

Towards the measurements of mass hierarchy and CP violation in neutrino oscillations

*Frontiers in Particle Physics:
From Dark Matter to the LHC and Beyond*

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Contents

- Current knowledge of neutrino oscillations
- Mass hierarchy determination
- Measurement of the CP phase
- Summary

Neutrino oscillations

(two flavors)

- Two parameters:

$$U = \begin{pmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{pmatrix}$$

Evidence for massive neutrinos!

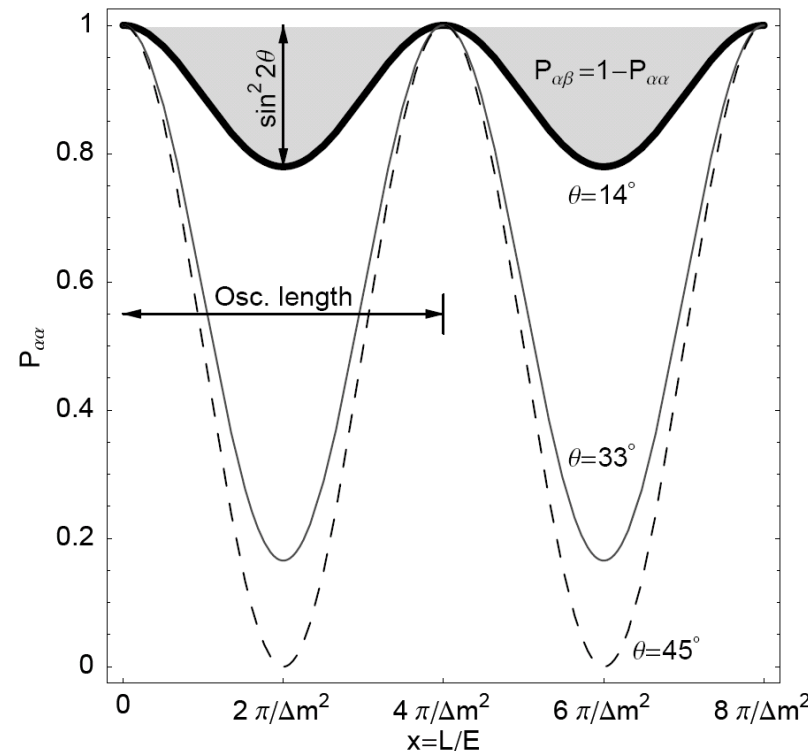
$$\Delta m^2 \equiv m_2^2 - m_1^2$$

- Disappearance or survival probability**

$$P_{\alpha\alpha} = 1 - \sin^2 2\theta \sin^2 \left(\frac{\Delta m^2 L}{4E} \right)$$

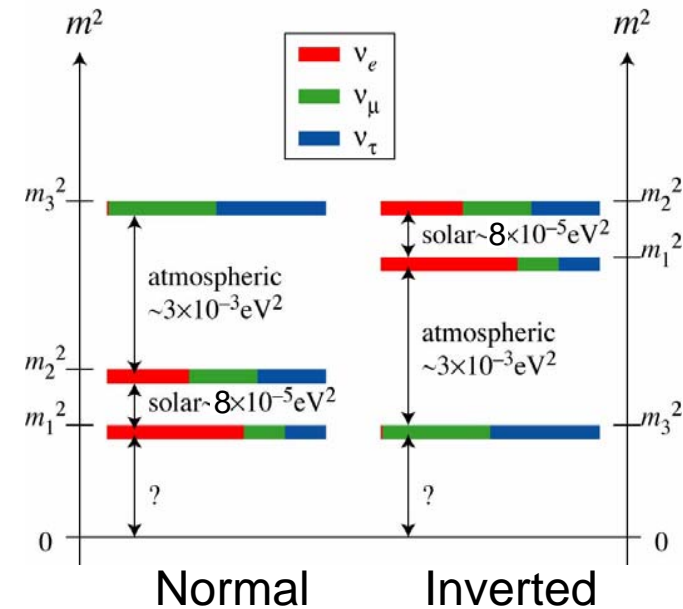
Appearance probability

$$P_{\alpha\beta} = \sin^2 2\theta \sin^2 \left(\frac{\Delta m^2 L}{4E} \right)$$



Three flavors: Masses and mixings

- Two independent mass squared splittings, typically
 - Δm_{21}^2 (solar)
 - Δm_{31}^2 (atmospheric)
- Mixing: Use same parameterization as for CKM matrix (4 params)



$$(s_{ij} = \sin \theta_{ij} \quad c_{ij} = \cos \theta_{ij})$$

Potential CP violation $\sim \theta_{13}$

$$U_{\text{PMNS}} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} c_{13} & 0 & s_{13} e^{-i\delta} \\ 0 & 1 & 0 \\ -s_{13} e^{i\delta} & 0 & c_{13} \end{pmatrix} \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix}.$$

Kirk T McDonald
Princeton U
(April 24, 2012)

on behalf of the Daya Bay Collaboration

$$P_{\bar{e}\bar{e}} \simeq 1 - \sin^2(2\theta_{13}) \sin^2 \Delta_{31}$$

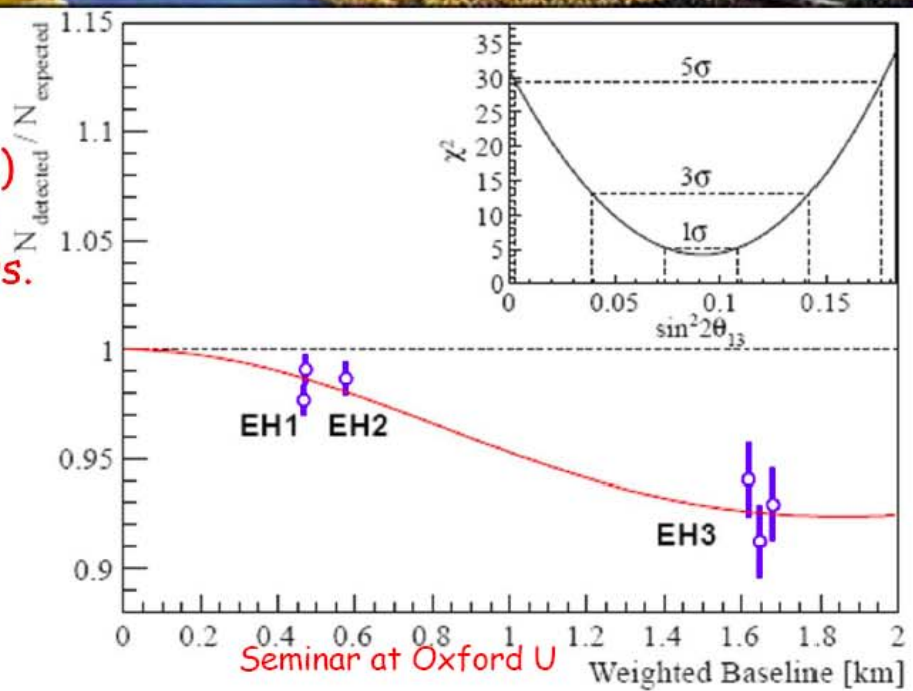
(short distance)



We observe that
 $\sin^2 2\theta_{13} = 0.092 \pm 0.016$ (stat.) ± 0.005 (syst.)
after 55 days of operation with 6 detectors
at 3 sites close to 3 pairs of ~ 3 GW reactors.

F.P. Ahn *et al.*
Phys. Rev. Lett. **108**, 171803 (2012).

