The Mathematics of Quantum Theory



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Quantum curves and the infinite-dimensional Grassmannian

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One says that a pair (P,Q) of ordinary differential operators specify a quantum curve if $[P,Q]=\hbar$. If a pair of difference operators (K,L) obey the relation $KL=\lambda LK$ where $\lambda=e^{\hbar}$ we say that they specify a discrete quantum curve.

This terminology is prompted by well known results about commuting differential and difference operators , relating pairs of such operators with pairs of meromorphic functions on algebraic curves obeying some conditions.

Our methods are based on the interpretation of quantum curves in terms of infinite-dimensional Grassmannian; in particular, it follows from this interpretation that (discrete) KP-hierarchy can be used to deform a (discrete) quantum curve.

The main goal is to study the moduli spaces of quantum curves. We will relate the moduli spaces for different \hbar . We will show how to quantize a pair of commuting differential or difference operators (i.e. to construct the corresponding quantum curve or discrete quantum curve)

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