

# Truth and Beauty Together: Evidence for s-channel Single Top Production



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SLAC EPP Seminar  
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# The Top (Truth) Quark

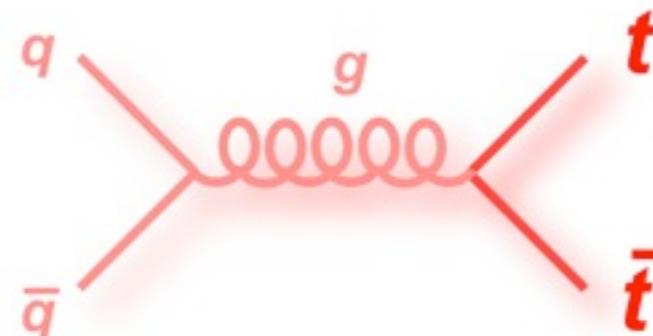
- Discovered by CDF and DØ at the Tevatron in 1995
- Heaviest known particle:  $173.2 \pm 0.9$  GeV ([arXiv:1305.3929](#))
  - couples very strongly to the Higgs because of its mass
  - Sensitive to new physics
  - Decays as a free quark: short lifetime
    - width was measured in single top analysis  
[PRD 85 091194 \(2012\)](#)

Three generations of matter (fermions)				
	I	II	III	
mass	$2.4 \text{ MeV}/c^2$	$1.27 \text{ GeV}/c^2$	$171.2 \text{ GeV}/c^2$	0
charge	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	0
spin	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	1
name	u	c	t	γ
	up	charm	top	photon
Quarks				
mass	$4.8 \text{ MeV}/c^2$	$104 \text{ MeV}/c^2$	$4.2 \text{ GeV}/c^2$	0
charge	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	0
spin	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	1
name	d	s	b	g
	down	strange	bottom	gluon
Leptons				
mass	$<2.2 \text{ eV}/c^2$	$<0.17 \text{ MeV}/c^2$	$<15.5 \text{ MeV}/c^2$	$91.2 \text{ GeV}/c^2$
charge	0	0	0	1
spin	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	0
name	v <sub>e</sub>	v <sub>μ</sub>	v <sub>τ</sub>	Z <sup>0</sup>
	electron neutrino	muon neutrino	tau neutrino	Z boson
Gauge bosons				
mass	$0.511 \text{ MeV}/c^2$	$105.7 \text{ MeV}/c^2$	$1.777 \text{ GeV}/c^2$	$80.4 \text{ GeV}/c^2$
charge	-1	-1	-1	$\pm 1$
spin	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	1
name	e	μ	τ	W <sup>±</sup>
	electron	muon	tau	W boson
<small>© 2013 Fermilab. All rights reserved.</small>				
<small>Periodic table of particles</small>				

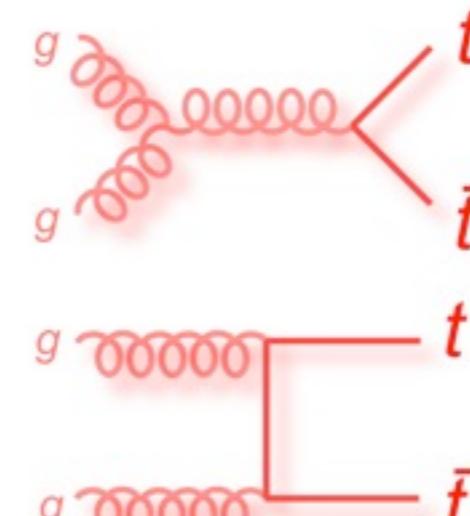
- Measurements:
  - production cross section
  - mass
  - angular properties of the decay products
  - width and lifetime
  - charge,  $m(t)-m(\bar{t})$

# Top Production at Hadron Colliders

- Strong interaction: top pair

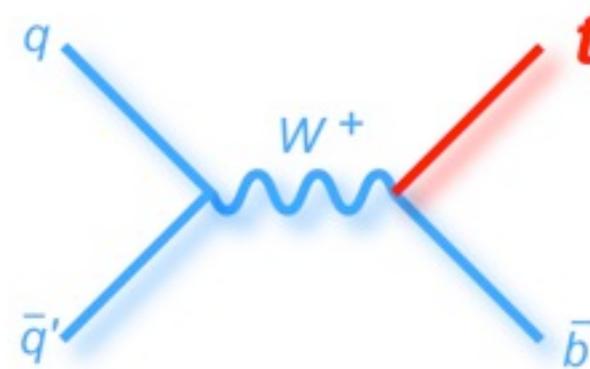


$q\bar{q}$  annihilation

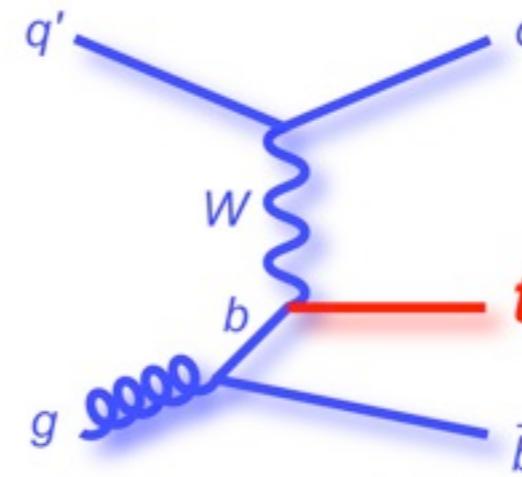


gg fusion

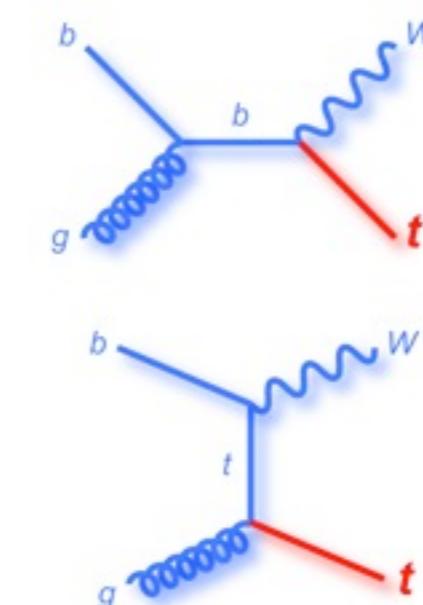
- Electroweak interaction: single top



s-channel ( $tb$ )



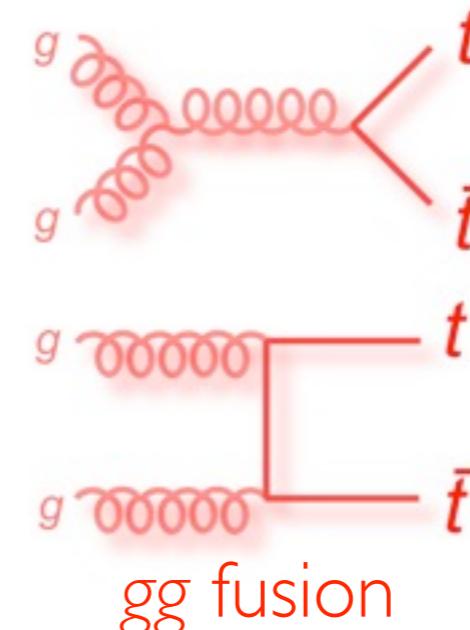
t-channel ( $tqb$ )



Associated ( $tW$ )

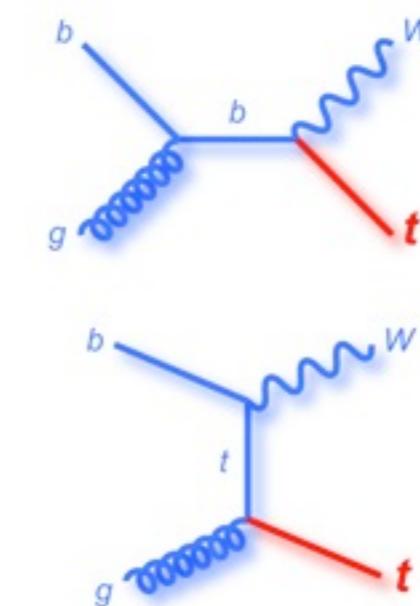
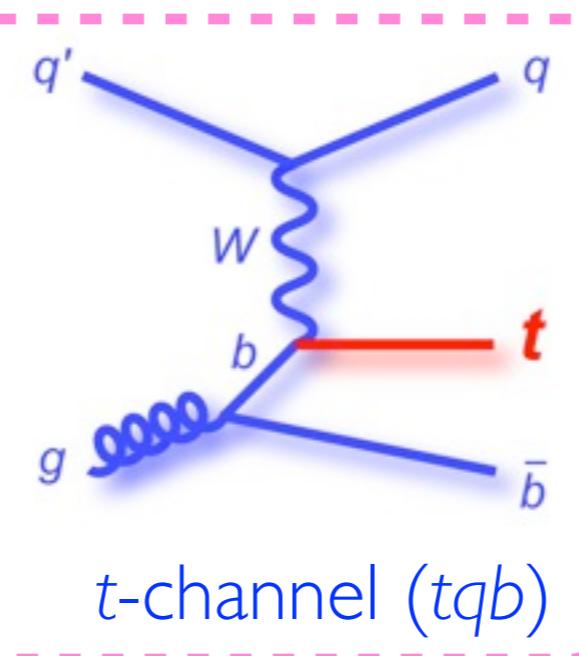
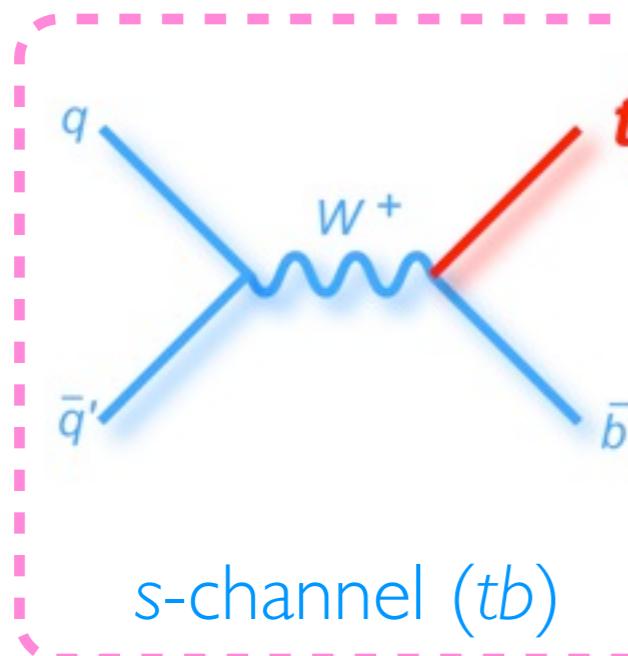
# Top Production at Hadron Colliders

- Strong interaction: top pair



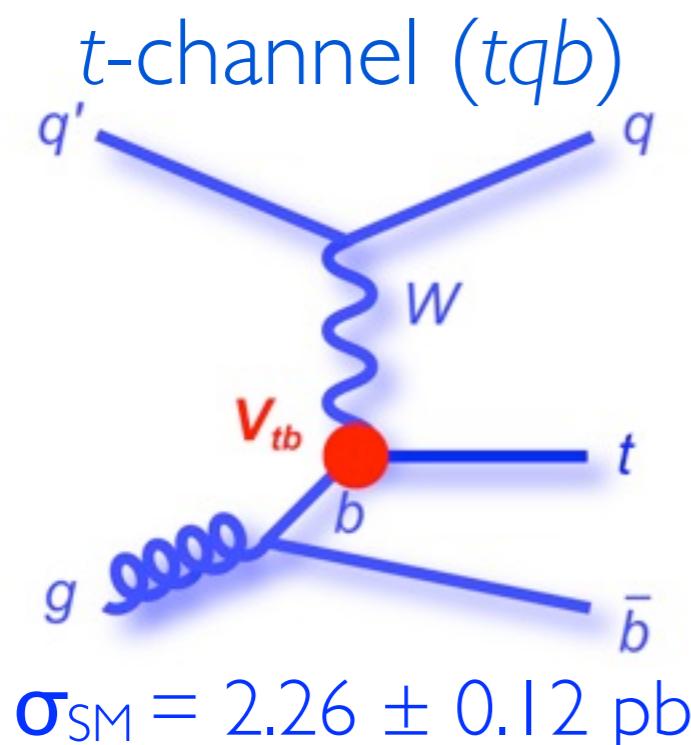
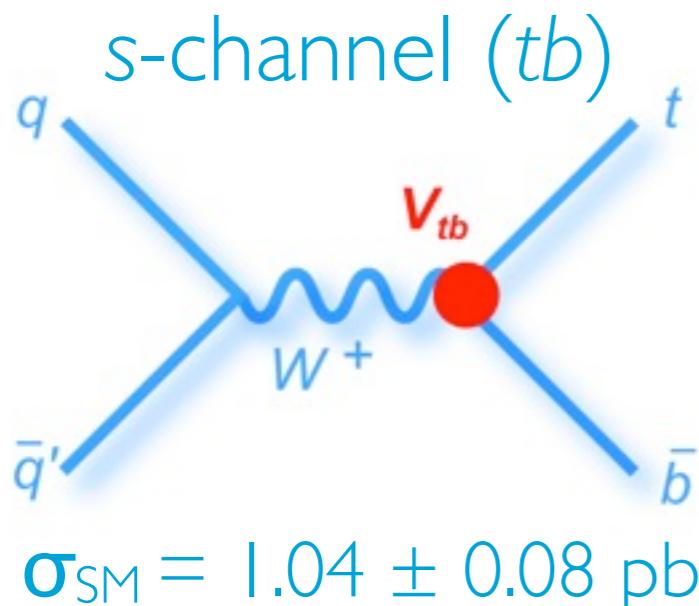
Main modes  
at Tevatron

- Electroweak interaction: single top



Associated ( $tW$ )

# EW Top Quark Production

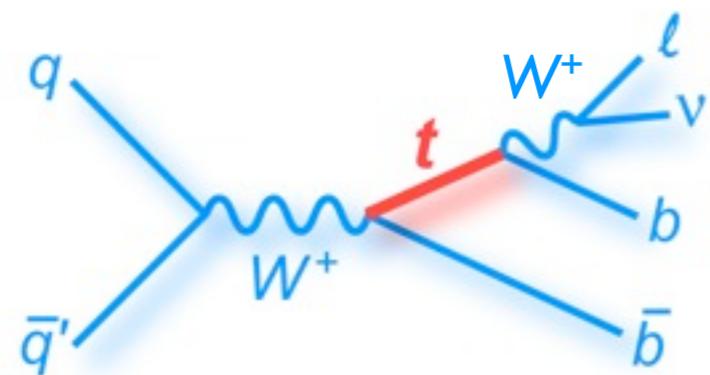
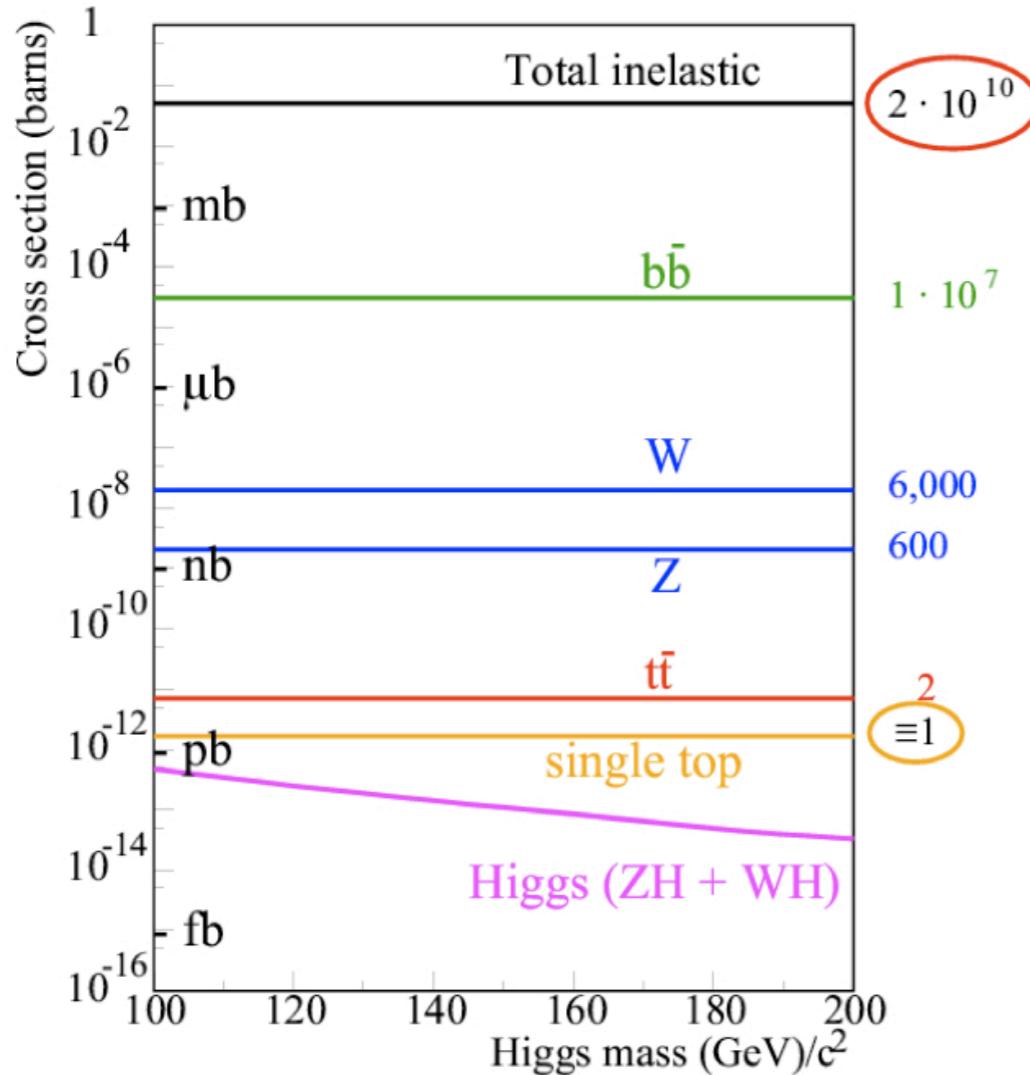


$$M_{\text{top}} = 172.5 \text{ GeV}$$

N. Kidonakis, PRD 74.114012 (2006)

- Measure the two important single top-quark production modes at Tevatron:  $s$  and  $t$  channel
- Directly probe the CKM matrix element  $|V_{tb}|$
- Measure the top decay width
- New physics can change  $\sigma_{tb}$  and  $\sigma_{tqb}$  differently:
  - $\sigma_{tb}$ : New bosons
  - $\sigma_{tqb}$ : FCNC, anomalous couplings
- $\sigma_{tw}$  at the Tevatron is negligible

# A Challenging Analysis



- Small cross section:  $\sim 3$  pb
  - Tevatron produced 32k single top events
  - Analyze leptonic final state: 6.8k single top events
- Background dominated
  - Main background:  $W+jets$
- To observe  $t\bar{b}+t\bar{q}b$ , needed 50 times more data than the top pair observation! (CDF, DØ)
  - PRL 103 092001 (2009)

# LHC: Limited $t\bar{b}$ Production

$\sigma$ (pb) ~NNLO	$t\bar{b}$	$t\bar{q}b$	$tW$
Tevatron (1.96 TeV)	1.04	2.26	0.3
	x4	x30	x50
LHC (7 TeV)	4.56	65.9	15.6

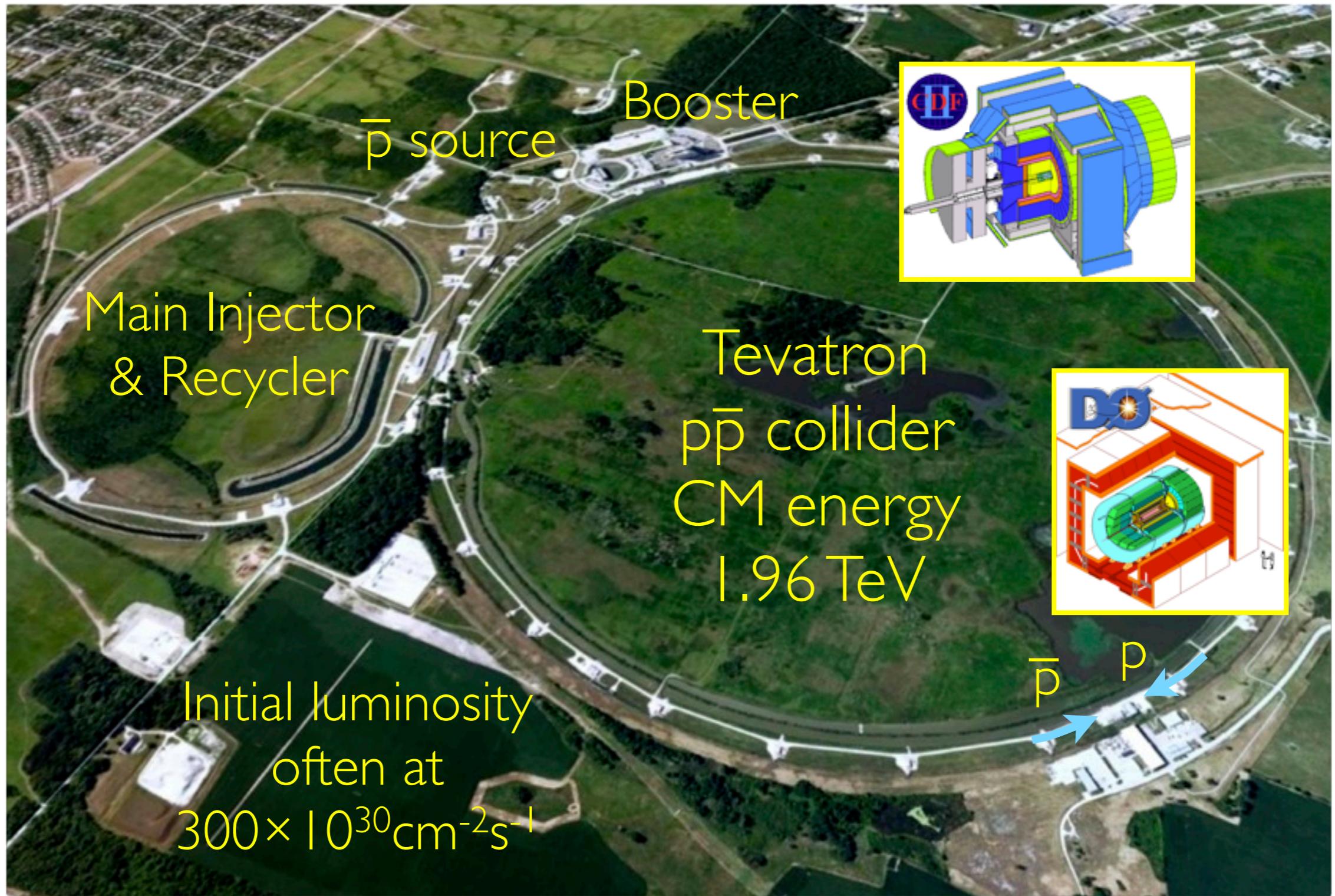
# Status up to June 2013

$\sigma$ (pb) ~NNLO	$tb$	$tqb$	$tW$
Tevatron Prediction (1.96 TeV)	1.04	2.26	0.3
CDF (7.5 fb <sup>-1</sup> )	1.8±0.6	1.49±0.45	-
DØ (5.4 fb <sup>-1</sup> )	0.98±0.63	<input checked="" type="checkbox"/> 2.9±0.59	-
LHC Prediction (7 TeV)	4.56	65.9	15.6
ATLAS (0.7-2.1 fb <sup>-1</sup> )	< 20.5 (95% C.L.)	<input checked="" type="checkbox"/> 83±20	<input type="checkbox"/> 17±6
CMS (1.2-4.9 fb <sup>-1</sup> )	-	<input checked="" type="checkbox"/> 67±6	<input type="checkbox"/> 16±5

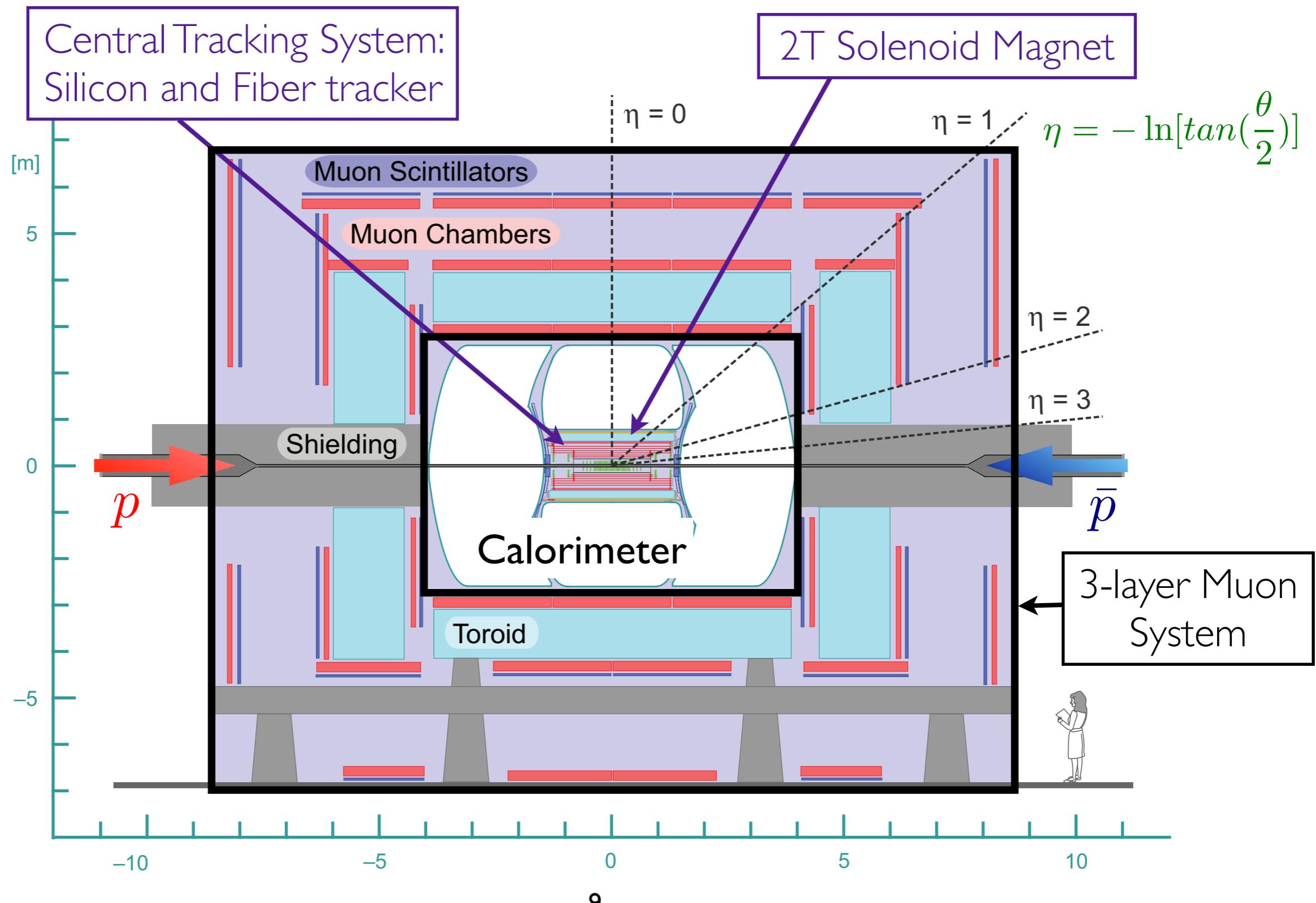
Evidence (3 SD)

Observation (5 SD)

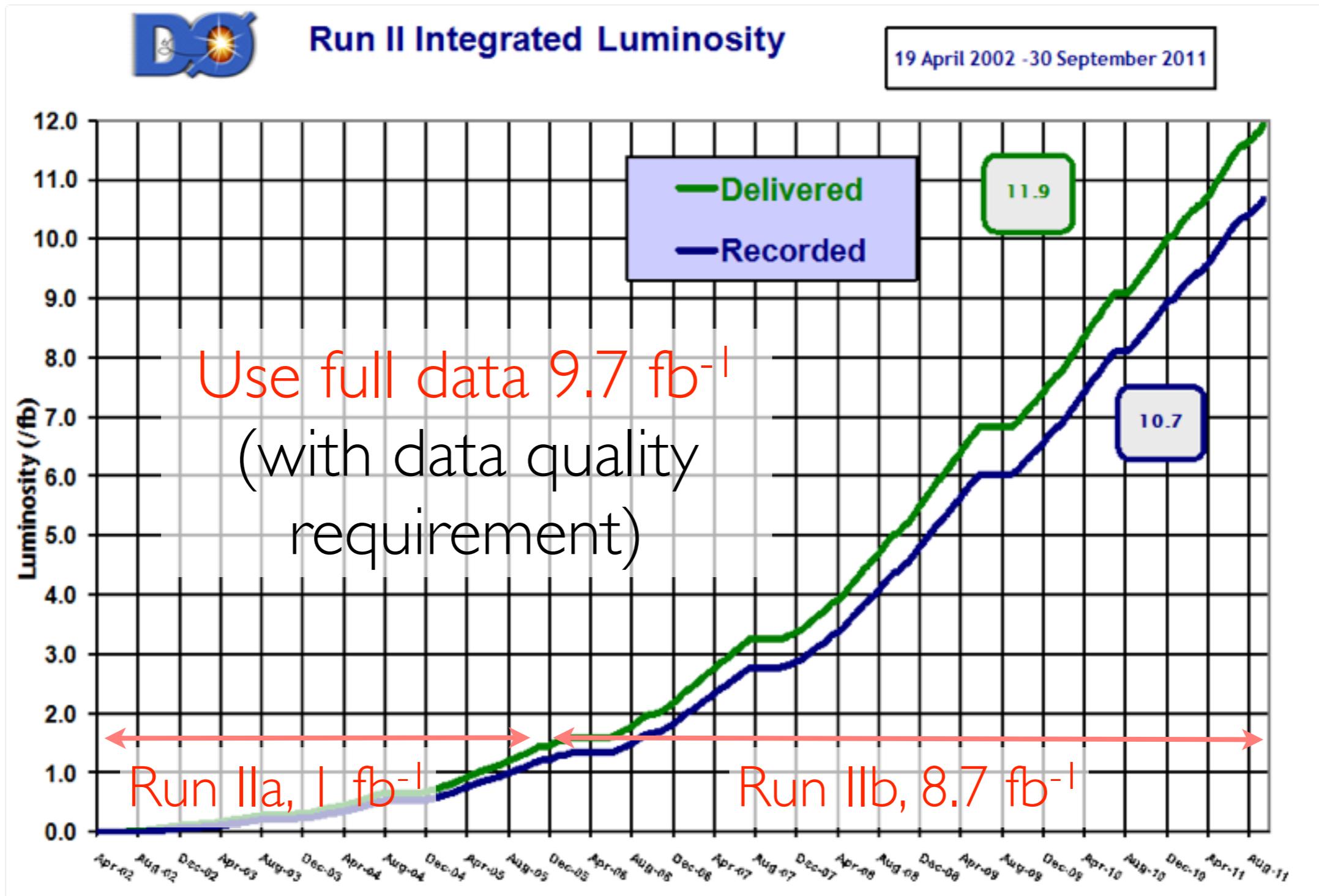
# Fermilab Tevatron



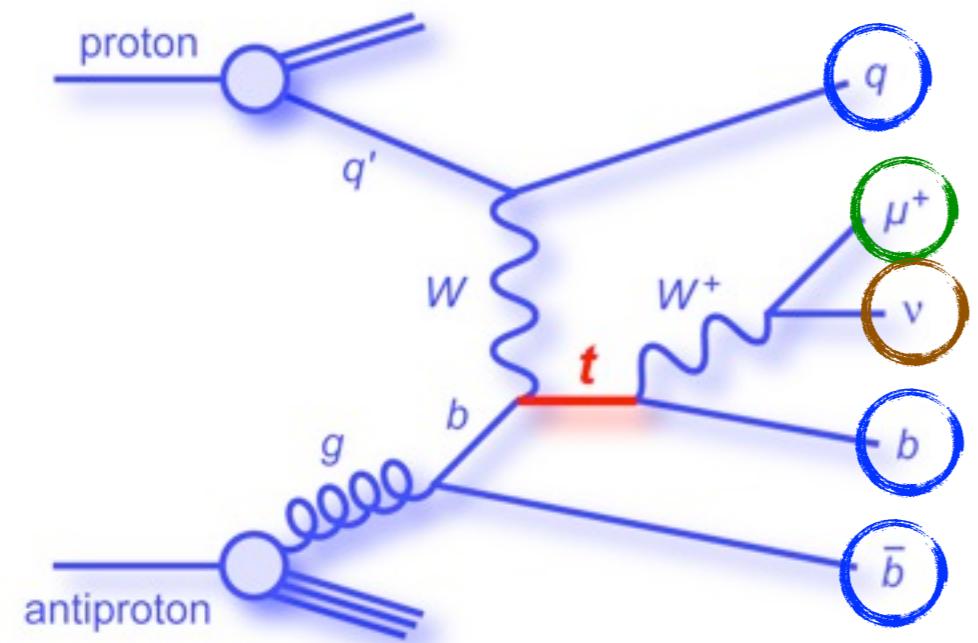
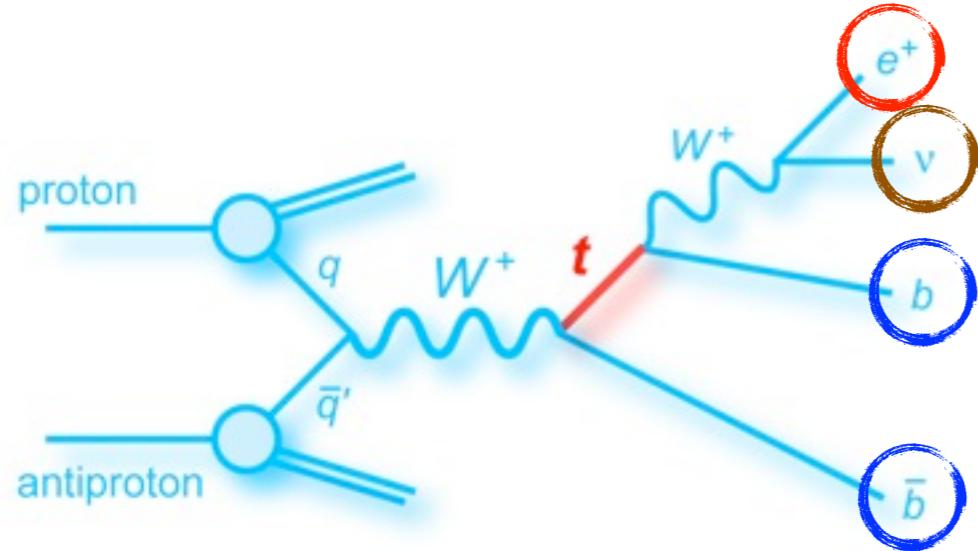
# D $\emptyset$ Detector



# Data Taking

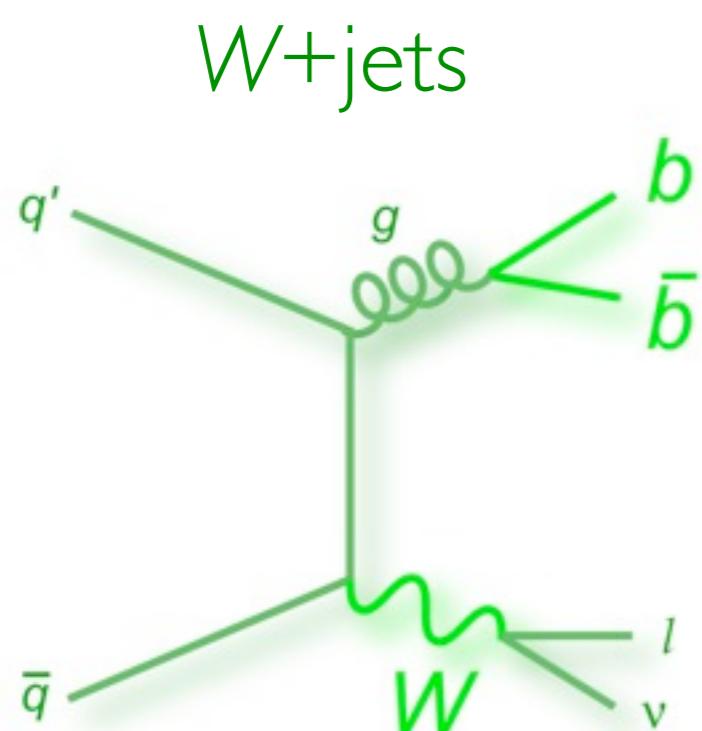
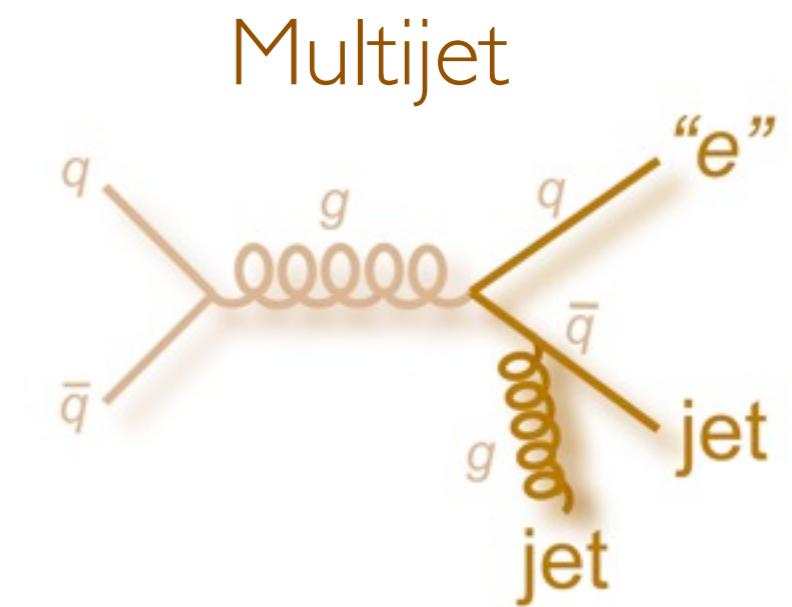
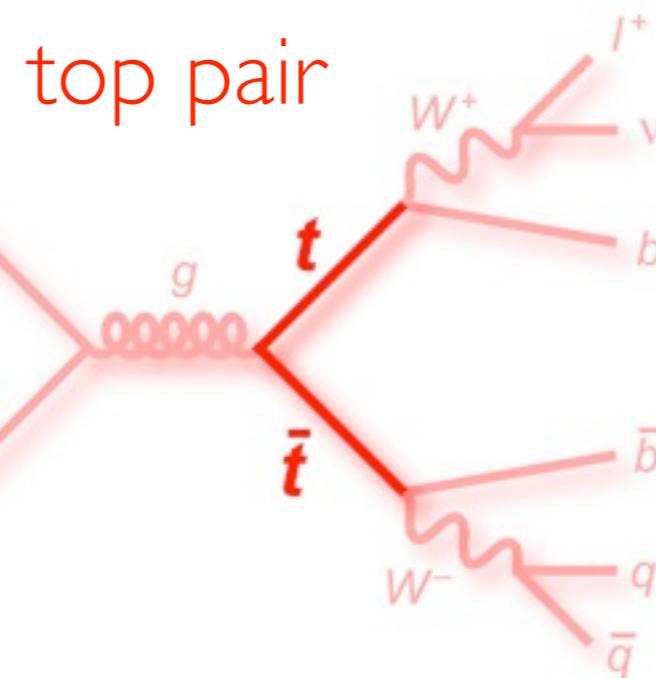
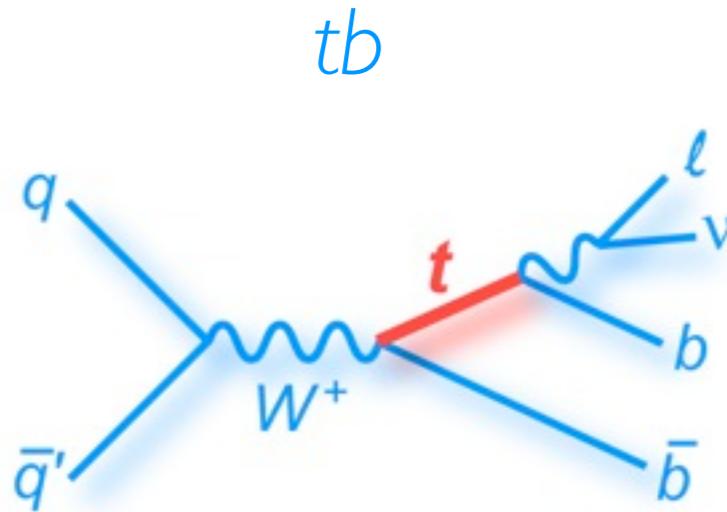


# Event Selection



- Only one high  $p_T$  isolated electron or muon:  $p_T > 20 \text{ GeV}$ 
  - electron:  $|n| < 1.1$
  - muon:  $|n| < 2.0$
- Two or three jets
  - $p_T > 20 \text{ GeV}, |n| < 2.5$
  - The leading jet  $p_T > 25 \text{ GeV}$
- Missing transverse energy  $> 20 \text{ GeV}$
- $H_T > 120 \text{ GeV}$ 
  - $H_T = \text{all jet } p_T + \text{lepton } p_T + \text{missing transverse energy}$

# Signal & Background Simulation



- Signals: CompHEP (NLO)+Pythia
- $W+jets$  & top pair: Alpgen+Pythia
  - Correct Alpgen (LL) to NLO
    - e.g. a factor 1.9 for  $W+bb$
- Multijet: Data with non-isolated lepton

# $W$ +jets & Multijet Normalization

- Determine the overall scales of multijet and  $W$ +jets background simultaneously

$$N_{\text{loose}} = N_{\text{loose}}^{\text{fake-}\ell} + N_{\text{loose}}^{\text{real-}\ell}$$

$$N_{\text{tight}} = \epsilon_{\text{fake-}\ell} N_{\text{loose}}^{\text{fake-}\ell} + \epsilon_{\text{real-}\ell} N_{\text{loose}}^{\text{real-}\ell}$$

# $W+jets$ & Multijet Normalization

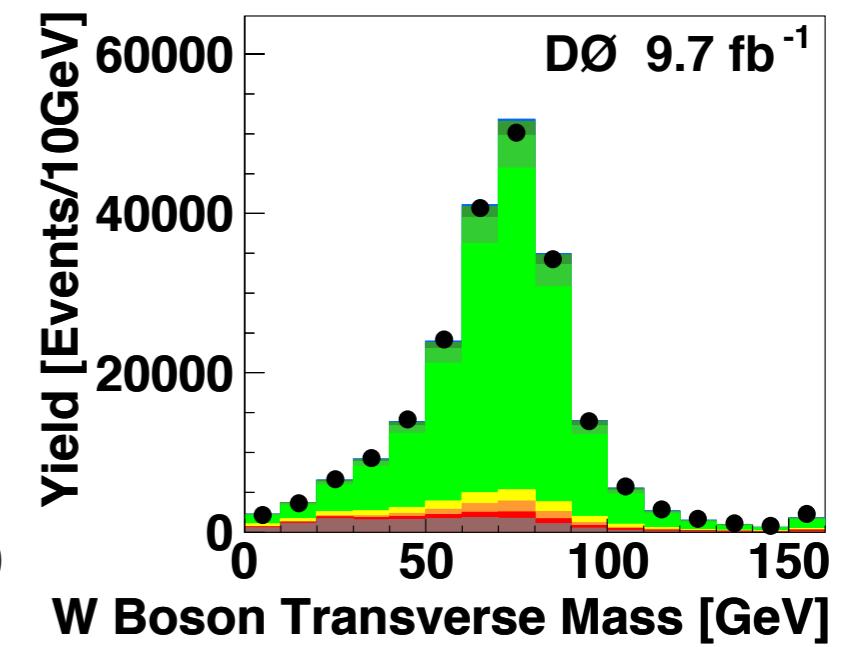
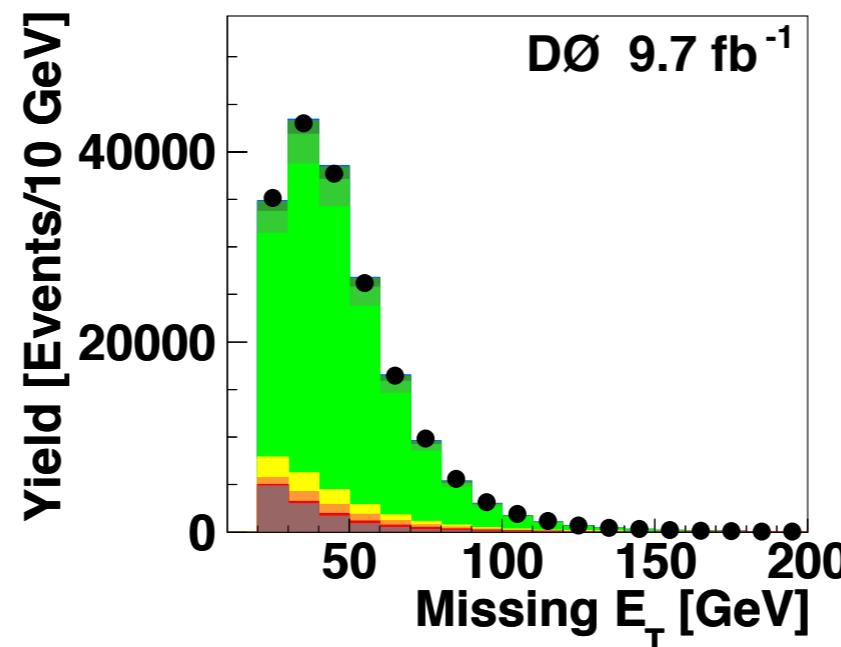
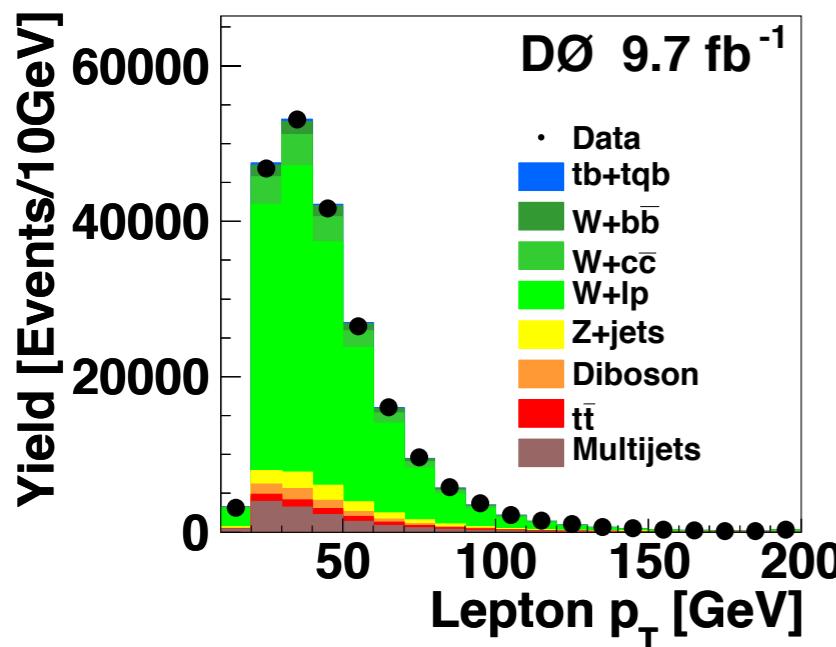
- Determine the overall scales of multijet and  $W+jets$  background simultaneously

Known from the selected data samples

$$N_{\text{loose}} = N_{\text{loose}}^{\text{fake-}\ell} + N_{\text{loose}}^{\text{real-}\ell}$$

