

PIDRIX: PARTICLE IDENTIFICATION MATRIX FACTORIZATION

Evan Sangaline

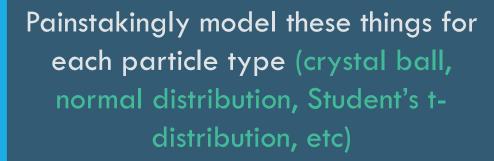
UC Davis

WWND 2014

TRADITIONAL PARTICLE IDENTIFICATION

Measure things that carry information about particle identity $(dE/dx, 1/\beta,$ invariant mass, Čerenkov radiation, calorimeter energy, etc)

Minimize the log-likelihood to determine our best estimates of shapes and yields



This step is really hard and error prone.

Can we just skip it?

PIDRIX

Measure things that carry information about particle identity $(dE/dx, 1/\beta,$ invariant mass, Čerenkov radiation, calorimeter energy, etc)



Minimize the log-likelihood to determine our best estimates of shapes and yields

Yes!

THE ASSUMPTIONS

- *We have a number of different particles that we measure
 - $\bullet \pi$, K, p, e, etc but could also be "background"
- For a given particle type each dimension of measurement is uncorrelated
- *e.g. ToF measurement error is not correlated with dE/dx measurement error
- *Bin on momentum and pseudorapidity to remove physics correlations
- Our particle yields follow Poisson statistics
 - No yields less than zero

TOWARDS SOMETHING MORE MATHEMATICAL

This means that we expect the observed density to be of the form

$$A_{total}(x,y) = \sum_{i=1}^{r} v_i(x) * u_i(y)$$
 where $v_i(x)$ and $u_i(y)$ are positive-definite and real

Get your bearings:

x, y are the measurement variables (dE/dx and 1/ β for instance)

 $A_{total}(x, y)$ is like a fit function

 $v_i(x) * u_i(y)$ is like the contribution to the fit function for the ith particle

r is the number of distinct particle types

FURTHER...

We use histograms so let's discretize things

$$A_{total}(x,y) = \sum_{i=1}^{r} v_i(x) * u_i(y)$$
 becomes $A_{m_x n} = U_{m_x r} V_{r_x n}$

$$A_{m_{x}n} = U_{m_{x}r}V_{r_{x}n}$$

Now say our observation histogram is T, then maximizing the log-likelihood is equivalent to minimizing the generalized Kullback-Leibler divergence:

$$D_{GKL}(T||A) = \sum_{i,j} T_{ij} ln \frac{T_{ij}}{A_{ij}} - T_{ij} + A_{ij}$$

NOW WHAT?

Traditional Fitting

Restrict the space of possible U and V matrices according to our models before minimizing.

e.g. "The columns of U must be Gaussians and the rows of V must be Student's t-distributions."

Pidrix

Don't model anything. Just minimize the KL divergence.

i.e. Skip the hard part.

MINIMIZING THE KULLBACK-LEIBLER DIVERGENCE

These update rules can quickly be seen to be stable when T=A.

$$U_{ip} \leftarrow U_{ip} \frac{\sum_{\alpha} V_{p\alpha} T_{i\alpha} / A_{i\alpha}}{\sum_{\alpha} V_{p\alpha}}$$

Also, if U and V start out positive definite and real then they will also remain so (our non-negative yield constraint).

$$V_{pj} \leftarrow V_{pj} \frac{\sum_{\alpha} U_{\alpha p} T_{\alpha j} / A_{\alpha j}}{\sum_{\alpha} U_{\alpha p}}$$

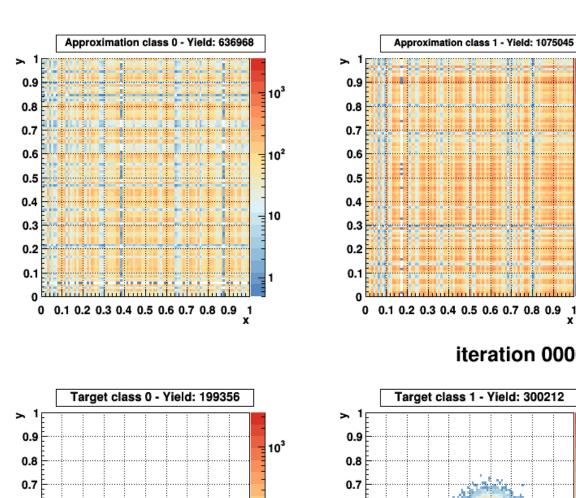
HOW DO THEY WORK?