(also: T2K, Double Chooz, RENO)

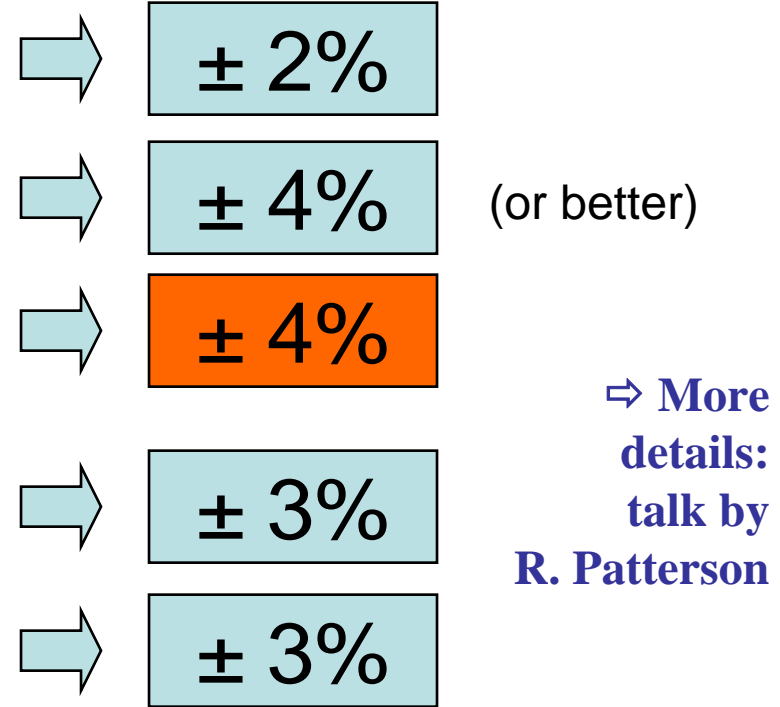


Precision of parameters?

Gonzalez-Garcia, Maltoni, Salvado, Schwetz, JHEP 1212 (2012) 123

NuFIT 1.2 (2013)

	bf μ $\pm 1\sigma$	3σ range
$\sin^2 \theta_{12}$	$0.306^{+0.012}_{-0.012}$	0.271 \rightarrow 0.346
$\theta_{12}/^\circ$	$33.57^{+0.77}_{-0.75}$	31.38 \rightarrow 36.01
$\sin^2 \theta_{23}$	$0.446^{+0.007}_{-0.007} \oplus 0.587^{+0.032}_{-0.037}$	0.366 \rightarrow 0.663
$\theta_{23}/^\circ$	$41.9^{+0.4}_{-0.4} \oplus 50.0^{+1.9}_{-2.2}$	37.2 \rightarrow 54.5
$\sin^2 \theta_{13}$	$0.0229^{+0.0020}_{-0.0019}$	0.0170 \rightarrow 0.0288
$\theta_{13}/^\circ$	$8.71^{+0.37}_{-0.38}$	7.50 \rightarrow 9.78
$\delta_{CP}/^\circ$	265^{+56}_{-61}	0 \rightarrow 360
$\frac{\Delta m_{21}^2}{10^{-5} \text{ eV}^2}$	$7.45^{+0.19}_{-0.16}$	6.98 \rightarrow 8.05
$\frac{\Delta m_{31}^2}{10^{-3} \text{ eV}^2}$ (N)	$+2.417^{+0.013}_{-0.013}$	+2.247 \rightarrow +2.623
$\frac{\Delta m_{32}^2}{10^{-3} \text{ eV}^2}$ (I)	$-2.410^{+0.062}_{-0.062}$	-2.602 \rightarrow -2.226



\Rightarrow More details:
talk by
R. Patterson

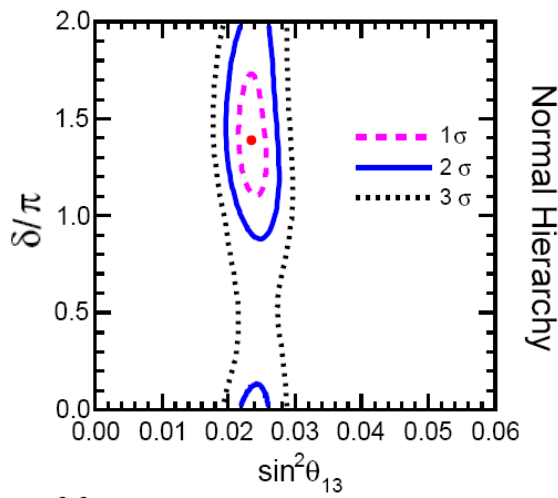
Open issues:

- Degeneracies (mass ordering, octant)
- CP phase

Age of the precision flavor physics of the lepton sector

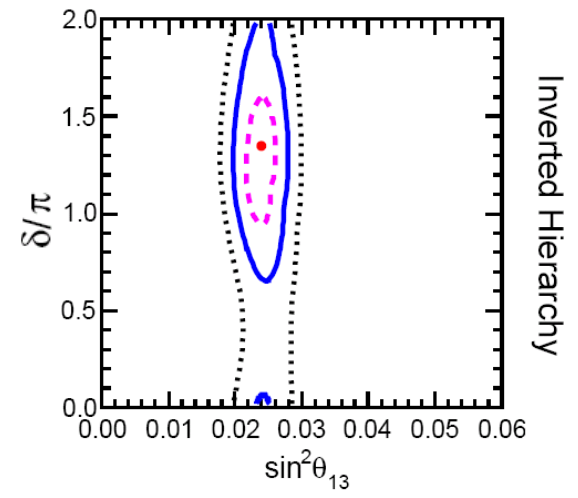
Latest fits vs. projection

- Indication for δ_{CP} , no evidence for mass hierarchy

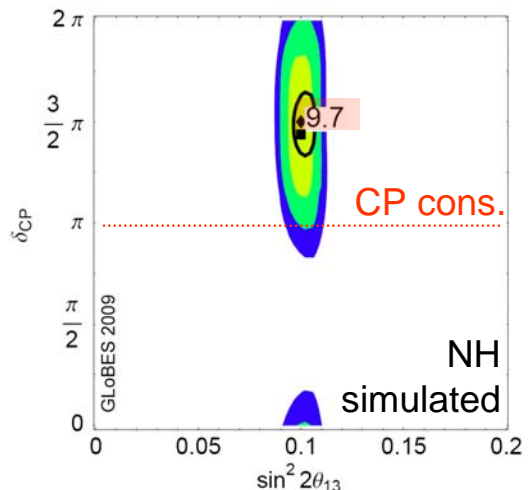


LBL Acc + Solar + KL
+ SBL Reactors
+ SK Atm

Capozzi, Fogli,
Lisi, Marrone,
Montanino, Palazzo,
arXiv:1312.2878



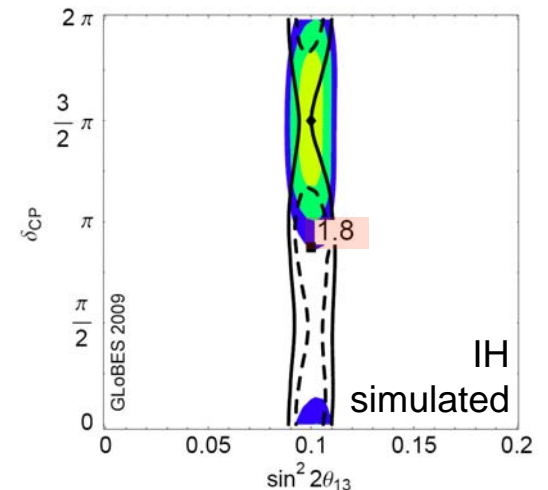
- Potential of existing equipment



T2K, NOvA,
Double Chooz, Daya Bay;
5 years each

High CL determination
requires new equipment

Huber, Lindner, Schwetz, Winter,
JHEP 0911 (2009) 044



Short-distance anomalies

... unresolved 2.0

$$\Delta m_{41}^2 L / (4E)$$

Example: $P_{ee} = 1 - 4|U_{e4}|^2(1 - |U_{e4}|^2) \sin^2 \Delta_{41}$, ?

