

# Theoretical predictions for top-pair and single-top production

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- Two-loop soft-gluon corrections
- Total cross sections
- Top  $p_T$  distributions in pair production
- Top rapidity distributions in pair production
- Top  $p_T$  distributions in single-top production

## Higher-order corrections

QCD corrections significant for top pair and single top production

Soft-gluon corrections are important

**Soft terms:**  $\left[ \frac{\ln^k(s_4/m_t^2)}{s_4} \right]_+$  with  $k \leq 2n - 1$ ,  $s_4$  distance from threshold

Resum these soft corrections - factorization and RGE

**NNLL accuracy**—two-loop soft anomalous dimensions

Approximate NNLO differential cross sections from expansion of resummed expressions

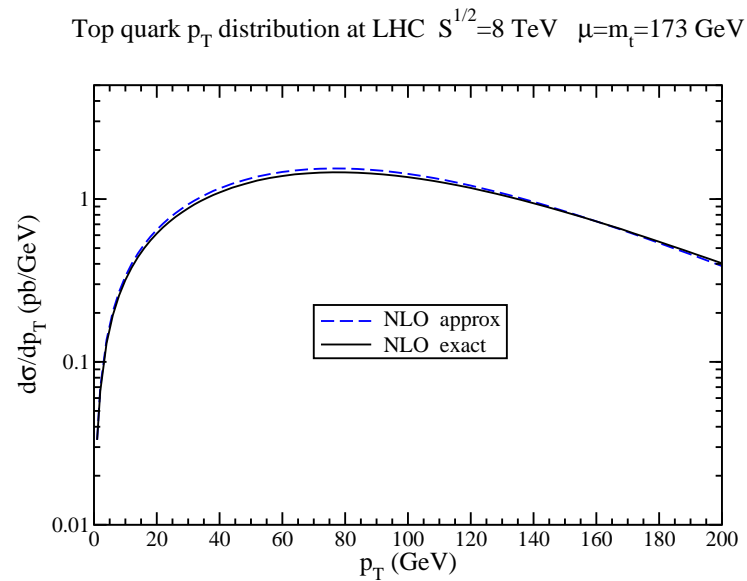
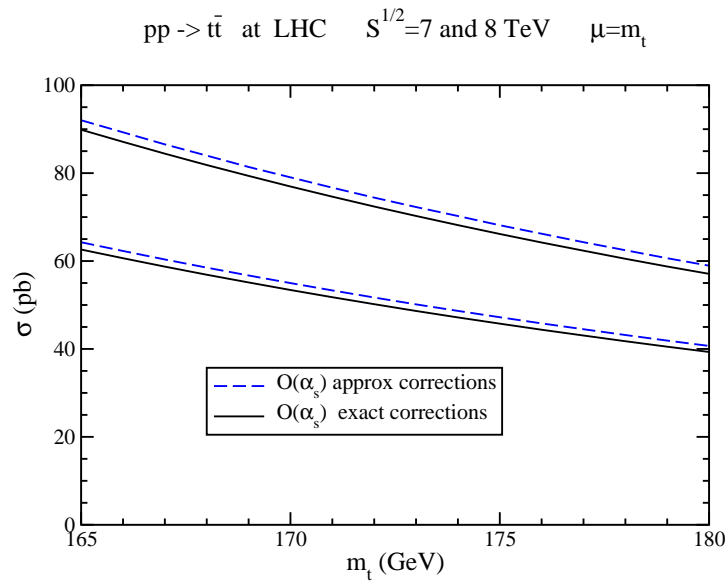
Calculation is for **partonic threshold at the double differential cross section level using the standard moment-space resummation in pQCD**

total cross section, and top  $p_T$  and rapidity distributions

**Latest results:** arXiv:1311.0283 [hep-ph]

## Threshold approximation

Approximation works very well for LHC and Tevatron energies



**excellent approximation:**

$\sim 1\%$  difference between NLO approximate and exact cross sections;  
and also for differential distributions;  
also true at NNLO for total cross sections

**For best prediction for differential distributions add NNLO approximate corrections to exact NLO result**

## Differences between various resummation/NNLO approx approaches

### Total vs differential cross section moment-space pQCD vs SCET

Name	Observable	Soft limit
single-particle-inclusive (1PI)	$d\sigma/dp_T dy$	$s_4 = s + t_1 + u_1 \rightarrow 0$
pair-invariant-mass (PIM)	$d\sigma/dM_{t\bar{t}} d\theta$	$(1 - z) = 1 - M_{t\bar{t}}^2/s \rightarrow 0$
production threshold	$\sigma$	$\beta = \sqrt{1 - 4m_t^2/s} \rightarrow 0$

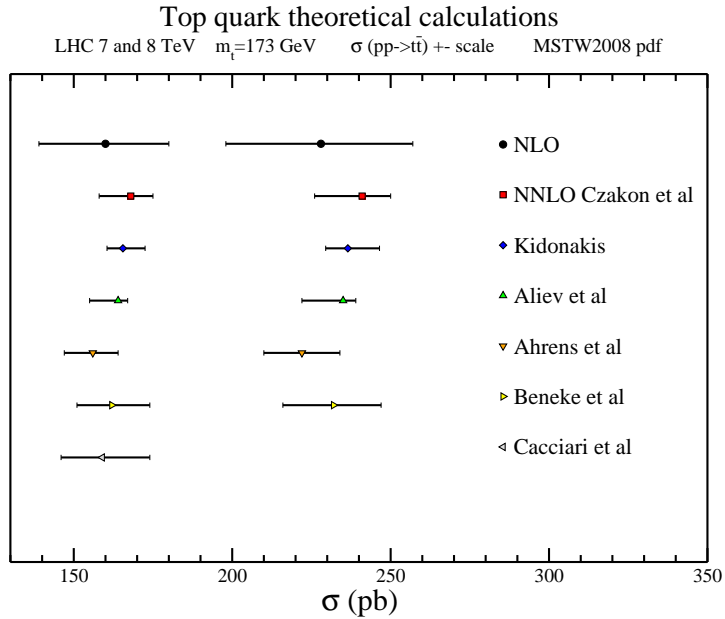
The more general approach is double-differential  
→  $p_T$  and rapidity distributions

total-only approaches are limit/special case (absolute vs partonic threshold)

For differential calculations, further differences arise from how the relation  $s + t_1 + u_1 = 0$  is used in the plus-distribution coefficients, how subleading terms are treated, damping factors, etc.