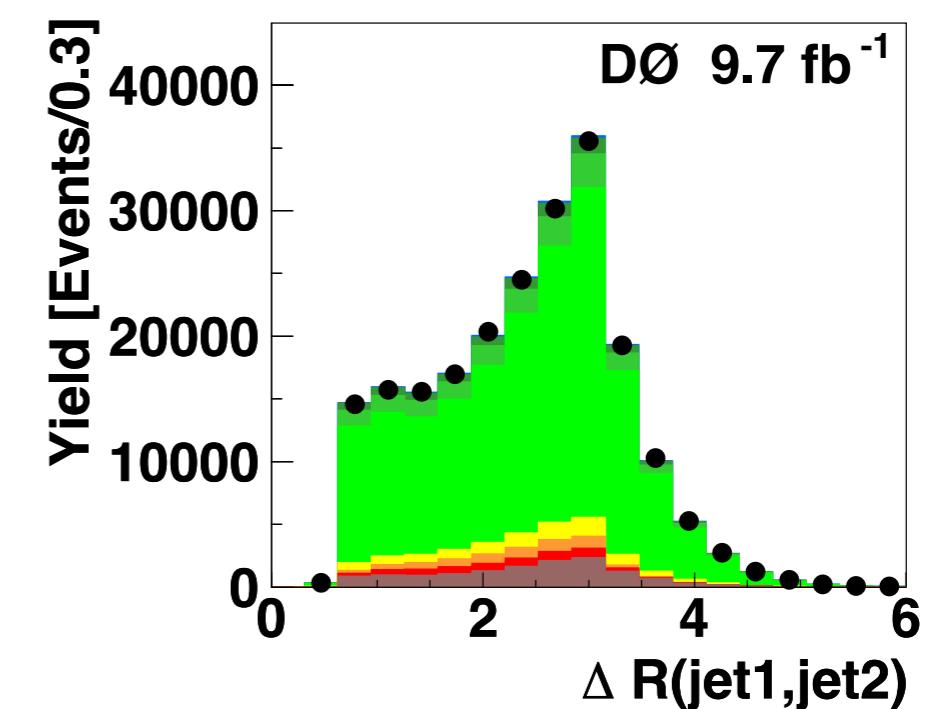
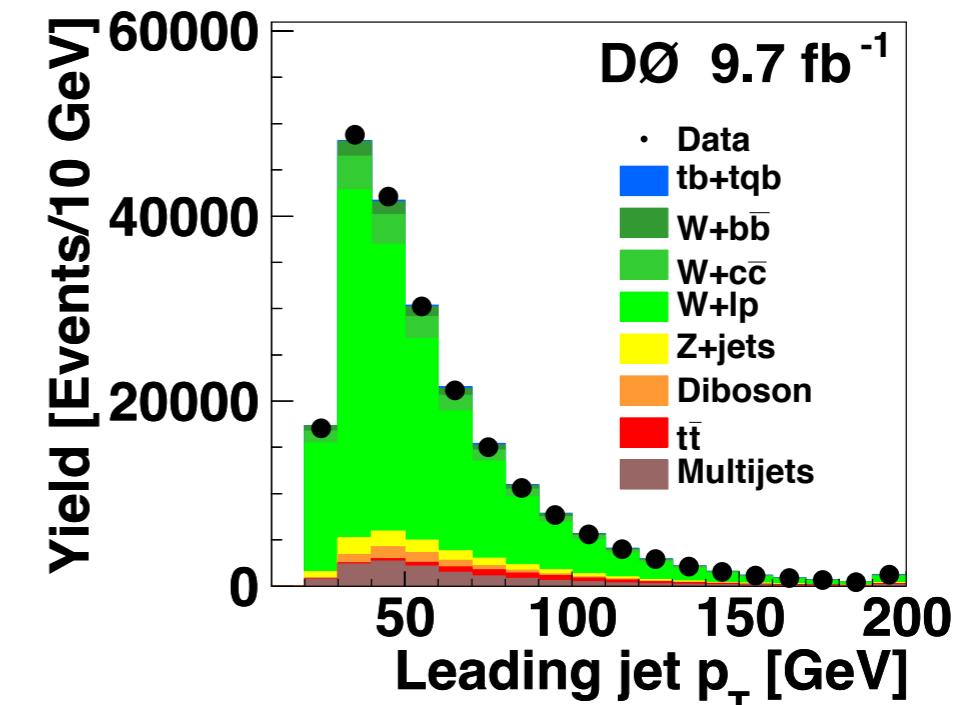
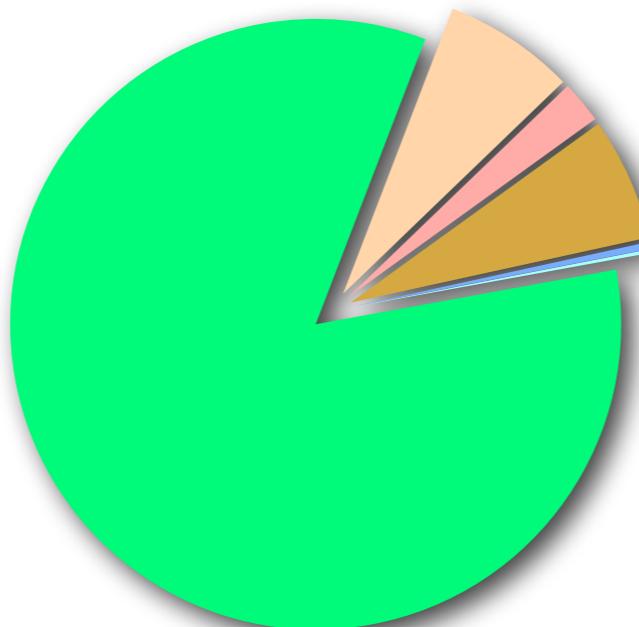
$$N_{\text{tight}} = \epsilon_{\text{fake-}\ell} N_{\text{loose}}^{\text{fake-}\ell} + \epsilon_{\text{real-}\ell} N_{\text{loose}}^{\text{real-}\ell}$$

Determined from MC and data samples

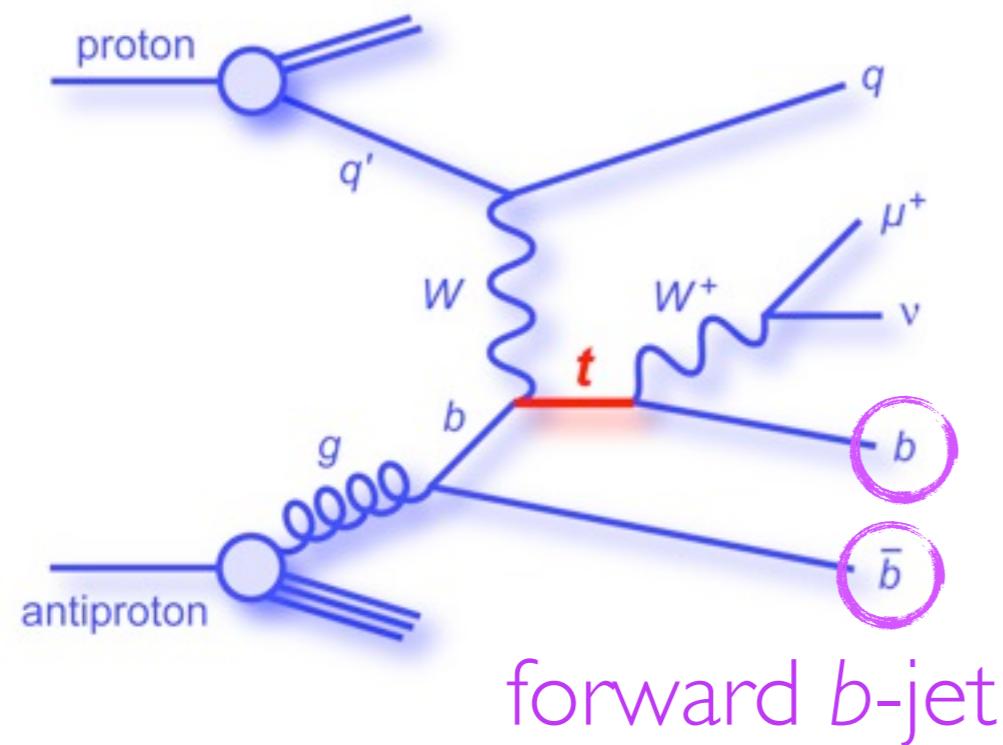
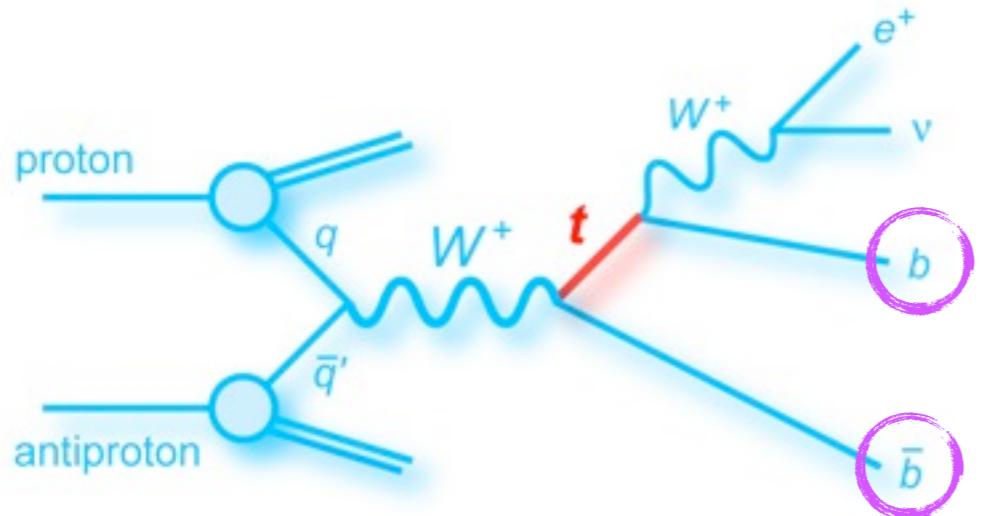


# Background Modeling

- Dominated by backgrounds
- Correct the efficiency of the simulated samples to that of data
- Reweight the angular distributions of  $W+jets$  MC to data

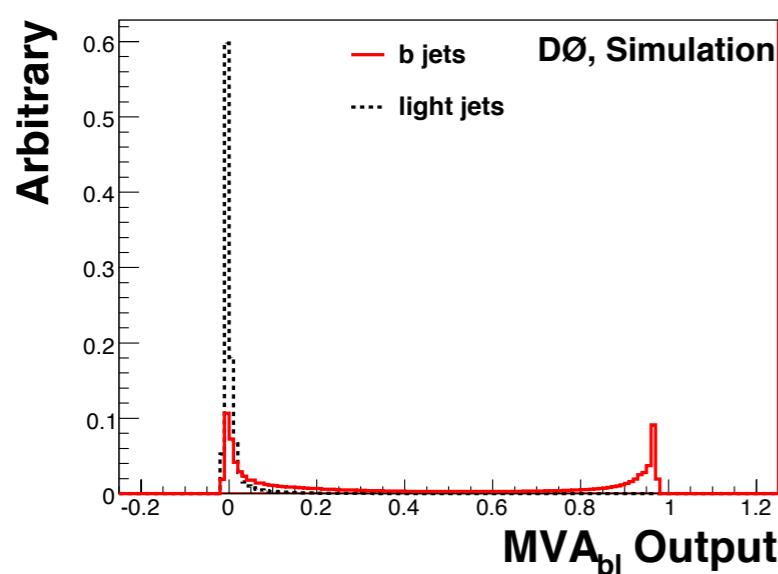
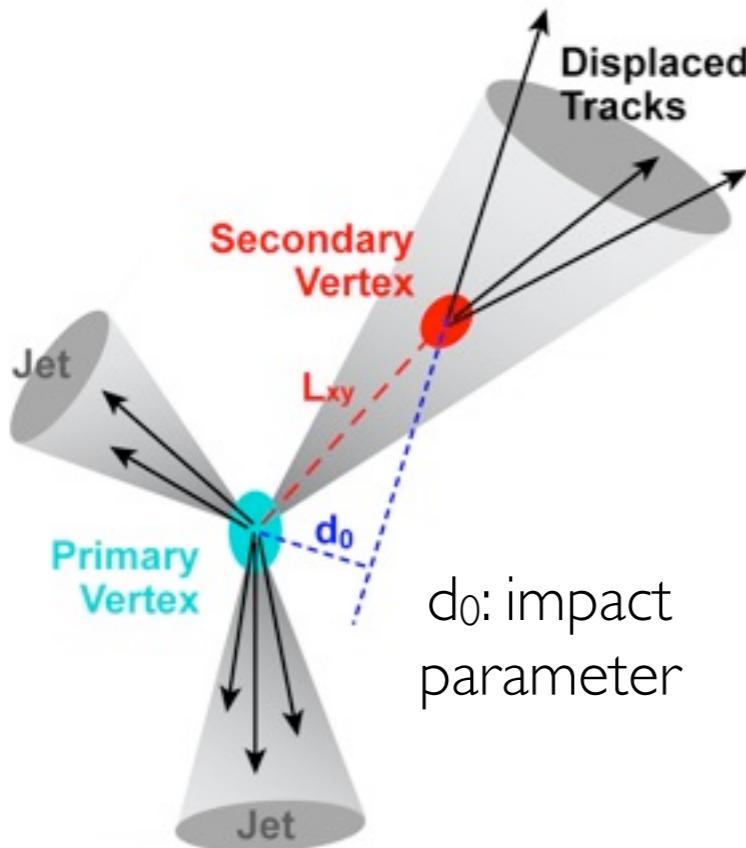


# Event Selection



- One high  $p_T$  isolated electron or muon:  $p_T > 20 \text{ GeV}/c$ 
  - electron:  $|n| < 1.1$
  - muon:  $|n| < 2.0$
- Two or three jets
  - $p_T > 20 \text{ GeV}/c, |n| < 2.5$
  - The leading jet  $p_T > 25 \text{ GeV}/c$
- Missing transverse energy  $> 20 \text{ GeV}/c$
- Total transverse energy ( $H_T$ )
- Require one or two identified  $b$ -jets ( $b$ -tagging)

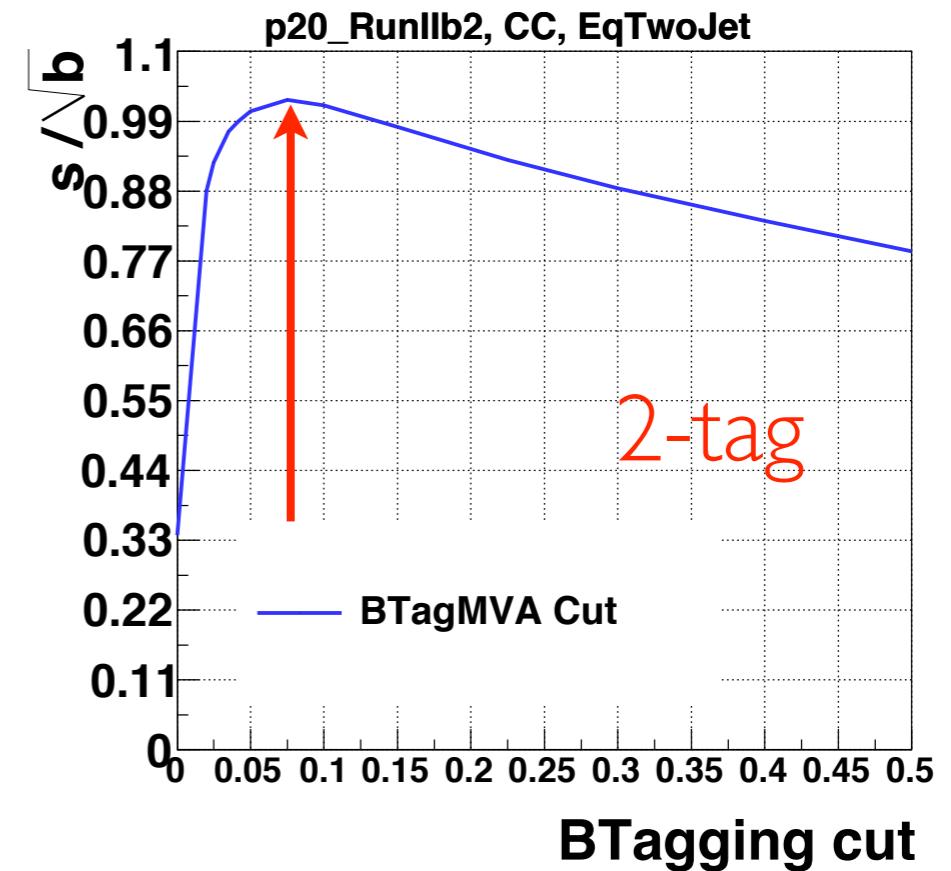
# $b$ -Jet Identification



- Identify  $b$ -jet from  $u, d, s, c$ , and  $g$  jets
  - reduces a lot of backgrounds
- Features of  $b$ -hadron in  $b$ -jet
  - Long lifetime ( $\sim 1$  ps,  $L_{xy} \sim 3$  mm)
  - Large invariant mass
- Reconstruct a secondary vertex
- Make use of the displaced tracks (with large impact parameter)
- Use a multivariate technique to combine this information

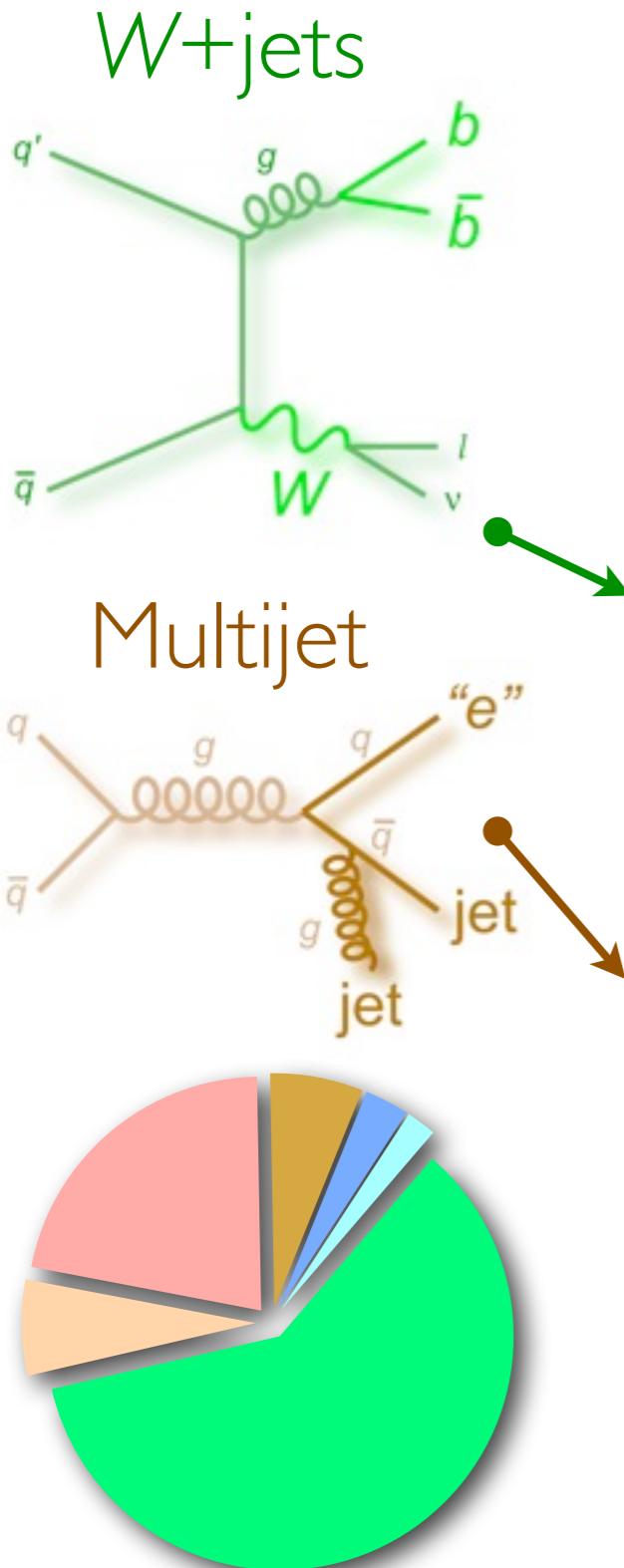
# $b$ -ID Cut Optimization

- Calculate  $s/\sqrt{b}$  from the predicted signal and background events with each  $b$ -ID cut
- Maximize the  $t\bar{b}$  signal rate
  - The  $t\bar{b}$  events have two central  $b$ -jets
  - 2-tag channel: 2 jets with Loose  $b$ -ID
  - 1-tag channel: 1 jet with Tight  $b$ -ID, veto the 2nd jet with Loose  $b$ -ID
  - Non-overlapping categories



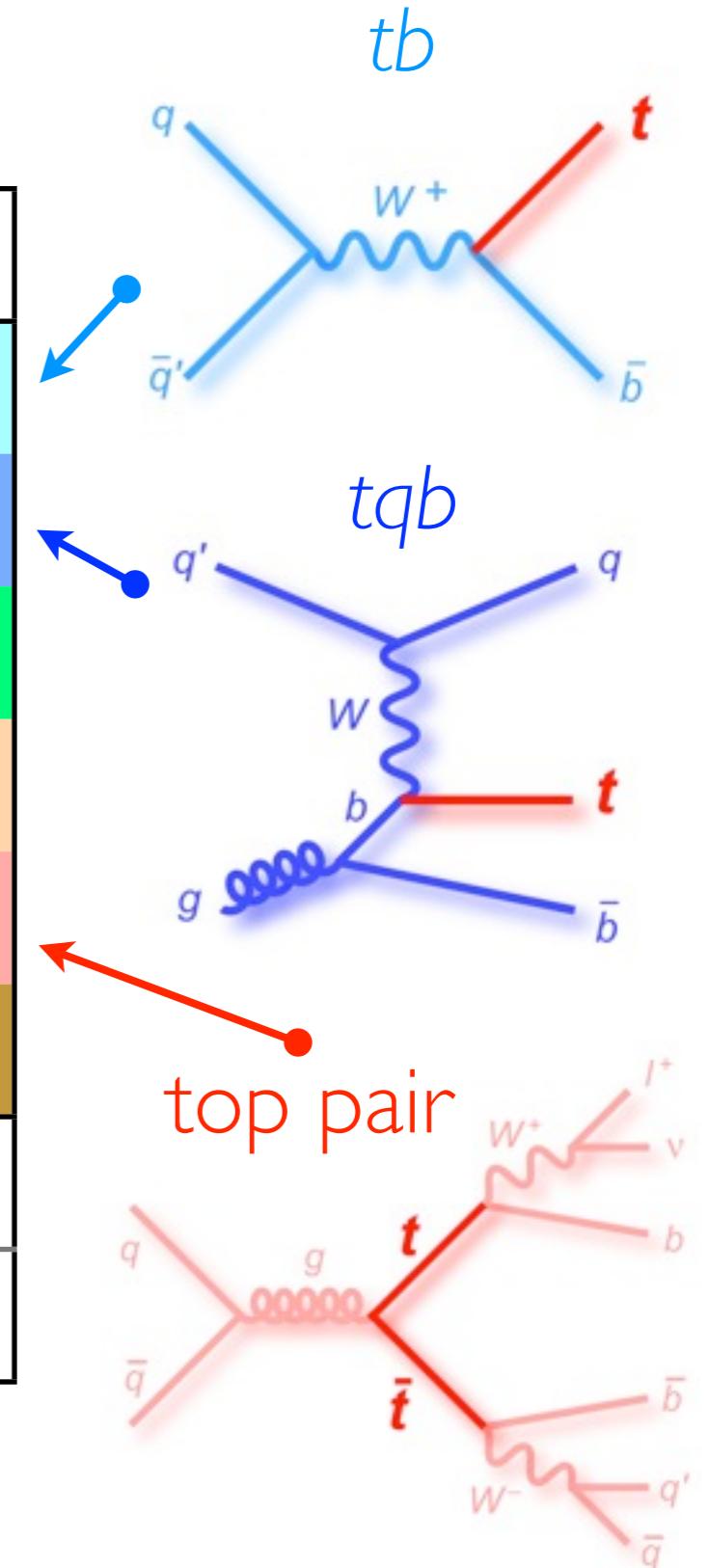
- Typical  $b$ -ID efficiency: 50% - 70%
- Fake rate: 2% - 7%

# Event Yield

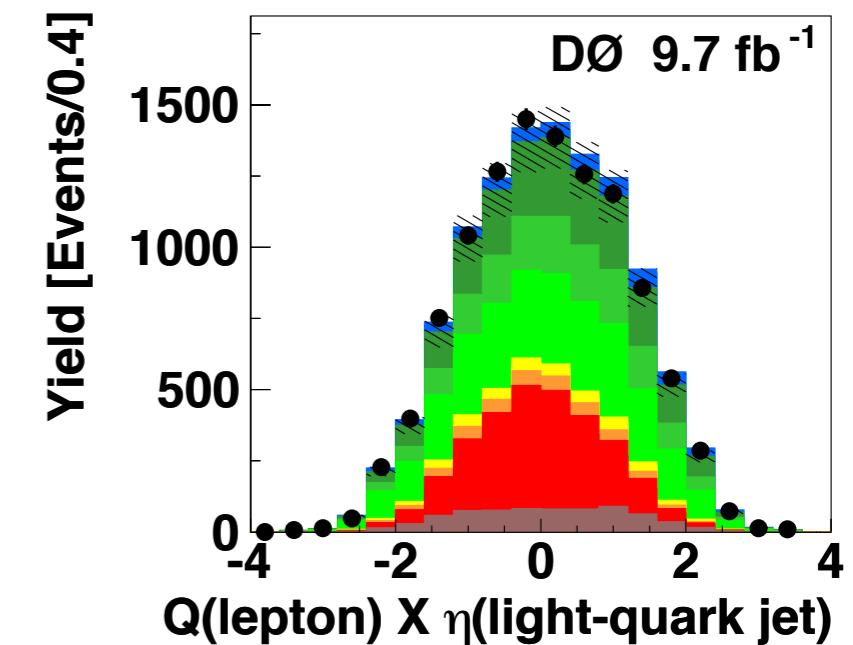
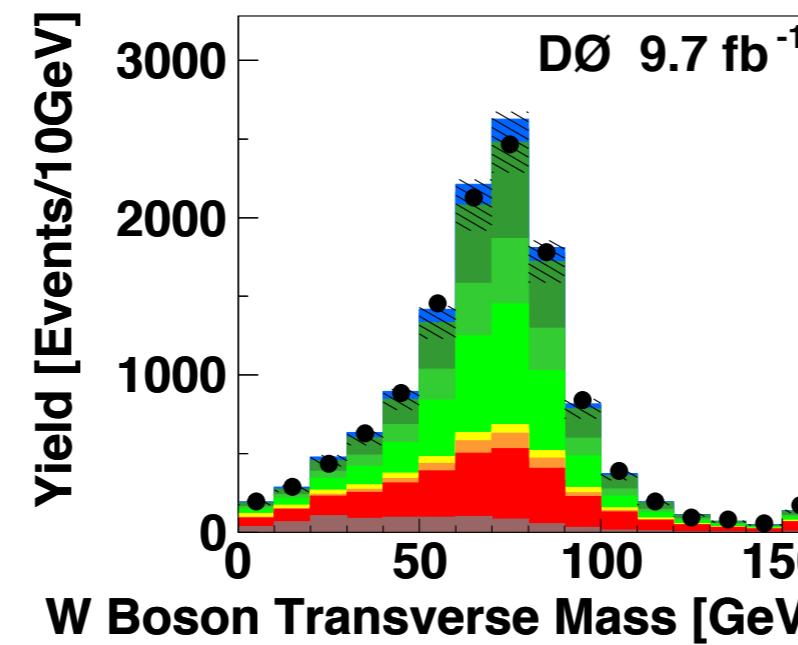
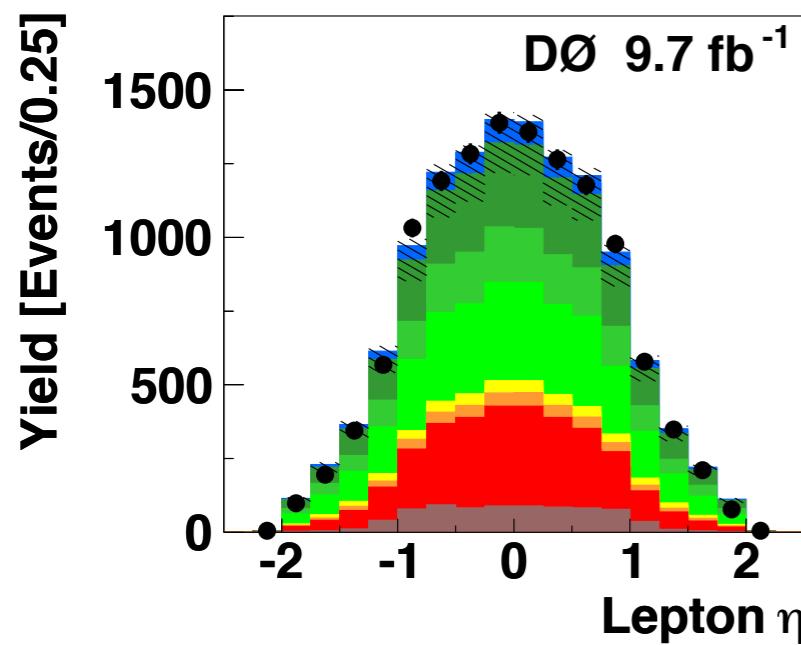
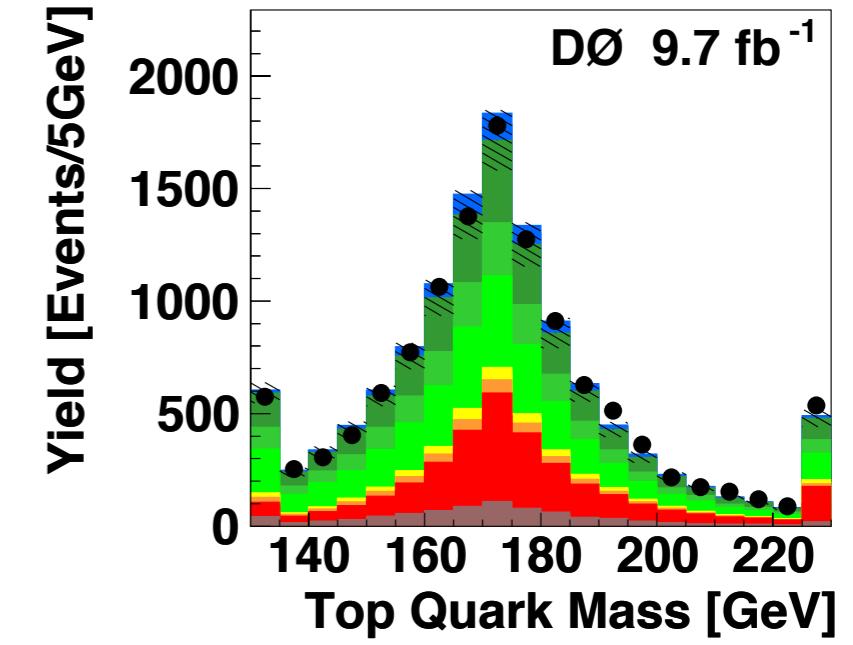
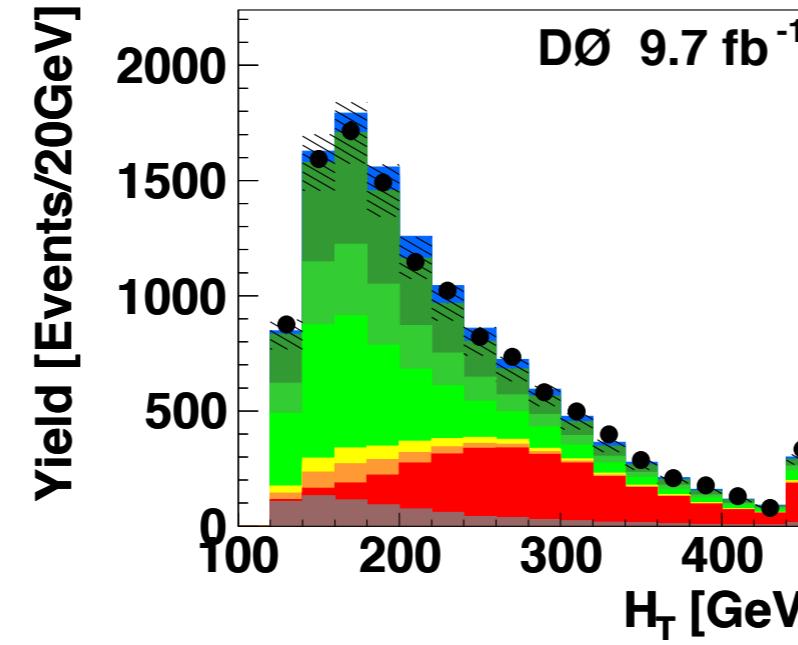
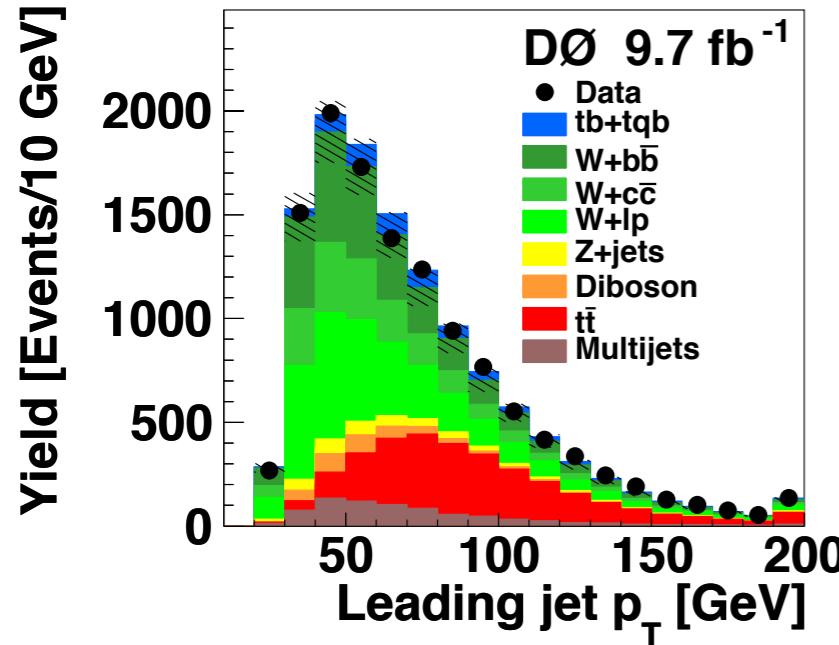


e, $\mu$ 2, 3-jets 1, 2 b-tags combined	
<i>tb</i>	$257 \pm 31$
<i>tqb</i>	$378 \pm 53$
<b>W+jets</b>	<b><math>7394 \pm 401</math></b>
diboson, Z+jets	$815 \pm 71$
top pair	$2672 \pm 284$
multijet	$789 \pm 81$
<b>Total background</b>	<b><math>11669 \pm 503</math></b>
Data	12103

*tb*: *tqb*: B = 1: 1.5: 45

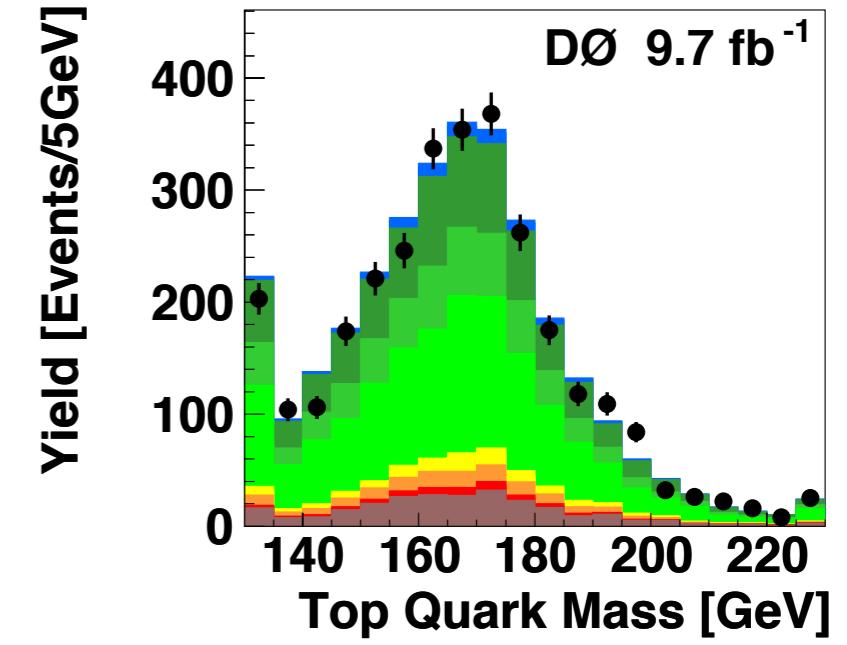
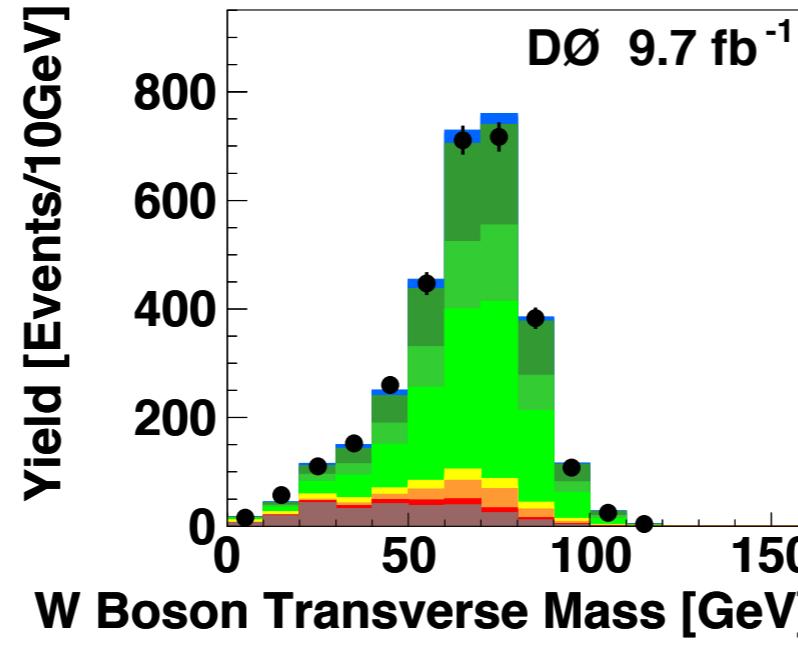
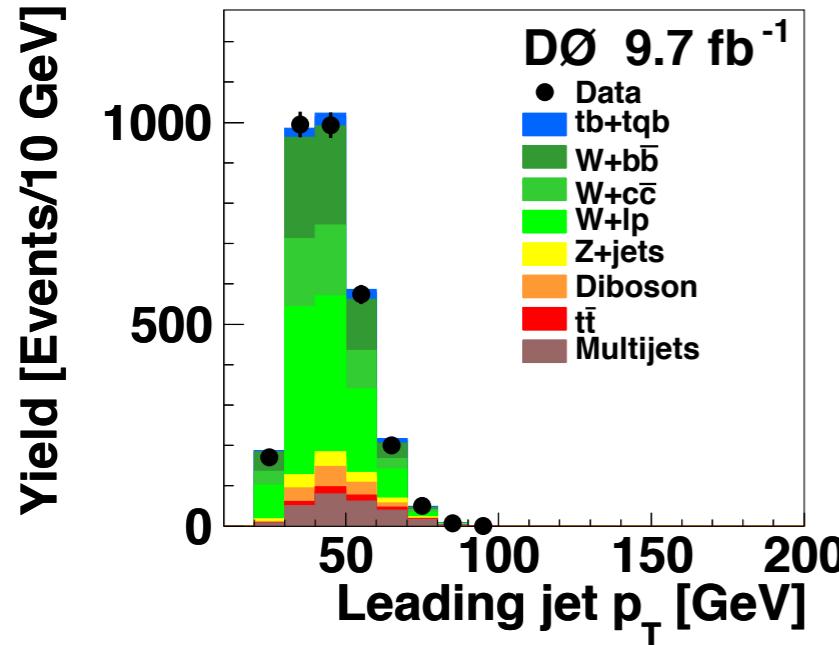


# Data-Simulation Comparison

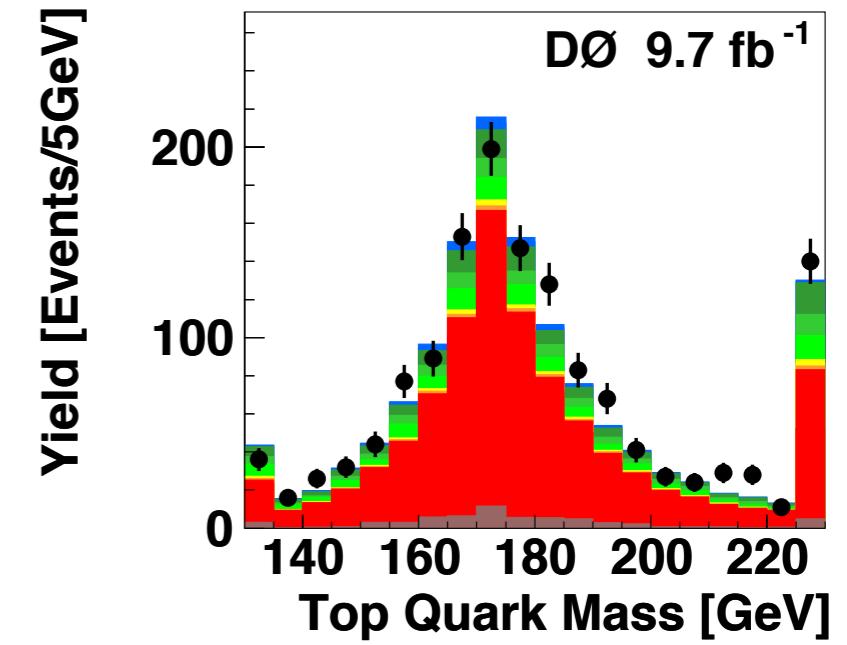
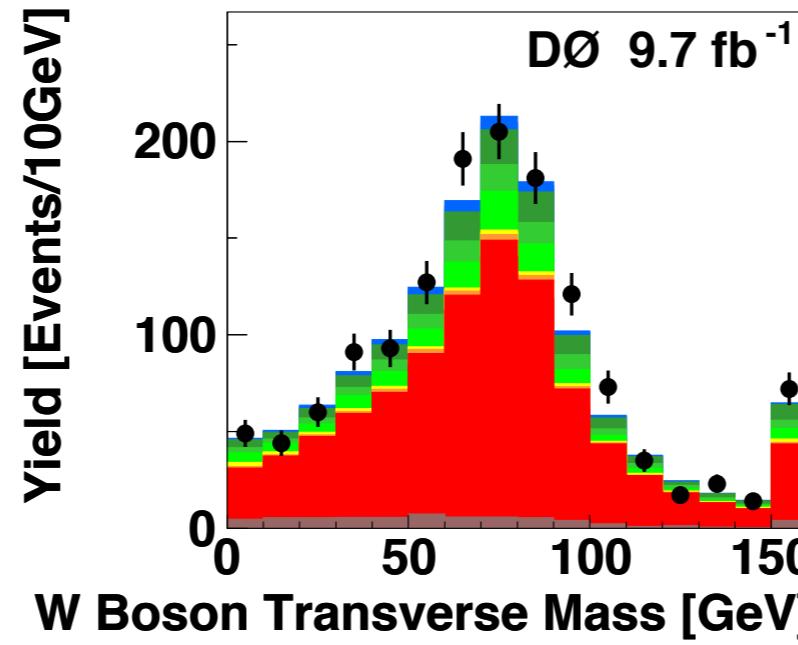
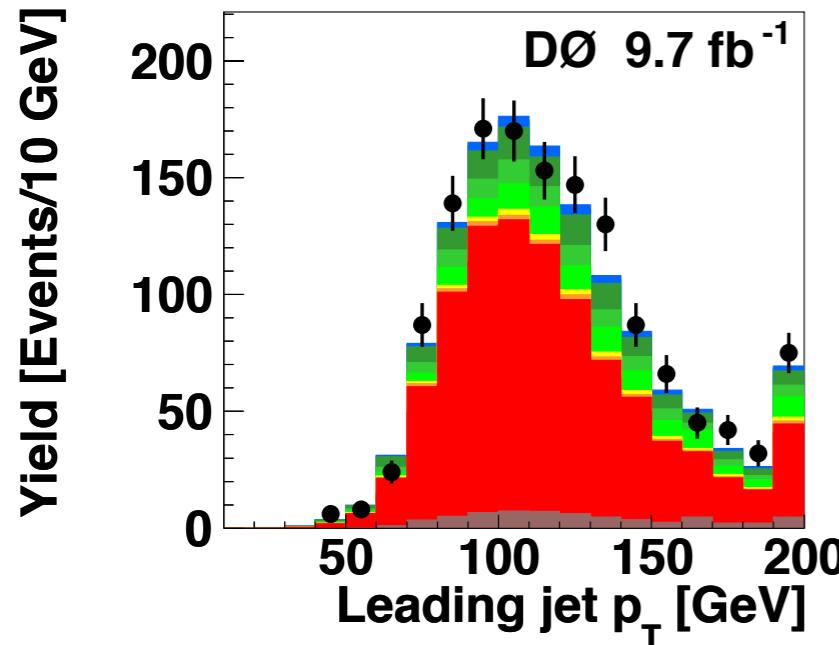


# Cross-Check Samples

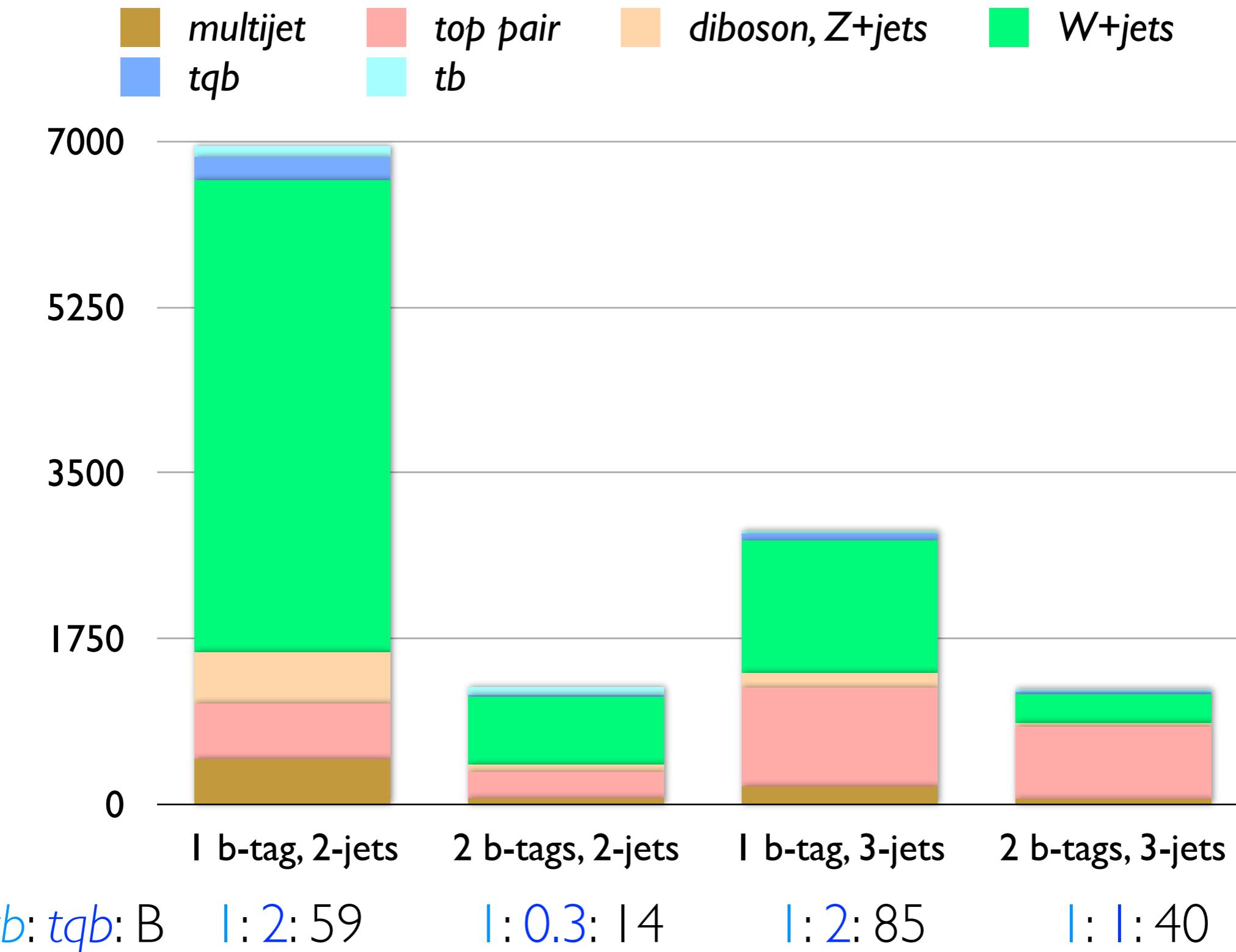
- $W+jets$  enriched sample: 1  $b$ -tag, 2 jets,  $H_T < 175$  GeV



