

Composite Light Quarks

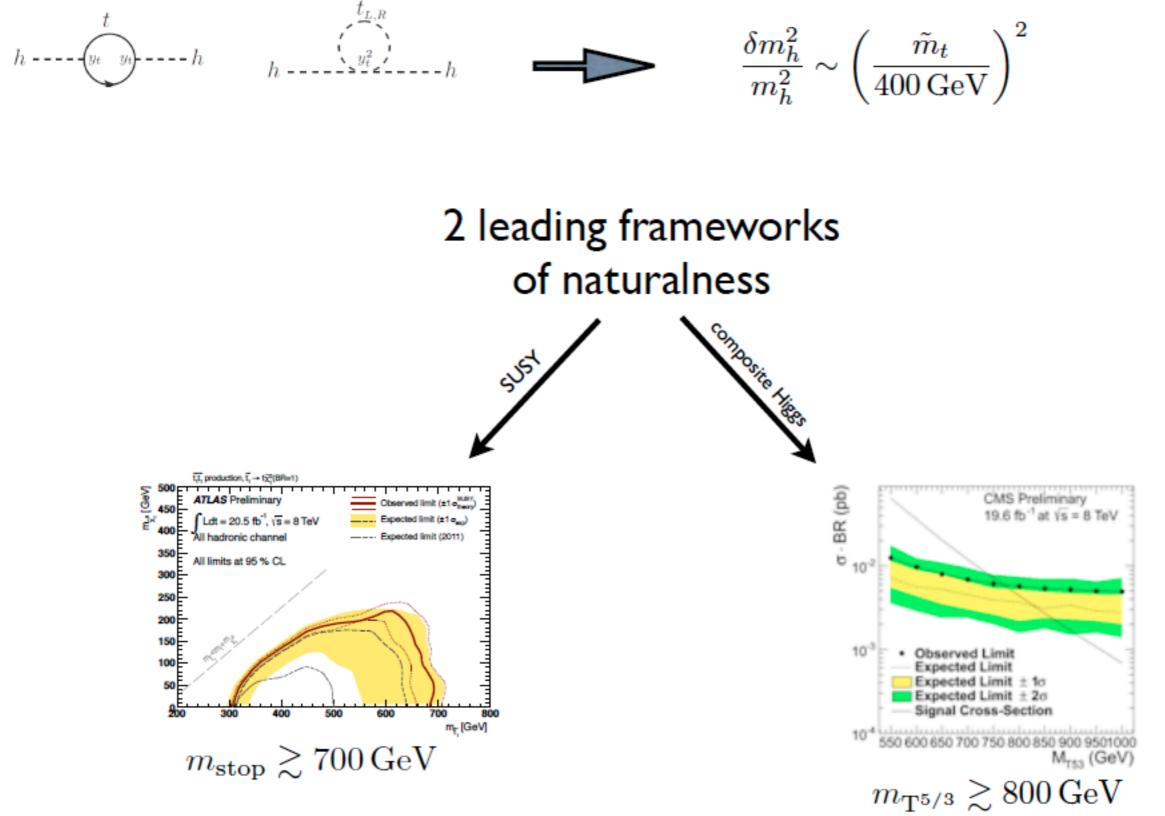




Delaunay, Fraille, Flacke, SL, Panico, Perez `13 Flacke, Kim, SL, Lim `13

Aspen Winter Conference 2014 Frontiers in Particle Physics: From Dark Matter to the LHC and Beyond

Motivation Joe Lyken & Gilad Perez's talk on Sunday Naturalness => new colored partners, potentially within the LHC reach.





Georgi, Kaplan '84; Kaplan '91; Agashe, Contino, Pomarol '05; Agashe et al '06; Giudice et al '07; Contino et al '07; Csaki, Falkowski, Weiler '08; Contno, Servant '08; Mrazek, Wulzer '10; Panico, Wulzer '11; De Curtis, Redi, Tesi '11, Marzocca, Serone, Shu '12; Pomarol, Riva '12; Bellazini et al '12; De Simone et al '12, Grojean, Matsedonskyi, Panico "13,...

Just as pion (PGB) is the lightest states in QCD, Higgs is a PGB of a new strong sector (with symmetry breaking scale f) => Higgs is lighter than other resonances Georgi & Kaplan '84

Warped XD models: 5D dual (AdS/CFT correspondence) Randall & Sundrum,... '90s of Composite Higgs: 5D model gives an explicit realization of the 4D GUT works just as good as in SUSY

Little Higgs: collective symmetry breaking

Two or more explicit symmetry breaking terms are needed to break all Arkani-Hamed, Cohen, Georgi '00s symmetries protecting the Higgs mass. No quadratic divergences at

Holographic Higgs: Higss as a component of GB (A5) Contino, Nomura, Pomarol; Agashe, Contino, Pomarol; Hosotani,...

Simple 4D effective description (Strongly-Interacting Giudice, Grojean, Pomarol, Rattazzi '07

NB: Higgs does not need to be a usual PGB and can arise from other mechanisms, i.e. it can be a light dilaton Bellazzini, Csaki, Hubisz, Serra, Terning '12



Higgs potential radiatively generated by resonances loops (top is the largest contribution)

***** Top contribution to the Higgs potential:

$$m_h^2 \simeq \frac{N_c}{\pi^2} \begin{bmatrix} \frac{m_t^2}{f^2} \frac{m_{Q_4}^2 m_{Q_1}^2}{m_{Q_1}^2 - m_{Q_4}^2} \log \left(\frac{m_{Q_1}^2}{m_{Q_4}^2}\right) \end{bmatrix}$$
 Pomarol, Riva '12
5 of SO(5) =4 + 1



Higgs potential radiatively generated by resonances loops (top is the largest contribution)

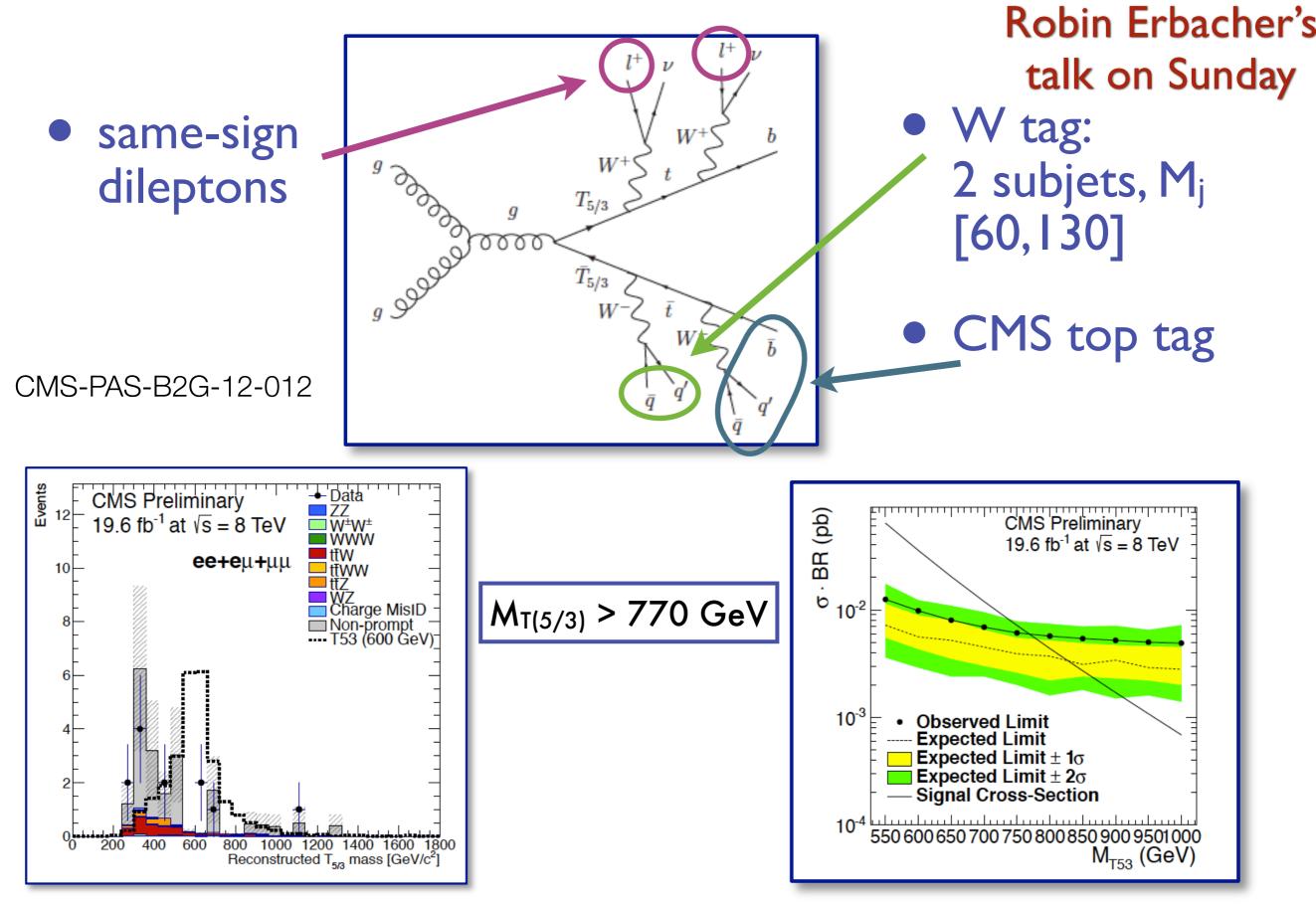
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 Contino et. al,
Pomarol, Riva '12
5 of SO(5) =4 + 1