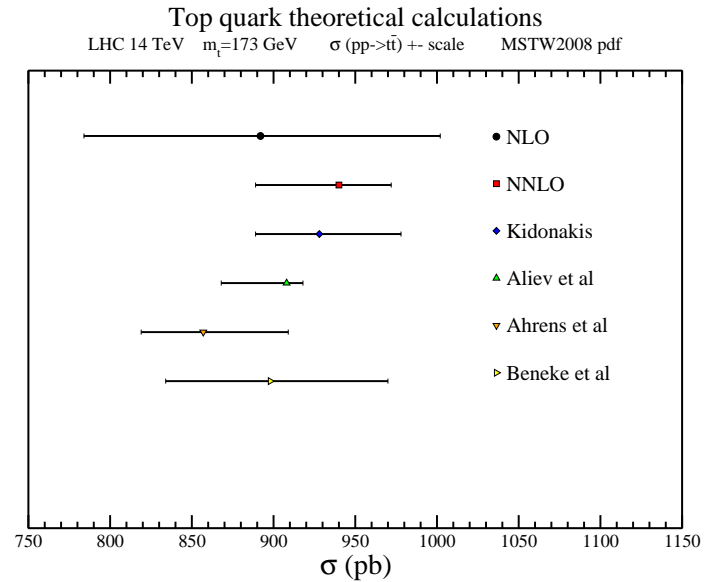
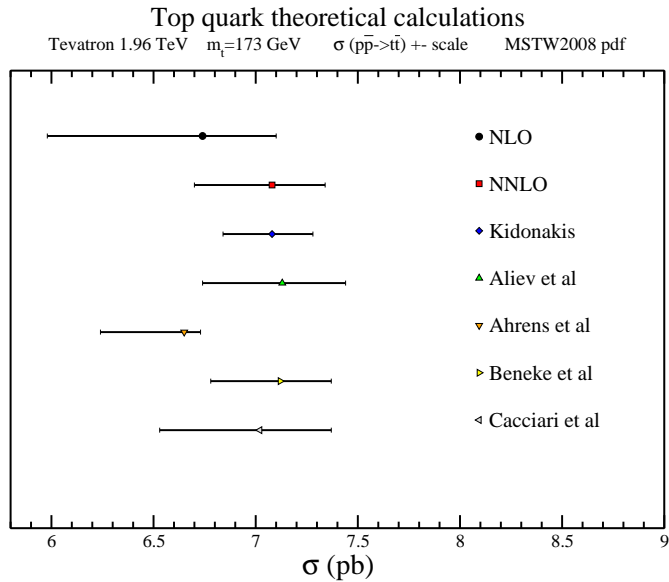
see N. Kidonakis and B.D. Pecjak, Eur. Phys. J C 72, 2084 (2012)

for details and review



**Comparison of various NNLO approx approaches  
all with the same choice of parameters**

**Kidonakis, PRD 82, 114030 (2010) differential-pQCD**  
**Aliev et al, CPC 182, 1034 (2011) total-pQCD**  
**Ahrens et al, PLB 703, 135 (2011) differential -SCET**  
**Beneke et al, NPB 855, 695 (2012) total-SCET**  
**Cacciari et al, PLB 710, 612 (2012) total-pQCD**



## Varying degree of success of the various approaches

My PRD 82 result is very close to the exact NNLO:  
both the central values and the scale uncertainty are nearly the same  
true for all collider energies and top quark masses

This was expected from comparison to NLO, and comparison of 1PI and PIM  
results at NNLO in 2003

(PRD 68, N. Kidonakis & R. Vogt; see also discussion in PRD78 and PRD82)

less than 1% difference between NLO approximate and exact cross sections  
at both NLO and NNLO

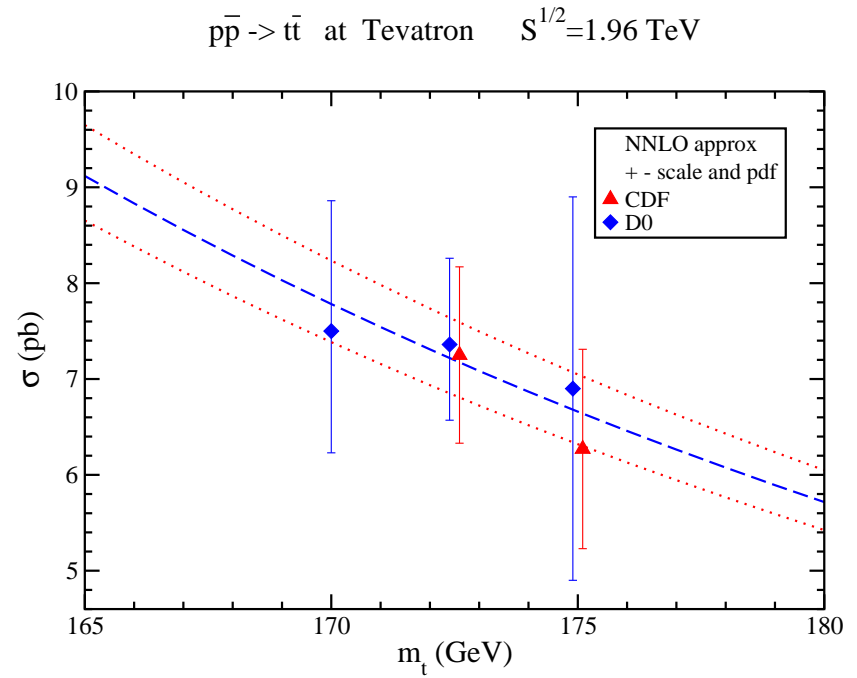
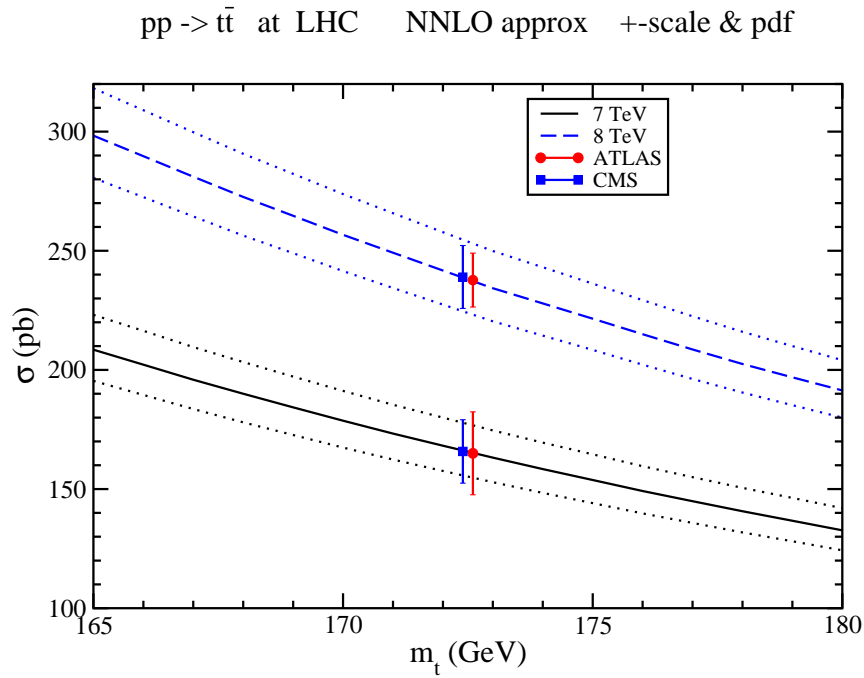
currently working on adding approximate NNNLO

stability of the theoretical NNLO approximate result in this  
double-differential pQCD resummation approach over the past decade

the reliability of the NNLO approximate result and near-identical  
value to exact NNLO is very important for several reasons