3+1 scenario

$$P_{\mu\mu} = 1 - 4|U_{\mu4}|^2(1 - |U_{\mu4}|^2) \sin^2 \Delta_{41}$$
, 👎

$$P_{e\mu} = P_{\mu e} = 4|U_{e4}|^2|U_{\mu4}|^2 \sin^2 \Delta_{41}$$
, ⇒ MiniBooNE 👍

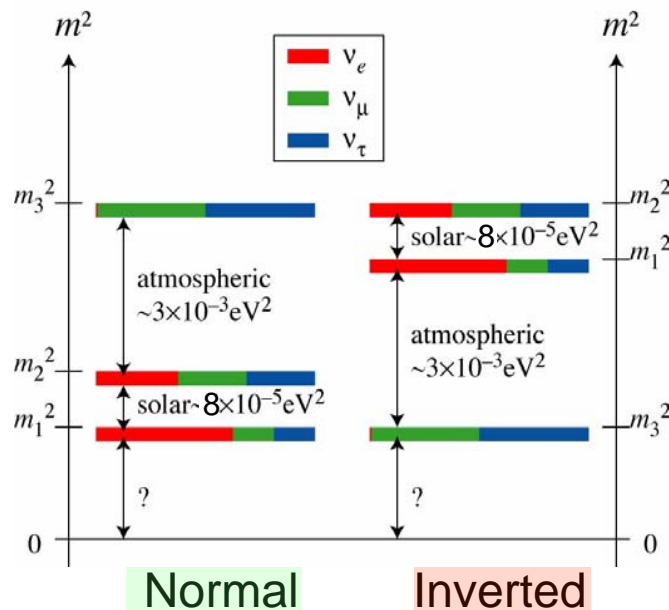
- Well known tension between appearance and disapp. data (appearance ⇒ disapp. in both channels)
- Need one or more new experiments which can test
 - ν_e disappearance (Gallium, reactor anomalies)
 - ν_μ disappearance (overconstrains 3+N frameworks)
 - ν_e - ν_μ oscillations (LSND, MiniBooNE)
 - Neutrinos and antineutrinos separately (CP violation? Gallium vs reactor?)
- Summary of options: Appendix of white paper [arXiv:1204.5379](https://arxiv.org/abs/1204.5379)
- Example: completely self-consistent test at **ν STORM - Neutrinos from STORed Muons**



Mass hierarchy determination

The background of the slide features a large, faint watermark of the University of Cambridge seal. The seal is circular and contains the Latin motto 'HABitu MENSURANDU' at the top and 'ANNO DOMINI MDCCLXV' at the bottom. The central part of the seal depicts a seated figure holding a book and a staff, with a shield below. The shield is divided into four quadrants with various symbols, including a cross and a chevron. The seal is rendered in a light gray color.

Why would one like to measure the mass hierarchy?



- Mass hierarchy is a good model discriminator (Albright, Chen, 2006)
- **Leading indicator for flavor model?** [determines structure of couplings in hierarchical models]

Reference	Hierarchy
Anarchy Model:	
dGM [18]	Either
$L_e - L_\mu - L_\tau$ Models:	
BM [35]	Inverted
BCM [36]	Inverted
GMN1 [37]	Inverted
GL [38]	Inverted
PR [39]	Inverted
S_3 and S_4 Models:	
CFM [40]	Normal
HLM [41]	Normal
KMM [42]	Inverted
MN [43]	Normal
MNY [44]	Normal
MPR [45]	Normal
RS [46]	Inverted
TY [47]	Inverted
T [48]	Normal
A_4 Tetrahedral Models:	
ABGMP [49]	Normal
AKKL [50]	Normal
Ma [51]	Normal
$SO(3)$ Models:	
M [52]	Normal
Texture Zero Models:	
CPP [53]	Normal
	Inverted
	Inverted
WY [54]	Either
	Either
	Either

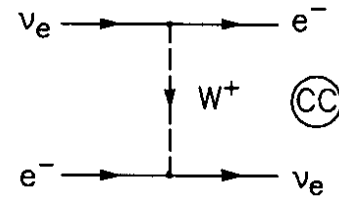
Parameter mapping

... for two flavors, constant matter density

■ Oscillation probabilities in

vacuum: $P_{\alpha\alpha} = 1 - \sin^2 2\theta \sin^2 \frac{\Delta m^2 L}{4E}$

matter: $P_{\alpha\alpha} = 1 - \sin^2 2\tilde{\theta} \sin^2 \frac{\Delta \tilde{m}^2 L}{4E}$



(Wolfenstein, 1978;
Mikheyev, Smirnov,
1985)

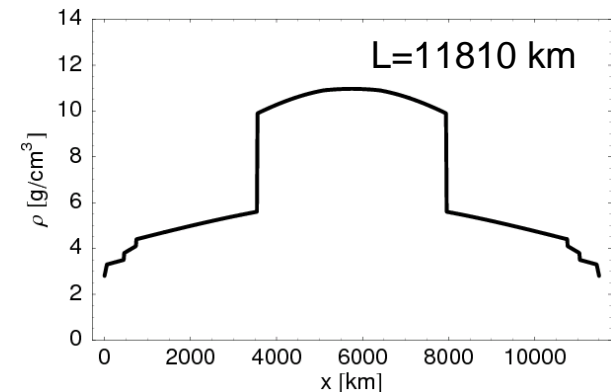
$$\Delta \tilde{m}^2 = \xi \cdot \Delta m^2, \quad \sin 2\tilde{\theta} = \frac{\sin 2\theta}{\xi}$$

$$\xi \equiv \sqrt{\sin^2 2\theta + (\cos 2\theta - \hat{A})^2}$$

$$\hat{A} = \frac{2EV}{\Delta m^2} = \frac{\pm 2\sqrt{2}E G_F n_e}{\Delta m^2} \Rightarrow \text{MH}$$

Resonance energy (from $\hat{A} \rightarrow \cos 2\theta$):

$$E_{\text{res}} [\text{GeV}] \sim 13\,200 \cos 2\theta \frac{\Delta m^2 [\text{eV}^2]}{\rho [\text{g/cm}^3]}$$



For ν_μ appearance, Δm_{31}^2 :

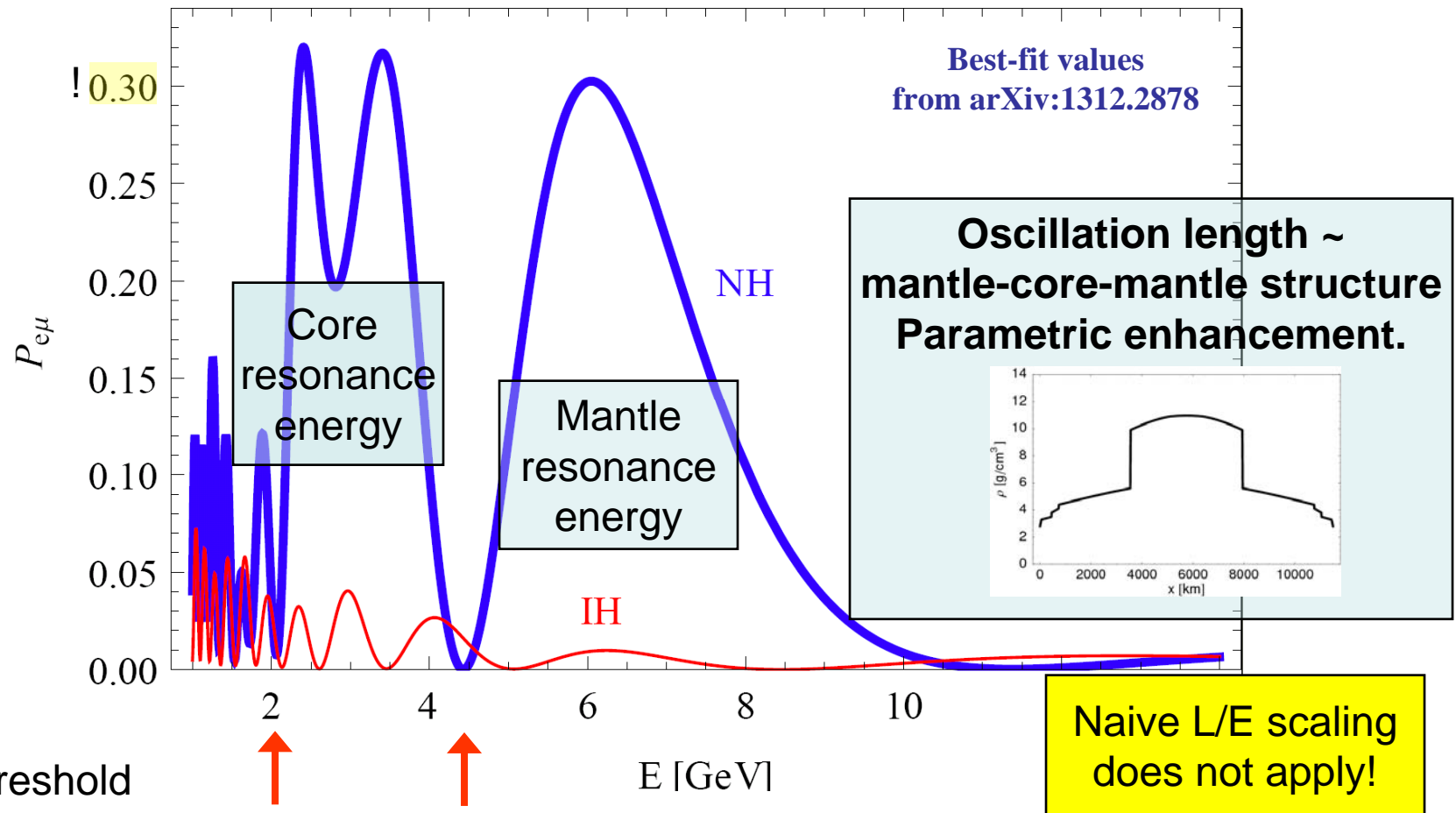
- $\rho \sim 4.7 \text{ g/cm}^3$ (Earth's mantle): $E_{\text{res}} \sim 6.4 \text{ GeV}$

