



# Design of IBS dominated low emittance rings

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# Layout

- General introduction to intrabeam scattering (IBS)
- CLIC DR parameters
- Benchmarking of theoretical models and existing Monte Carlo codes
- Optics optimization steps for reducing IBS
  - TME cell optimization
  - Energy optimization
- IBS measurements at the SLS
- Summary

# The Intrabeam scattering effect

- Small angle **multiple Coulomb scattering** effect
  - Redistribution of beam momenta
  - Beam diffusion with impact on the beam quality
    - Brightness , luminosity, etc
- **Different approaches** for the probability of scattering
  - Classical Rutherford cross section
  - Quantum approach
    - Relativistic “Golden Rule” for the 2-body scattering process
- **Several theoretical models** and their **approximations** developed over the years → **three main drawbacks**:
  - Gaussian beams assumed
  - Betatron coupling not trivial to be included
  - Impact on damping process?

# The Intrabeam scattering effect

- Theoretical models calculate the **IBS growth rates**:

$$\frac{1}{T_i} = f(\text{optics}, \text{beam params})$$

- **Complicated integrals** averaged around the rings
  - Depend on **optics** and **beam properties**

- Classical models of Piwinski (**P**) and Bjorken-Mtingwa (**BM**)
  - Benchmarked with measurements for hadron beams but not for lepton beams in the presence of synchrotron radiation (SR) and quantum excitation (QE)
- High energy approximations **Bane** and **CIMP**
  - Integrals with analytic solutions
- Tracking codes **SIRE** and **CMAD-IBStrack**
  - Based on the classical approach

# IBS Calculations

Horizontal, vertical and longitudinal **equilibrium states** and **damping times** due to SR damping

The IBS growth rates in one turn (or one time step)

$$\frac{1}{T_i} = \langle f_i \rangle$$

Complicated integrals averaged around the ring.

$$\begin{aligned} \frac{d\varepsilon_x}{dt} &= -\frac{2}{\tau_x}(\varepsilon_x - \varepsilon_{x0}) + \frac{2\varepsilon_x}{T_x(\varepsilon_x, \varepsilon_y, \sigma_p)} \\ \frac{d\varepsilon_y}{dt} &= -\frac{2}{\tau_y}(\varepsilon_y - \varepsilon_{y0}) + \frac{2\varepsilon_y}{T_y(\varepsilon_x, \varepsilon_y, \sigma_p)} \\ \frac{d\sigma_p}{dt} &= -\frac{1}{\tau_p}(\sigma_p - \sigma_{p0}) + \frac{\sigma_p}{T_p(\varepsilon_x, \varepsilon_y, \sigma_p)} \end{aligned}$$

If = 0

**Steady State emittances**

If ≠ 0

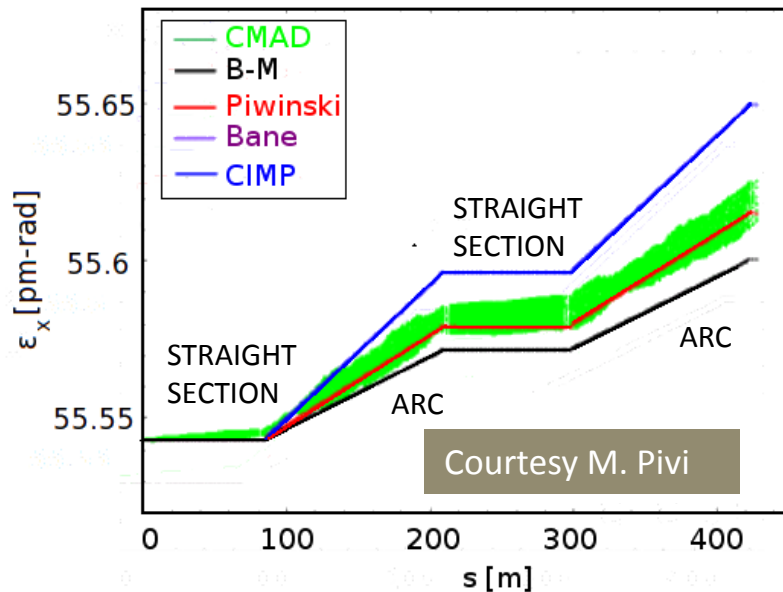
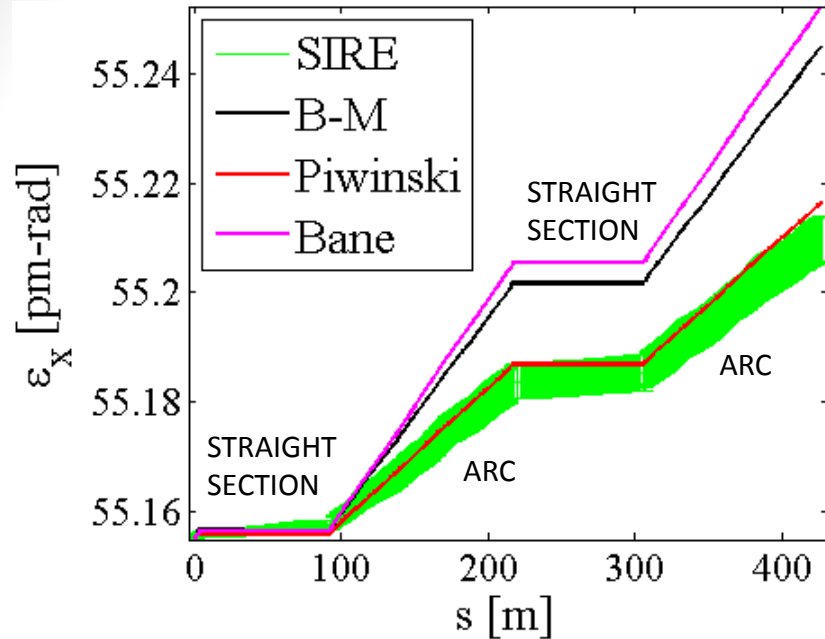
Steady state exists if we are below transition or in the presence of SR .