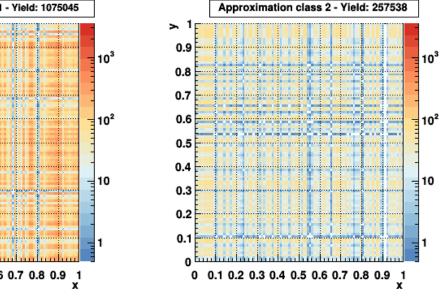
$$U_{ip} \leftarrow U_{ip} \frac{\sum_{\alpha} V_{p\alpha} T_{i\alpha} / A_{i\alpha}}{\sum_{\alpha} V_{p\alpha}}$$

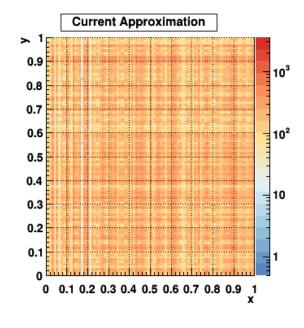
- \bullet First: think of T/A (element-wise) like a residual
 - If an entry is less than one then we are underestimating that bin with our approximation, greater than one and we're overestimating
- \bullet For a given particle p (proton) we look at a specific i (dE/dx)
- Then we take our current normalized ToF distribution (the pth column of V) corresponding to protons and dot that with the row of T/A that corresponds to our current i value (dE/dx value)
- If this particle's ToF distribution has lots of yield where we are underestimating (overestimating) T then we'll increase (decrease) the dE/dx distribution for this particle at our current i

UP TO SPEED?

- *"Yes."
 - ❖Great!
- *"You lost me on the last two slides"
- Don't worry about getting the details right now. Just think of it as a gradient descent like method for minimizing the negative log-likelihood.
- *"What's a Pidrix? Can you just show us some cool animations?"
- *Yes, thanks for asking! No more math... pretty picture time.

