

POWHEG NLO matching in Herwig++

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work in collaboration with Peter Richardson and Keith Hamilton



NLO matching in parton showers

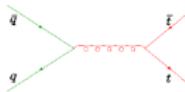
Parton showers
NLO matching

The POWHEG method

Herwig++ implementation
Shower infra-structure

Results

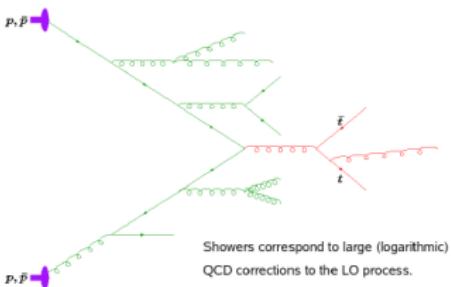
- ▶ Monte Carlo event generators are crucial tools for planning and analysis of experiments



Generally a leading order QCD,
EW (or BSM) calculation.

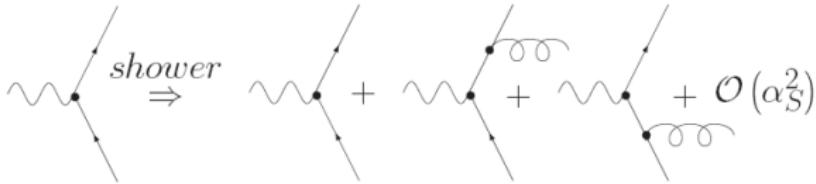
- ▶ leading order n body configuration generated
- ▶ external legs undergo Sudakov evolution down to hadronization scale
- ▶ hadronization and decay models applied
- ▶ corresponds to summing collinear and soft leading logarithm terms to all orders
- ▶ underestimates hard radiation - match to exact higher order terms - ME Corrections [1], CKKW[2] etc

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- ▶ **NLO matching** combines features of parton shower and NLO
 - ▶ inclusive observables in agreement with NLO
 - ▶ LL accuracy of shower retained
- ▶ naive MC+NLO:
 - ▶ NLO generator (eg MCFM) generates n and $n + 1$ body events
 - ▶ attach events to parton shower
- ▶ this approach would result in **double counting**

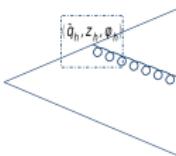


- ▶ MC@NLO [3] scheme available for many processes
 - ▶ subtracts shower emission weights from NLO
 - ▶ not positive definite

- ▶ POWHEG [4] method of Nason is an alternate scheme
 - ▶ produces only positive weight events
 - ▶ requires modification of the shower (truncated and vetoed showers)
- ▶ POWHEG has been implemented for a few processes but with no or approximated truncated shower
- ▶ KH, PR, JT implemented within Herwig++ with full truncated shower for processes
 - ▶ $e + e^-$ annihilation to hadrons.
 - ▶ Drell-Yan vector boson production.
- ▶ POWHEG method contains two steps:
 1. reorganisation of the angular ordered shower

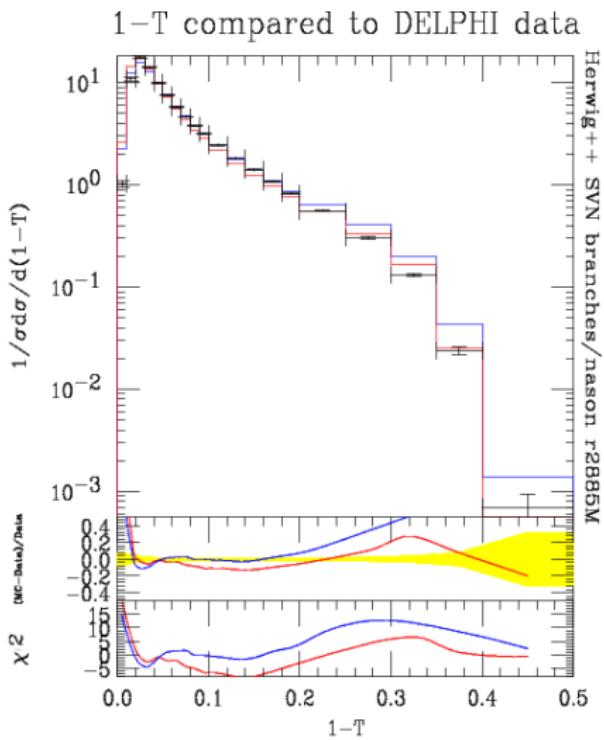
shower = hardest + truncated + vetoed
 2. generation of hardest emission with modified Sudakov Form Factor