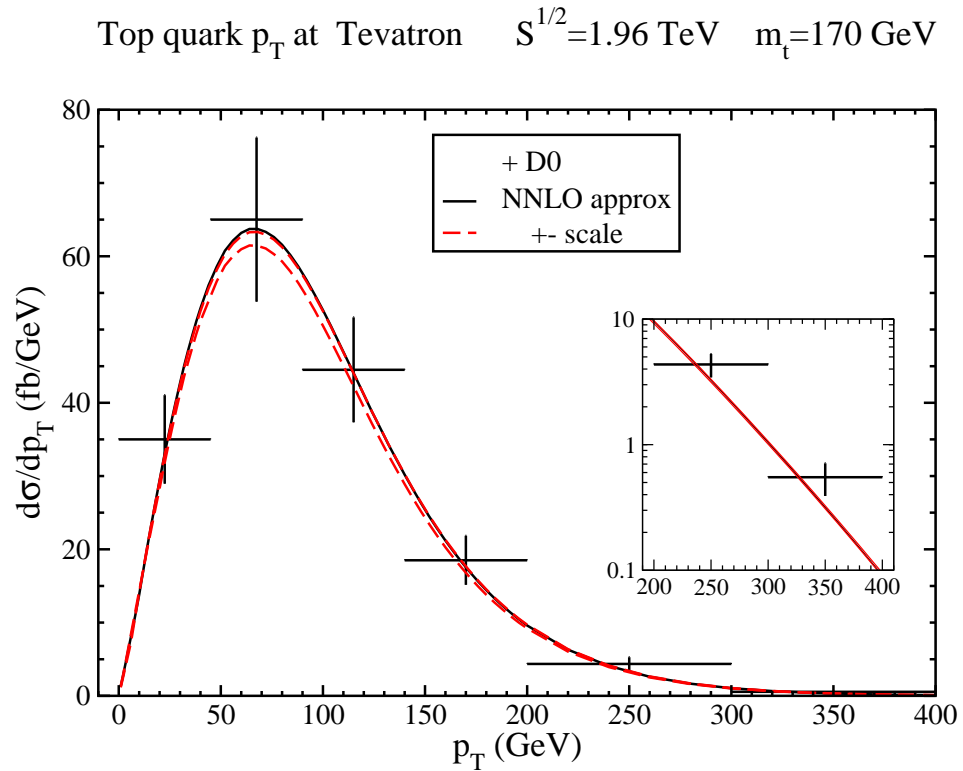
- provides confidence of application to other processes (single-top, W, etc)
- used as background for many analyses (Higgs, etc)
- means that we have near-exact NNLO  $p_T$  and rapidity distributions

## Top-pair cross sections at the LHC and the Tevatron



Excellent agreement of theory with data

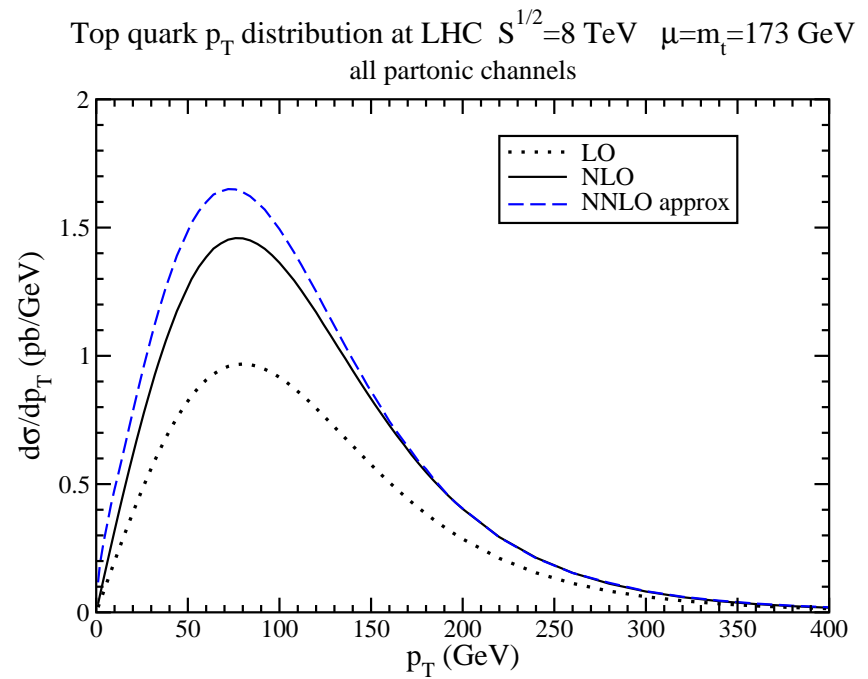
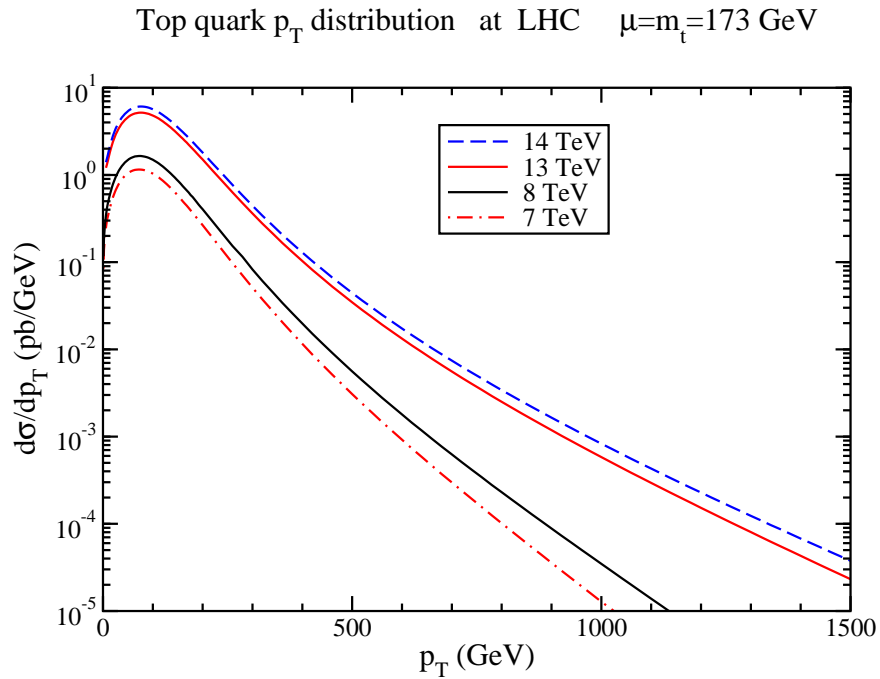
## Top quark $p_T$ distribution at the Tevatron