- $\rho \sim 10.8 \text{ g/cm}^3$ (Earth's outer core): $E_{\text{res}} \sim 2.8 \text{ GeV}$

Mantle-core-mantle

(Parametric enhancement: Akhmedov, 1998; Akhmedov, Lipari, Smirnov, 1998; Petcov, 1998)

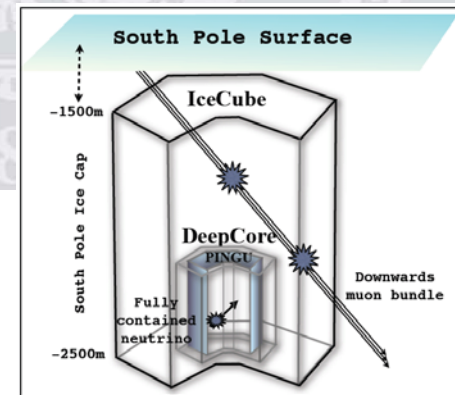
- Probability for $L=11810$ km



Threshold effects expected at:

2 GeV

4-5 GeV

Emerging technologies:
PINGU

- Fill in IceCube/DeepCore array with additional strings

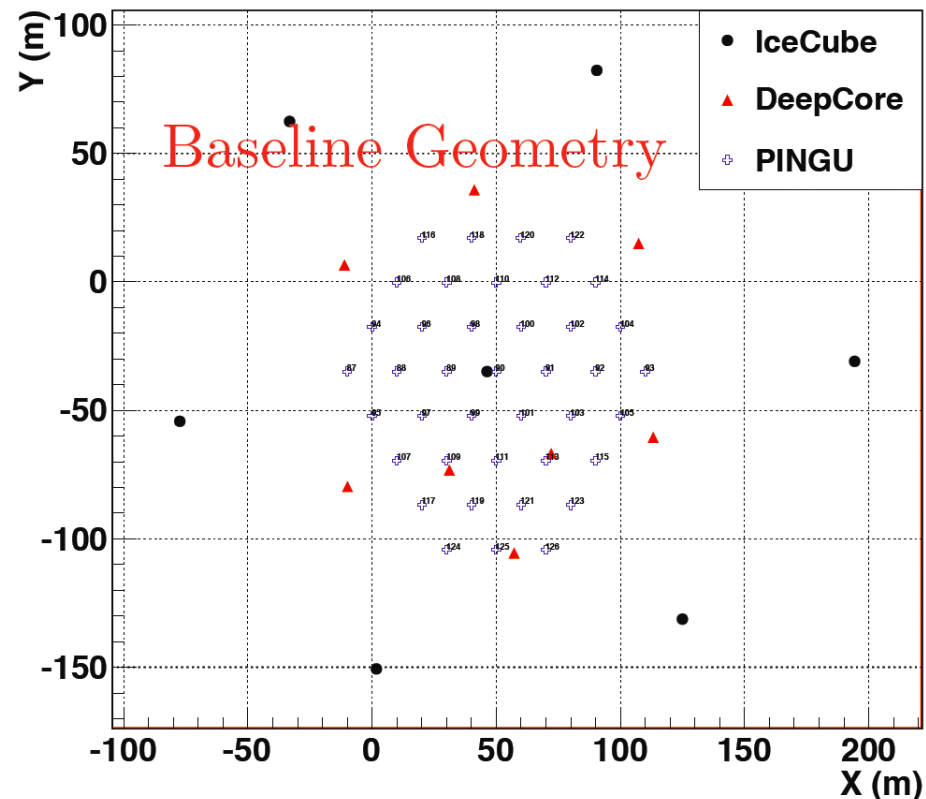
- Lower threshold

- Particle physics!?

- PINGU

(“Precision IceCube Next Generation Upgrade“):

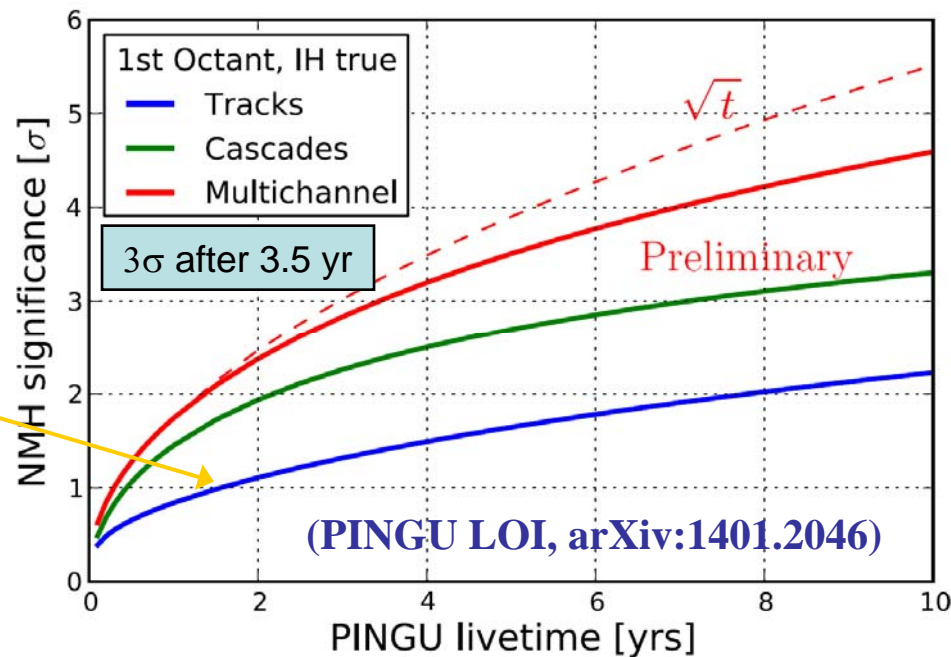
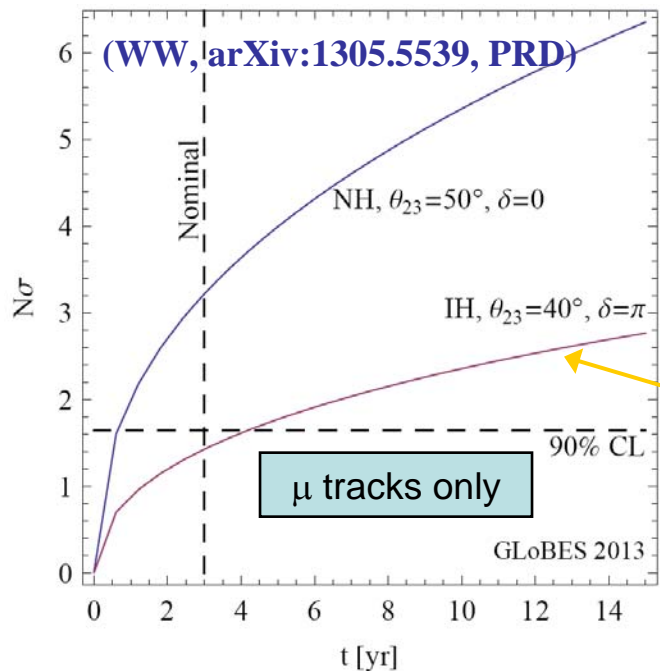
- 40 additional strings, 60 optical modules each
- Modest cost, US part ~ 55-80 M\$, foreign ~ 25 M\$ (including contingency)
- Completion 2019/2020?