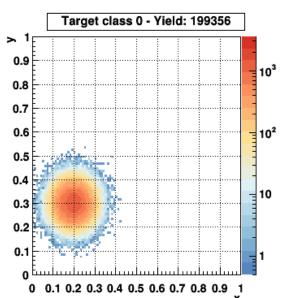


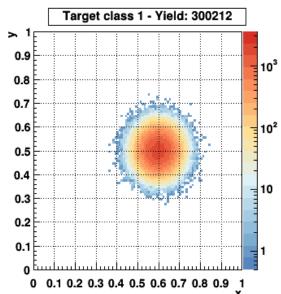


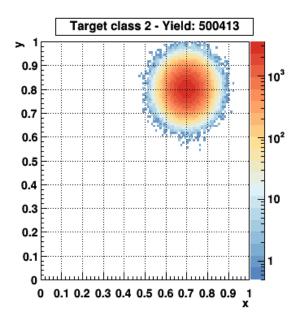


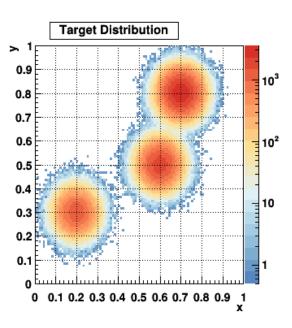
iteration 000000

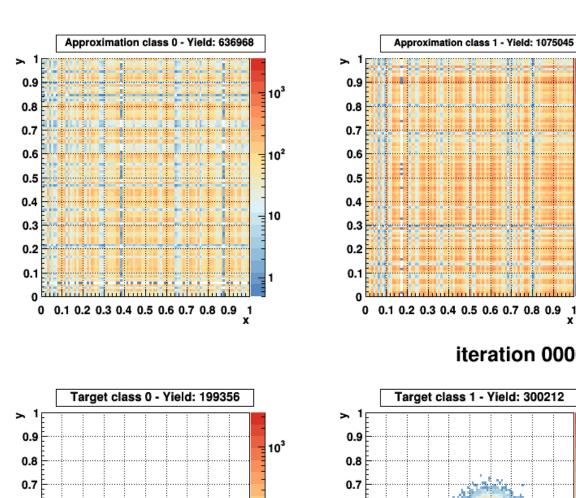
 $\chi^2/NDF = 9488.33$

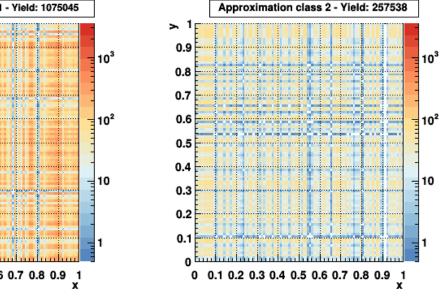


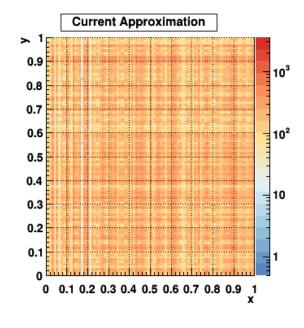






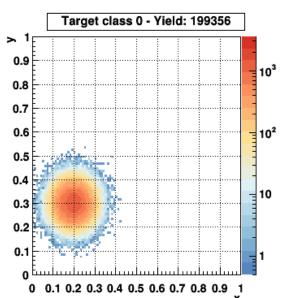