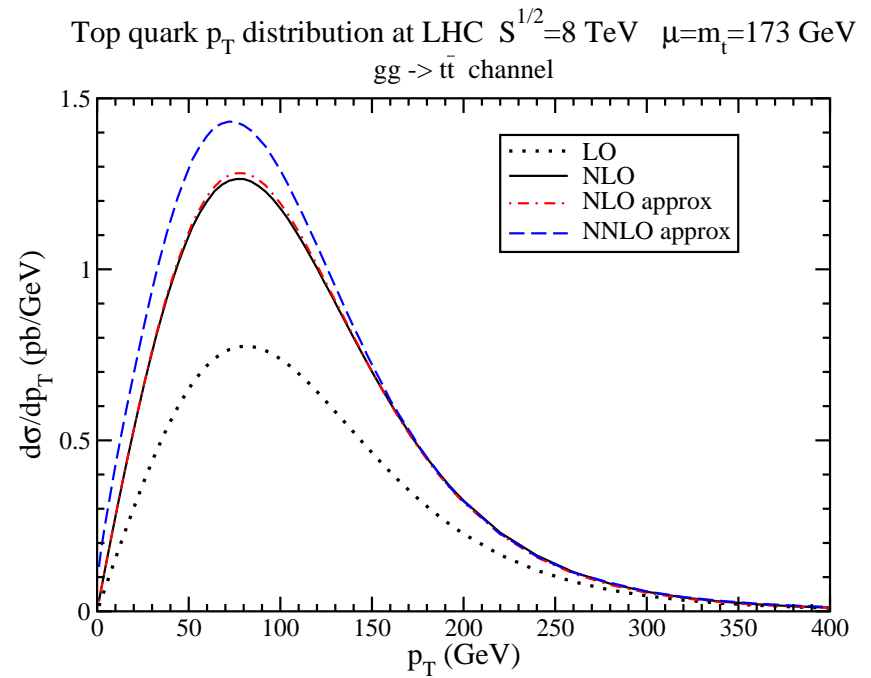
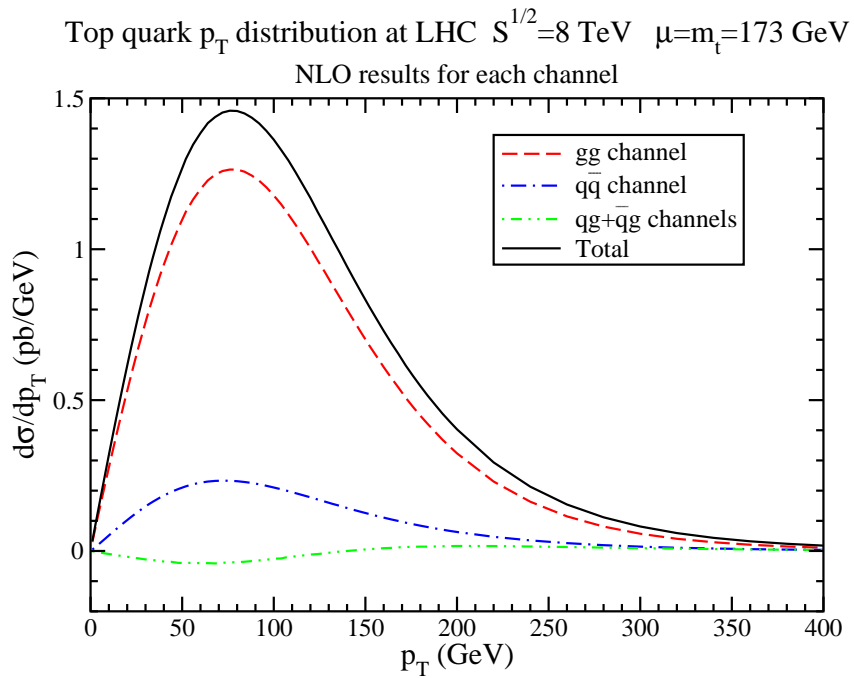
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## Top quark $p_T$ distribution at the LHC

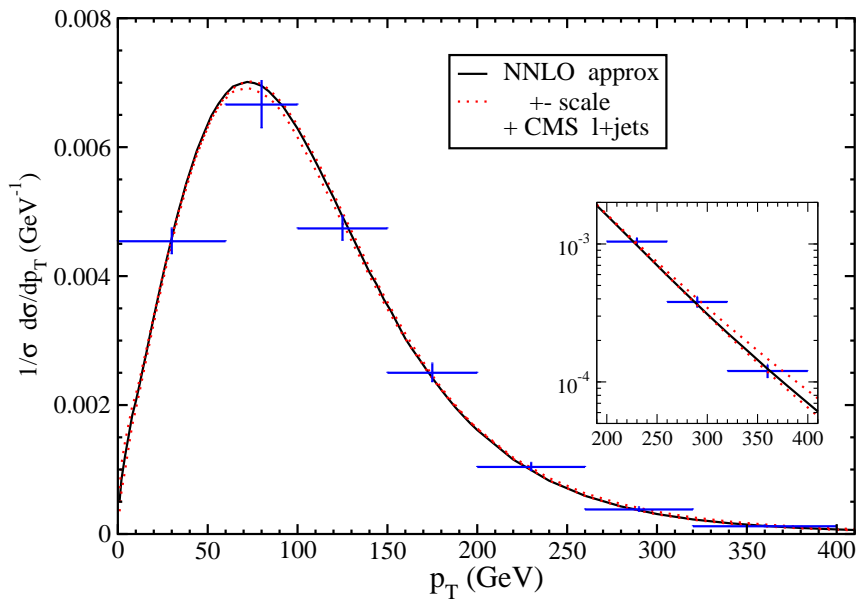


## Top quark $p_T$ distribution at the LHC

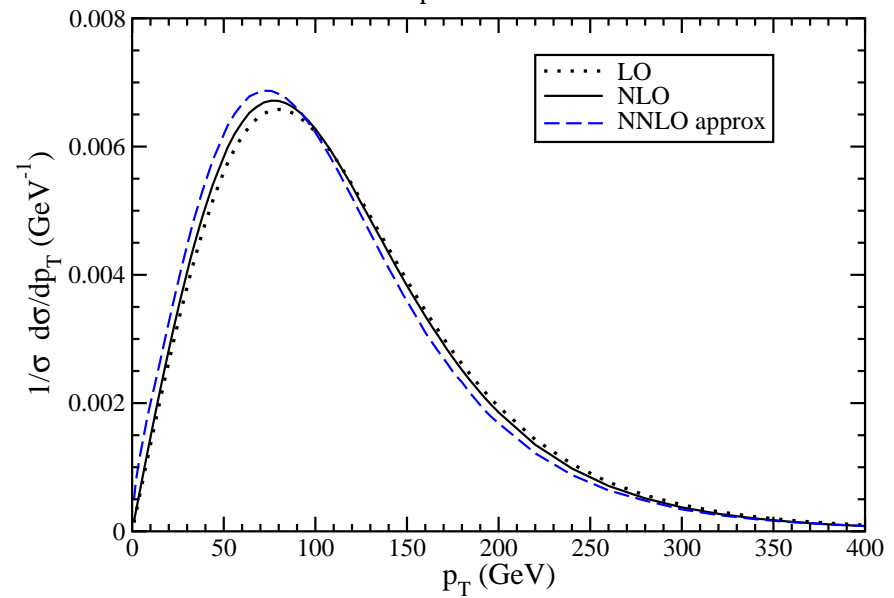


## Normalized top quark $p_T$ distribution at the LHC

Normalized top  $p_T$  distribution at LHC  $S^{1/2}=7$  TeV  $m_t=173$  GeV



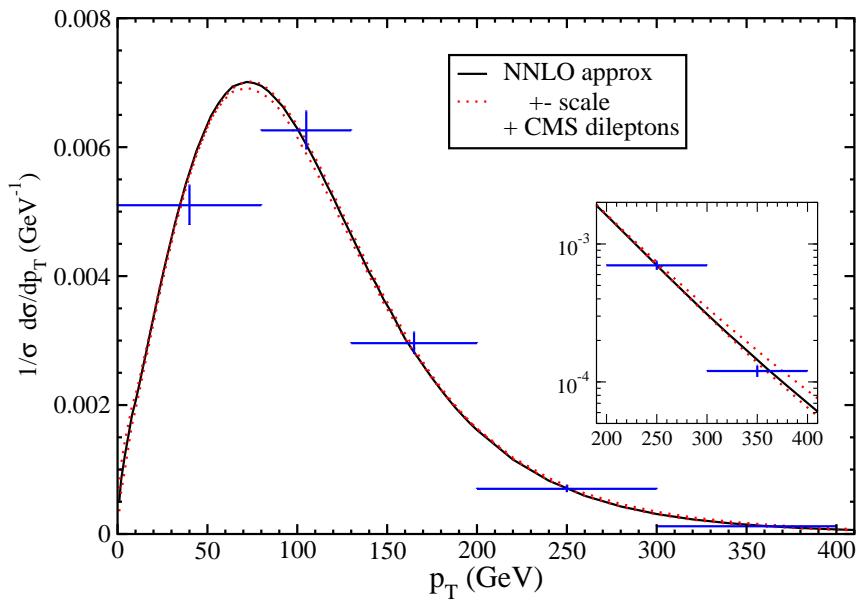
Normalized top  $p_T$  distribution at LHC  $S^{1/2}=8$  TeV  $\mu=m_t=173$  GeV  
all partonic channels