# The CLIC DR parameters

Parameters	1 GHz	2 GHz	V06
General			
Energy [GeV]	2.86	2.86	2.424
Circumference [m]	427.5	427.5	493.05
Bunches per train	156	312	312
Energy loss/turn [MeV]	3.98	3.98	3.98
RF voltage [MV]	5.1	4.5	4.3
RF harmonic (h)	1425	2850	3287
RF stationary phase [°]	51	62	67
Energy Acceptance [%]	1	2.5	0.98
Natural chromaticity x/y	-115/-85	-115/-85	-148.8/-79.0
Momentum compaction factor [ $10^{-4}$ ]	1.27	1.27	0.644
Damping times x/y/s [ms]	2/2/1	2/2/1	2/2/1
Number of arc cells/wigglers	100/52	100/52	100/76
Phase advance per arc cell x/y	0.408/0.05	0.408/0.05	0.442/0.045
Dipole focusing strength $K_1[m^{-2}]$	-1.1	-1.1	-1.1
Dipole length [m]/field [T]	0.58/1.03	0.58/1.03	0.4/1.27
Without the IBS			
Normalized Hor. emittance [nm-rad]	312	312	148
Energy spread [ $10^{-3}$ ]	1.2	1.3	1.12
Bunch Length [mm]	1.18	1.46	0.95
Longitudinal Emittance [keV-m]	5.01	4.39	2.58
With the IBS			
Bunch population [ $10^9$ ]	4.1	4.1	4.1
Normalized Hor. emittance [nm-rad]	456	472	436
Normalized Vert. emittance [nm-rad]	4.8	4.8	5
$\epsilon_{x,IBS}/\epsilon_{x,0}$	1.44	1.5	2.9
Longitudinal Emittance [keV-m]	6	6	5
Space charge tune shift	-0.10	-0.11	-0.2

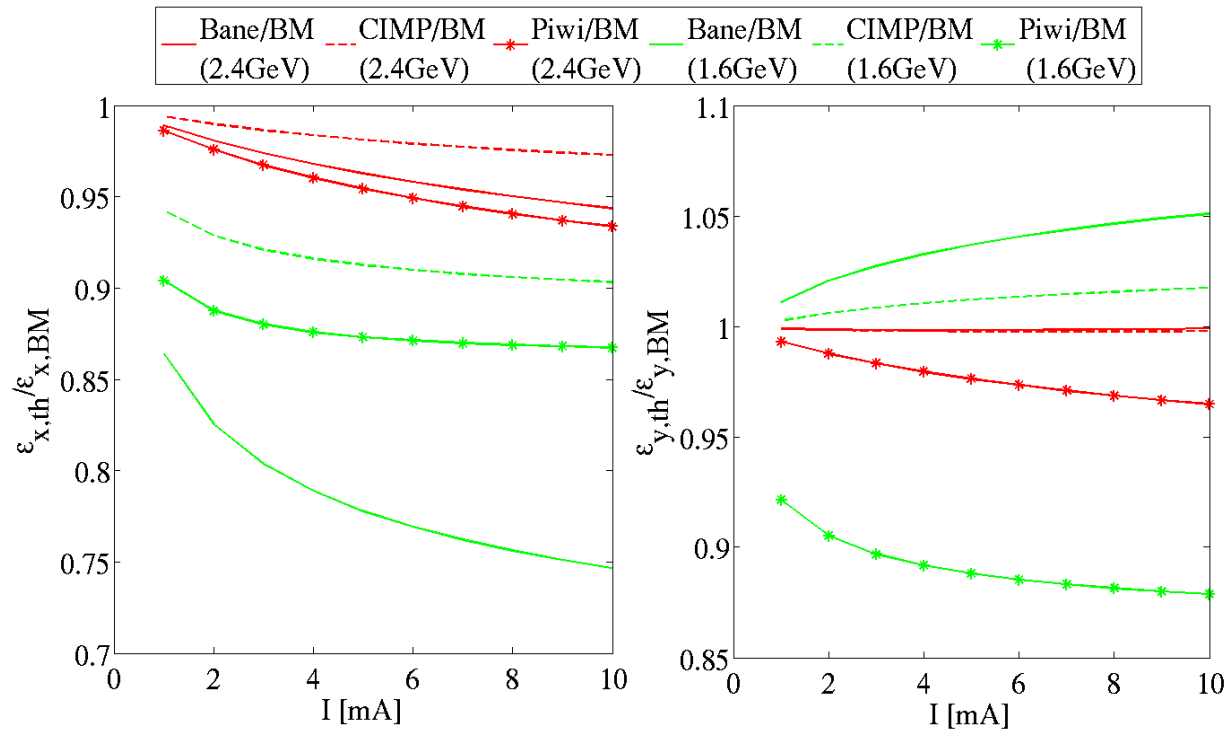
- Performance parameters of the CLIC Damping Rings
- 2 RF options (1 & 2 GHz)
- V06: Intermediate design stage
- The output emittances strongly dominated by the IBS effect
  - The motivation of our IBS studies
  - The effect will be even stronger in a low energy CLIC option where the bunch current should be increased

