

Top mass measurement.

A summary of Tevatron and LHC results

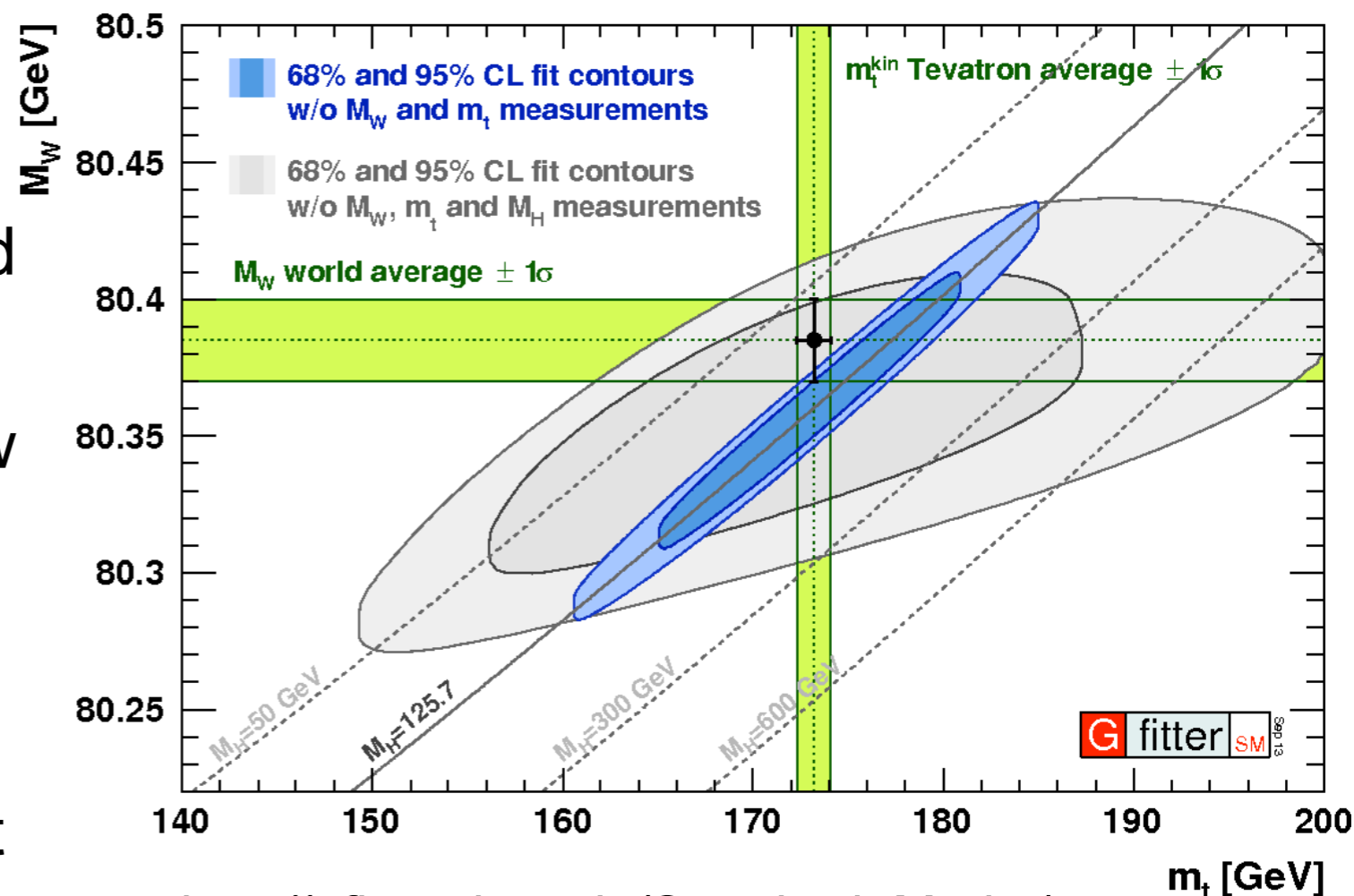
Karl-Johan Grahn, DESY

On behalf of the ATLAS, CMS, D0, and CDF collaborations

Aspen DM, January 2014

- > Why top mass?
- > What mass?
- > Tevatron and LHC: standard measurements
- > Tevatron and LHC: combinations
- > Mass from cross section
- > Alternative direct measurements
- > Measurements of top–anti-top mass difference
- > Conclusions

- Fundamental parameter of the Standard Model.
- Relationship between top, W and Higgs masses predicted.
- With H mass known, we can now check internal consistency.
- Useful constraint for future calibrations.
- Mass difference top–anti-top test of CPT invariance.



http://gfitter.desy.de/Standard_Model/

- > Top mass not an observable, but a parameter.
- > Value depends on chosen renormalization scheme.
- > "Conventional" measurements typically fit template distributions of Monte Carlo simulation to data.
- > Measures a "Monte Carlo mass", which can be argued to be equivalent to the pole mass within 0.5~1 GeV.
- > Alternative: Extract mass from comparison of experimental measurements to full NLO or NNLO calculations.

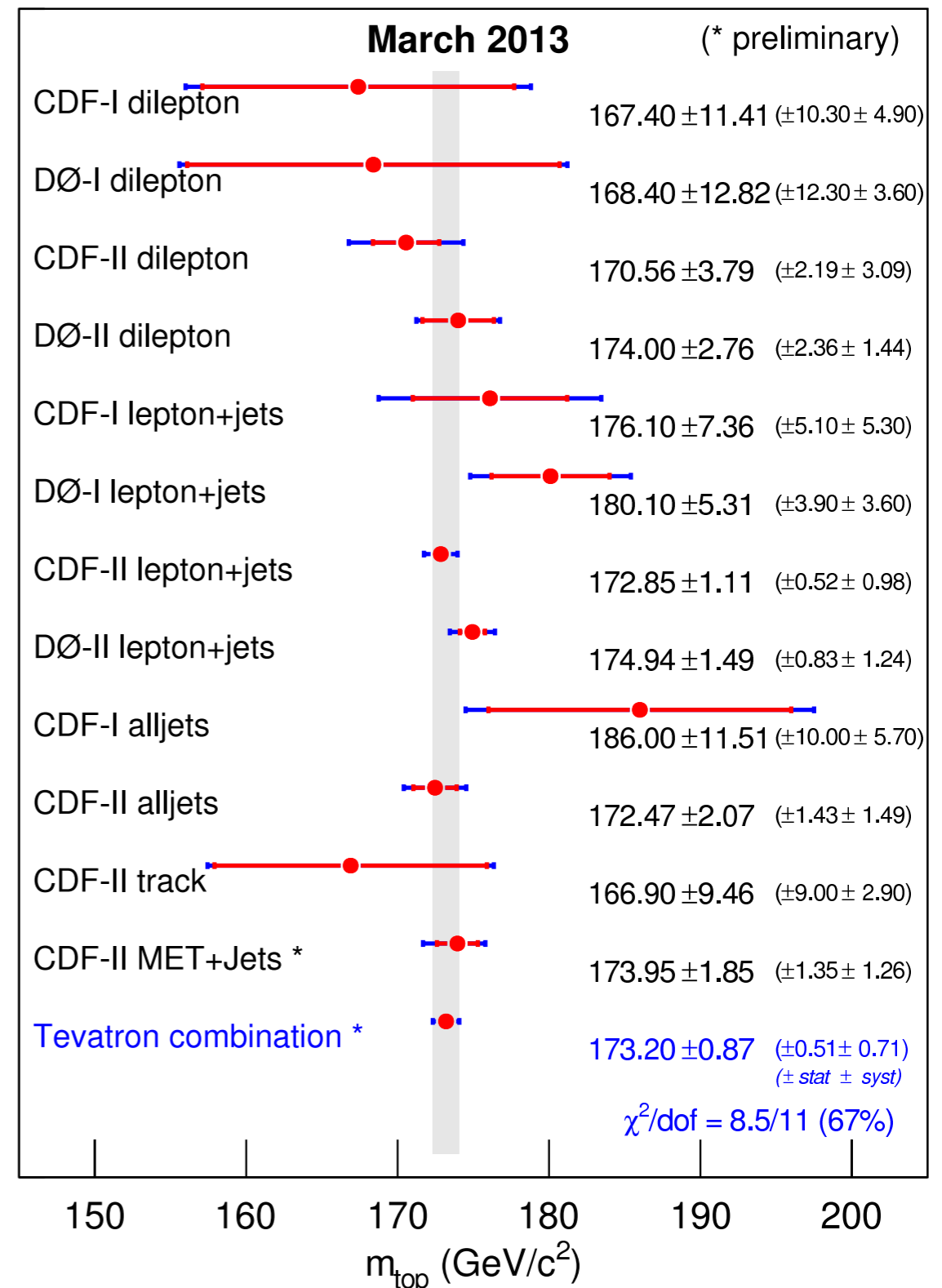
- > As usual for $t\bar{t}$ measurements, can be done in di-lepton, lepton+jets, and all-hadronic channels.
- > Lepton+jets channel providing best accuracy in both LHC and Tevatron.
- > Measurements (both Tevatron-II and LHC) generally limited by systematics.
- > LHC measurements thus still mostly using 2011 data (up to 5.0 fb^{-1}).
- > Tevatron
 - CDF-I dilepton, lepton+jets, all hadronic
 - CDF-II dilepton, lepton+jets, all hadronic, track, MET+jets
 - D0-I dilepton, lepton+jets
 - D0-II dilepton, lepton+jets
- > LHC
 - ATLAS dilepton, lepton+jets, all hadronic, delta m
 - CMS dilepton, lepton+jets, all hadronic, delta m, kinematic endpoints, B hadron lifetime



- > Large number of measurements performed by D0 and CDF.
- > Runs I and II.
- > Up to 8.7 fb^{-1} per experiments.
- > Most precise measurements in lepton +jets channel.
- > Combined using BLUE method (details later).
- > 2013 combination updated with respect to 2011: CDF-II l+jets and CDF-II MET +Jets using full 8.7 fb^{-1} data set.

[arXiv:1305.3929](http://arxiv.org/abs/1305.3929), <http://tevewwg.fnal.gov>

Mass of the Top Quark



ATLAS lepton+jets

> World's first measurement constraining JES and b JES in simultaneous fit with m_t .

> Full 2011 data set (4.7 fb^{-1}).