=> light top partners (< ~I TeV) are required to obtain 125 GeV Higgs mass

$$V(h) = \underbrace{I_L}_T + \underbrace{I_R}_T + \cdots_T +$$

Limit on composite Top partner

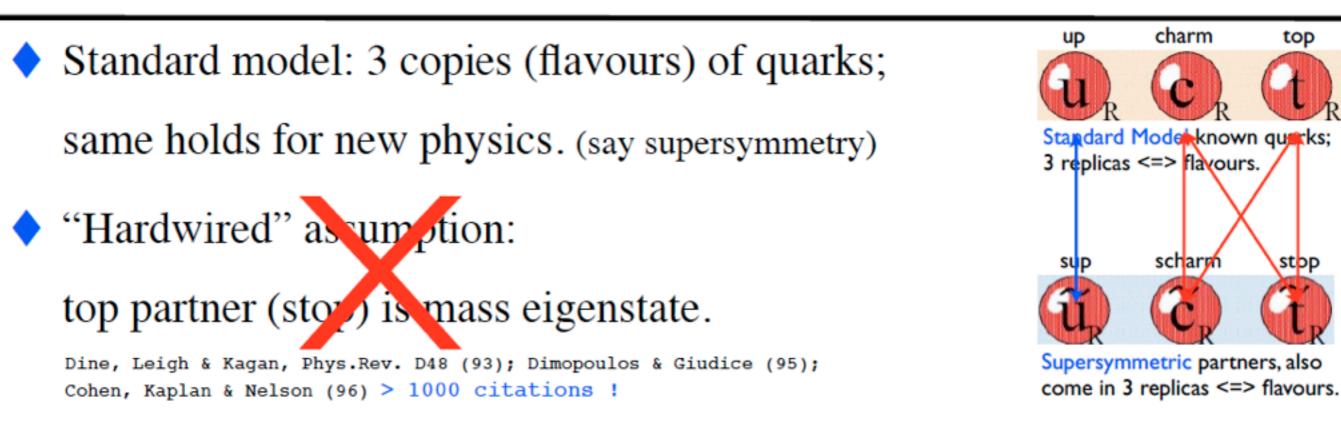


Flavourful naturalness

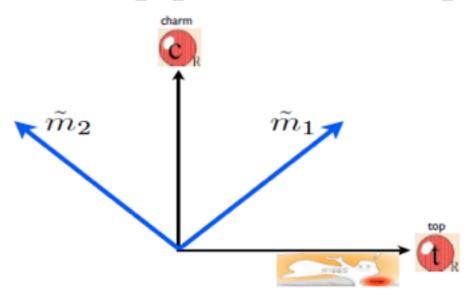
Gilad Perez's talk on Sunday

top

stop



This need not be the case, top-partner => "stop-scharm" admixture.



Composite Light Quark

Custodial symmetry for Z->bb Agashe, Contino, Da Rold, Pomarol '12 => allow for composite light quark without tension with precision tests Delaunay, Gedalia, SL, Perez, Ponton (x2) '10; Redi, Weiler 'II MFV

Trastic change to phenology: large production rates, top forward-backward asymmetry, non-standard flavor signals ... Delaunay, Gedalia, SL, Perez, Ponton (x2) '10; Redi, Weiler '11;

Redi, Sanz, de Vries, Weiler '13; Da Rold, Delaunay, Grojean, Perez '13; Atre, Chala, Santiago '13

And LHC implications for non-degenerate first 2generation partners. Delaunay, Fraille, Flacke, SL, Panico, Perez `13

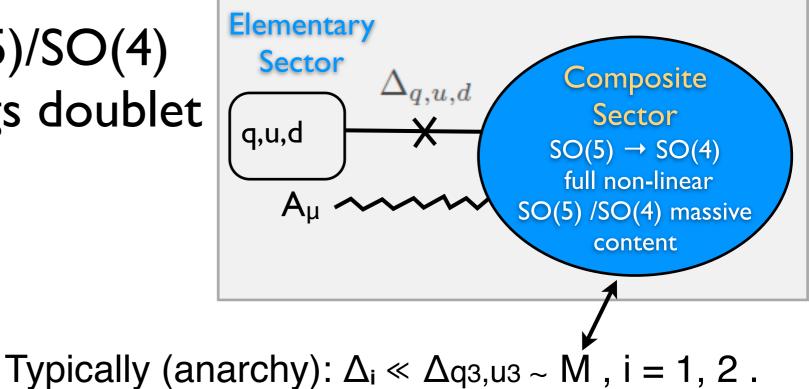
Kim, Flake, SL, Lim '13

Partial Compositeness

Partial Compositeness: D.B. Kaplan; Gorssman & Neubert; Huber,... Elementary-composite states talk through linear couplings.

The flavor problem of TC theories can be improved if the Yukawa couplings arise through mixings of elementary quarks with fermionic operators of the strong sector

minimal model: SO(5)/SO(4)
 with 4 GBs => Higgs doublet
 Agashe, Contino, Pomarol '05



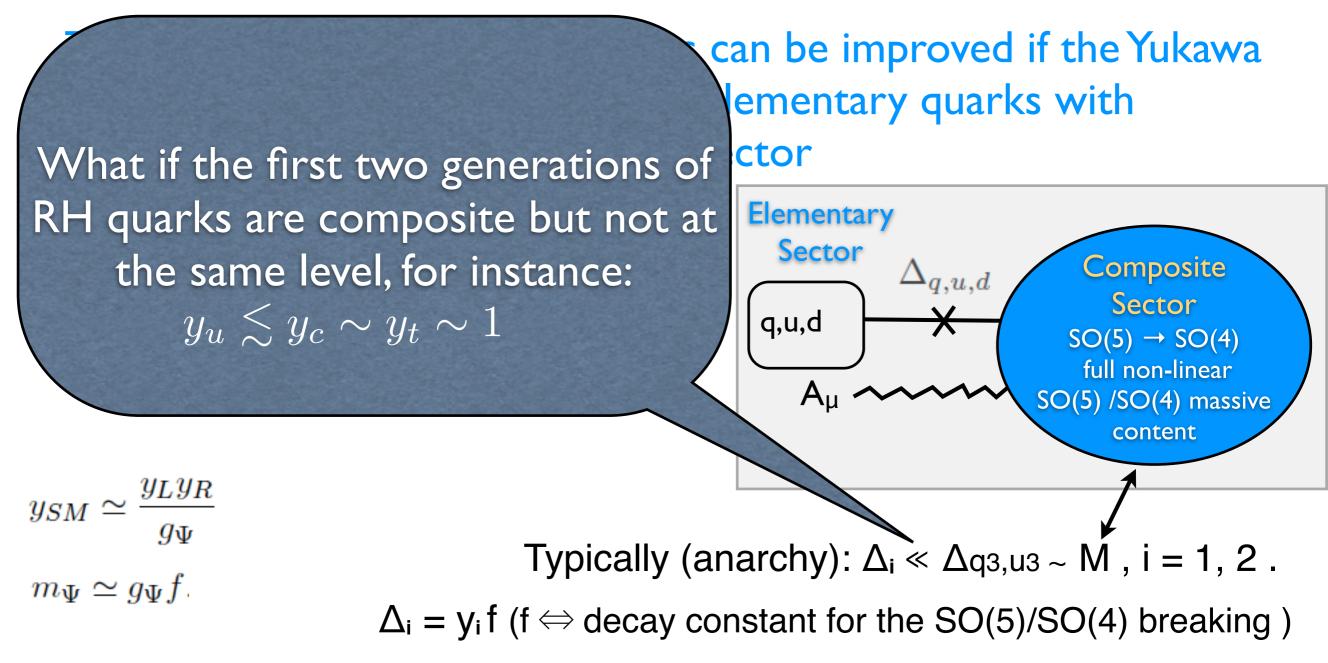
 $\Delta_i = y_i f$ (f \Leftrightarrow decay constant for the SO(5)/SO(4) breaking)

 $y_{SM} \simeq \frac{y_L y_R}{y_L y_R}$

 $m_{\Psi} \simeq g_{\Psi} f$.

Partial Compositeness

Partial Compositeness: D.B. Kaplan; Gorssman & Neubert; Huber,... Elementary-composite states talk through linear couplings.



General Set-up



As a setup we choose the minimal composite Higgs model based on SO(5)/SO(4). We use the CCWZ construction in order to write down \mathcal{L}_{eff} in a nonlinearly invariant way under SO(5) Coleman, Wess, Zumino '69, Callan, Coleman '69 Note: possible vector resonances are "integrated out" and do not appear directly in the effective description

The model contains elementary fermions *q* and composite fermionic resonances of the strongly coupled theory, which mix via linear interactions

$$\mathcal{L}_{\textit{mix}} = y \overline{q}_{I_{\mathcal{O}}} \mathcal{O}^{I_{\mathcal{O}}} + \mathsf{h.c.}$$

where \mathcal{O} is an operator of the strongly coupled theory in the rep. $I_{\mathcal{O}}$, and $\overline{q}_{I_{\mathcal{O}}}$ is an (incomplete) embedding of the elementary q into SO(5).

One common choice (partially composite quarks):

$$\overline{q}_{L}^{5} = \frac{1}{\sqrt{2}} \left(-i\overline{d}_{L}, \overline{d}_{L}, -i\overline{u}_{L}, -\overline{u}_{L}, 0 \right),$$

$$\overline{u}_{R}^{5} = (0, 0, 0, 0, \overline{u}_{R}),$$

This fixes composite partner quarks to be embedded as 5 reps. of SO(5):

$$\psi = \begin{pmatrix} Q \\ \tilde{U} \end{pmatrix} = \frac{1}{\sqrt{2}} \begin{pmatrix} iD - iX_{5/3} \\ D + X_{5/3} \\ iU + iX_{2/3} \\ -U + X_{2/3} \\ \sqrt{2}\tilde{U} \end{pmatrix}$$

General Set-up

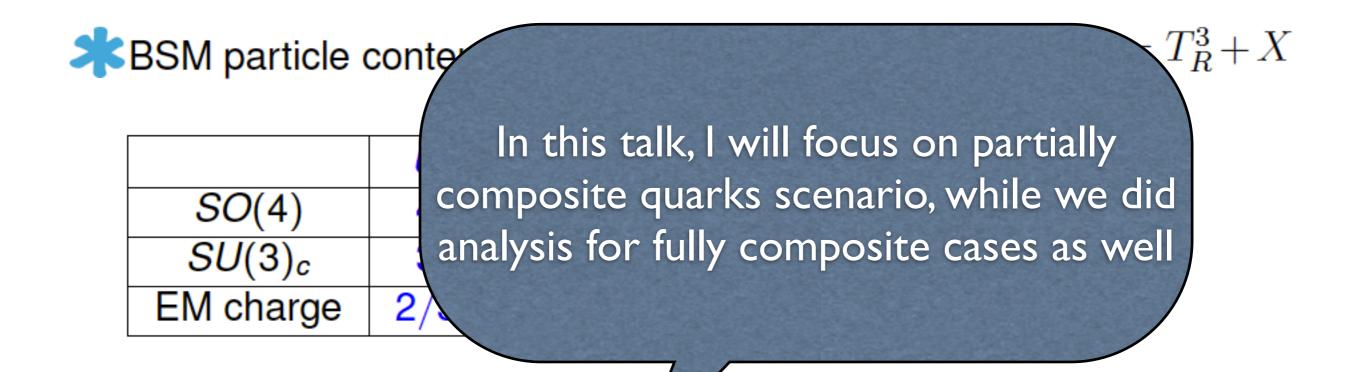
***BSM particle content:**
$$5 = 4 + 1$$
 $Y = T_R^3 + X$