# Benchmarking of MC codes with theories



- **SIRE** (top) and **CMAD-IBStrack** (bottom) benchmarking with theoretical models for the CLIC DR lattice
  - 1 turn emittance evolution comparison
- **Excellent** agreement with **Piwinski** as expected
- All models and codes follow the **same trend** on the emittance evolution
- Clear **dependence** on the **optics**
  - Large contribution from the arcs

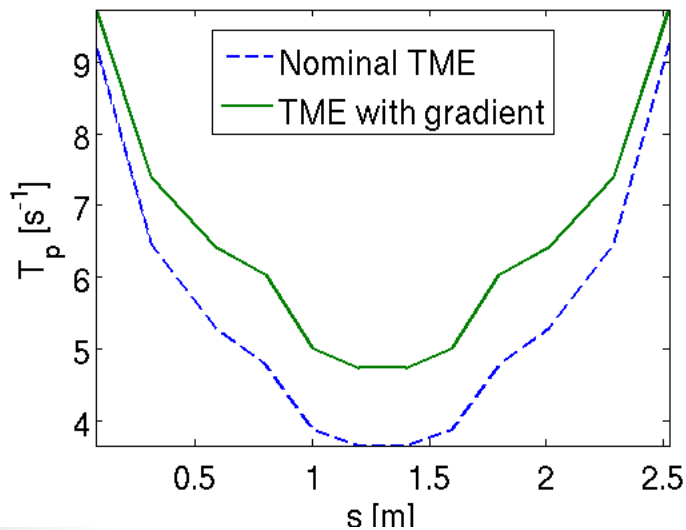
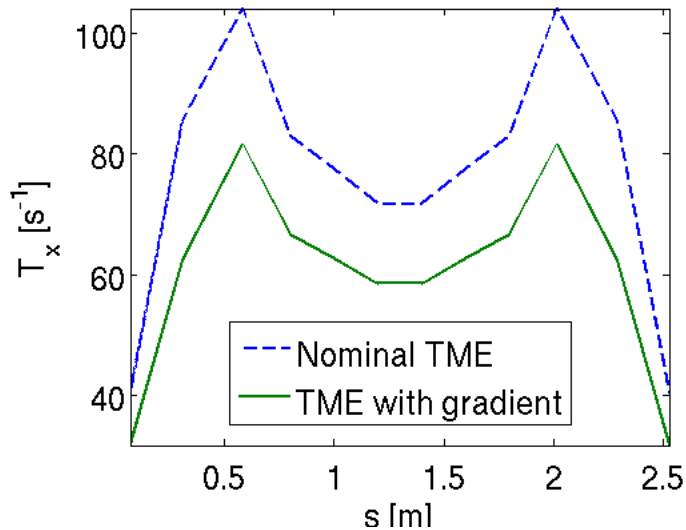
# Comparison between theoretical models



- Comparison between the theoretical models for the SLS lattice
- All results normalized to the ones from BM
- Good agreement at weak IBS regimes
- Divergence grows as the IBS effect grows
  - Benchmarking of theoretical models and MC codes with measurements is essential