> Require:

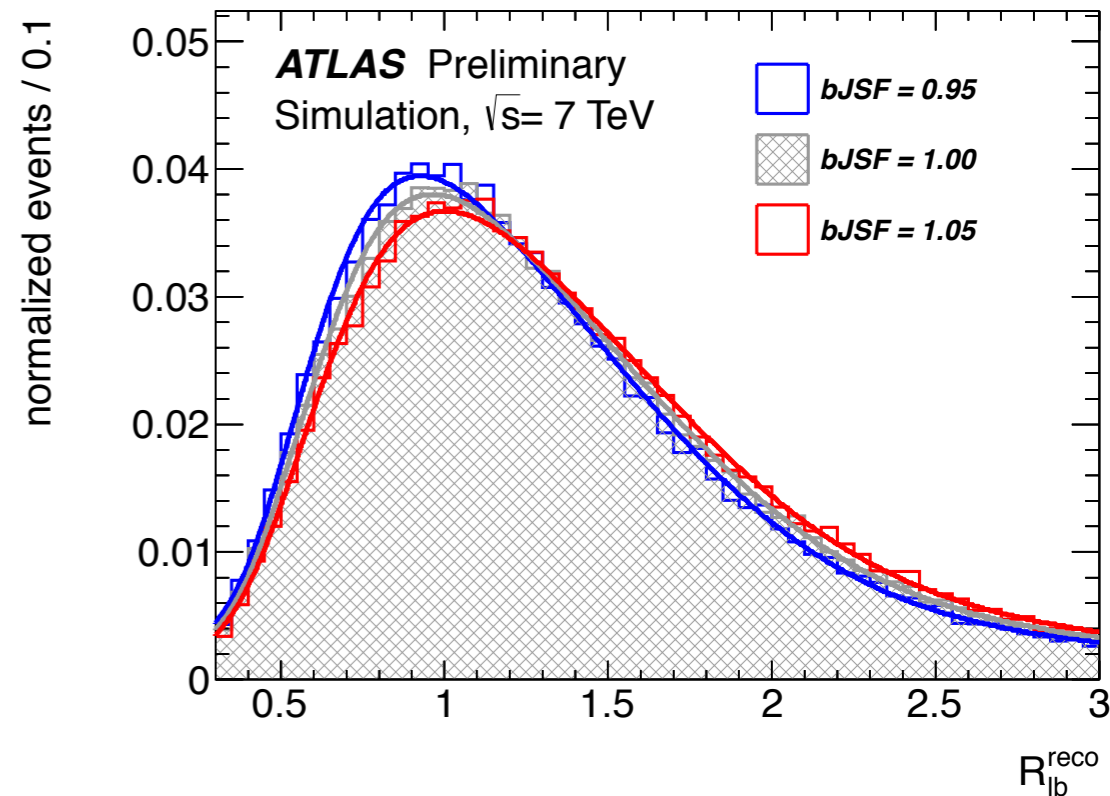
- 1 lepton
- 4 jets, of which at least one b -tagged
- $E_{T,\text{miss}}$
- $m_{T,W}$ (el channel) or $m_{T,W} + E_{T,\text{miss}}$ (mu channel)

> Full event reconstruction through kinematic likelihood fit using parton-jet transfer functions.

> 3D template fit in

- $m^{\text{reco}}_{\text{top}}$
- m^{reco}_W
- R^{reco}_{lb}

constrains the relative ratio of the b JES and overall JES

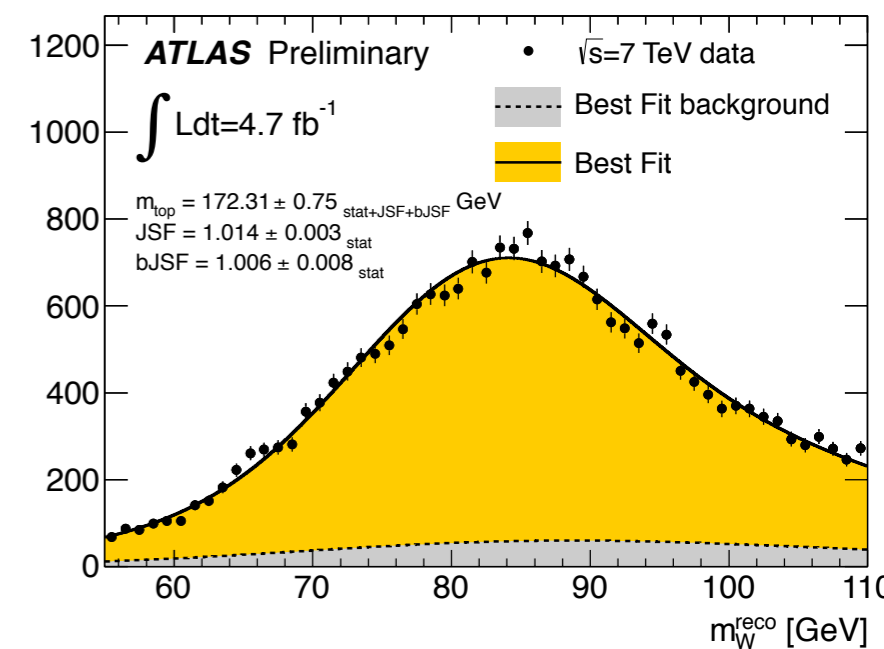
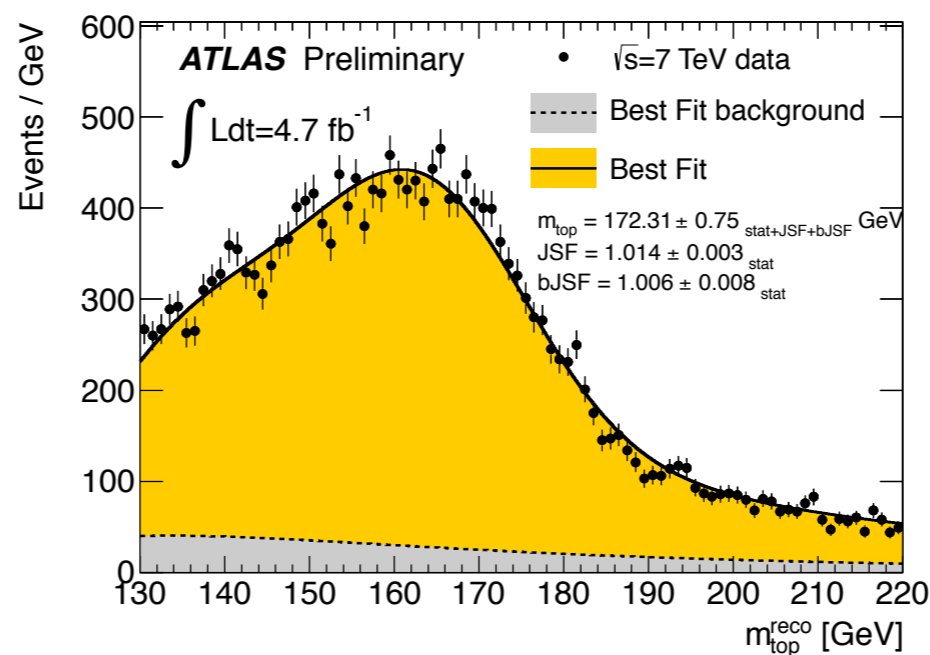
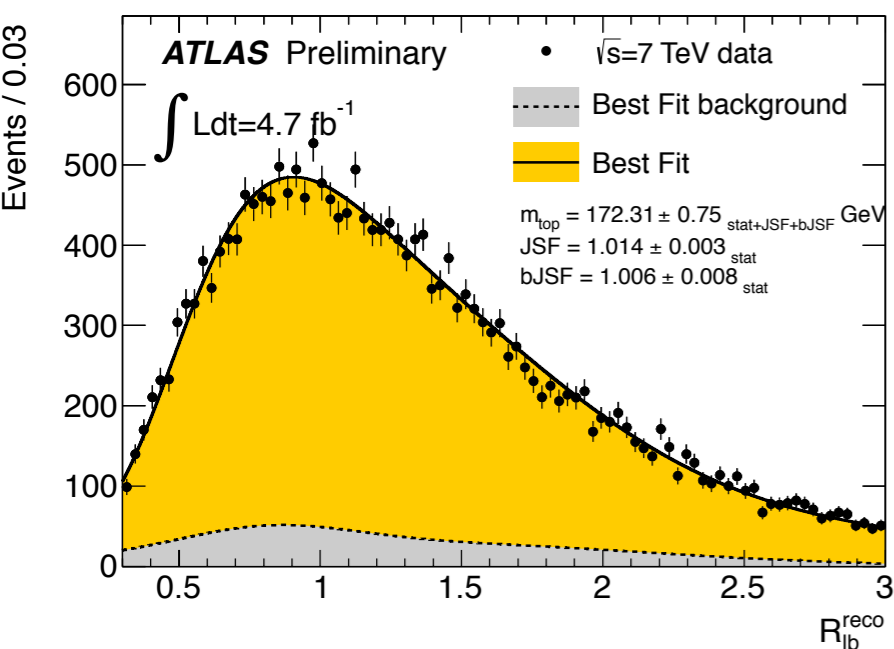


ATLAS-CONF-2013-046

$$R_{lb}^{\text{reco},2b} = \frac{p_T^{b_{\text{had}}} + p_T^{b_{\text{lep}}}}{p_T^{W_{\text{jet}1}} + p_T^{W_{\text{jet}2}}}$$

$$R_{lb}^{\text{reco},1b} = \frac{p_T^{b_{\text{tag}}}}{(p_T^{W_{\text{jet}1}} + p_T^{W_{\text{jet}2}})/2}$$

Fitted distributions



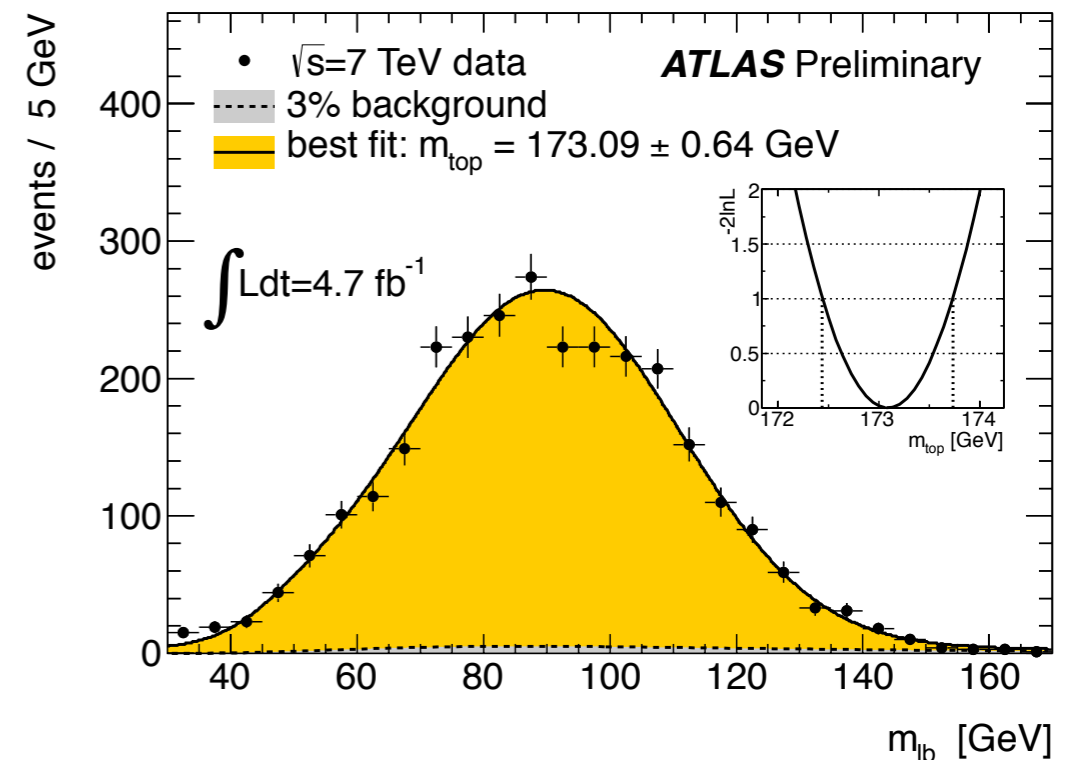
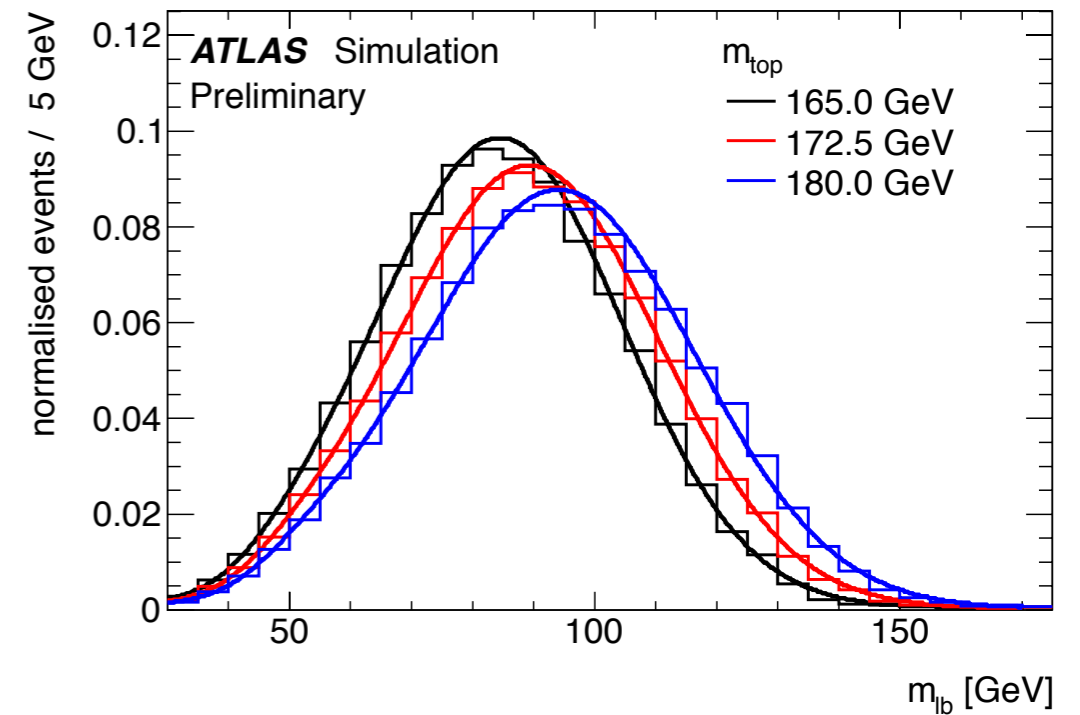
- > Jet energy scale uncertainty considerably constrained (but still one of the largest)
- > Other dominating uncertainties: modeling, b-tagging