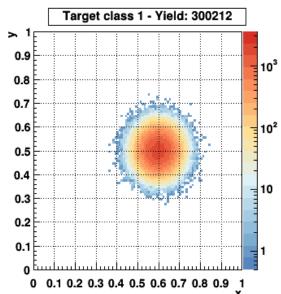


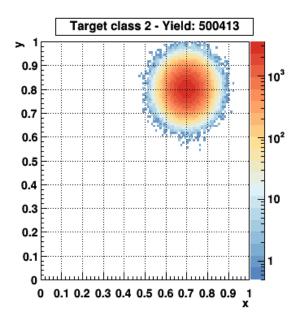


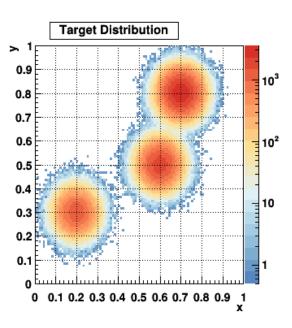
iteration 000000

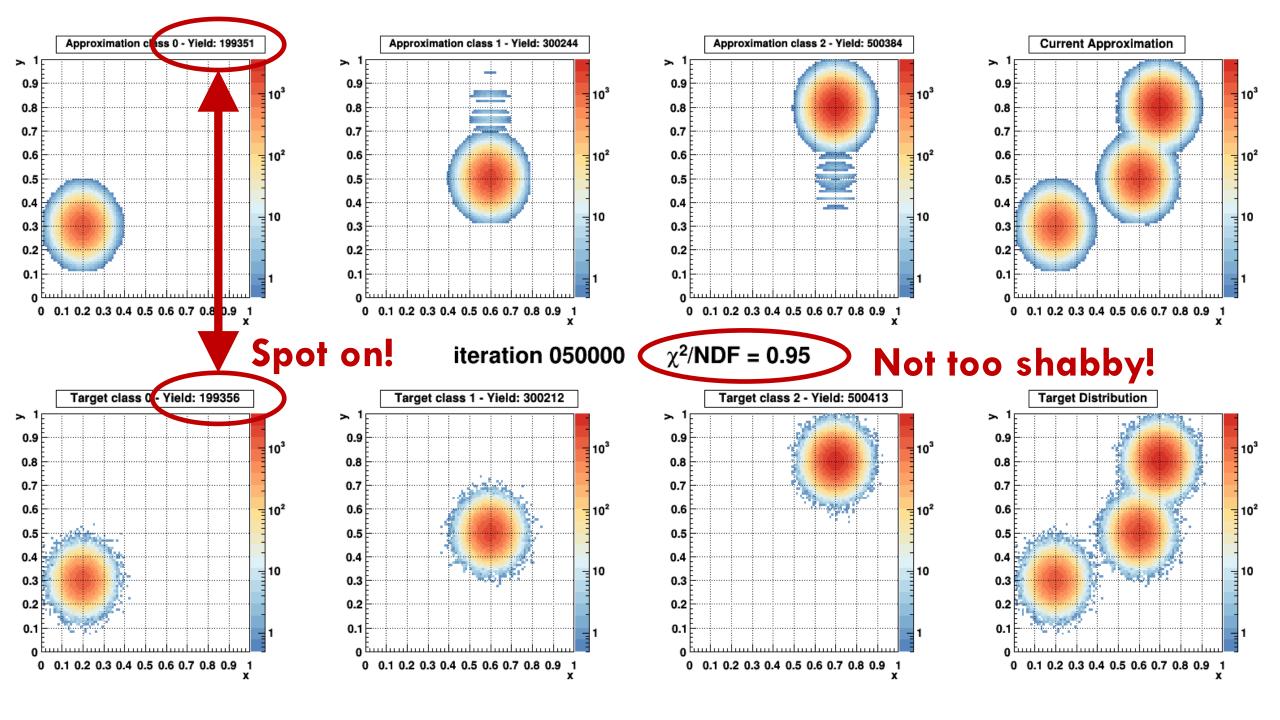
 $\chi^2/NDF = 9488.33$





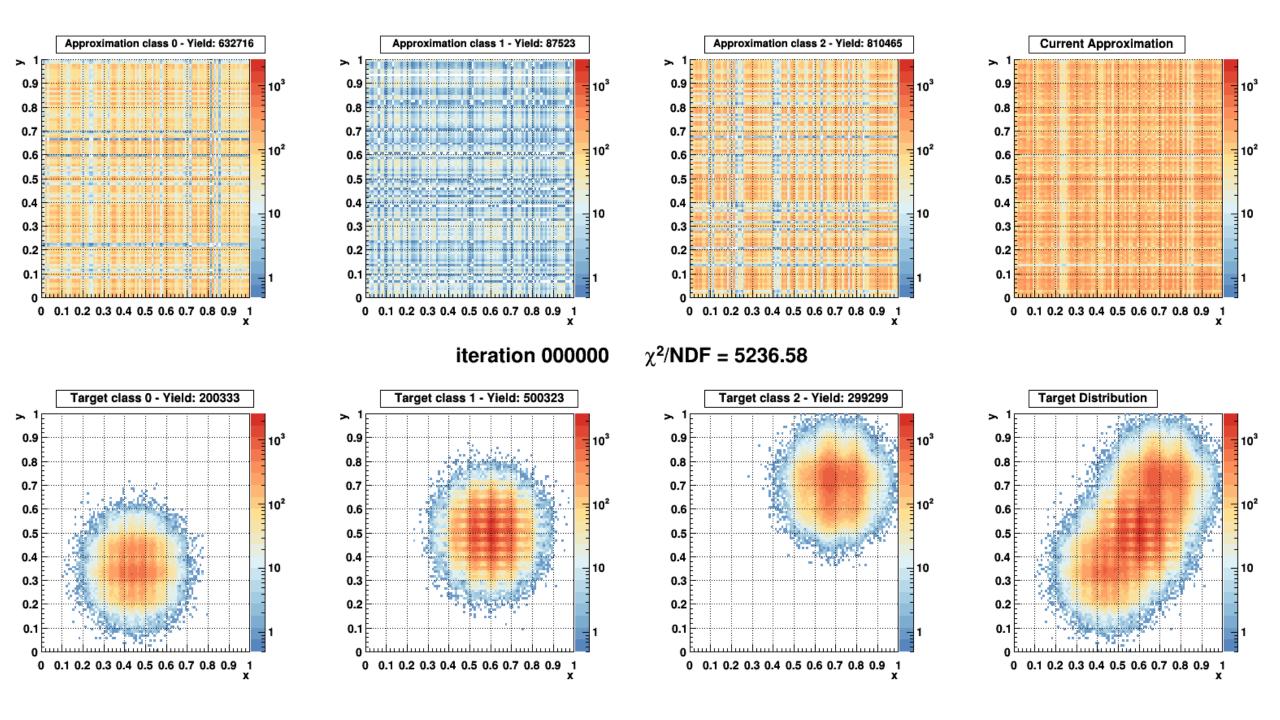


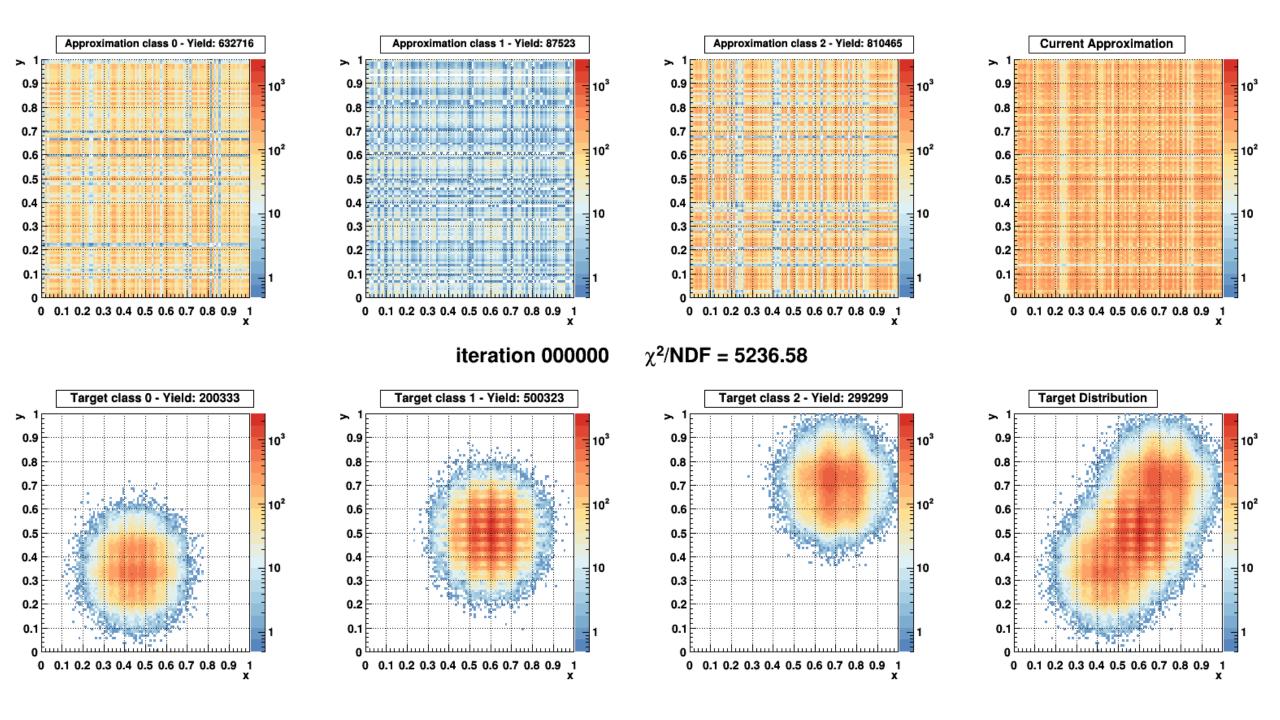


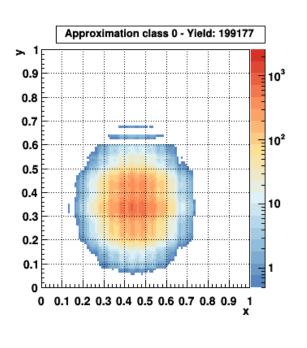


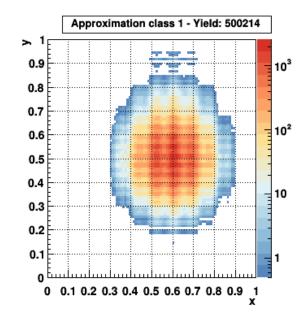
THAT ONE WAS TOO EASY!