	U	X _{2/3}	D	<i>X</i> _{5/3}	Ũ
<i>SO</i> (4)	4	4	4	4	1
<i>SU</i> (3) _c	3	3	3	3	3
EM charge	2/3	2/3	-1/3	5/3	2/3

Two principal ways to embed the right-handed up-type quarks:

- In the elementary sector, which mix with their partners, (→ "partially composite quarks")
- or as chiral composite states.
 (→ "fully composite quarks")

General Set-up



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- or as chiral composite states.
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Partial Composite light quarks

*****Fermion Lagrangian:

Delaunay, Fraille, Flacke, SL, Panico, Perez `13 Flacke, Kim, SL, Lim `13

$$\mathcal{L}_{\textit{comp}} = i \,\overline{Q} (D_{\mu} + i e_{\mu}) \gamma^{\mu} Q + i \overline{\tilde{U}} D \widetilde{U} - M_4 \overline{Q} Q - M_1 \overline{\tilde{U}} \widetilde{U} + \left(i c \overline{Q}^i \gamma^{\mu} d^i_{\mu} \widetilde{U} + \text{h.c.}
ight)$$

 $\mathcal{L}_{el,mix} = i \overline{q}_L \mathcal{D} q_L + i \overline{u}_R \mathcal{D} u_R - y_L f \overline{q}_L^5 U_{gs} \psi_R - y_R f \overline{u}_R^5 U_{gs} \psi_L + \text{h.c.},$

where d_{μ}^{i} , e_{μ} are the CCWZ "connections", and U_{gs} is the Goldstone matrix

$$U_{gs} = \begin{pmatrix} 1 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & \cos \overline{h}/f & \sin \overline{h}/f \\ 0 & 0 & 0 & -\sin \overline{h}/f & \cos \overline{h}/f \end{pmatrix},$$

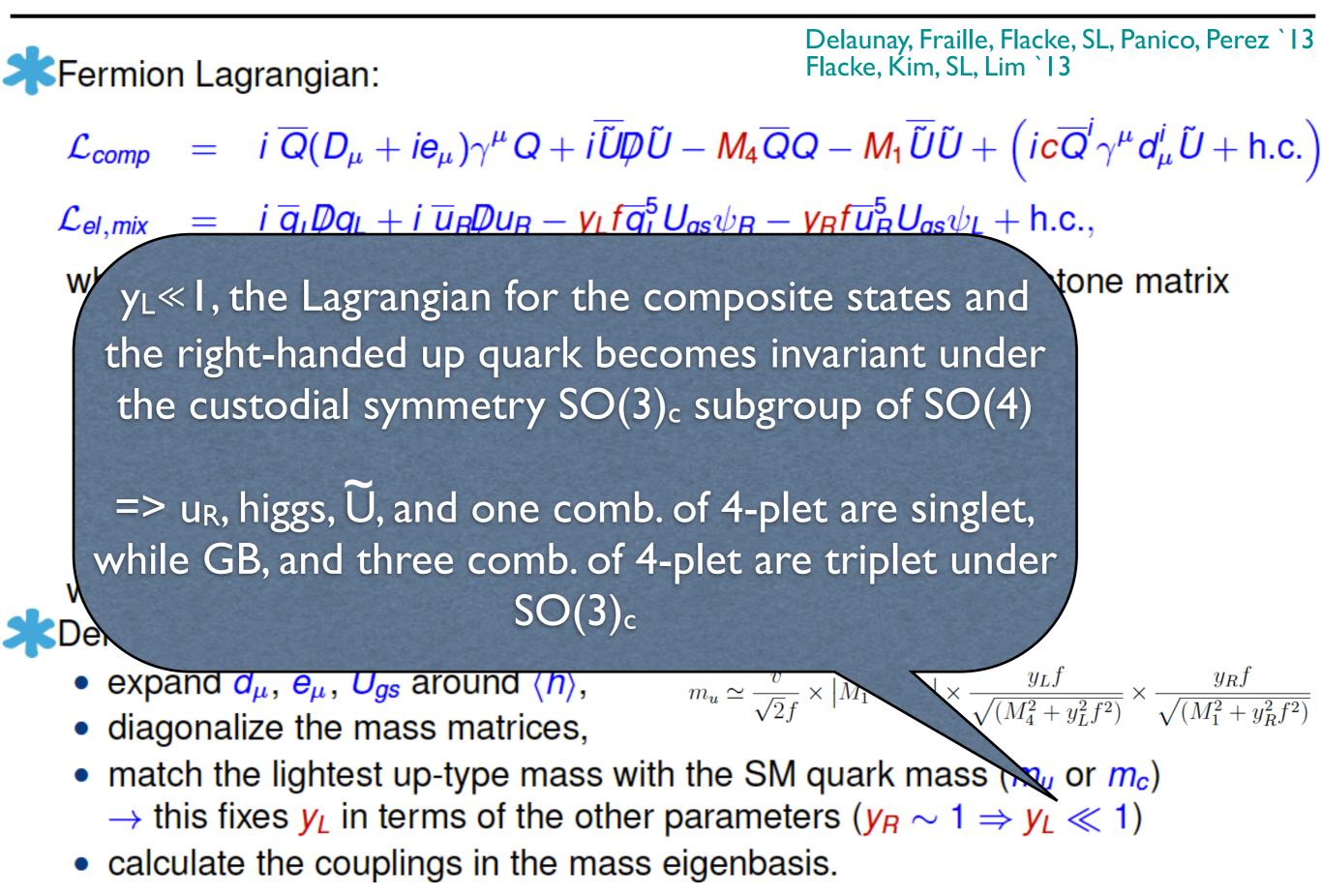
with $\overline{h} = \langle h \rangle + h$. Derivation of Feynman rules:

• expand d_{μ} , e_{μ} , U_{gs} around $\langle h \rangle$,

$$m_u \simeq \frac{v}{\sqrt{2}f} \times |M_1 - M_4| \times \frac{y_L f}{\sqrt{(M_4^2 + y_L^2 f^2)}} \times \frac{y_R f}{\sqrt{(M_1^2 + y_R^2 f^2)}}$$

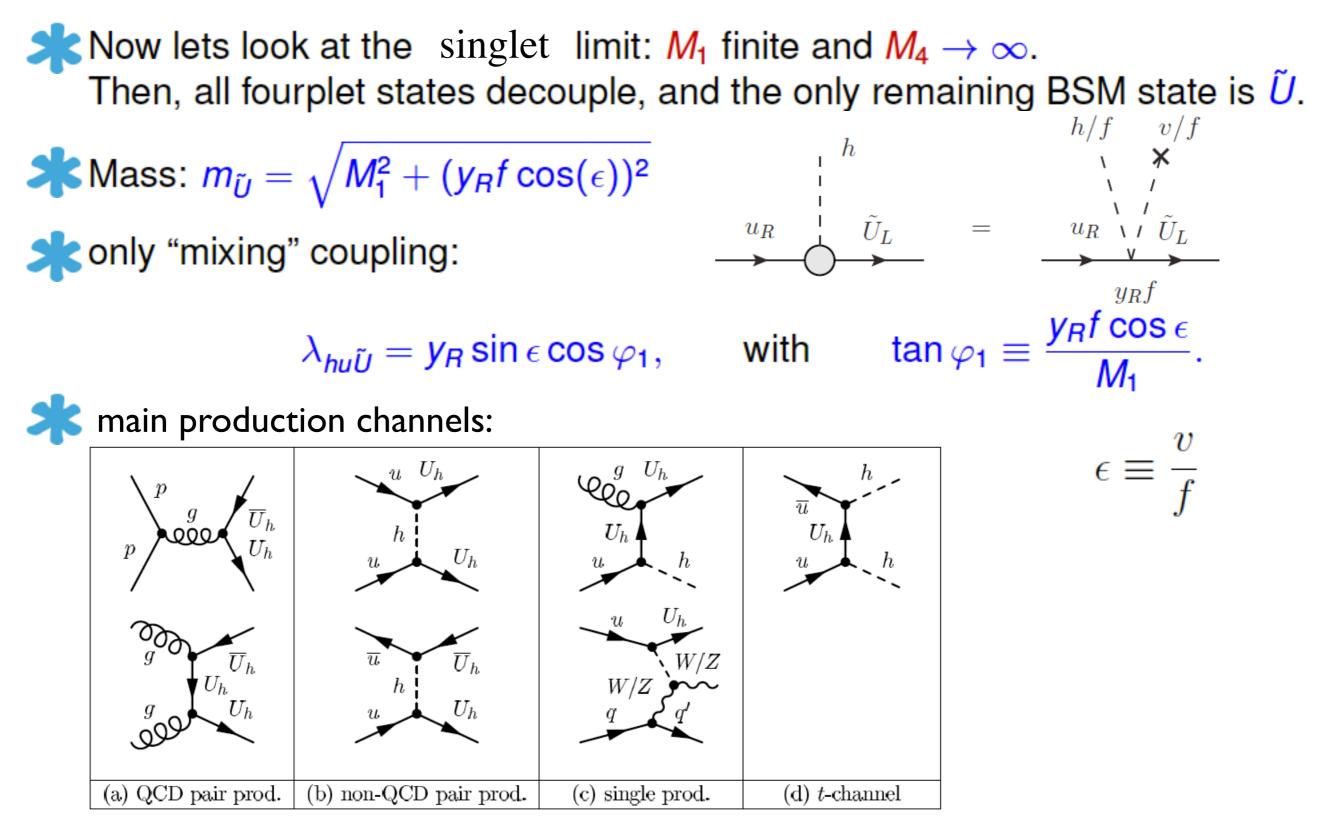
- diagonalize the mass matrices,
- match the lightest up-type mass with the SM quark mass $(m_u \text{ or } m_c)$ \rightarrow this fixes y_L in terms of the other parameters $(y_R \sim 1 \Rightarrow y_L \ll 1)$
- calculate the couplings in the mass eigenbasis.

