

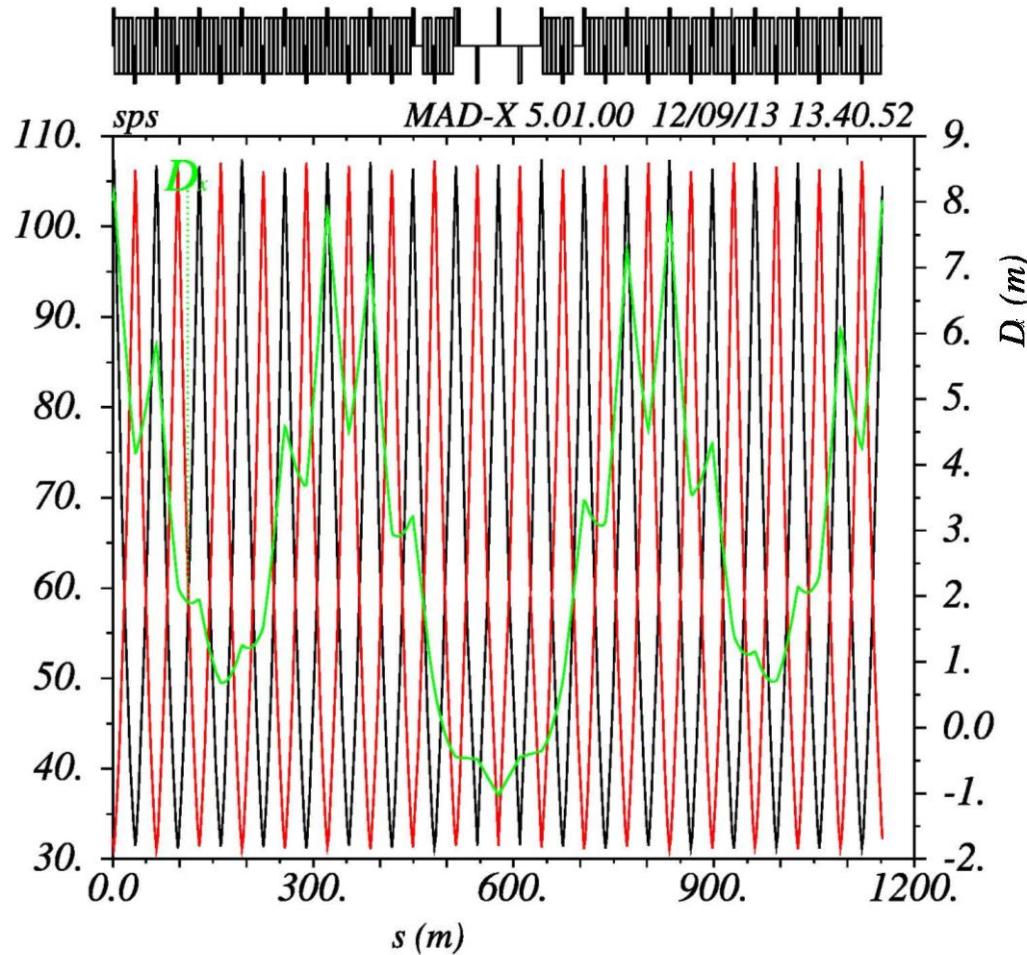
Intrabeam Scattering Computations for the SPS Lead Ion Beams

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- SPS beam parameters at injection (lead ion Pb⁸²₂₀₈)
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SPS optics (1st sextant)