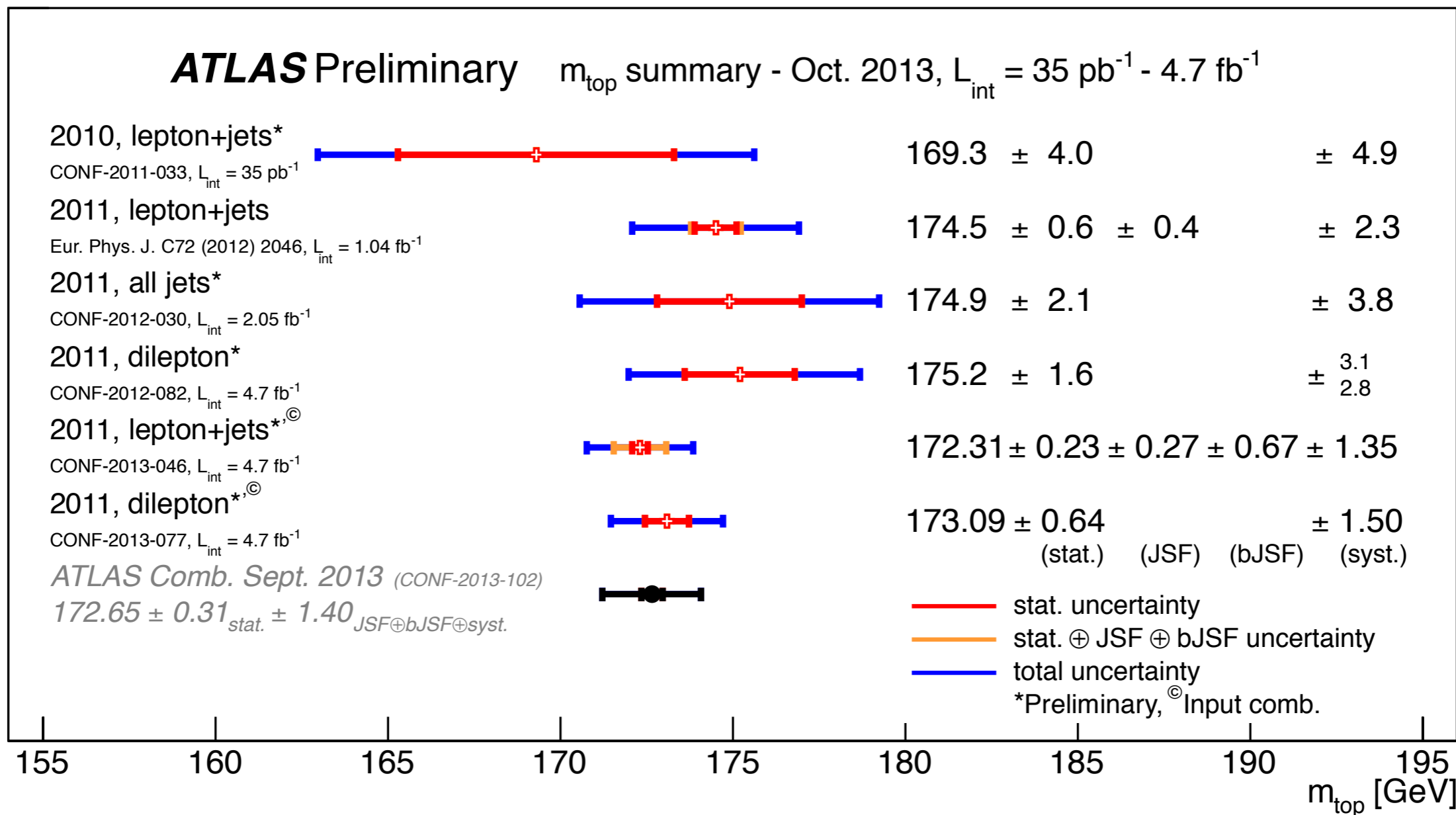
ATLAS-CONF-2013-046

**172.31 ± 0.75 (stat + JSF + bJSF) ± 1.35 (syst) GeV, or
 172.31 ± 0.23 (stat) ± 0.27 (JSF) ± 0.67 (bJSF) ± 1.35 (syst) GeV**

- > Full 2011 data set (4.7 fb^{-1}).
- > Require:
 - 2 leptons
 - 2 b-tagged jets
 - E_{miss} (ee/mumu) or HT (emu)
- > Consider m_{lb} (lepton–b-jet invariant mass). Assignment with lowest average picked (77% correct).
- > One-dimensional template fit.
- > Very pure sample: only 3% background (almost only single top).
- > Dominant systematics: JES, bJES, b-tagging.

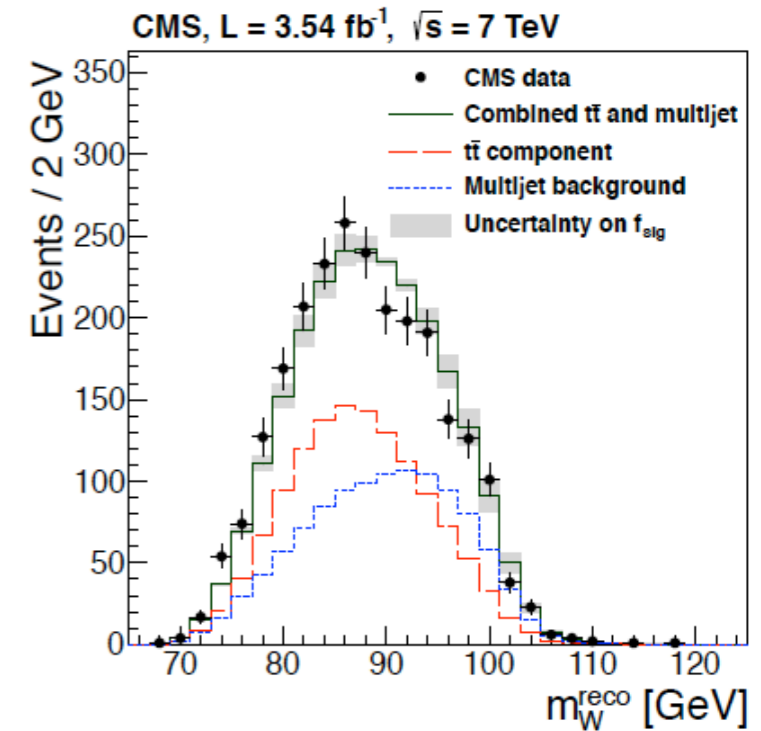
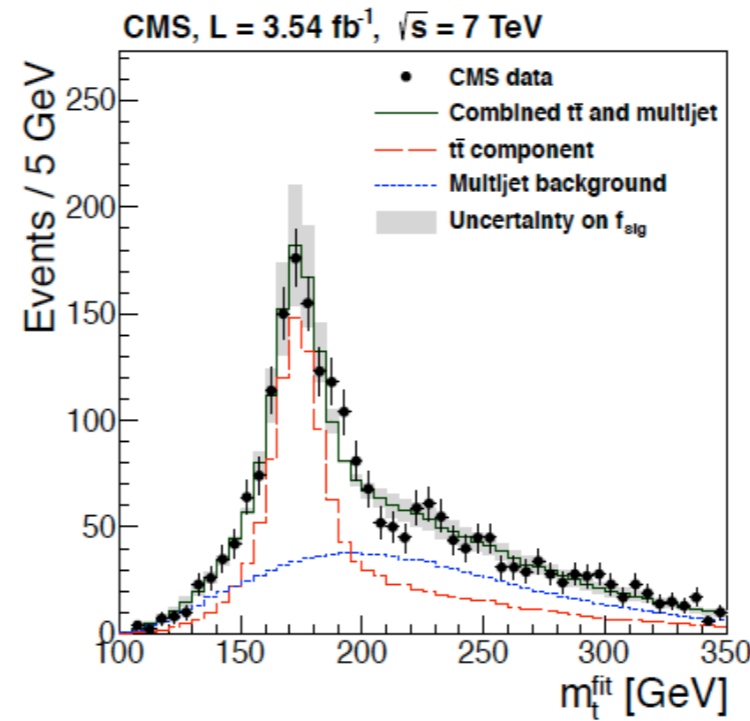
$173.09 \pm 0.64 \text{ (stat)} \pm 1.50 \text{ (syst)} \text{ GeV}$





- > 3.54 fb⁻¹ from 2011.
- > Require
 - 6 jets
 - 2 of which b-tagged.
- > Multi-jet background obtained by mixing events.
- > Top mass reconstructed directly through kinematic fit.
- > Likelihood constructed with ideogram method.

$$\prod_{\text{events}} P\left(m_t^{\text{fit}}, m_W^{\text{reco}} \mid m_t, \text{JES}\right)^{w_{\text{event}}}$$



