 In practice, QCD followed by QED or QED followed by QCD evolution lead to different results.

# Strategy

## *Combining QCD and QED Evolutions*

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$$[\Gamma^{\text{QCD}}, \Gamma^{\text{QED}}] \neq 0$$

- 🍏 In practice, QCD followed by QED or QED followed by QCD evolution lead to different results.

*Is there anything wrong?*

# Strategy

## *Combining QCD and QED Evolutions*

- 🍏 Solving the DGLAP QCD+QED evolution equations in Mellin space and expanding the solution, one finds:

$$[\Gamma^{\text{QCD}}, \Gamma^{\text{QED}}] = \mathcal{O}(\alpha\alpha_s)$$



# Strategy

## Combining QCD and QED Evolutions

- 🍏 Solving the DGLAP QCD+QED evolution equations in Mellin space and expanding the solution, one finds:

$$[\Gamma^{\text{QCD}}, \Gamma^{\text{QED}}] = \mathcal{O}(\alpha\alpha_s)$$

- 🍏 Two **equivalent** possibilities:

1)  $\Gamma^{\text{QCED}}(\mu, \mu_0; \nu, \nu_0) \equiv \Gamma^{\text{QED}}(\nu, \nu_0) \otimes \Gamma^{\text{QCD}}(\mu, \mu_0)$

2)  $\Gamma^{\text{QECD}}(\mu, \mu_0; \nu, \nu_0) \equiv \Gamma^{\text{QCD}}(\mu, \mu_0) \otimes \Gamma^{\text{QED}}(\nu, \nu_0)$

*Subleading*

- 🍏 whose perturbative expansions are:

$$\Gamma^{\text{QCED}} = 1 + \alpha A + \alpha_s B + \alpha\alpha_s C + \dots$$

$$\Gamma^{\text{QECD}} = 1 + \alpha A + \alpha_s B - \alpha\alpha_s C + \dots$$

- 🍏 This suggests the **averaged** solution:

3)  $\Gamma^{\text{QavD}} \equiv \frac{\Gamma^{\text{QCED}} + \Gamma^{\text{QECD}}}{2}$

# Strategy

## *Advantages of the APFEL Approach*

- 🍏 Possibility to treat QCD and QED **separately**:
  - 🍏 optimized PDF evolution basis for each sector (not a common one),
  - 🍏 better numerical efficiency.
- 🍏 Possibility to explore different solutions differing by subleading terms (**QCED, QECD, QavD**):
  - 🍏 estimate of the **theoretical error** due to the missing higher-order terms,
  - 🍏 benchmark of the internal FastKernel code used by the NNPDF collaboration to obtain the NNPDF2.3 QED PDF sets [[arXiv:1005.0397](#)] which uses QECD.

# Validation and Benchmark

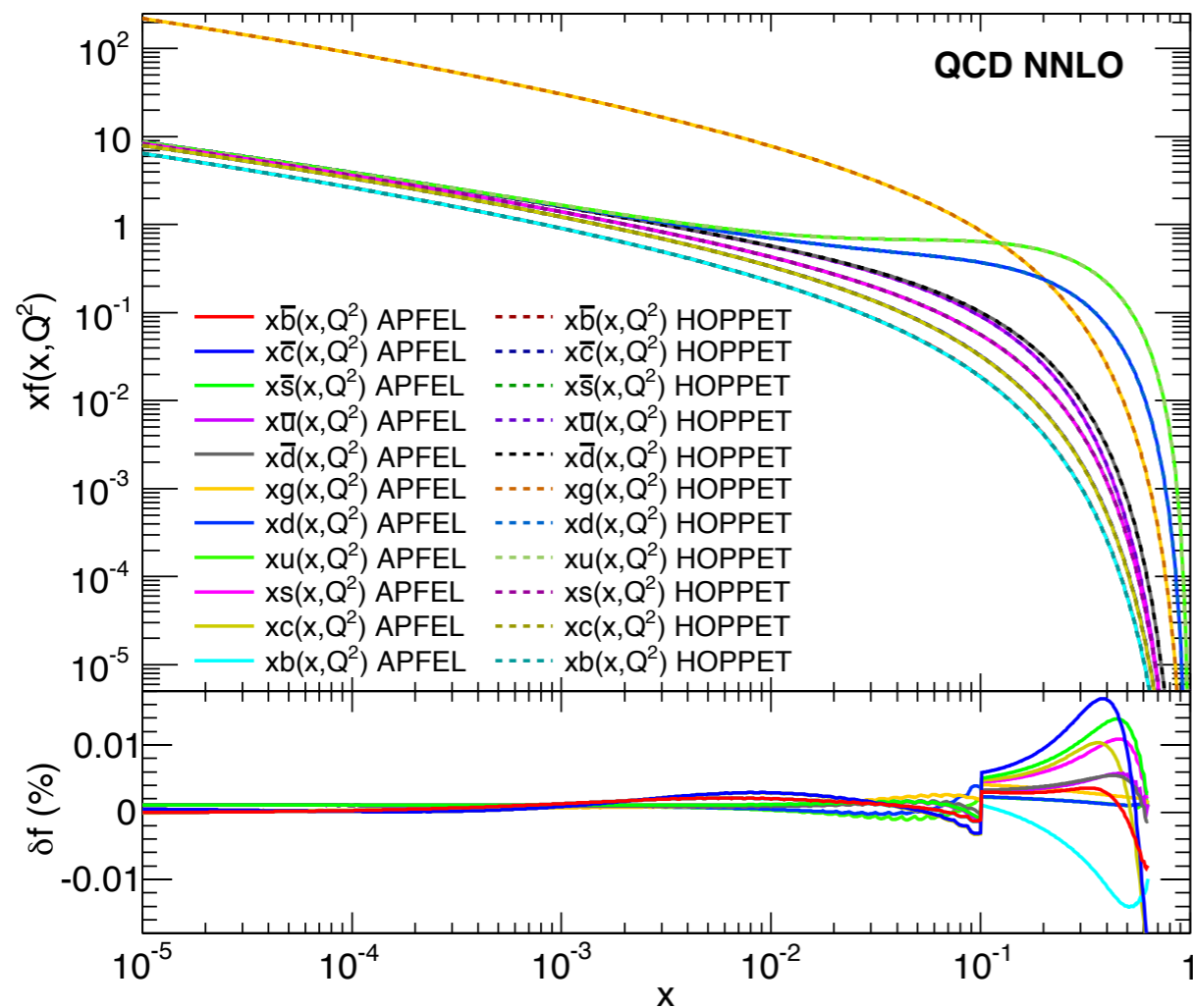
*APFEL vs. HOPPET* G. Salam and J. Rojo [arXiv:1005.0397]