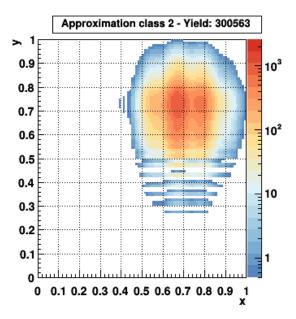
Fine, let's try a harder one then.

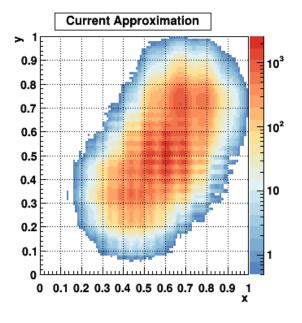






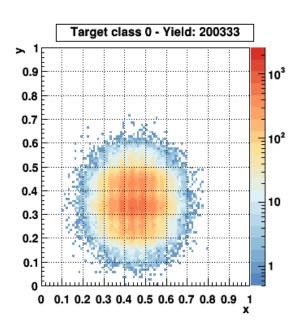


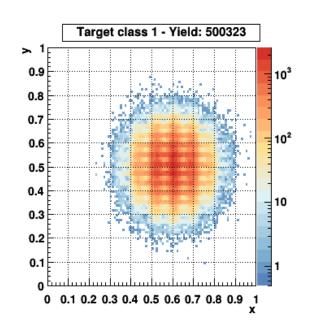


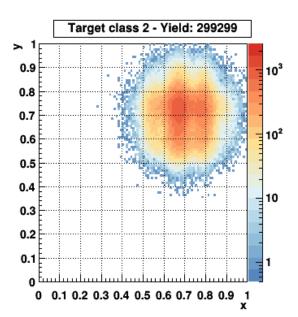


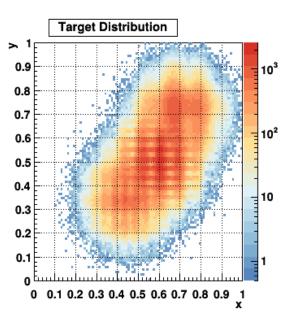
iteration 100000

 $\chi^2/NDF = 2.44$







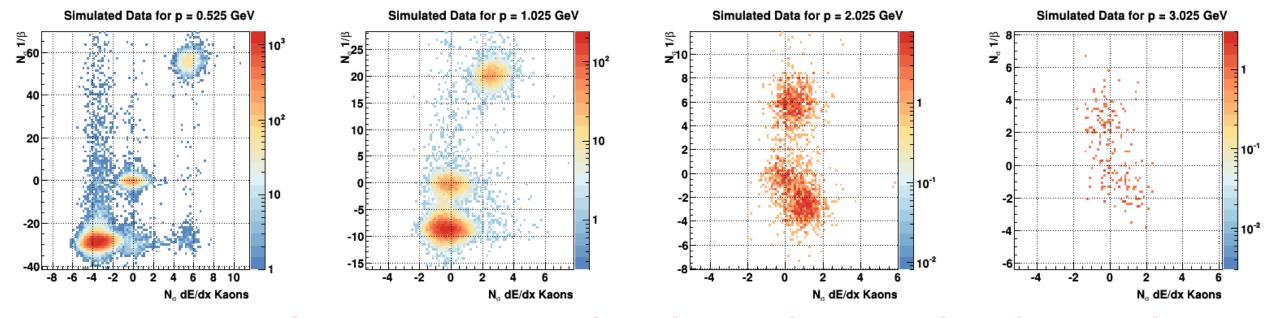


TOO UNREALISTIC! THOSE ARE WAFFLES!