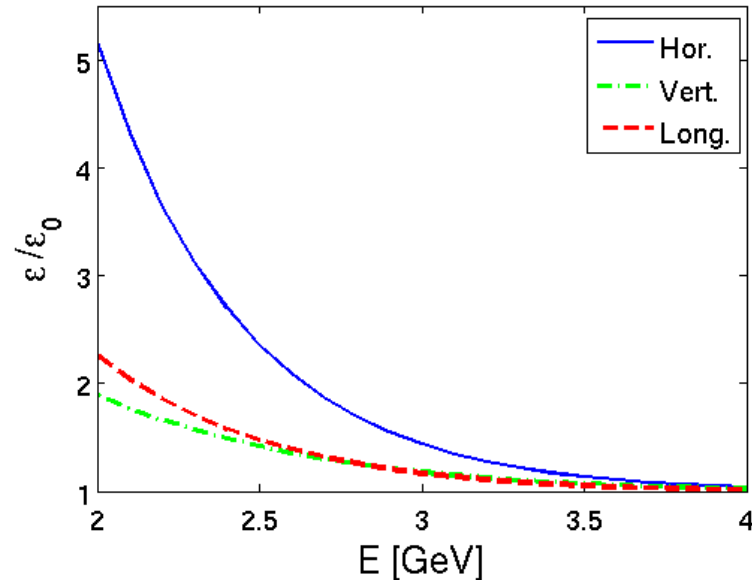
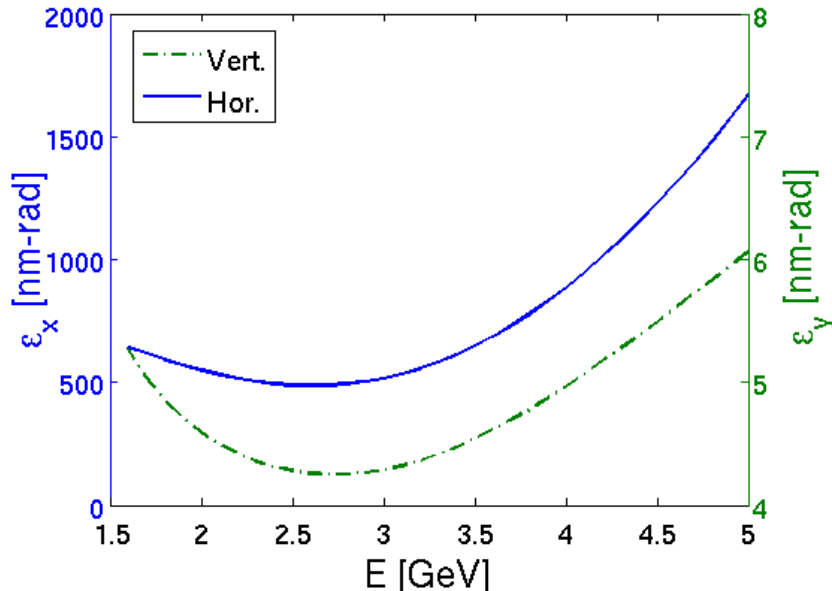


# TME optimization with respect to IBS



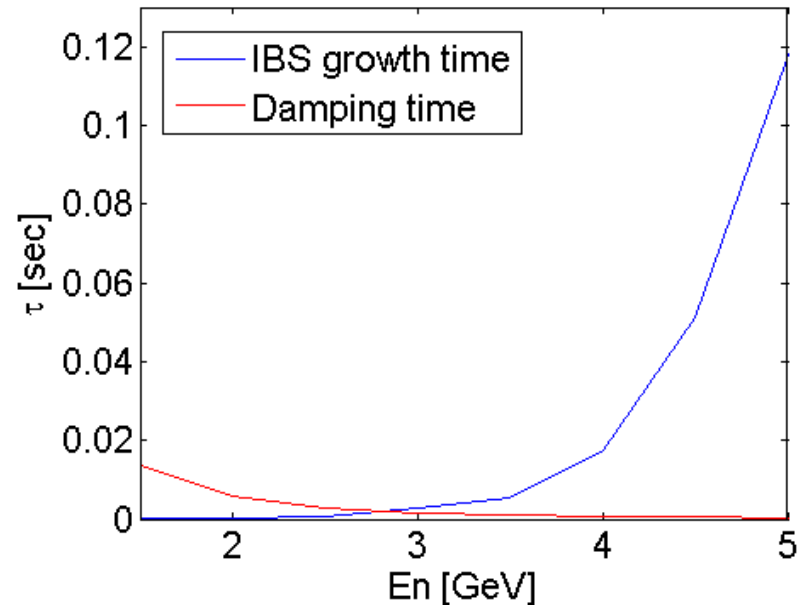
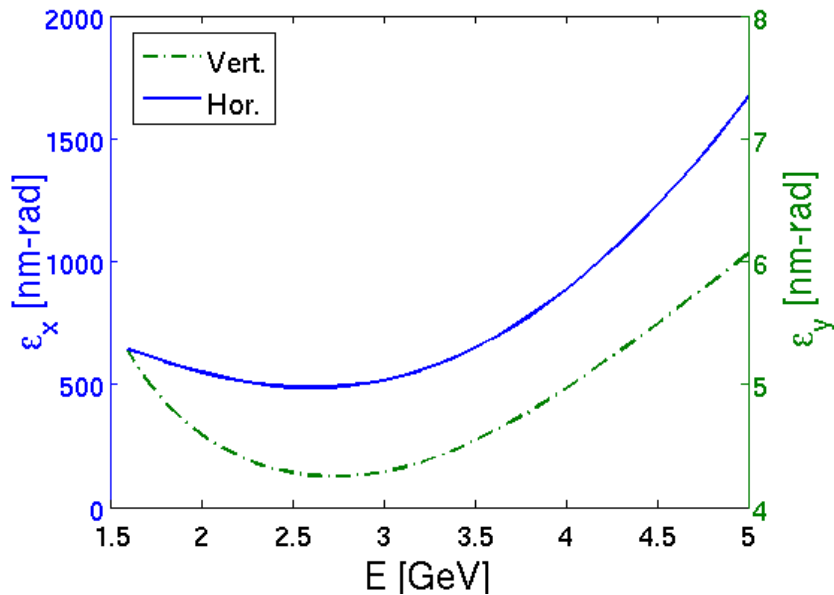
- IBS growth rate in the initial (2007) design a factor of 6
- The main contribution to the IBS growth comes from the arcs (small dispersion and beta functions at the center of the TME dipole)
- Using a modified TME cell, with combined function dipole with small defocusing gradient, has a positive impact on the IBS effect → Reduced the effect by a factor of 2 (from 6 → 3)
- Still room for improvement!