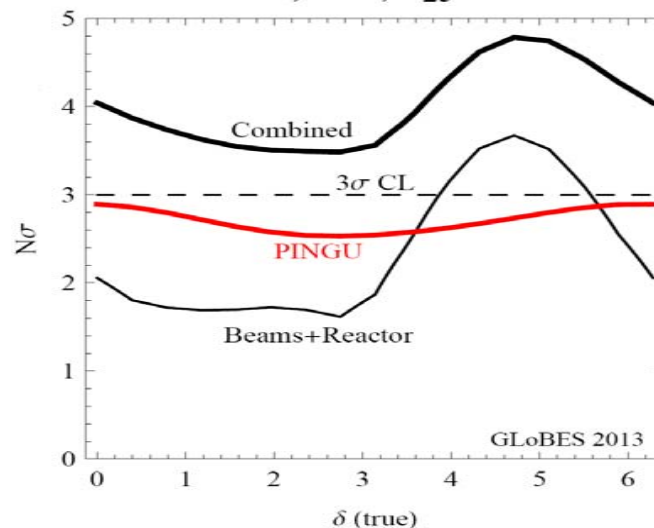
(PINGU LOI, arXiv:1401.2046)

Mass hierarchy measurement

... PINGU, using atmospheric neutrinos

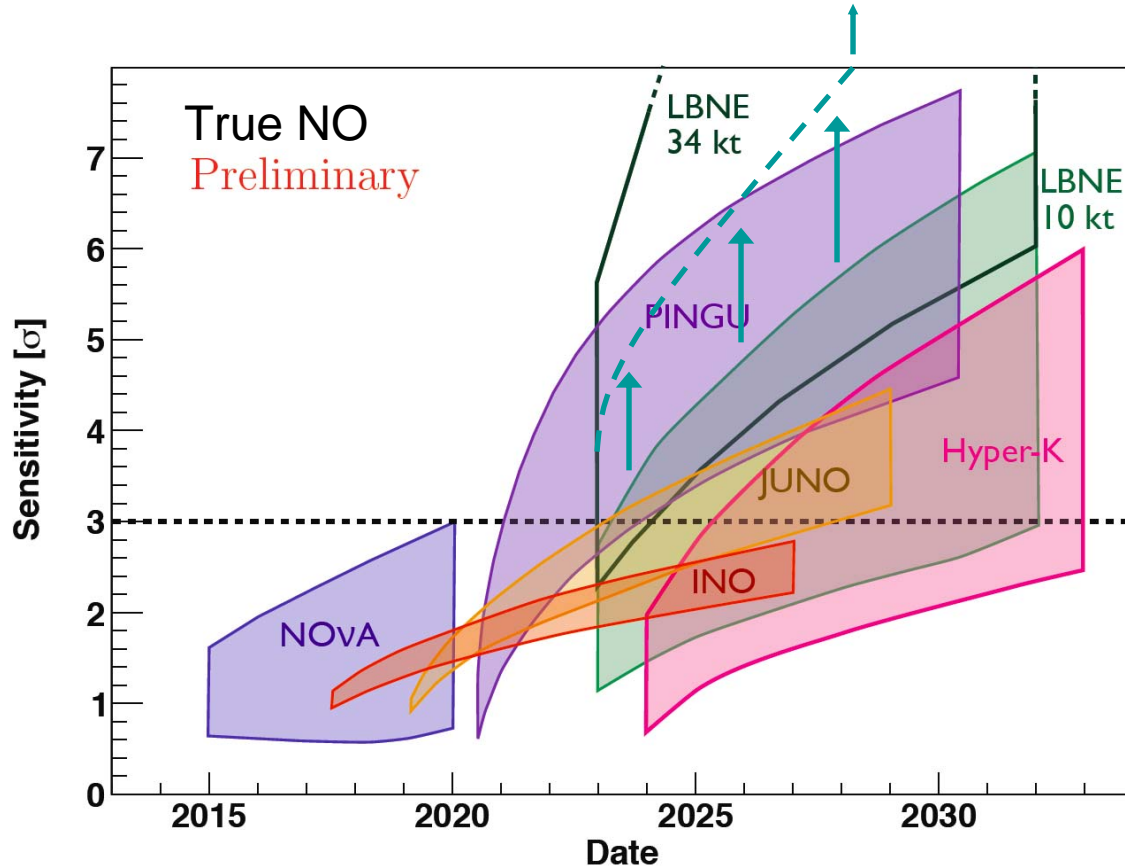


- 3σ conceivable after three years of operation
- Complementary to beams+reactor



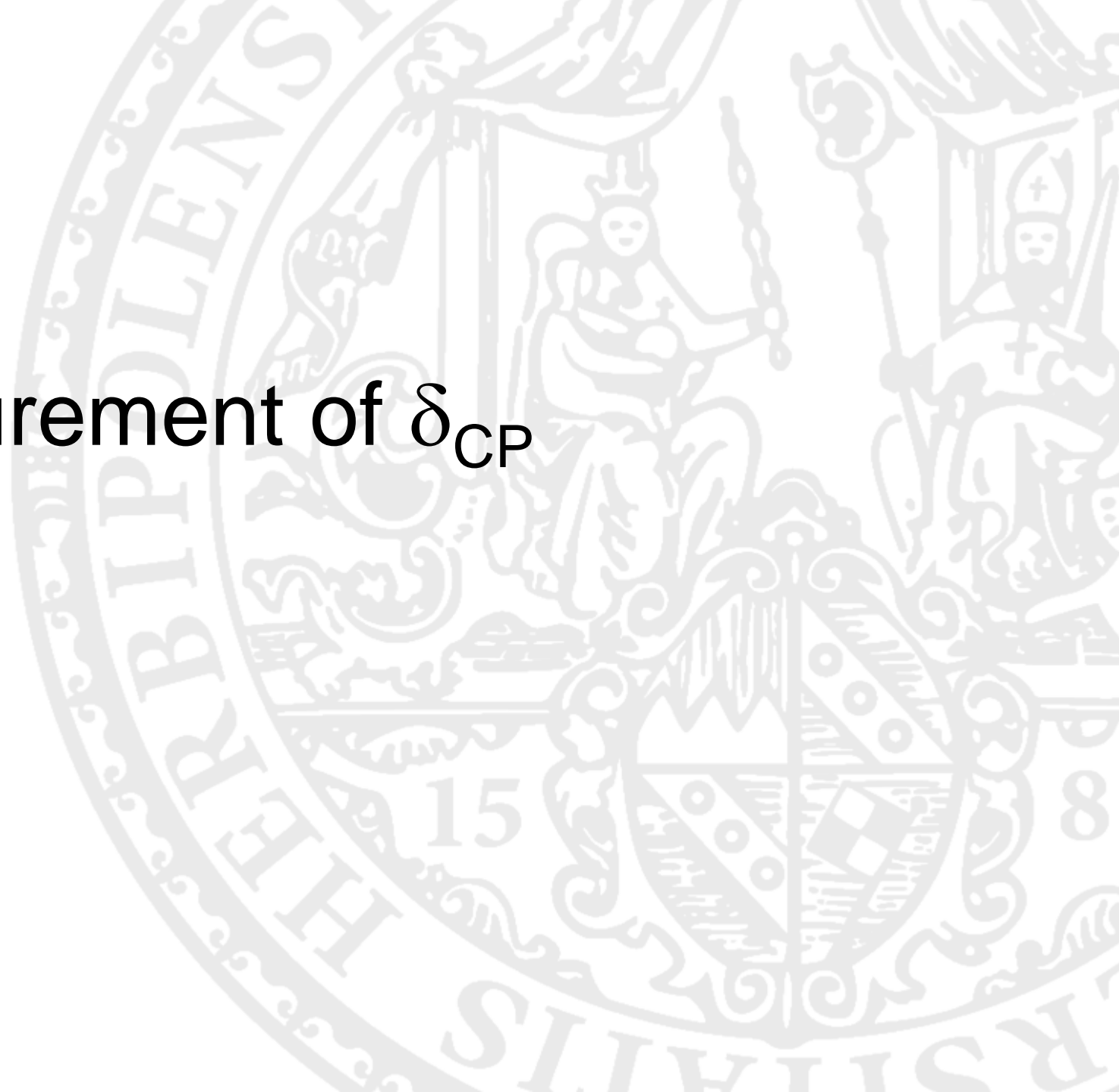
(WW, arXiv:1305.5539, PRD)

LBNE 10kt if θ_{23} varied as well
 ⇒ Fig. 9 in arXiv:1305.5539



- Bands: risk wrt θ_{23} (PINGU, INO), δ_{CP} (NOvA, LBNE), energy resolution (JUNO)
- LBNE and sensitivity also scales with θ_{23} !