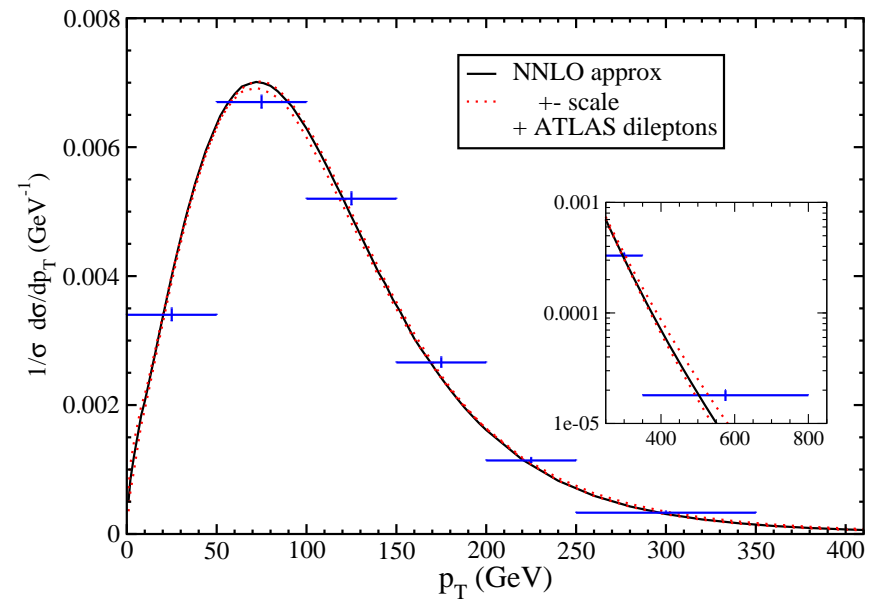
Excellent agreement with CMS data at 7 TeV; also at 8 TeV

## Normalized top quark $p_T$ distribution at the LHC

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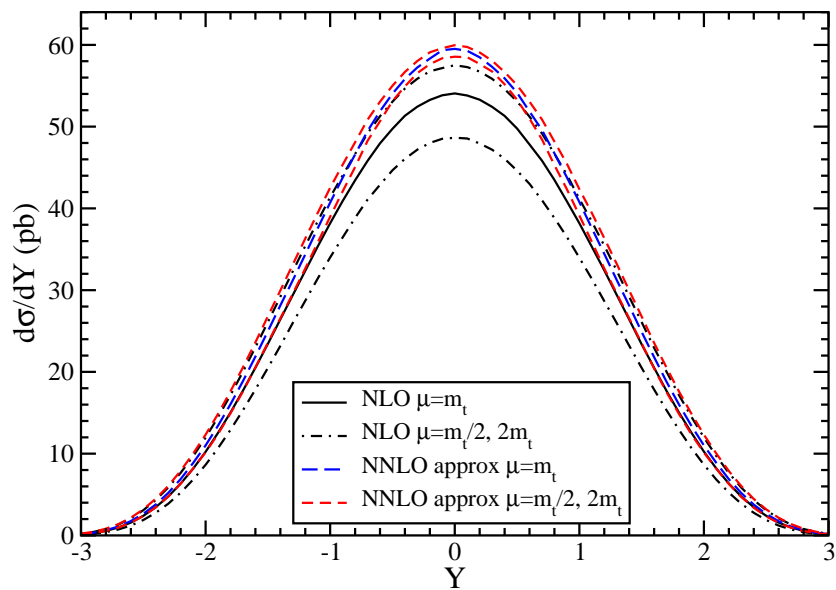


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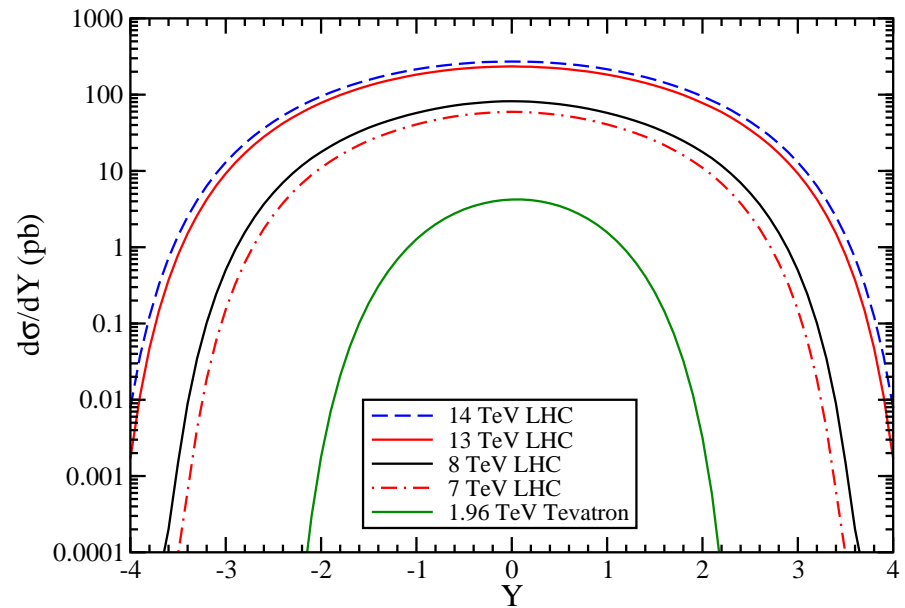