# Energy choice for IBS reduction



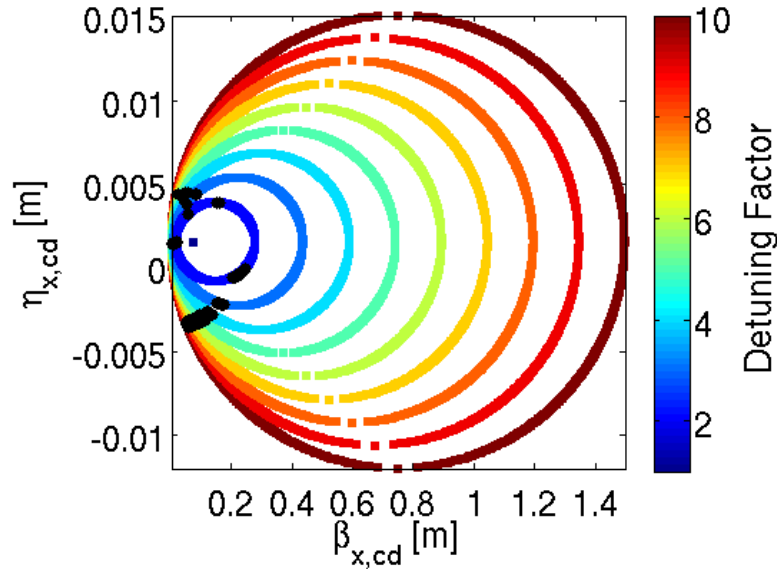
- **Scaling** of output transverse emittances with **energy** (taking into account IBS)
- Broad minimum of the emittances around 2.5 GeV (left) while the IBS effect becomes weaker with energy (right)
  - Higher energies are interesting for IBS but not for the emittance requirements
- **Energy increase** (2.424  $\rightarrow$  2.86 GeV)  $\rightarrow$  **reduction of the IBS effect** by a factor of 2 (3  $\rightarrow$  1.5)

# Energy choice for IBS reduction

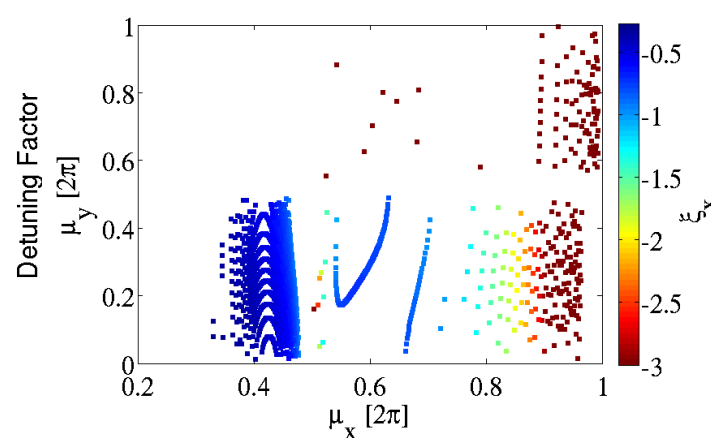
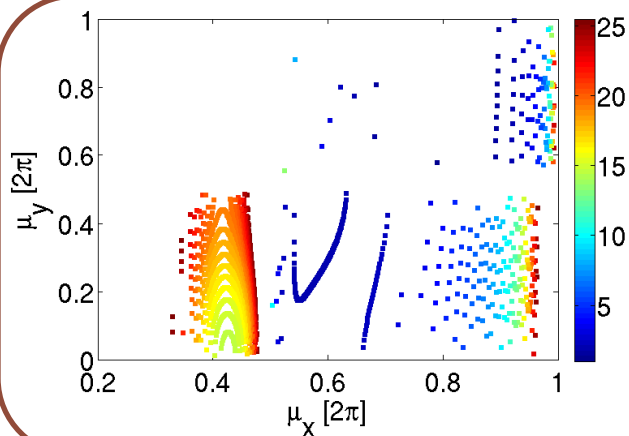


- Interesting to notice that the scaling of the output emittance with energy reflects the domination of damping time or IBS growth time in each energy regime.