🍏 Benchmark of the **pure QCD** evolution at NNLO in the **VFNS**:

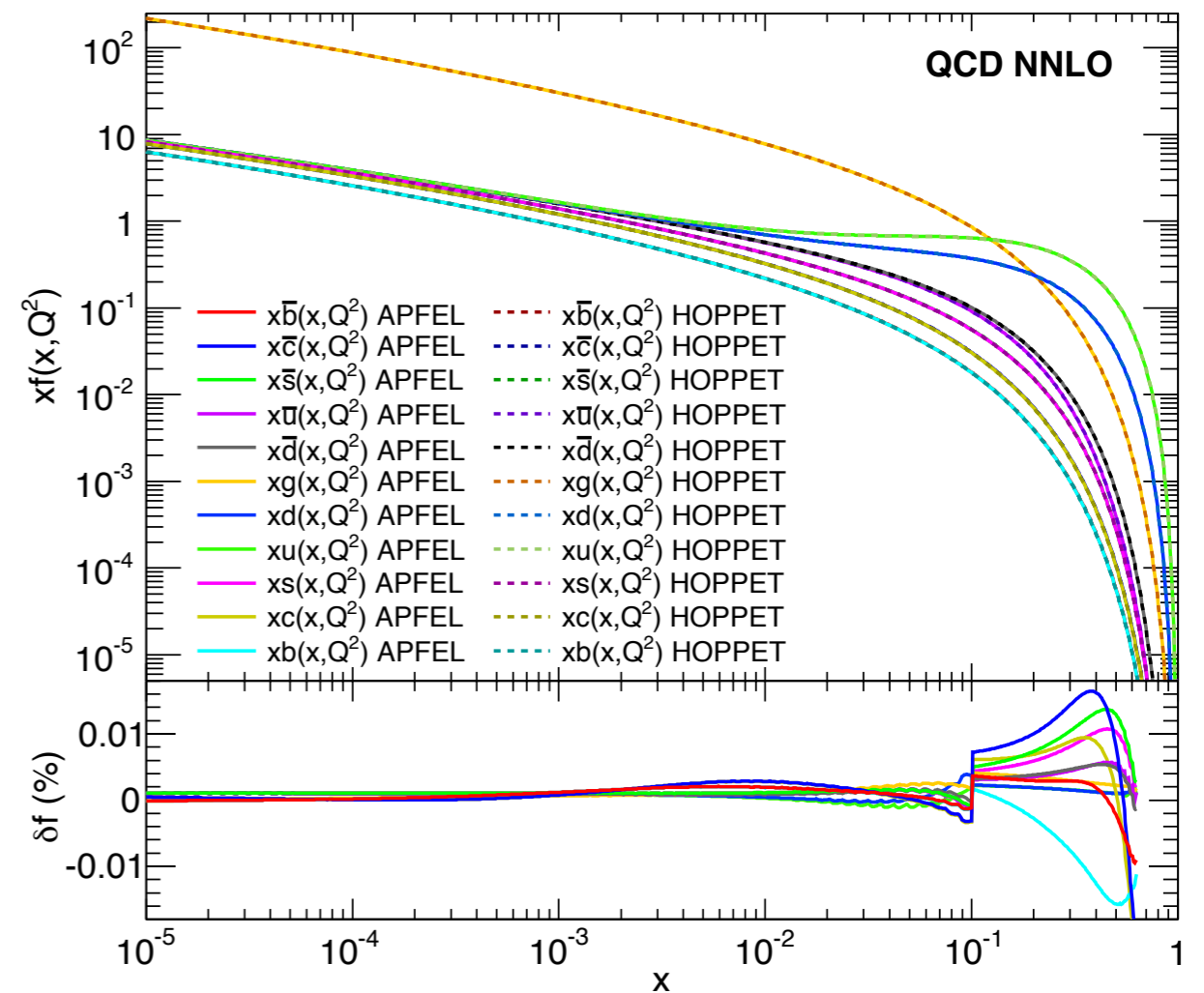
**Pole masses**

**$\overline{\text{MS}}$  masses**

APFEL vs HOPPET evolution pole mass at  $Q^2 = 10^4 \text{ GeV}^2$



APFEL vs HOPPET evolution  $\overline{\text{MS}}$  at  $Q^2 = 10^4 \text{ GeV}^2$



**Excellent agreement!**

# Validation and Benchmark

## *APFEL vs. partonevolution*

**partonevolution** (M. Roth and S. Weinzierl [hep-ph/0403200]) was the only public code implementing QED corrections in the PDF evolution.

Limitations of **partonevolution**:

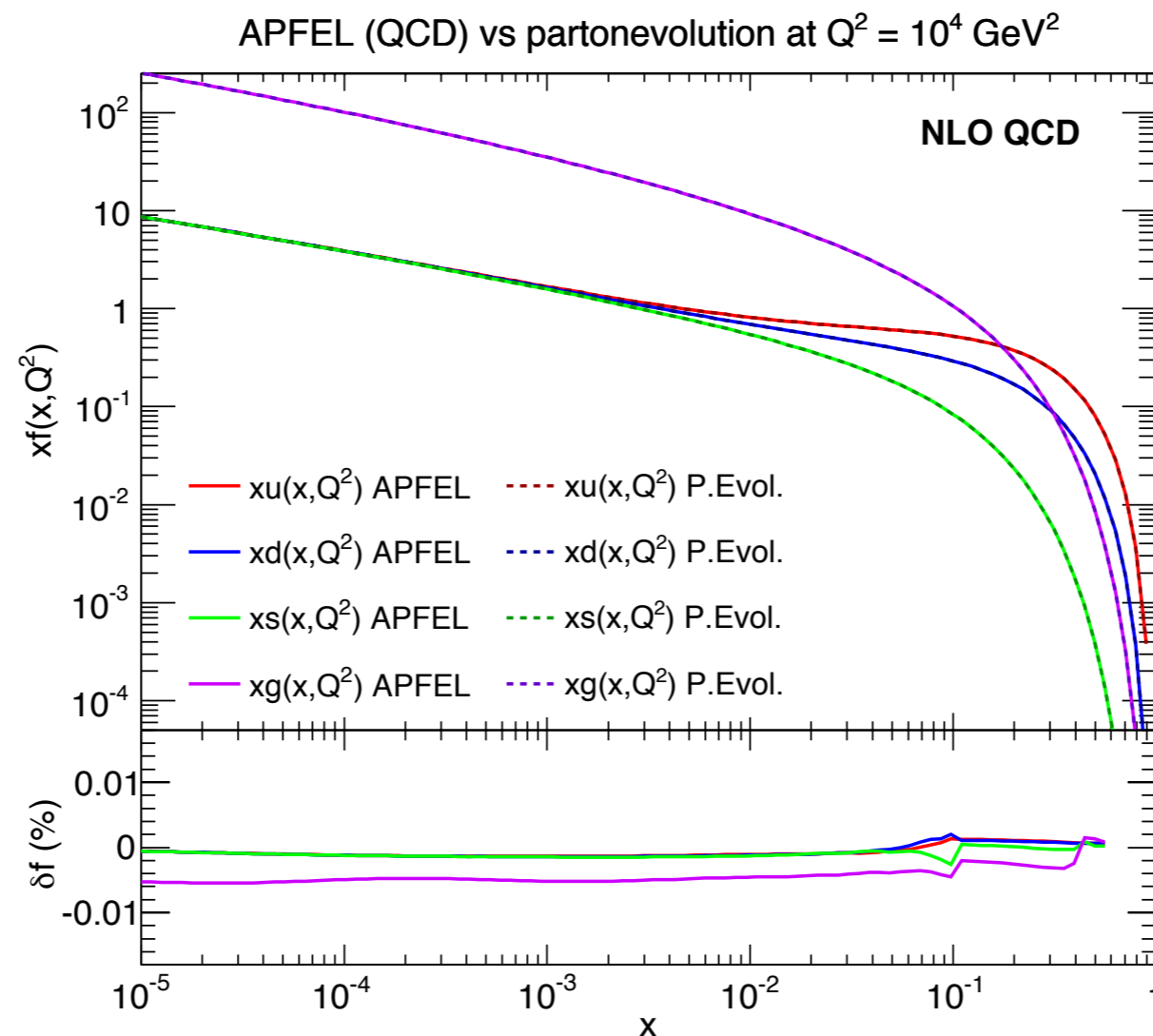
- 🍏 up to NLO in QCD,
- 🍏 only FFNS,
- 🍏 no possibility to interface it to an arbitrary PDF set ( $\mathcal{N}$ -space approach),
- 🍏 slow and unpractical to use.

# Validation and Benchmark

## *APFEL vs. partonevolution*

🍏 Check of the **pure QCD** evolution at NLO in the **FFNS**:

🍏 to disentangle the QED effects.



**Very good agreement!**

# Validation and Benchmark

## *APFEL vs. partonevolution*

🍏 Test of the **QCD+QED evolution** in the **FFNS**:

🍏 APFEL provides **three different options** for the QCD+QED evolution:

### QCED

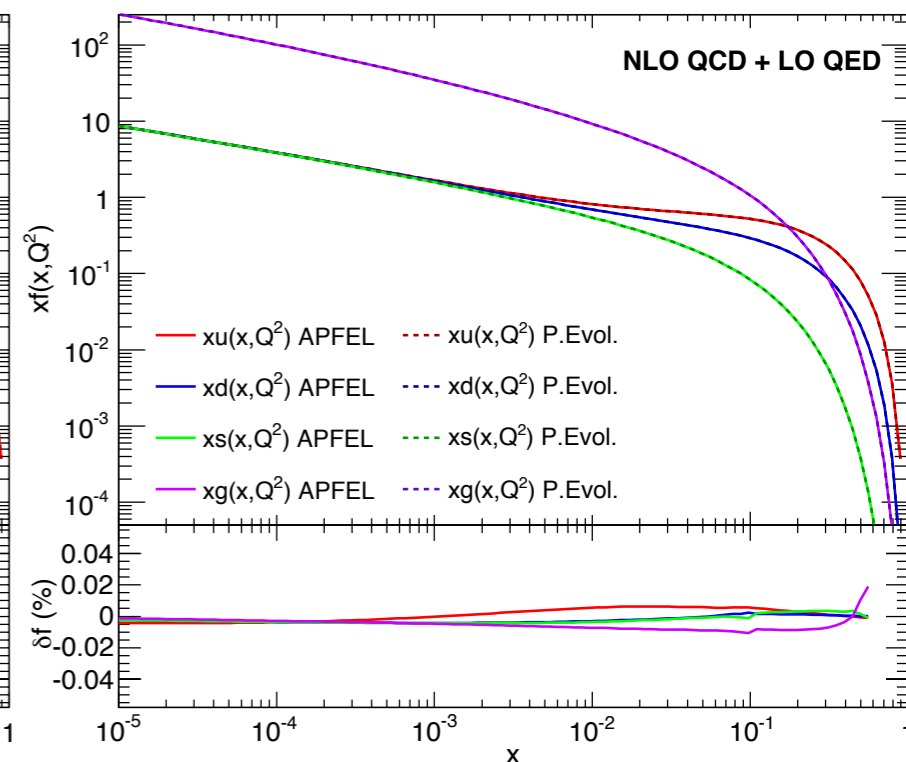
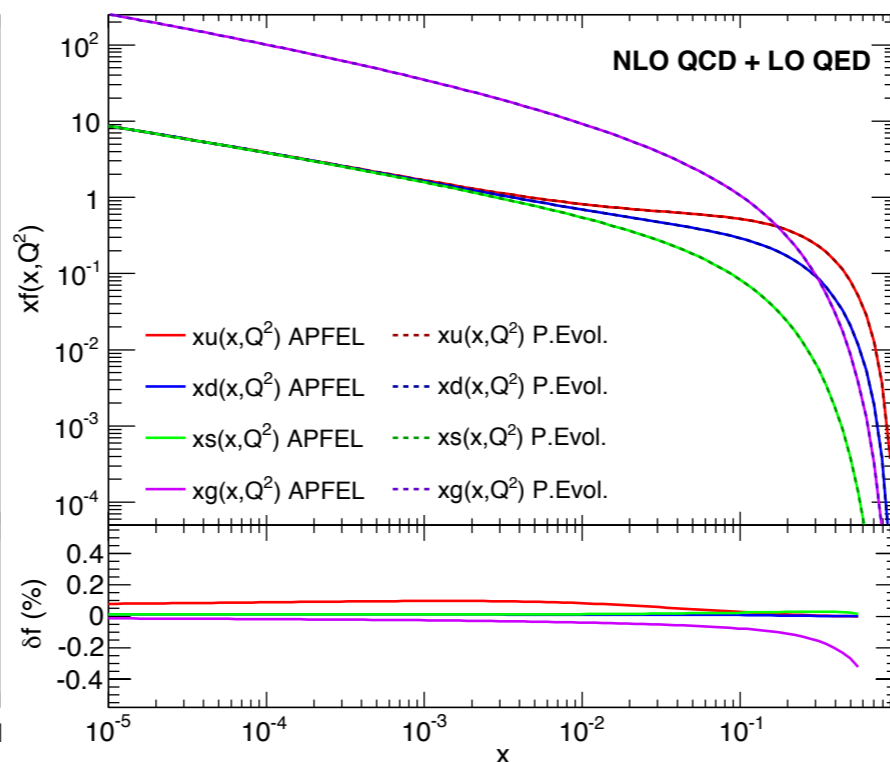
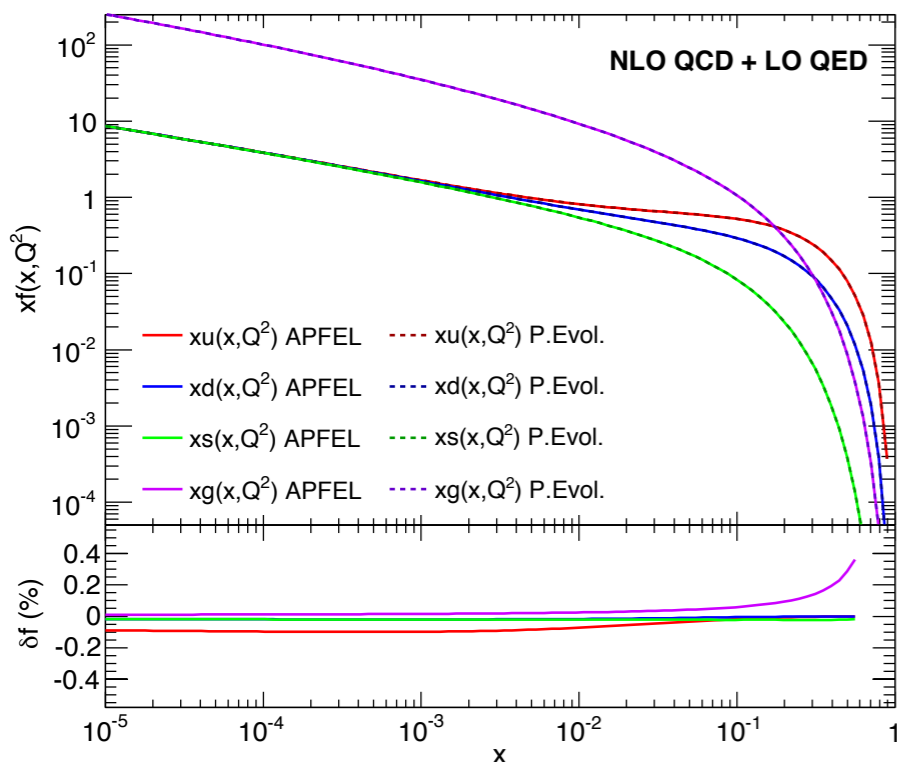
### QECD

### QavD

APFEL (QCED) vs partonevolution at  $Q^2 = 10^4 \text{ GeV}^2$

APFEL (QECD) vs partonevolution at  $Q^2 = 10^4 \text{ GeV}^2$

APFEL (QavD) vs partonevolution at  $Q^2 = 10^4 \text{ GeV}^2$



🍏 **Quarks and gluon** are in good agreement for all the three options, though the **QavD** solutions ensures an even **better** agreement.