Dominant uncertainties: JES, bJES, modeling

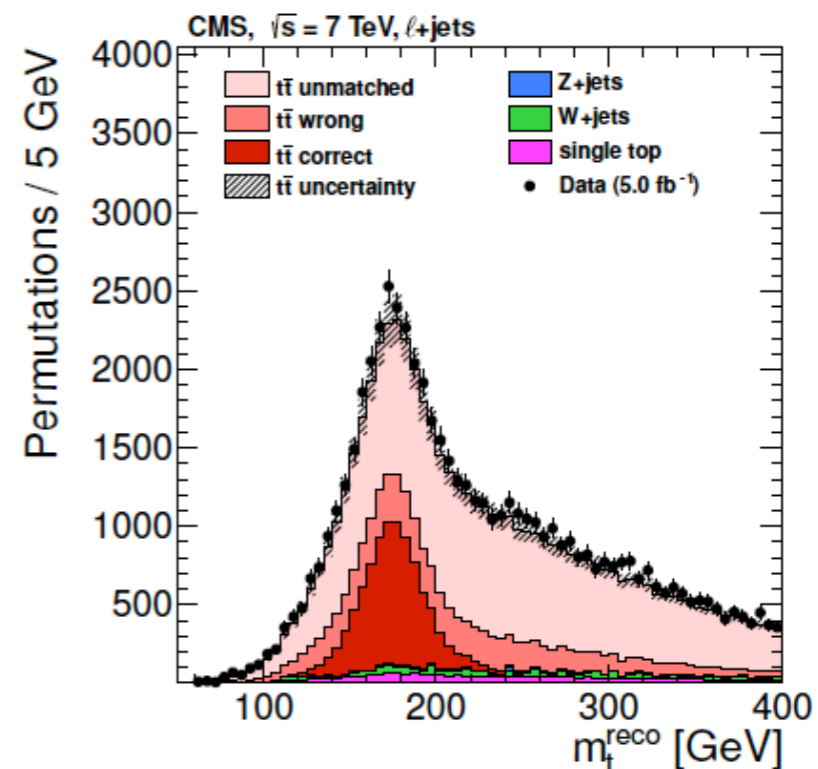
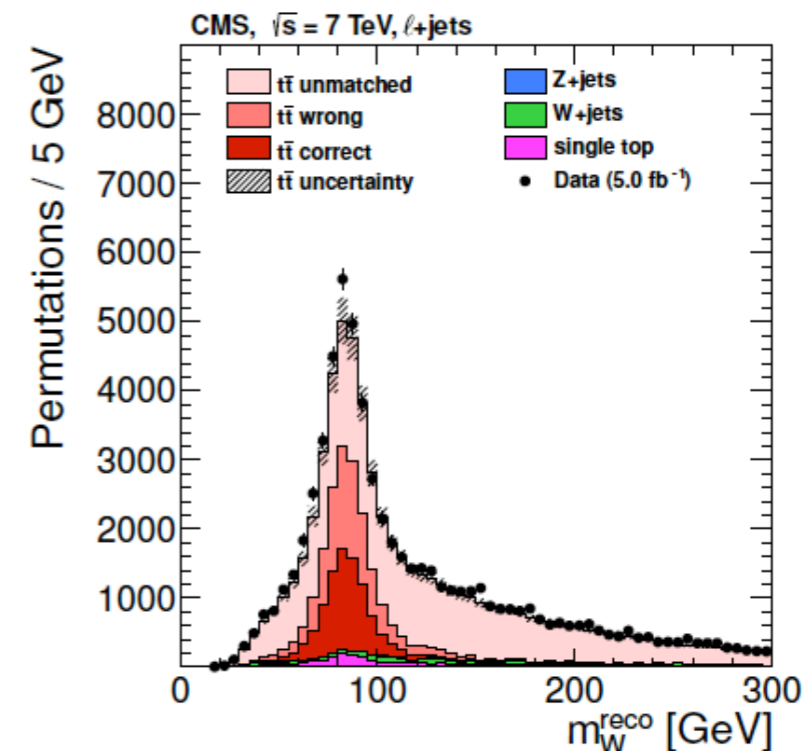
**174.28 ± 1.00 (stat+JES) ± 1.23 (syst) GeV, or fixing JES,
173.49 ± 0.69 (stat) ± 1.21 (syst) GeV**

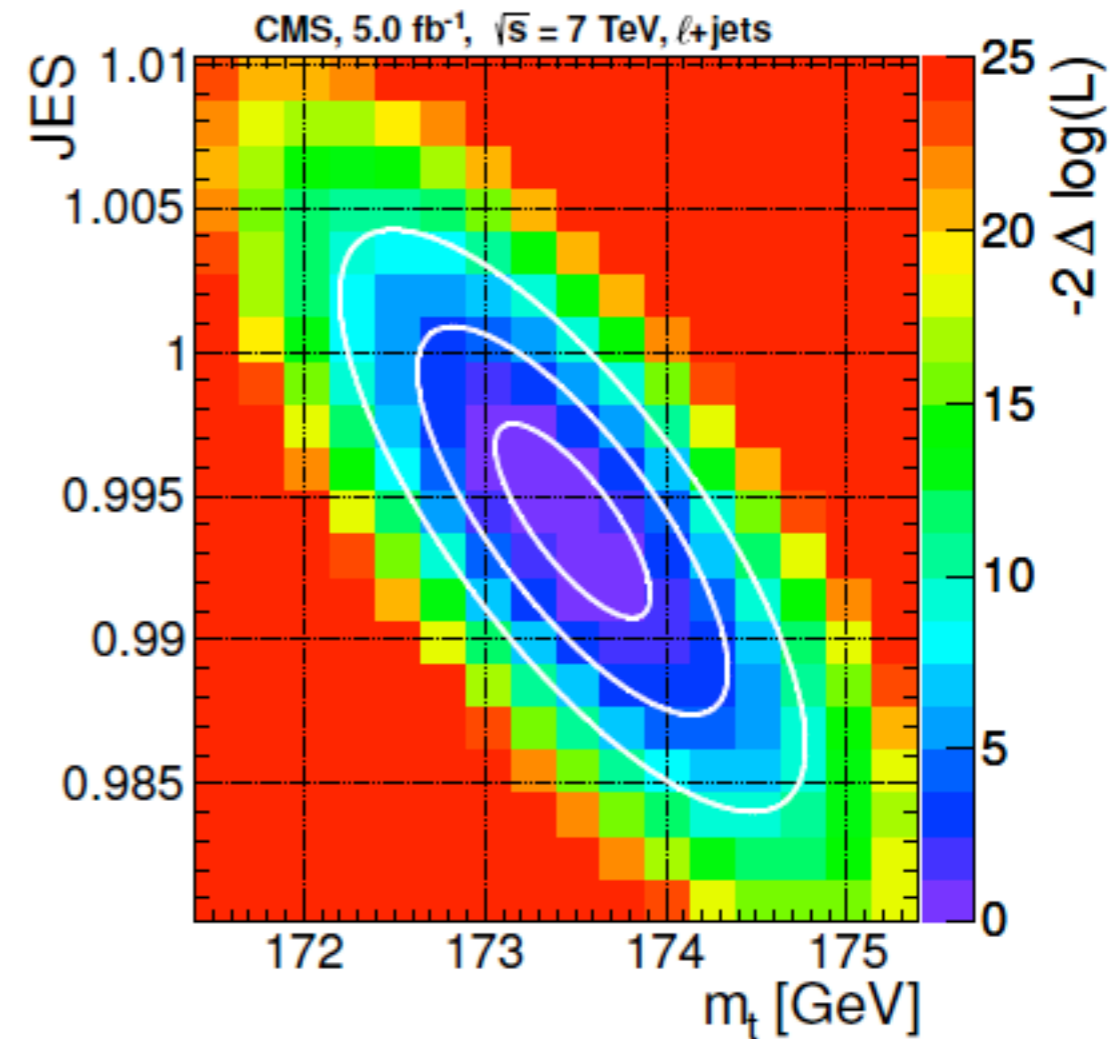
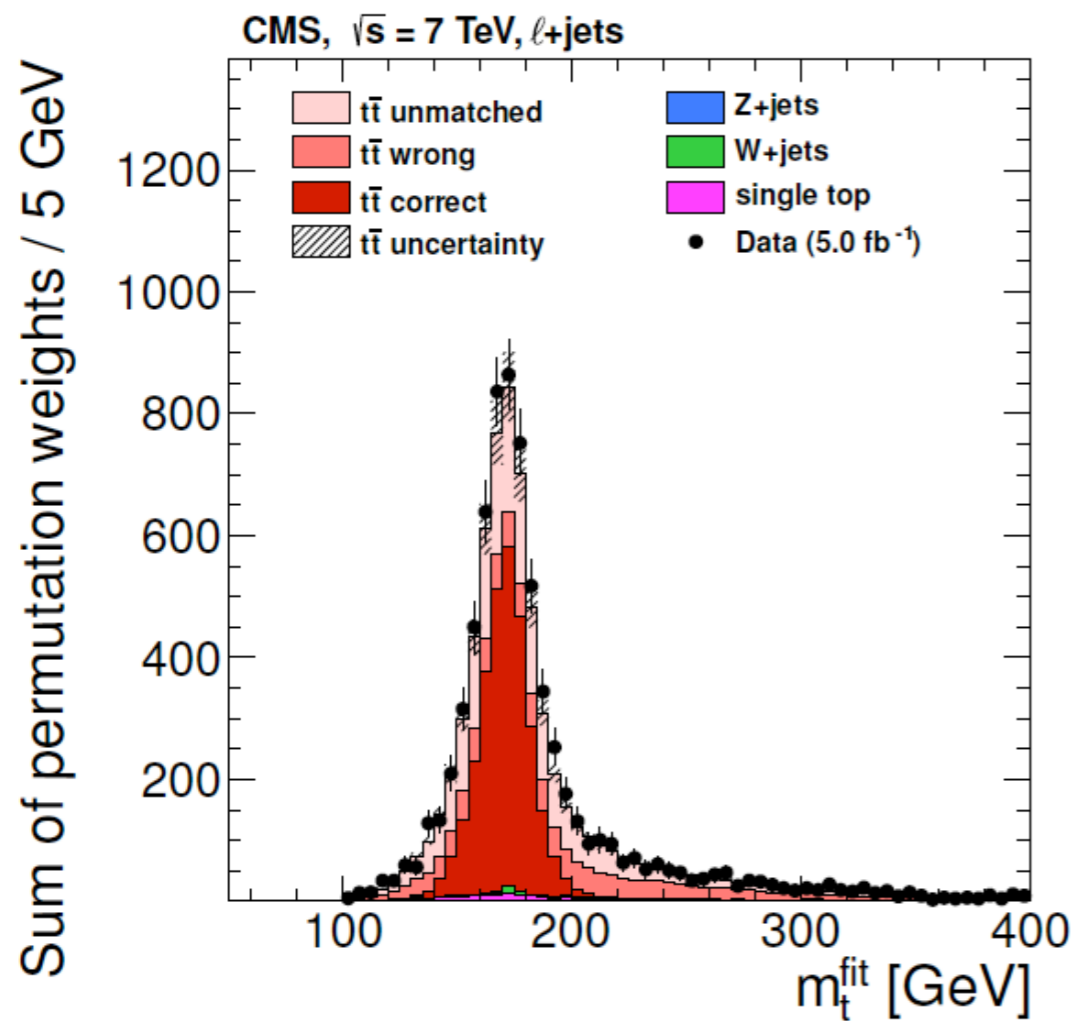
CMS-TOP-11-017, submitted to Eur. Phys. J. C, July 2013

- > Full 2011 data set (5.0 fb⁻¹).
- > Require:
 - 1 lepton
 - 4 or more jets (2 or more b-tagged)
- > Kinematic fit, cut on goodness of fit.
- > Ideogram method, weighting with goodness of fit

$$\prod_{\text{events}} \left(\sum_{i=1}^n c P_{\text{gof}}(i) P \left(m_{t,i}^{\text{fit}}, m_{W,i}^{\text{reco}} | m_t, \text{JES} \right) \right)^{w_{\text{event}}}$$