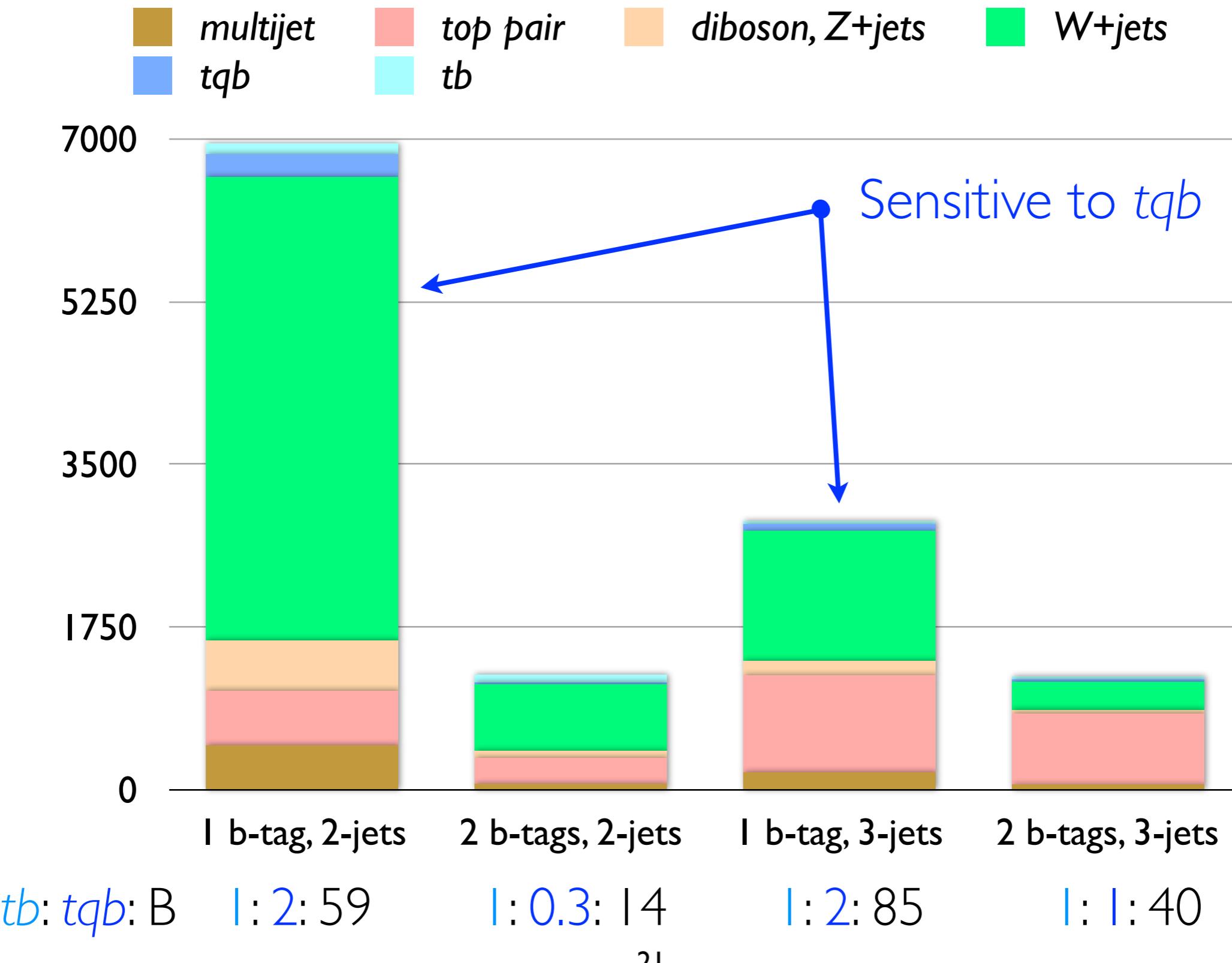
- top pair enriched sample: at least 1  $b$ -tag, 3 jets,  $H_T > 300$  GeV



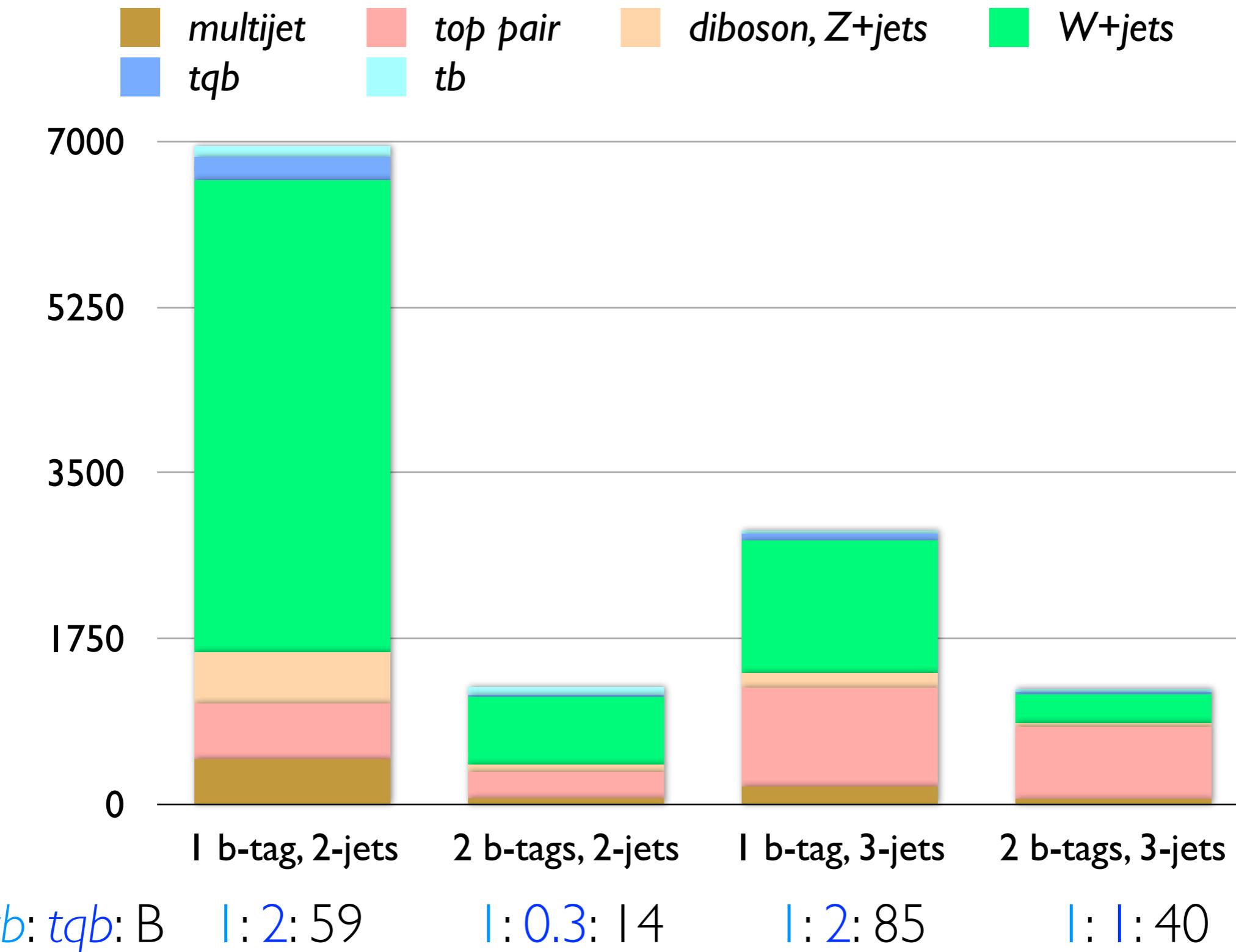
# Background Contributions



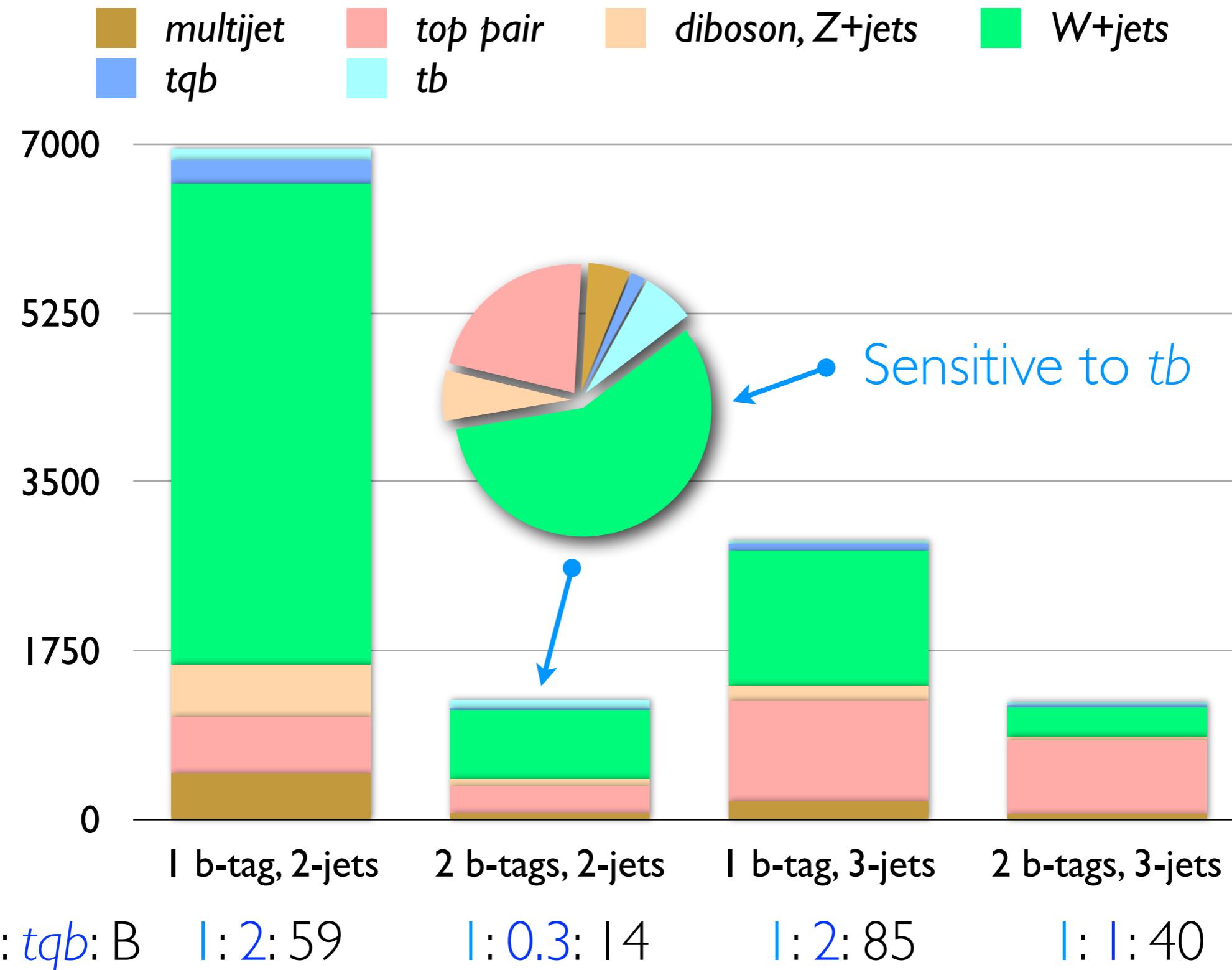
# Background Contributions



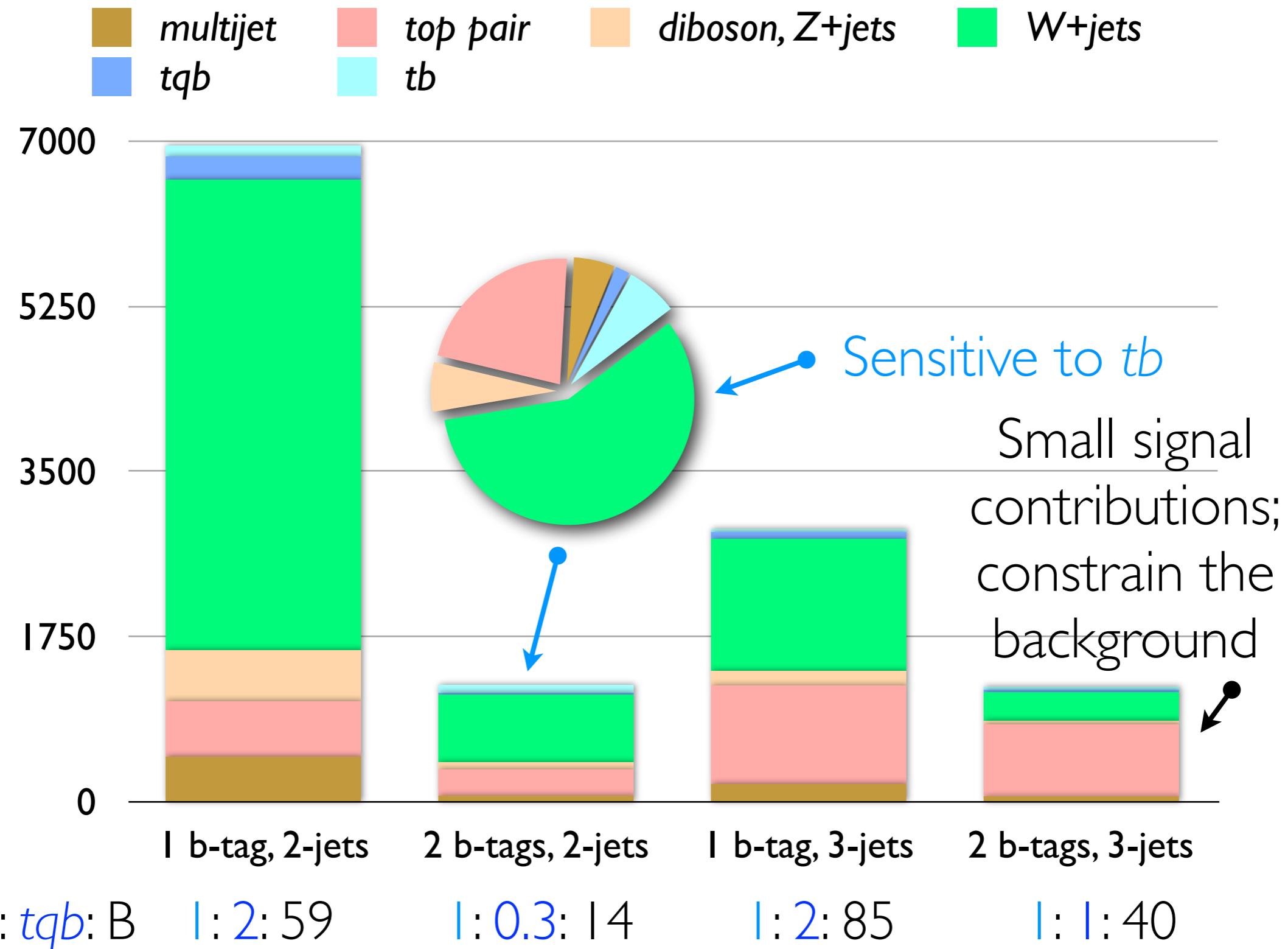
# Background Contributions



# Background Contributions

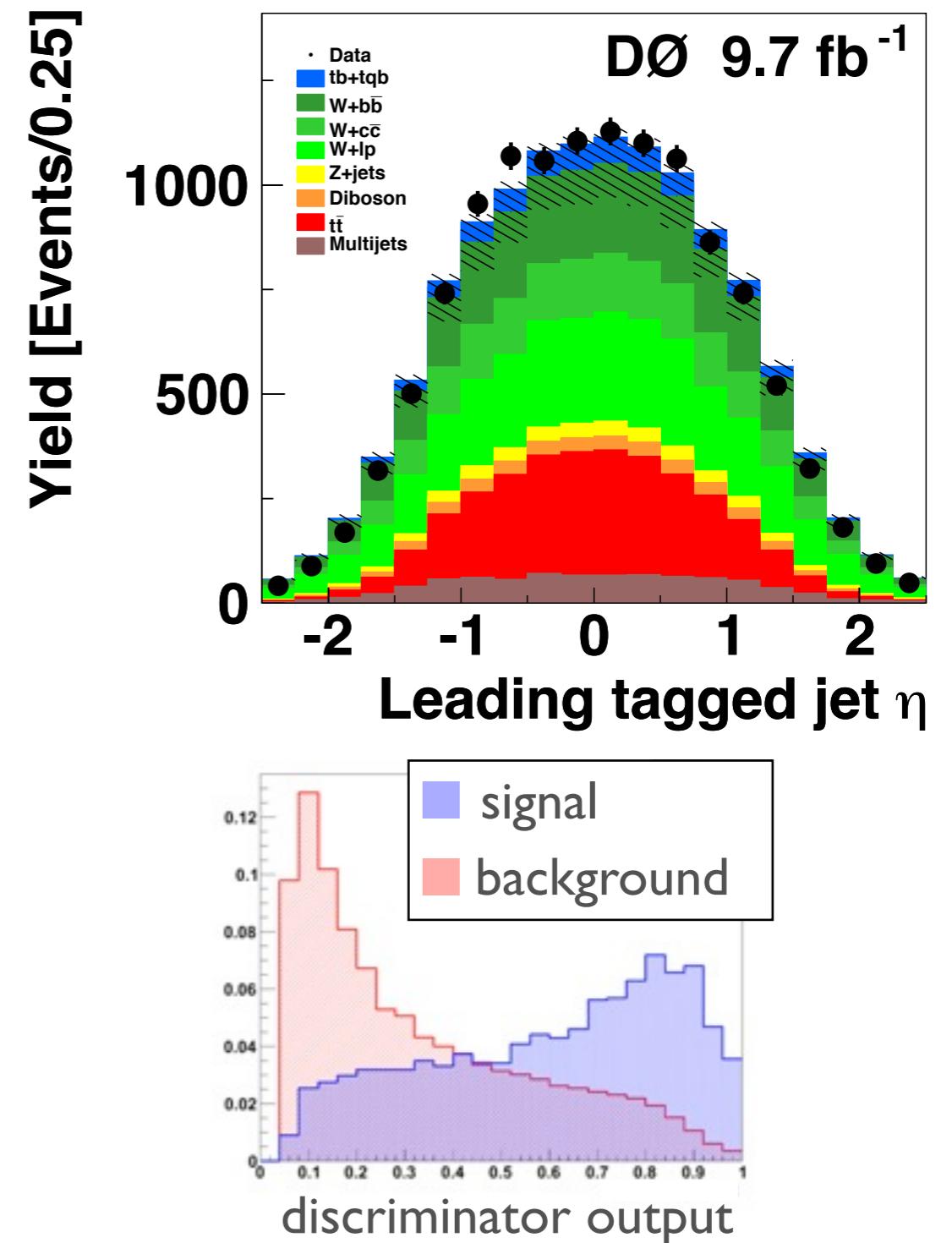


# Background Contributions



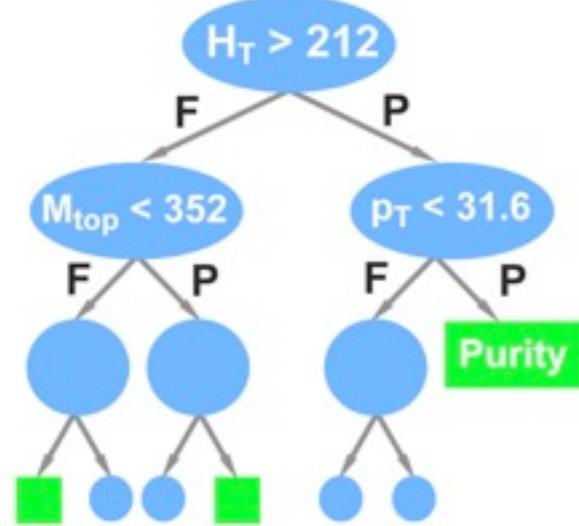
# Not A Counting Experiment

- The amount of signal is less than the uncertainty on the backgrounds
- Not feasible to perform a counting experiment
- Need a variable to separate the signals and backgrounds
- No single kinematic or topological variable is sufficient
- Need a multivariate method

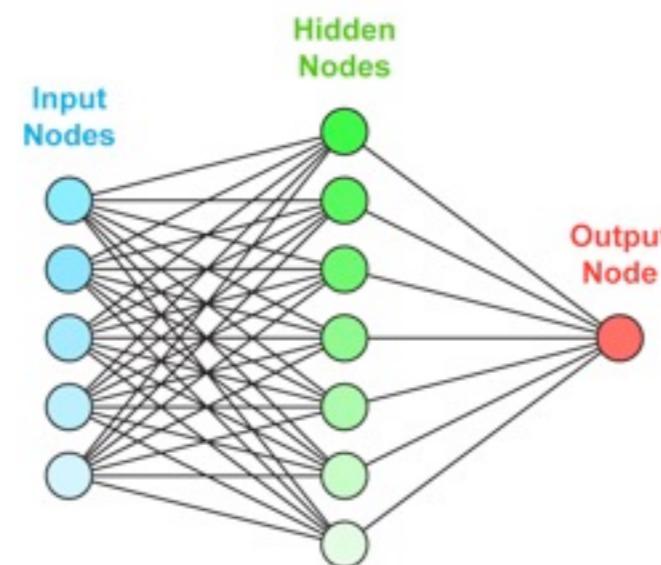


# Multivariate Techniques

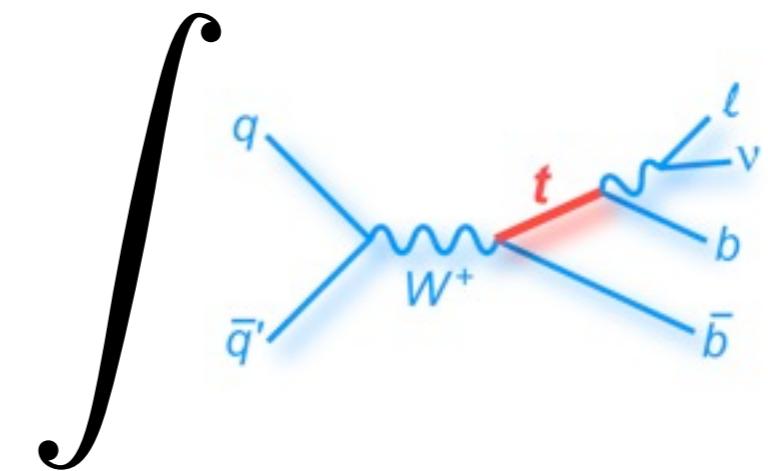
BDT



BNN

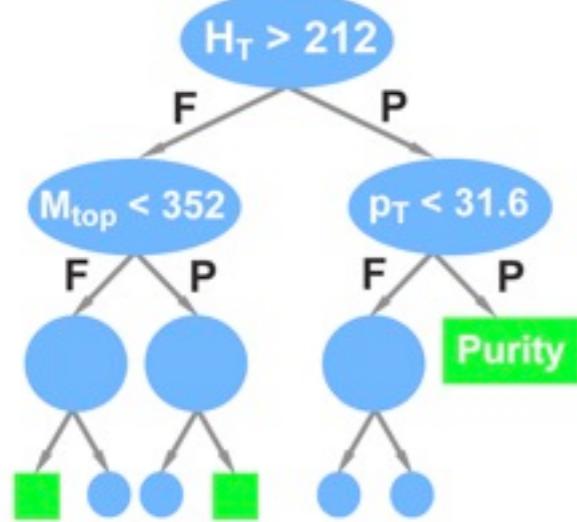


ME

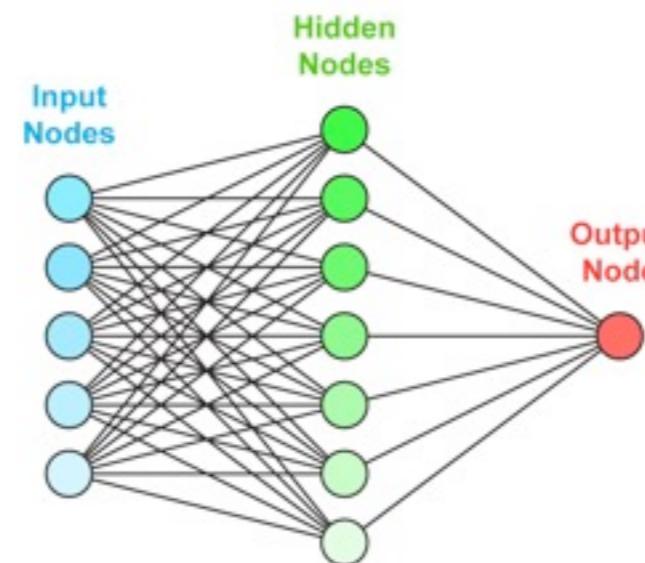


# Multivariate Techniques

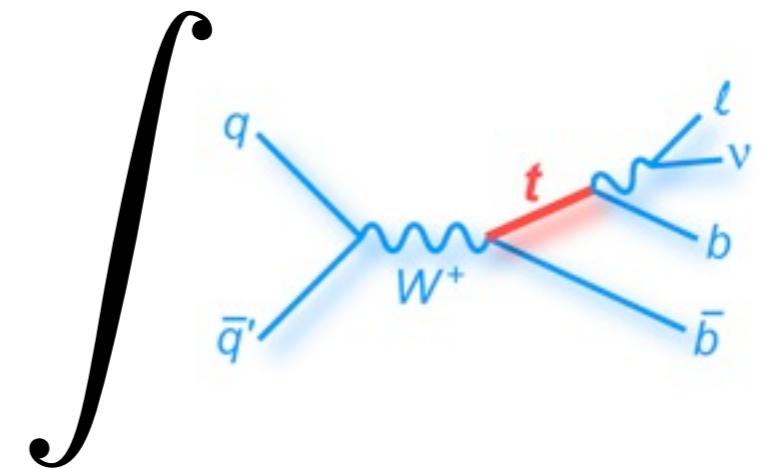
BDT



BNN



ME



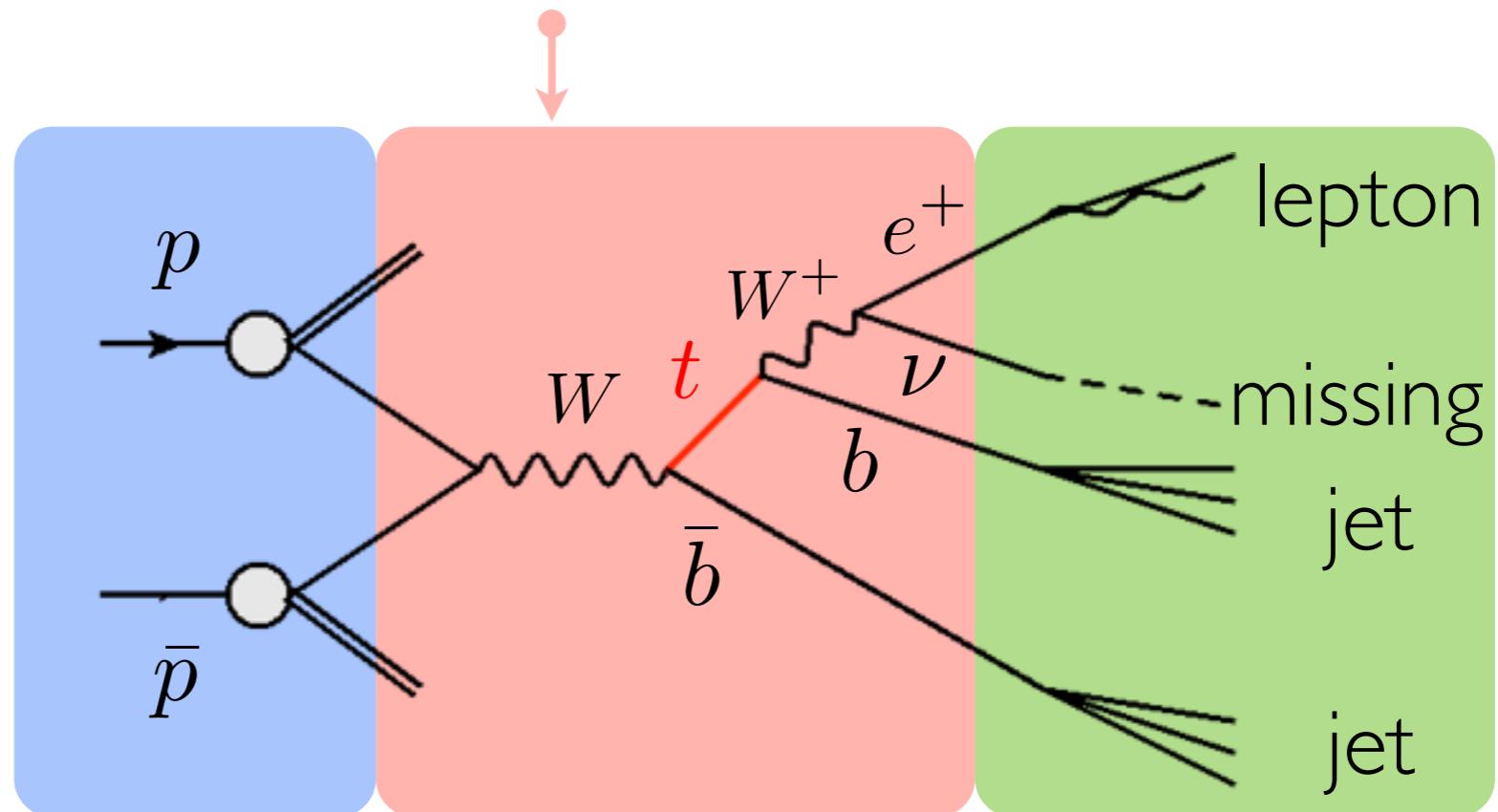
- Machine learning technique
- Use well-described variables ( $KS>0.25$ ) as the input
- Train  $tb$  and  $tqb$  individually  
1/4 MC for training, 1/2 measurement
- Form  $tb$  and  $tqb$  discriminants

- Calculate probabilities
- Form  $tb$  and  $tqb$  likelihood ratios
- Less correlated with the others

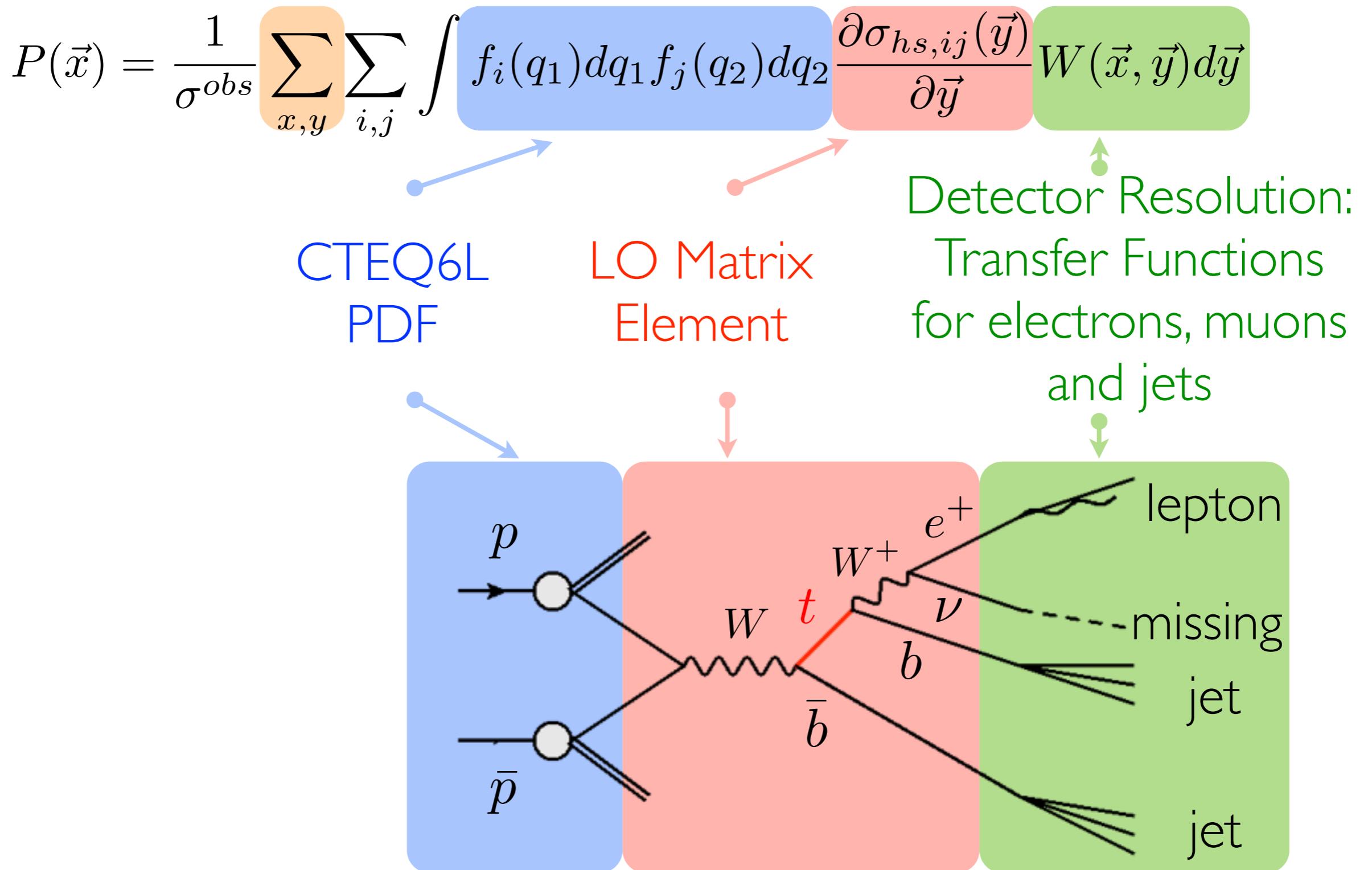
# Matrix Element Method

$$P(\vec{x}) = \frac{1}{\sigma^{obs}} \sum_{x,y} \sum_{i,j} \int f_i(q_1) dq_1 f_j(q_2) dq_2 \frac{\partial \sigma_{hs,ij}(\vec{y})}{\partial \vec{y}} W(\vec{x}, \vec{y}) d\vec{y}$$

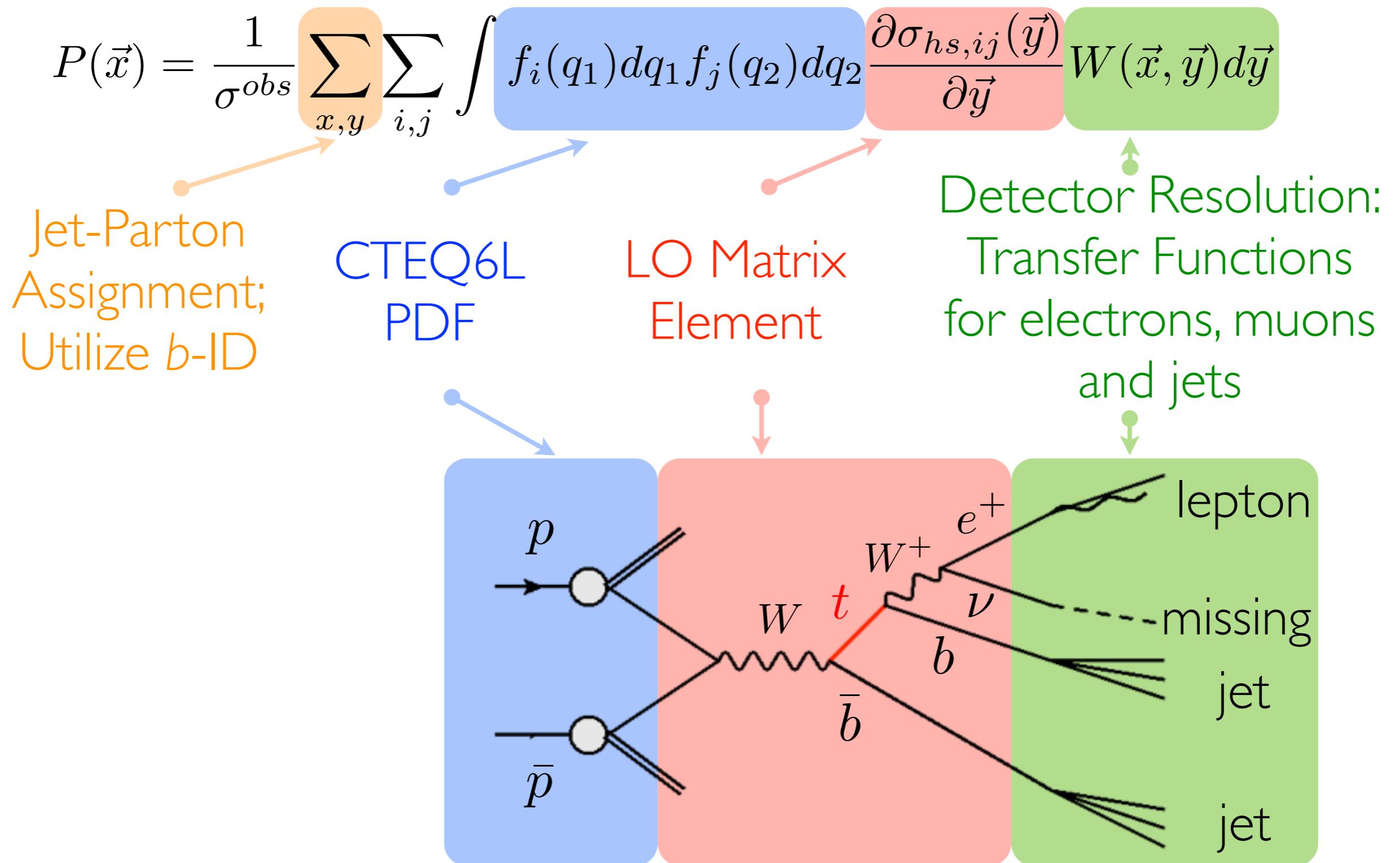
LO Matrix  
Element



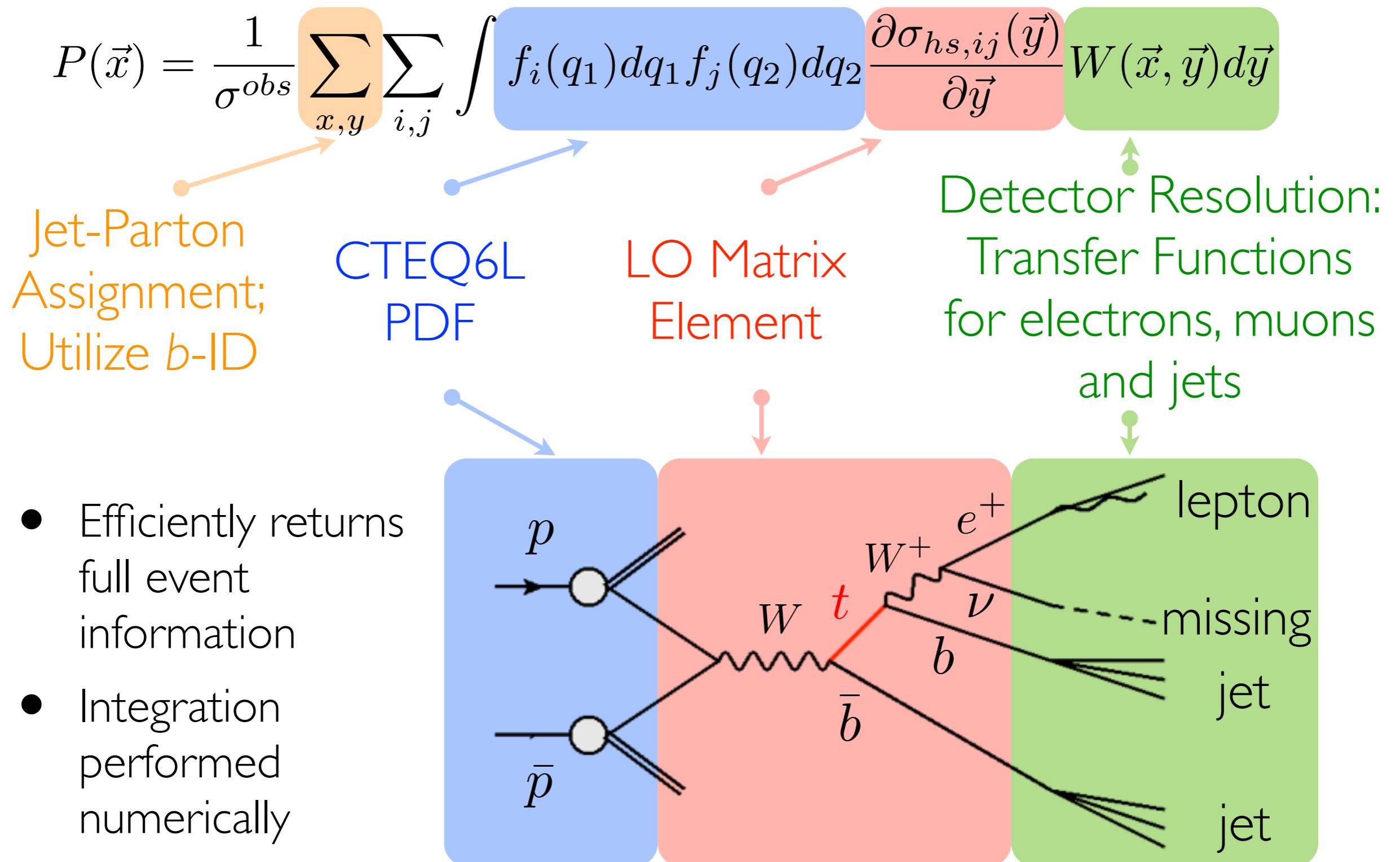
# Matrix Element Method



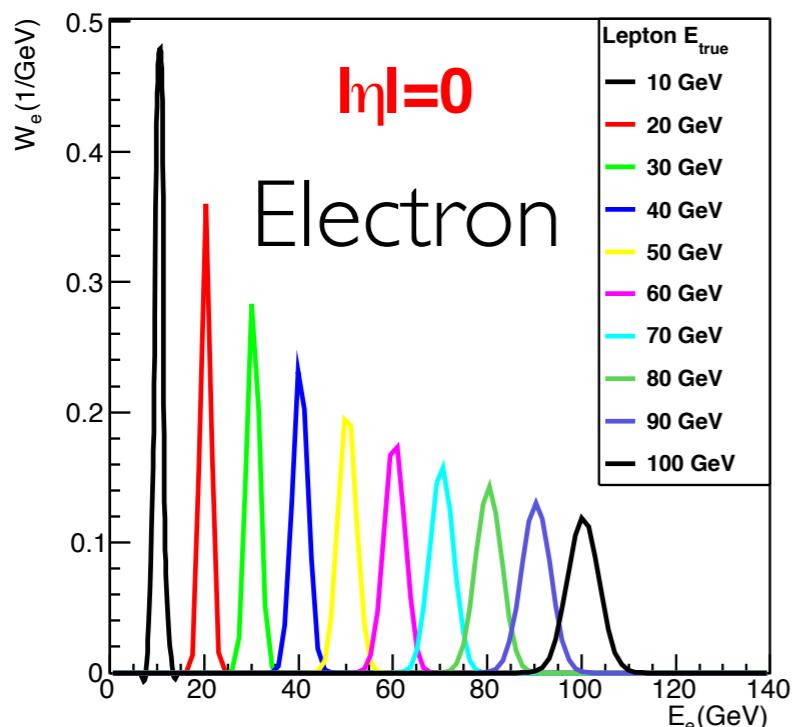
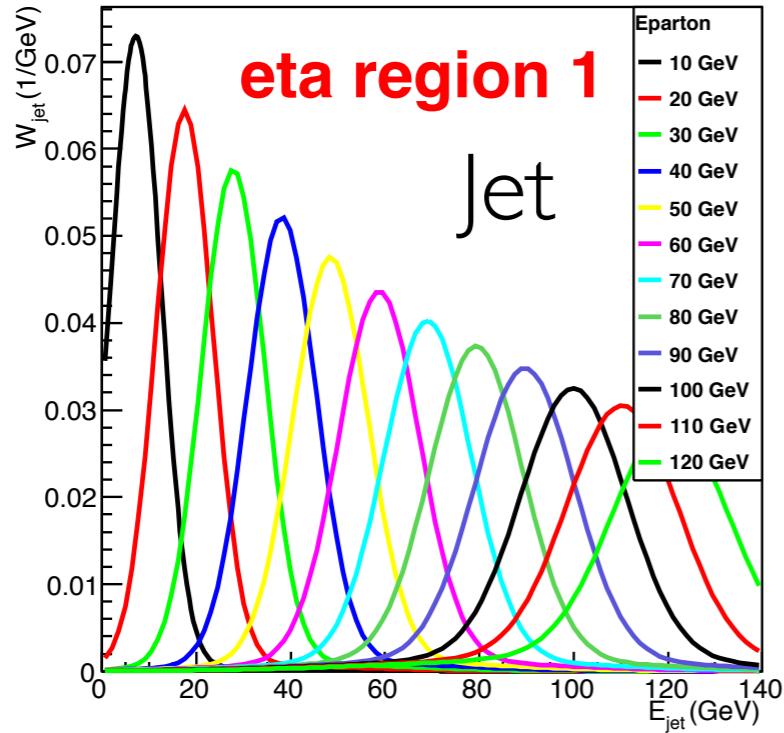
# Matrix Element Method



# Matrix Element Method



# Transfer Functions: $W(\vec{x}, \vec{y})$



- Model the detector resolution effects
- For all final state objects: electrons, muons, jets, and jets mis-reconstructed as electrons
- Gaussian functions of difference between:
  - reconstructed and true energy (electrons, jets, fake electrons)
  - reconstructed and true transverse momentum (muons)
- Parameters determined from the simulated samples

# Matrix Element Processes

Two Jets		Three Jets	
Name	Process	Name	Process
$\textcolor{cyan}{tb}$	$u\bar{d} \rightarrow t\bar{b}$	$\textcolor{cyan}{tbg}$	$u\bar{d} \rightarrow t\bar{b}g$
$tq$	$ub \rightarrow td$ $\bar{d}b \rightarrow t\bar{u}$	$\textcolor{blue}{tqb}$	$ug \rightarrow t\bar{d}\bar{b}$ $\bar{d}g \rightarrow t\bar{u}\bar{b}$
		$\textcolor{blue}{tqg}$	$ub \rightarrow tdg$ $\bar{d}b \rightarrow t\bar{u}g$
$Wbb$	$u\bar{d} \rightarrow Wb\bar{b}$	$Wbbg$	$u\bar{d} \rightarrow Wb\bar{b}g$
$Wcg$	$sg \rightarrow Wcg$	$Wugg$	$\bar{u}g \rightarrow W\bar{u}gg$
$Wgg$	$u\bar{d} \rightarrow Wgg$		
$WW$	$u\bar{u} \rightarrow WW$		
$WZ$	$u\bar{d} \rightarrow WZ$		
$ggg$	$gg \rightarrow ggg$		
$t\bar{t}$	$u\bar{u} \rightarrow t\bar{t}$	$t\bar{t}$	$u\bar{u} \rightarrow t\bar{t}$

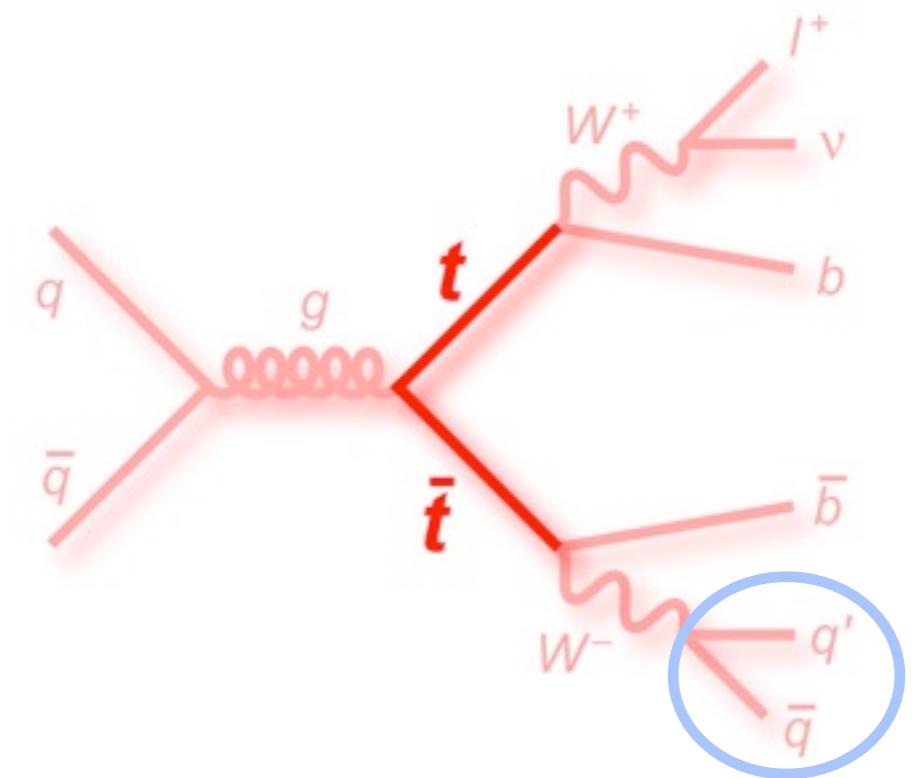
- the more background diagrams, the better discrimination

# Dimensionality of Phase Space

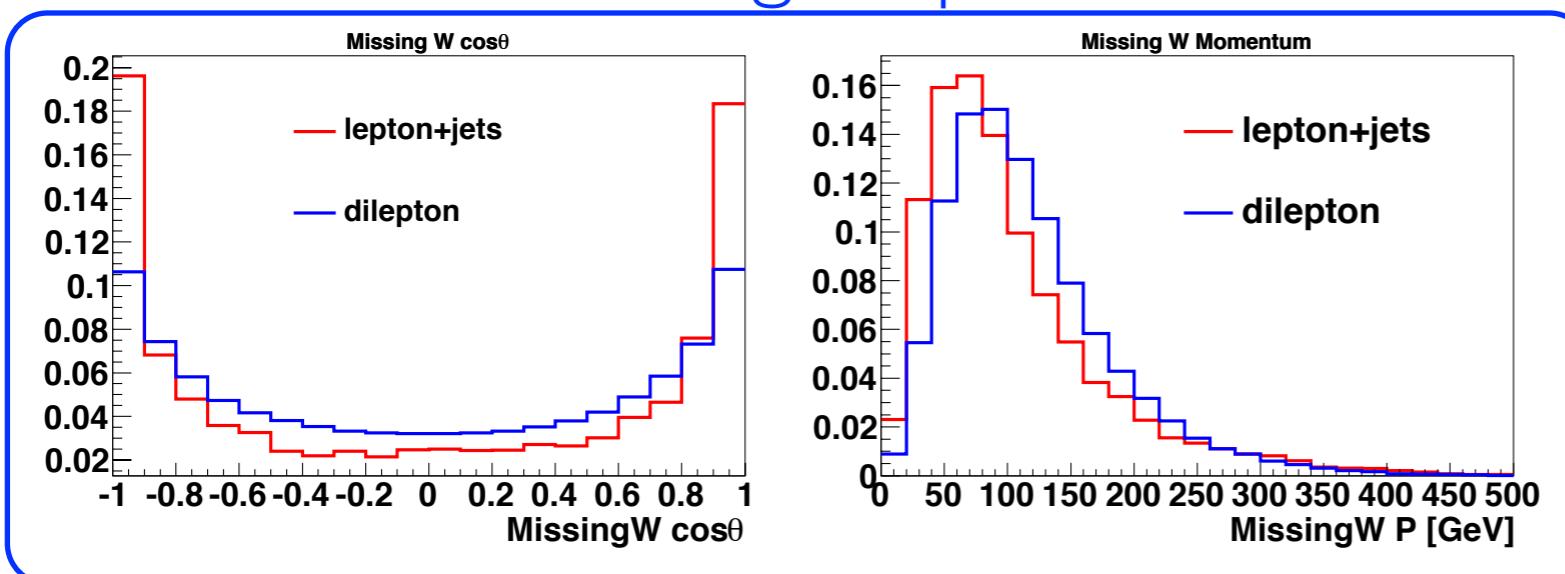
	D.O.F.	$n=4$ (2jets)	$n=5$ (3jets)
2 initial and $n$ final state objects	$(2+n) \times 4$	24	28
Energy and momentum conservation	-4	-4	-4
All masses are known	$-(2+n)$	-6	-7
The initial partons are in $z$ -axis	$-2 \times 2$	-4	-4
The directions of the final objects are well measured, except neutrinos	$-2 \times (n-1)$	-6	-8
Remaining dimensions	$n$	4	5
Final integration for signals		$S_W, S_t, P_q, P_{q,z}^{\text{tot}}$	$S_W, S_t, P_q, P_{q',z}^{\text{tot}}$

# Top Pair Modeling

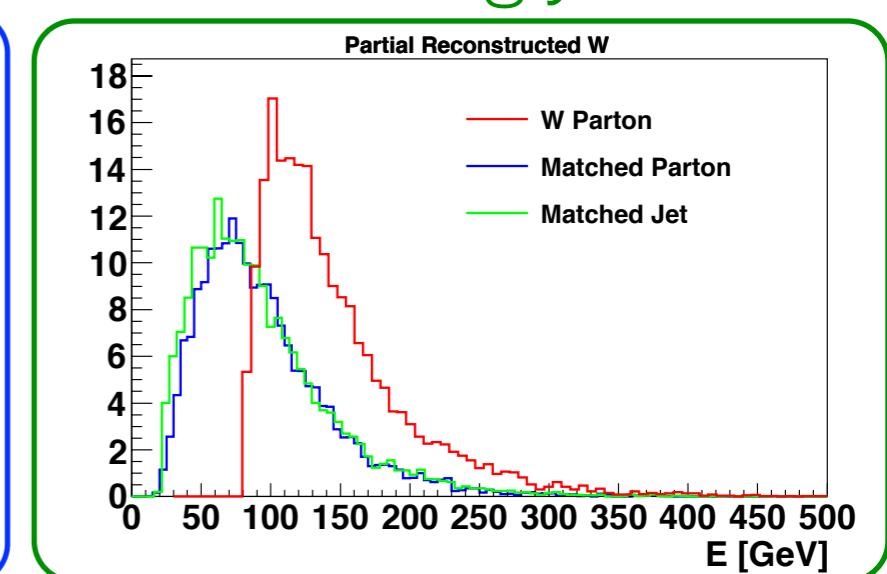
- Top pair  $\rightarrow l\nu b\bar{q}q'b$  (4 jets)
- Top pair yields in 2jet & 3jet channels are comparable to single top
- Light-jets are 1.6 times more likely to be lost than  $b$ -jets
- Use simulation to obtain a prior of missing jet (3jet) or missing  $W$  (2jet)



Missing  $W$  prior



Missing Jet



# Discriminant

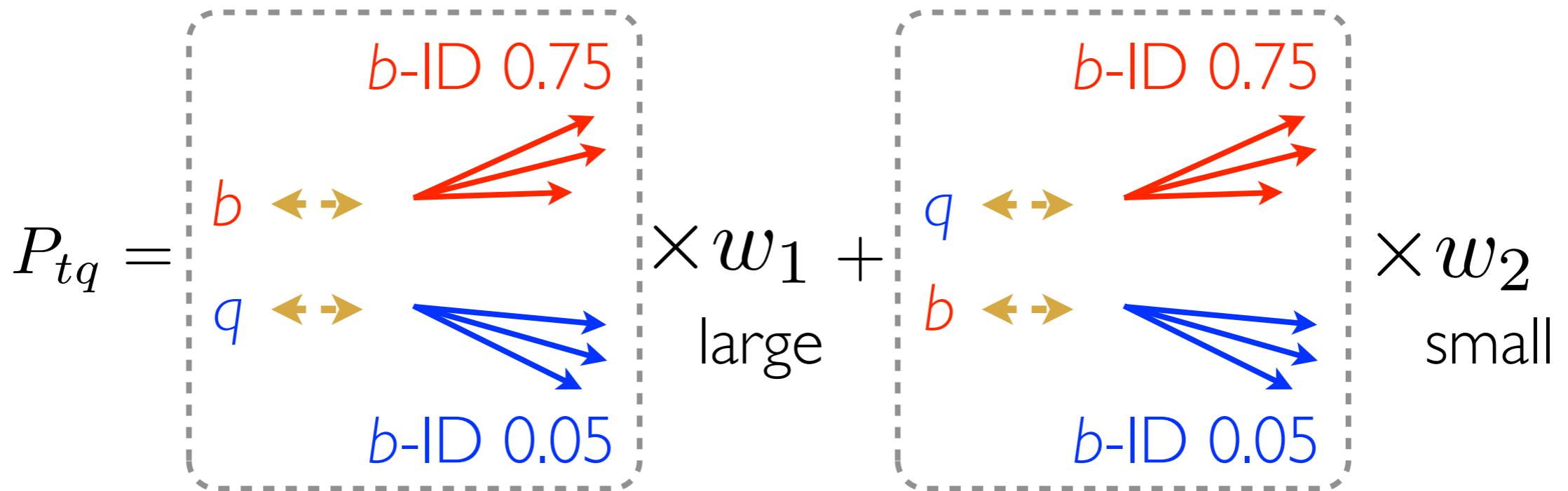
- $b$ -ID output information included

$$P_{tq} = \begin{array}{c} b \\ q \end{array} \leftrightarrow \begin{array}{c} b\text{-ID } 0.75 \\ b\text{-ID } 0.05 \end{array} \times w_1 + \begin{array}{c} q \\ b \end{array} \leftrightarrow \begin{array}{c} b\text{-ID } 0.75 \\ b\text{-ID } 0.05 \end{array} \times w_2$$

The diagram illustrates a discriminant function  $P_{tq}$  as a weighted sum of two components. Each component consists of a pair of inputs ( $b$  and  $q$ ) and their corresponding  $b$ -ID values (0.75 and 0.05). The first component is labeled 'large' and has weight  $w_1$ . The second component is labeled 'small' and has weight  $w_2$ . The inputs  $b$  and  $q$  are shown with double-headed arrows indicating they can be either  $b$  or  $q$ .