Measurement of δ_{CP}



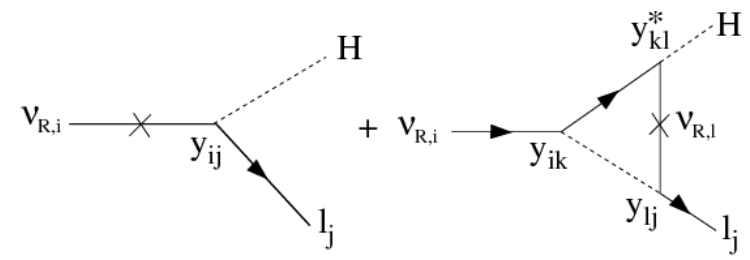
Why is δ_{CP} interesting?

- **CP violation** **$\sin\delta$**

Necessary condition for successful baryogenesis

(dynamical mechanism to create matter-antimatter asymmetry of the universe)

⇒ thermal leptogenesis by decay of heavy see-saw partner?



- **Model building** **$\cos\delta$**

⇒ C. Hagedorn

$$U_{PMNS} = U_\ell^\dagger U_\nu$$

Correction leading to non-zero θ_{13} ?

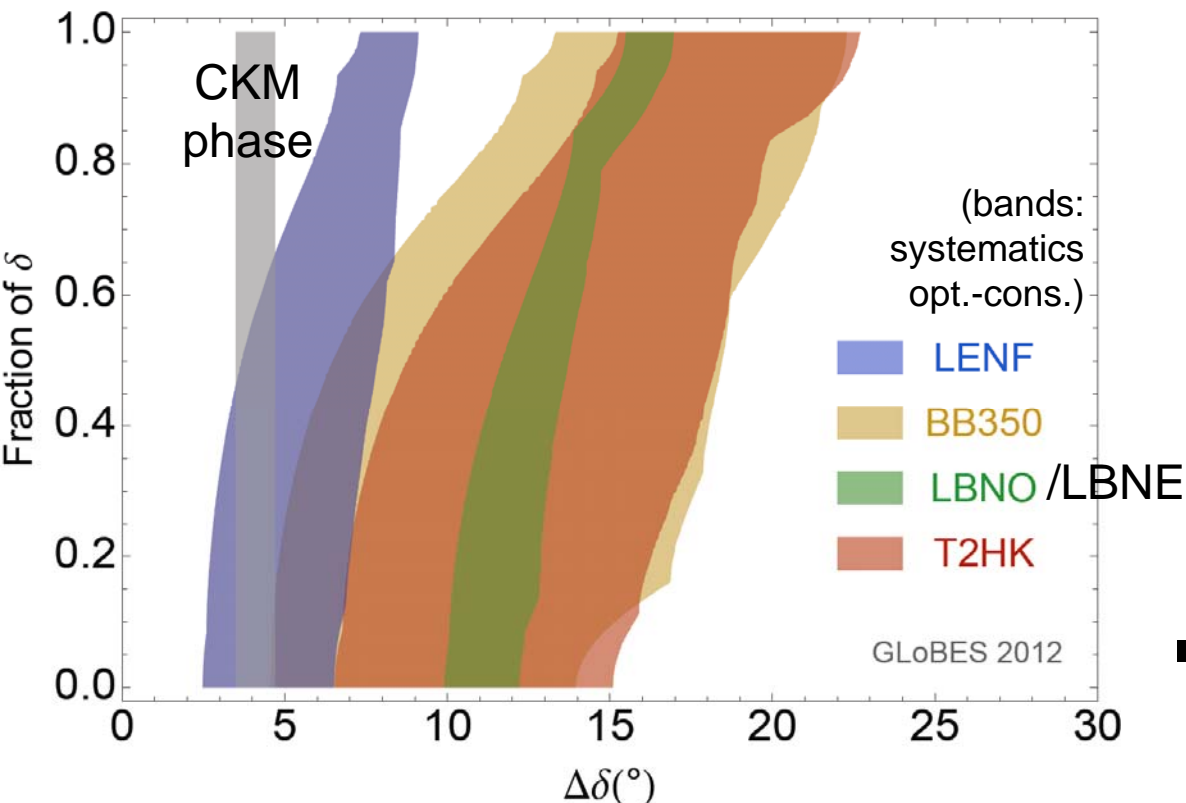
Symmetry e.g. TBM, BM, ...?
⇒ $\theta_{13}=0$

e.g. TBM sum rule: $\theta_{12} = 35^\circ + \theta_{13}$ **$\cos\delta$** (Antusch, King, ...)

➤ Discuss precision of δ_{CP} rather than CP violation

Precision of δ_{CP}

⇒ More details: talk by A. Sousa



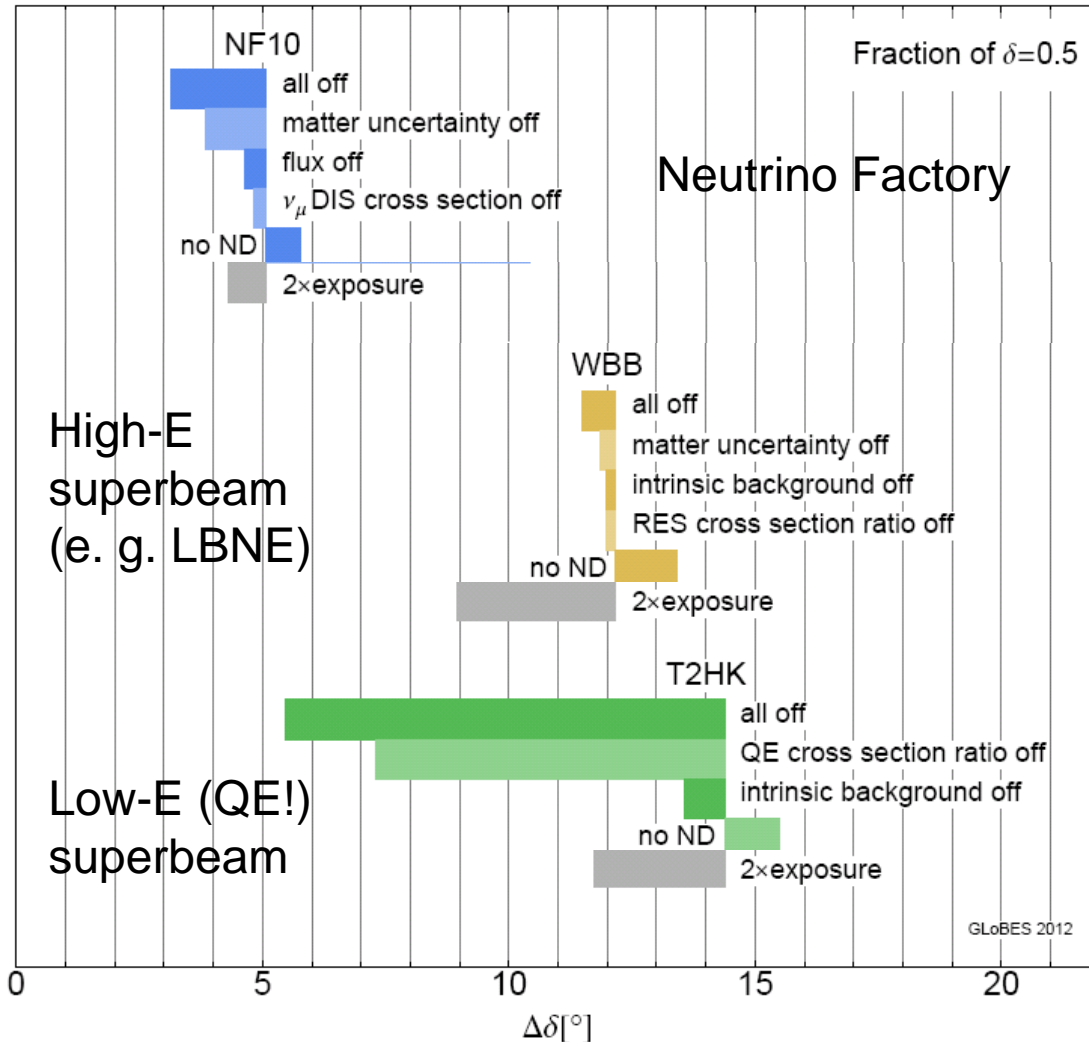
(Coloma, Huber, Kopp, Winter, arXiv:1209.5973)

Systematics important

- Use explicit near-far detector simulations
- Use same knowledge for cross sections for all experiments
- Use same assumptions for systematics implementation!