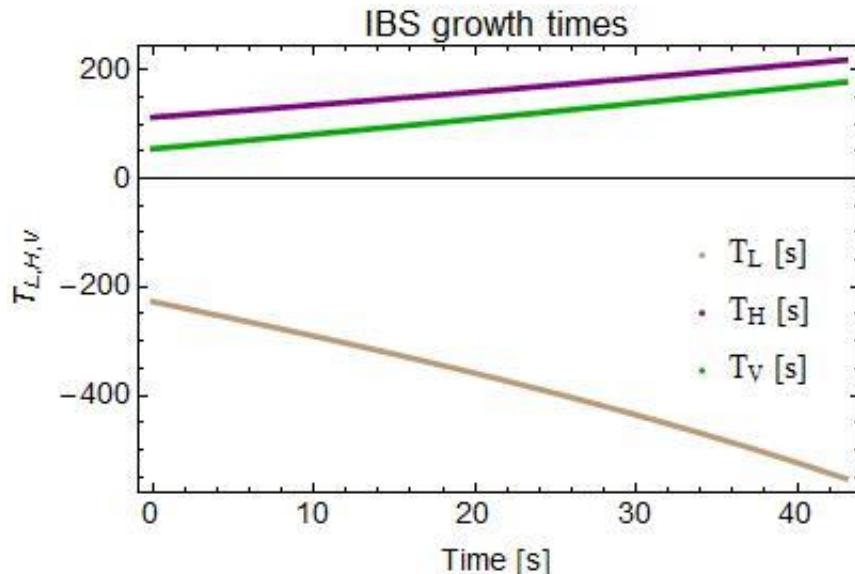
Q20 lattice : $Q_h=20.13$, $Q_v=20.18$

SPS beam parameters at injection (lead ion Pb⁸²₂₀₈)

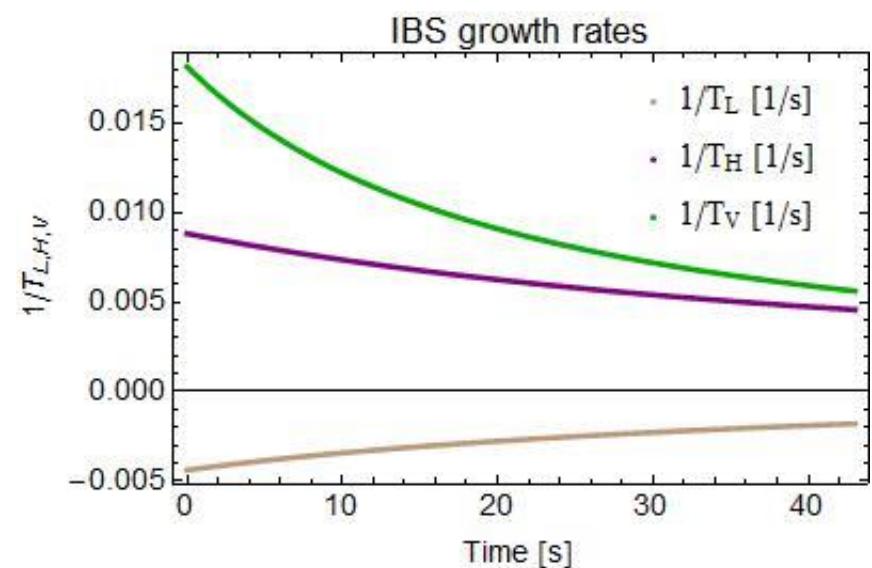
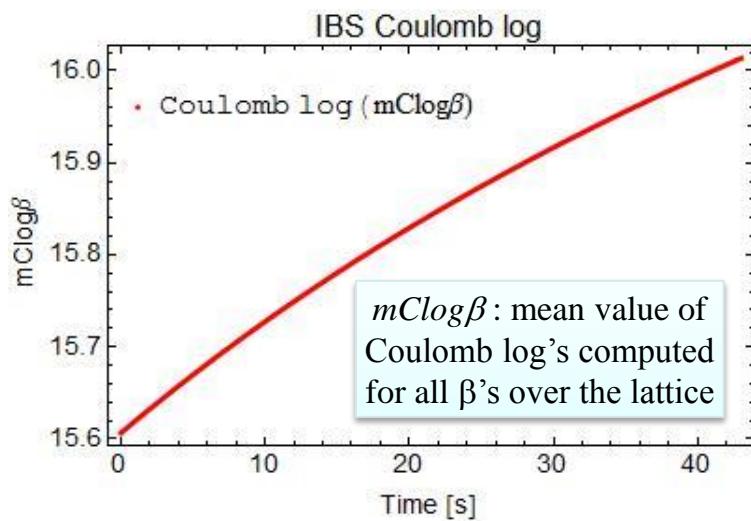
Relativistic factor γ	7.31
Momentum, pc , (GeV/c)/u	6.75
Proton equivalent momentum, pc_{PEM} , (GeV/c)/charge	17.11
Bunch intensity, ions/bunch	3.6×10^8
Circumference, m	6911.5
RF voltage, MV	2.4
Bunch length (4 rms) τ_B , ns (s_B , m) ($\sigma_{\tau_B} = \tau_B/4$, $\sigma_{s_B} = s_B/4$)	4.0 (1.2)
Relative momentum spread (2 rms) $\delta_p = \Delta p/p$ ($\sigma_{\delta_p} = \delta_p/2$)	1.13×10^{-3}
Longitudinal emittance (2 rms) $\varepsilon^{2\sigma}_L = 4\pi pc \sigma_{\delta_p} \sigma_{\tau_B}$, eVs/u	4.79×10^{-2}
Longitudinal emittance $\varepsilon^{2\sigma}_L = 4\pi E_{ion} \sigma_{\delta_E} \sigma_{\tau_B} = 4\pi \beta \gamma A E_u \sigma_{\delta_p} \sigma_{s_B} / c$, eVs	9.97
Horizontal normalized emittance (rms) $\varepsilon^{1\sigma}_H$, μm	0.9
Vertical normalized emittance (rms) $\varepsilon^{1\sigma}_V$, μm	0.7