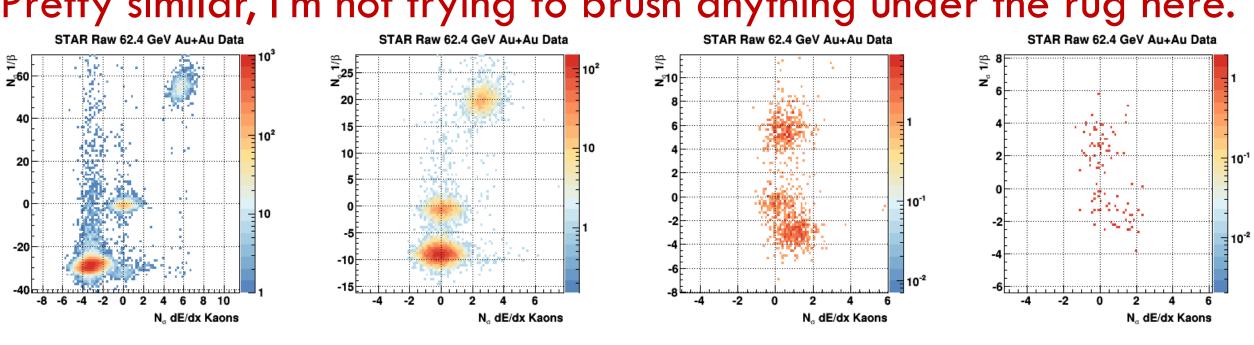
Ok, we can get more realistic.

SIMULATED DATASET: 1 BILLION TRACKS

- *π/K/p momentum spectra approximates those from Au+Au 62.4 GeV
- ❖Time-of-Flight and dE/dx measurements are made for each particle
- ❖Non-Gaussian Shapes
- Landau distribution for 15-45 dE/dx hits with highest 30% of measurements rejected for each track
- \diamond Possibility of similar momentum tracks merging and having higher dE/dx measurements
- Possibility of ToF measurement mistmatches between different particles
- Student's t-distribution for ToF measurement resolution
- *Momentum has limited resolution (2% on curvature)
- Finite momentum bin width size (50 MeV bins)
- ❖It's dirty, it's messy, and it's realistic



Pretty similar, I'm not trying to brush anything under the rug here.



DRUMROLL PLEASE...

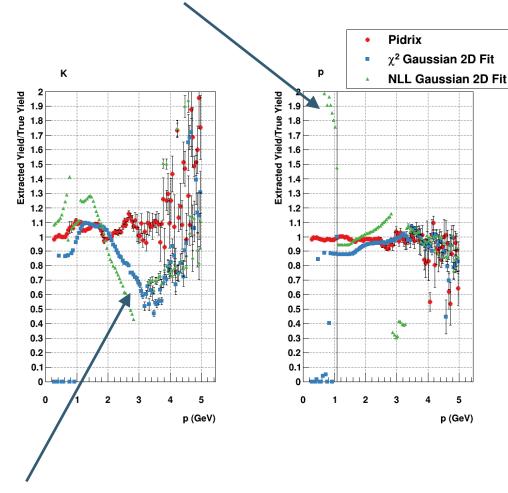
We're about to look at the ratio of Gaussian model fits and Pidrix fits over the true yields from simulations.



Yuck, failed fits. What do we have to fudge to get these to work?

Pidrix hands down
outperforms the
model fits.

Off the charts!



We don't realize when we make this mistake because the spectra still looks realistic.

p (GeV)

WHAT ABOUT ERRORS?

What factor would the yield error have to be multiplied by to be correct?

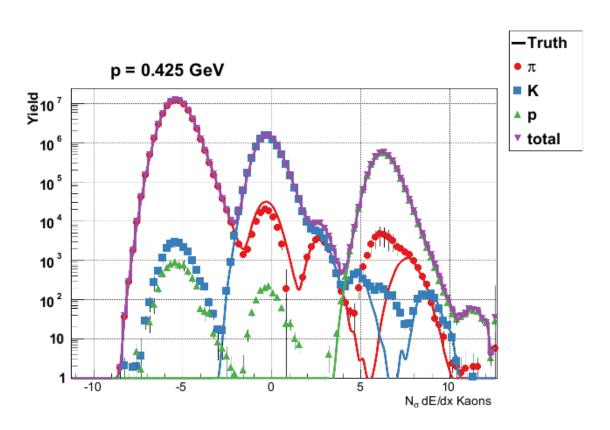
	Pidrix	Chi-squared	Log-likelihood
π	4.6	750000	77
K	7.2	230000	160
Р	4.2	270000	360

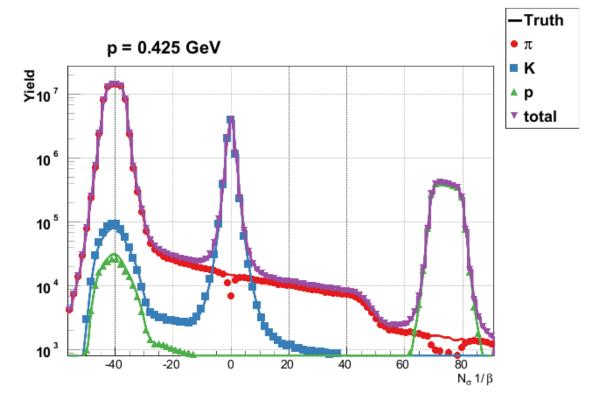
Minuit errors don't mean much when the model isn't exactly right. Pidrix gives <u>far more accurate errors</u> and I'm working on making them even better.