Partial Composite light quarks



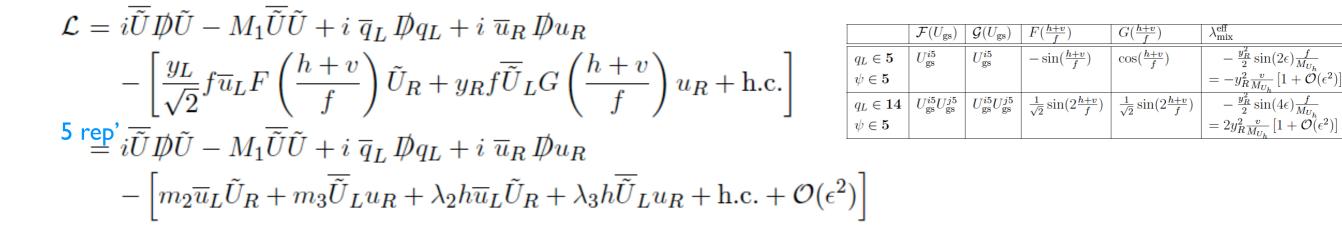
Partners in Singlet

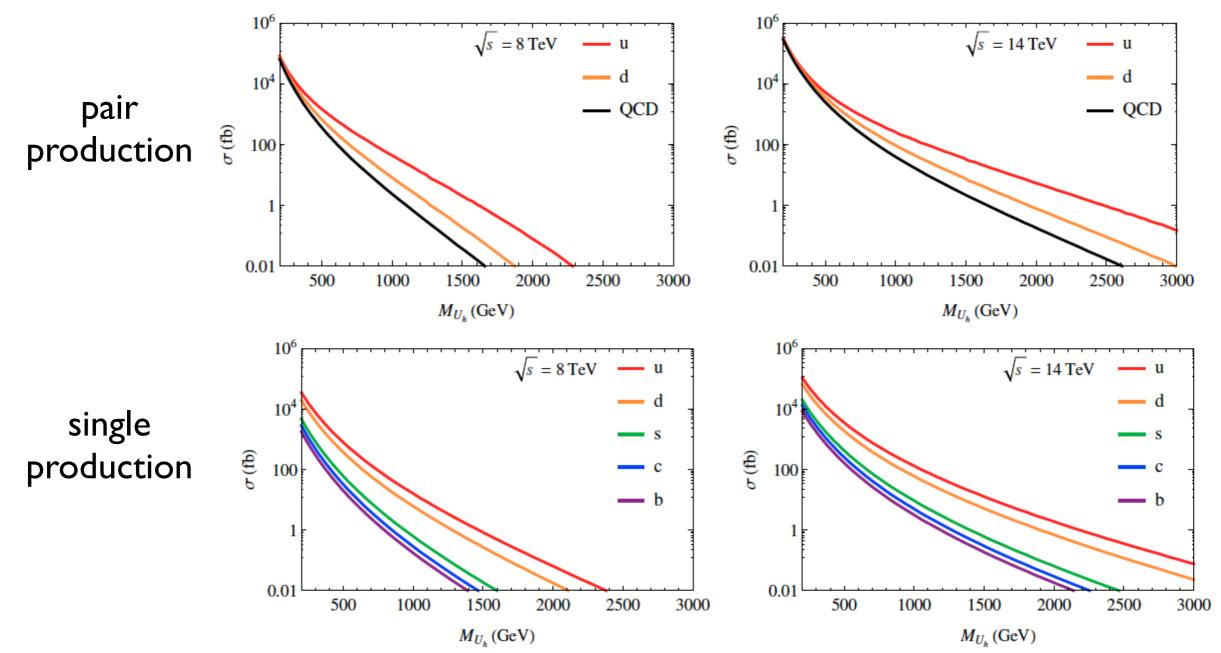
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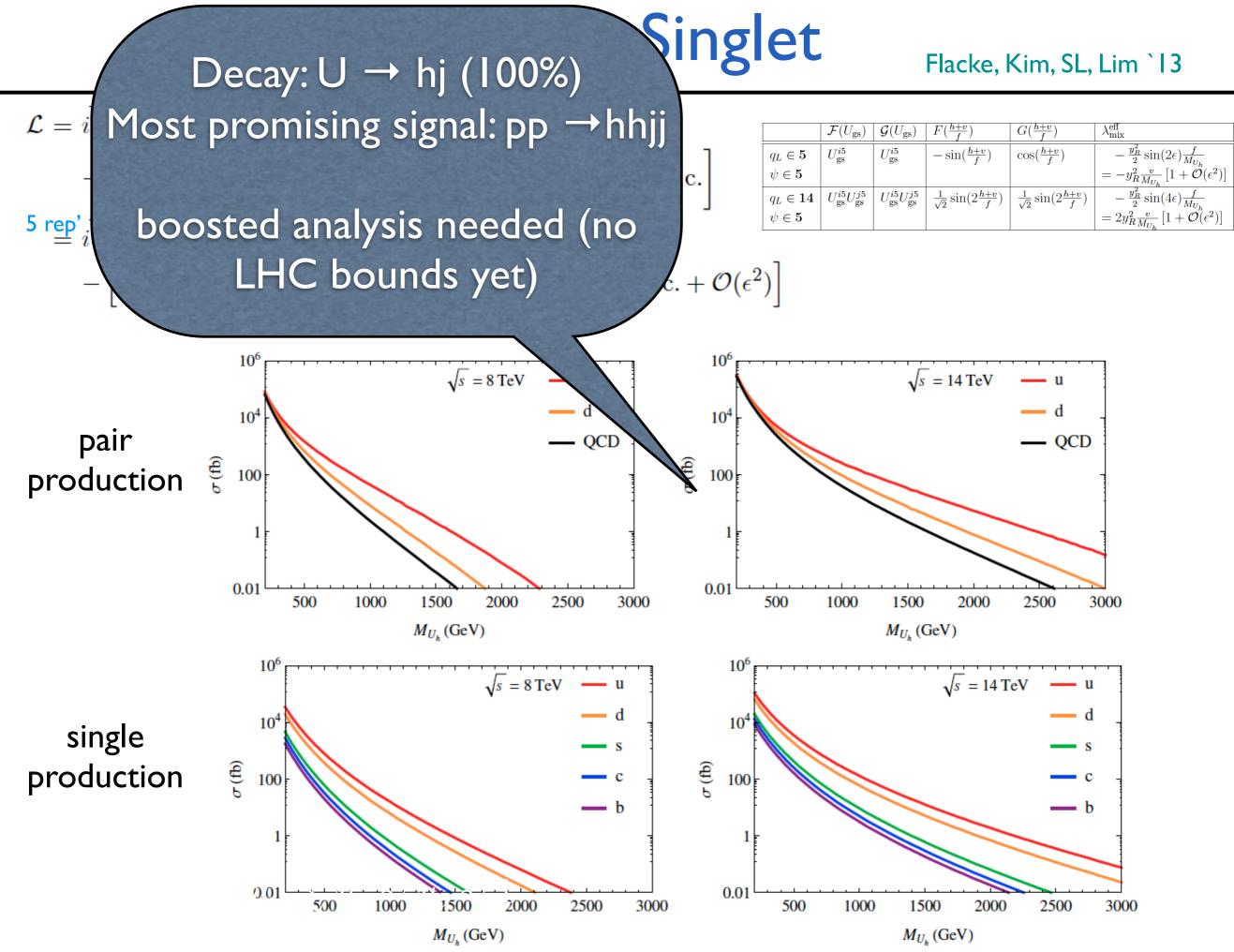


Partners in Singlet

Flacke, Kim, SL, Lim `I 3



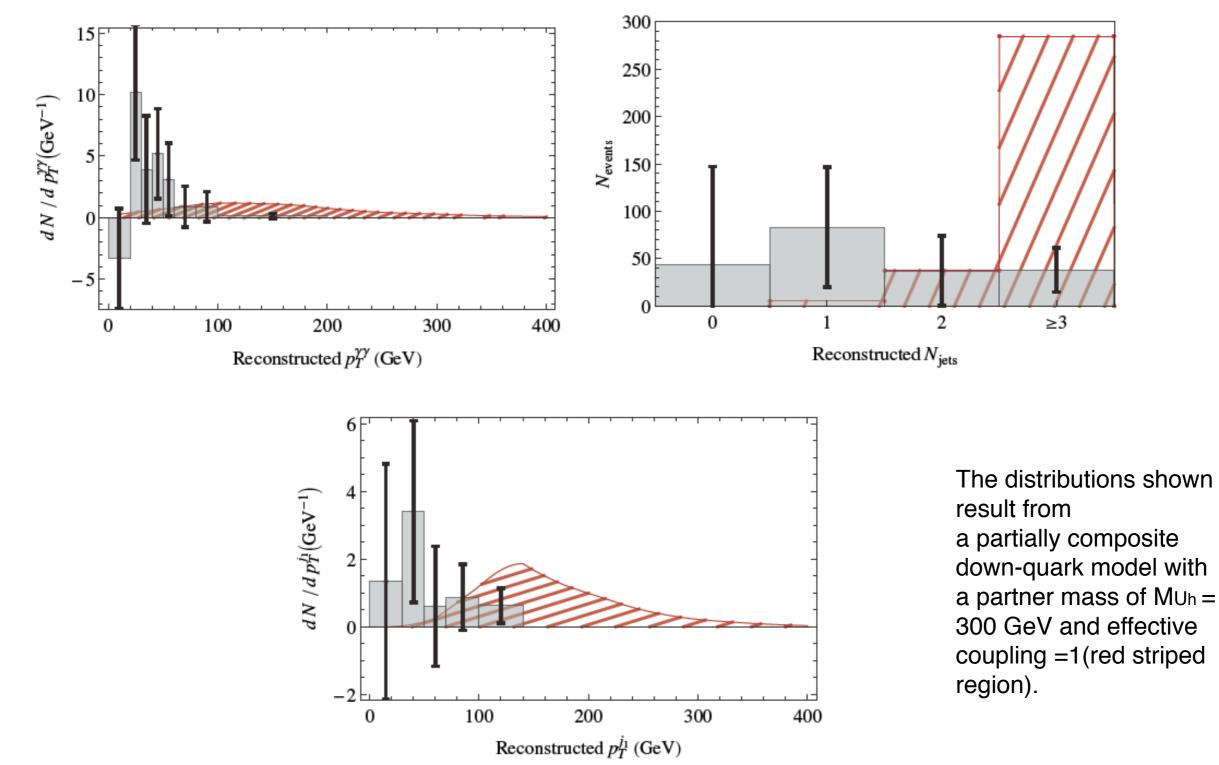




Partners in Singlet

LHC bounds comes mostly from $h \rightarrow \gamma \gamma$ Atlas-Conf-2013-072

Look for a deviations in pp \rightarrow h(hjj) $\rightarrow \gamma \gamma X$ or bbX i.e. modifications to SM Higgs signals and their angular and p_T distributions