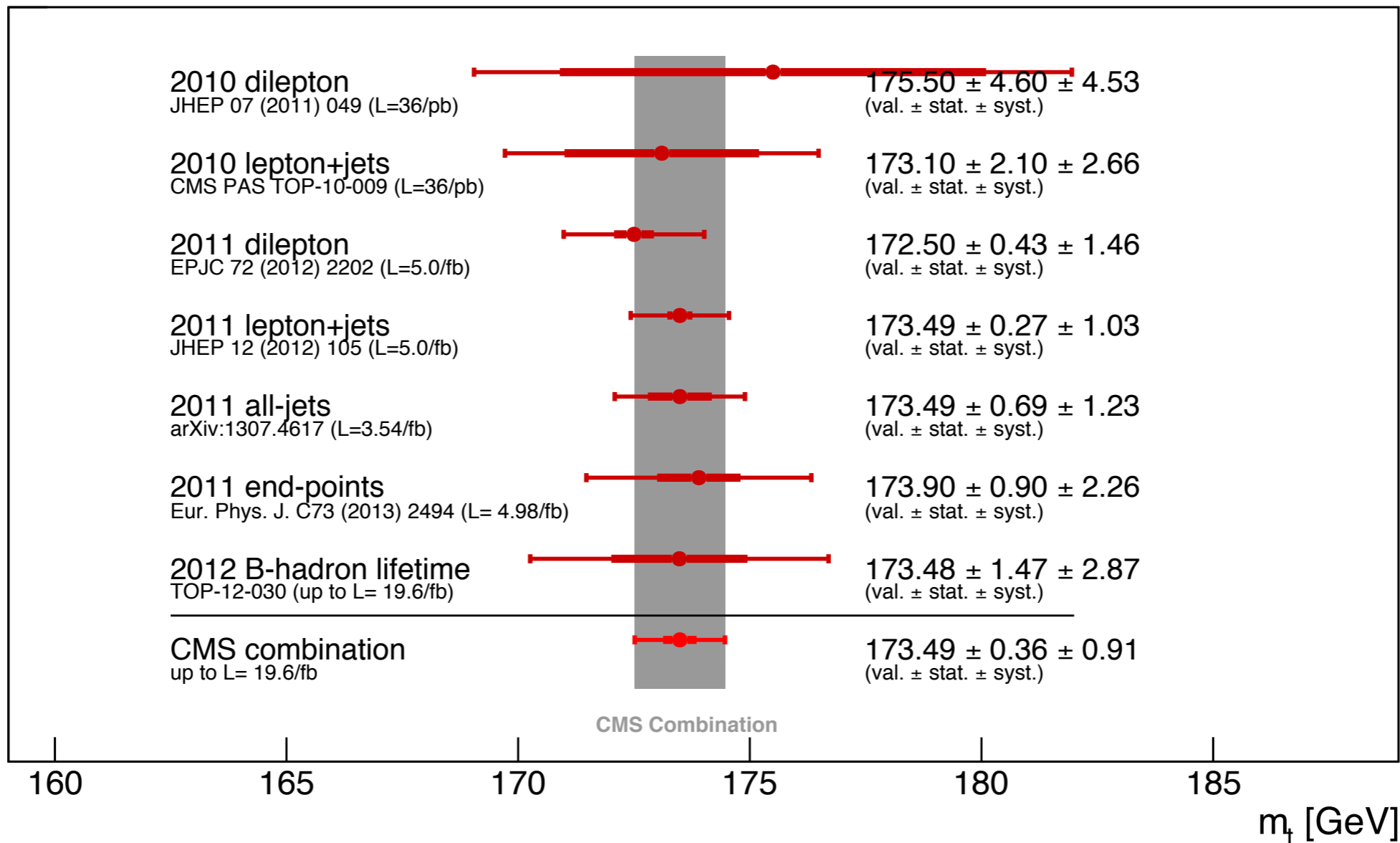
- > Constraining JES.
- > Most precise measurement to date.





173.49 ± 0.43 (stat+JES) ± 0.98 (syst) GeV

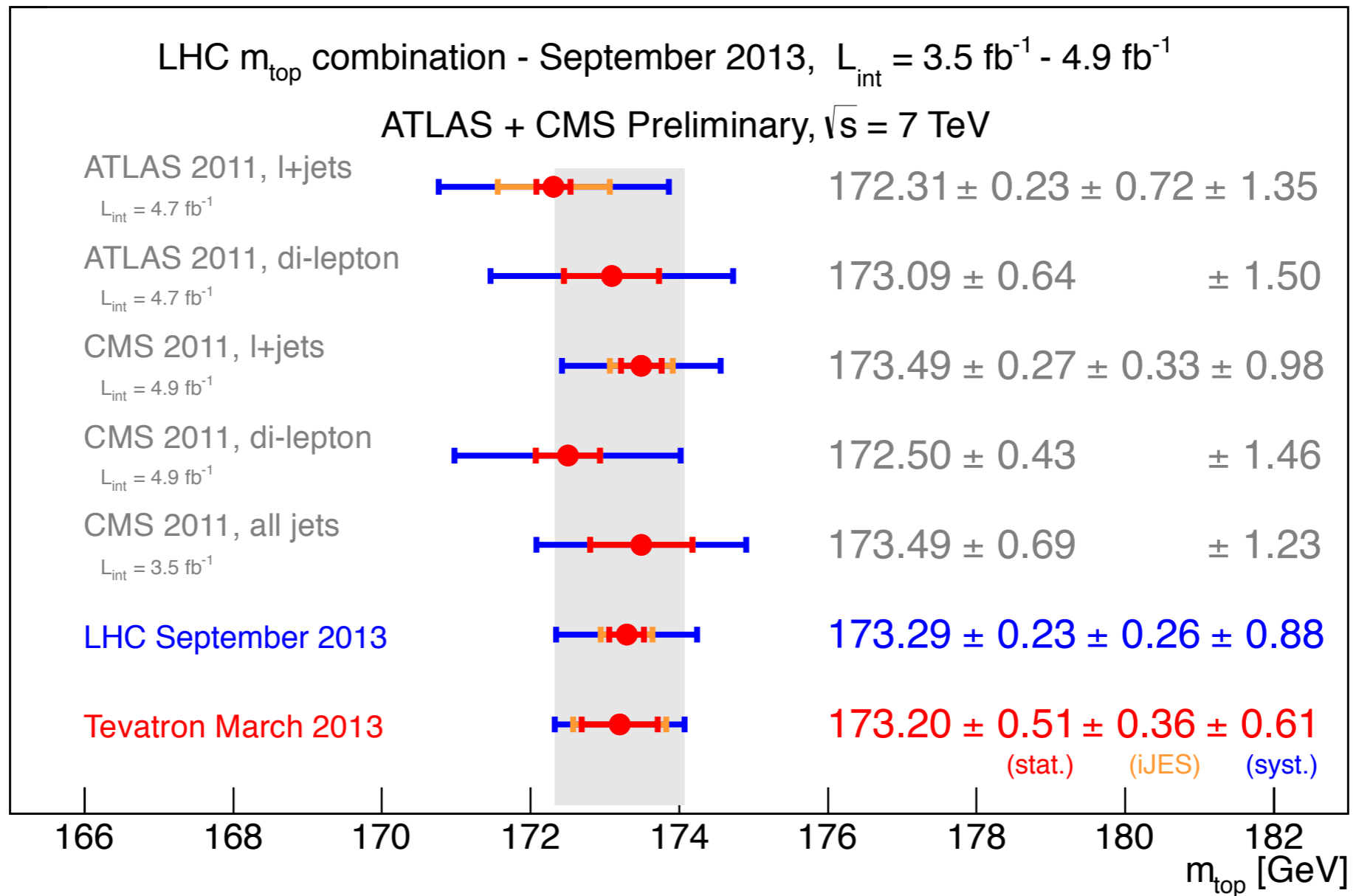
CMS Preliminary, $\sqrt{s} = 7$ and 8 TeV



CMS-TOP-13-002,
September 2013



- > **Best Linear Unbiased Estimate.**
- > Used for both Tevatron and LHC combinations.
- > Linear combination of measurements; weights optimized to minimize uncertainty on combined result.
- > Correlations between systematic uncertainty sources taken into account.
 - Careful categorization of, e.g., JES uncertainties.
 - Coordinated through top LHC working group.
- > Tested varying assumptions on correlations, found to be stable.
- > Further study needed: ATLAS takes explicit hadronization systematic uncertainty (difference between Herwig and Pythia) into account, which CMS doesn't.



ATLAS-CONF-2013-102
 CMS PAS TOP-13-005

Summary of best values

Single most precise measurements, per experiment

> CDF-II (l+jets)	172.85	± 0.52 (stat)	± 0.98 (syst)	GeV
> D0-II (l+jets)	174.94	± 0.83 (stat)	± 1.24 (syst)	GeV
> ATLAS (2011, l+jets)	172.31	± 0.23 (stat)	± 1.53 (syst)	GeV
> CMS (2011, l+jets)	173.49	± 0.27 (stat)	± 1.03 (syst)	GeV

Combinations

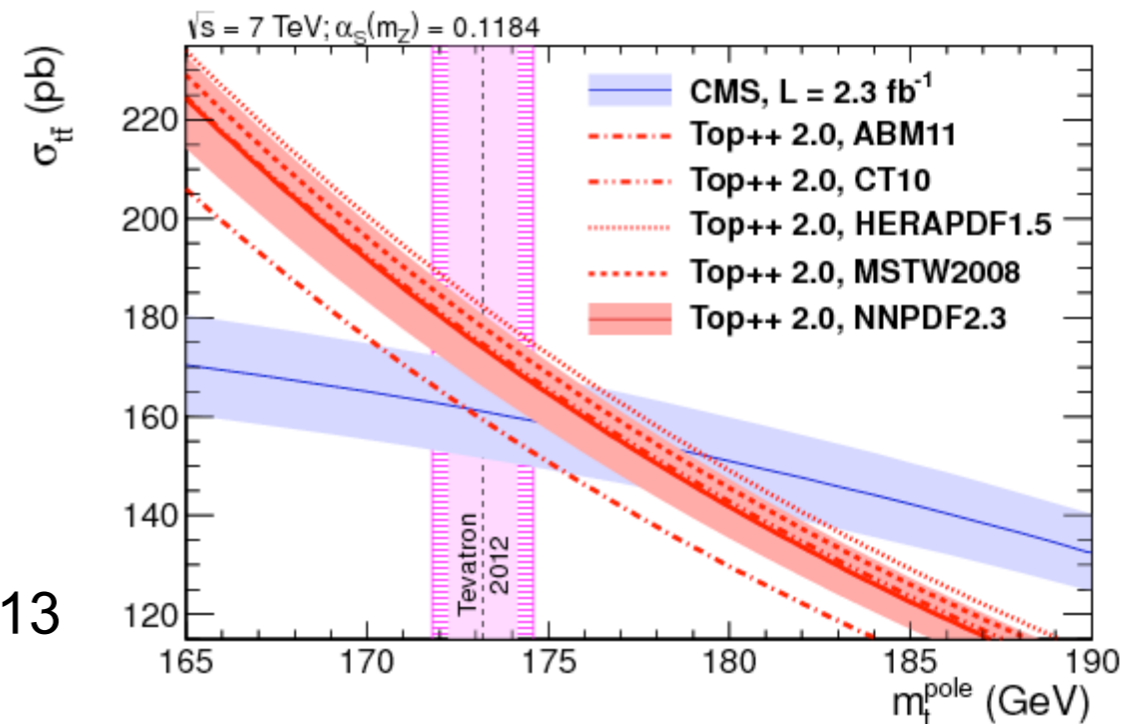
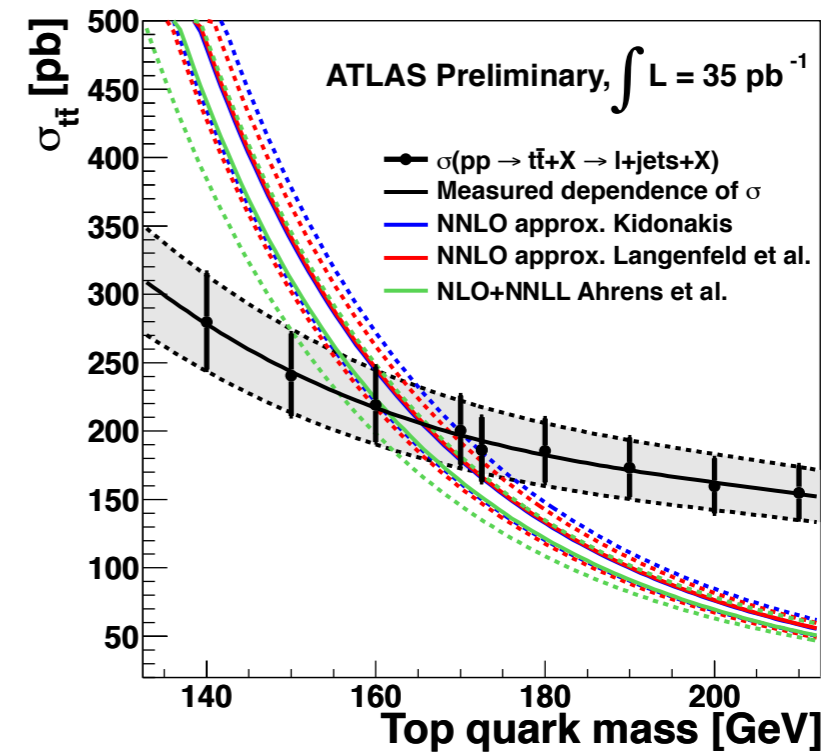
> Tevatron (Aug 2013)	173.20	± 0.51 (stat)	± 0.71 (syst)	GeV
> ATLAS (Sep 2013)	172.65	± 0.31 (stat)	± 1.40 (syst)	GeV
> CMS (Sep 2013)	173.49	± 0.36 (stat)	± 0.41 (syst)	GeV
> LHC (Sep 2013)	173.29	± 0.51 (stat)	± 0.92 (syst)	GeV