## Top quark rapidity distribution at LHC and Tevatron

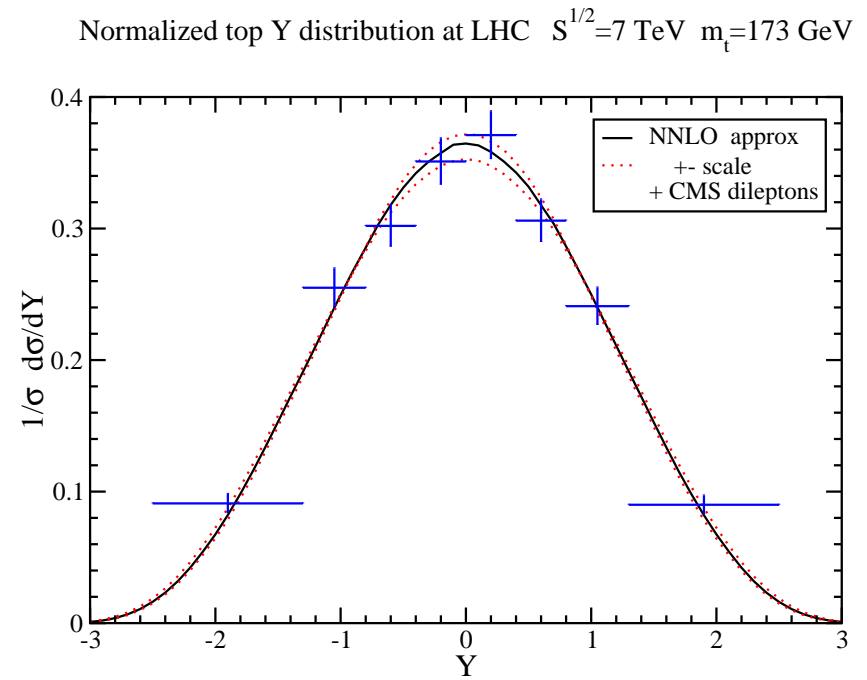
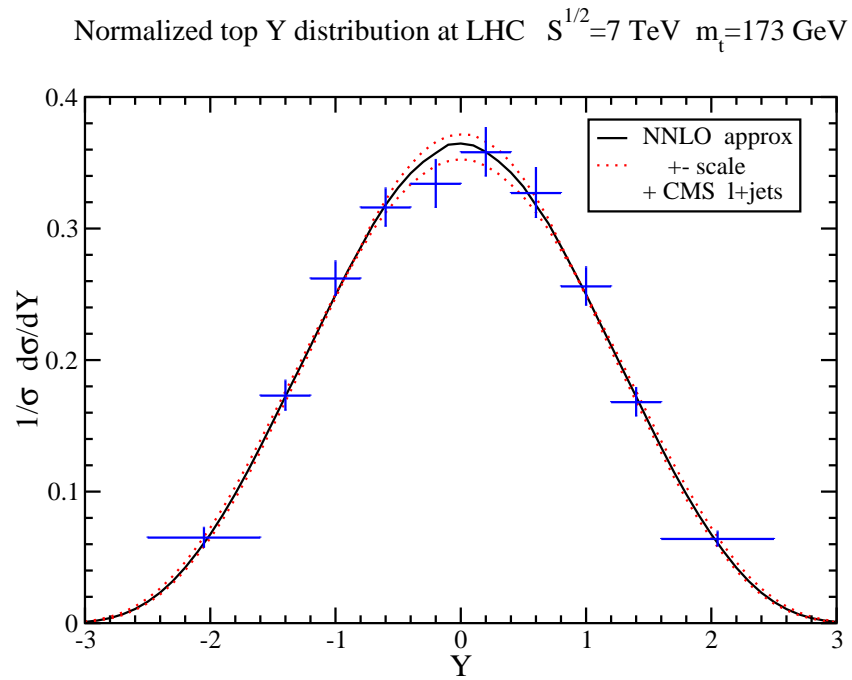
Top quark rapidity at LHC  $S^{1/2}=7$  TeV  $m_t=173$  GeV



Top quark rapidity distribution NNLO approx  $\mu=m_t=173$  GeV



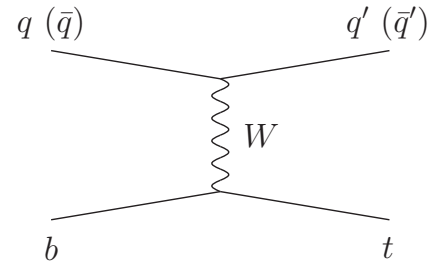
## Normalized top quark rapidity distribution at LHC



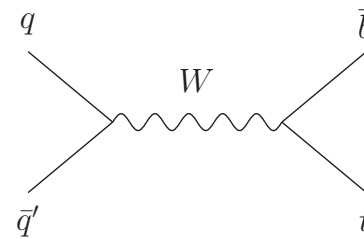
Excellent agreement with CMS data at 7 TeV; also at 8 TeV

## Single-top partonic processes at LO

- **$t$  channel:**  $qb \rightarrow q't$  and  $\bar{q}b \rightarrow \bar{q}'t$   
dominant at Tevatron and LHC

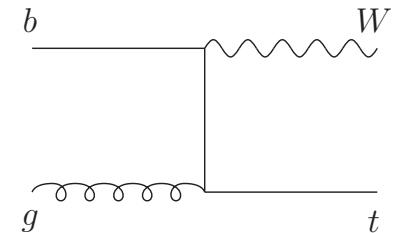
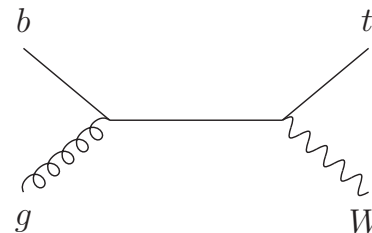


- **$s$  channel:**  $q\bar{q}' \rightarrow \bar{b}t$   
small at Tevatron and LHC

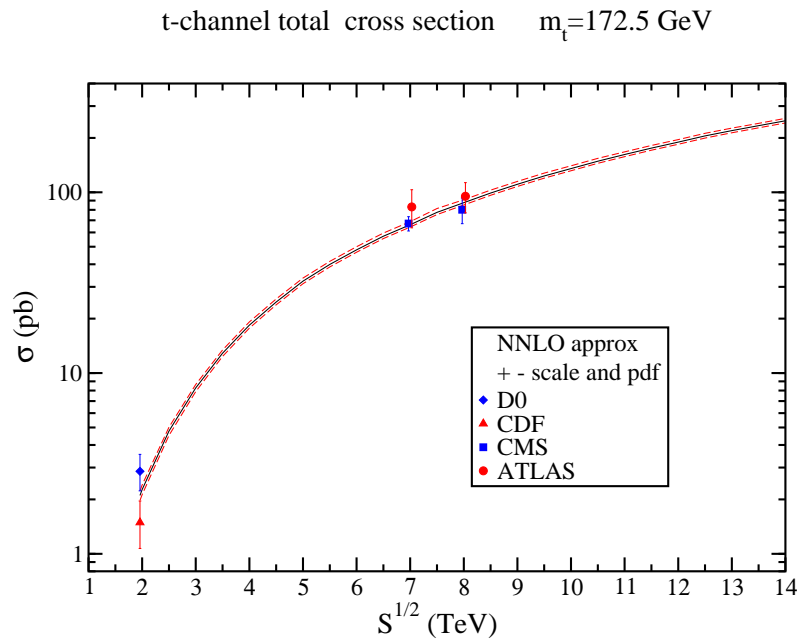
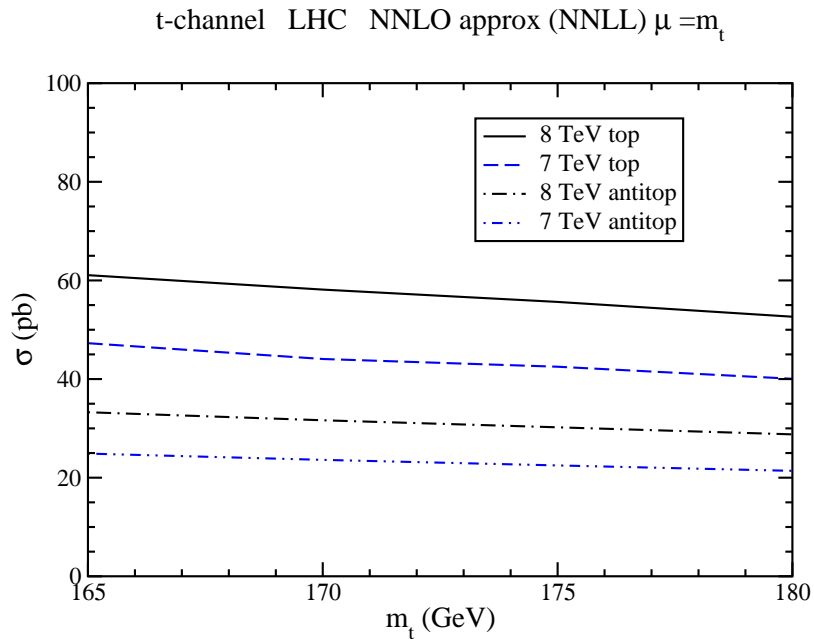