# TME cell optimization with respect to IBS

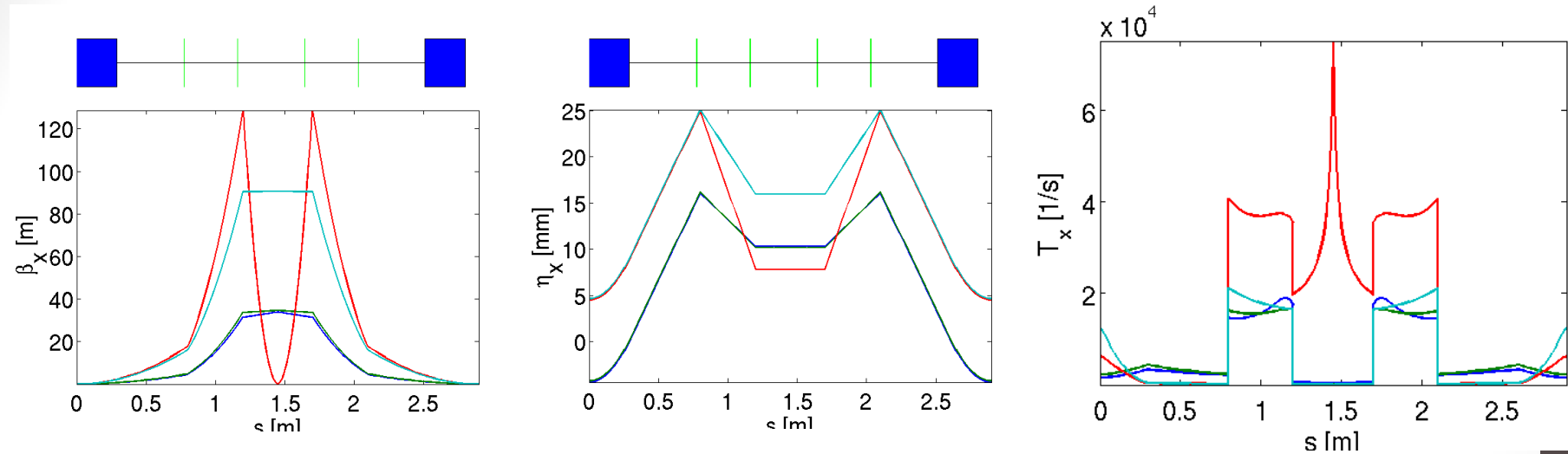


- Analytical parameterization of the TME cell
  - All cell properties globally determined
- Solutions of the hor. beta and dispersion in the center of the dipole lie in ellipses
  - Each ellipse corresponds to different emittance
- For the same detuning factor different optics options
- Only the solutions in black satisfy the stability criteria in both horizontal and vertical planes

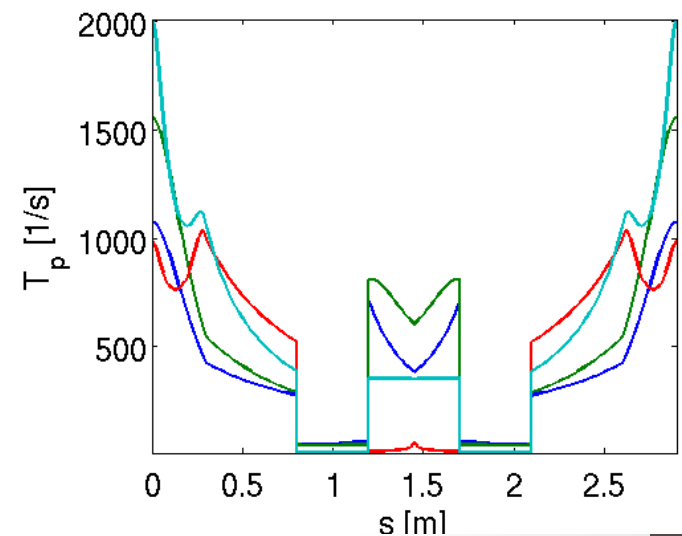


Large detuning factor and small hor. and vert. phase advances for small chromaticity