Mass from cross section

- > Extract mass from comparison of dependence of cross section on top mass in experiment and in NLO or NNLO calculations. Alternative to direct measurement.
- > Advantage: Extract mass in well-defined renormalization scheme.
- > Disadvantage: Less precise.
- > Values of $m_{t,\text{pole}}$

- D0 $167.5^{+5.4}_{-4.9}$ GeV ($\sim 3\%$, 5.3 fb^{-1})
- ATLAS $166.4^{+7.8}_{-7.3}$ GeV ($\sim 5\%$, 35 pb^{-1})
- CMS $176.7^{+3.8}_{-3.4}$ GeV ($\sim 2\%$, 2.3 fb^{-1})

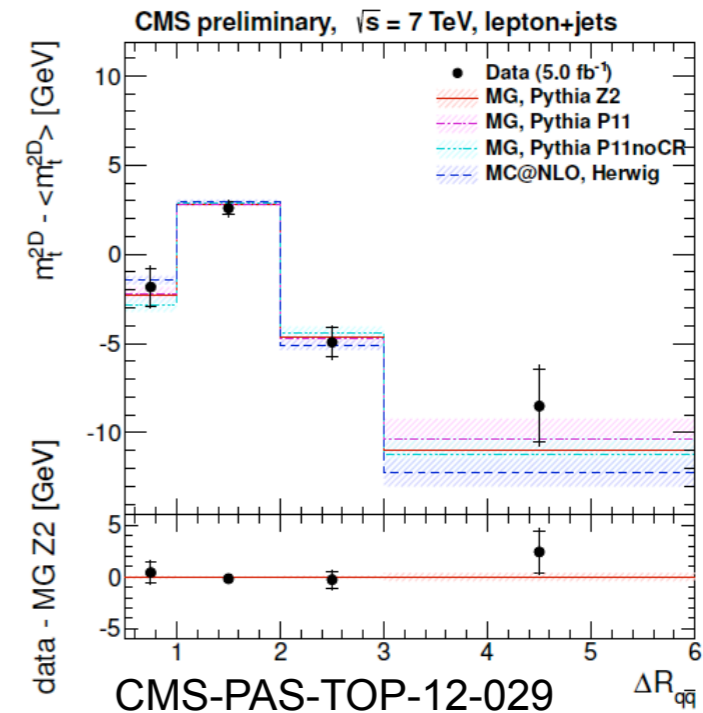
ATLAS-CONF-2011-054 March 2011
 CMS TOP-12-022, Phys. Lett. B 728 (2013) 496, July 2013
 D0 PLB 703, 422 (2011)



Alternative methods for direct measurement (I)

> Study of dependence on kinematic variables (CMS)

- Study the dependence of reconstructed mass on kinematic variables, e.g., related to ISR/FSR and color reconnection.
- Data results well described by simulation.
- Within available statistics, models cannot be distinguished.



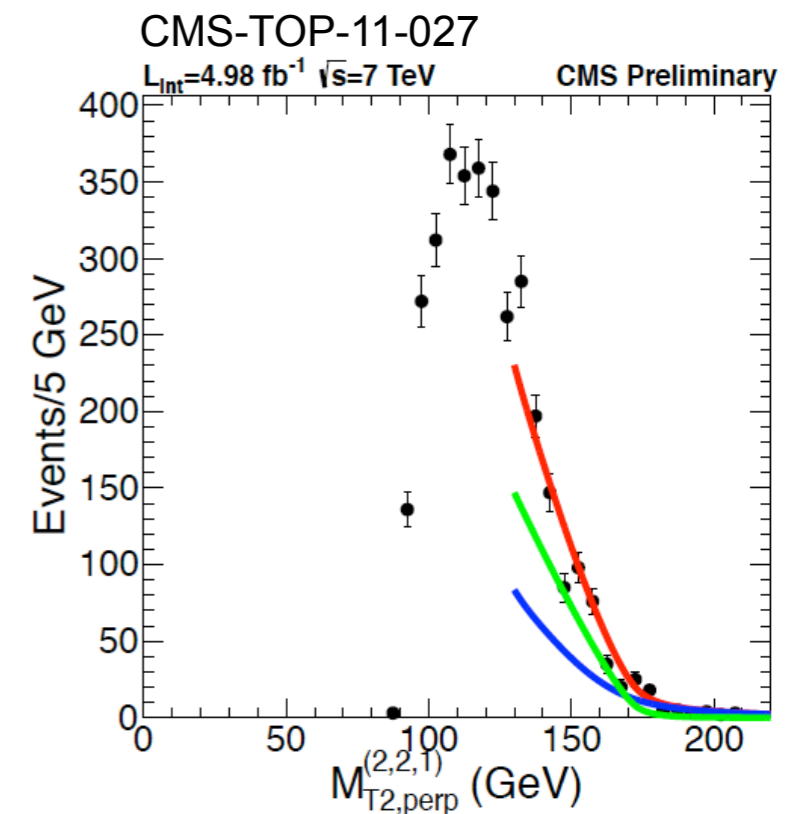
> Kinematic endpoint method (CMS)

- Use endpoint distribution of M_{T2} : minimum parent mass consistent with the observed kinematics

$$M_{T2} \equiv \min_{\mathbf{p}_T^a + \mathbf{p}_T^b = \mathbf{E}_T} \left\{ \max(M_T^a, M_T^b) \right\}$$

- Dominating systematics: JES
- Performance comparable to di-lepton standard measurements.

173.9 ± 0.9 (stat) + 1.2 - 1.8 (syst) GeV





> B hadron lifetime

- Lifetime and decay length depends directly on top quark mass.
- Advantage: Low dependence on jet energy scale, instead on tracking.
- Disadvantage: Sensitive to b fragmentation modeling.
- Measured by CDF-II and CMS.

20 fb⁻¹ 2012 data! CMS-PAS-TOP-12-030

Channel	m_t [GeV]
muon+jets	$173.2 \pm 1.0_{\text{stat}} \pm 1.6_{\text{syst}} \pm 3.3_{p_T(t)}$
electron+jets	$172.8 \pm 1.0_{\text{stat}} \pm 1.7_{\text{syst}} \pm 3.1_{p_T(t)}$
electron-muon	$173.7 \pm 2.0_{\text{stat}} \pm 1.4_{\text{syst}} \pm 2.4_{p_T(t)}$

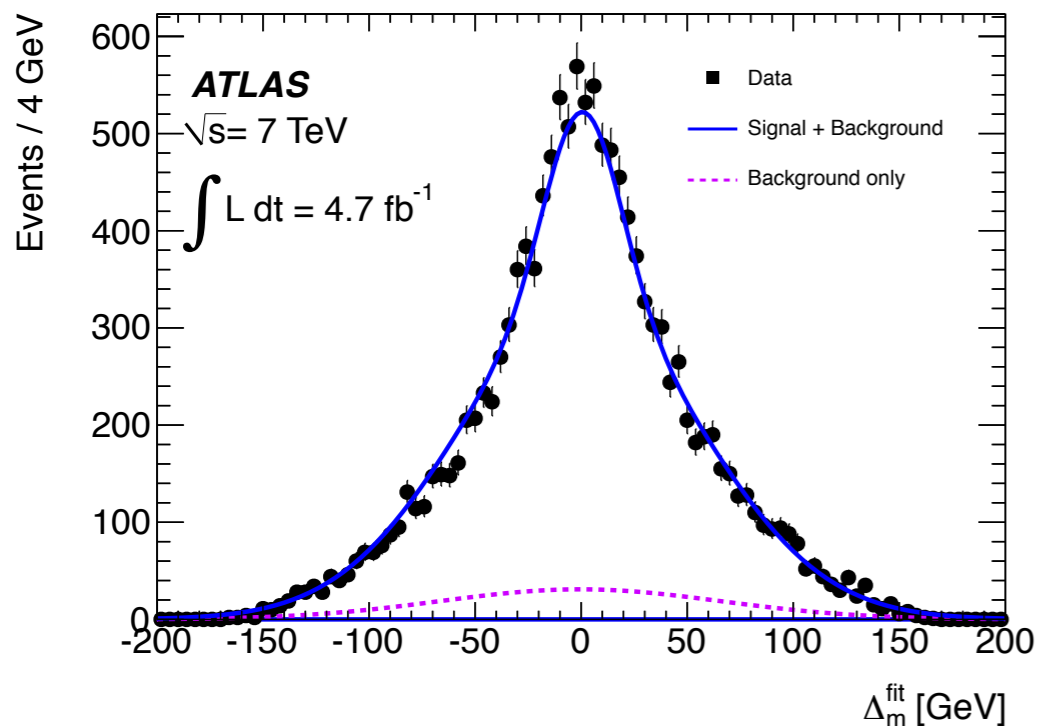
$$m_t = 173.5 \pm 1.5_{\text{stat}} \pm 1.3_{\text{syst}} \pm 2.6_{p_T(t)} \text{ GeV,}$$

> Other proposed alternative measurements

- J/ψ +jets: Use invariant mass of leptons from W and J/ψ (from b fragmentation) $\rightarrow \mu\mu$. Experimentally clean, but low branching ratio.
- $t\bar{t}$ +jets

Top-anti-top mass difference: test of CPT invariance

- > ATLAS: Recently published!
- > 2011 data, lepton+jets channel
- > Template fit.