- **associated  $tW$  production:**  $bg \rightarrow tW^-$   
very small at Tevatron, significant at LHC

**Related process:**  $bg \rightarrow tH^-$



## Single top $t$ -channel cross sections at LHC



$m_t = 173$  GeV

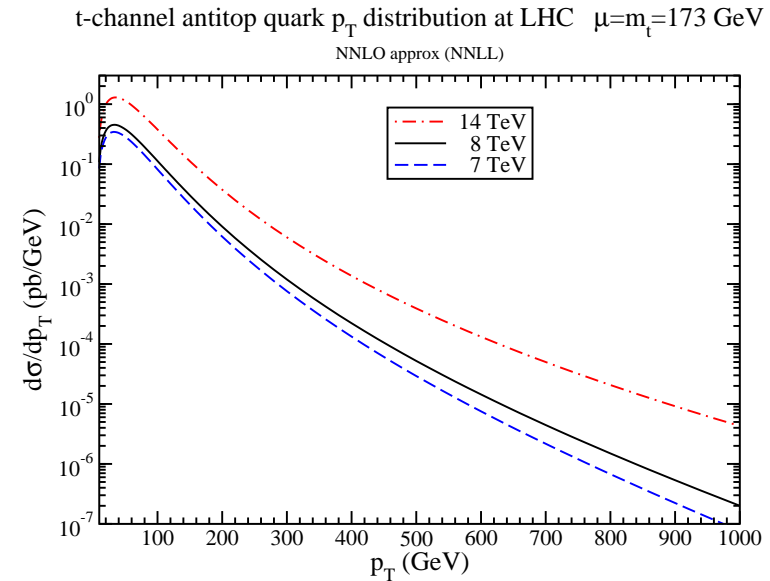
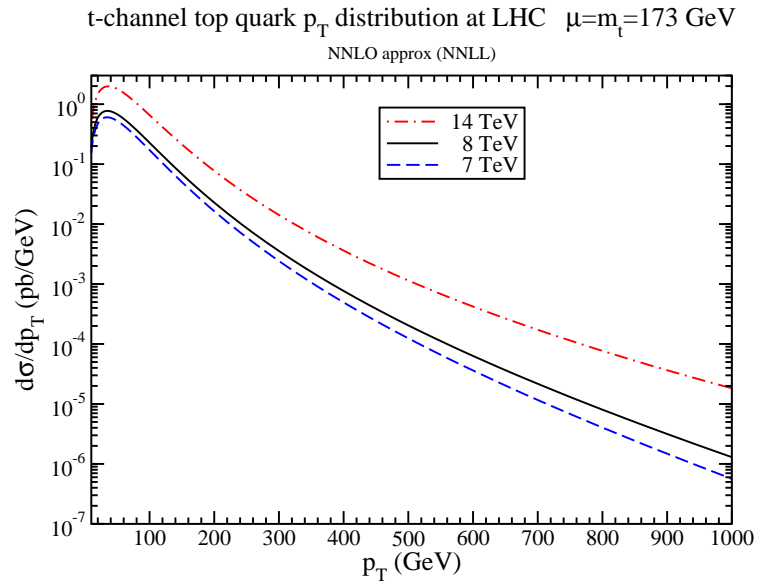
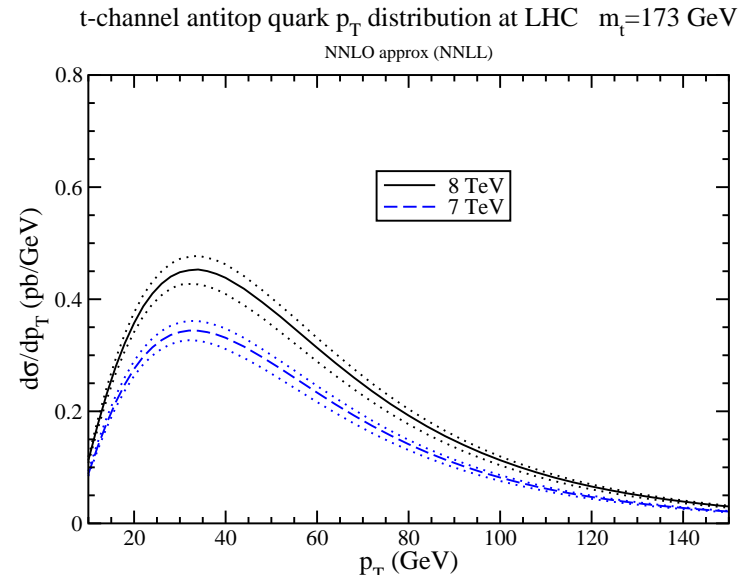
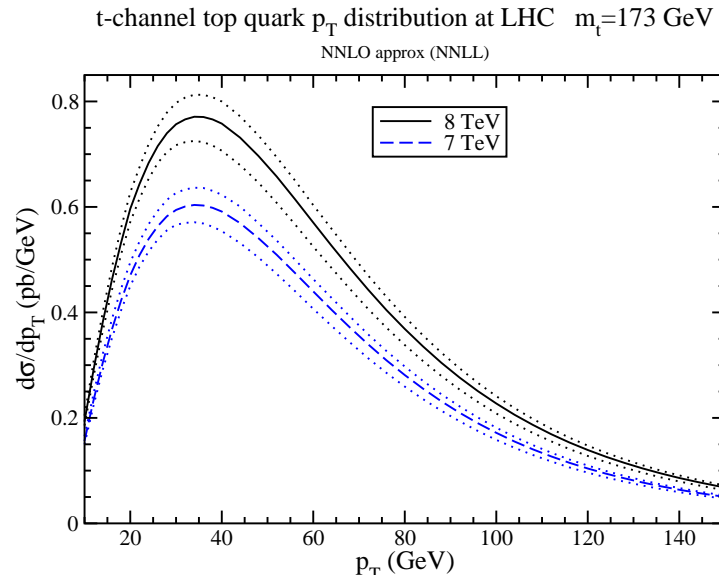
LHC	$t$	$\bar{t}$	Total (pb)
7 TeV	$43.0^{+1.6}_{-0.2} \pm 0.8$	$22.9 \pm 0.5^{+0.7}_{-0.9}$	$65.9^{+2.1+1.5}_{-0.7-1.7}$
8 TeV	$56.4^{+2.1}_{-0.3} \pm 1.1$	$30.7 \pm 0.7^{+0.9}_{-1.1}$	$87.2^{+2.8+2.0}_{-1.0-2.2}$
14 TeV	$154^{+4}_{-1} \pm 3$	$94^{+2+2}_{-1-3}$	$248^{+6+5}_{-2-6}$