- ▶ Produce full POWHEG shower as a single Herwig++ shower with conditions applied
 1. hardest emission generated
 2. $n + 1$ body configuration $\rightarrow n$ body configuration with shower emission $(\tilde{q}_h, z_h, \phi_h)$

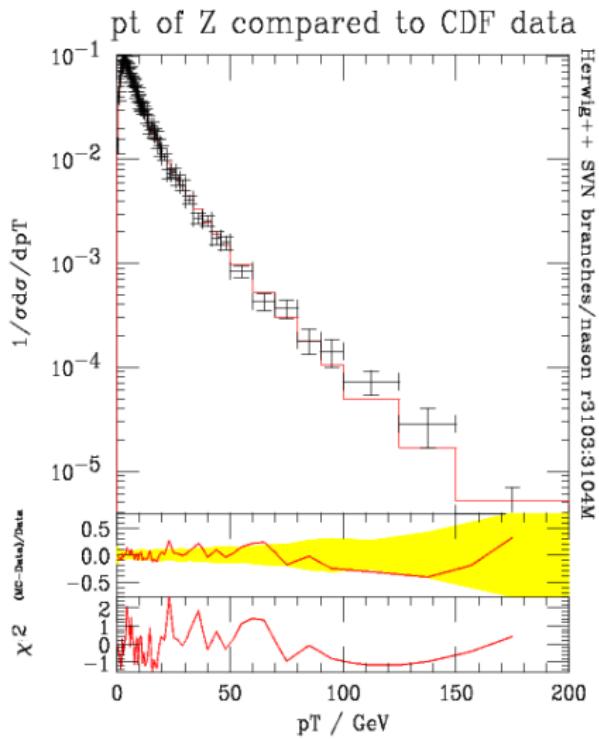


3. truncated shower evolves down to hardest emission scale \tilde{q}_h
 - ▶ $p_T < p_{T_h}$
 - ▶ $\tilde{q}z > \tilde{q}_h$
 - ▶ non flavour changing emission
4. hardest emission is forced with emission variables $(\tilde{q}_h, z_h, \phi_h)$
5. shower evolves down to hadronization scale with veto at p_{T_h}

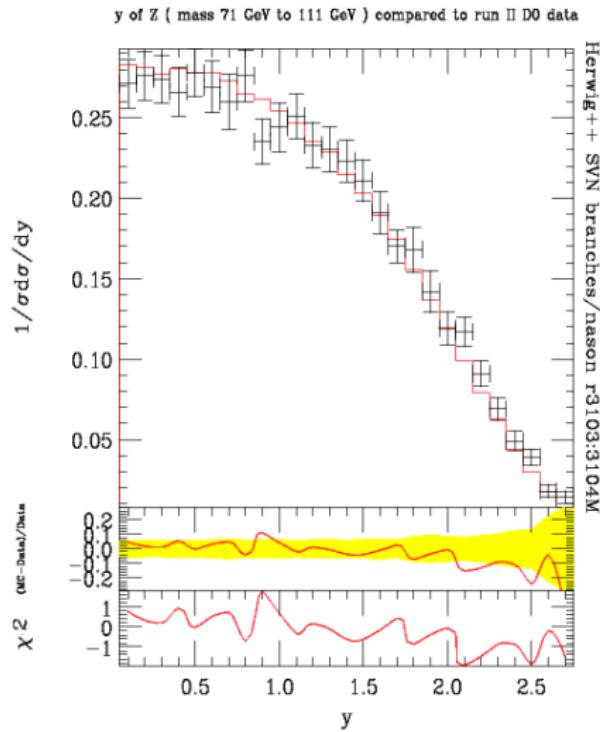
e + e- plots with DELPHI LEP [5] data: Thrust



Drell Yan plots with CDF run I data [6] : Z p_T



Drell Yan plots with D0 run II data [7] : Z rapidity



Summary and outlook

- ▶ POWHEG is a positive weight NLO matching scheme
- ▶ method fully implemented in Herwig++ for
 - ▶ $e + e^-$ annihilation to hadrons
 - ▶ Drell Yan vector boson production
- ▶ reasonable agreement found with data, similar to ME corrections. Paper soon.
- ▶ infra-structure in place to allow for straight forward implementation of other processes
 - ▶ $gg \rightarrow H$