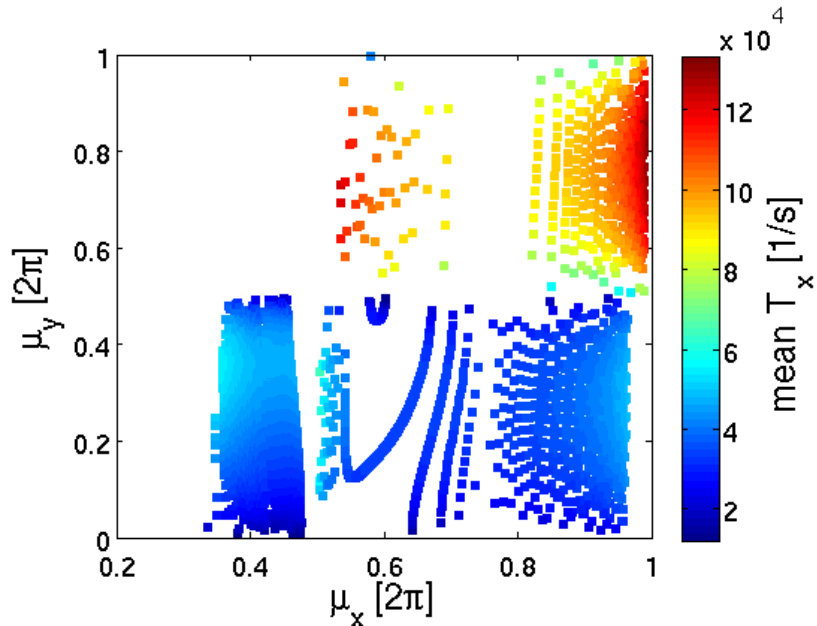
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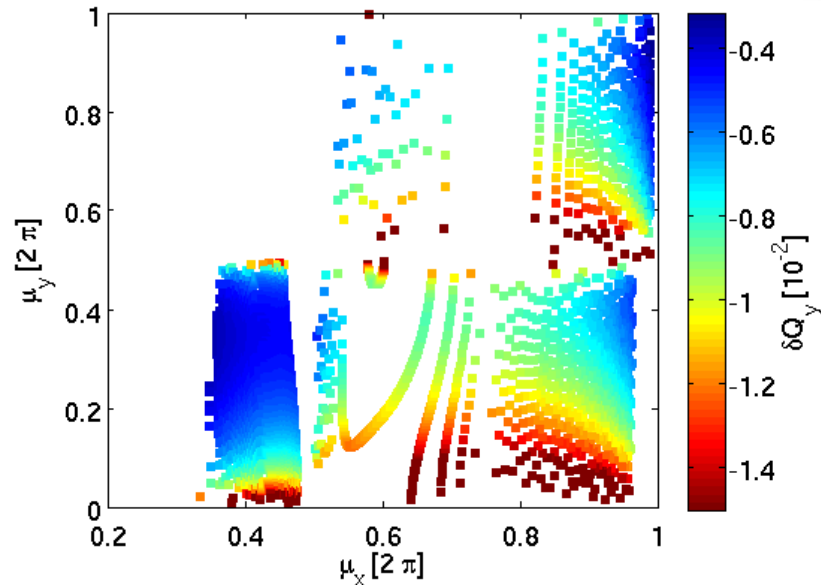
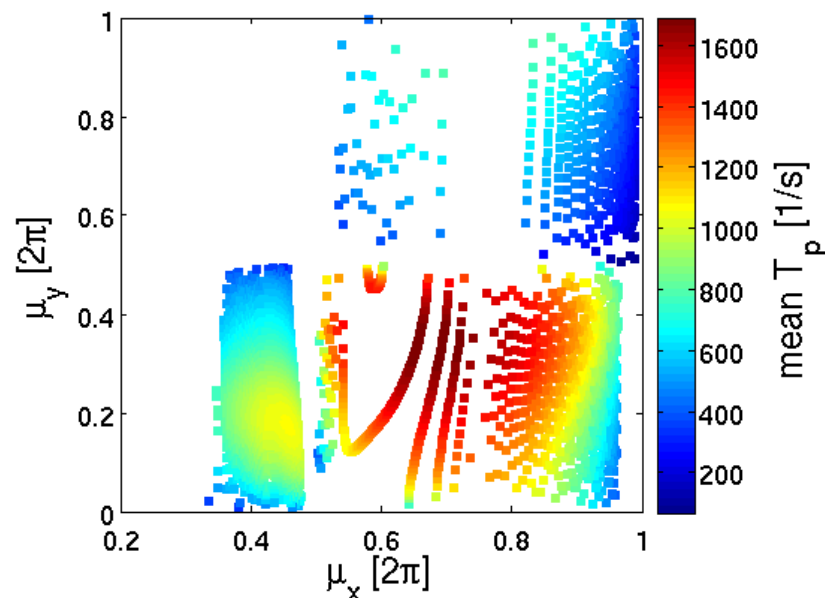
- For the same detuning factor (here DF=6) different optics options (top plots)
- The corresponding horizontal and longitudinal growth rates along a TME cell (right plots)
- **Careful optics choice very important for the IBS optimization**



# TME optimization with respect to IBS



- Scanning on the detuning factor (here DF=1..25), optimal phase advances can be found where chromaticity, IBS growth rates and space charge detuning are minimized
- Other interesting regions according to the requirements of the design also exist