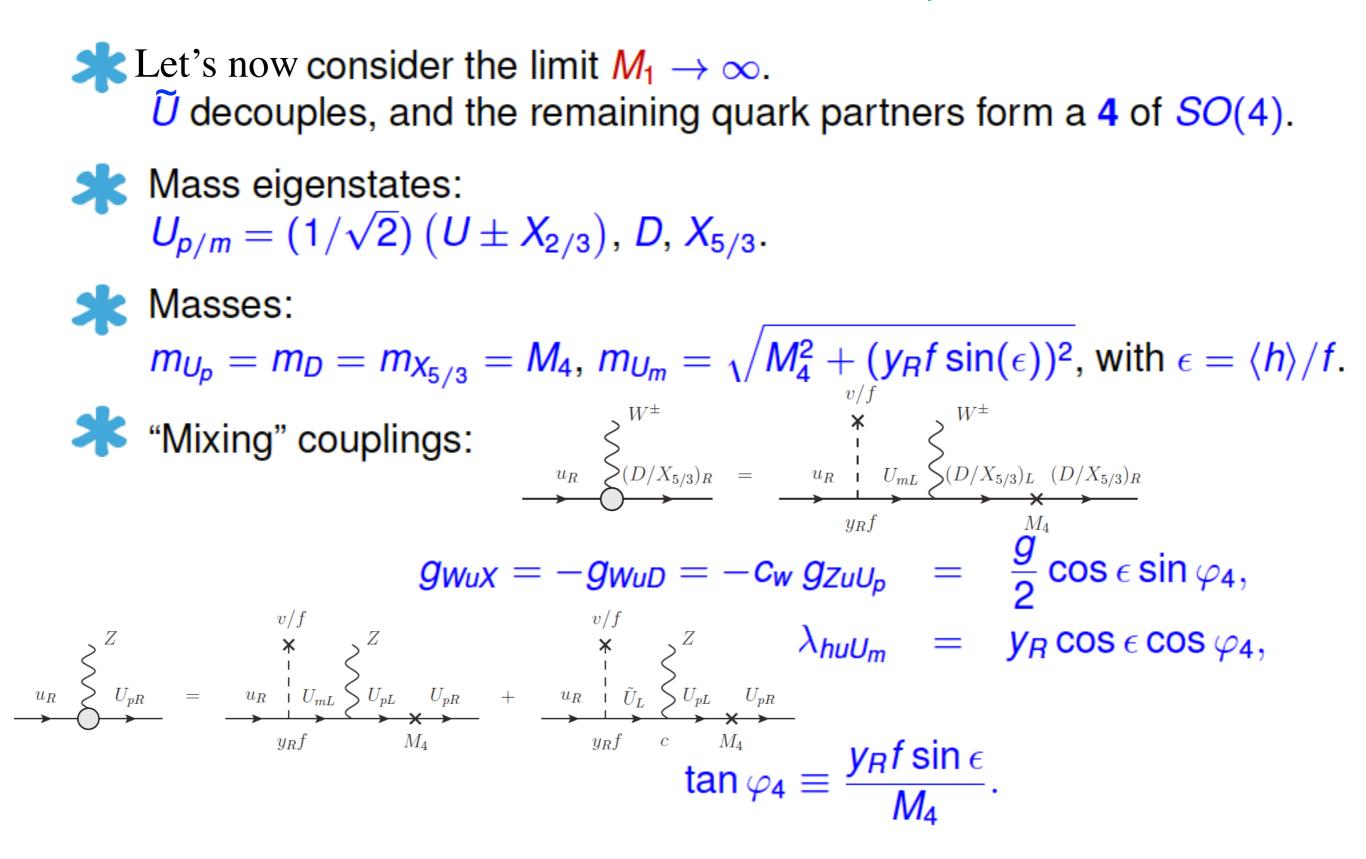


Partners in Singlet Flacke, Kim, SL, Lim `13 LHC bounds comes from QCD pair production: fully composite: $M_{U_h} \gtrsim 212 \text{ GeV}$ partially composite: $M_{U_h} \gtrsim 310 \text{ GeV}$ LHC bounds for single production (partially composite): overflow bean is used does not provide a unfolding correction factor 6 6 A^{eff} A^{eff} 2 2 --- $\Gamma/M_{U_{h}} = 1/3$ --- $\Gamma/M_{U_{h}} = 1/3$ 500 1000 1500 2000 500 1000 1500 2000 M_{U_h} (GeV)

 M_{U_h} (GeV)

Partners in 4-plet

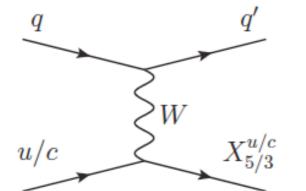
Delaunay, Fraille, Flacke, SL, Panico, Perez `13

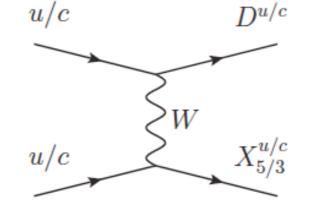


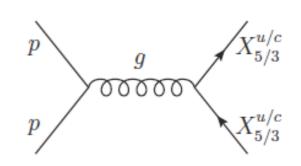
Partners in 4-plet

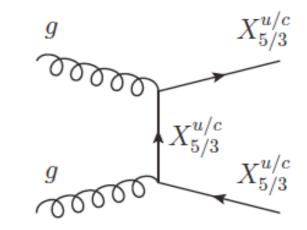
Delaunay, Fraille, Flacke, SL, Panico, Perez `13

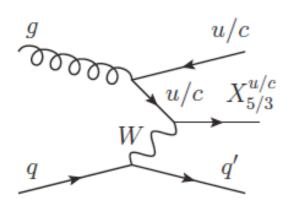
Production mechanisms (shown here: $X_{5/3}$ production)











(a) EW single production

Recays:

- $X_{5/3} \rightarrow W^+ u$ (100%),
- $D \rightarrow W^- u$ (100%),
- $U_p \to Zu$ (100%),
- $U_m \rightarrow hu$ (100%).

(b) EW pair production

Single production: Wjj, Zjj [D0 Collaboration], Phys. Rev. Lett. 106, 081801 (2011) [CDF Collaboration], CDF/PUB/ EXOTIC/PUBLIC/1026 [ATLAS Collaboration], ATLAS-CONF-2012-137 (4.64 fb⁻¹ 7 TeV) [CMS Collaboration],CMS-PAS-EXO-12-024 (19.8 fb⁻¹ 8 TeV)

(c) QCD pair production

Pair production: WWjj, ZZjj, hhjj [D0 Collaboration], Phys. Rev. Lett. 107, 082001

(2011)

[CDF Collaboration], Phys. Rev. Lett. 107, 261801 (2011)

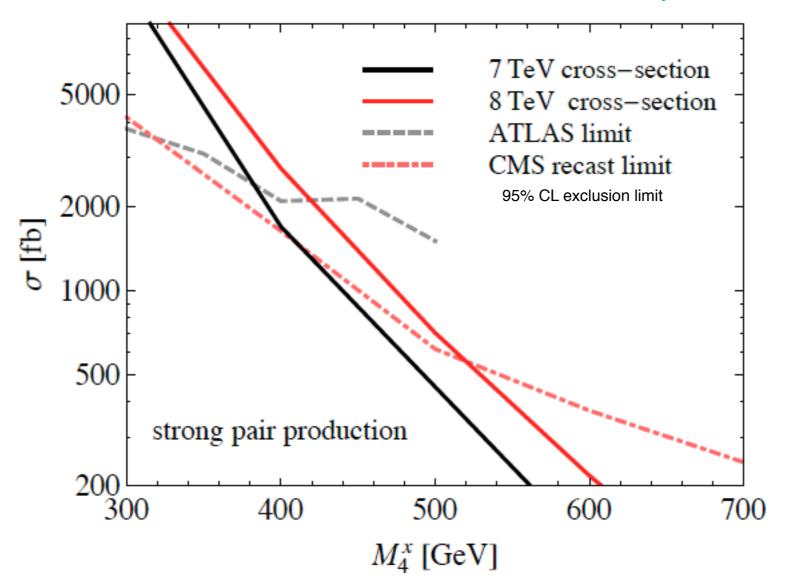
[ATLAS Collaboration], Phys. Rev. D 86, 012007 (2012) (1.04 fb ⁻¹ 7 TeV)

[CMS Collaboration], CMS-PAS-EXO-12-042 (19.6

fb⁻¹ 8 TeV); Leptoquark search, final state: μμjj)

Bounds on u/c partner from 7TeV LHC

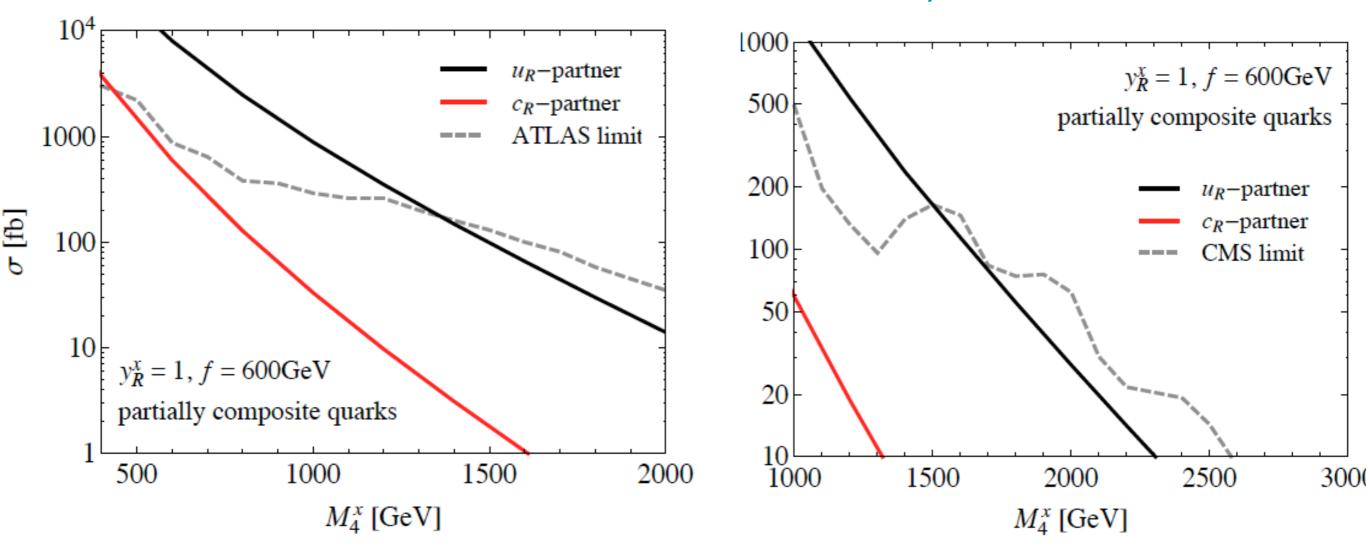
Delaunay, Fraille, Flacke, SL, Panico, Perez `13



Model Independent predictions for WWjj cross sections through QCD pair production of -1/3 and 5/3 charge partners of the composite right-handed up and charm quarks. The solid black (red) line stands for the 7TeV (8TeV) cross section. They are the same for the first two generations and in both partially and fully quark scenarios.