# Discriminant

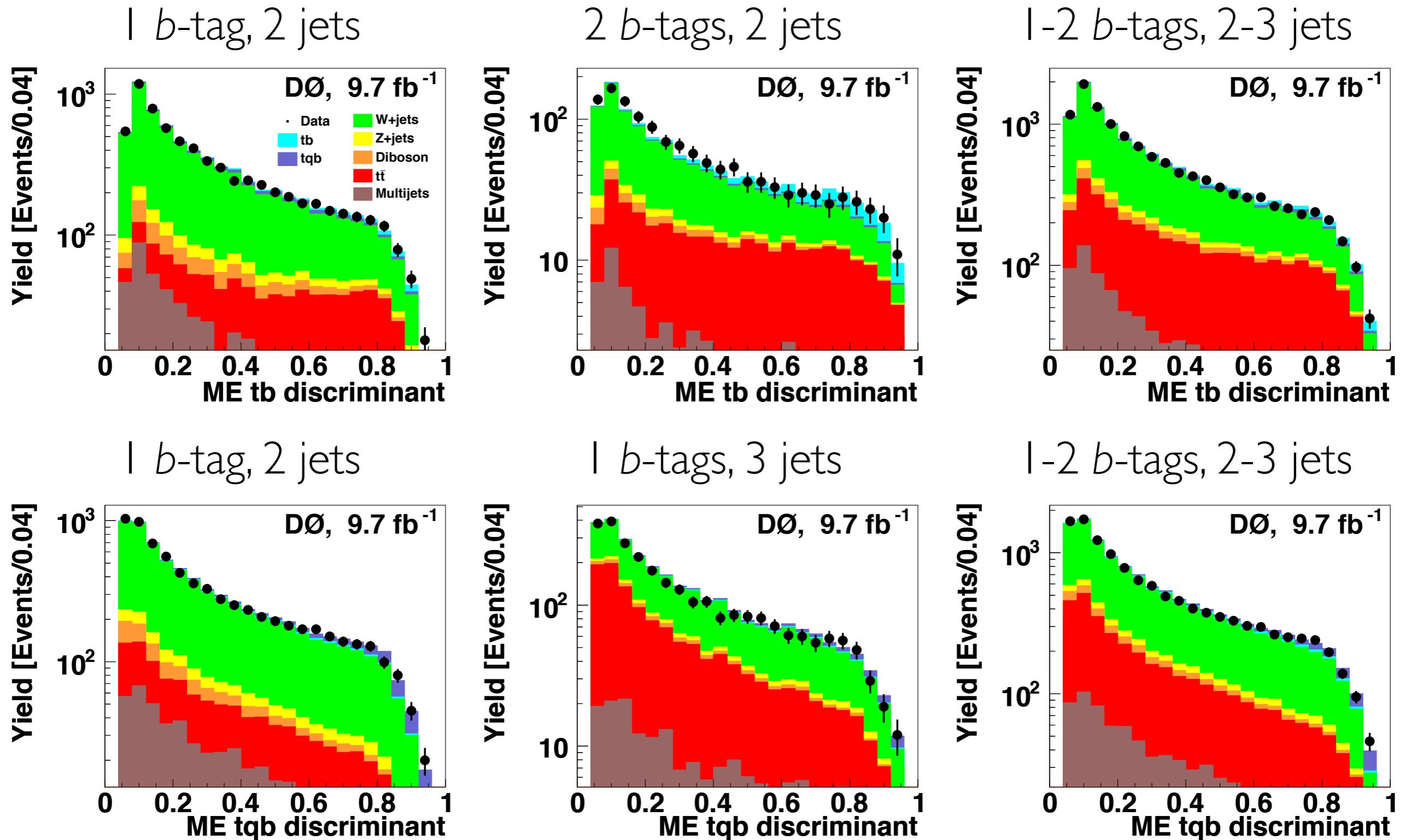
- $b$ -ID output information included



- Discriminant: Likelihood ratio

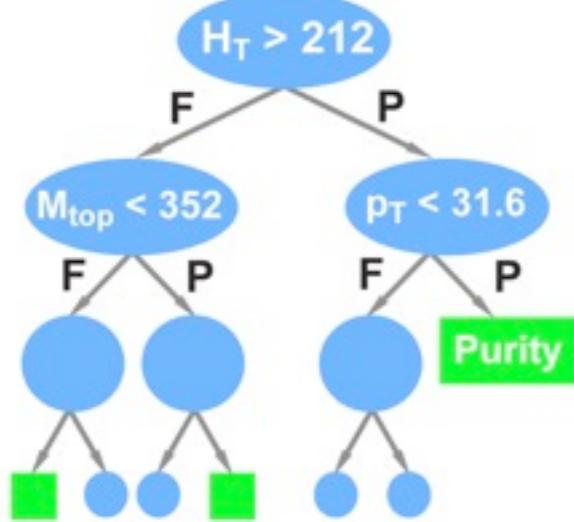
$$D(x) = \frac{P_{sig}(x)}{P_{sig}(x) + P_{bkgd}(x)}$$

# ME Discriminant

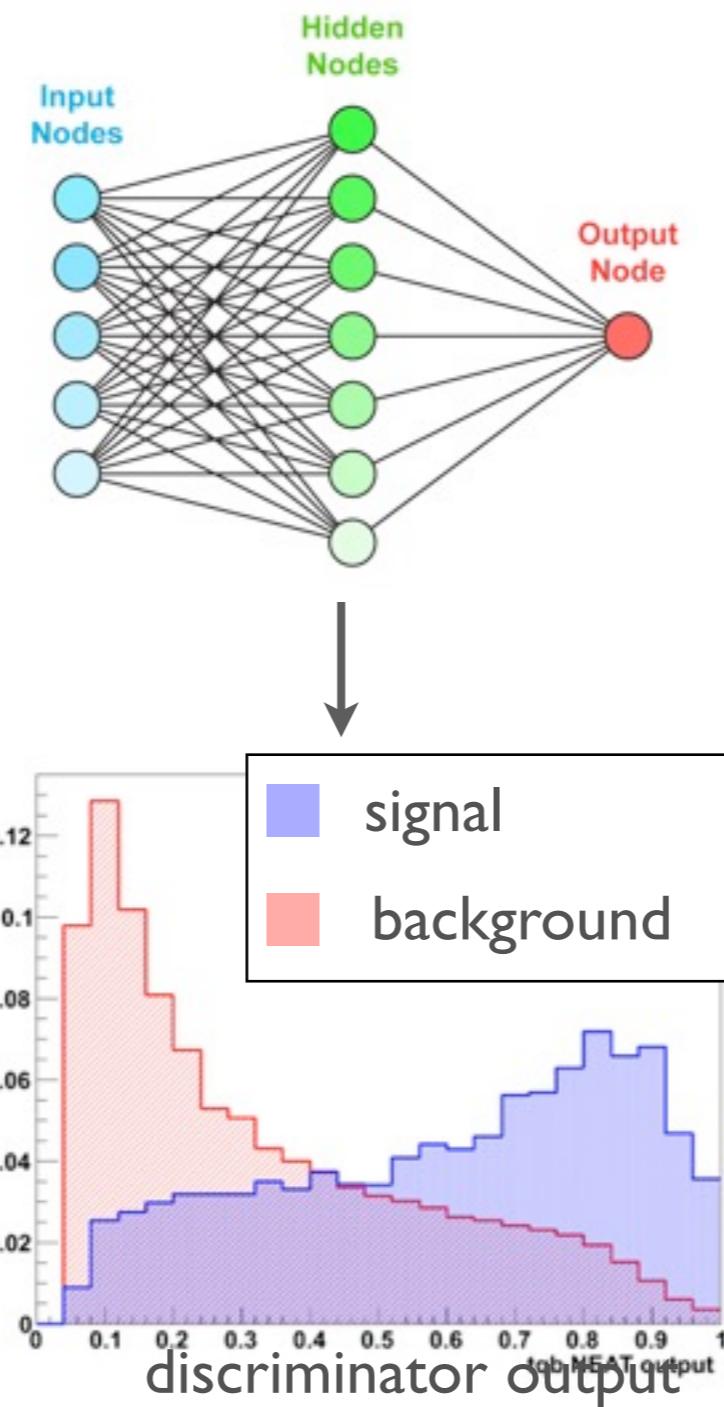


# BNN Combination

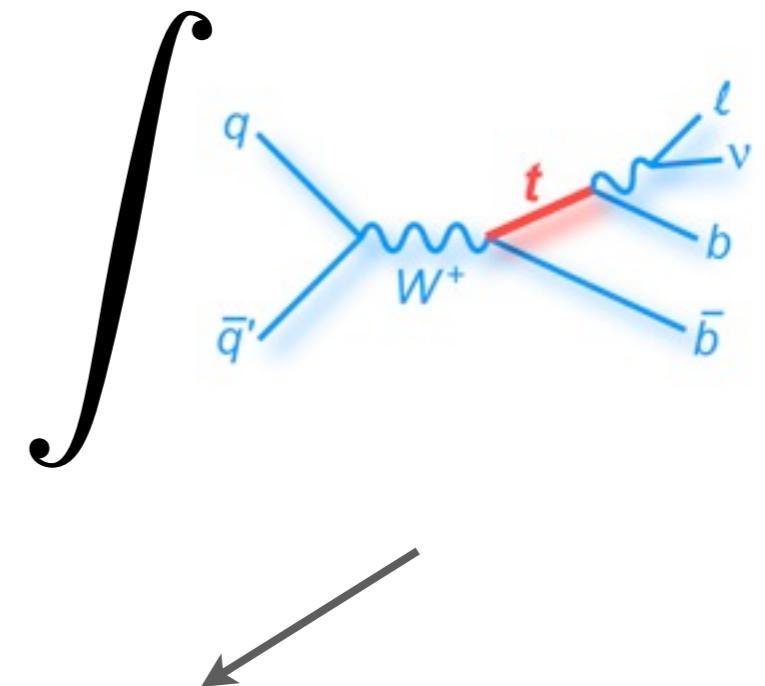
BDT



BNN



ME

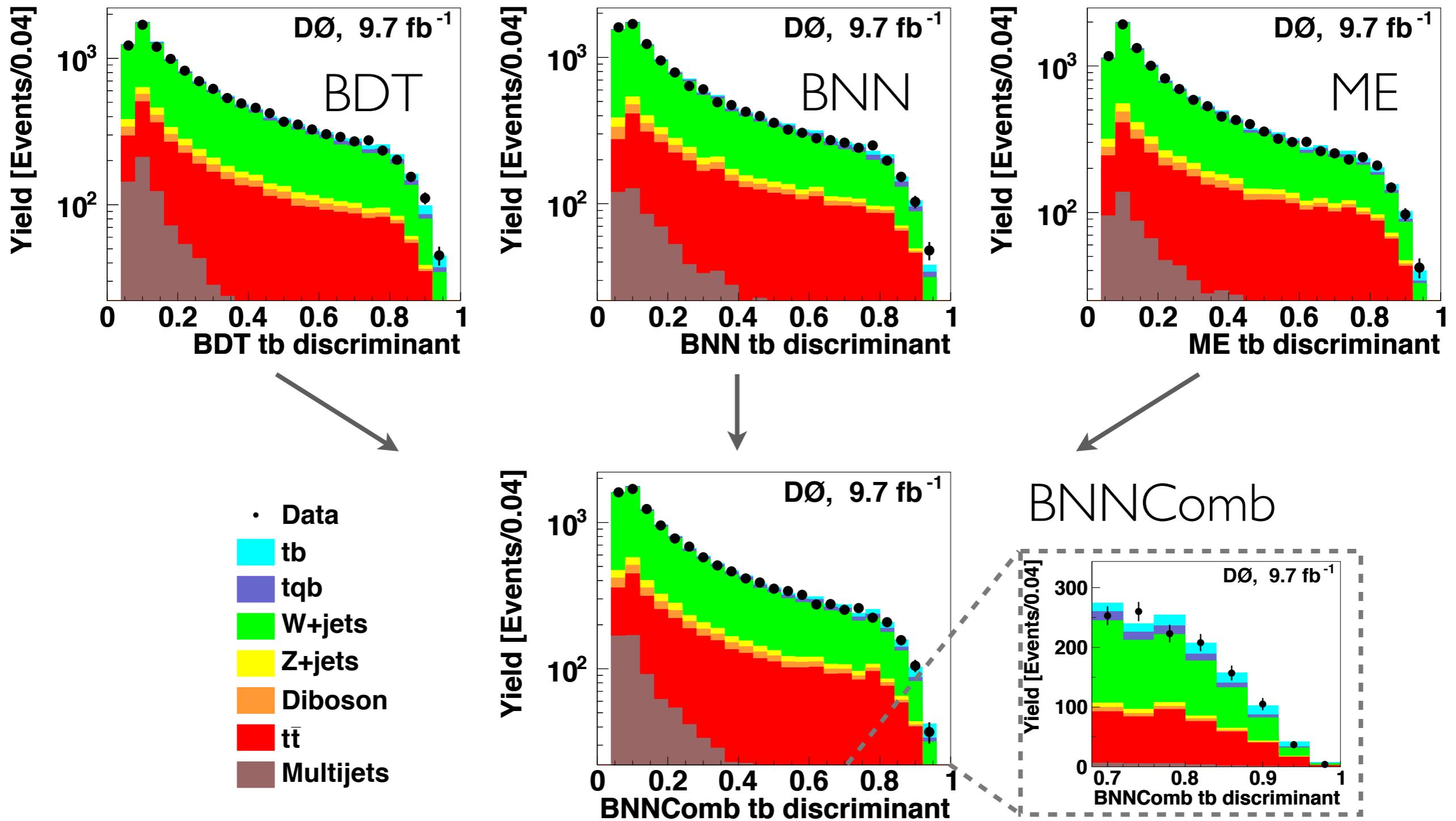


Use BNN to  
combine the 3  
methods

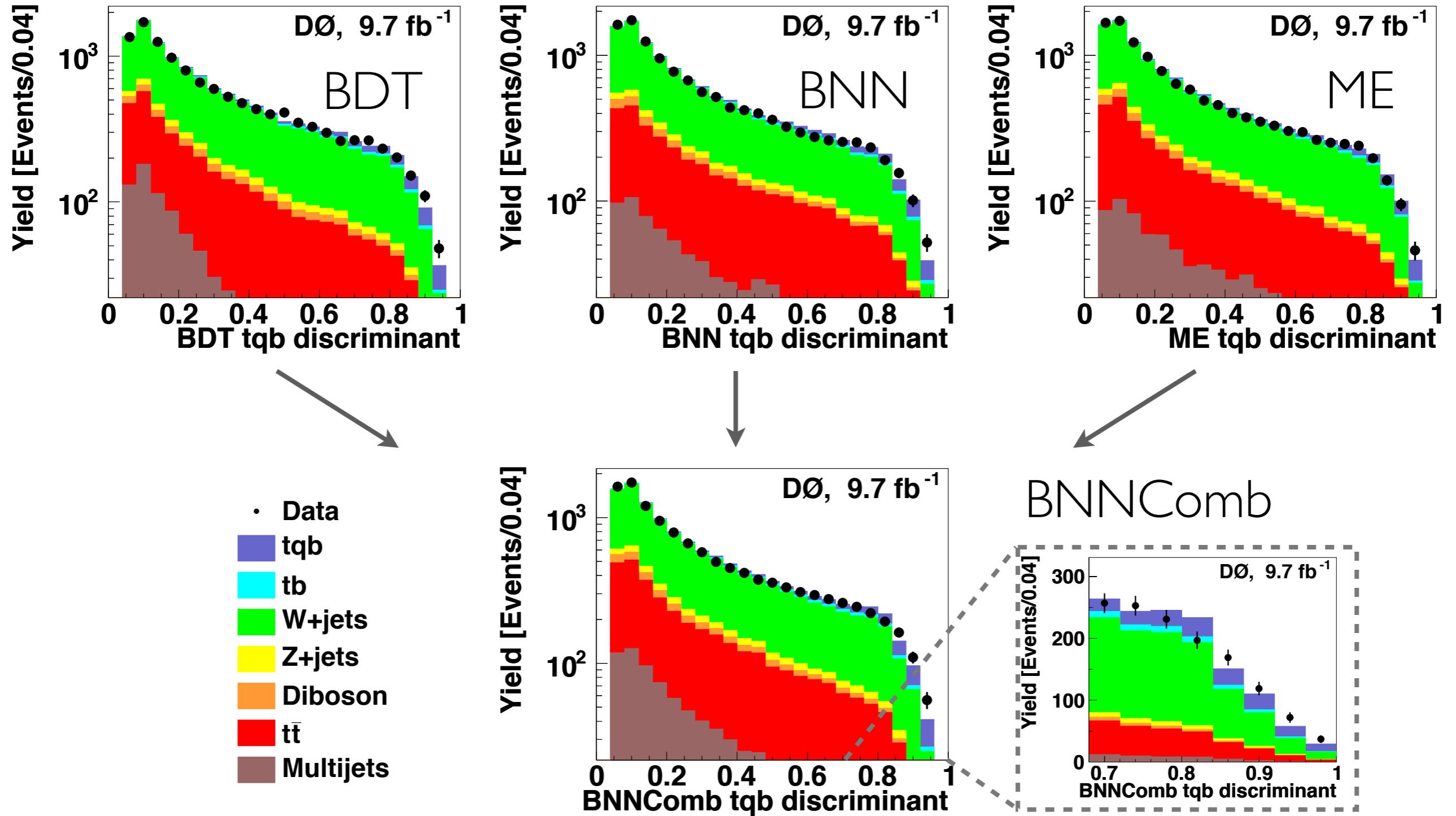
Correlations

BDT  
77%  
↔  
BNN  
↔  
ME  
75%  
73%

# BNN $tb$ Combination

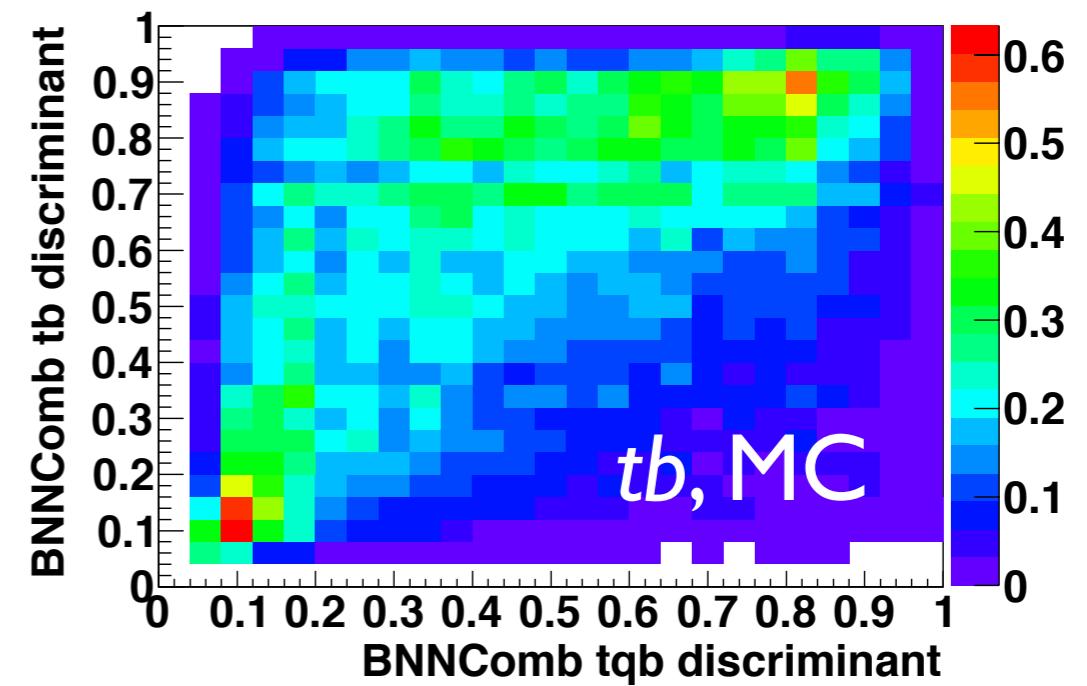
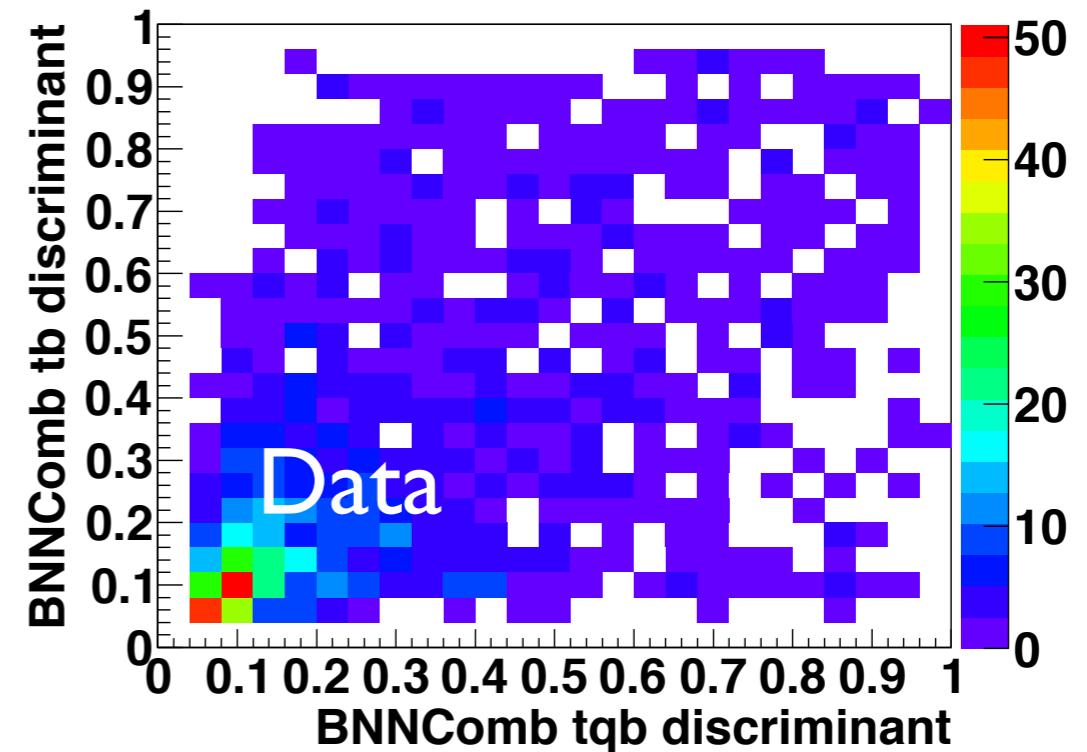


# BNN $tqb$ Combination



# New Discriminant

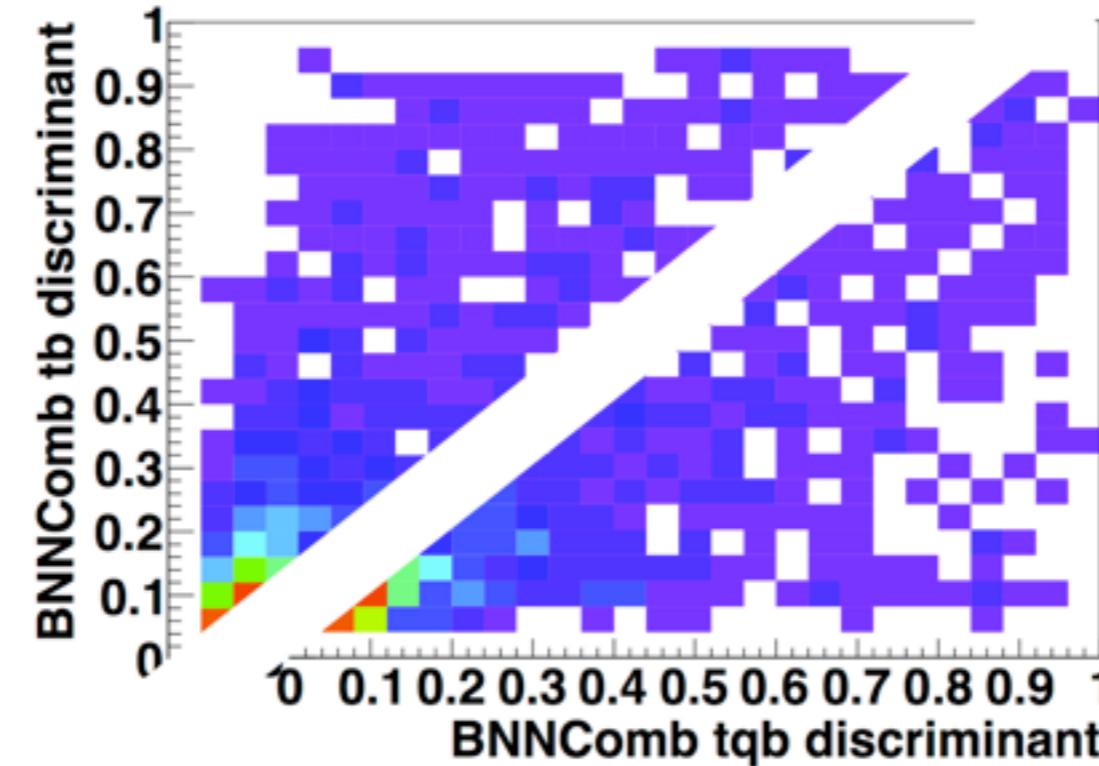
- Aim to simultaneously measure  $tb$  and  $tqb$  signals without assuming the SM prediction for either
- At a first step, use a discriminant sensitive to both signals
- Ensure each bin containing enough statistics to have a stable measurement



# New Discriminant

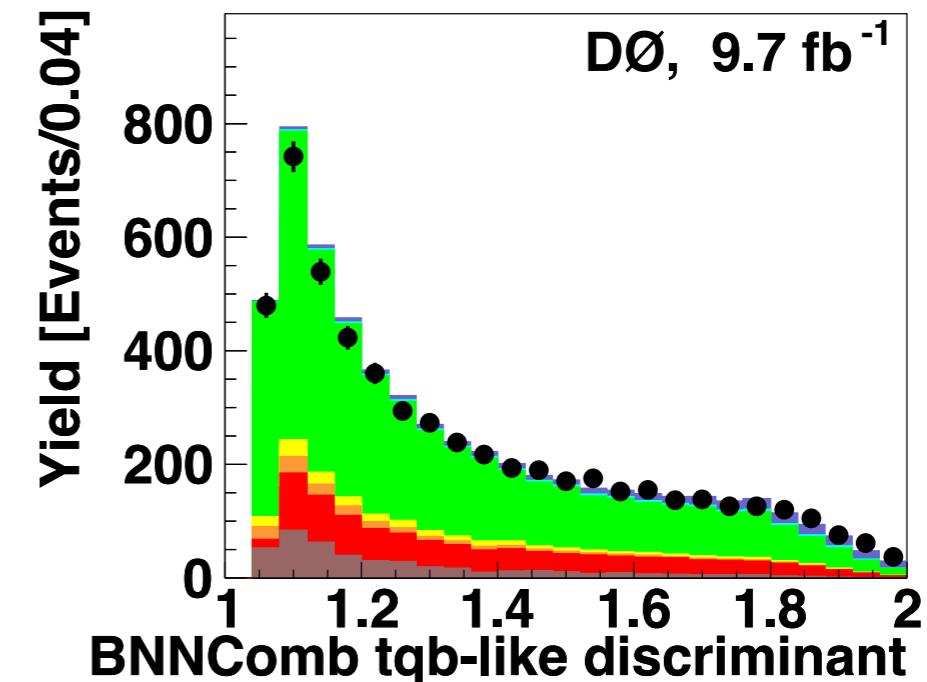
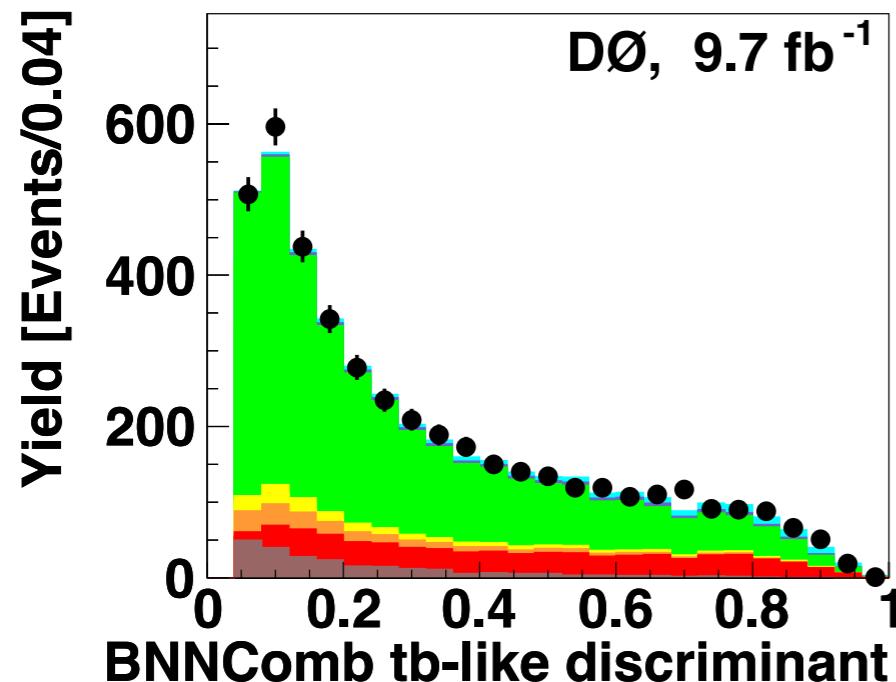
If  $D_{tb} > D_{tqb}$ :

- $tb$  category
- Use  $D_{tb}$
- Plot in the range  $[0, 1]$



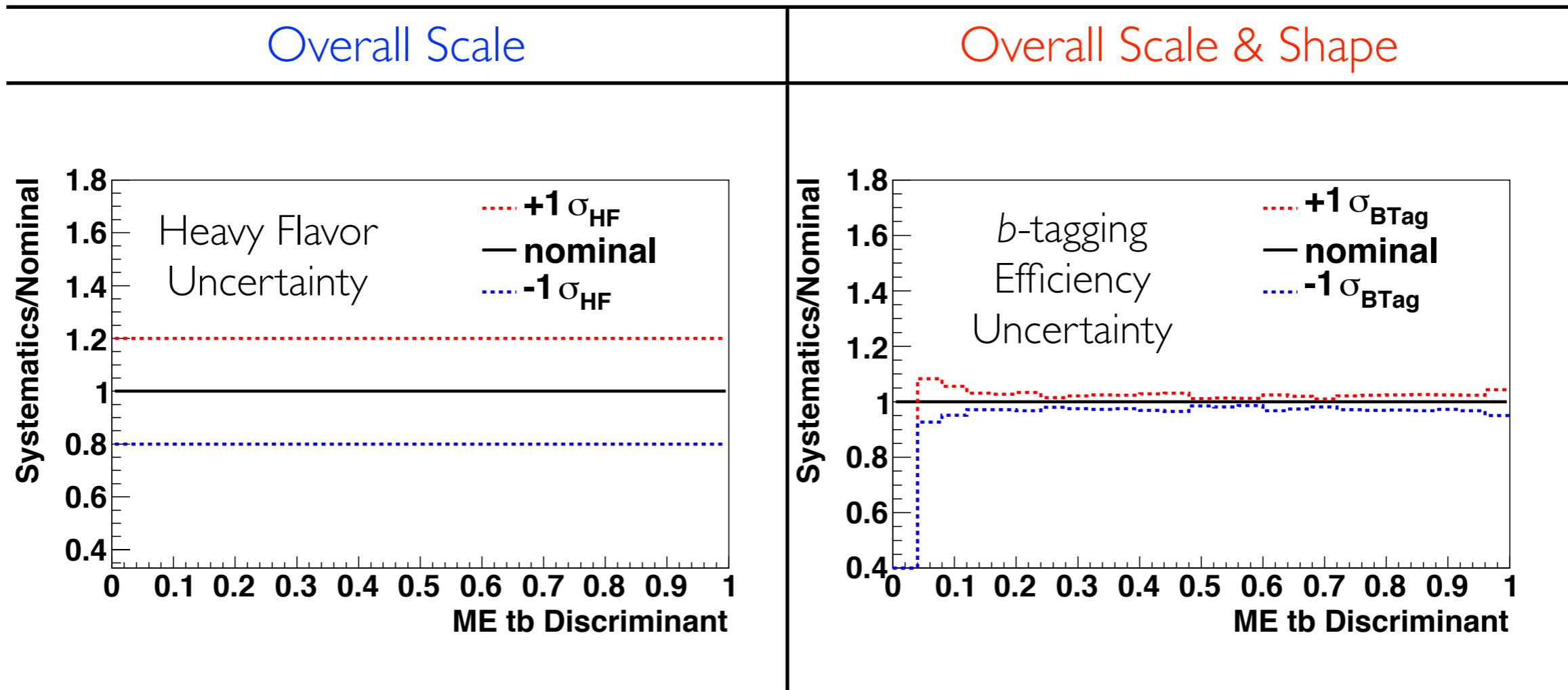
If  $D_{tqb} > D_{tb}$ :

- $tqb$  category
- Use  $D_{tqb}$
- Plot in the range  $[1, 2]$



# Systematic Uncertainties

- Assign to each background and each analysis channel
- Some affect only the **overall scale**, and others affect also the **discriminant outputs bin-by-bin (shape-changing)**



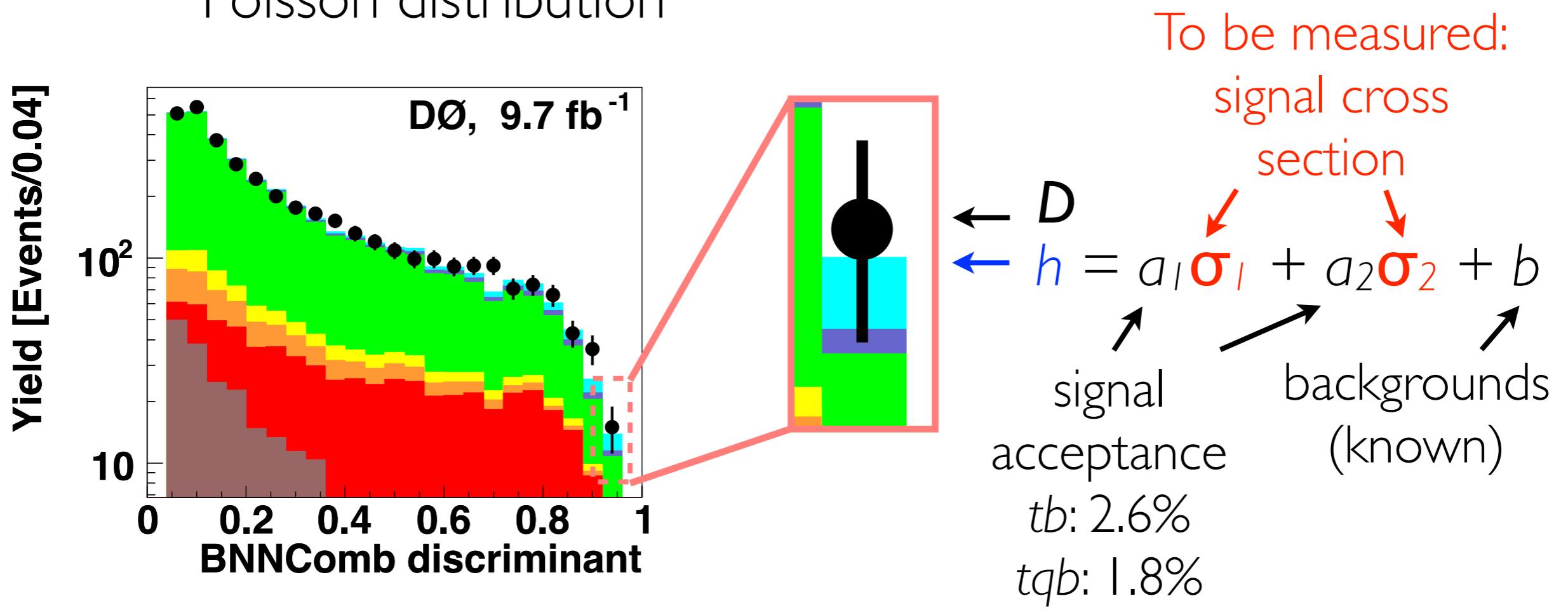
# Systematic Uncertainties

- Assign to each background and each analysis channel
- Some affect only the **overall scale**, and others affect also **the discriminant outputs bin-by-bin (shape-changing)**
- Main uncertainties are listed here

Overall Scale	Overall Scale & Shape
Integrated luminosity	6.1%
Top pair cross section	9%
Diboson cross section	7%
Trigger efficiencies	(3-5)%
Jet fragmentation+higher order	(0.7-7.0)%
Initial- and final-state radiation	(0.8-10.9)%
Heavy-flavor correction	20%
Multijet normalization	(9.2-42.1)%
	Jet reconstruction up to 1.4%
	Jet energy resolution up to 1.1%
	Jet energy scale up to 1.2%
	Flavor-dependent JES up to 1.3%
	Jet vertex confirmation up to 11%
	<i>b</i> -ID, 1 <i>b</i> -tagged channel up to 6.6%
	<i>b</i> -ID, 2 <i>b</i> -tagged channel up to 8.8%

# Cross Section Extraction

- Use the BNN combination discriminant in 25 bins
  - Use all bins (we don't cut on the discriminant)
- For each bin, the likelihood  $L$  to observe  **$D$  data events** with a **known mean  $h$**  is modeled by the Poisson distribution

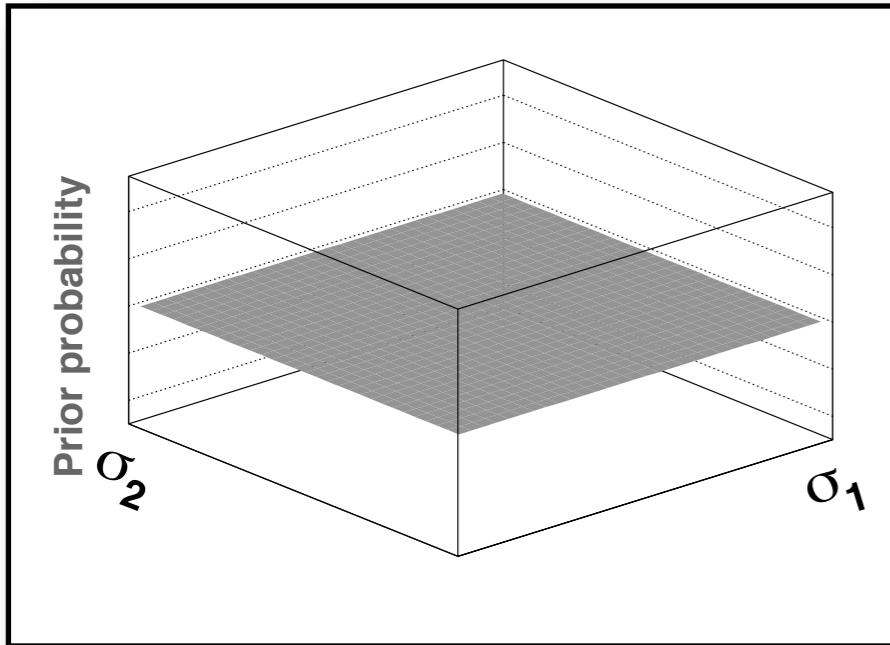


# Bayesian Approach

Poisson likelihood

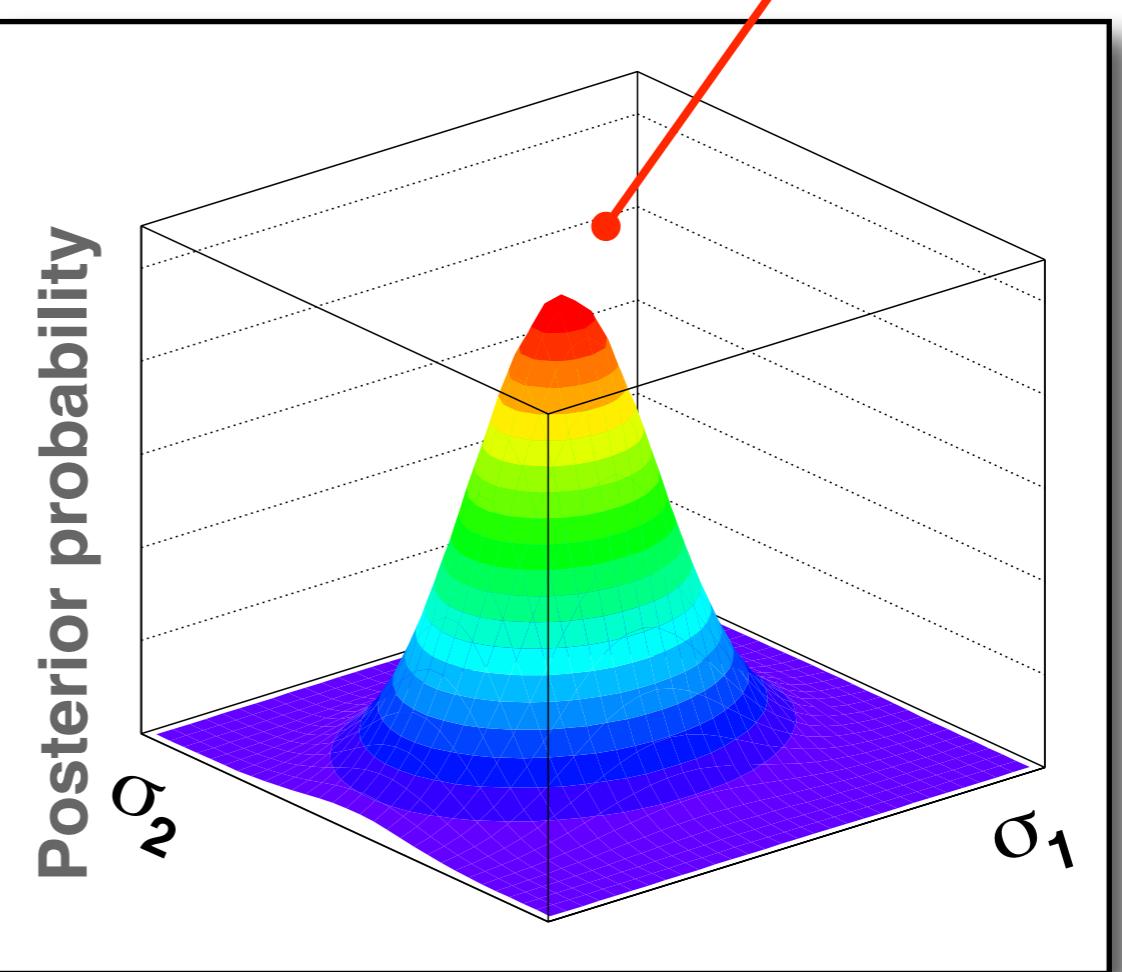
$$\int L(\mathbf{D}|\sigma_1, \sigma_2, \mathbf{a}_1, \mathbf{a}_2, \mathbf{b}) \pi(\sigma_1, \sigma_2) \pi(\mathbf{a}_1, \mathbf{a}_2, \mathbf{b}) d\mathbf{a}_1 d\mathbf{a}_2 db \propto p(\sigma_1, \sigma_2 | D)$$