- ▶ General QCD NLO cross section may be written

$$d\sigma = \bar{B}(v) dv [\Delta_R^{(NLO)}(0) + \Delta_R^{(NLO)}(p_T) \frac{R(v, r)}{B(v)} dr] \quad (1)$$

- ▶ with modified Sudakov Form Factor

$$\Delta_R^{(NLO)}(p_T) = \exp - \int dv dr \frac{R(v, r)}{B(v)} \Theta(k_T(v, r) - p_T) \quad (2)$$

$$\bar{B}(v) = B(v) + V(v) + \int (R(v, r) - C(v, r)) dr \quad (3)$$

- ▶ monte carlo interpretation

1. generate n body configurations (v) according to \bar{B}
2. generate radiative $n+1$ configurations according to

$$\Delta_R^{(NLO)}(p_T) \frac{R(v, r)}{B(v)}$$

- ▶ positive weights only

- ▶ Ingredients for $e + e^-$ hardest emission generation:



- ▶ radiative corrections
- ▶ p_T chosen as one of the radiative variables leading to a simple implementation of $\Theta(k_T - pT)$
- ▶ modified splitting function given by:

$$\frac{R(v, r)}{B(v)} dr = \frac{C_F \alpha_S}{\pi} \frac{x_1^2(p_T, y) + x_2^2(p_T, y)}{(1 - x_1(p_T, y))(1 - x_2(p_T, y))} \frac{p_T}{s} dp_T dy \quad (4)$$

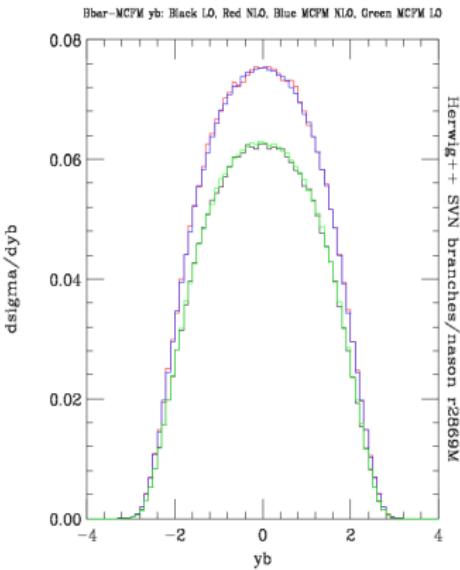
- ▶ \bar{B} in this case is just integrated cross section

$$\bar{B} = \sigma_{LO} \left(1 + \frac{\alpha_S}{\pi} \right) \quad (5)$$

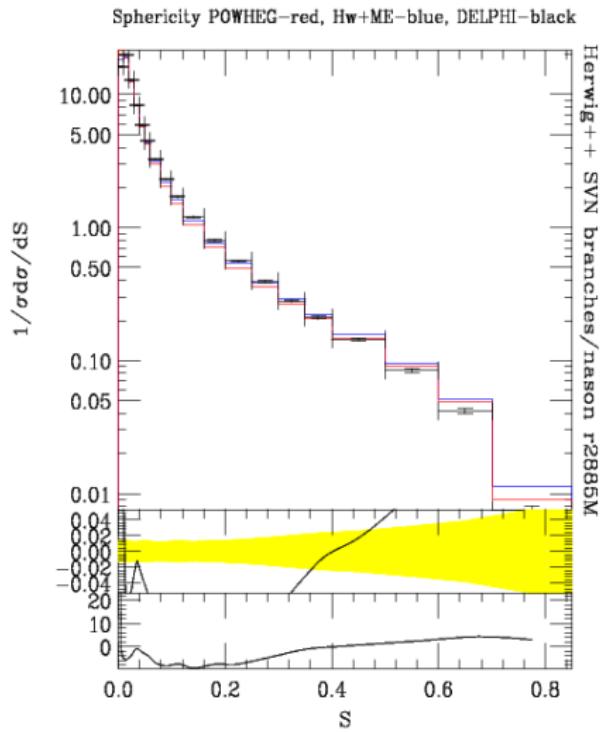
Drell Yan hard generator

- ▶ three partonic processes in real corrections
 - ▶ $q\bar{q} \rightarrow gV$, $qg \rightarrow qV$, $g\bar{q} \rightarrow \bar{q}V$
- ▶ \bar{B} requires full NLO calculation differential in y_B