Bounds on u/c partner from 7TeV LHC

Delaunay, Fraille, Flacke, SL, Panico, Perez `13

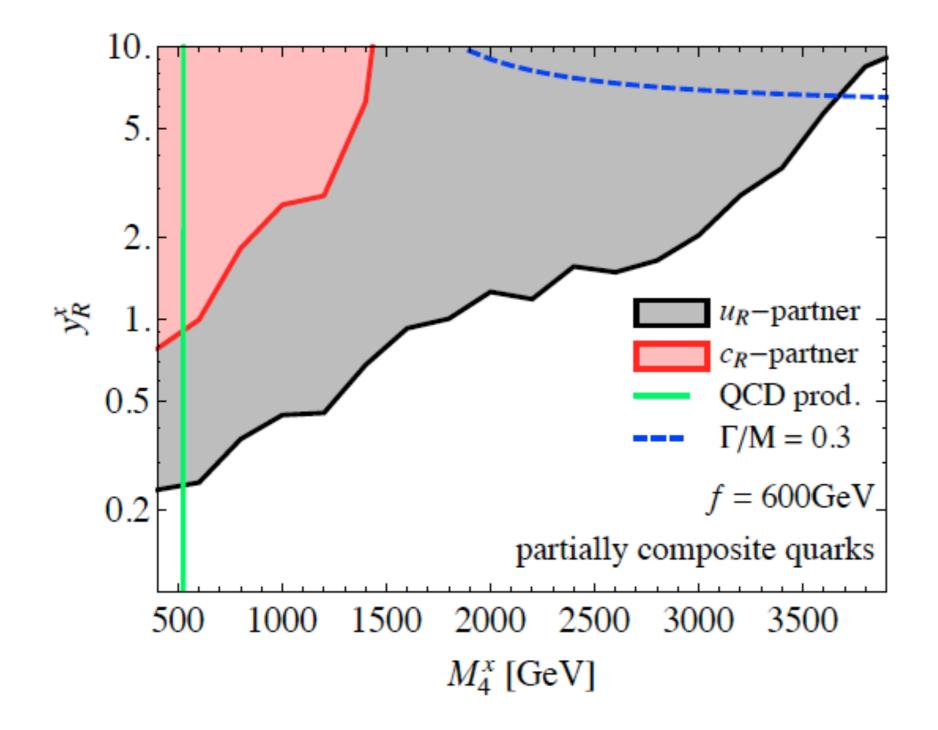


Predictions for Wjj cross sections of function of the fourplet partner mass $M_{4^{x}}$, x = u, c, in the partially composite right-handed for two generation quarks. dashed curve is the 95% CL exclusion limit from the ATLAS and CMS searches at the 7TeV LHC run

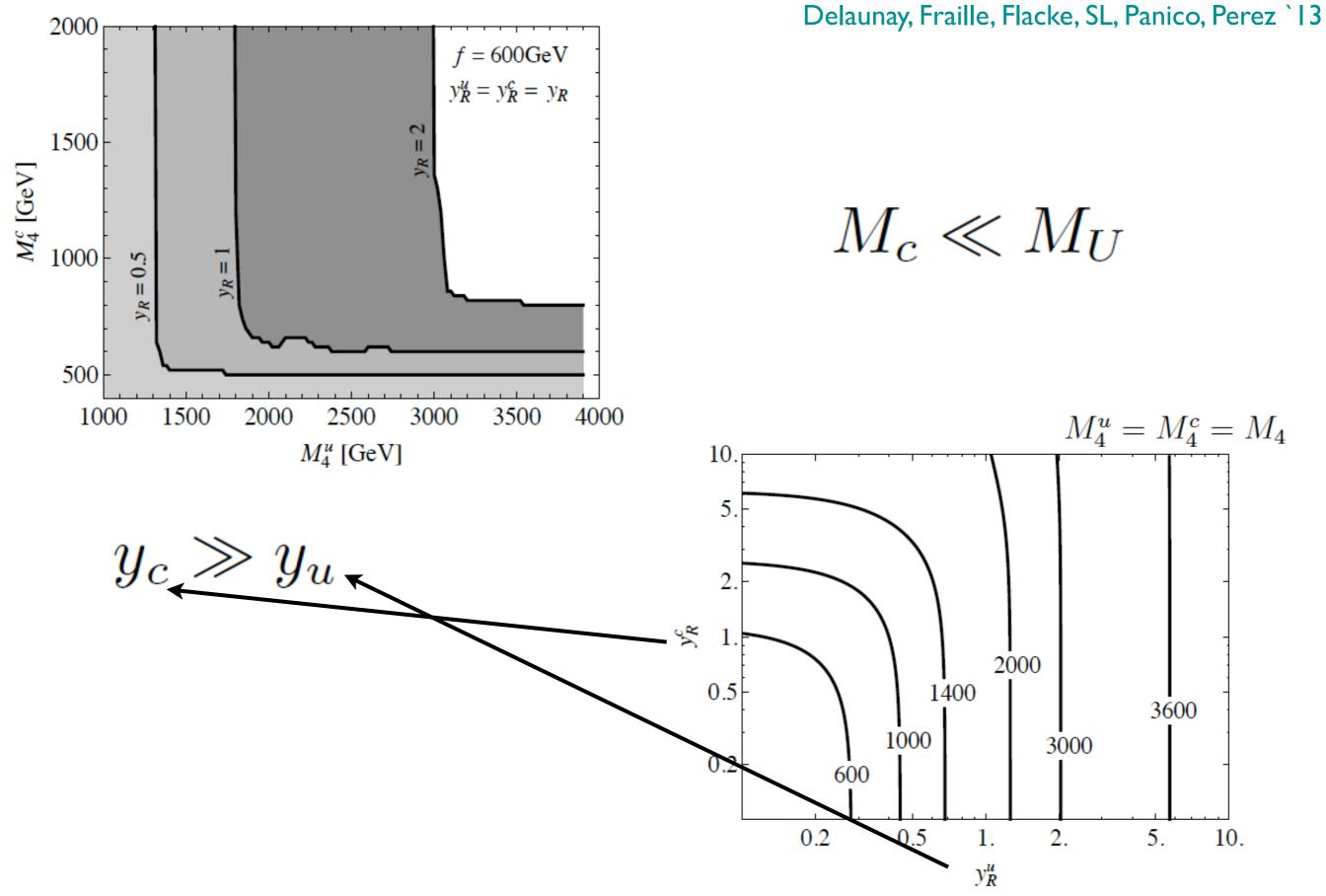
Partners in 4-plet

Delaunay, Fraille, Flacke, SL, Panico, Perez `13

95% CL exclusion limits



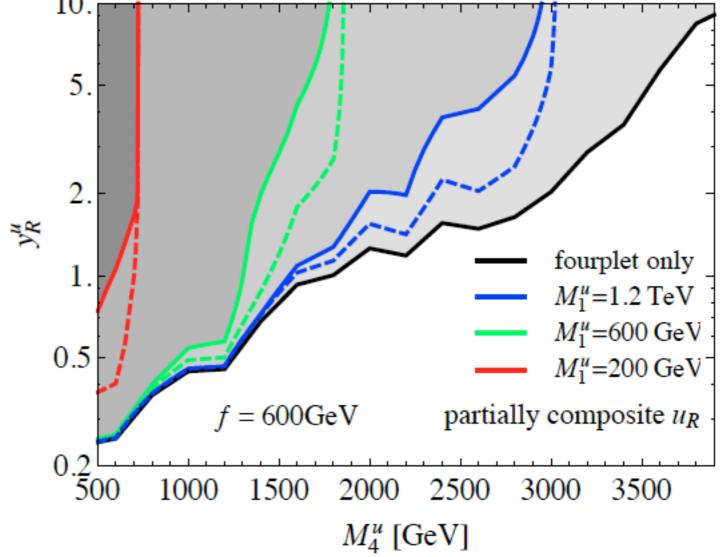
Collider implications for split 2 generations (similar to SUSY case)