The NF can measure δ_{CP} with a precision comparable to the quark sector

Main challenges for δ_{CP}



Robust wrt systematics

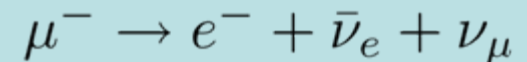
Main impact:
Matter density uncertainty

Operate in statistics-limited regime

Exposure more important than near detector

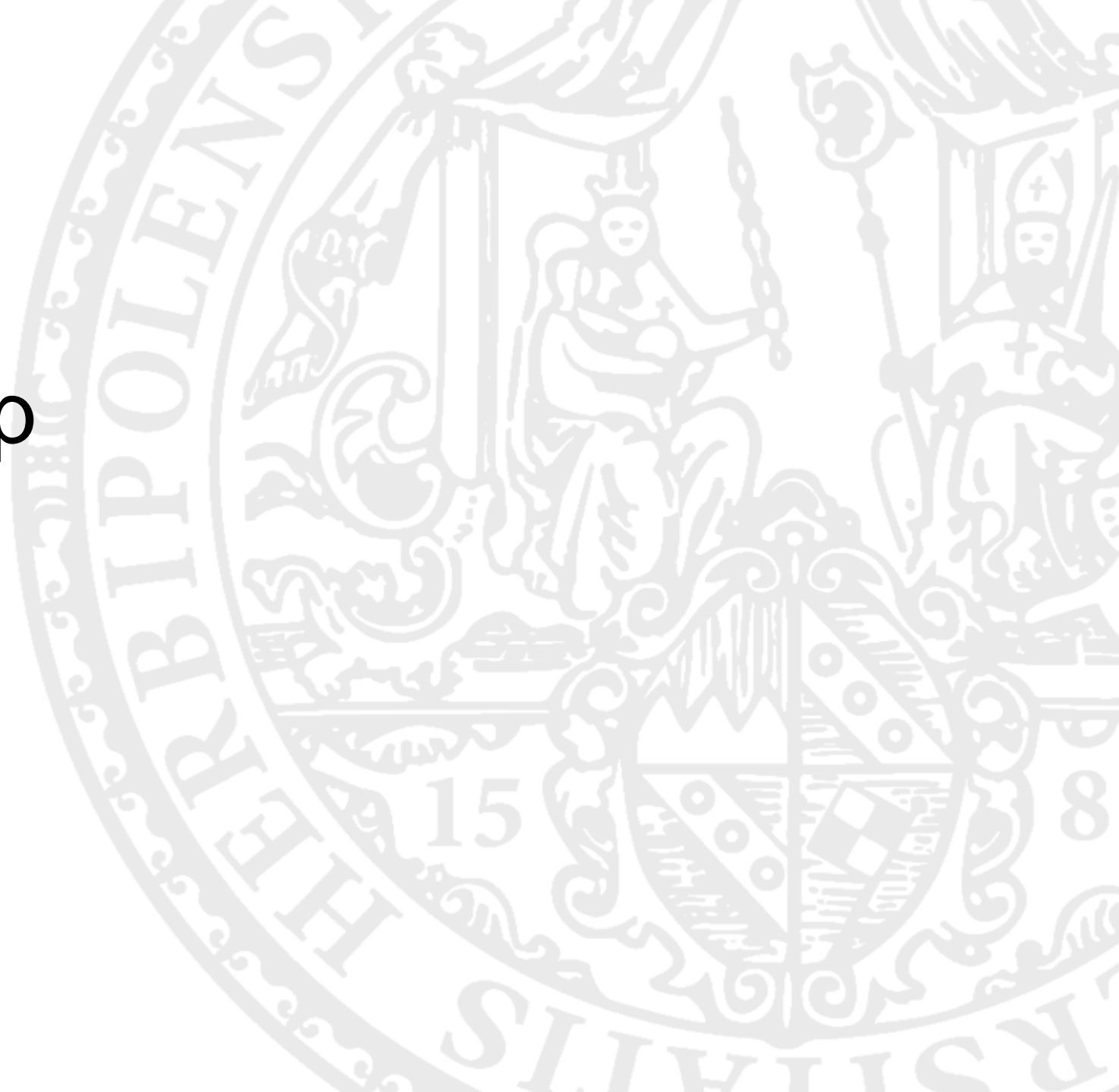
QE ν_e X-sec critical: cannot be measured in near detector

Theory: ν_e/ν_μ ratio?
Experiment:



- Mass hierarchy: may be tested in beginning of 2020s by “emerging technologies“, such as PINGU or JUNO
- CP violation: requires a new long-baseline experiment, such as LBNE, T2HK, NuFact
- Other issues: θ_{23} maximal? Octant? Sun and Earth tomography? New physics?
- Light sterile neutrinos - best candidate for physics B ν SM? Test short-baseline anomalies, measure neutrino X-secs, ...

Backup



Options

	Setup	E_ν^{peak}	L	OA	Detector	kt	MW	Decays/yr	$(t_\nu, t_{\bar{\nu}})$
Benchmark	BB350	1.2	650	–	WC	500	–	$1.1(2.8) \times 10^{18}$	(5,5)
	NF10	5.0	2 000	–	MIND	100	–	7×10^{20}	(10,10)
	WBB	4.5	2 300	–	LAr	100	0.8	–	(5,5)
	T2HK	0.6	295	2.5°	WC	560	1.66	–	(1.5,3.5)
Alternative	BB100	0.3	130	–	WC	500	–	$1.1(2.8) \times 10^{18}$	(5,5)
	+ SPL			–			4		–
	NF5	2.5	1 290	–	MIND	100	–	7×10^{20}	(10,10)
	LBNE _{mini}	4.0	1 290	–	LAr	10	0.7	–	(5,5)
	NO ν A ⁺	2.0	810	0.8°	LAr	30	0.7	–	(5,5)
2020	T2K	0.6	295	2.5°	WC	22.5	0.75	–	(5,5)
	NO ν A	2.0	810	0.8°	TASD	15	0.7	–	(4,4)