Uniform prior for the signal cross section

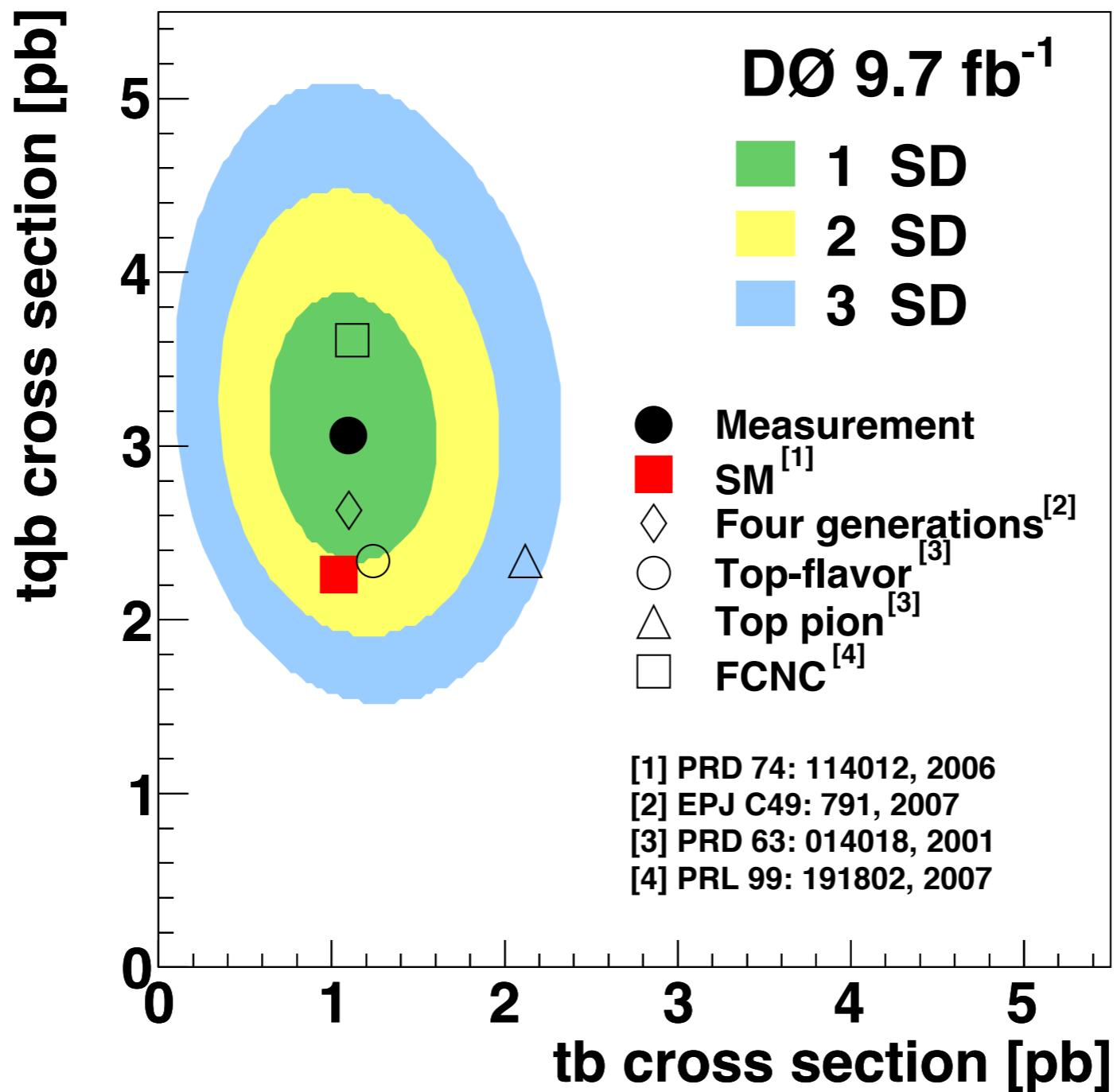


Our state of knowledge,  $a, b$  with systematic uncertainties

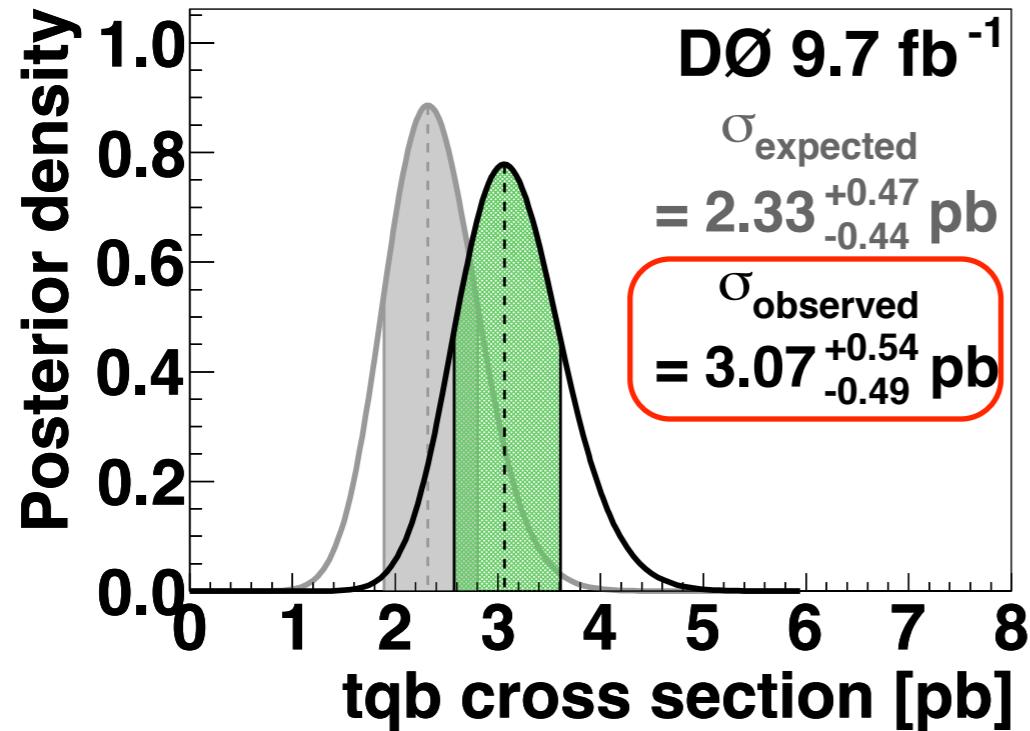
All systematics and their correlations taken into account



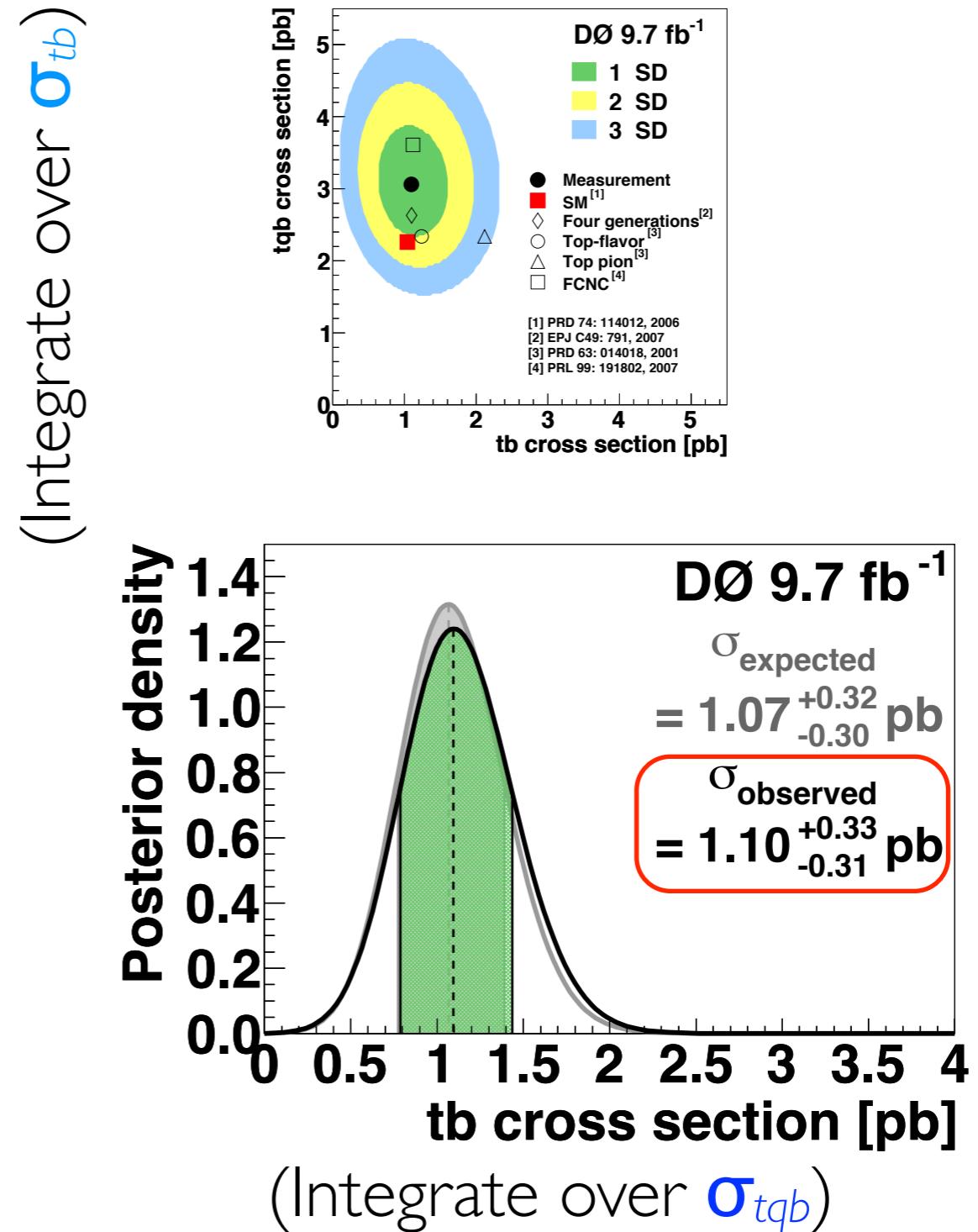
# Two-dimensional Posterior



# Measured Cross Section

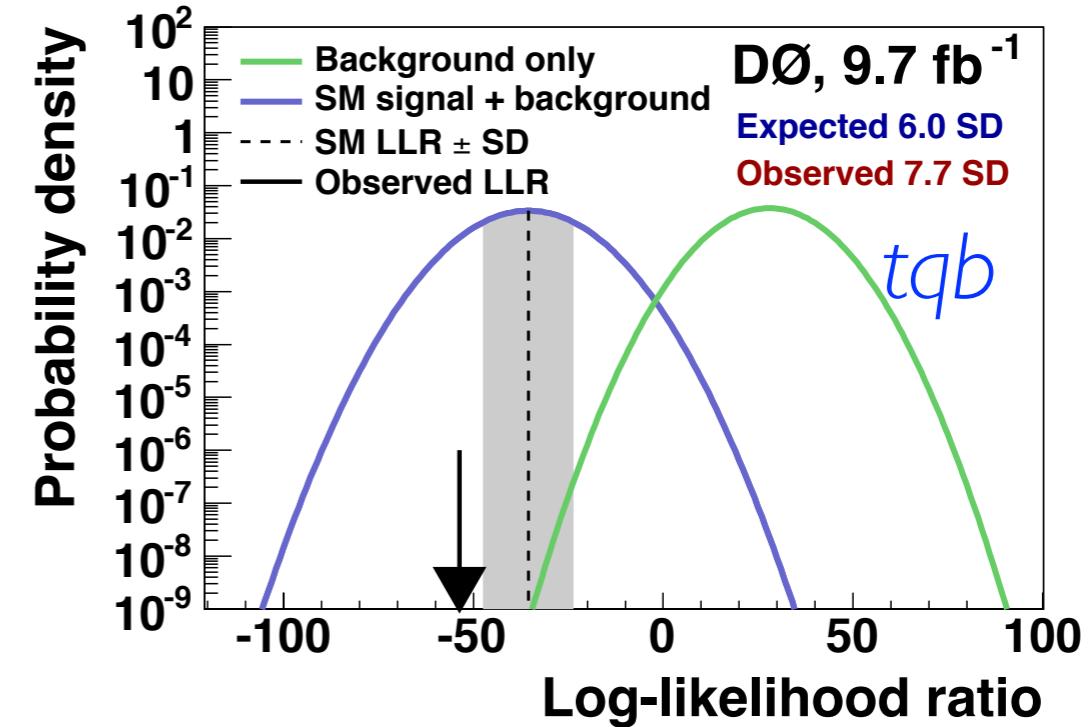
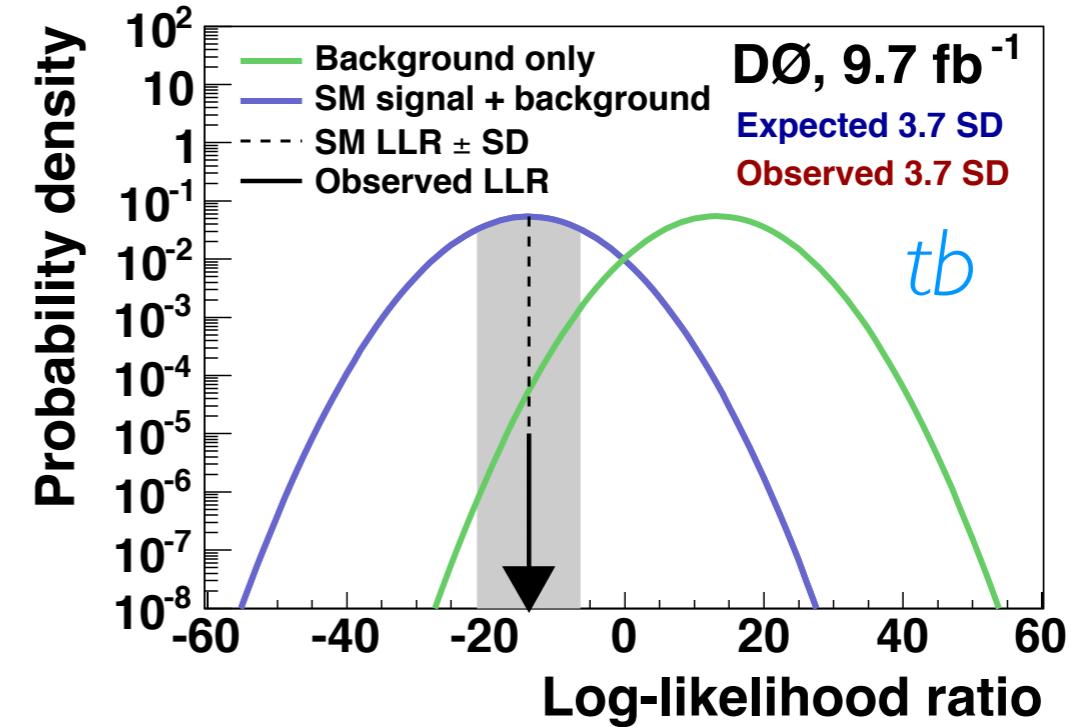


No assumption  
on SM  $\sigma_{tb}/\sigma_{tqb}$ !



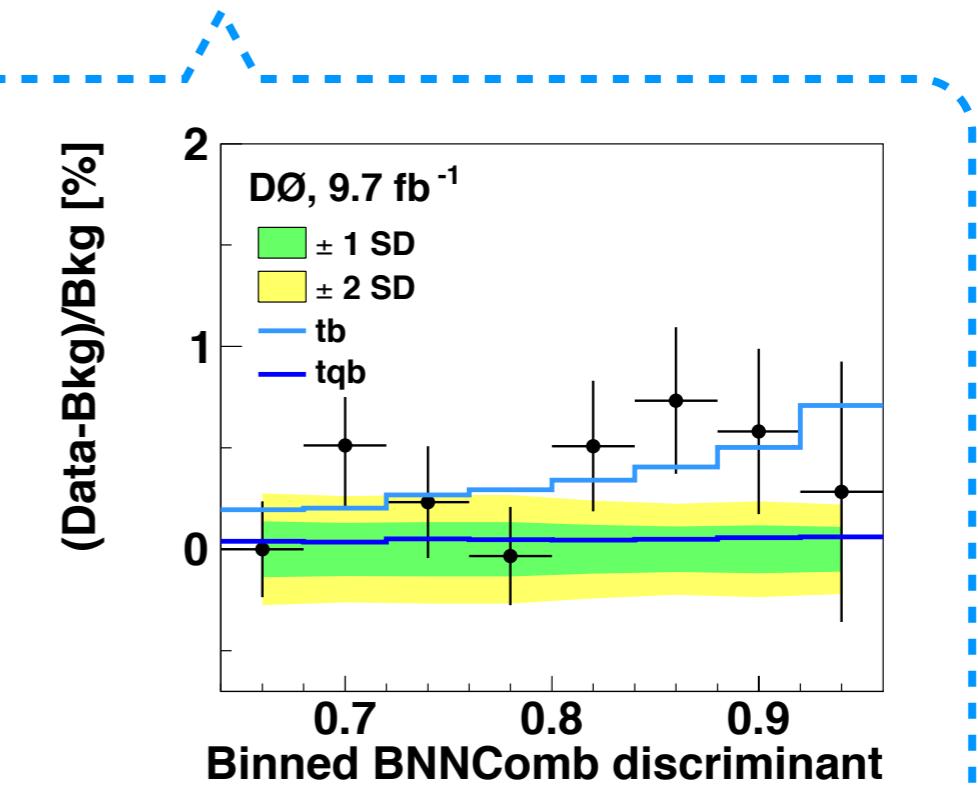
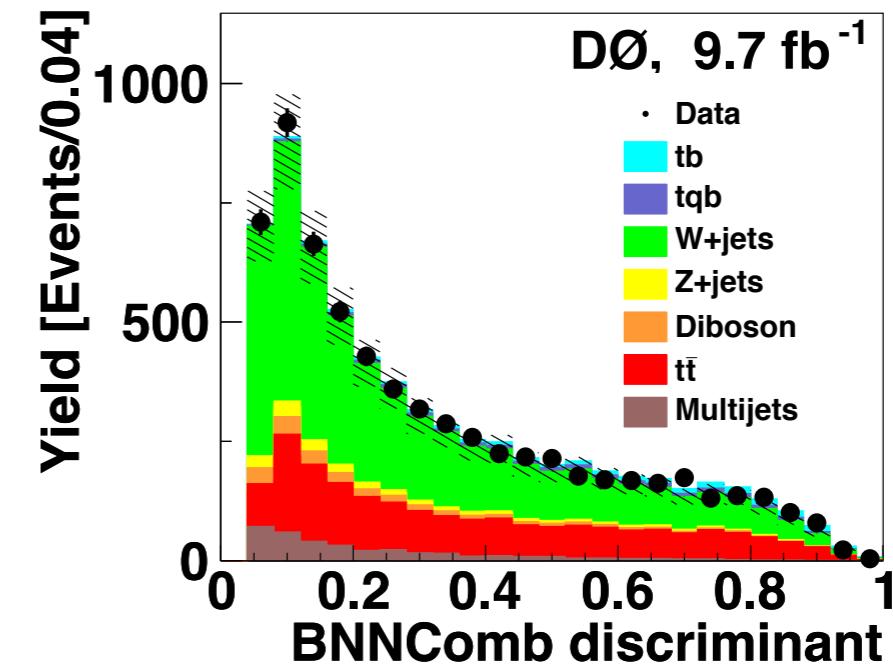
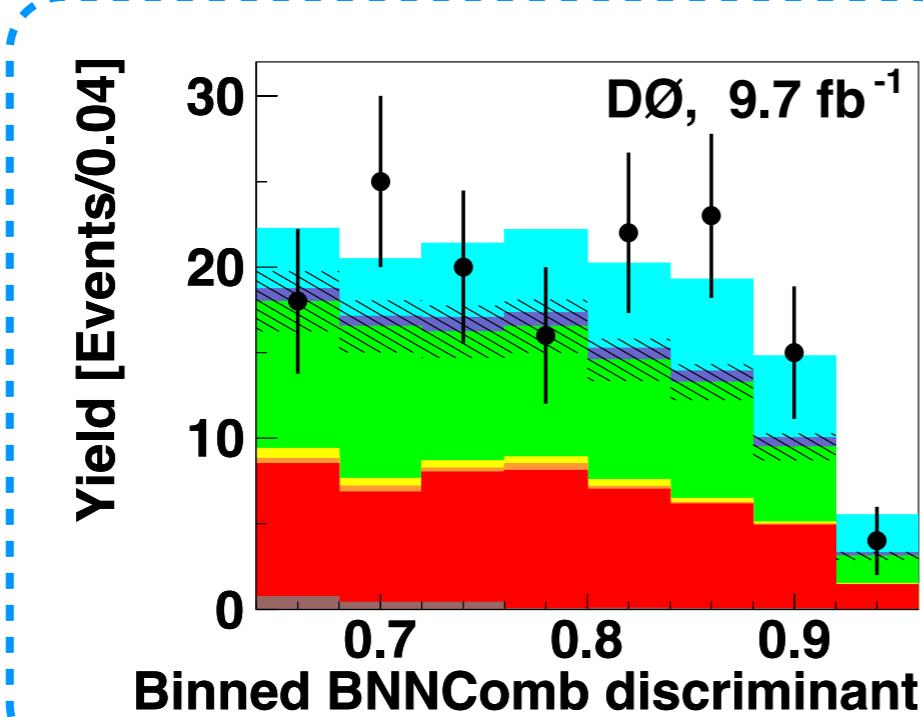
# Significance

- Asymptotic approximation of the log-likelihood ratio
  - tests how likely the data is to fluctuate to the measured  $\sigma$  value, in the absence of the signals
- Expected p-values:
  - $t b$ :  $1.0 \times 10^{-4}$  (3.7 SD)
  - $t q b$ :  $1.0 \times 10^{-9}$  (6.0 SD)
- Observed p-values:
  - $t b$ :  $1.0 \times 10^{-4}$  (3.7 SD)
  - $t q b$ :  $7.1 \times 10^{-15}$  (7.7 SD)



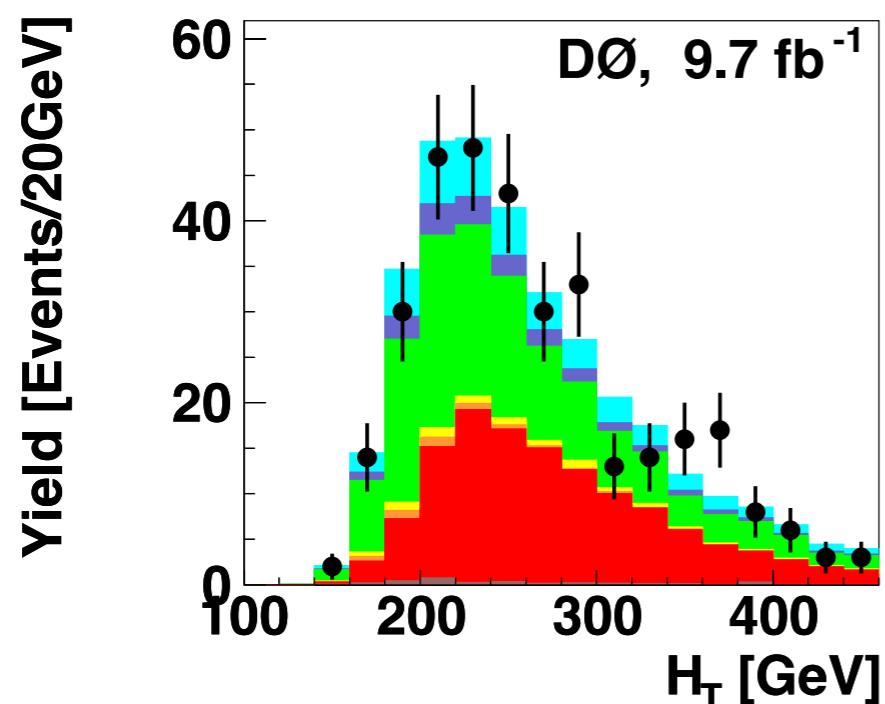
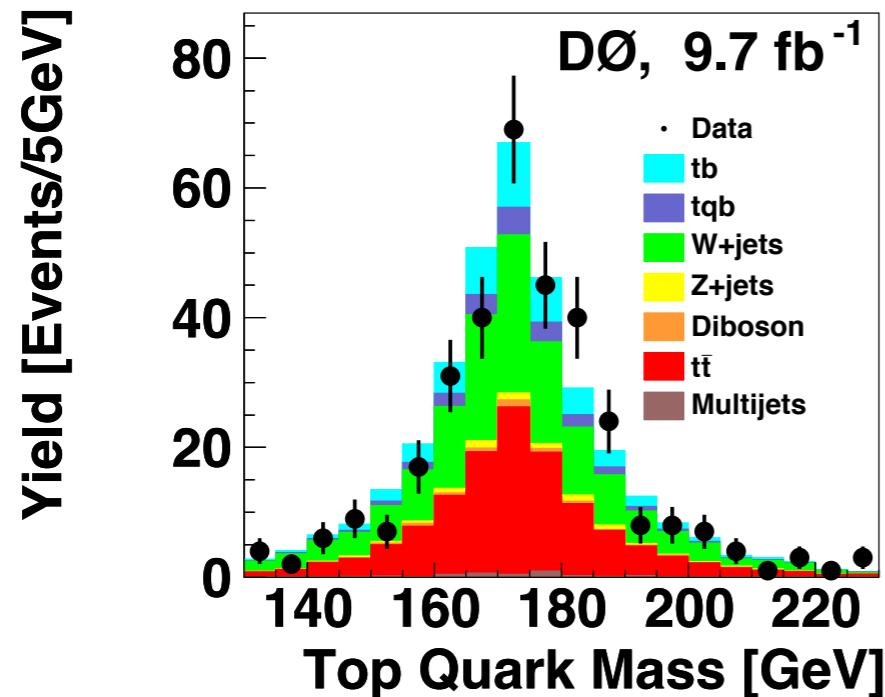
# *tb* or Not *tb*?

- BNNComb discriminant with the post-fit uncertainty
- Examine the most sensitive bins (largest S/B)
- Data favors the “**truth and beauty**”!

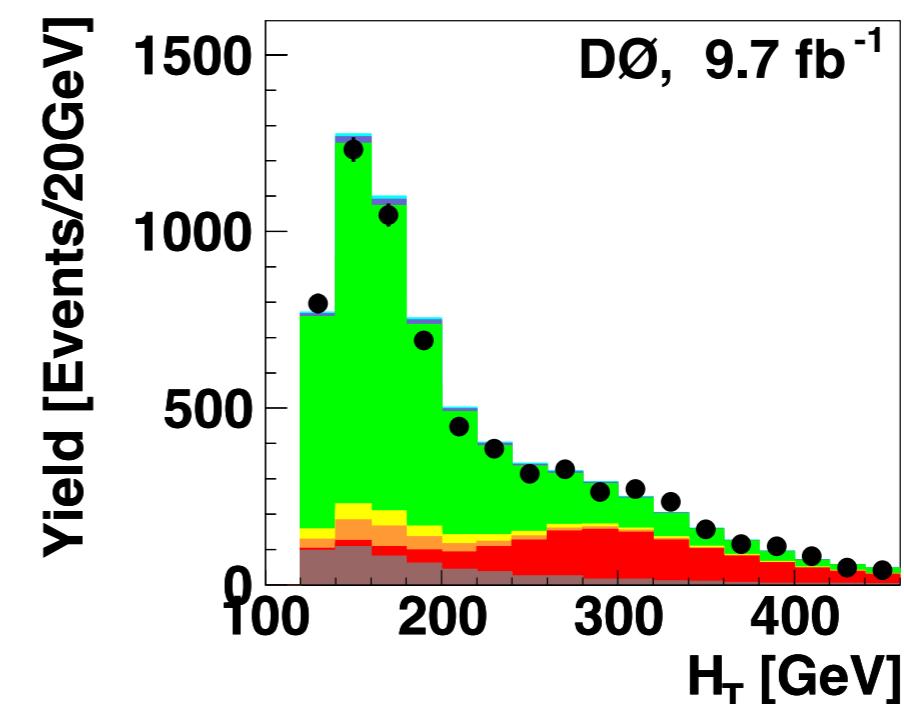
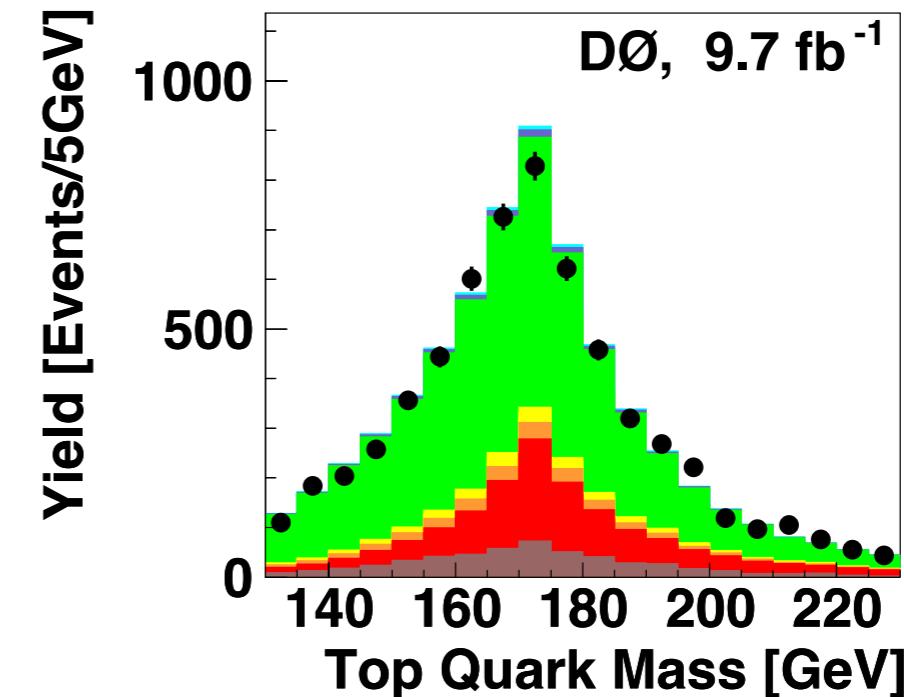


# Event Characteristics

*tb* Category:  $D_{tb} > 0.8$

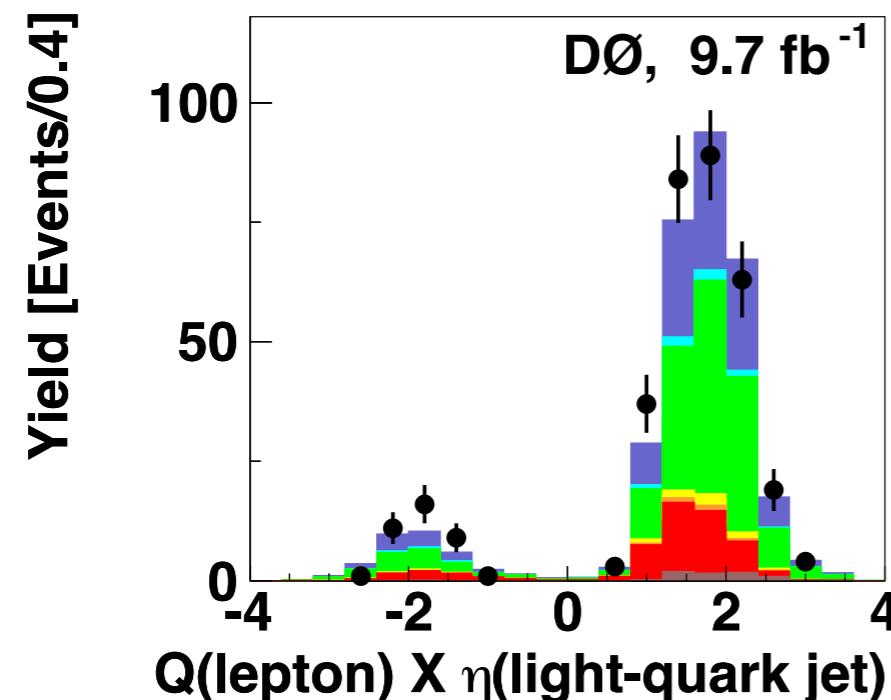
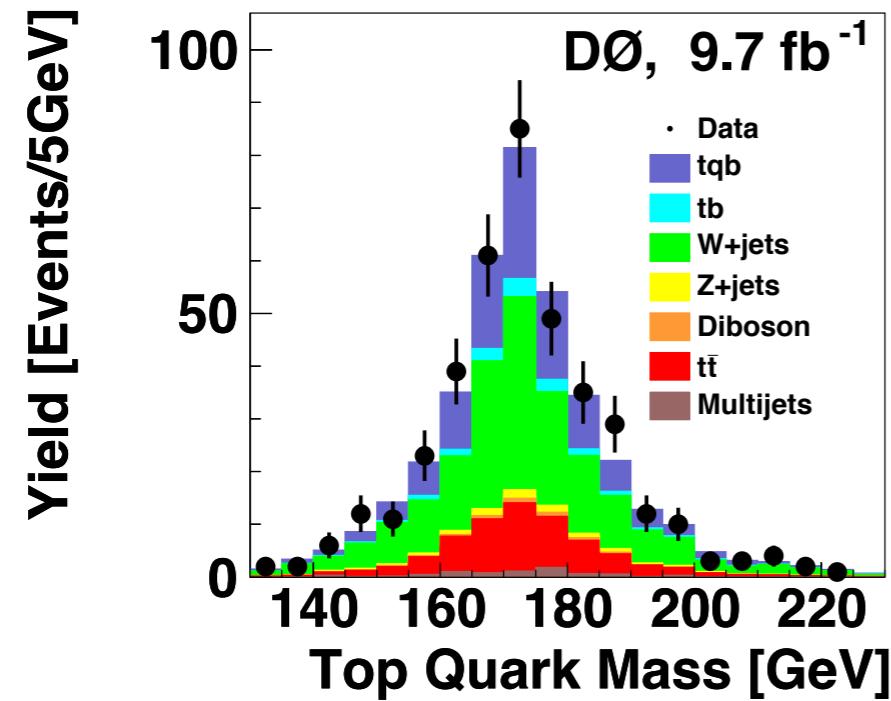


*tb* & *tqb* Depleted Region

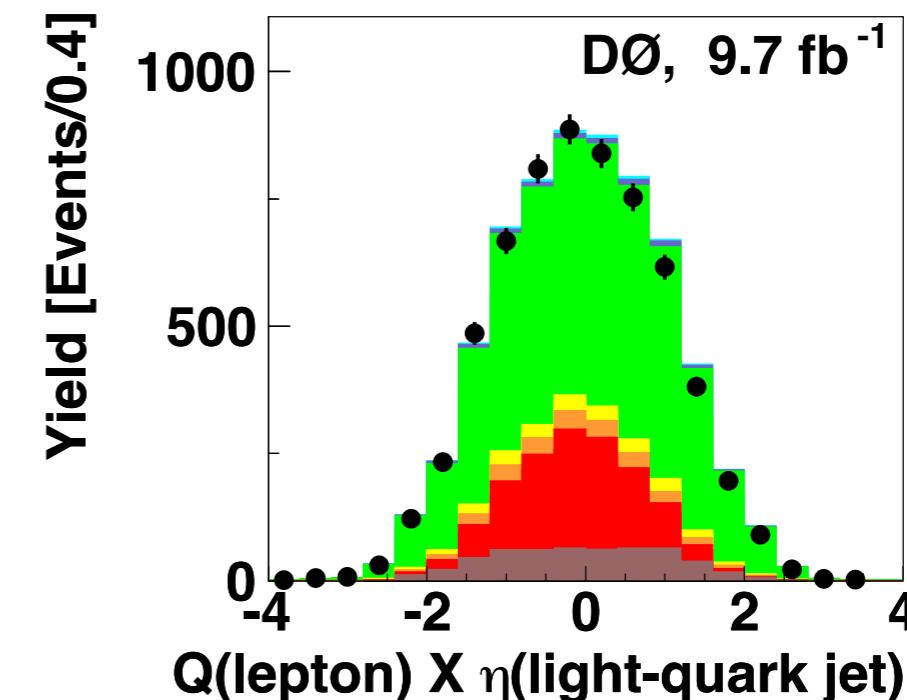
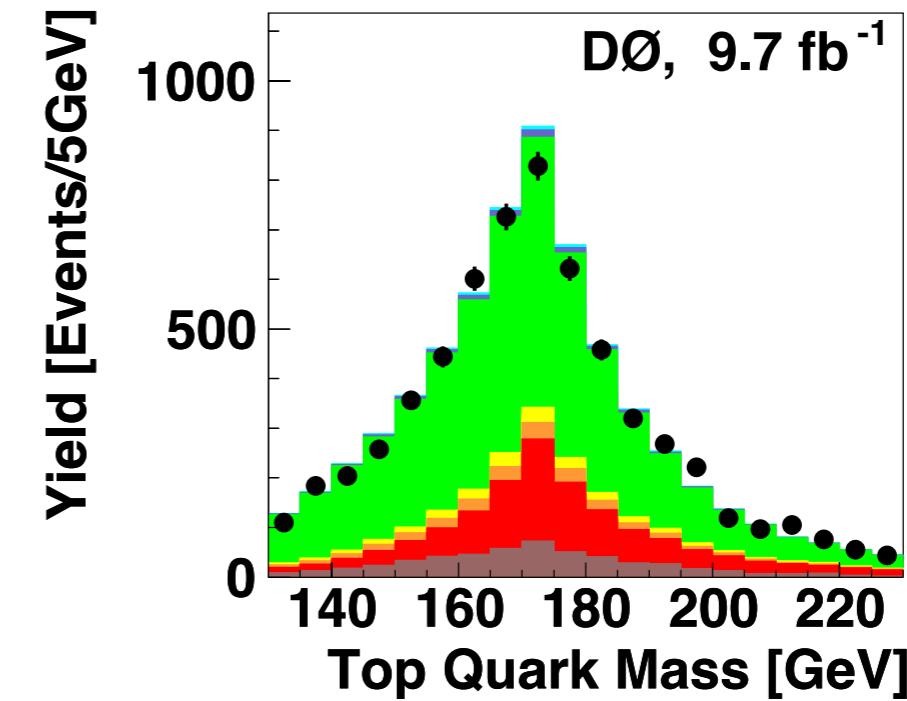


# Event Characteristics

$tqb$  Category:  $D_{tqb} > 0.8$



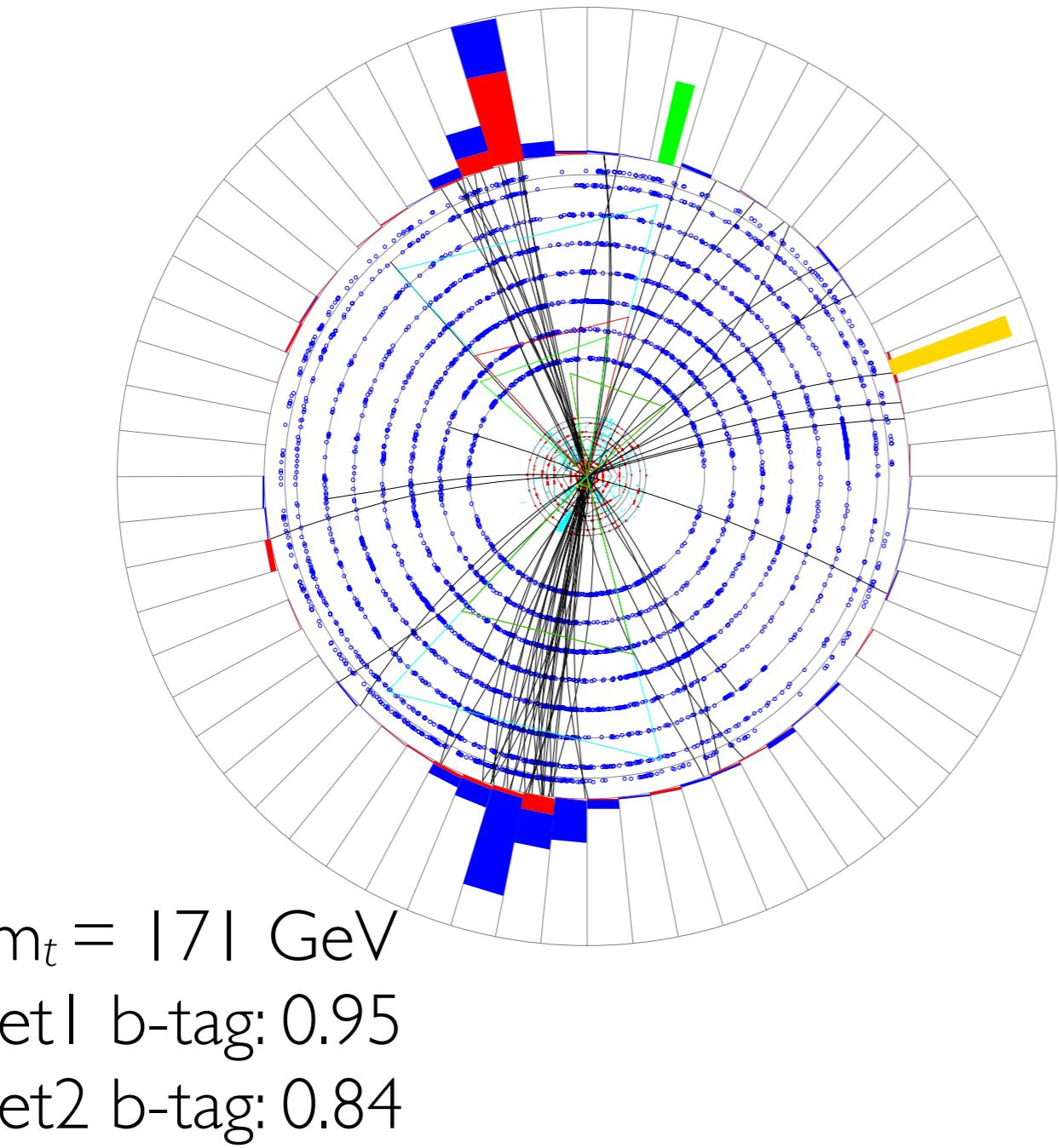
$tb$  &  $tqb$  Depleted Region



# A $t\bar{b}$ Candidate

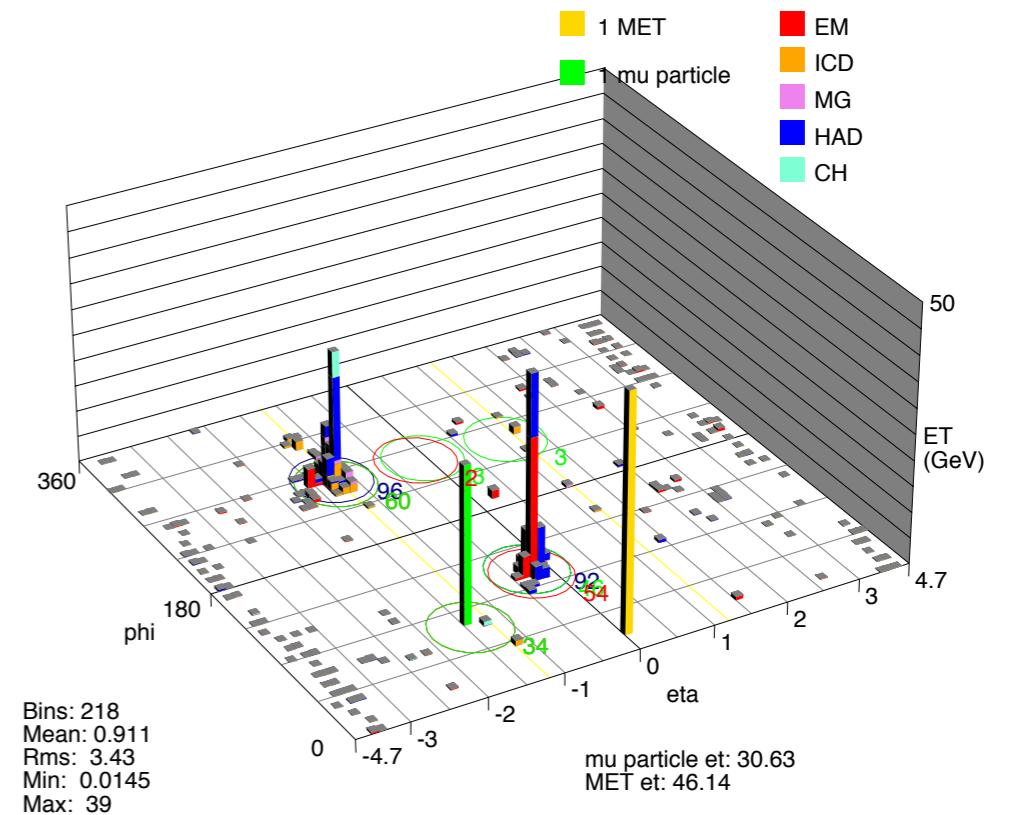
Run 252918 Evt 51093921 Sat Jun 13 23:07:10 2009

ET scale: 54 GeV



Run 252918  
Event 51093921  
Sat. June 13 23:07:10 2009

Run 252918 Evt 51093921 Sat Jun 13 23:07:10 2009



# Single Top in June 2013

$\sigma$ (pb) ~NNLO	$tb$	$tqb$	$tW$
Tevatron Prediction (1.96 TeV)	1.04	2.26	0.3
CDF (7.5 fb <sup>-1</sup> )	$1.81 \pm 0.6$	$1.49 \pm 0.45$	-
DØ (9.7 fb <sup>-1</sup> )	<input type="checkbox"/> 1.10±0.33	<input checked="" type="checkbox"/> 3.07±0.54	-
LHC Prediction (7 TeV)	4.56	65.9	15.6
ATLAS (0.7-2.1 fb <sup>-1</sup> )	< 20.5 (95% C.L.)	<input checked="" type="checkbox"/> 83±20	<input type="checkbox"/> 17±6
CMS (1.2-4.9 fb <sup>-1</sup> )	-	<input checked="" type="checkbox"/> 67±6	<input type="checkbox"/> 16±5

Evidence (3 SD)

Observation (5 SD)