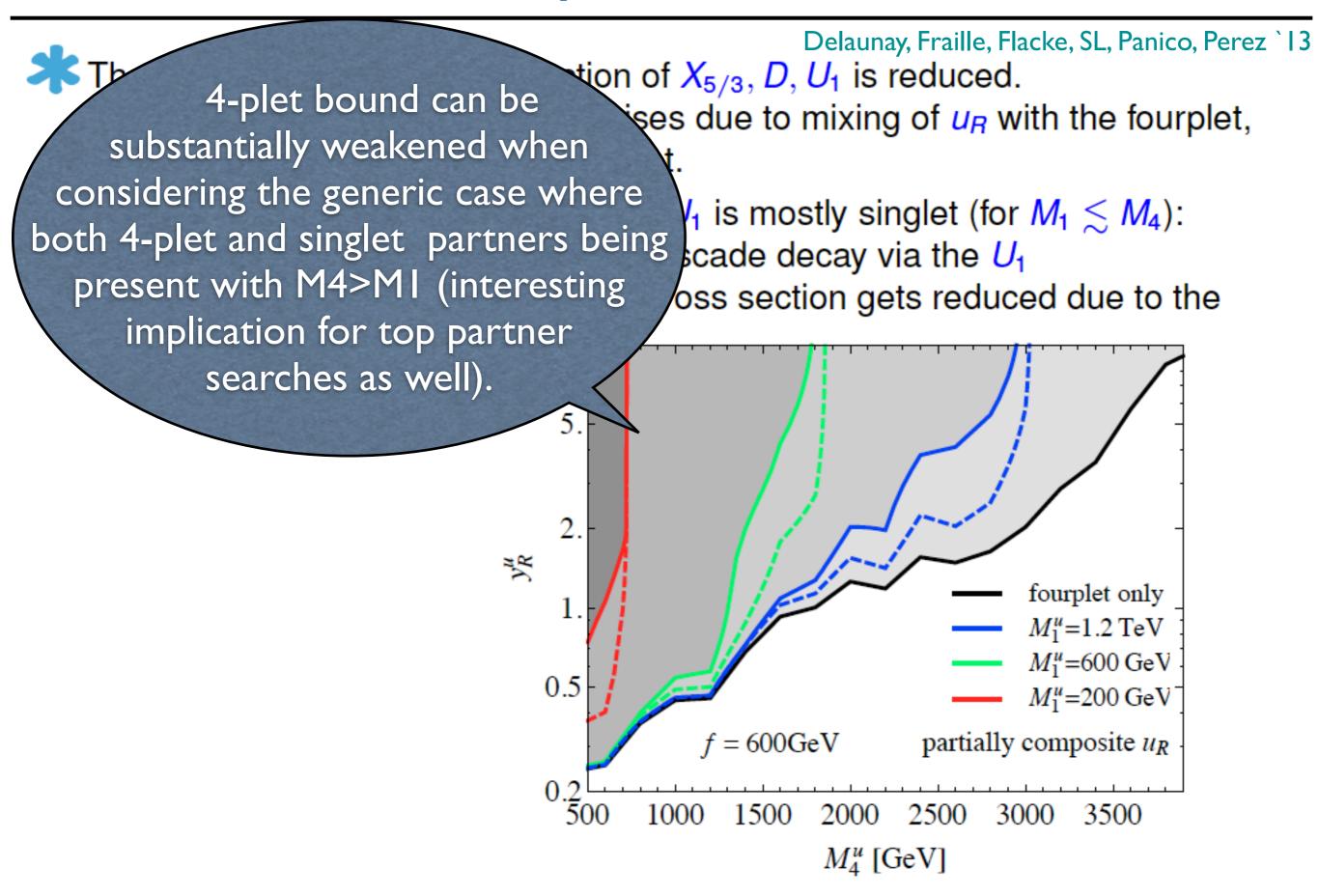
General 5-plet case: 4 + 1

- Delaunay, Fraille, Flacke, SL, Panico, Perez `13 The single-production cross section of $X_{5/3}$, D, U_1 is reduced. Physical reason: The production arises due to mixing of u_R with the fourplet, but now, u_R also mixes with the singlet.
- If the lighter up-type mass eigenstate U_1 is mostly singlet (for $M_1 \leq M_4$): Fourplet states U_p , D, $X_{5/3}$ can also cascade decay via the U_1

 \rightarrow The previously considered signal cross section gets reduced due to the BR into cascade decays. 10.



General 5-plet case: 4 + 1



Indirect constraints from dijet production Strong dynamics

Delaunay, Fraille, Flacke, SL, Panico, Perez `13

* new physics dijet sources are generically induced by unknown physics at the cut-off scale $\Lambda \sim 4\pi f$.

$$\frac{1}{2f^2} \left[(\bar{Q}\gamma_\mu Q)^2 + (\bar{\tilde{U}}\gamma_\mu \tilde{U})^2 + (\bar{u}_R\gamma_\mu u_R)^2 \right]$$

In the presence of mixings between the chiral quarks and the vector-like heavy resonances

$$\mathcal{L}_{4f} = \frac{c_{uu}}{2} \left(\bar{u}_R^{SM} \gamma_\mu u_R^{SM} \right)^2 + \frac{c_{cc}}{2} \left(\bar{c}_R^{SM} \gamma_\mu c_R^{SM} \right)^2 + c_{uc} \left(\bar{u}_R^{SM} \gamma^\mu u_R^{SM} \right) \left(\bar{c}_R^{SM} \gamma_\mu c_R^{SM} \right)$$

$$\chi_j \equiv e^{2y_j} \qquad \text{uniform for QCD background, while it's peacked}$$

$$|c_{qq}|^{-1/2} \gtrsim 2.2 \text{ TeV} \qquad \text{for} \qquad c_{qq} > 0 \qquad \text{from ATLAS}$$

$$|c_{qq}|^{-1/2} \gtrsim 2.1 (3.0) \text{ TeV} \qquad \text{for} \qquad c_{qq} > 0 \qquad \text{from CMS}$$

Indirect constraints from dijet production Strong dynamics

Fraille, Flacke, SL, Panico, Perez `13

* new physic
unknown
Neither ATLAS nor CMS has looked at this:
require it does not deviate
from SM expectations more than in the presence of

$$c_{qq}/2 \times (\bar{q}_L^{SM} \gamma_\mu q_L^{SM})^2$$
, with $|c_{qq}|^{-1/2} = 3 \text{ TeV}$
=> indirect bound is not strong, smaller than
direct bound!
 $\mathcal{L}_{4f} = \frac{c_{uu}}{2} (\bar{u}_R^{SM} \gamma_\mu q_L^{SM}) + (\bar{c}_R^{SM} \gamma_\mu c_R^{SM})$
 $\chi_j \equiv e^{2y_j}$ uniform for $c_{pq} > 0$ from ATLAS
 $|c_{qq}|^{-1/2} \gtrsim 2.1 (3.0) \text{ TeV}$ for $c_{qq} > 0$ from CMS

Summary

Composite Higgs model (with H as PGB) provides a viable solution to the hierarchy problem and generically predict partner states to the fermions

The phenomenology of composite light quarks differs from top partner phenomenology

Bound on charm partners is much weaker than that of up and top partners (charm tagging may help probing charm partners) => Flavorful Naturalness

Content of the second s

* Work in progress: Flavor physics and EWPT

Da Rold, Flacke, SL, Perez, Soreq, Weiler

Delaunay, Flacke, Han, Kim, SL

Backup Slide

Coleman, Wess, Zumino 69, Callan, Coleman 69

* a prescription on how to express low energy L_{eff} for theories with SSB (G/H)

classified all possible nonlinear transformation laws of fields in a neighborhood of the VEV

 \Rightarrow every element of G can be expressed as $e^{\pi^{\hat{a}}T^{\hat{a}}}h'$

unbroken element of H

broken generator of G

=> for any group element g of G, we can write $g e^{\pi^{\hat{a}}T^{\hat{a}}} = e^{\pi'^{\hat{a}}T^{\hat{a}}}h$

with $\pi'^{\hat{a}}$ and $h \in H$

Н

* with a field redefinition, one can find a "standard parametrization" $(\pi^{\hat{a}}, \psi^{i})$ with the transformation law under $g \in G$

$$\pi^{\hat{a}} \to \pi'^{\hat{a}}, \qquad \psi^{i} \to D(h)^{i}_{j} \psi^{j}$$

linear representation of

Coleman, Wess, Zumino 69, Callan, Coleman 69 \gtrsim a prescription on how to express low energy L_{eff} for theories with SSB (G/H) * classified all possible nonlinear transformation laws of fields in a neighborhood of the VEV broken generator of G * every element of G can be expressed as

span all possible nonlinear realizations of the group G: CCWZ classified all Ginvariant Lagrangians constructed out of them (and their derivatives) with a field redefinition parametrization" $(\pi^{\hat{a}}, \psi^{i})$ with the transformation law under $g \in G$

$$\pi^{\hat{a}} \to \pi'^{\hat{a}}, \qquad \psi^{i} \to D(h)^{i}_{j} \psi^{j}$$

linear representation of H

CCWZ

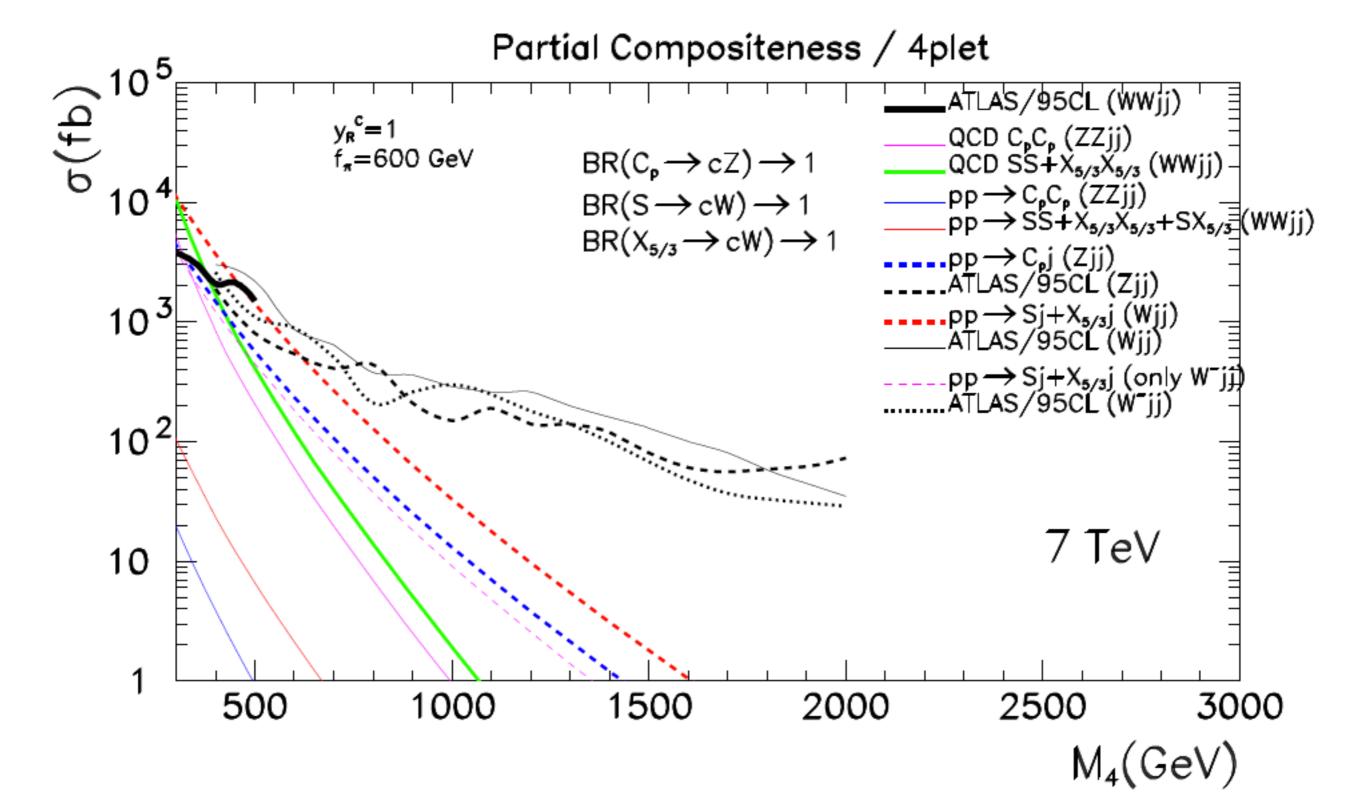
Standard form of derivatives can be given in terms of d and e symbol: $U^{-1}\partial_{\mu}U = d^{\hat{a}}_{\mu}T^{\hat{a}} + e^{a}_{\mu}T^{a} \qquad \qquad U \equiv \exp(\pi^{\hat{a}}T^{\hat{a}})$ unbroken generator generalized to continuous G transformation: $U^{-1}(\partial_{\mu} - A_{\mu})U = d^{\hat{a}}_{\mu}T^{\hat{a}} + e^{a}_{\mu}T^{a}$ $A_{\mu} = A^{\hat{a}}_{\mu}T^{\hat{a}} + A^{a}_{\mu}T^{a}$ and $\nabla_{\mu}\psi^{i} \equiv \partial_{\mu}\psi^{i} + e^{a}_{\mu}\rho(T^{a})^{i}_{j}\psi^{j}$ such that $\nabla_{\mu}\psi^{i} \rightarrow D(h)^{i}_{j}\nabla_{\mu}\psi^{j}$ **Constructed** out of $(\pi^{\hat{a}}, \psi^{i})$, and their derivatives is equivalent to the one constructed out of $U, \psi^i, d_\mu, and \nabla_\mu \psi^i$ For example, in SO(5)/SO(4), $e_{\mu}^{1,2} = -\cos^2\left(\frac{h}{2f}\right)gW_{\mu}^{1,2}, \quad e_{\mu}^3 = -\cos^2\left(\frac{h}{2f}\right)gW_{\mu}^3 - \sin^2\left(\frac{h}{2f}\right)g'B_{\mu}$ $e^{4,5}_{\mu} = -\sin^2\left(\frac{h}{2f}\right)gW^{1,2}_{\mu}, \quad e^6_{\mu} = -\cos^2\left(\frac{h}{2f}\right)g'B_{\mu} - \sin^2\left(\frac{h}{2f}\right)gW^3_{\mu}$ TT712TT73 6 ID