SPS IBS growth times and growth rates						
	τ_L s	τ_H s	τ_V s	τ_L^{-1} s	τ_H^{-1} s	τ_V^{-1} s
Bjorken & Mtingwa (M.M.)	-227.1	113.2	55.0	-4.4×10^{-3}	8.8×10^{-3}	1.8×10^{-2}
Piwinski (Ch.C)	-223.7	112.9	56.8	-4.5×10^{-3}	8.9×10^{-3}	1.8×10^{-2}

SPS IBS growth times and growth rates



$$\begin{aligned}\tau_L(0) &= -227.1 \text{ s} \\ \tau_H(0) &= 113.2 \text{ s} \\ \tau_V(0) &= 55.0 \text{ s}\end{aligned}$$

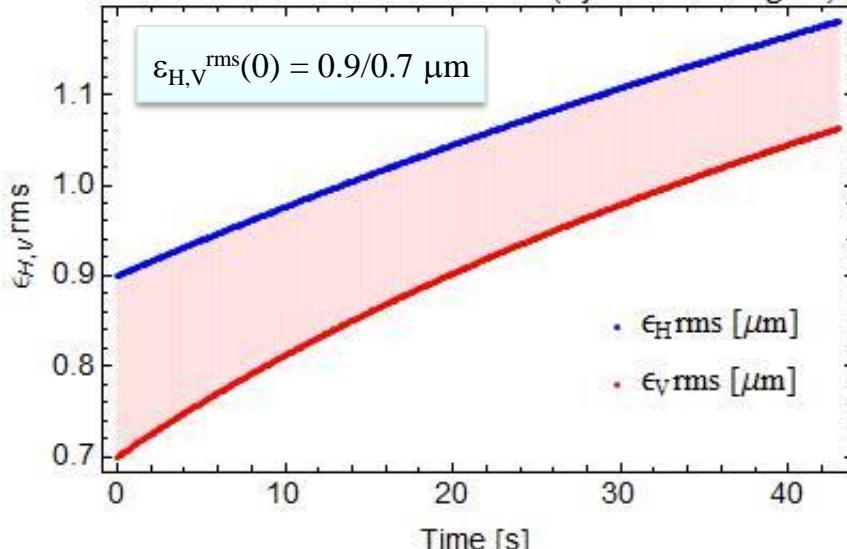


$$\begin{aligned}\tau_L^{-1}(0) &= -4.40 \times 10^{-3} \text{ s}^{-1} \\ \tau_H^{-1}(0) &= 8.83 \times 10^{-3} \text{ s}^{-1} \\ \tau_V^{-1}(0) &= 1.82 \times 10^{-2} \text{ s}^{-1}\end{aligned}$$

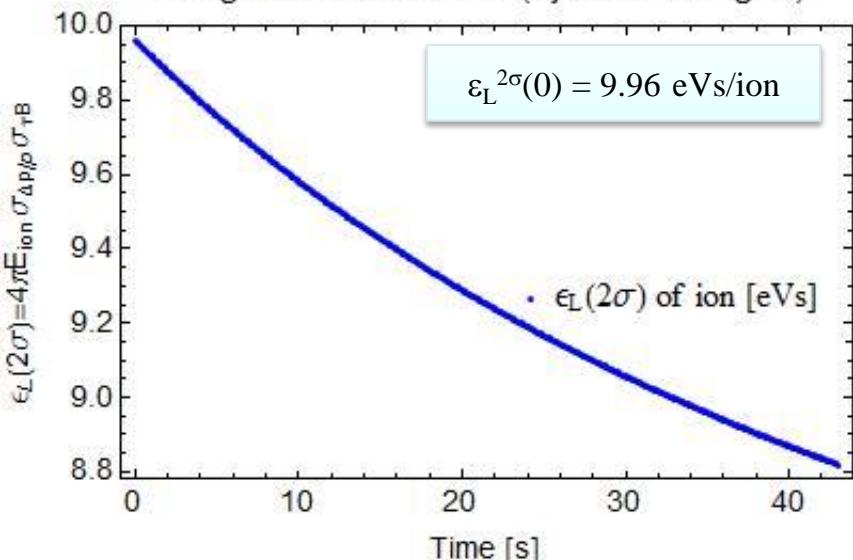
Evolution on the 43 s SPS injection plateau (Bjorken-Mtingwa IBS model)