# Single Top Today

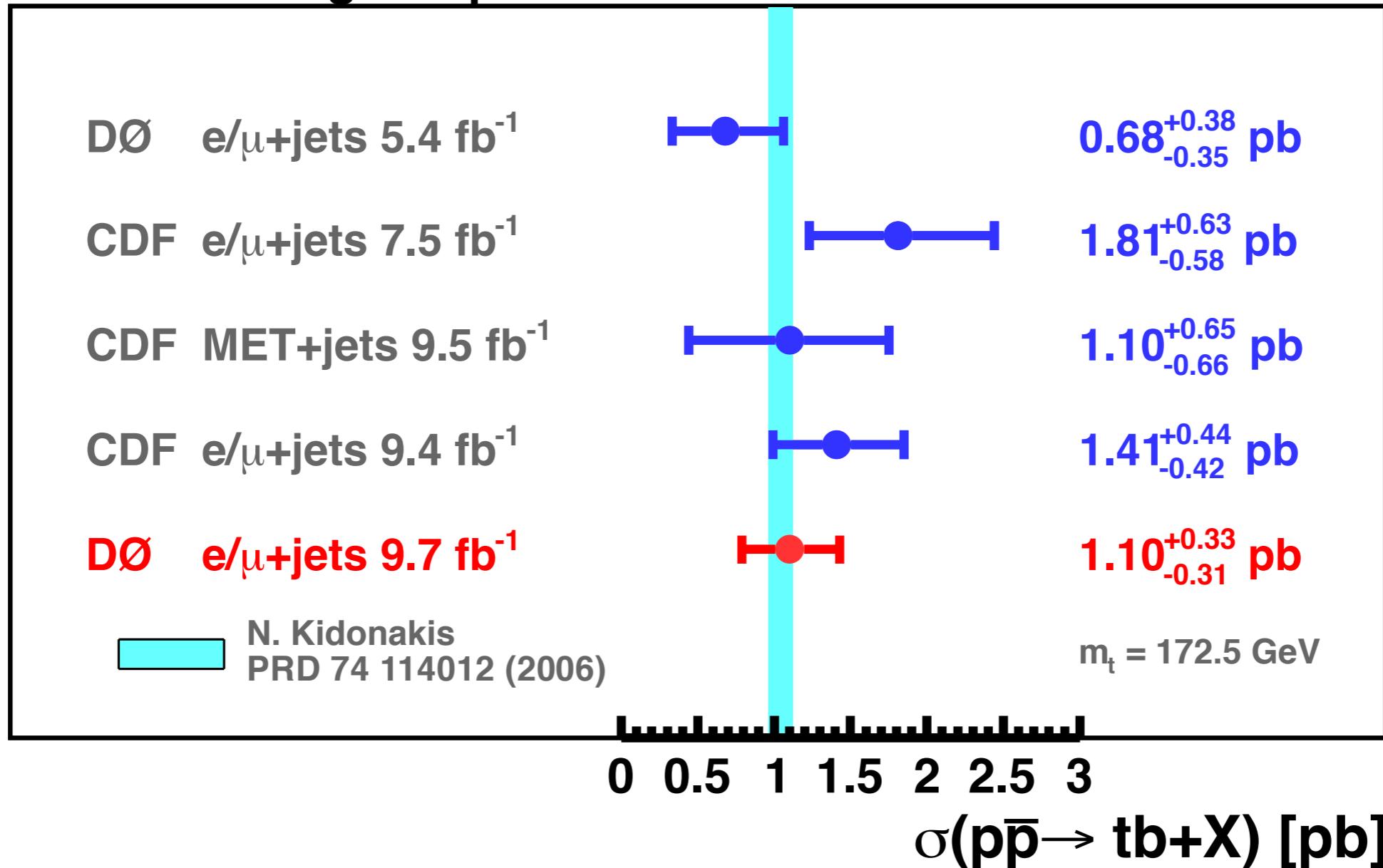
$\sigma$ (pb) ~NNLO	$tb$	$tqb$	$tW$
Tevatron Prediction (1.96 TeV)	1.04	2.26	0.3
CDF (9.4 $\text{fb}^{-1}$ )	<input type="checkbox"/> 1.41 $\pm$ 0.44 prelim.	Not ready	-
DØ (9.7 $\text{fb}^{-1}$ )	<input type="checkbox"/> 1.10 $\pm$ 0.33	<input checked="" type="checkbox"/> 3.07 $\pm$ 0.54	-
LHC Prediction (8 TeV)	5.55	87.2	22.2
ATLAS (0.7-20.3 $\text{fb}^{-1}$ )	< 26.5 (7 TeV)	<input checked="" type="checkbox"/> 95 $\pm$ 18	<input type="checkbox"/> 27 $\pm$ 5.8
CMS (1.2-12.2 $\text{fb}^{-1}$ )	-	<input checked="" type="checkbox"/> 80 $\pm$ 13	<input checked="" type="checkbox"/> 23 $\pm$ 5.5

Evidence (3 SD)

Observation (5 SD)

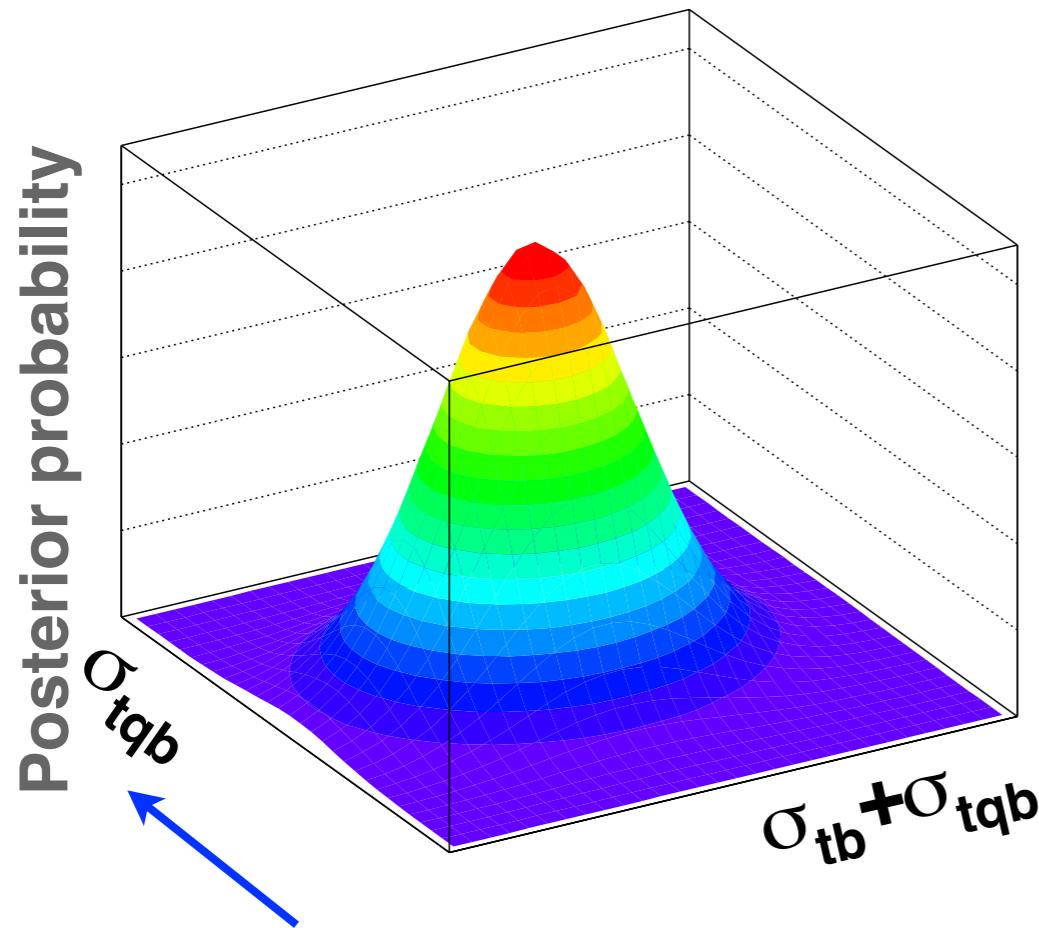
# $\sigma_{tb}$ Measurement History

## s-channel Single Top Quark Cross Section



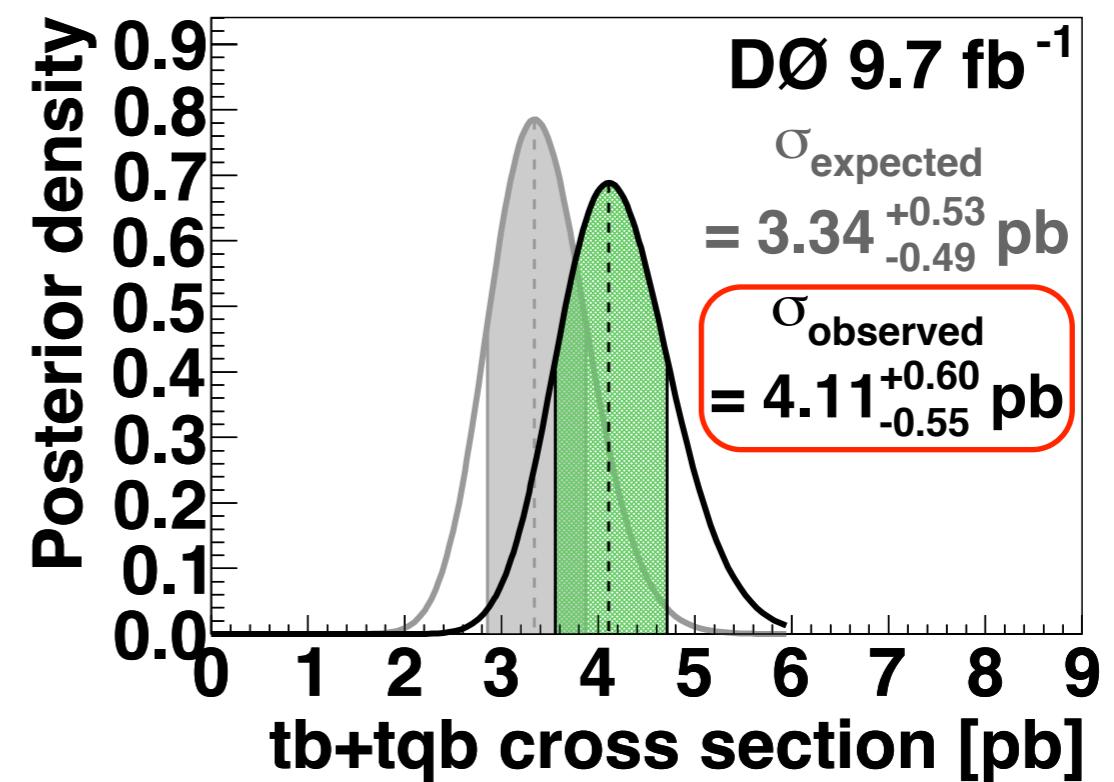
Each single method in the DØ  $9.7 \text{ fb}^{-1}$  analysis measures  $\sigma_{tb}$  with  $> 3 \text{ SD}$

# Measured $\sigma_{tb+tqb}$



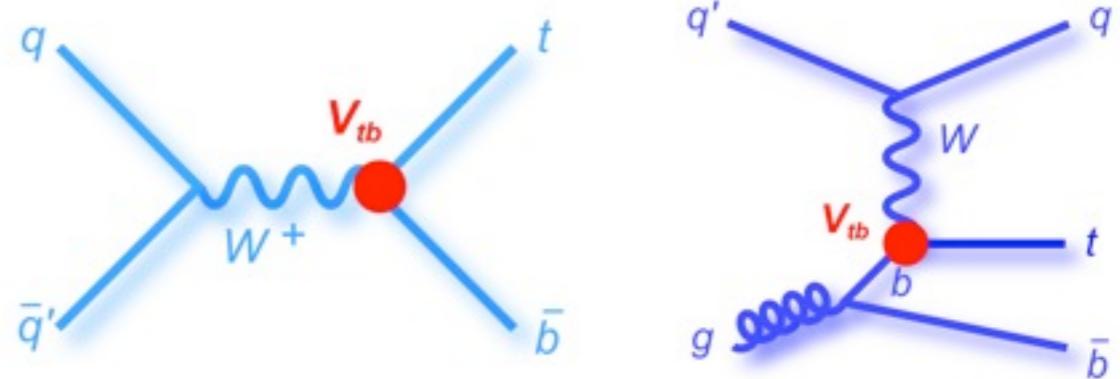
Integrate over  $\sigma_{tqb}$  and obtain a 1D posterior p.d.f. of  $\sigma_{tb+tqb}$

- Measure  $\sigma_{tb+tqb}$  without assuming the SM  $\sigma_{tb}/\sigma_{tqb}$
- Use 2D posterior p.d.f.



# CKM Matrix Element $|V_{tb}|$

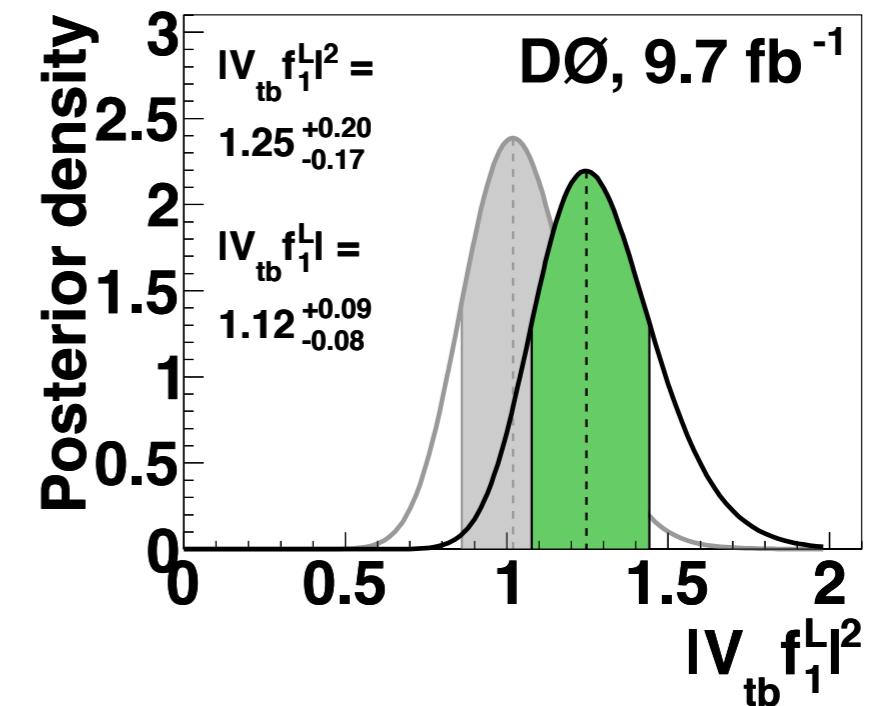
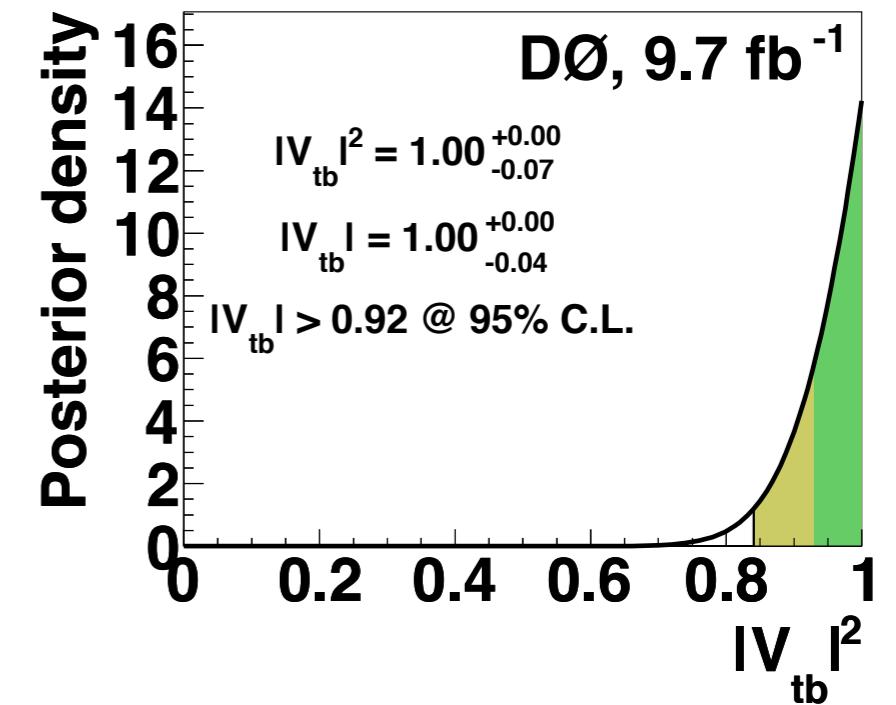
$$V_{CKM} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$



- $\sigma_{tqb}$  proportional to  $|V_{tb}|^2$
- Lagrangian:  $\mathcal{L} = -\frac{g}{\sqrt{2}} V_{tb} \bar{b} \gamma^\mu (f_1^L P_L) t W_\mu^-$       SM:  $f_1^L = 1$
- Assume:
  - SM top decay:  $|V_{td}|^2 + |V_{ts}|^2 \ll |V_{tb}|^2$
  - Pure V-A interaction
  - CP conservation
- DO NOT assume
  - 3 generations
  - unitarity of the CKM matrix; allow  $|V_{tb} f_1^L|^2 > 1$
  - $\sigma_{tb}/\sigma_{tqb}$  (NEW)

# CKM Matrix Element $|V_{tb}|$

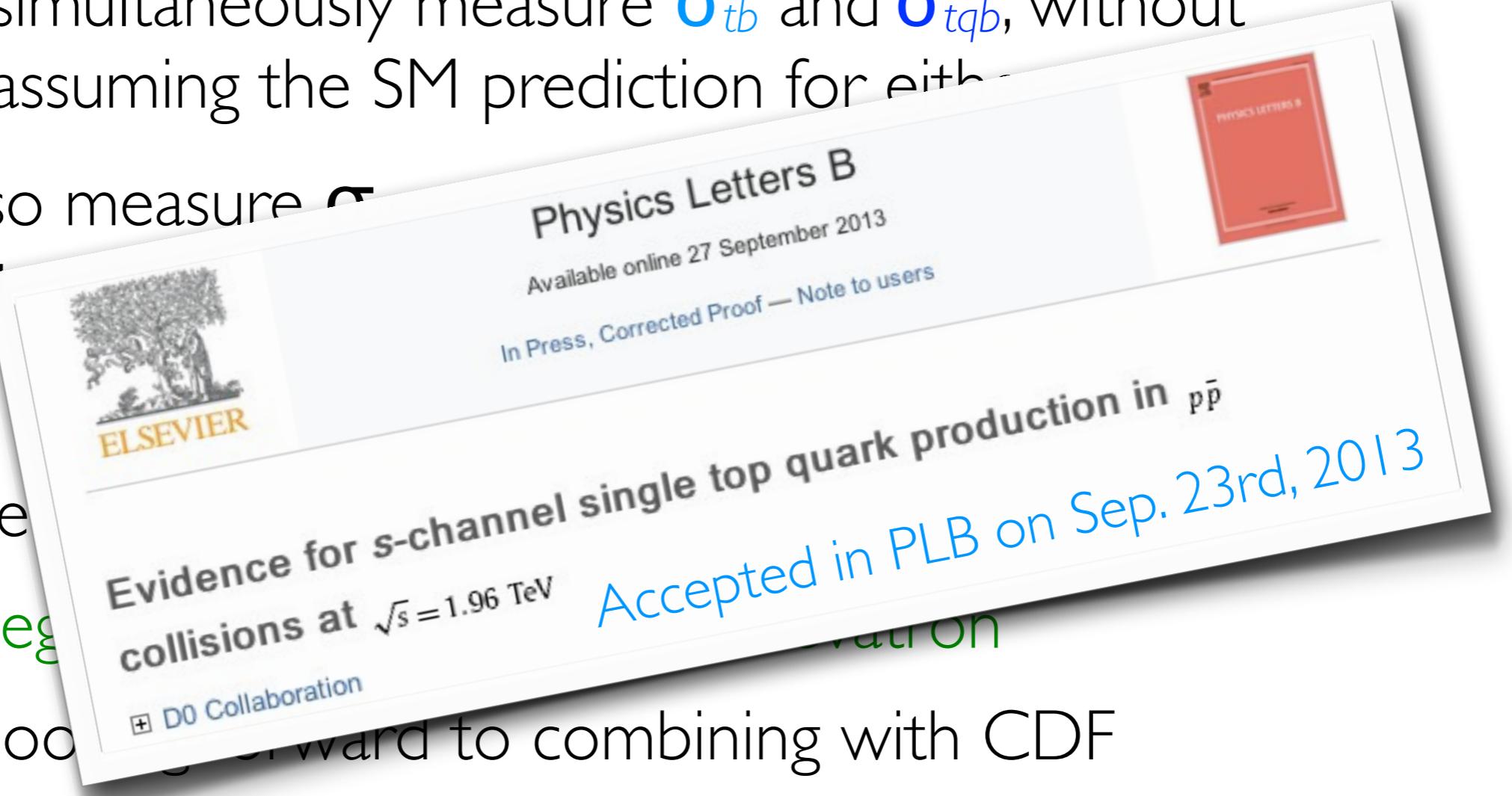
- Assume  $0 \leq |V_{tb}|^2 \leq 1$ 
  - $|V_{tb}| > 0.92 @ 95\% \text{ C.L.}$
- Allow  $|V_{tb} f_1^L|^2 > 1$ 
  - $|V_{tb} f_1^L| = 1.12^{+0.09}_{-0.08}$
- Additional systematic uncertainties
  - theoretical uncertainty on single top cross sections
- Complementary to  $R_{Wb/Wq}$  measurement in top decays  
PRD 85, 091104 (2012)

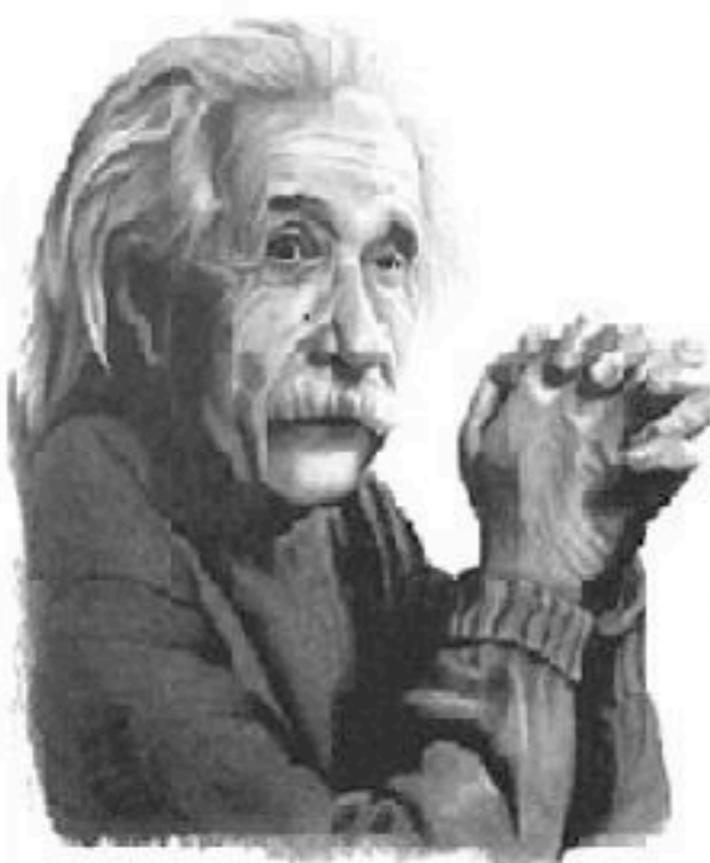


# Conclusion

- First evidence of s-channel single top quark production
  - $\sigma_{tb} = 1.10 \pm 0.33 \text{ pb}$
  - simultaneously measure  $\sigma_{tb}$  and  $\sigma_{tqb}$ , without assuming the SM prediction for either
- Also measure  $\sigma_{tb+tqb}$  and  $|V_{tb}|$  without assuming the SM ratio of  $\sigma_{tb}/\sigma_{tqb}$ 
  - $|V_{tb}| > 0.92 @ 95\% \text{ C.L.}$
- The results are consistent with the SM predictions
- A legacy measurement at the Tevatron
  - looking forward to combining with CDF

# Conclusion

- First evidence of s-channel single top quark production
    - $\sigma_{tb} = 1.10 \pm 0.33 \text{ pb}$
    - simultaneously measure  $\sigma_{tb}$  and  $\sigma_{tqb}$ , without assuming the SM prediction for either
  - Also measure  $\sigma_{tqb}$  without assuming the SM prediction
  - In addition to the SM, also measure the anomalous couplings
  - The first evidence for s-channel single top quark production
  - A legend for the SM and beyond SM contributions to the evaluation
  - looking forward to combining with CDF
- 



quotespedia.info

The pursuit of truth and  
beauty is a sphere of  
activity in which we are  
permitted to remain children  
all our lives.

Albert Einstein

Thank you for your attention!

# Backup Slides

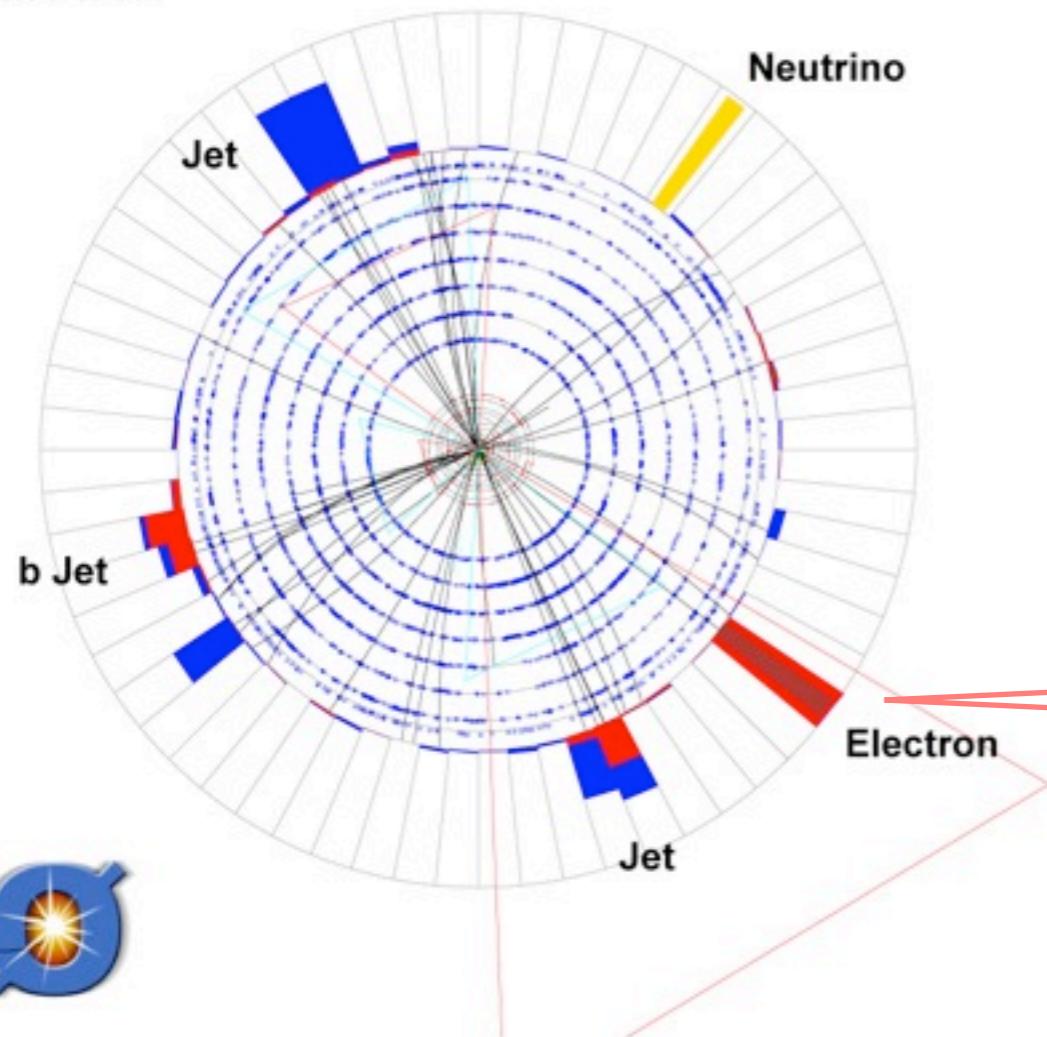
# Electron Reconstruction

Transverse plane: Perpendicular  
to the proton beam

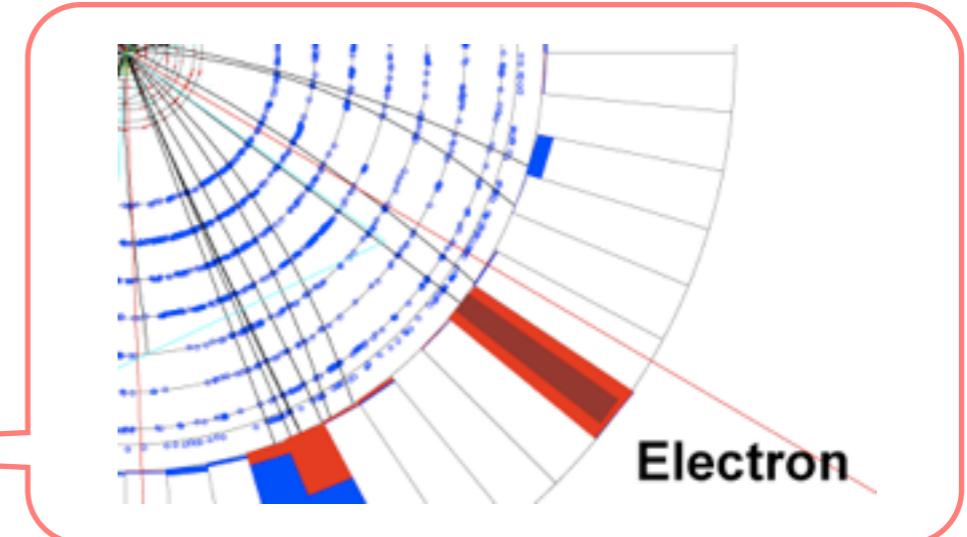
## DØ Experiment Event Display Single Top Quark Candidate Event, $2.3 \text{ fb}^{-1}$ Analysis

Run 229388 Evt 13339887 Wed Jan 3 21:05:14 2007

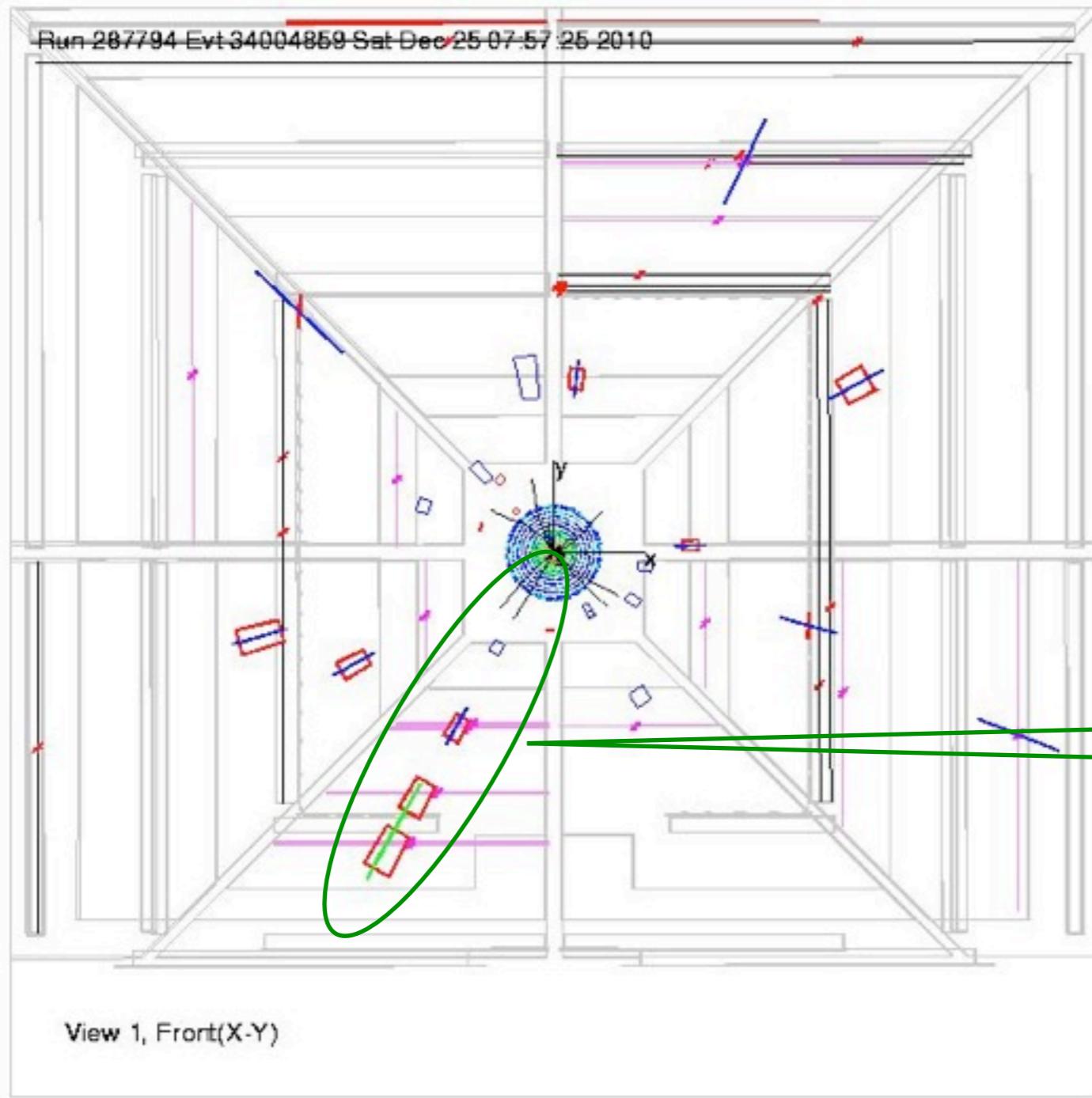
ET scale: 39 GeV



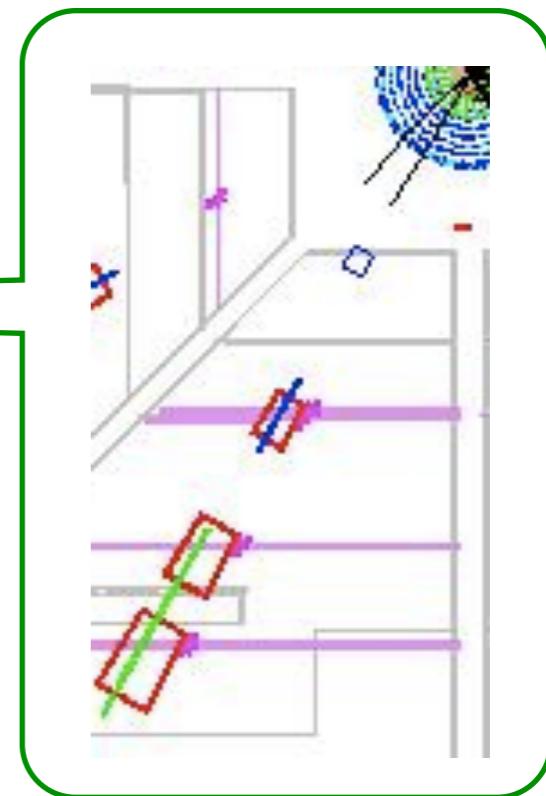
- Electron: Narrow cone of isolated EM calorimeter cluster



# Muon Reconstruction



- Muon: Identified in the muon spectrometer and a matched track in the central tracker



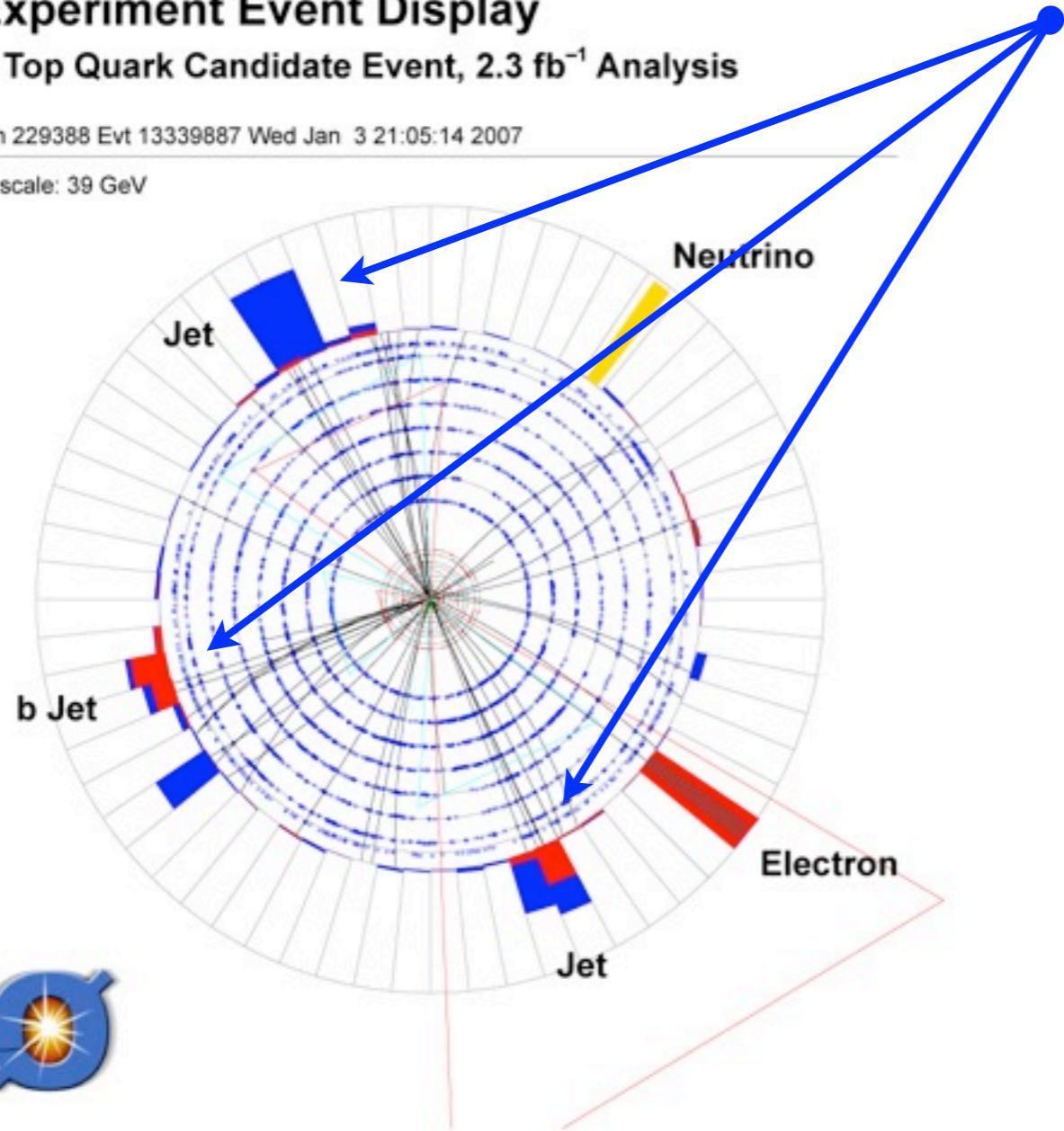
# Jet Reconstruction

Transverse plane: Perpendicular  
to the proton beam

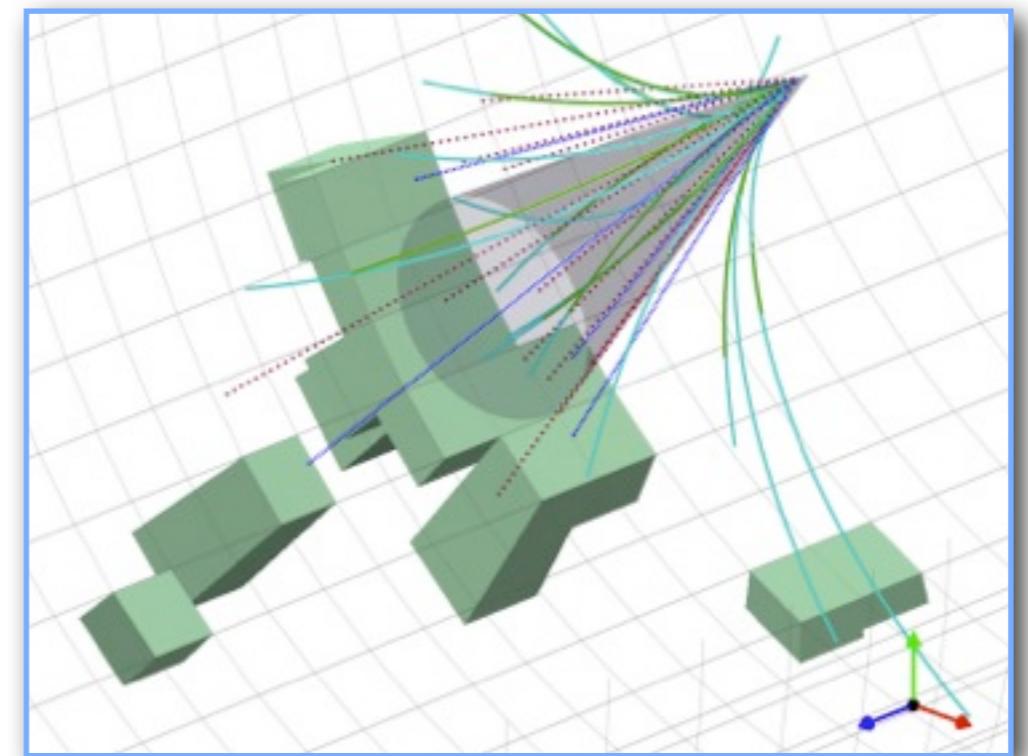
**DØ Experiment Event Display**  
Single Top Quark Candidate Event,  $2.3 \text{ fb}^{-1}$  Analysis

Run 229388 Evt 13339887 Wed Jan 3 21:05:14 2007

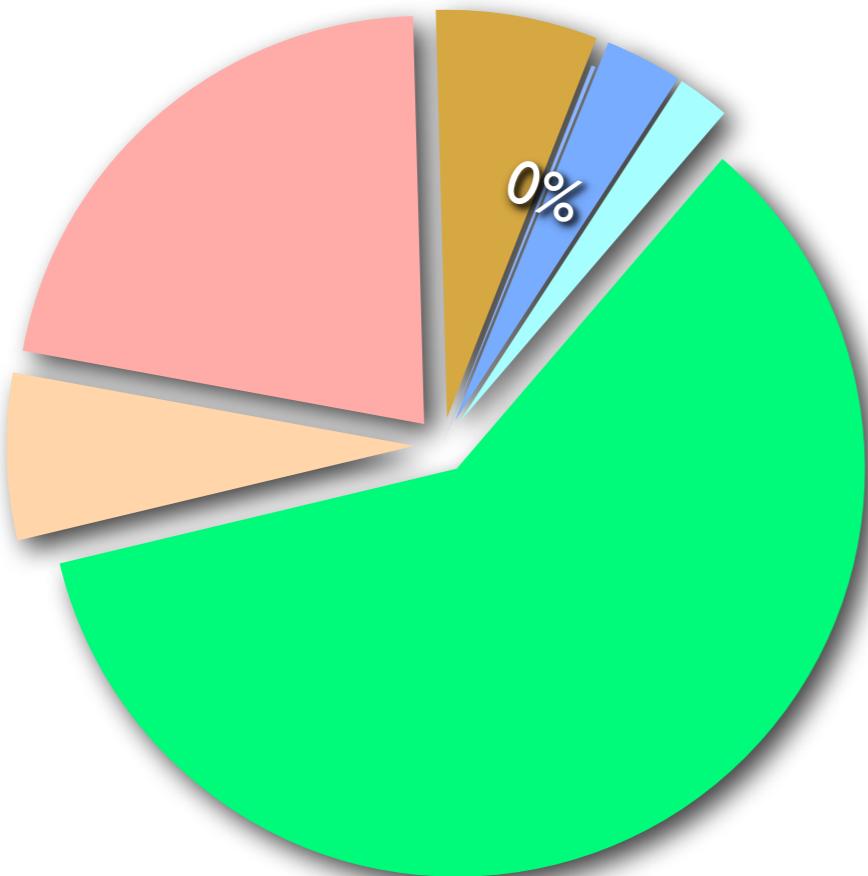
ET scale: 39 GeV



- Quark and gluon fragments → jet: Wide cone of hadron calorimeter energy clusters



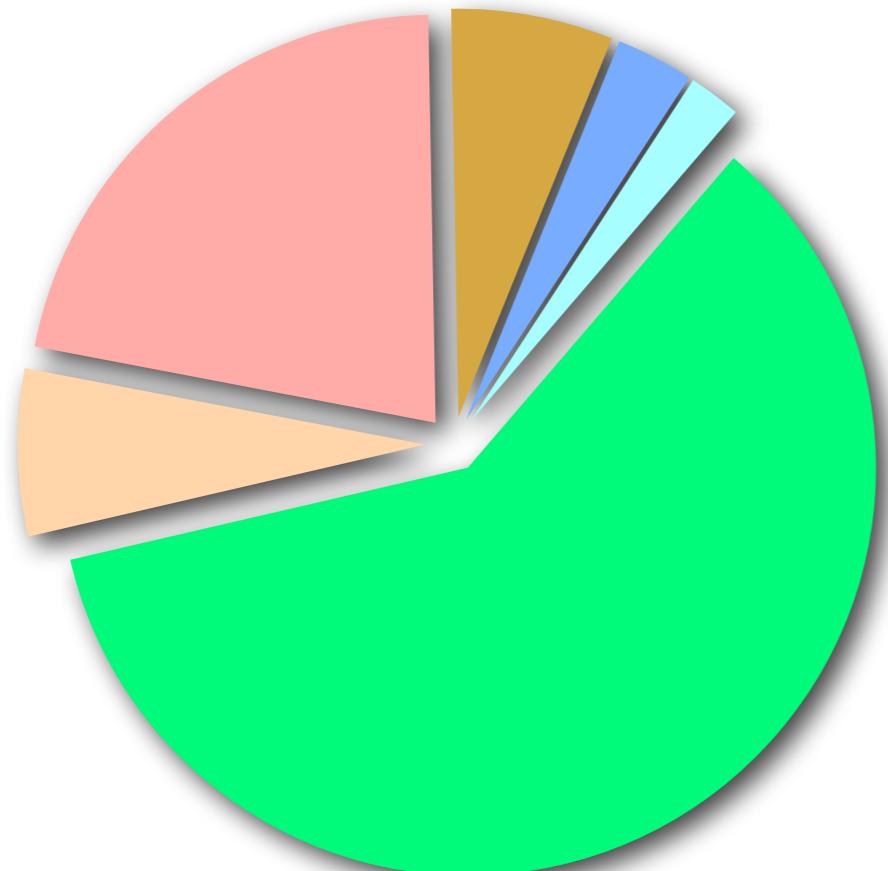
# $tW$ Contribution at DØ



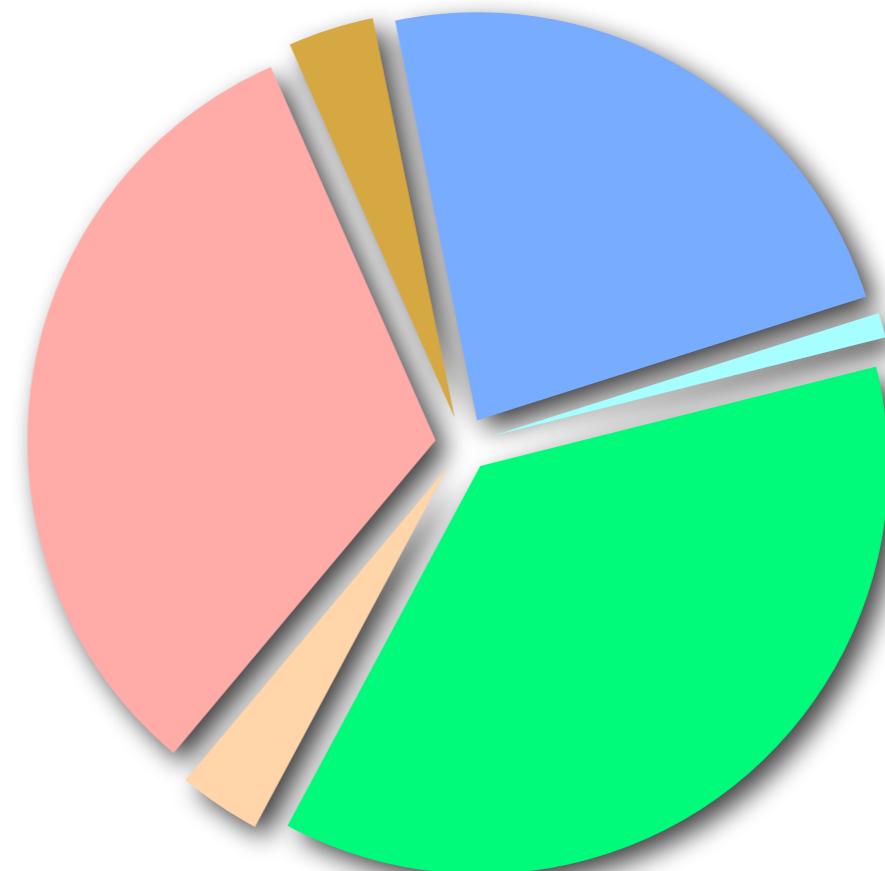
e, $\mu$ 2, 3-jets 1, 2 $b$ -tags combined	
$s$ -channel	257
$t$ -channel	378
$tW$	20
$W+\text{jets}$	7394
diboson, $Z+\text{jets}$	815
top pair	2672
multijet	789
Total background	11669
Data	12103

# Background Contribution

DØ



CMS  
(arXiv:1209.4533v1)