$$d_{\mu}^{1,2} = -\sin(\bar{h}/f)\frac{gW_{\mu}^{1,2}}{\sqrt{2}}, \quad d_{\mu}^{3} = \sin(\bar{h}/f)\frac{gB_{\mu} - gW_{\mu}^{3}}{\sqrt{2}}, \quad d_{\mu}^{4} = \frac{\sqrt{2}}{f}\partial_{\mu}h$$

Friday, January 24, 2014

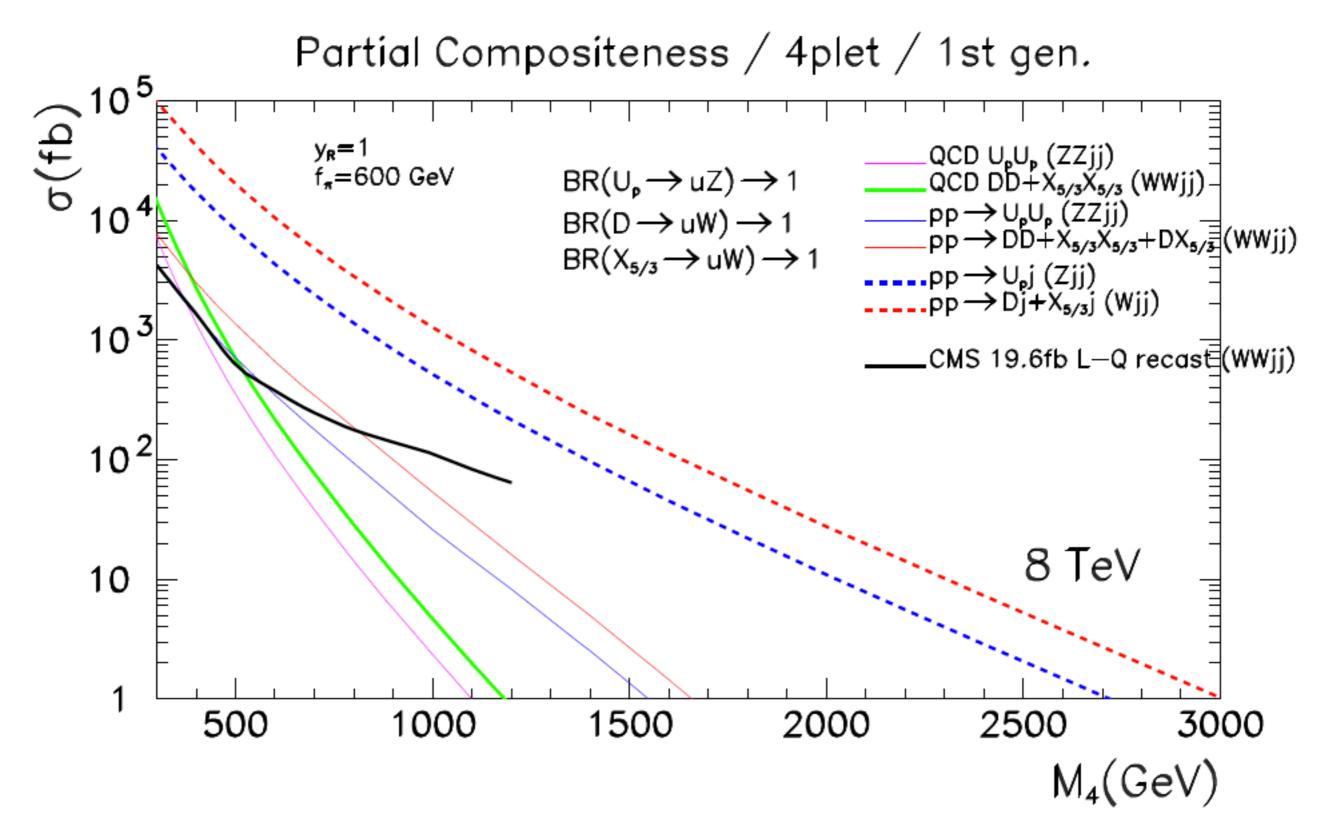
Bounds on c partner from 7TeV LHC

experimental bounds: Wjj, Zjj with 4.64 fb⁻¹ [ATLAS-CONF-2012-137], WWjj, ZZjj with 1.04 fb⁻¹ [ATLAS PRD 86, 012007 (2012)]



Bounds on u/c partner from 8TeV LHC

experimental bounds: scalar leptoquark search (final state: $\mu^+\mu^-jj$) with 19.6 fb⁻¹ [CMS-PAS-EXO-12-042]



Fermion Lagrangian (with both up and down sector combined)

$$\mathcal{L} = \mathcal{L}_{comp} + \mathcal{L}_{el} + \mathcal{L}_{mix},$$

with

$$\begin{aligned} \mathcal{L}_{comp} &= i \ \overline{Q^{u}}(D_{\mu} + ie_{\mu})\gamma^{\mu}Q^{u} + i \ \overline{Q^{d}}(D_{\mu} + ie_{\mu})\gamma^{\mu}Q^{d} + i \widetilde{U} \not\!\!D \widetilde{U} + i \widetilde{D} \not\!\!D \widetilde{D} \\ &- M_{4}^{u} \overline{Q^{u}}Q^{u} - M_{4}^{d} \overline{Q^{d}}Q^{d} - M_{1}^{u} \widetilde{U} \widetilde{U} - M_{1}^{d} \overline{D} \widetilde{D} \\ &+ \left(i c^{u} \overline{Q^{u}}^{i} \gamma^{\mu} d_{\mu}^{i} \widetilde{U} + i c^{d} \overline{Q^{d}}^{i} \gamma^{\mu} d_{\mu}^{i} \widetilde{D} + \text{h.c.} \right), \\ \mathcal{L}_{el} &= i \ \overline{q}_{L} \not\!\!D q_{L} + i \ \overline{u}_{R} \not\!\!D u_{R} + i \ \overline{d}_{R} \not\!\!D d_{R} \\ \mathcal{L}_{mix} &= -y_{L}^{u} f \overline{q}_{L1}^{5} U_{gs} \psi_{R}^{u} - y_{L}^{d} f \overline{q}_{L2}^{5} U_{gs} \psi_{R}^{d} - y_{R}^{u} f \overline{u}_{R}^{5} U_{gs} \psi_{L}^{u} - y_{R}^{d} f \overline{d}_{R}^{5} U_{gs} \psi_{L}^{d} + \text{h.c.} \end{aligned}$$

			SO(5)	SO(4)	$SU(2)_L$	$SU(2)_R$	$U(1)_X$	$U(1)_Y$	$U(1)_{em}$
q_{L1}^{5}			5′	4'	2	2'	2/3	1/6	
		u_L					2/3	1/6	2/3
		d_L					2/3	1/6	-1/3
q_{L2}^{5}			5'	4'	2	2'	-1/3	1/6	
		u_L					-1/3	1/6	2/3
		d_L					-1/3	1/6	-1/3
u_R			5'	1	-	-	2/3	2/3	2/3
d_R			5'	1	-	-	-1/3	-1/3	-1/3
ψ^U	~		5				2/3		
	\tilde{U}			1	-	-	2/3	2/3	2/3
	Q^u			4			2/3		
		U^{u}					2/3	1/6	2/3
		D^u					2/3	1/6	-1/3
		$X^{u}_{5/3}$					2/3	7/6	5/3
		$X_{2/3}^{u}$					2/3	7/6	2/3
ψ^D		-	5				-1/3		
	$\begin{array}{c} \tilde{D} \\ Q^d \end{array}$			1	-	-	-1/3	-1/3	-1/3
	Q^d			4			-1/3		
		$X^{d}_{-1/3}$					-1/3	-5/6	-1/3
		$X^{d}_{-1/3} \\ X^{d}_{-4/3} \\ U^{d}$					-1/3	-5/6	$-1/3 \\ -4/3 \\ 2/3$
		$U^{\tilde{d}}$					-1/3	1/6	2/3
		D^d					-1/3	1/6	-1/3