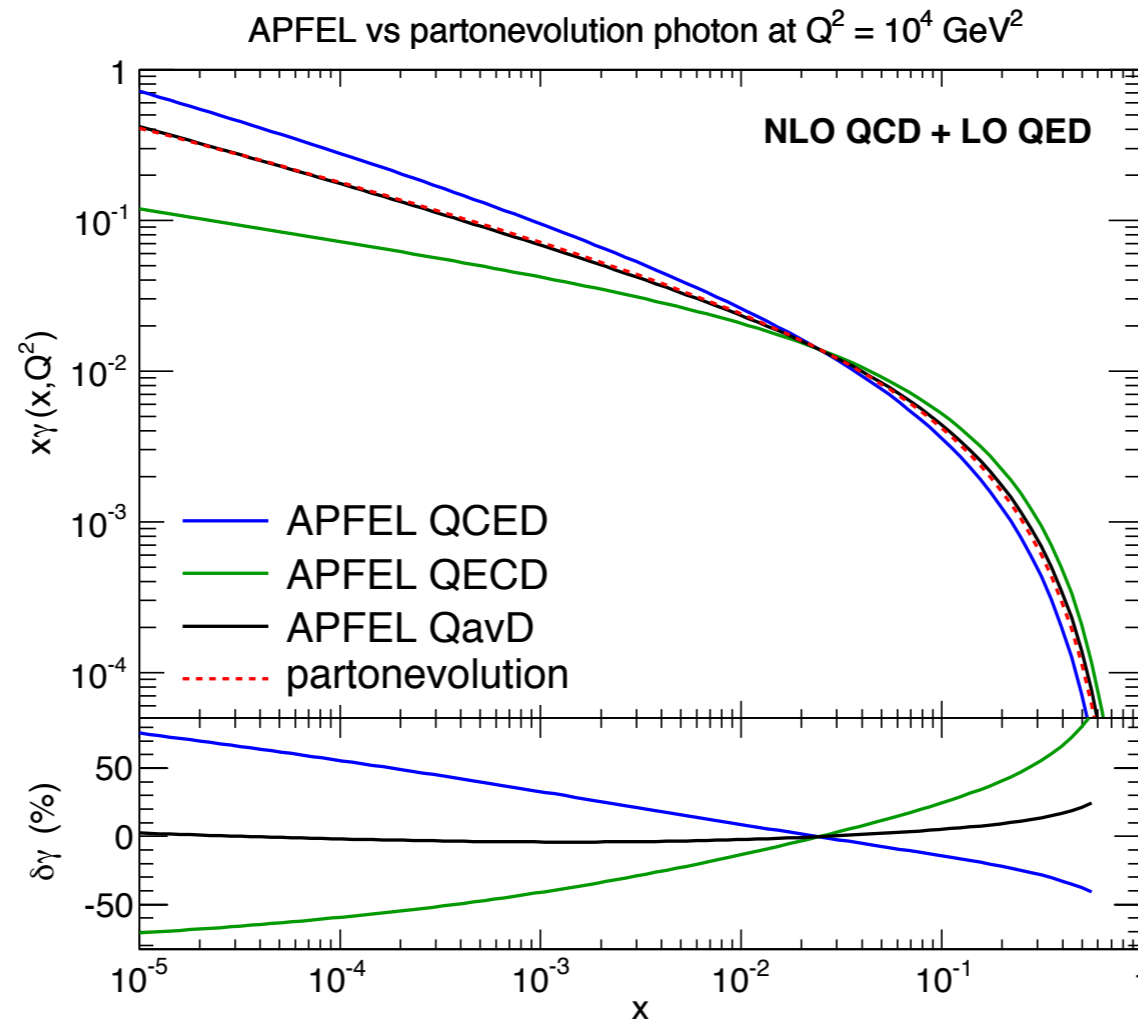
# APFEL



# Validation and Benchmark

## *APFEL vs. partonevolution*

🍏 Test of the **QCD+QED evolution** in the **FFNS**:



**Photon PDF** more sensitive to **higher-order corrections**:

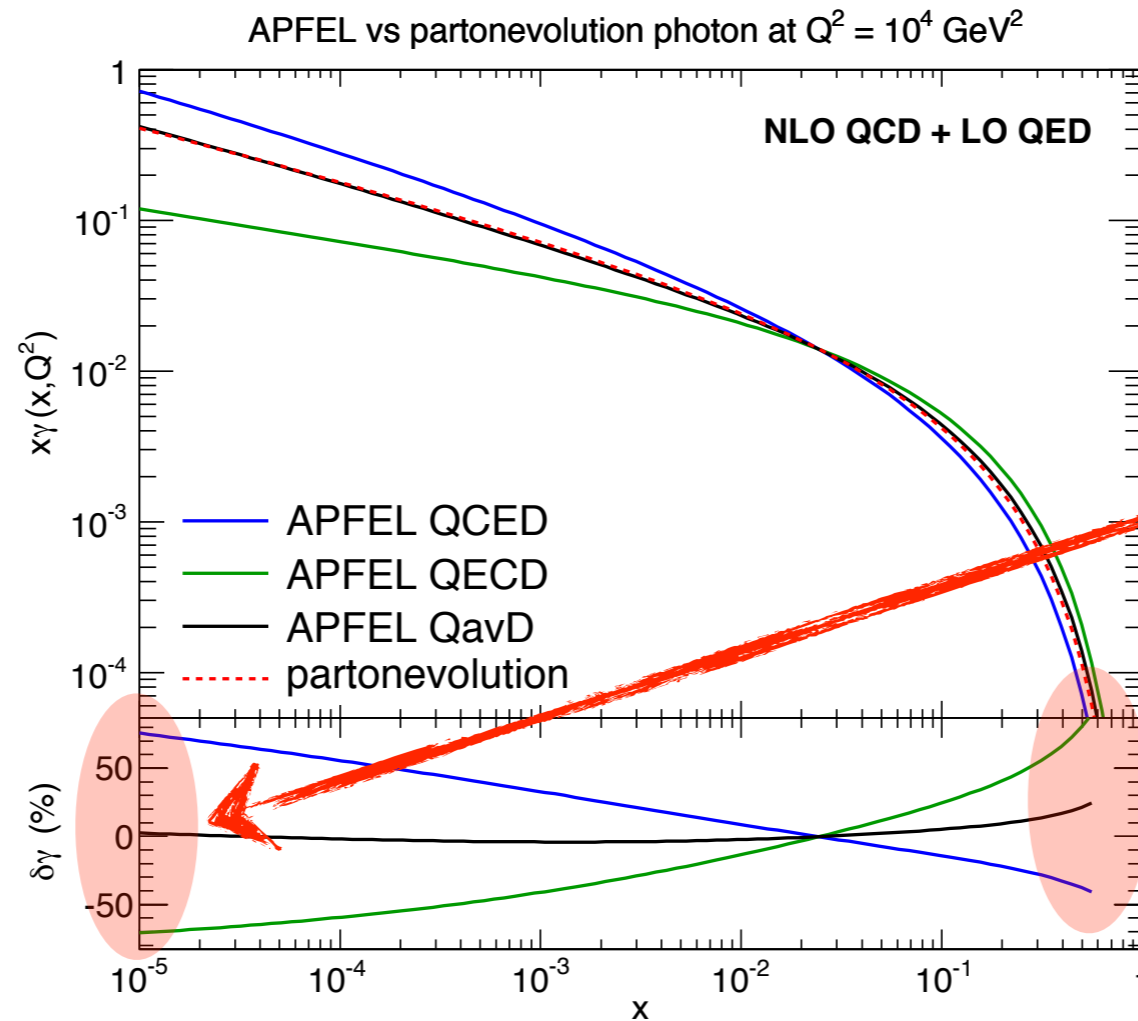
- 🍏 discrepancy between PE and APFEL(QCED/QECD) up to 60%,
- 🍏 PE and APFEL(QavD) in good agreement at a few percent level.