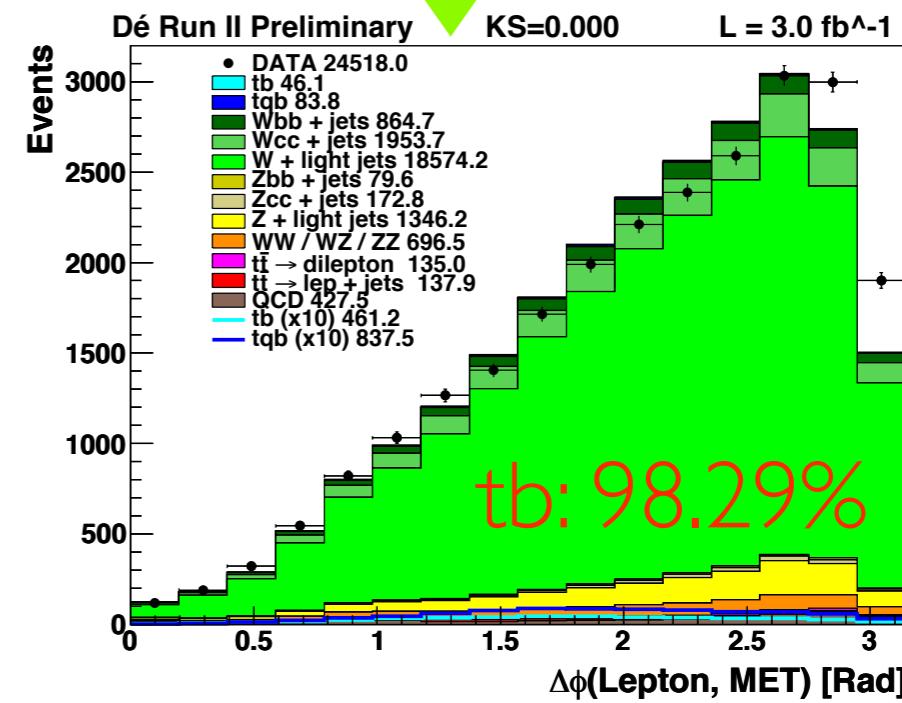
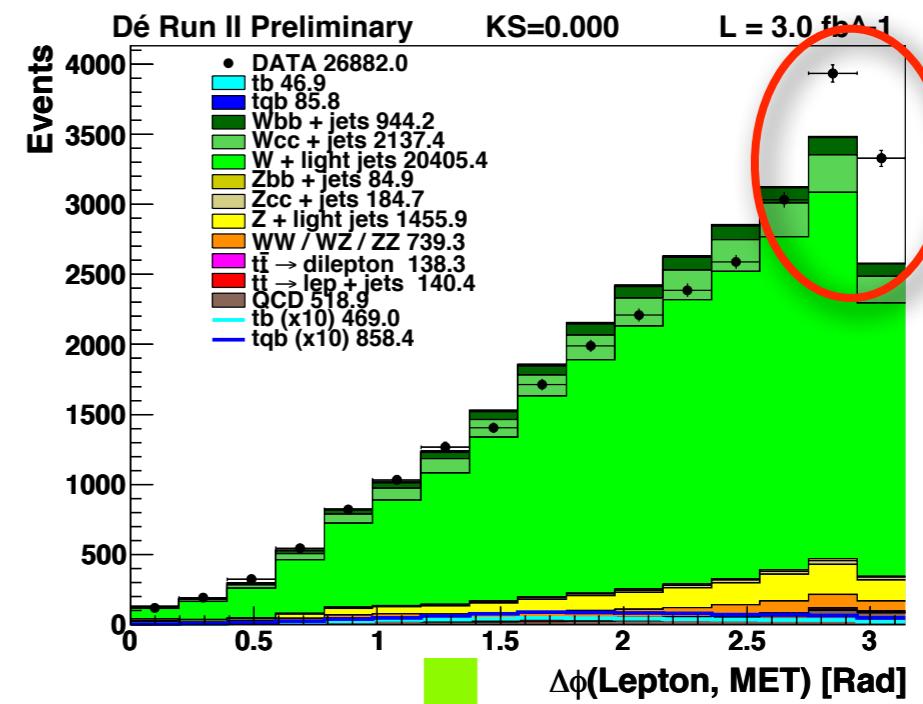
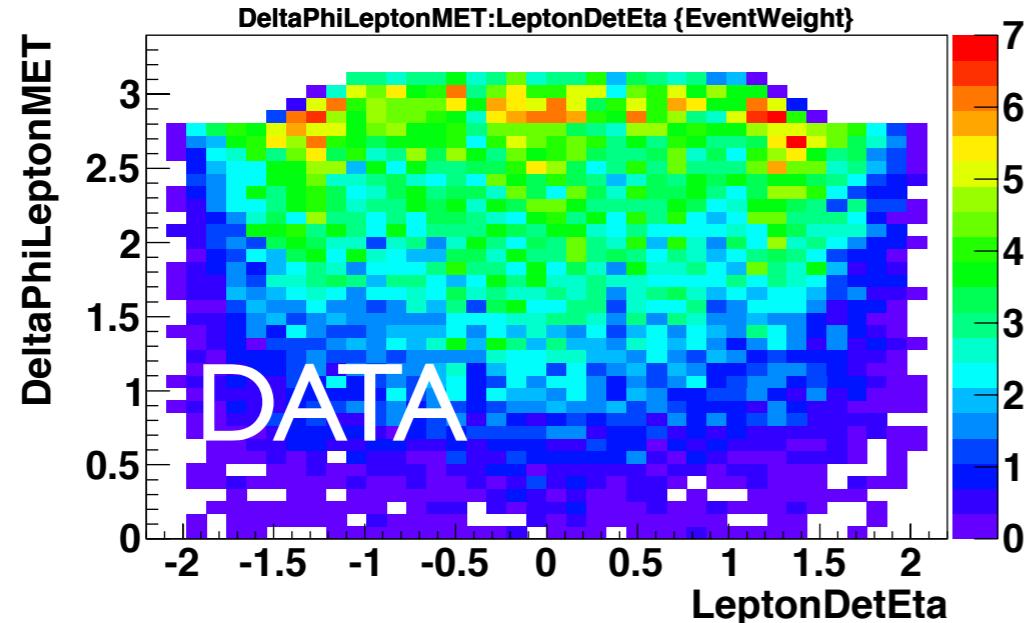
s-channel t-channel W+jets Z+jet, dibosons tt+jet Multijets

# Additional Cuts

- $H_T > 120/140/160 \text{ GeV}$  (2/3/4 jet)
- $\text{MET} > 25 \text{ GeV}$  (3 and 4 jet)
- $\Delta\varphi(\text{MET}, \text{Jet1}) < 1.5 + 0.0469\text{MET}$
- Electron channel
  - $\Delta\varphi(\text{MET}, \text{Lep}) > 2.0 - 0.05\text{MET}$
  - $\Delta\varphi(\text{MET}, \text{Lep}) > 1.5 - 0.03\text{MET}$
  - $\Delta\varphi(\text{MET}, \text{Lep}) < 2.0 + 0.0476\text{MET}$
- Muon channel
  - $\Delta\varphi(\text{MET}, \text{Lep}) > 1.4 - 0.0141\text{MET}$
  - $\Delta\varphi(\text{MET}, \text{Lep}) < 2.5 + 0.0214\text{MET}$
  - $-ab/(\pi-a) + b \Delta\varphi(\text{MET}, \text{Lep})/(\pi-a) < |\mu_{trkcursig}|$   
 $(a, b) = (2.9, 10)$  (modified)
- Trapezoid cut (new)

# $\Delta\varphi(\text{Muon, MET})$ Issue

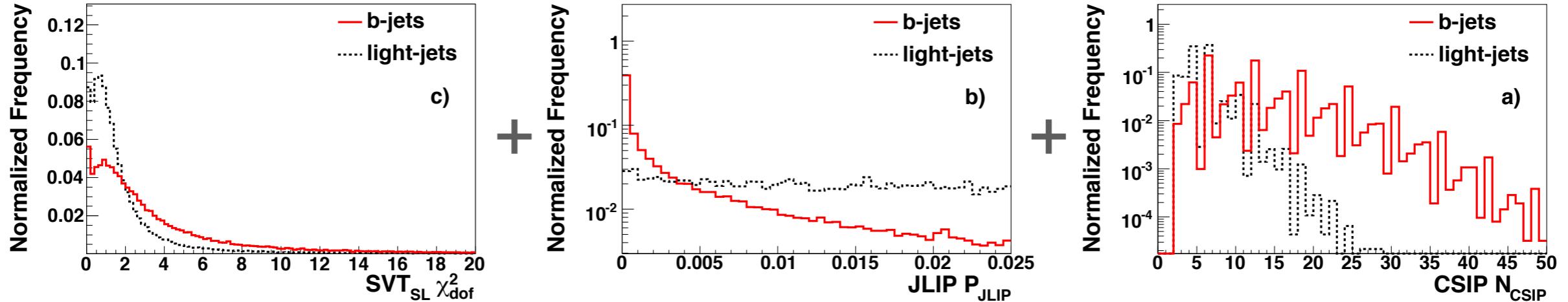
- Data-MC disagreement in the last bin of  $\Delta\varphi(\text{Muon, MET})$  for mu+jets channel
- Re-derive muon TrackCurvSig cut
- Derive a “trapezoid” cut, and apply it after LeptonDetEta reweighting



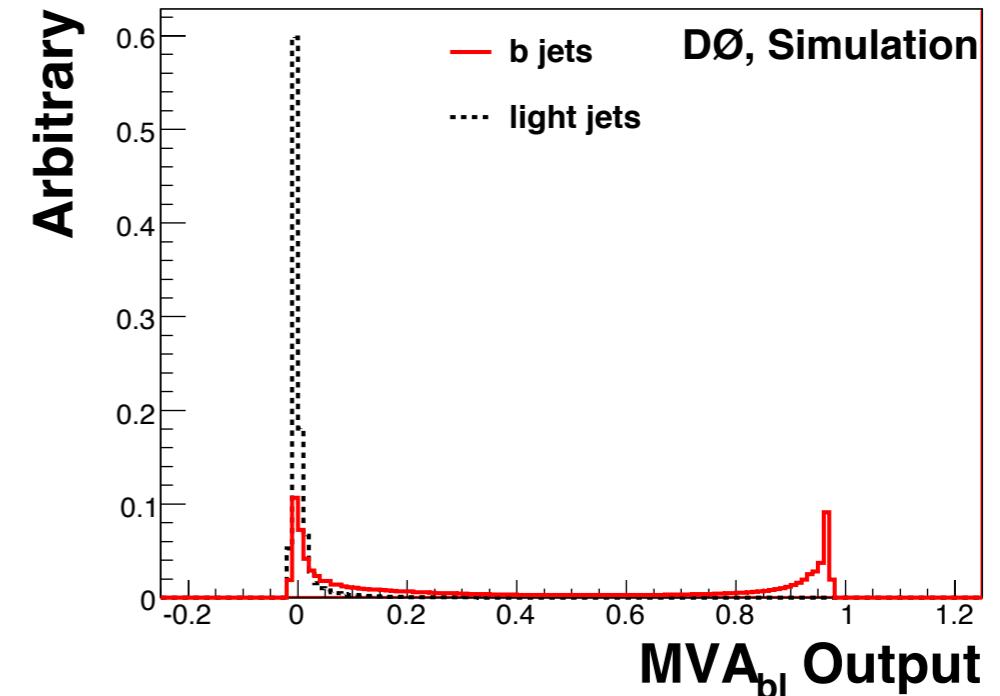
# Reweighting

- The same reweightings as used in previous single top analysis
- $e+jets$ :
  - InstLumi, Angular corrections
- $\mu+jets$ :
  - InstLumi, Lepton Detector  $\eta$ , Angular corrections
  - InstLumi and Lepton Detector  $\eta$  reweightings
    - bin by bin, applied on all MCs
  - Angular corrections
    - $Jet1\eta, Jet2\eta, \Delta R(Jet1, Jet2), Jet3\eta, Jet4\eta$
    - Originally from Higgs group, with our ICD methods

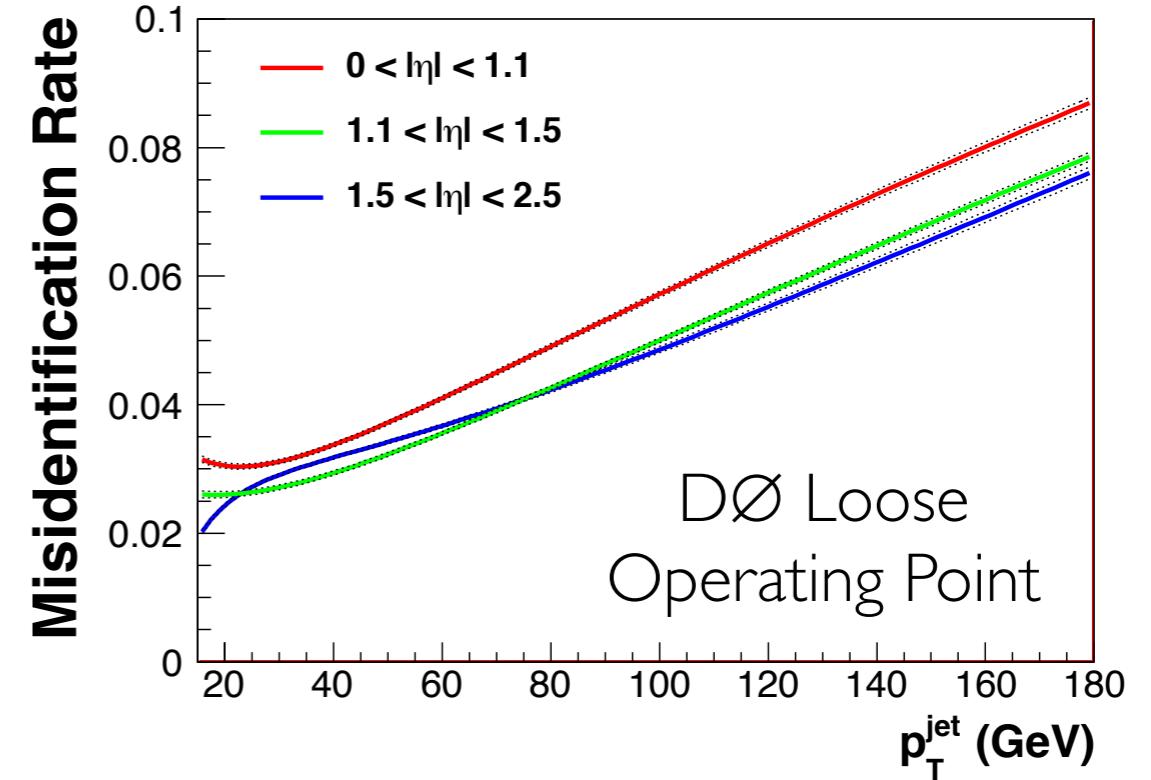
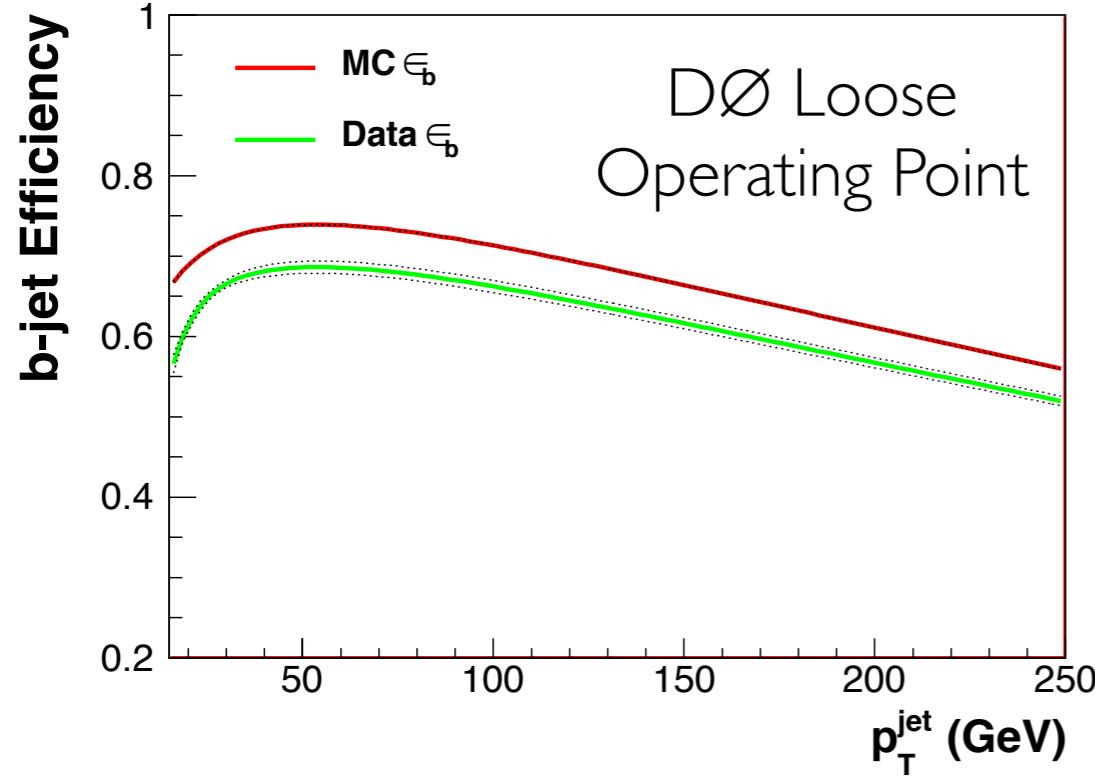
# $b$ -Jet Identification



- Use the multivariate technique (MVA) to combine these variables
- Optimize the cut on (the MVA output) to this analysis



# $b$ -ID Efficiency



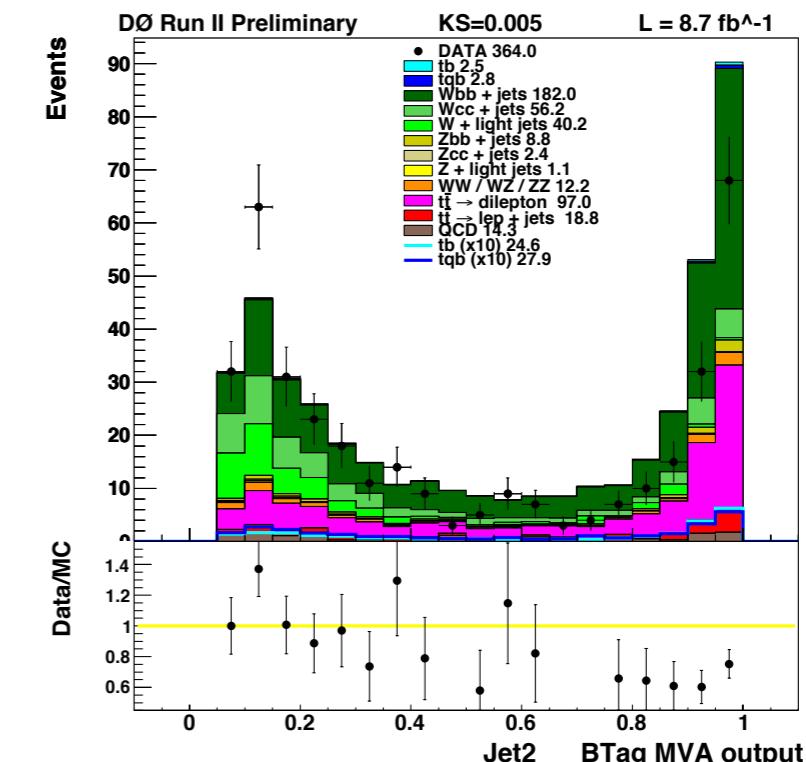
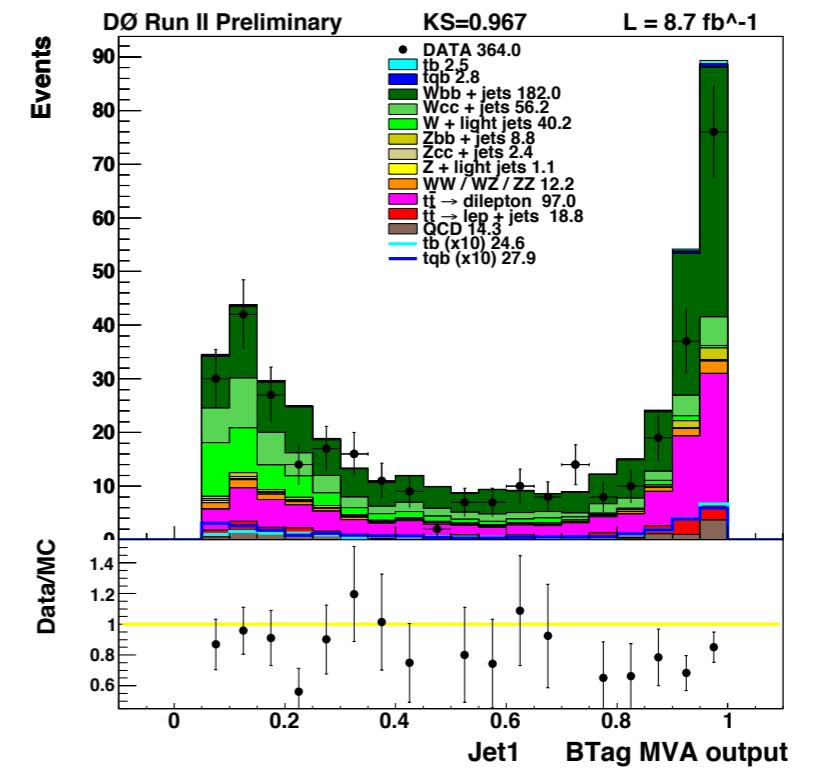
- $b$ -identification efficiency: (50-70)%
- Misidentification rate: (3-8)%
- Obtain scale factors to correct the MC samples

# W Transverse Mass

$$M_T^2(W) = [\cancel{E}_T + p_T(\ell)]^2 - [\cancel{E}_{T_x} + p_x(\ell)]^2 - [\cancel{E}_{T_y} + p_y(\ell)]^2$$

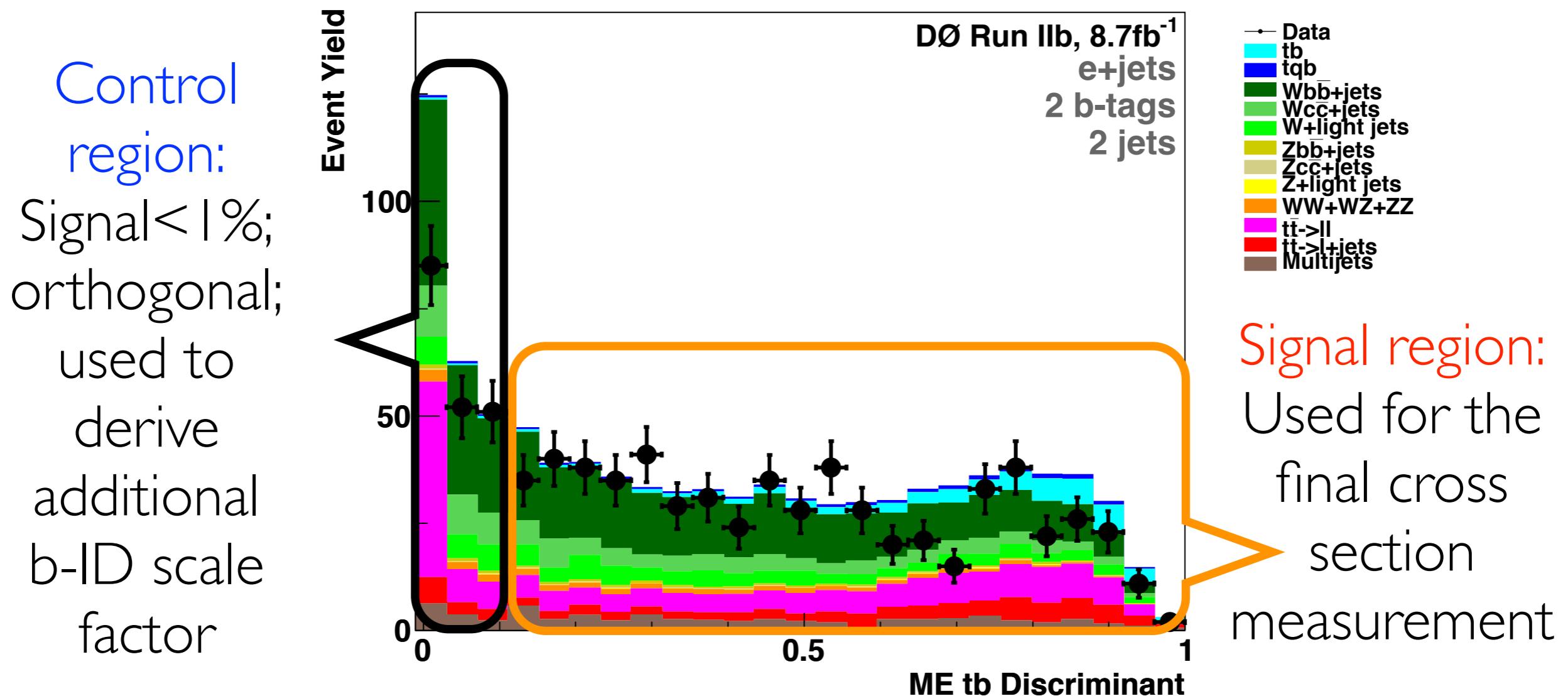
# Heavy-Flavor Modeling

- Observed mis-modeling in high  $b$ -ID output regions
  - particularly in 2-jet 2-tag channel
- Possible sources:
  - Alpgen distributions of the  $W+bb/cc$  samples
  - mis-modeling of the  $b$ -ID efficiency
- Could not identify the source owing to low data statistics in the mis-modeled regions
- Need an ad hoc correction



# Heavy-Flavor Correction

- Use a part of data to derive the correction
- The Matrix Element discriminant is unbiased by the DØ simulation

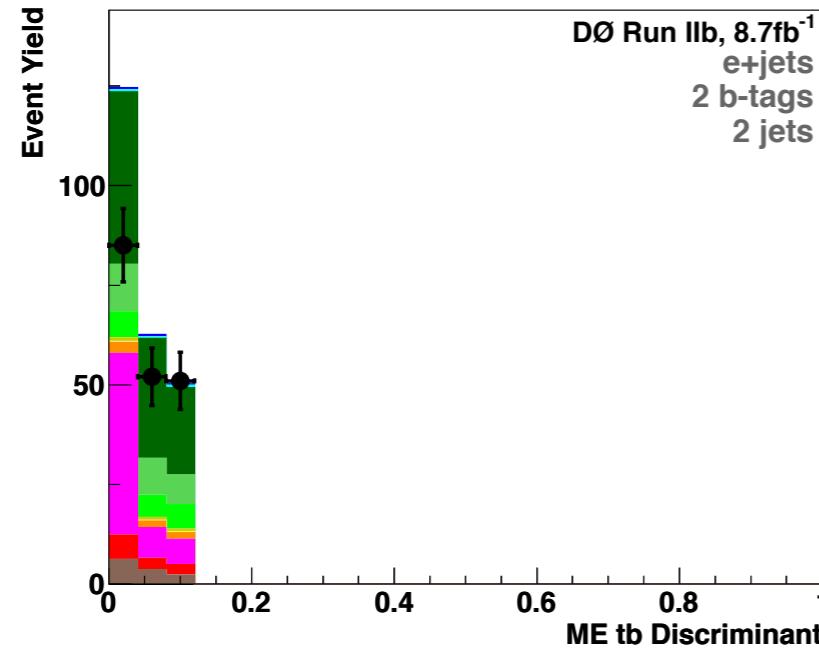
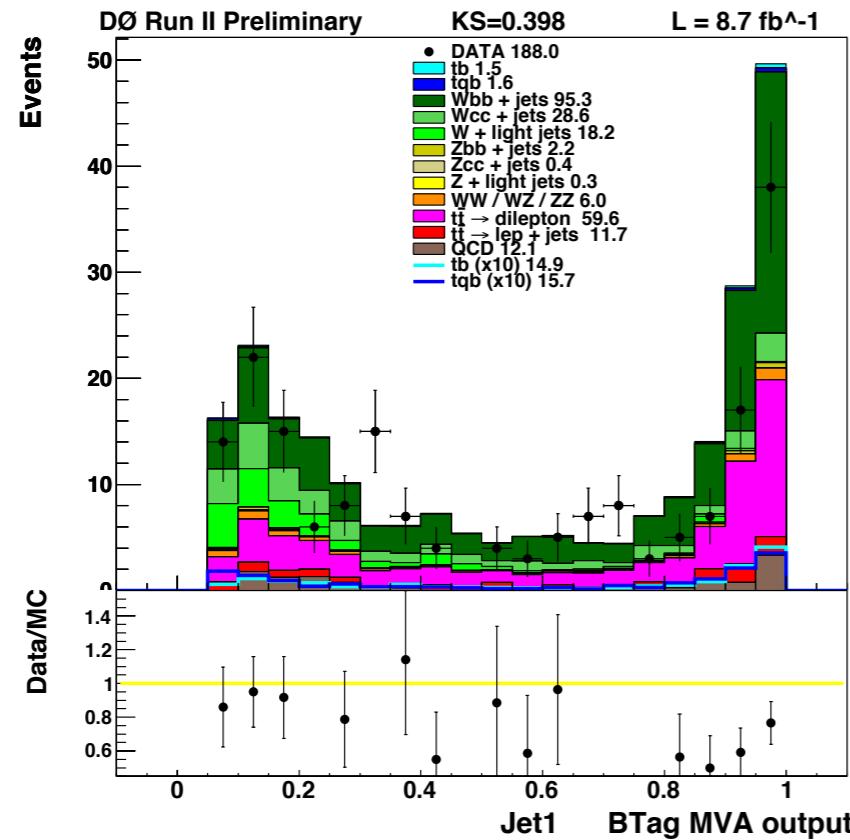


# Heavy-Flavor Correction

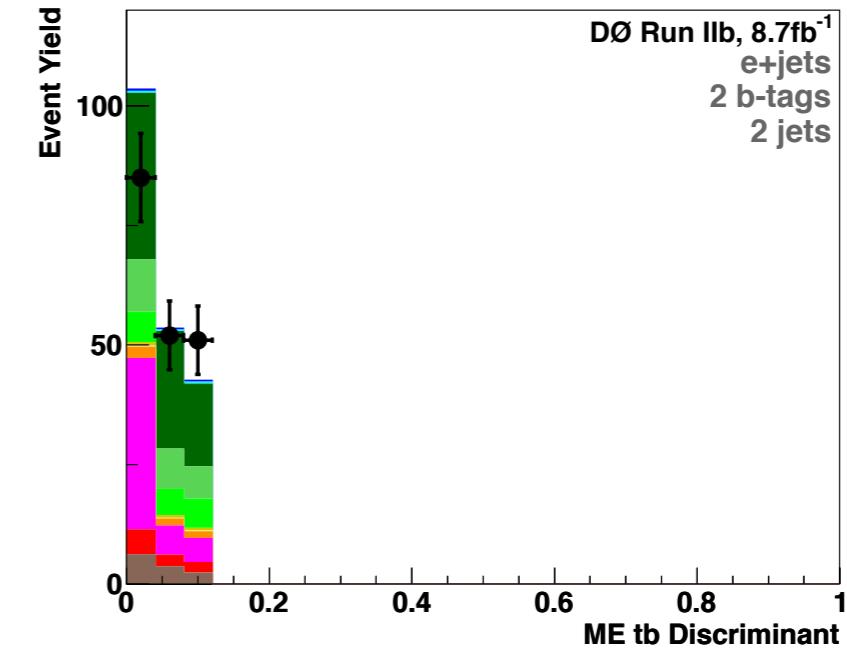
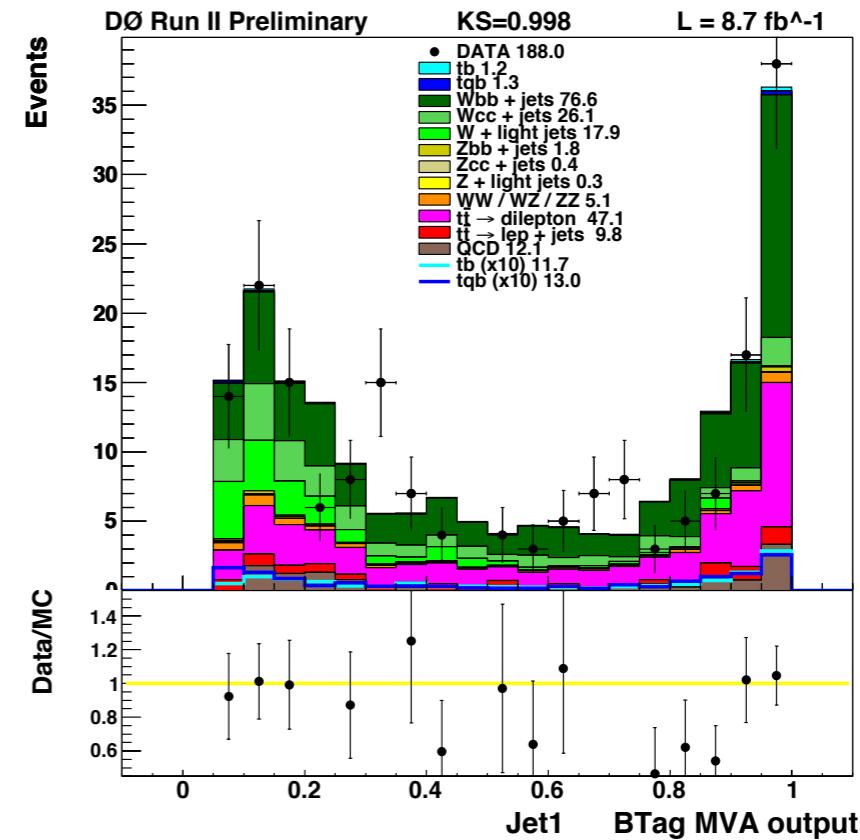
- Without the constant heavy flavor scale factor 0.8
- Use the events with  $\text{MED} < 0.12$ , orthogonal to the events used for the cross section measurement
- Use the two JetBTagMVA (BL) bins,  $(0.9, 0.95)$ ,  $(0.95, 1)$ , to derive a jet-based correction
- The corrections are found to be channel-dependent
  - Derive from 1tag and 2tag, 2jet and 3jet channels individually
  - Combine the electron and muon channels
- Apply on the jet with  $\text{JetBTagMVA (BL)} > 0.9$ , for all heavy flavor jets in all the MC samples
  - The Data-MC agreement in  $\text{JetBTagMVA (BL)} < 0.9$  is good

# Control Region: e+2jets 2tag

before corrections



after corrections



# 3 Methods for HF Scales

- Method 1: Use zero tagged samples

$$N^{(0)} = N_{wlp}^{(0)} + \lambda_{HF} N_{whp}^{(0)}$$

- Method 2: Normalize to Data in the orthogonal(0) and tagged(1) samples

$$N^{(0)} = \lambda(N_{wlp}^{(0)} + \lambda_{HF} N_{whp}^{(0)})$$

$$N^{(1)} = \lambda(N_{wlp}^{(1)} + \lambda_{HF} N_{whp}^{(1)})$$

- Method 3: Minimize  $\chi^2$  for b-ID outputs

$$\chi^2(\lambda_{HF}) = \sum_i \frac{[N_i - \lambda(\lambda_{HF})(N_{wlp,i} + \lambda_{HF} N_{whp,i})]^2}{E_i^2 + E_{wlp,i}^2 + E_{whp,i}^2}$$

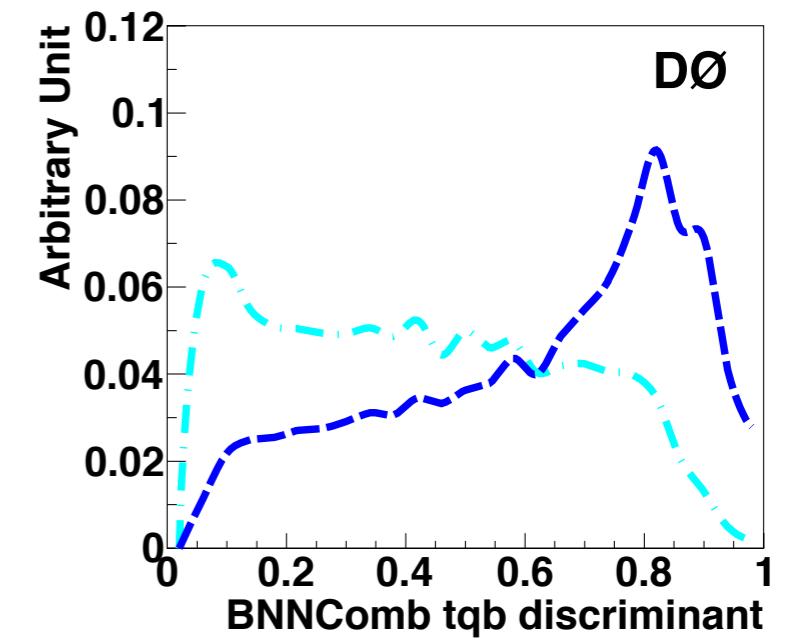
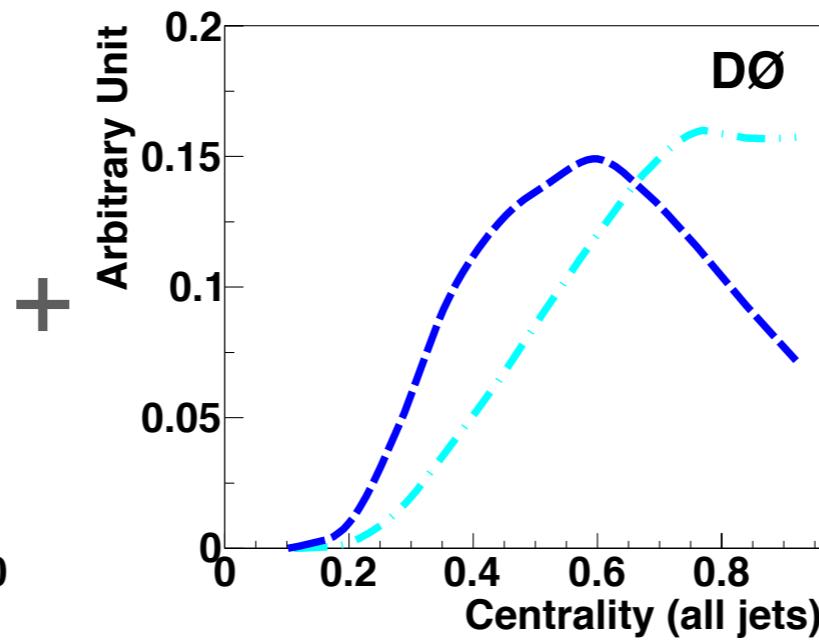
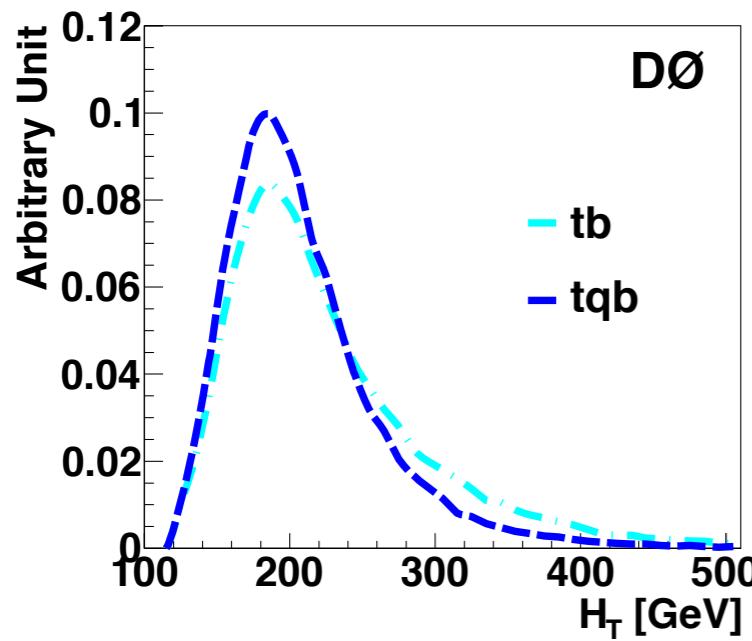
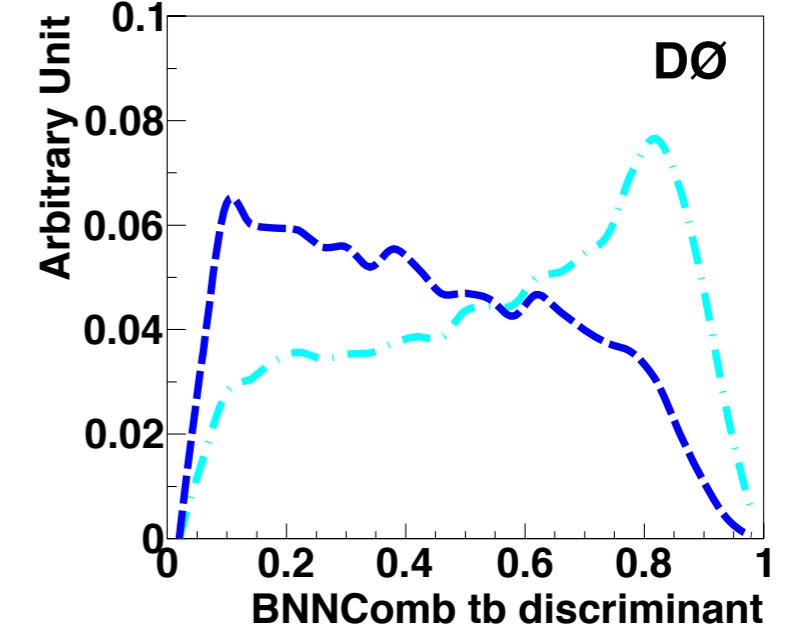
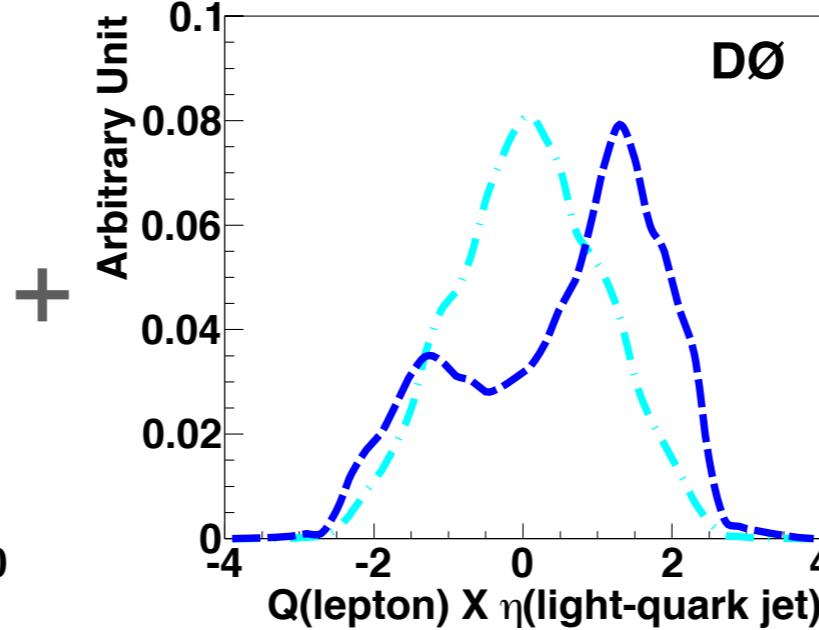
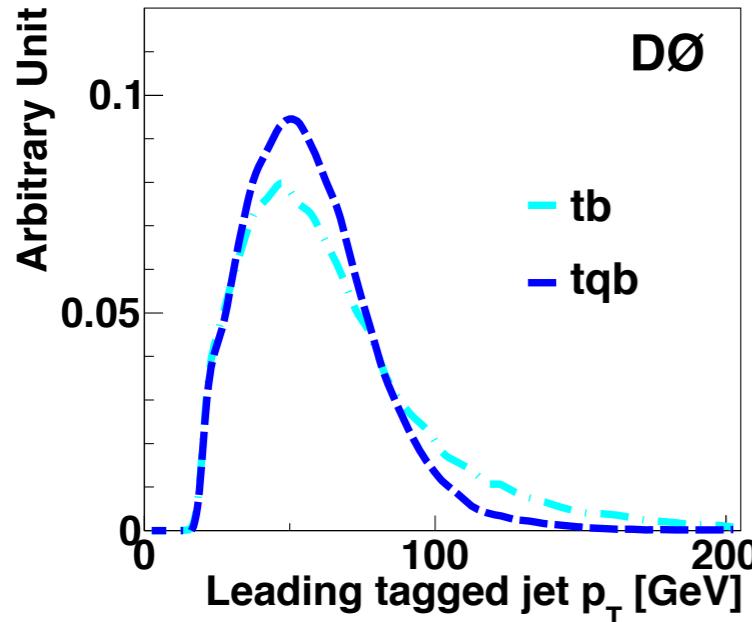
# Heavy Flavor Scale Factor

- Derived the heavy flavor scale factor with the new HF corrected samples

	$\lambda$	$\lambda_{\text{HF}}$
Method 1	1	$1.01 \pm 0.03$
Method 2	1.00	$0.98 \pm 0.03$
Method 3	1.00	$1.04 \pm 0.05$

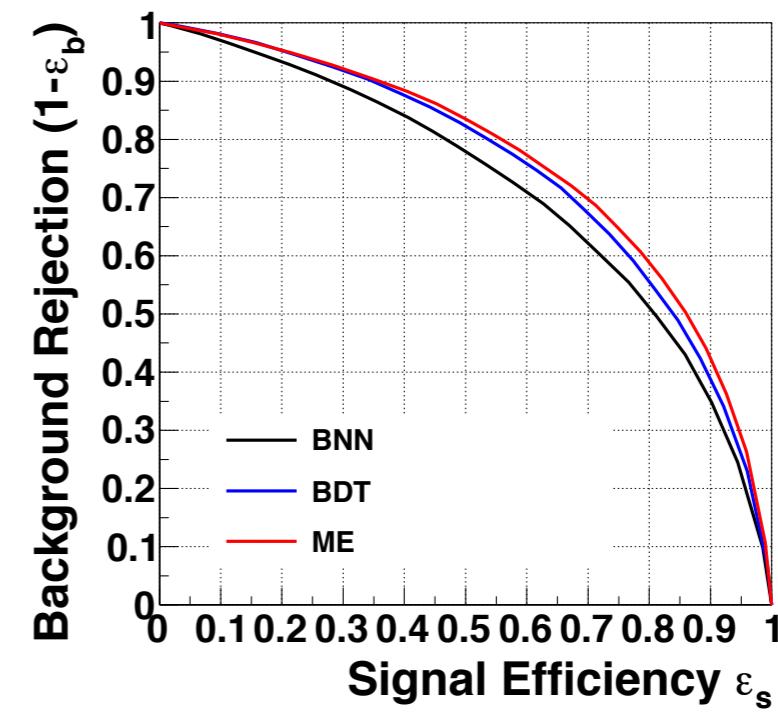
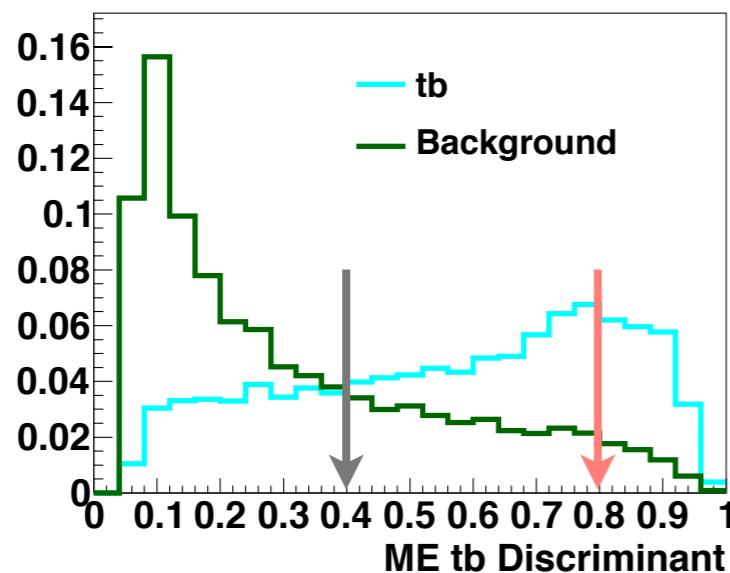
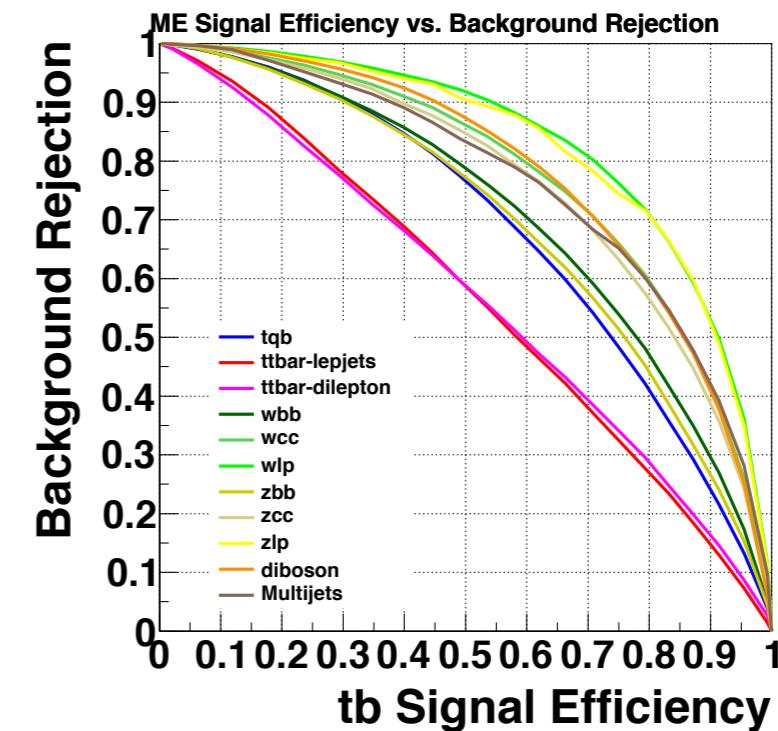
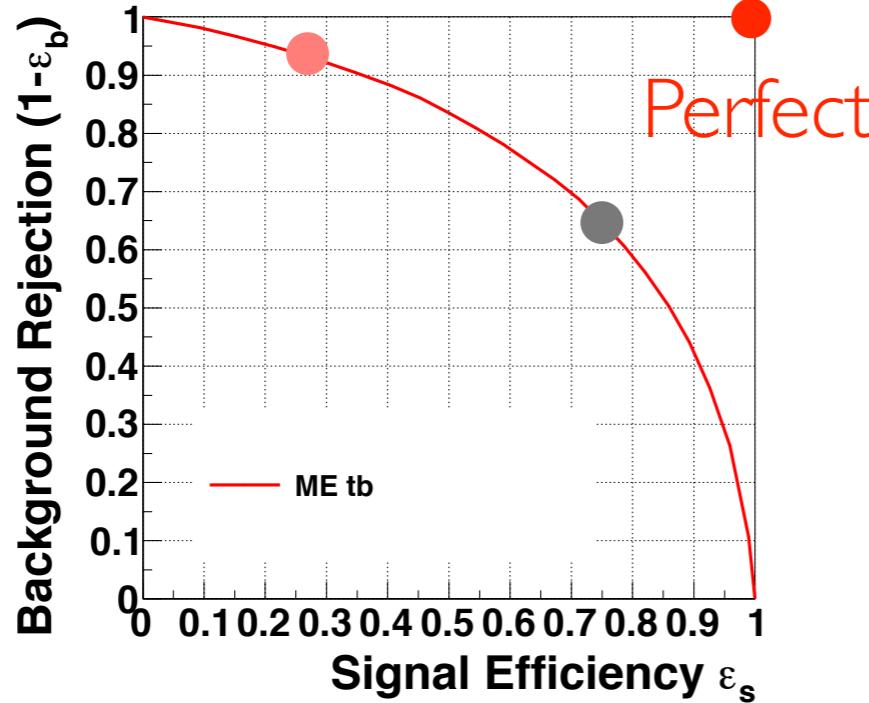
- The heavy flavor scale factors derived from all the three method are **consistent with one**
- $\lambda_{\text{HF}}$  was 1.0 from M1 but 0.8 from M2 and M3