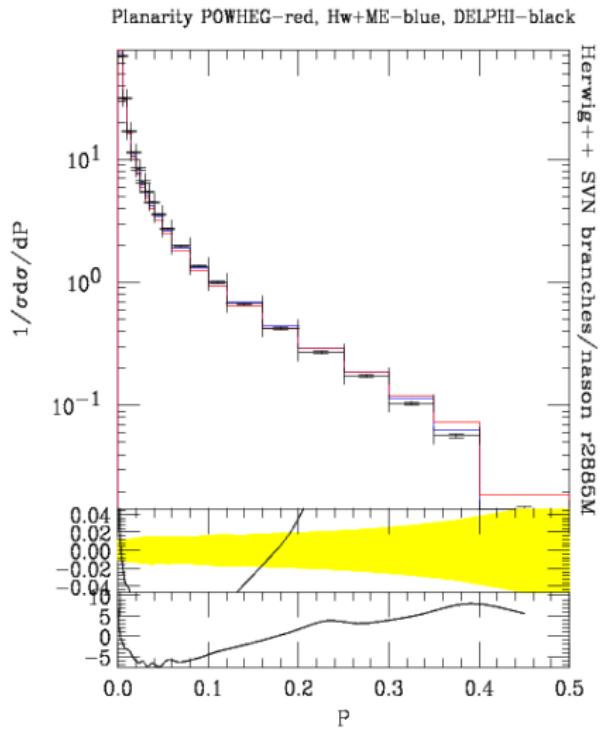
- ▶ calculation performed in CALKUL [10] gauge
 - ▶ born factorised result
 - ▶ implemented as reweighting of LO ME
- ▶ \bar{B} and MCFM agree to 0.5%



e + e- plots with DELPHI LEP [5] data: Sphericity



e + e- plots with DELPHI LEP [5] data: Planarity



-  M. H. Seymour, "Matrix Element Corrections To Parton Shower Algorithms," *Comput. Phys. Commun.* **90**, 95 (1995) [[arXiv:hep-ph/9410414](https://arxiv.org/abs/hep-ph/9410414)].
-  S. Catani, F. Krauss, R. Kuhn and B. R. Webber, "QCD matrix elements + parton showers," *JHEP* **0111**, 063 (2001) [[arXiv:hep-ph/0109231](https://arxiv.org/abs/hep-ph/0109231)].
-  S. Frixione and B. R. Webber, "Matching NLO QCD computations and parton shower simulations," *JHEP* **0206**, 029 (2002) [[arXiv:hep-ph/0204244](https://arxiv.org/abs/hep-ph/0204244)].
-  P. Nason, "A new method for combining NLO QCD with shower Monte Carlo algorithms," *JHEP* **0411**, 040 (2004) [[arXiv:hep-ph/0409146](https://arxiv.org/abs/hep-ph/0409146)].

-  P. Abreu *et al.* [DELPHI Collaboration], “Tuning and test of fragmentation models based on identified particles and Z . Phys. C **73**, 11 (1996).
-  A. A. Affolder *et al.* [CDF Collaboration], Phys. Rev. Lett. **84**, 845 (2000) [[arXiv:hep-ex/0001021](https://arxiv.org/abs/hep-ex/0001021)].
-  V. M. Abazov *et al.* [D0 Collaboration], Phys. Rev. D **76**, 012003 (2007) [[arXiv:hep-ex/0702025](https://arxiv.org/abs/hep-ex/0702025)].
-  P. Nason and G. Ridolfi, “A positive-weight next-to-leading-order Monte Carlo for Z pair hadroproduction,” JHEP **0608**, 077 (2006) [[arXiv:hep-ph/0606275](https://arxiv.org/abs/hep-ph/0606275)].
-  O. Latunde-Dada, S. Gieseke and B. Webber, “A positive-weight next-to-leading-order Monte Carlo for $e^+ e^-$ annihilation to hadrons,” JHEP **0702**, 051 (2007) [[arXiv:hep-ph/0612281](https://arxiv.org/abs/hep-ph/0612281)].

-  P. De Causmaecker, R. Gastmans, W. Troost and T. T. Wu,
"Multiple Bremsstrahlung In Gauge Theories At High-Energies.
1. General Formalism For Quantum Electrodynamics," Nucl.
Phys. B **206**, 53 (1982).
-  S. Frixione, P. Nason and G. Ridolfi, "A Positive-Weight
Next-to-Leading-Order Monte Carlo for Heavy Flavour
Hadroproduction," JHEP **0709**, 126 (2007) [arXiv:0707.3088
[hep-ph]].