$\pm$  scale  $\pm$  pdf errors with MSTW2008 NNLO pdf 90% CL

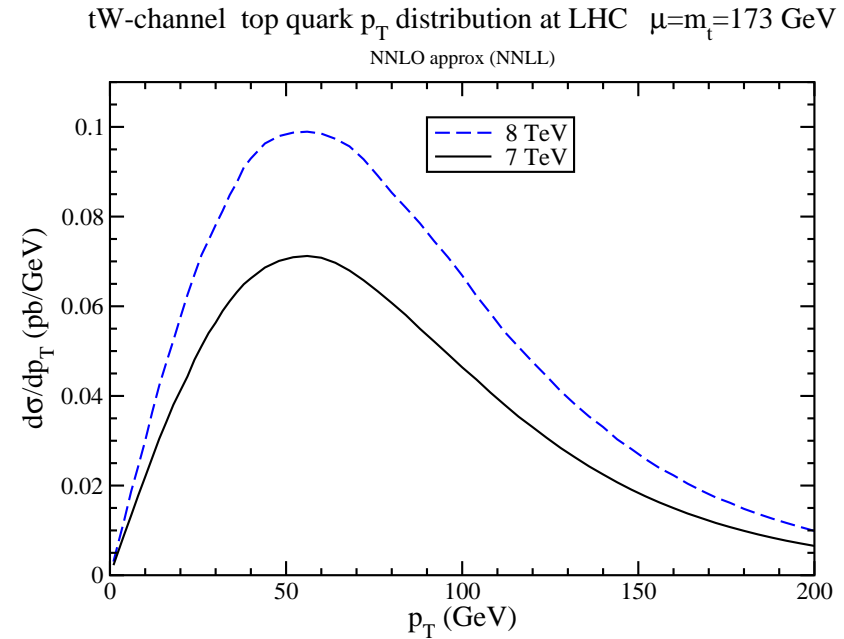
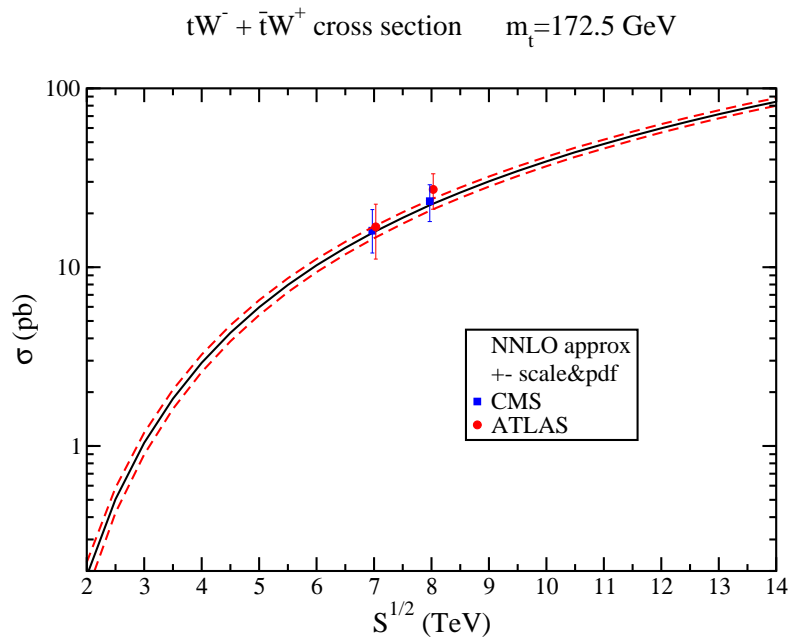
ratio  $\sigma(t)/\sigma(\bar{t}) = 1.88^{+0.11}_{-0.09}$  at 7 TeV - compares well with ATLAS result  $1.81^{+0.23}_{-0.22}$



## $t$ -channel top and antitop $p_T$ distributions at LHC



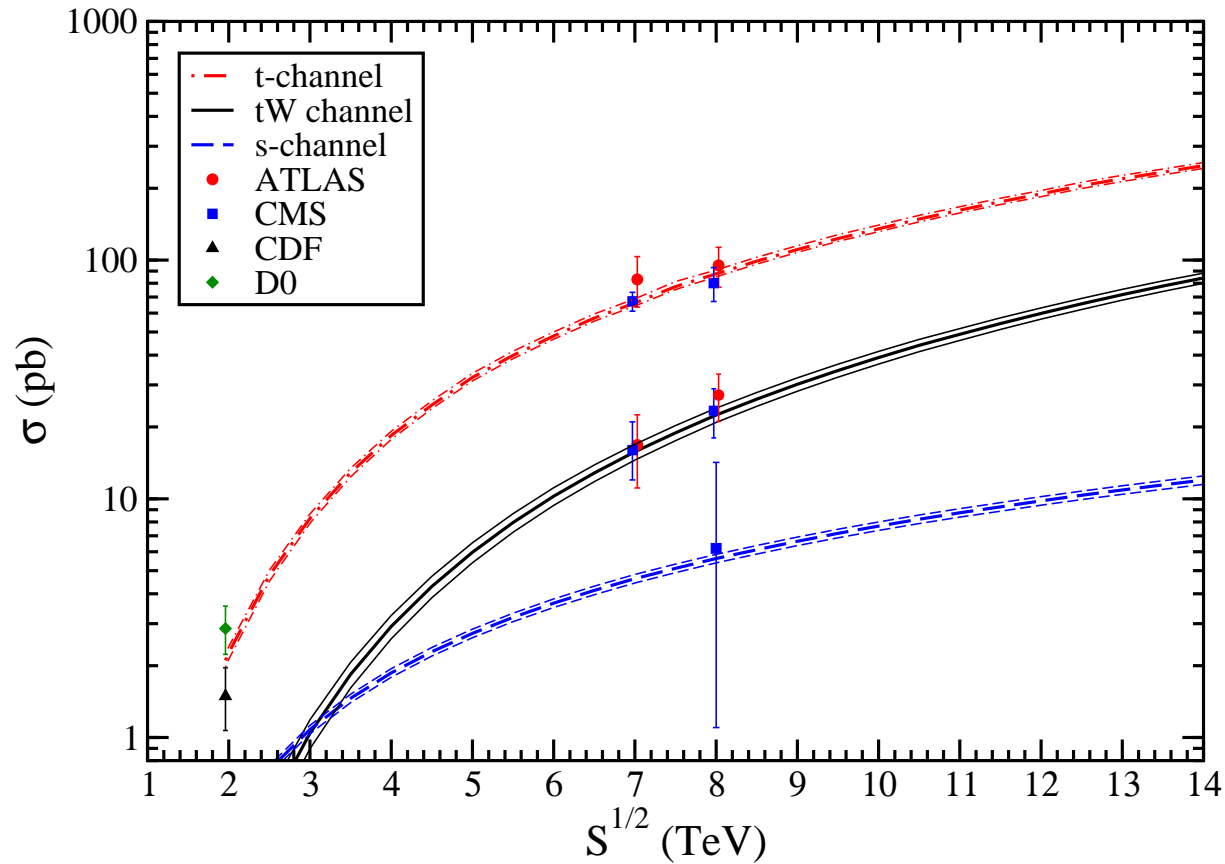
## Associated $tW^-$ production at the LHC



Cross section for  $\bar{t}W^+$  production is identical to  $tW^-$

## Single-top cross sections

NNLO approx single-top cross sections +-scale&pdf  $m_t=172.5$  GeV



Excellent agreement of theory with data for all three channels

## Summary

- NNLL soft-gluon corrections for top-pair and single-top production
- total cross sections
- top quark  $p_T$  and rapidity distributions
- NNLO approx corrections are significant at the LHC and the Tevatron
- excellent agreement with LHC and Tevatron data
- currently working on NNNLO soft-gluon corrections
- future work on more differential distributions