Small errors aren't better if they're wrong!

REMEMBER U AND V?

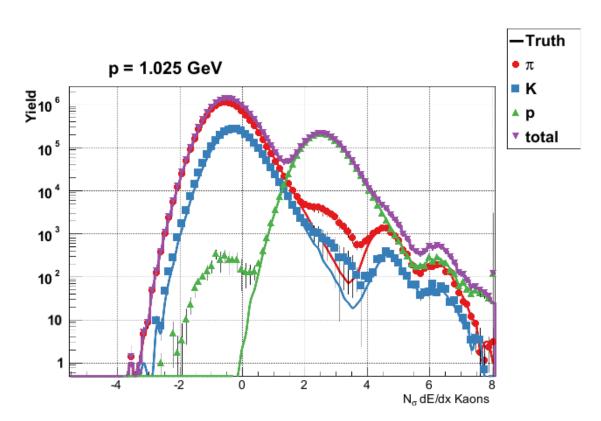
Their columns and rows have physical meaning.

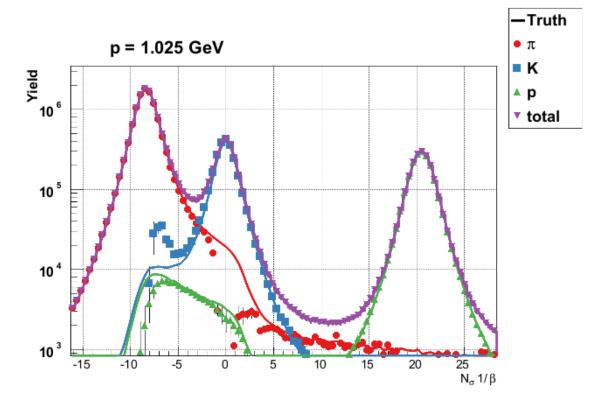




IT'S NOT PERFECT

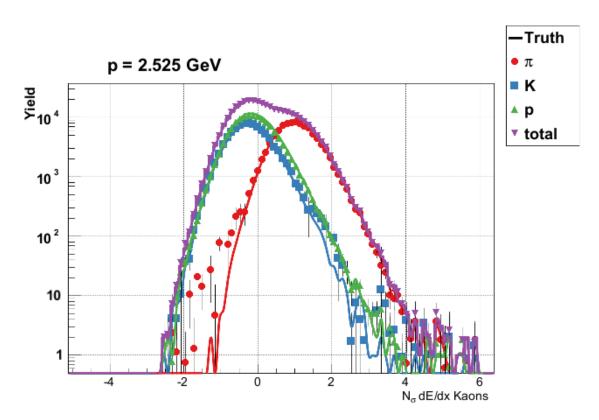
But it's pretty damn close.

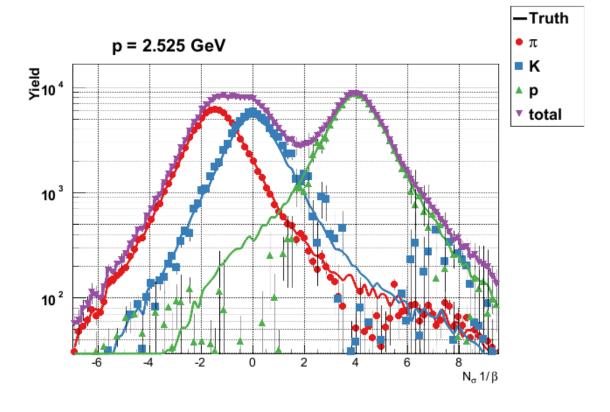




THIS IS A HARD ONE

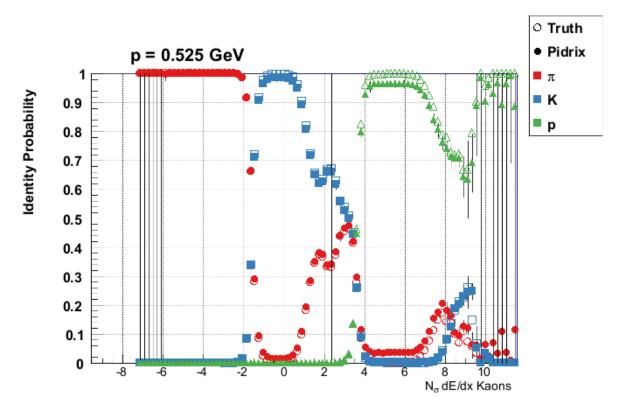
Should I bring back out the wow clipart yet?