SPS IBS emittance increase

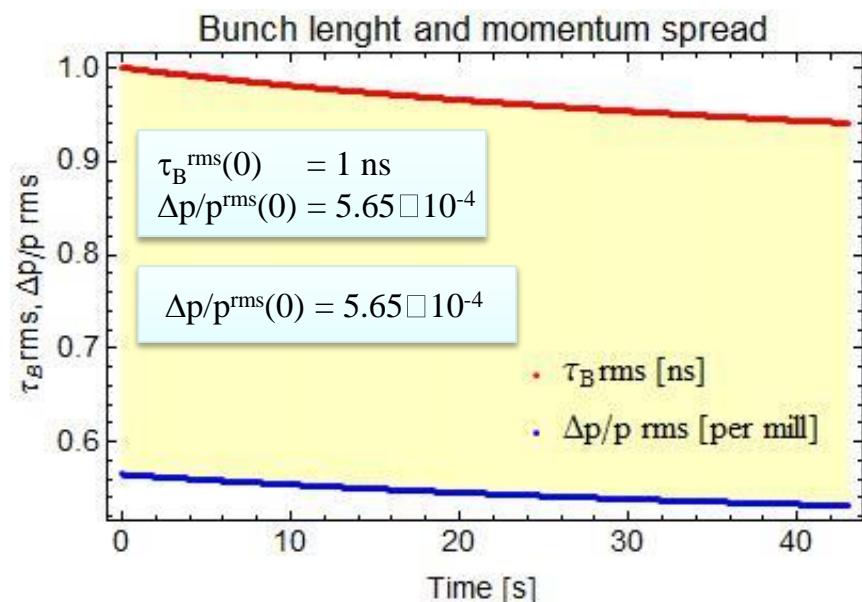
H&V normalized emittances (Bjorken–Mtingwa)



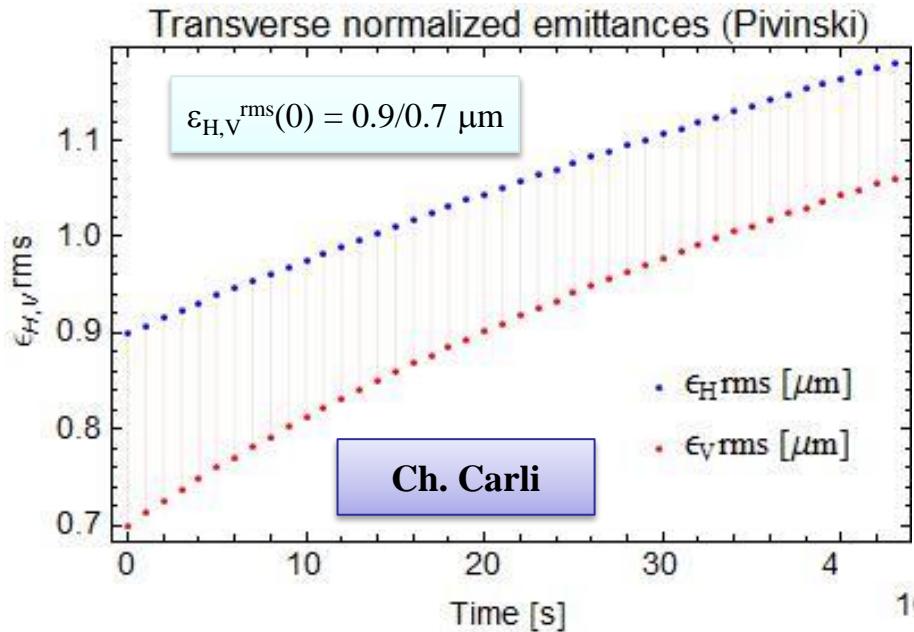
Longitudinal emittance (Bjorken–Mtingwa)



**Evolution along the 43 s
SPS injection plateau
(Bjorken-Mtingwa IBS model)**



SPS IBS emittance increase



**Evolution along the 43 s
SPS injection plateau
(Piwinski IBS model)**