**APFEL**

# Validation and Benchmark

## *APFEL vs. partonevolution*

🍏 Test of the **QCD+QED evolution** in the **FFNS**:



*Subleading terms can be very large!*

**Photon PDF more sensitive to higher-order corrections:**

- 🍏 discrepancy between PE and APFEL(QCED/QECD) up to 60%,
- 🍏 PE and APFEL(QavD) in good agreement at a few percent level.

**APFEL**

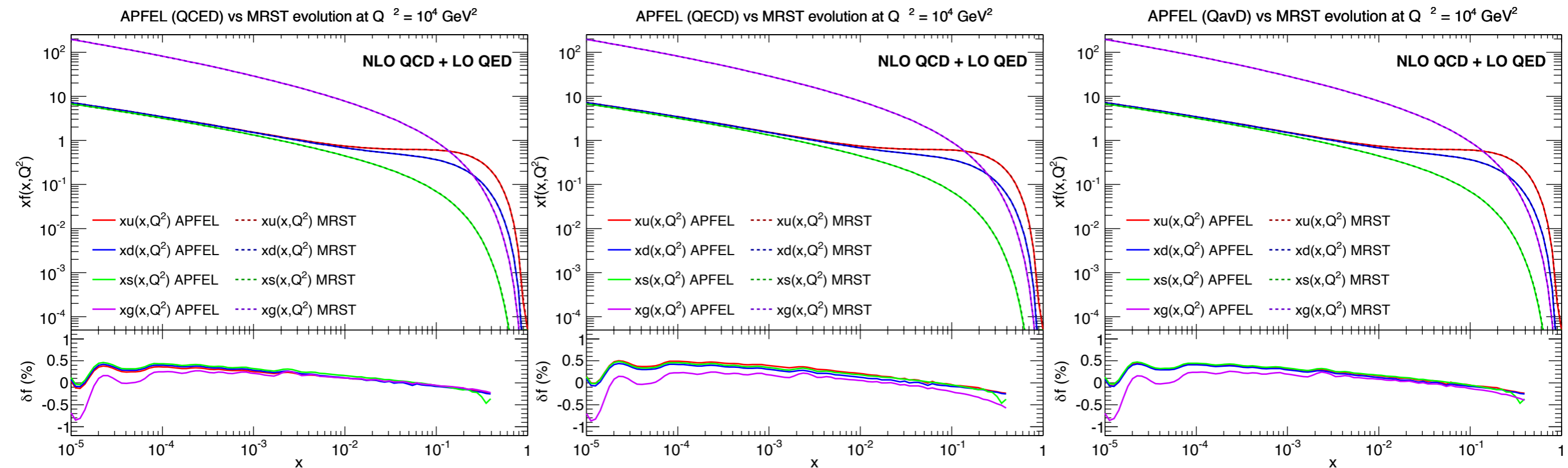


# Validation and Benchmark

## *APFEL vs. MRST2004QED*

A.D. Martin et al. [hep-ph/0411040]

🍏 Test of the **QCD+QED evolution** in the **VFNS**:



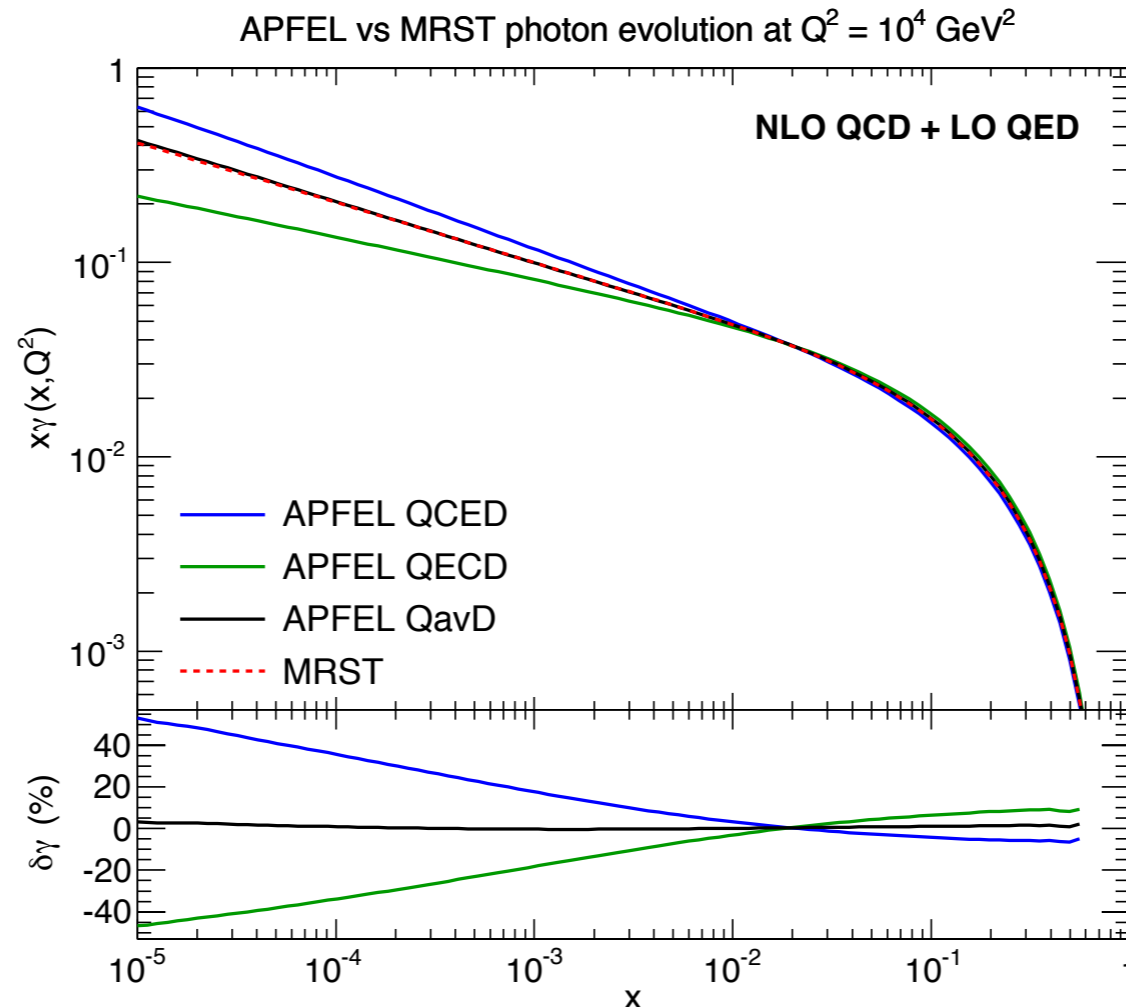
🍏 Same picture as for partonevolution:

🍏 Quark and gluon PDFs in good agreement

# Validation and Benchmark

## *APFEL vs. MRST2004QED*

🍏 Test of the **QCD+QED evolution** in the **VFNS**:



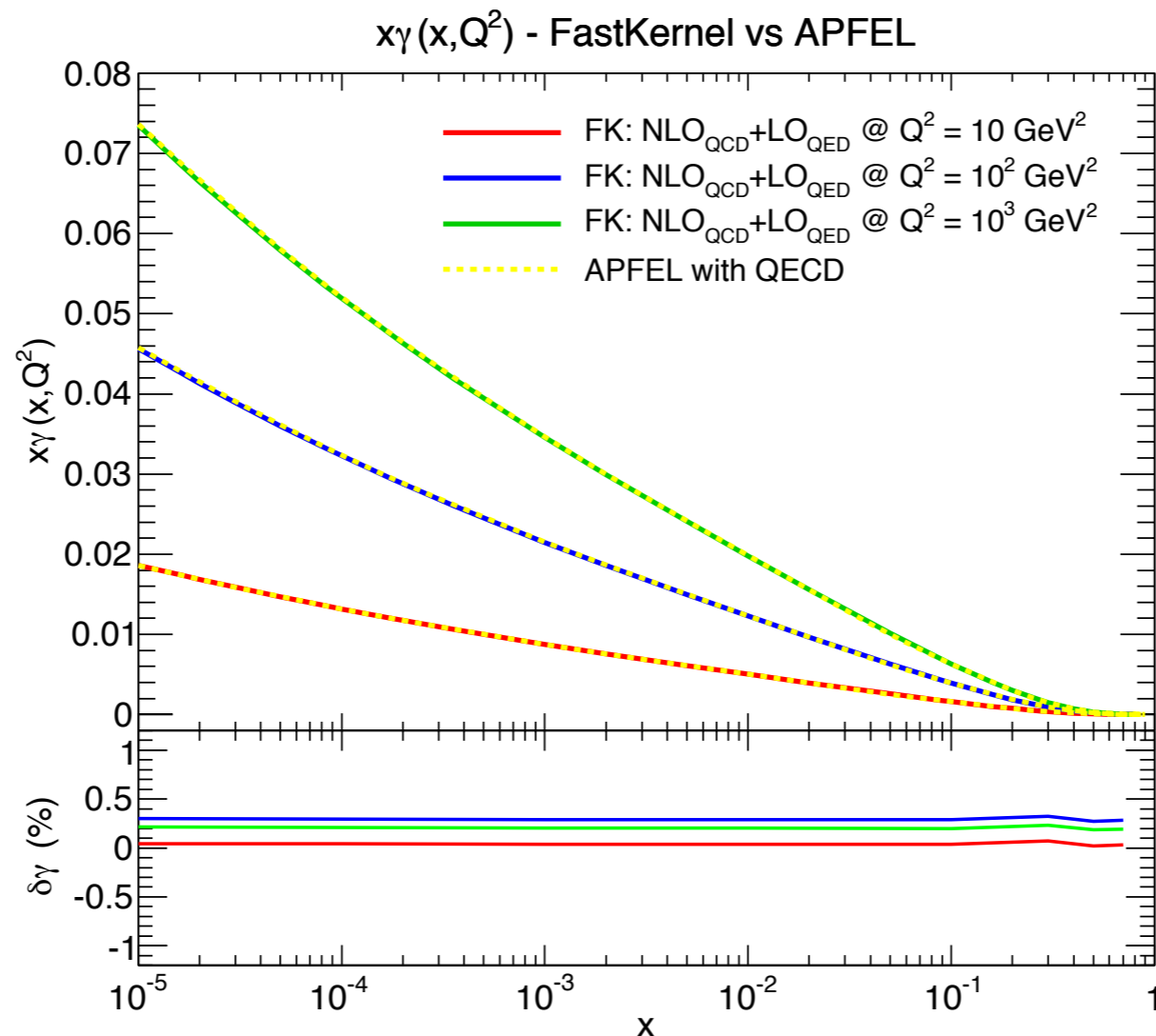
🍏 Same picture as for partonevolution:

- 🍏 Quark and gluon PDFs in good agreement
- 🍏 larger spread for the photon but good agreement for QavD

# Validation and Benchmark

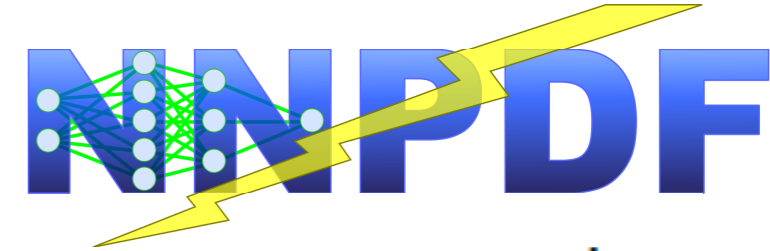
## *APFEL vs. FastKernel (NNPDF)*

- 🍏 APFEL has been employed to validate the **FastKernel** code used to produce the **NNPDF2.3 QED** sets:
  - 🍏 whose evolution is equivalent to the **QECD solution**.