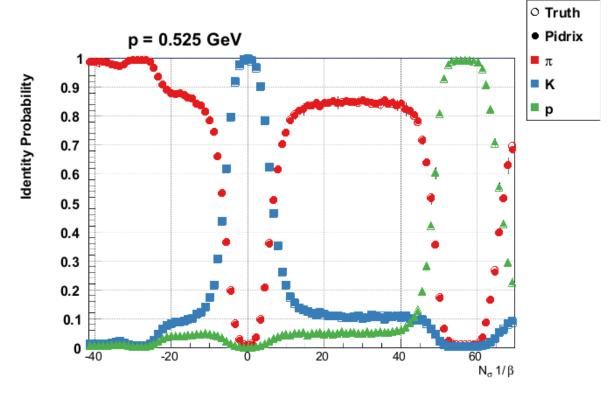




PURITY IS A VIRTUE

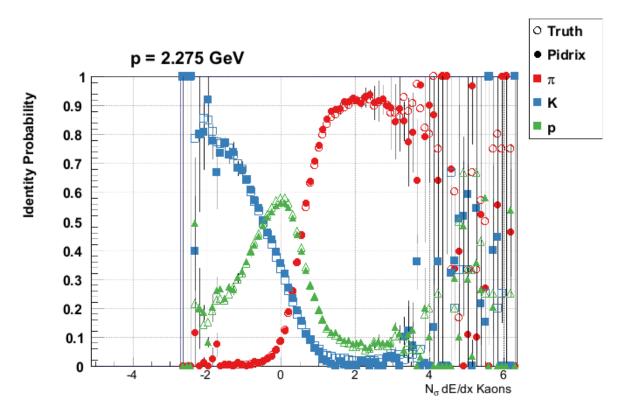
Want some help picking your cuts for high purity?

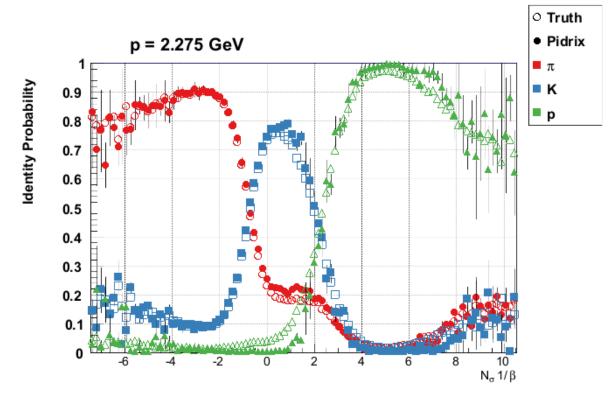




PURITY IS A VIRTUE

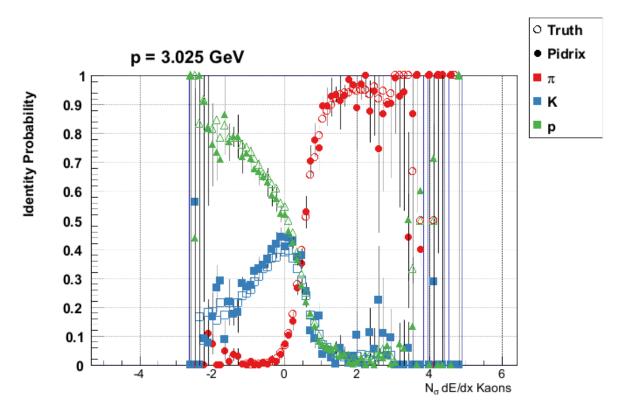
Or calculating what your cut efficiency is?

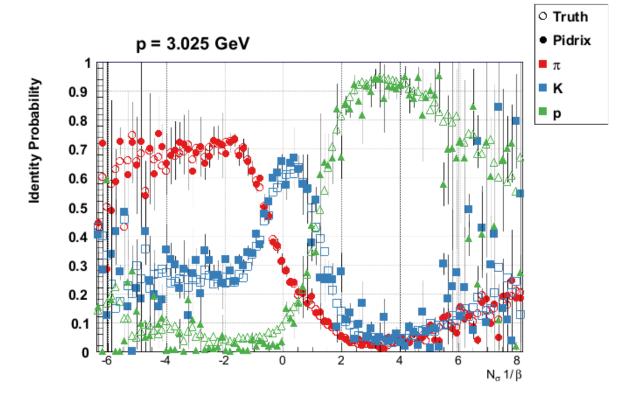




PURITY IS A VIRTUE

The method excels at purity estimates more so than finding the distributions.





REITERATION

- We're doing a negative log-likelihood minimization
 - ❖ Just not using a model and being clever about how we do this
- The worst assumption is that the measurements are uncorrelated
- Even when this is broken by momentum resolution and finite bin width it still works great
- The same code applies to any scenario
 - No model means no model tuning
- It seems to work really, really, really well!

LESS IS MORE?

- A new method for particle identification has been proposed
- *Faster, easier, and less assumption oriented than model based fitting
- Extremely promising accuracy observed in early tests
- Trivial extension to dimensions higher than two
- Progress is being made towards better understanding systematics
- Current clustering approach is a solid starting point
- There are crucial subtleties here
 - Some distributions are ill suited for unique factorization (non-unique minimums)
- FOSS implementation is in the works (not live yet, but will be soon)
- https://github.com/foobs/pidrix

THE END