$\Delta m = 0.67 \pm 0.61$ (stat)
 ± 0.41 (syst) GeV

Physics Letters B 728C
(2014), pp. 363-379

- > CMS: 2011 (5.0 fb⁻¹) and 2012 (18.9 fb⁻¹) data.
- > lepton+jets channel.
- > Ideogram method.

$\Delta m = -0.44 \pm 0.46$ (stat)
 ± 0.27 (syst) GeV (2011)

$\Delta m = -0.27 \pm 0.20$ (stat)
 ± 0.12 (syst) GeV (2012)

2011: TOP-11-019, JHEP 06 (2012) 109
2012: TOP-12-031

No significant deviation
from zero observed.

- LHC and Tevatron measurements/combinations compatible and have equivalent accuracy (both $\sim 0.5\%$).
- Systematics limited already with full 2011 data set. Some potential for improvement in even better understanding of detectors and modeling. Central is understanding and constraining of jet energy scale. b-tagging.
- Alternative methods with different systematics are being investigated.
- No mass difference observed between top and anti-top.
- Considerable ongoing work on refining combinations. Understanding correlations between experiments. Moving towards Tevatron+LHC world average.

BACKUP

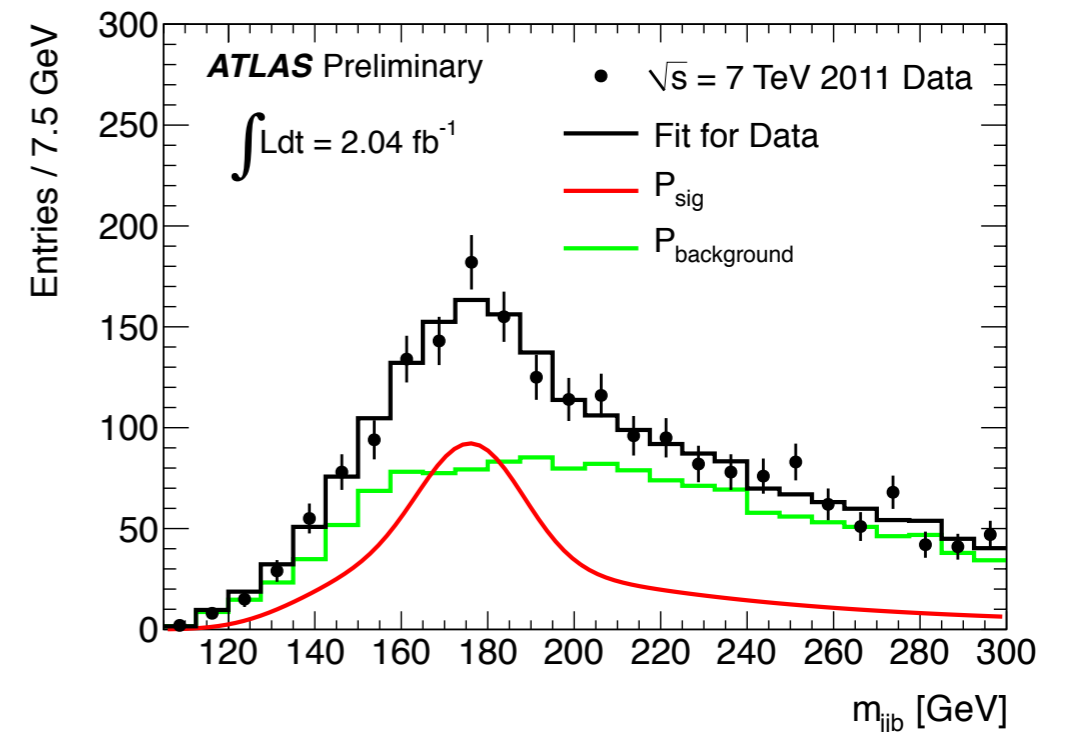
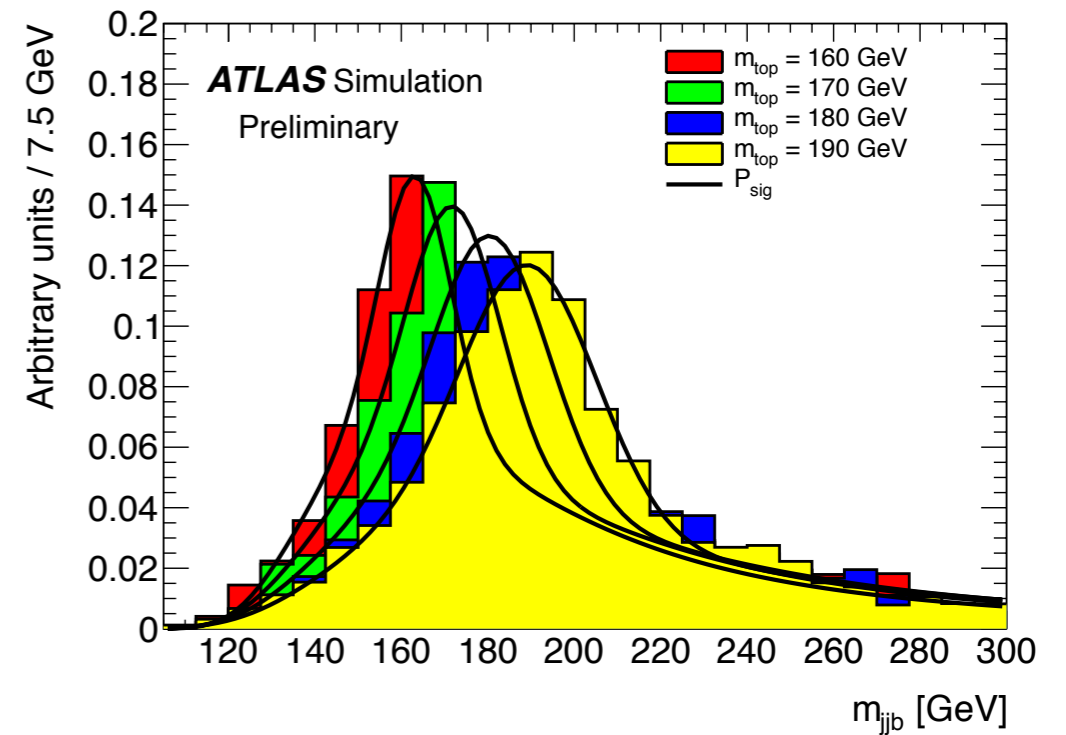
ATLAS all-hadronic

- > 2.04 fb⁻¹ from 2011.
- > Require
 - 6 jets
 - 2 of which b-tagged.
- > Multi-jet background obtained by mixing events.
- > Jets assigned to top decay products by minimizing "mass chi2".

$$\chi^2 = \frac{(m_{j_1, j_2} - m_W)^2}{\sigma_W^2} + \frac{(m_{j_1, j_2, b_1} - m_t)^2}{\sigma_t^2} + \frac{(m_{j_3, j_4} - m_W)^2}{\sigma_W^2} + \frac{(m_{j_3, j_4, b_2} - m_t)^2}{\sigma_t^2}$$

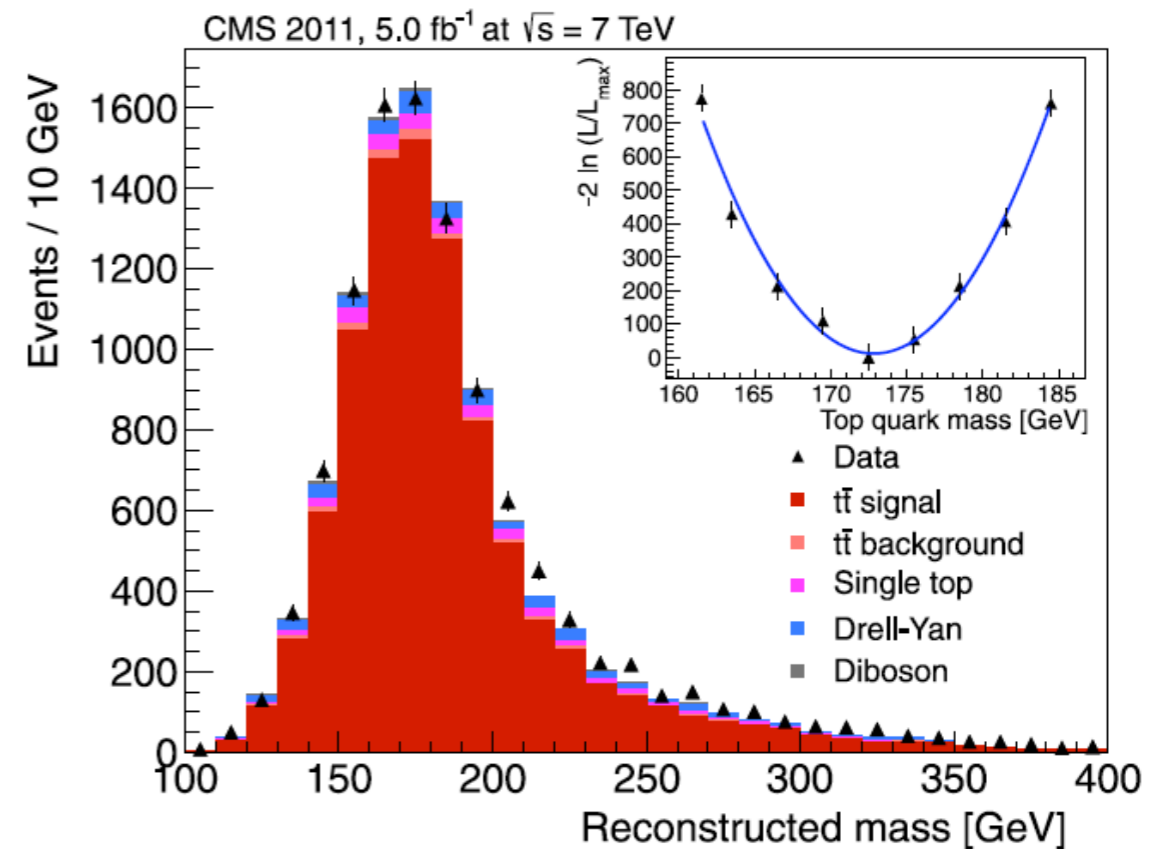
- > One-dimensional template fit in m_{j**bb**}.