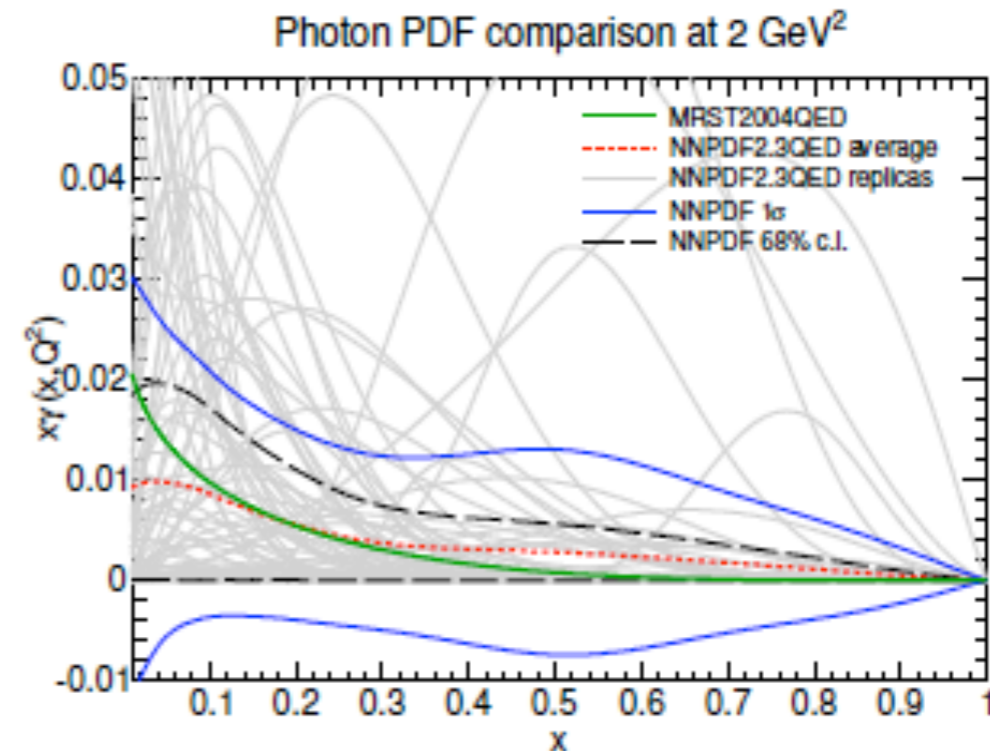
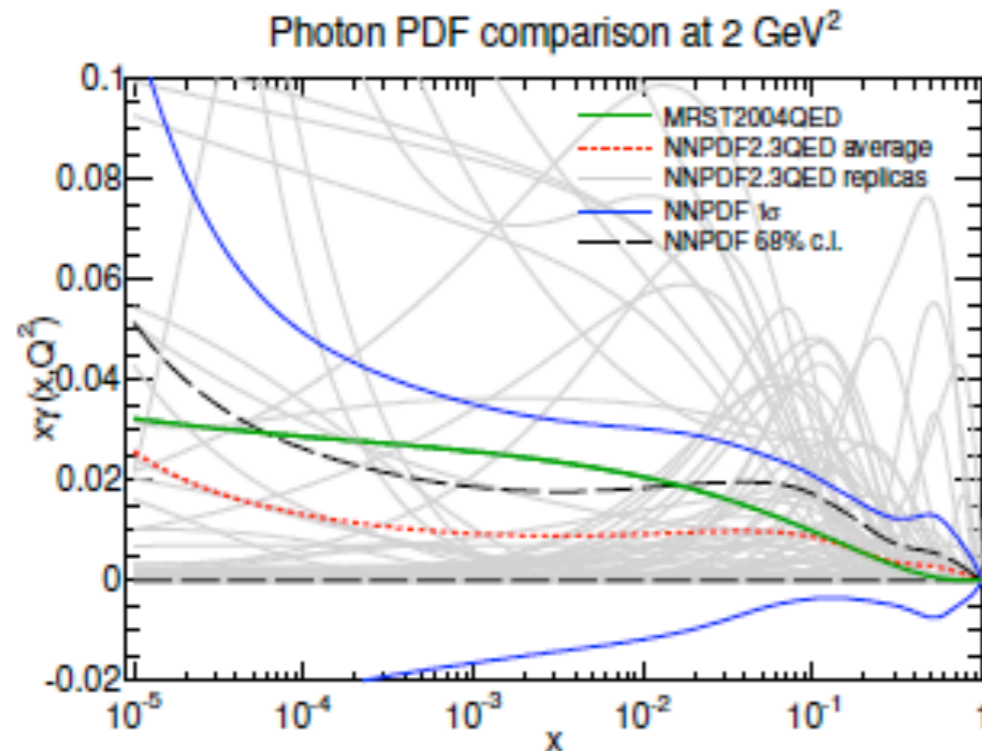


# APFEL and NNPDF

## Motivation



- APFEL and NNPDF:
  - ▶ independent cross-check implementation of the FastKernel code
- QED evolution in new NNPDF2.3QED set:



- Photon PDF extracted from DIS data and LHC data.
  - ▶ LO in QED and up to NNLO in QCD ( $\alpha_s = 0.117, 0.118, 0.119$ )
  - ▶ public PDF sets available from LHAPDF  $\geq 5.9.0$ .



# Conclusions and Outlook

- 🍏 APFEL is a public library for QCD+QED combined evolution:
  - 🍏 up to NNLO in QCD and LO in QED,
  - 🍏 FFNS and VFNS implemented,
  - 🍏 Pole and  $\overline{\text{MS}}$  heavy quark masses.
- 🍏 Modern approach for PDF manipulation:
  - 🍏 interface to LHAPDF.
- 🍏 Good agreement with the existing public codes.

## Outlook:

- 🍏 time-like evolution (fragmentation functions),
- 🍏 DIS factorization scheme,
- 🍏 polarized evolution...

**APFEL** is available on: <http://apfel.hepforge.org/>

*User support service included!  
Contact us for any question.*