# $tb$ versus $tqb$



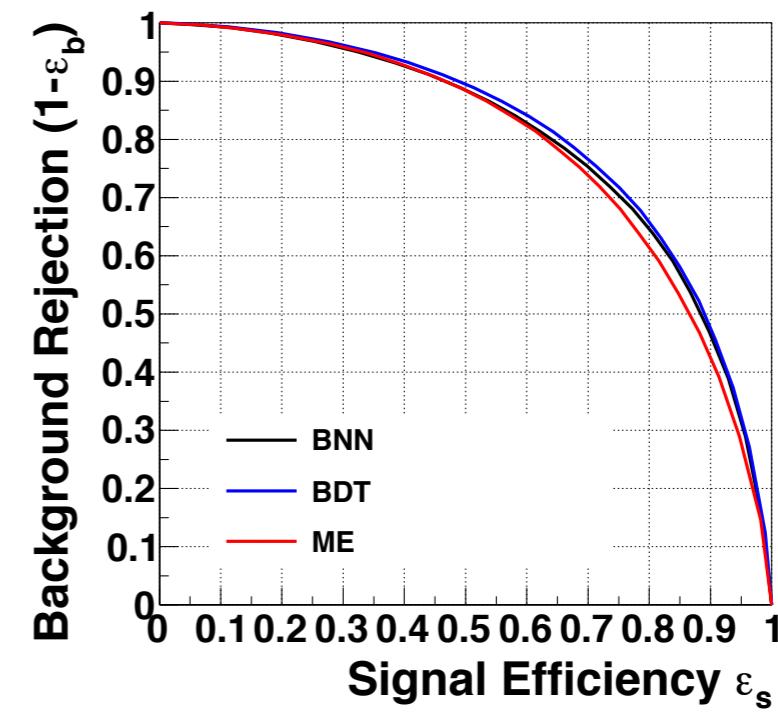
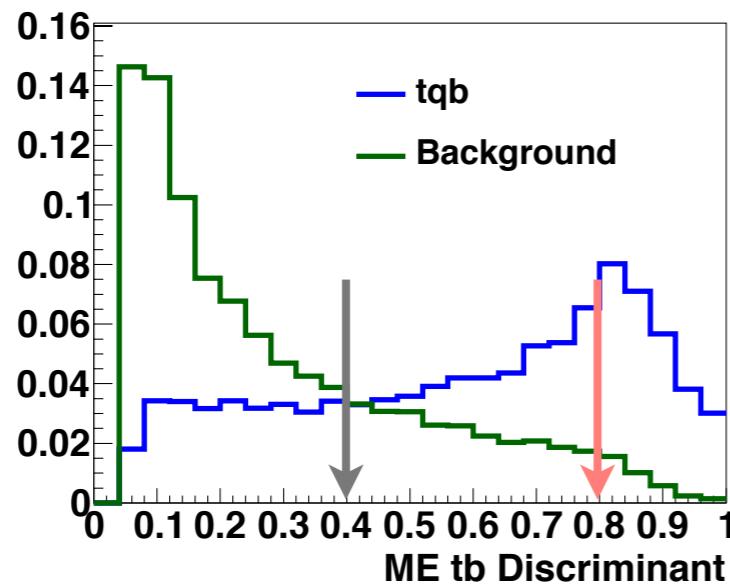
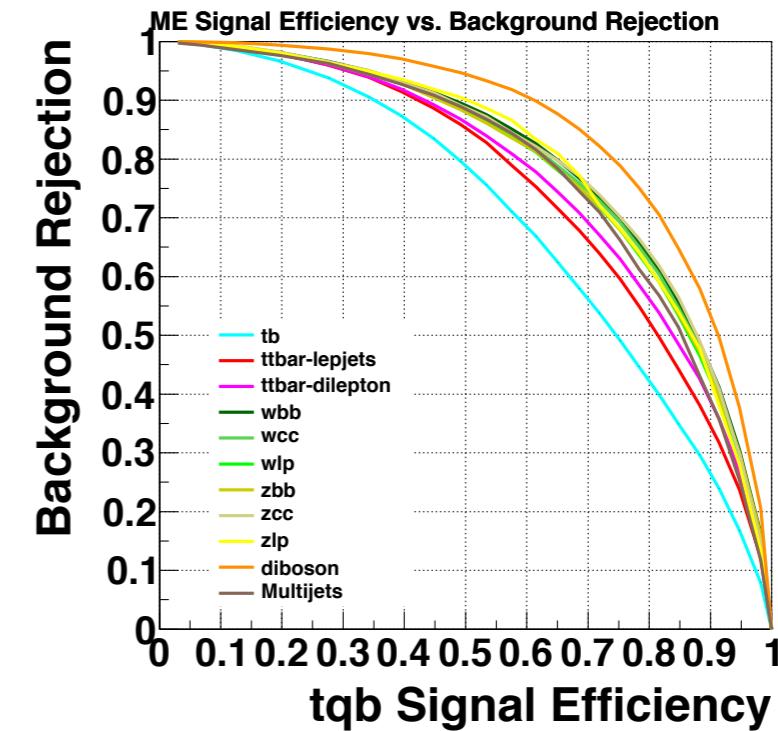
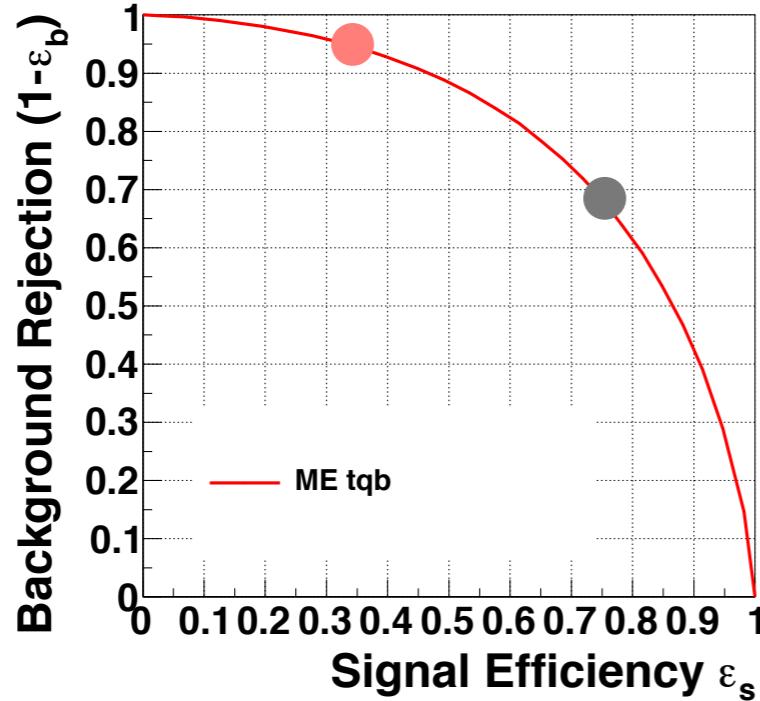
# $s$ -channel Performance

2  $b$ -tags, 2 jets



# $t$ -channel Performance

|  $b$ -tag, 2 jets



# Final tqb Discriminant

- ME discriminant: likelihood ratio

$$D(x) = \frac{P_{sig}(x)}{P_{sig}(x) + P_{bkgd}(x)}$$

- Include  $b$ -ID outputs in the probability:  $P \rightarrow P^{bl}$

	b	I	weight
Assignment 1	jet1	jet2	$btag1 \times (1 - btag2)$
Assignment 2	jet2	jet1	$(1 - btag1) \times btag2$

$$P^{bl} = \frac{w_1 d\sigma_1 + w_2 d\sigma_2}{(w_1 + w_2)\sigma}$$

# Final tb Discriminant

- b-ID outputs washed out by symmetric final states in 2 jet (sensitive to the s-channel)
- Use the probability without the  $b$ -ID outputs

$$P = \frac{d\sigma_1 + d\sigma_2}{\sigma}$$

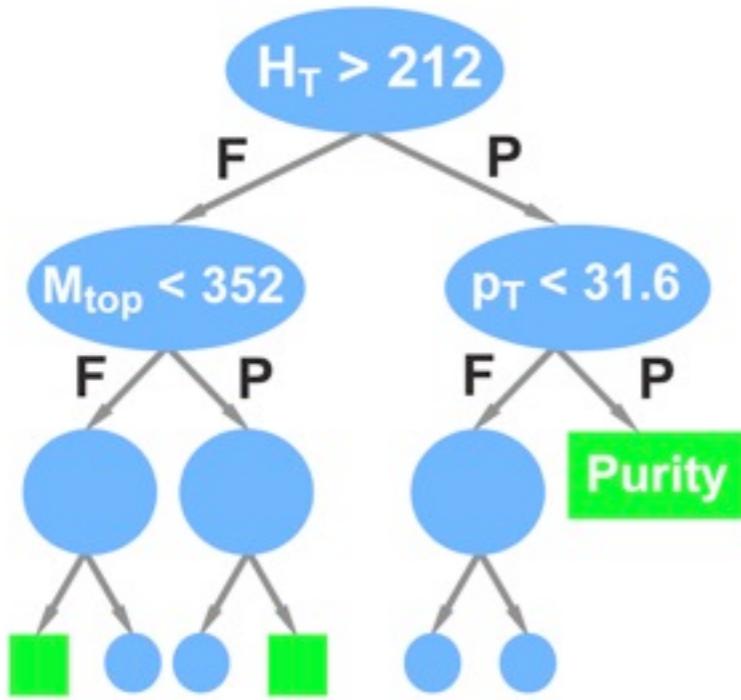
- Include the  $b$ -ID outputs according to each process

$$D(\vec{x}) = \frac{b \cdot P_S(\vec{x})}{b \cdot P_S(\vec{x}) + b \cdot P_{B:b-fs}(\vec{x}) + (1 - b) \cdot P_{B:light-fs}(\vec{x})}$$

$$b = \text{btag1} \cdot \text{btag2}; \quad 1 - b = (1 - \text{btag1})(1 - \text{btag2})$$

# Boosted Decision Tree

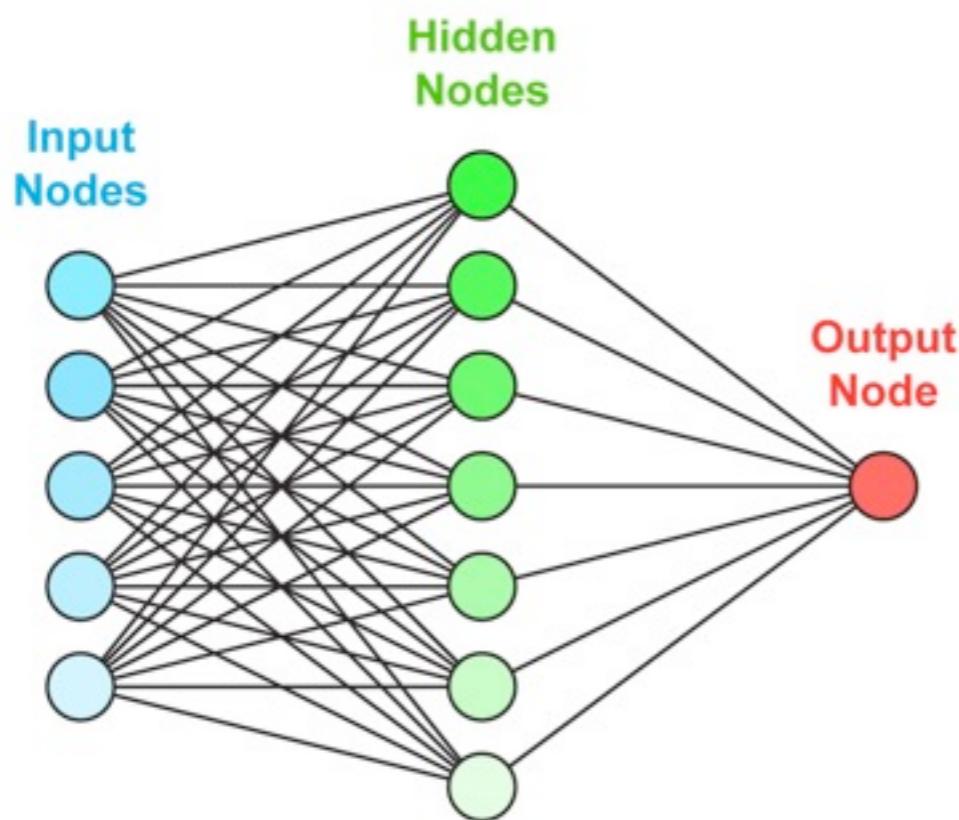
- Apply sequential cuts but keep the failing events
- Train another tree produced by enhancing misclassified events (boosting)
- Average multiple trees and boost the performance
- Up to 30 variables



#	BDT input variables
1	$E_T$
2	$p_T(\ell)$
3	$\eta(\ell)$
4	$M(\text{jet1})$
5	$p_T(\text{untag1})$
6	$E(\text{untag1})$
7	$M(\text{untag1})$
8	$b_{\text{ID}}(\text{untag1})$
9	$p_T(\text{jet2})$
10	$b_{\text{ID}}(\text{tag1})$
11	$\Delta R(\text{jet1}, \text{jet2})$
12	$\Delta R_{\min}(\ell, \text{jet})$
13	$\Delta\Phi(\ell, E_T)$
14	$\Delta\Phi(\text{jet2}, E_T)$
15	$\Delta\Phi(\text{jet1}, E_T)$
16	$Q(\ell) \times \eta(\text{untag1})$
17	$Q(\ell) \times \eta(\text{jet2})$
18	$Q(\ell) \times \eta(\ell)$
19	$Q(\ell) \times \eta(\text{tag1})$
20	$Q(\ell) \times \eta(\text{jet1})$
21	$\cos(\ell, \text{jet2})_{\text{lab}}$
22	$\cos(\ell, \text{jet1})_{\text{lab}}$
23	$H_T(\text{alljets})$
24	$H_T(\ell, E_T, \text{alljets})$
25	$H_T(\ell, E_T)$
26	Centrality(alljets)
27	$M_{\text{jet1}}, \text{jet2}$
28	$p_T(\text{jet1}, \text{jet2})$
29	$M_T(W)$
30	$p_T(W)$

# Bayesian Neural Network

- NN produces a **probability** of an event to be produced by signal processes
- Average over many networks and improve the performance

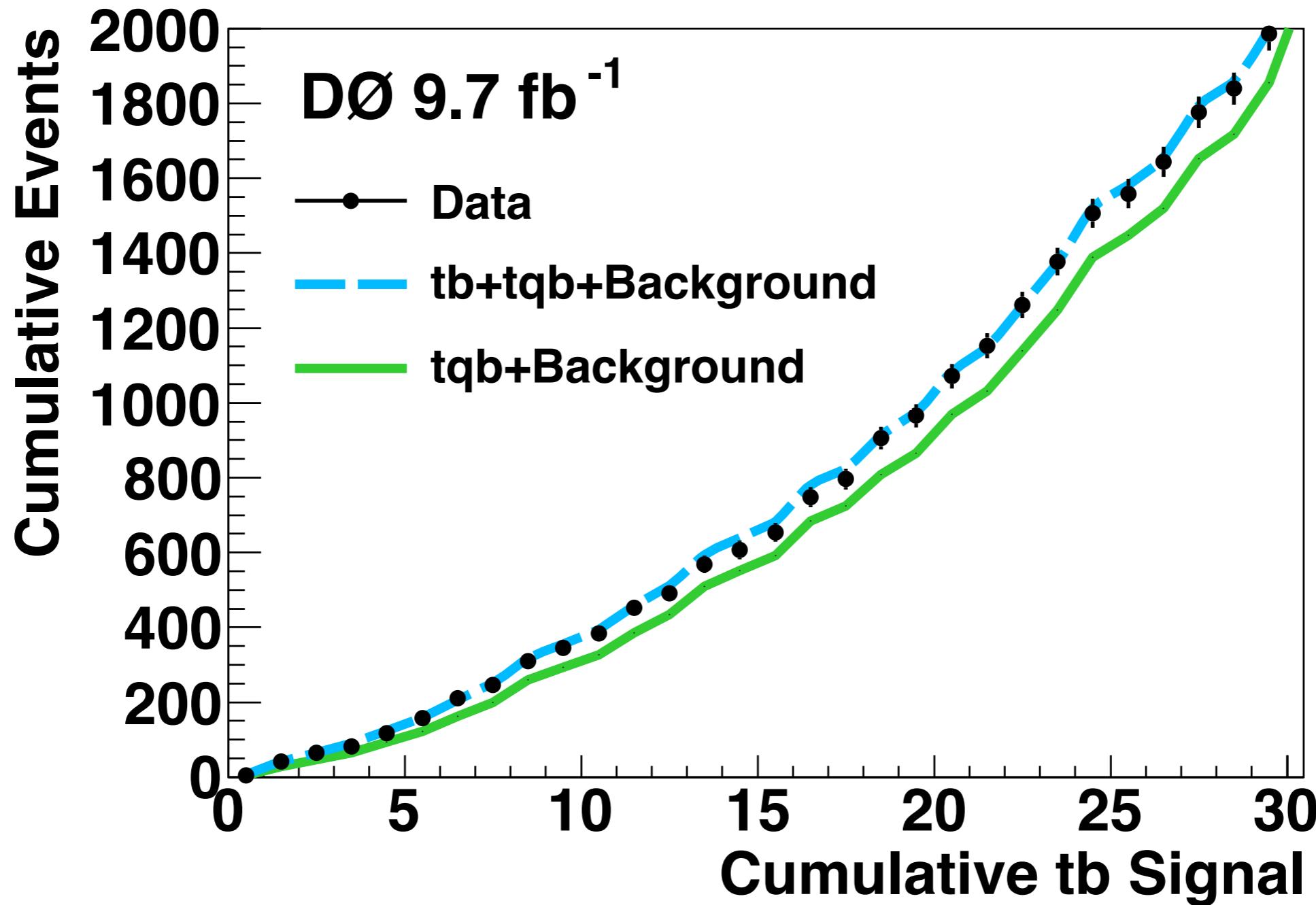


- Up to 21 variables

#	BNN input variables
1	$p_T(\text{tag1})$
2	$\eta(\text{tag1})$
3	$\Delta\Phi(\ell, \text{tag1})$
4	$b_{\text{ID}}(\text{tag1})$
5	$p_T(\text{untag1})$
6	$\eta(\text{untag1})$
7	$\Delta\Phi(\ell, \text{untag1})$
8	$b_{\text{ID}}(\text{untag1})$
9	$p_T(\ell)$
10	$\eta(\ell)$
11	$E_T$
12	$\Delta\Phi(\ell, E_T)$
13	$p_T(\text{tag2})$
14	$\eta(\text{tag2})$
15	$\Delta\Phi(\ell, \text{tag2})$
16	$b_{\text{ID}}(\text{tag2})$
17	$p_T(\text{untag2})$
18	$\eta(\text{untag2})$
19	$b_{\text{ID}}(\text{untag2})$
20	$M_T(W)$
21	$Q(\ell) \times \eta(\text{untag1})$

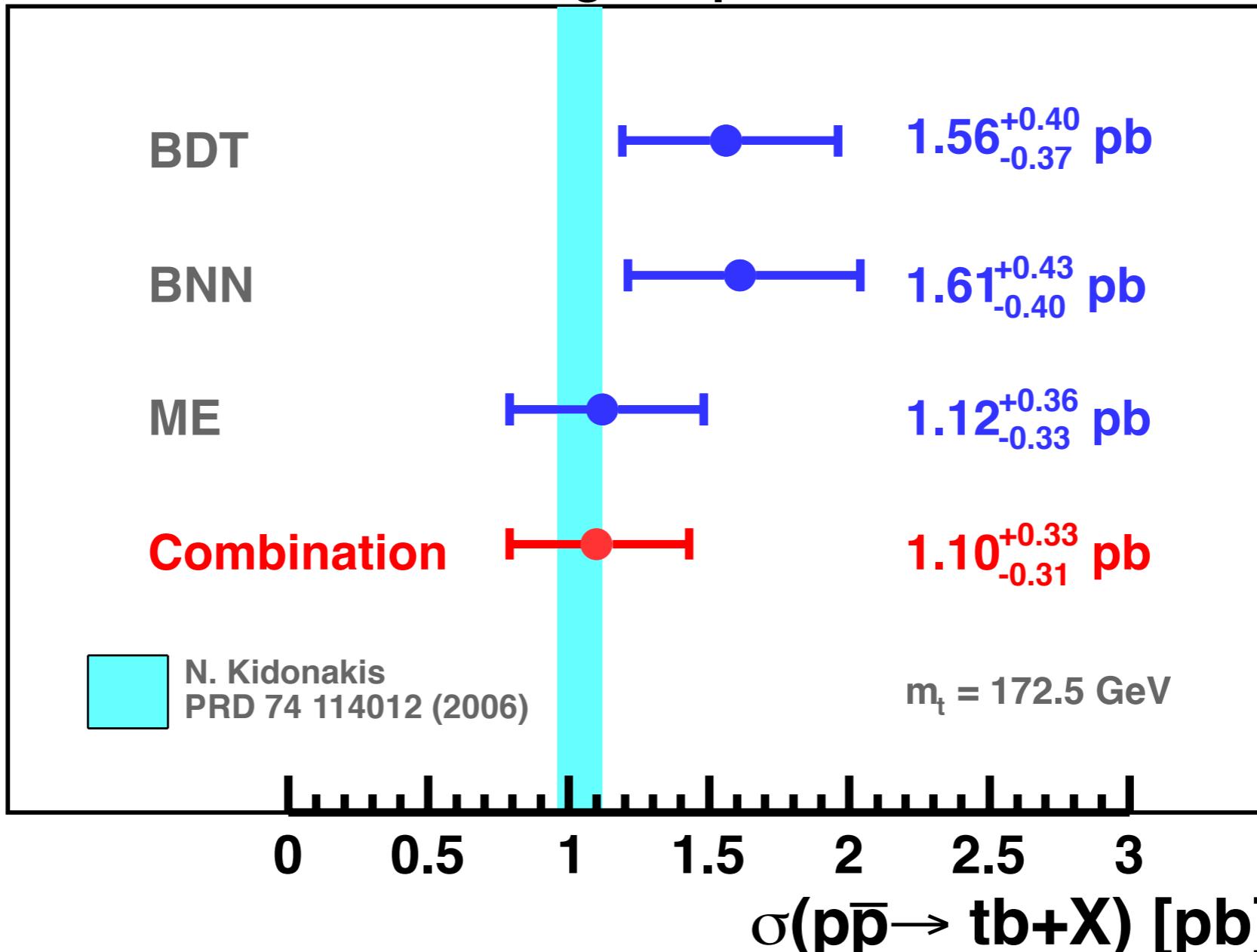
# Cumulative $tb$ -Signal Plot

Integrating from the high significance bins backward

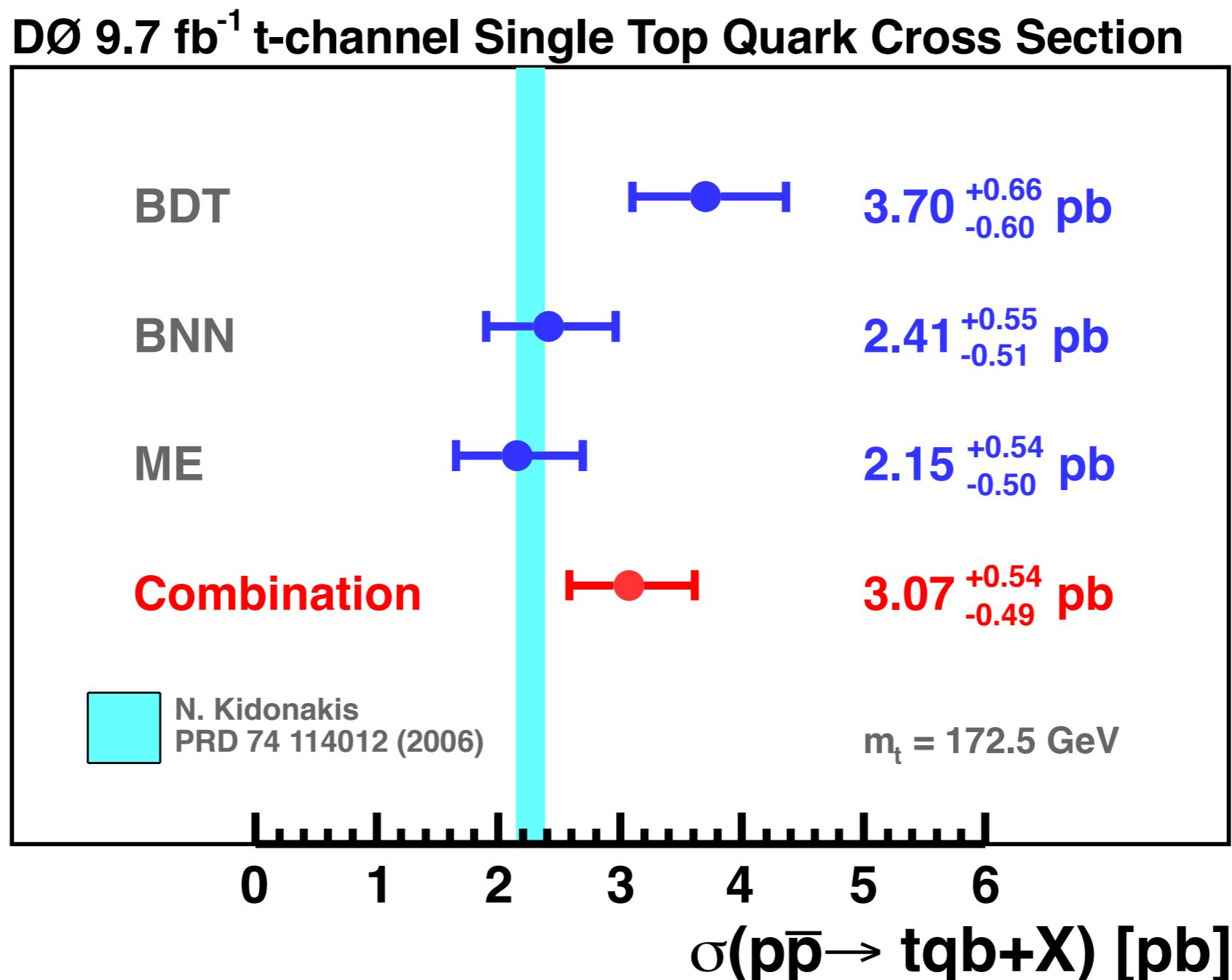


# Summary of $t\bar{b}$ Results

DØ 9.7 fb<sup>-1</sup> s-channel Single Top Quark Cross Section



# Summary of $tqb$ Results



# Bayesian Approach

- Bayes' theorem

$$p(\sigma|D) = \frac{p(D|\sigma)p(\sigma)}{p(D)}$$

- Posterior p.d.f.

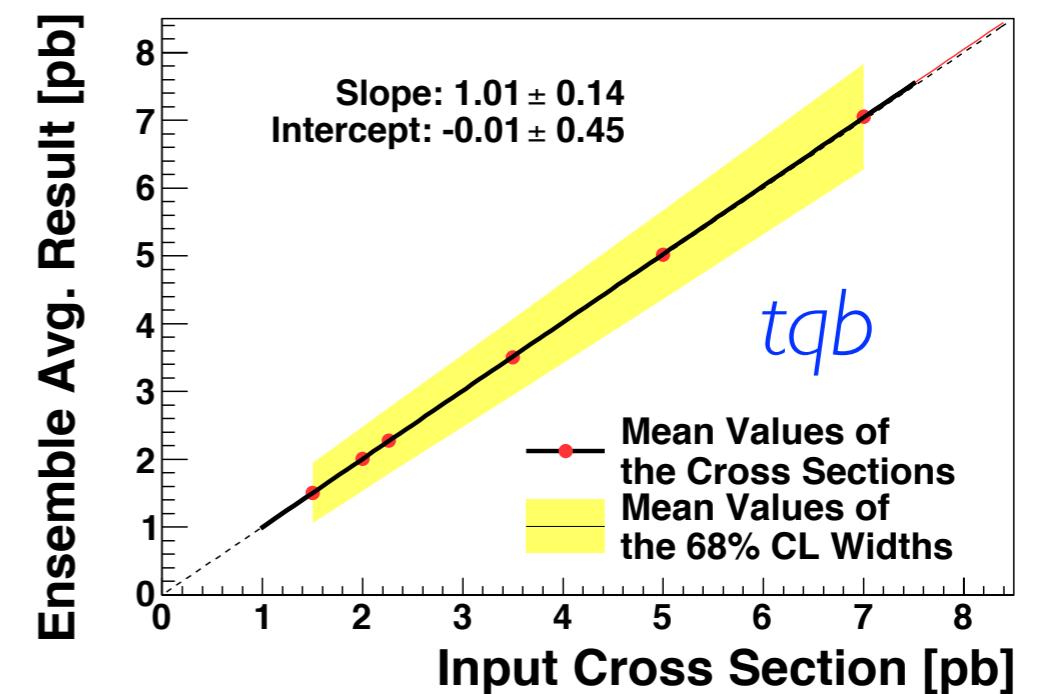
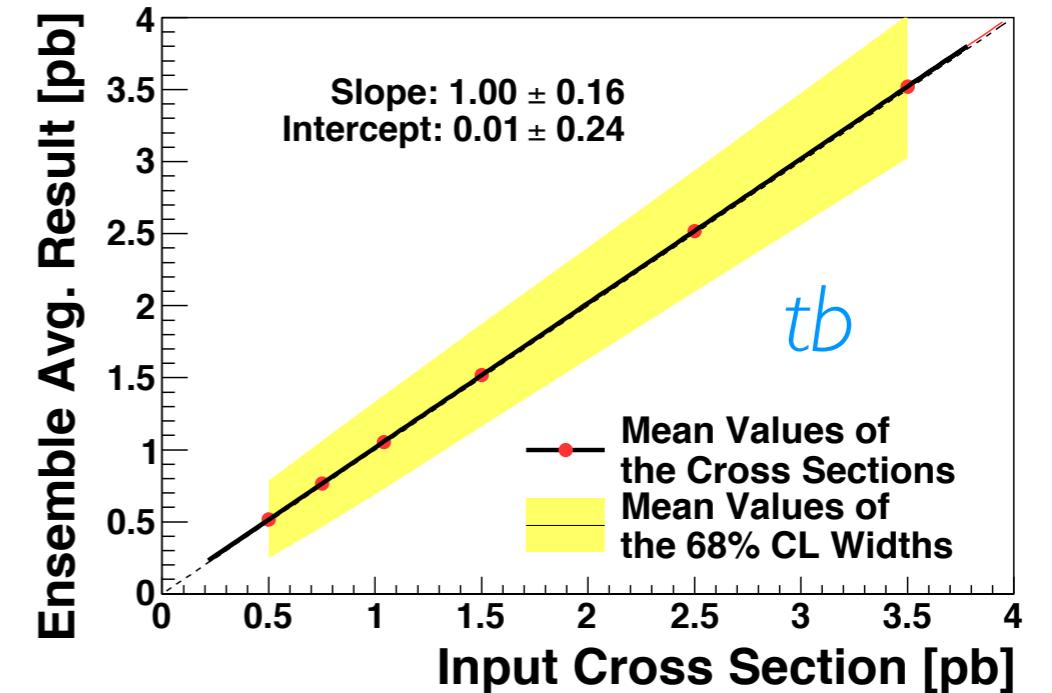
$$p(\sigma|D) = \frac{L(D|\sigma)\pi(\sigma)}{\int L(D|\sigma')\pi(\sigma')d\sigma'}$$

- Poisson distribution

$$L(D|d) = \frac{e^{-d}d^D}{\Gamma(D+1)}$$

# Ensemble Test

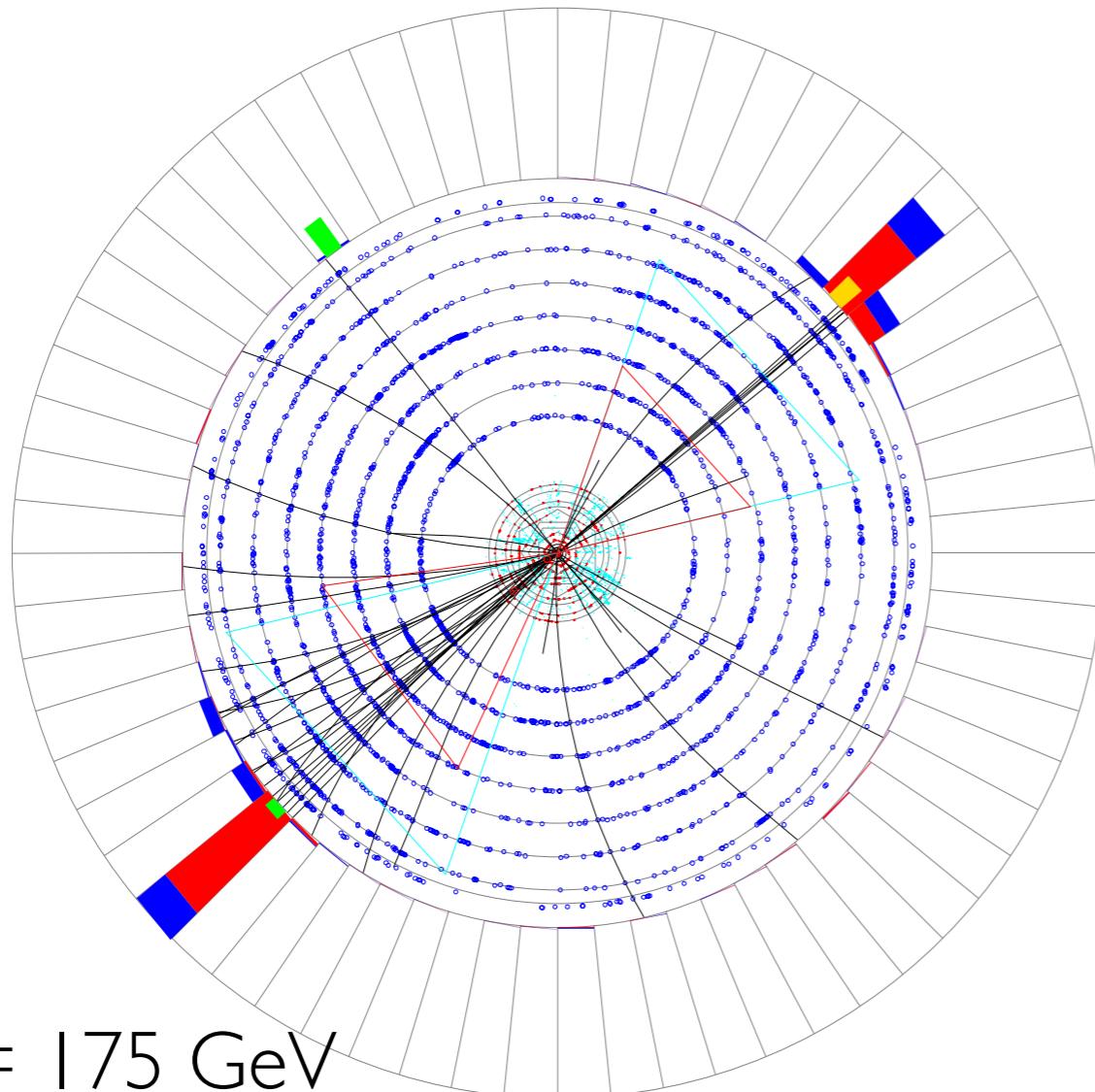
- Generate ensembles of pseudo-data samples
  - Each ensemble has a different input signal  $\sigma$
  - All systematics included
- Extract the signal cross section from each pseudo-data sample
- No calibration needed



# Another $t\bar{b}$ Candidate

Run 264600 Evt 37760117 Wed Sep 8 07:49:49 2010

ET scale: 143 GeV



$m_t = 175$  GeV

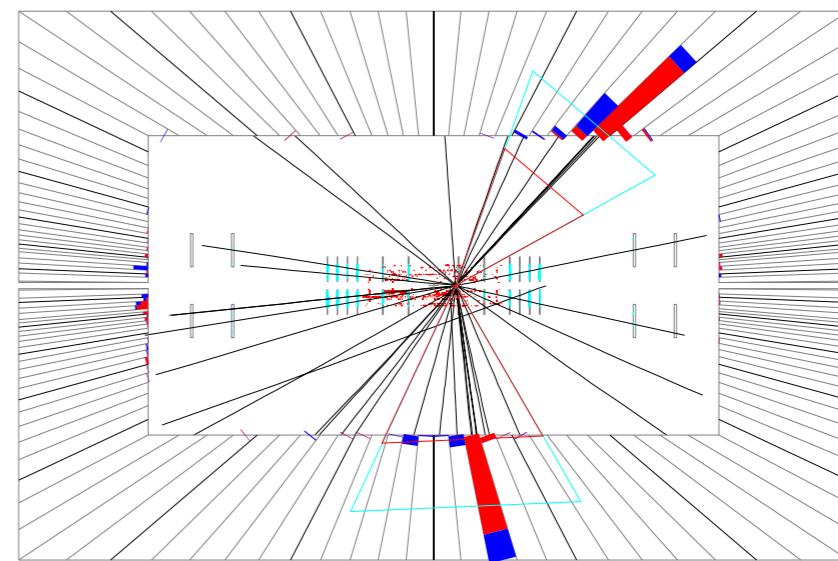
Jet1 b-tag: 0.32

Jet2 b-tag: 0.39

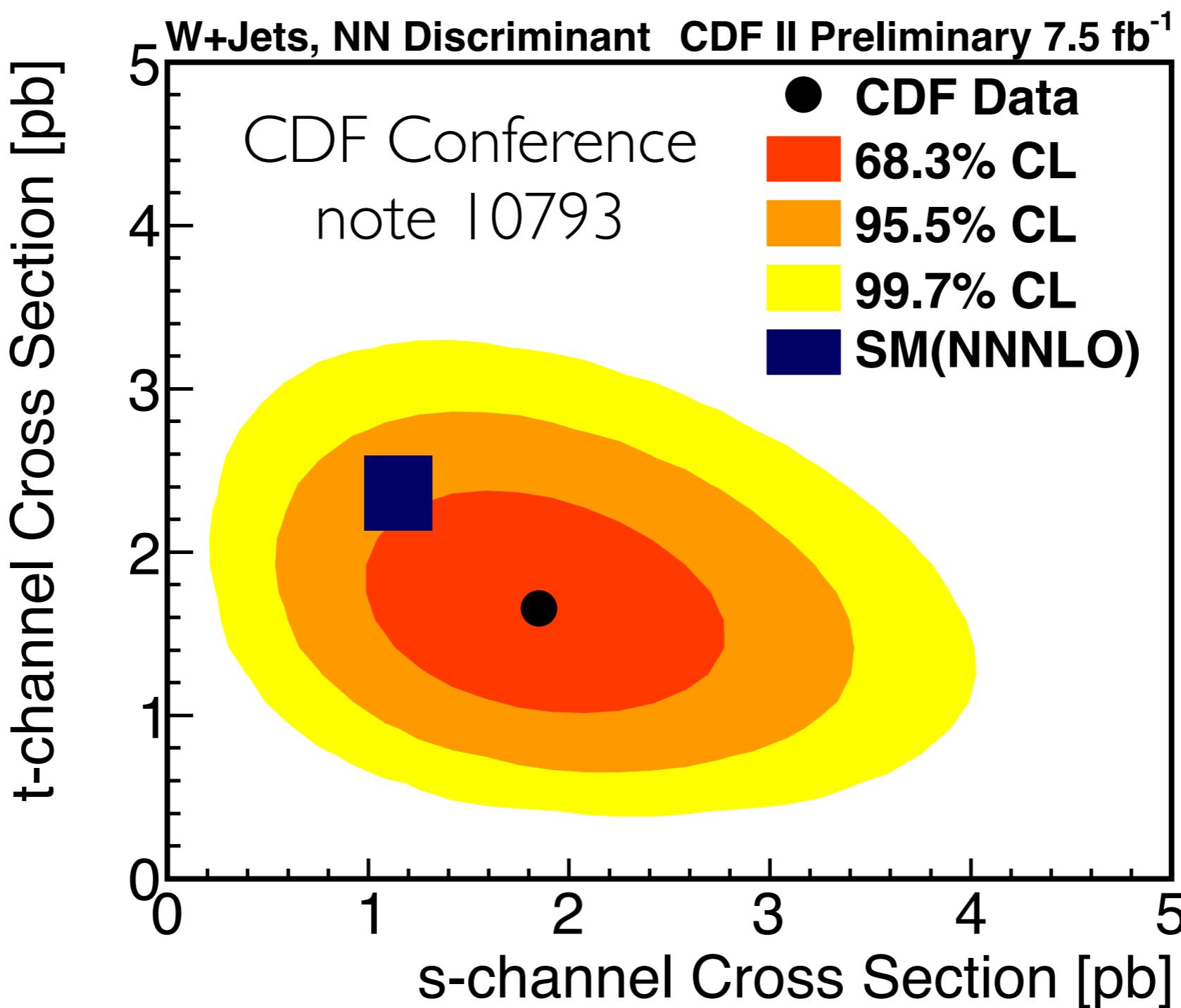
Run 264600  
Event 37760117  
Wed. Sep. 8 07:49:49 2010

Run 264600 Evt 37760117 Wed Sep 8 07:49:49 2010

E scale: 141 GeV



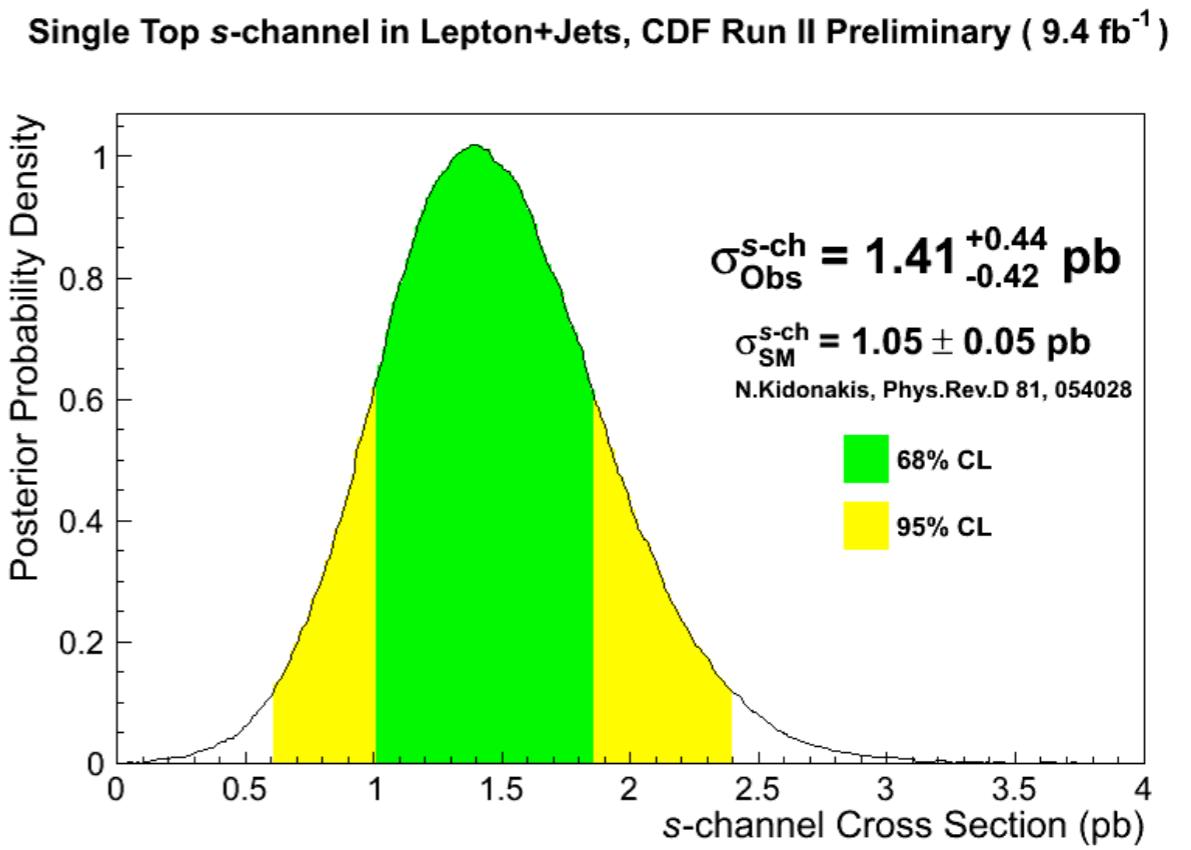
# CDF Result $7.5 \text{ fb}^{-1}$



# CDF Confirms Our Result

- In August, CDF also has the  $t\bar{b}$  single top cross section measurement with  $9.4 \text{ fb}^{-1}$  (preliminary)
  - assumes the SM  $tqb$  production
  - has evidence of the  $t\bar{b}$  production
    - $\sigma_{t\bar{b}} = 1.41 \pm 0.44 \text{ pb}$
    - Significance: 3.8 SD (expected 2.9 SD)
  - confirms our result!

CDF presentation at DPF



# CDF 9.4 fb<sup>-1</sup>: Event Yield

Category	TT	TL	T	LL
$WW$	$1.7 \pm 0.4$	$13.2 \pm 2.7$	$184 \pm 23$	$24.8 \pm 3.9$
$WZ$	$17.8 \pm 2.2$	$21.2 \pm 2.0$	$52.7 \pm 5.4$	$9.9 \pm 0.9$
$ZZ$	$2.4 \pm 0.3$	$2.4 \pm 0.2$	$7.1 \pm 0.7$	$0.96 \pm 0.08$
$Z + \text{jets}$	$10.9 \pm 1.2$	$20.7 \pm 2.3$	$163 \pm 18$	$27.1 \pm 3.1$
$t\bar{t}$	$163 \pm 21$	$194 \pm 19$	$502 \pm 50$	$58.1 \pm 6.6$
Higgs	$6.1 \pm 0.6$	$6.4 \pm 0.4$	$10.3 \pm 0.7$	$1.7 \pm 0.2$
$Wbb$	$246 \pm 99$	$327 \pm 130$	$1166 \pm 468$	$109 \pm 44$
$Wcc$	$19.0 \pm 7.8$	$120 \pm 49$	$1158 \pm 467$	$164 \pm 67$
$W + \text{Mistag}$	$4.3 \pm 1.3$	$62 \pm 13$	$978 \pm 141$	$242 \pm 34$
Multijet	$29 \pm 12$	$47 \pm 19$	$281 \pm 112$	$45 \pm 18$
$t$ and $Wt$ -channel	$18.1 \pm 2.5$	$35.3 \pm 4.2$	$251 \pm 28$	$13.6 \pm 1.5$
$s$ -channel	$54.5 \pm 6.7$	$61.2 \pm 5.6$	$109 \pm 10$	$17.8 \pm 2.1$
Total Prediction	$573 \pm 155$	$911 \pm 248$	$4860 \pm 1320$	$714 \pm 181$
Observed	466	765	4620	718
Significance	2.52	2.21	1.60	0.66

# CDF 9.4 fb<sup>-1</sup>: Systematics

Source of uncertainty	Rate	Shape	Affected samples
<i>b</i> tagging scale factor uncertainty	4%-18%		$t\bar{t}$ , single top, $WZ$ , $ZZ$ , Higgs
Charm mistag rate	7%-37%		$WW$
$W$ +jets mistag rate	4%-37%		$W$ + Mistag jets
Luminosity uncertainty	6%		$t\bar{t}$ , single top, diboson, Higgs
Lepton acceptance uncertainty	2%-4%		$t\bar{t}$ , single top, diboson, Higgs
Cross section uncertainty	6%-10%		$t\bar{t}$ , single top, diboson, Higgs
Initial/Final state radiation	0%-10%	✓	$t\bar{t}$ , single top
Multijet normalization	40%		Multijet
$Z$ +jets normalization	45%		$Z$ +jets
$Wbb$ and $Wcc$ normalization	30%		$Wbb$ , $Wcc$
$Wc$ normalization	30%		$Wc$
Jet energy scale	0%-10%	✓	All
Normalization and factorization scale		✓	$W$ +jets
Electron multijet background		✓	Electron multijet