174.9 ± 2.1 (stat) ± 3.8 (syst) GeV



ATLAS-CONF-2012-030 (March 2012)

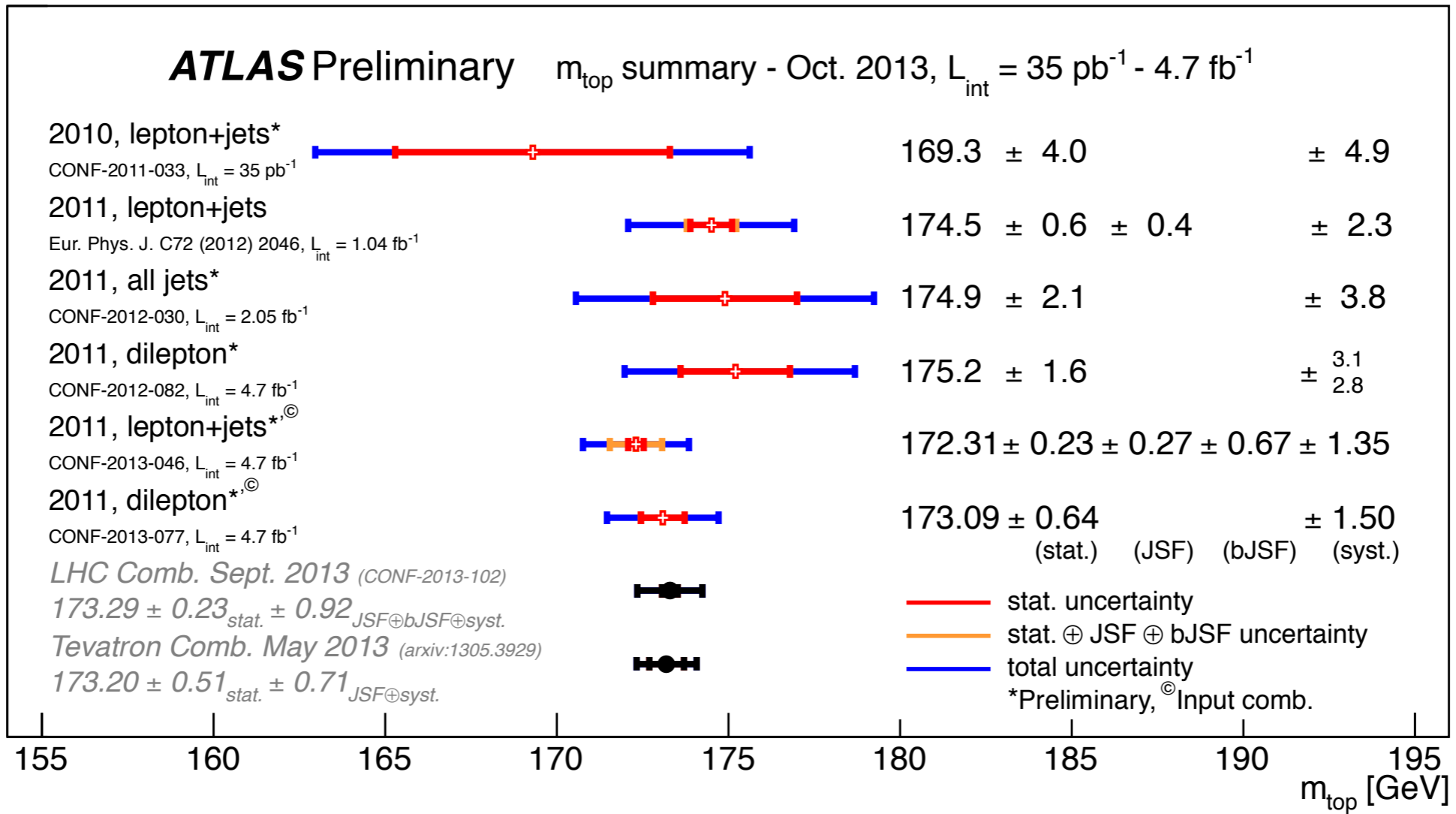
- > Full 2011 data set (5.0 fb⁻¹).
- > Require:
 - 2 leptons
 - 2 or more jets, of which 1 b-tagged
 - E_{miss}
- > Analytical matrix weighting technique (AMWT):
 - Kinematic equations for neutrino momenta solved for different top mass hypotheses.
 - Repeated 1000 times for each hypothesis with smeared jets.
 - Weights assigned to each solution based on prob. to observe charged lepton.
 - For each event, mass hypothesis with maximum weight is reconstructed top mass.

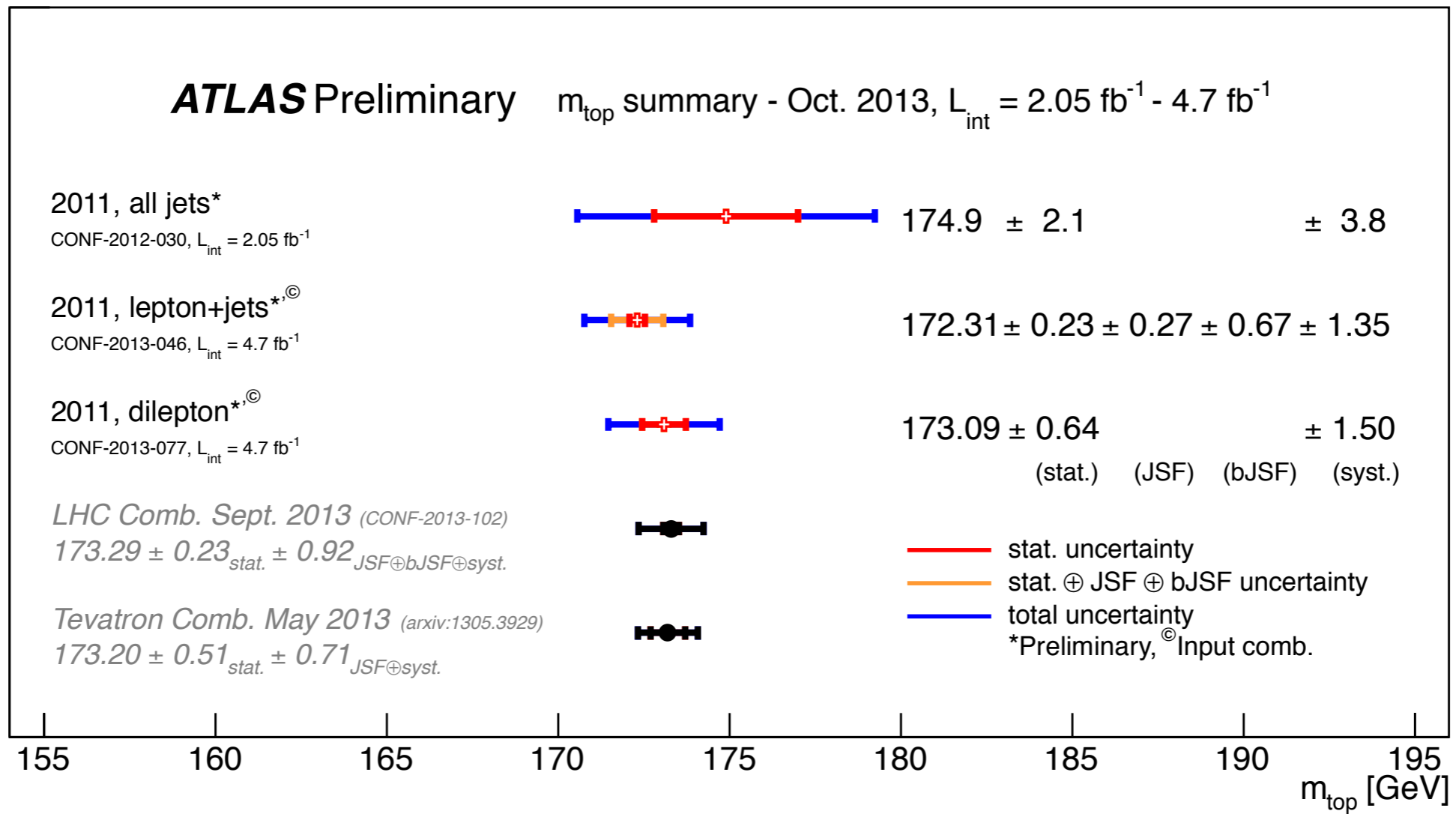


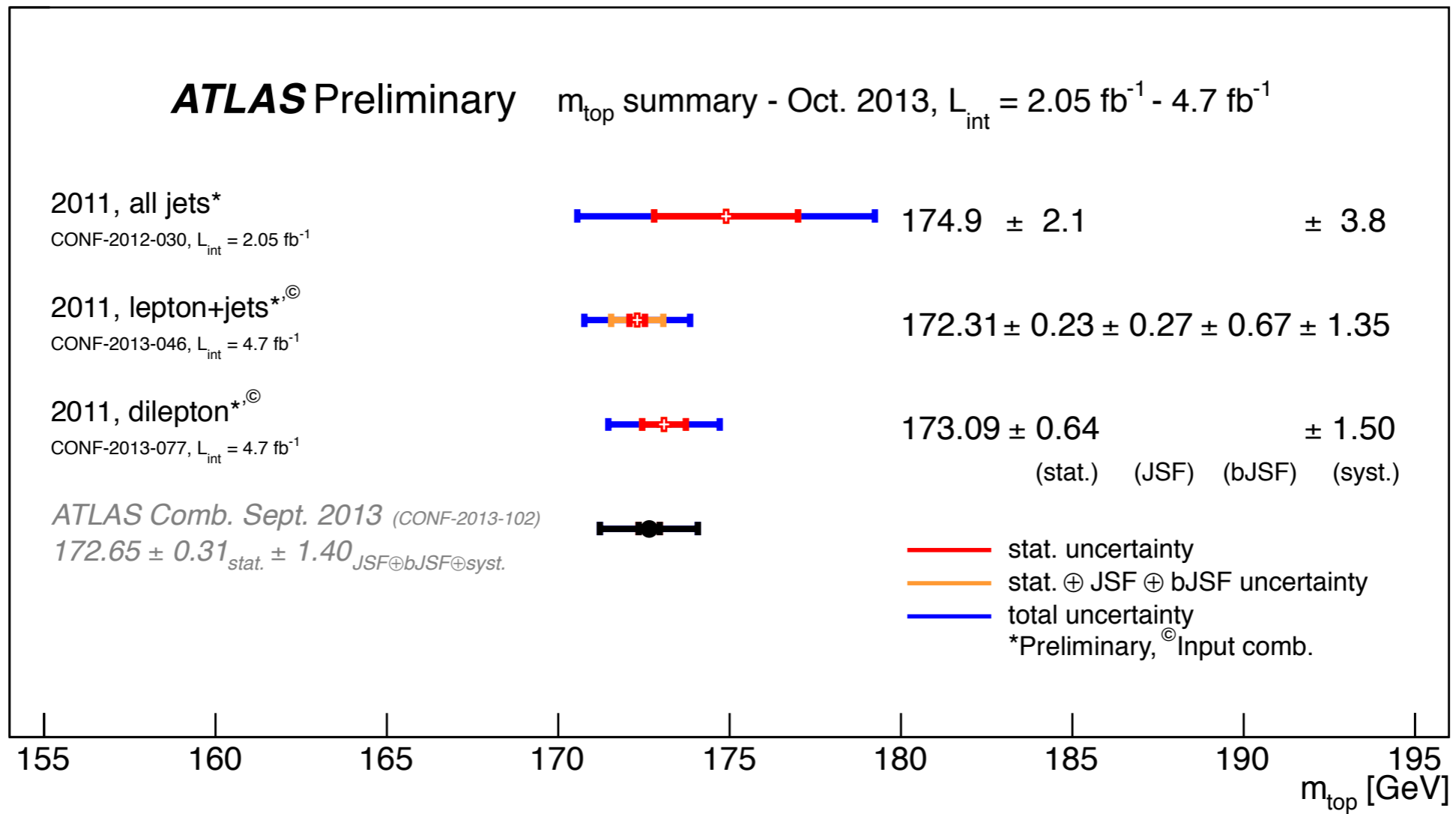
$$w = \left\{ \sum f(x_1) f(x_2) \right\} p(E_{\ell^+}^* | m_t) p(E_{\ell^-}^* | m_t),$$

$$p(E^* | m_t) = \frac{4m_t E^* (m_t^2 - m_b^2 - 2m_t E^*)}{(m_t^2 - m_b^2)^2 + M_W^2 (m_t^2 - m_b^2) - 2M_W^4}$$

172.5 ± 0.4 (stat) ± 1.5 (syst) GeV







CMS Preliminary