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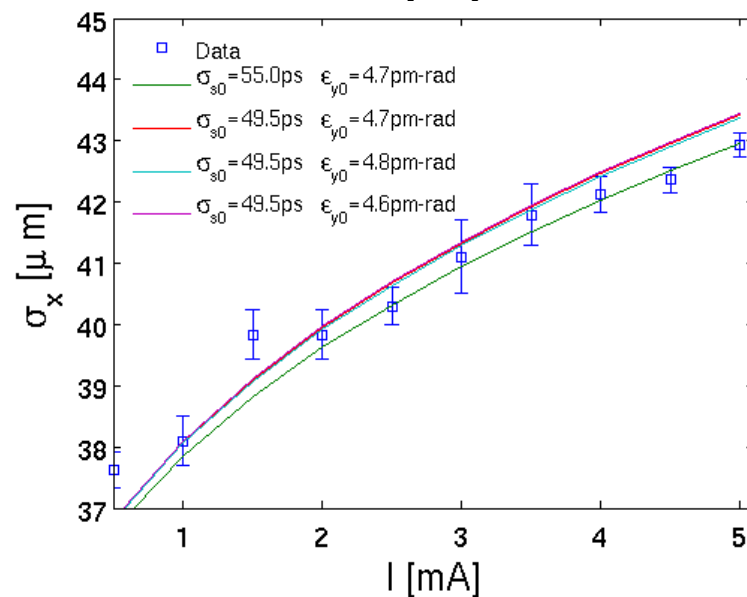
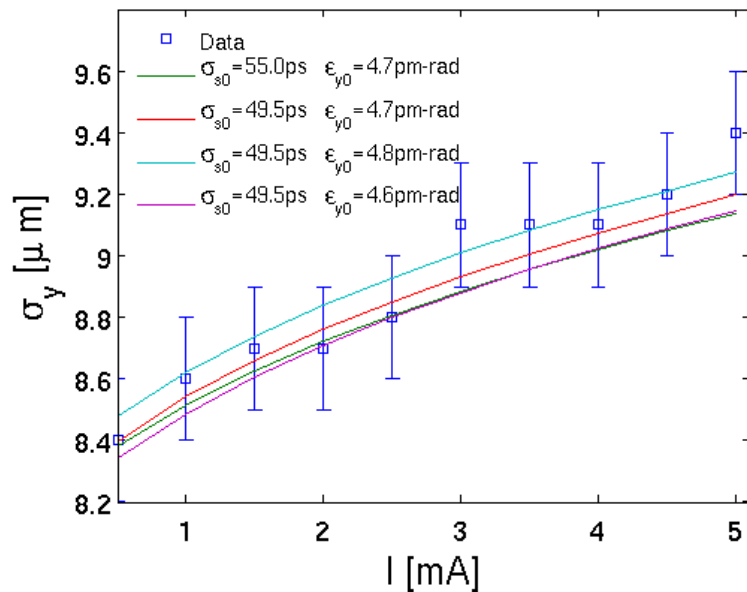
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- **Performance parameters** of the CLIC DR for the **1 GHz** and **2 GHz** options and for an intermediate design (**V06**)

- Increased energy (2.424 → 2.86 GeV)
- Ultra-low emittances in all 3 planes
- Reduced IBS effect (from 3 to 1.5)
- Reduced space charge tune shift (-0.2 → -0.1)
- Lower RF stable phase (70° → 51° (62°))

- ✓ **Fullfills the requirements of the design**
- ✓ **Included in the CLIC CDR**

# IBS measurements at the SLS



- Beam size measurements with the **vis-UV** (v) and the **pinhole** (h) cameras.
- **Multi-bunch** measurements with always same total current (Optimum performance of the pinhole camera for  $I_{\text{tot}} > 60$  mA)
- Longitudinal phase space dominated by the **3<sup>rd</sup> harmonic cavity** (due to high current)
  - Non-Gaussian bunch length profiles
- Comparison with **CIMP** predictions
- Different assumptions for the zero current energy spread and vertical emittance
- **Agreement** in the **transverse** plane
- Information from the **longitudinal** plane is **missing**
  - Non-gaussian bunch length profiles
  - Unknown energy spread model (under development)



# Summary

- Intrabeam scattering is the main limitation to the ultralow emittance of the CLIC DR
  - The effect is well understood for the core particles or if the effect is a perturbation (of the order of a few percent)
  - We don't know what is the effect on the tails and in the ultra-high brightness regime
- Tools used to study the effect
  - Theoretical models (Bjorken-Mtingwa, Piwinski, Bane, CIMP, etc)
  - Multiparticle tracking codes (SIRE, CMAD-IBStrack → both frozen)
- Tools' drawbacks
  - Always assume Gaussian beam distributions
  - Impact on the damping process is not known
  - Inclusion of coupling not trivial
  - The interaction between IBS and spin is not known
    - Important for the Damping Rings where the beam stays in the ring for a very short amount of time
- Benchmarking of theoretical models and tracking codes
  - All agree very well at weak IBS regimes (the effect on the final steady state emittance not very strong)
  - Divergence grows as the IBS effect on the output emittance grows

# Summary

- Carefull optics design is important and can help on the minimization of the effect
  - The analytical approach was very helpful in our design
  - Can/Need to be extended to other type of low emittance cells
  - It is now extended to variable bends as well (see poster of S. Papadopoulou in the students' poster session)
- Benchmarking of all theoretical models and tracking codes with measurements is very important
  - At weak IBS regimes already good agreement between tools and measurements has been demonstrated (see for example results from CESR-TA, SLS)
  - We need to understand what is happening at strong IBS regimes (i.e. does the beam distribution remain Gaussian?)
  - A good knowledge of the machine model is important in order to disentangle IBS from other current dependent effects

Thank you!