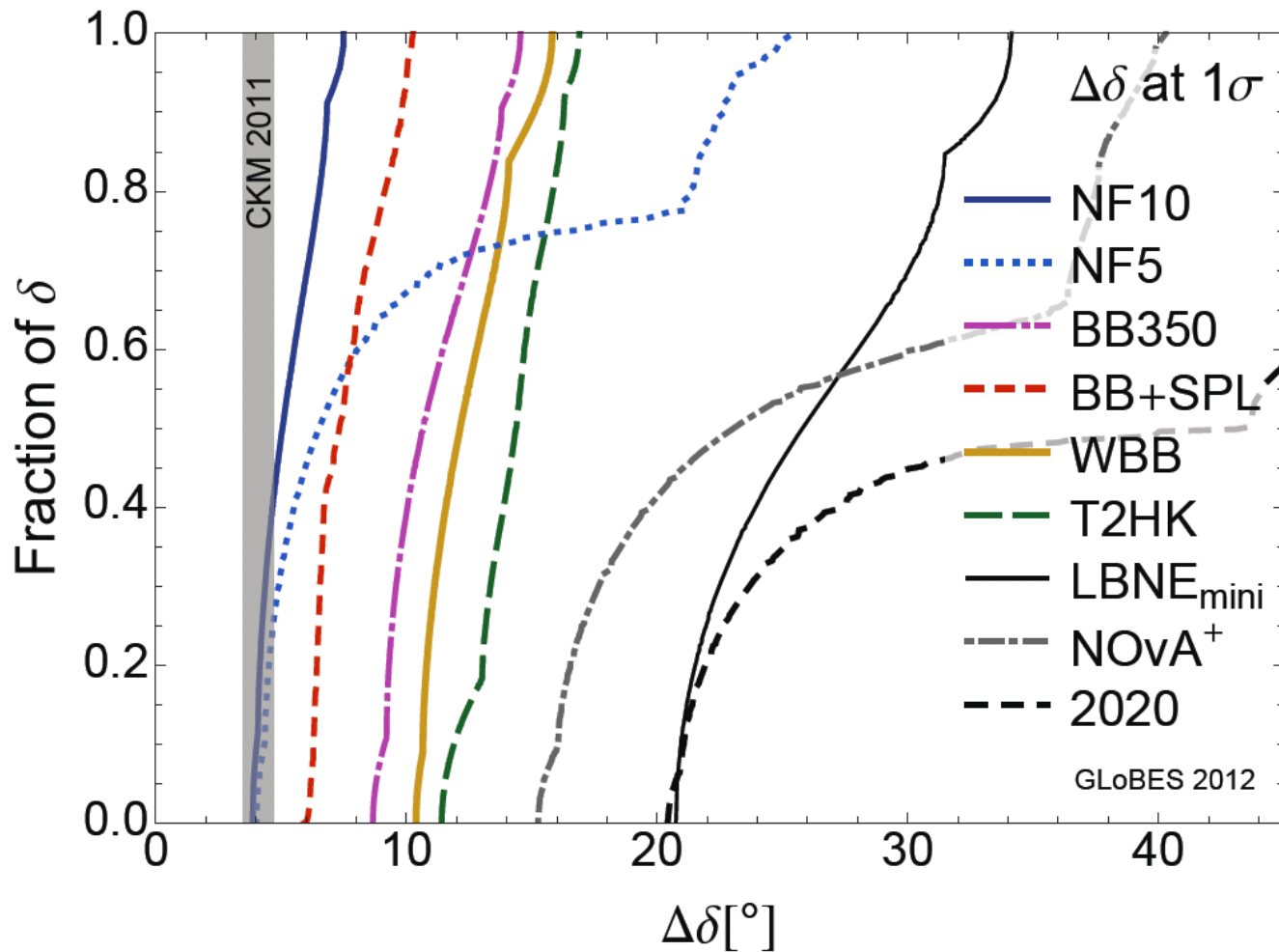
+ Daya
Bay

Systematics

Systematics	SB			BB			NF		
	Opt.	Def.	Cons.	Opt.	Def.	Cons.	Opt.	Def.	Cons.
Fiducial volume ND	0.2%	0.5%	1%	0.2%	0.5%	1%	0.2%	0.5%	1%
Fiducial volume FD (incl. near-far extrap.)	1%	2.5%	5%	1%	2.5%	5%	1%	2.5%	5%
Flux error signal ν	5%	7.5%	10%	1%	2%	2.5%	0.1%	0.5%	1%
Flux error background ν	10%	15%	20%	correlated			correlated		
Flux error signal $\bar{\nu}$	10%	15%	20%	1%	2%	2.5%	0.1%	0.5%	1%
Flux error background $\bar{\nu}$	20%	30%	40%	correlated			correlated		
Background uncertainty	5%	7.5%	10%	5%	7.5%	10%	10%	15%	20%
Cross secs \times eff. QE [†]	10%	15%	20%	10%	15%	20%	10%	15%	20%
Cross secs \times eff. RES [†]	10%	15%	20%	10%	15%	20%	10%	15%	20%
Cross secs \times eff. DIS [†]	5%	7.5%	10%	5%	7.5%	10%	5%	7.5%	10%
Effec. ratio ν_e/ν_μ QE [*]	3.5%	11%	–	3.5%	11%	–	–	–	–
Effec. ratio ν_e/ν_μ RES [*]	2.7%	5.4%	–	2.7%	5.4%	–	–	–	–
Effec. ratio ν_e/ν_μ DIS [*]	2.5%	5.1%	–	2.5%	5.1%	–	–	–	–
Matter density	1%	2%	5%	1%	2%	5%	1%	2%	5%

(Coloma, Huber, Kopp, Winter, arXiv:1209.5973)

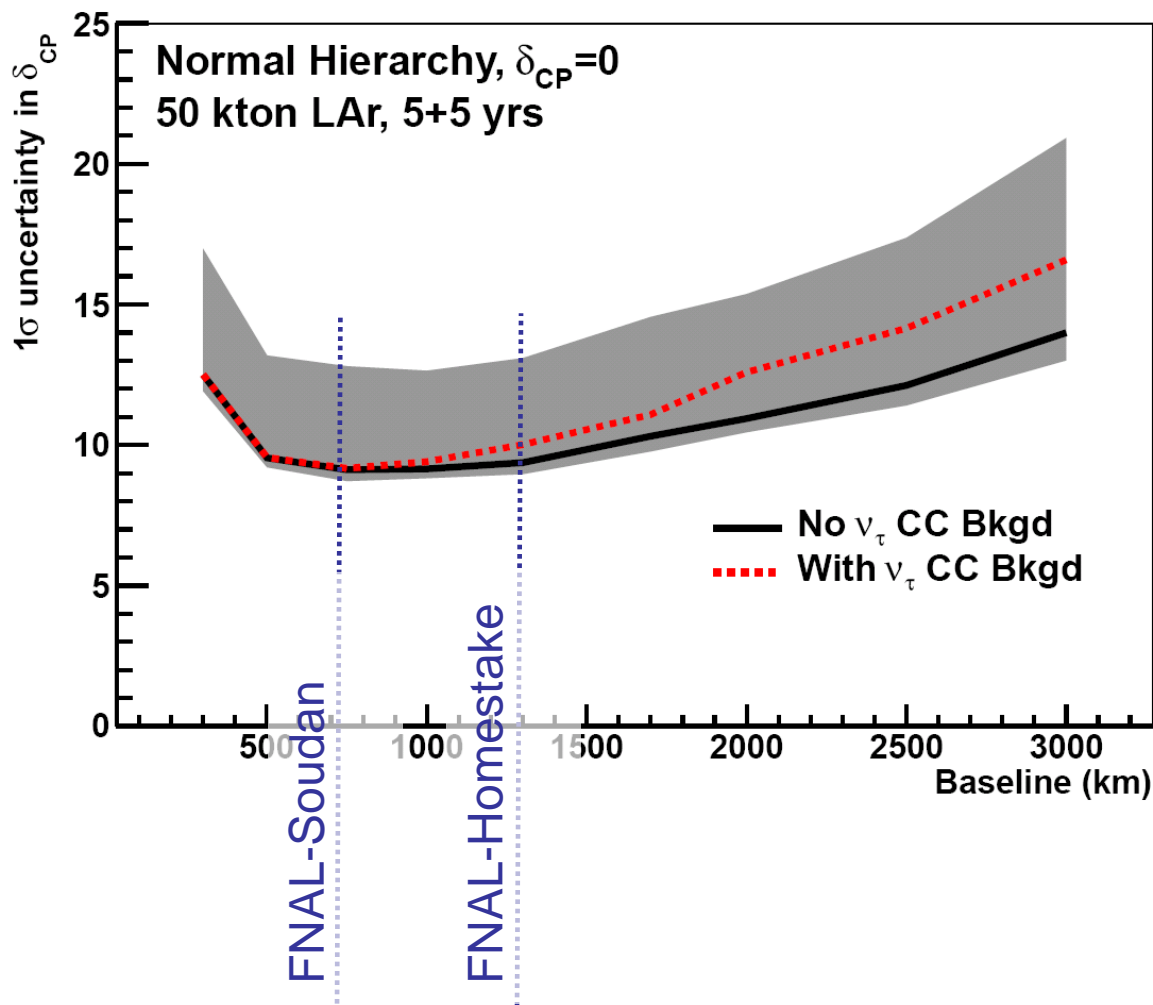
■ Comparison at default systematics:



NF5 exhibits strong dependence on δ_{CP} (some dependence on binning!)

BB100+SPL is the only setup comparable with NuFact

LBNE: Optimal baseline?



- For δ_{CP} : ~500 – 1300 km
- For MH, octant > 1000 km