

“Sapienza” Università di Roma – INFN sez. Roma 1

# Production of tetraquarks at the LHC

A. Pilloni

10<sup>th</sup> Quarkonium Working Group, CERN – November 14<sup>th</sup>, 2014

in coll. w/ A. Guerrieri, F. Piccinini, A.D. Polosa

Phys.Rev. D90, 034003 – arXiv:1405.7929

---

# Outline

- Production of X(3872)
- A new mechanism?
- X(3872) vs. Deuteron production
- Hadronization and Feshbach mechanism
- Conclusions

# Prompt production of $X(3872)$

$X(3872)$  is the Queen of exotic resonances, the most popular interpretation is a  $D^0\bar{D}^{0*}$  molecule (bound state, pole in the 1<sup>st</sup> Riemann sheet?)

We aim to evaluate prompt production cross section at hadron colliders via Monte-Carlo simulations

**Q.** What is a molecule in MC? **A.** «Coalescence» model



$$\sigma(p\bar{p} \rightarrow X(3872)) \sim \int d^3k |\langle X | D\bar{D}^* \rangle \langle D\bar{D}^* | p\bar{p} \rangle|^2 < \int_{k < k_{max}} d^3k |\langle D\bar{D}^* | p\bar{p} \rangle|^2$$

This should provide an upper bound for the cross section

# Estimating $k_{max}$

The binding energy is  $E_B \approx -0.16 \pm 0.31$  MeV: **very small!**

In a simple square well model this corresponds to:

$$\sqrt{\langle k^2 \rangle} \approx 50 \text{ MeV}, \sqrt{\langle r^2 \rangle} \approx 10 \text{ fm}$$

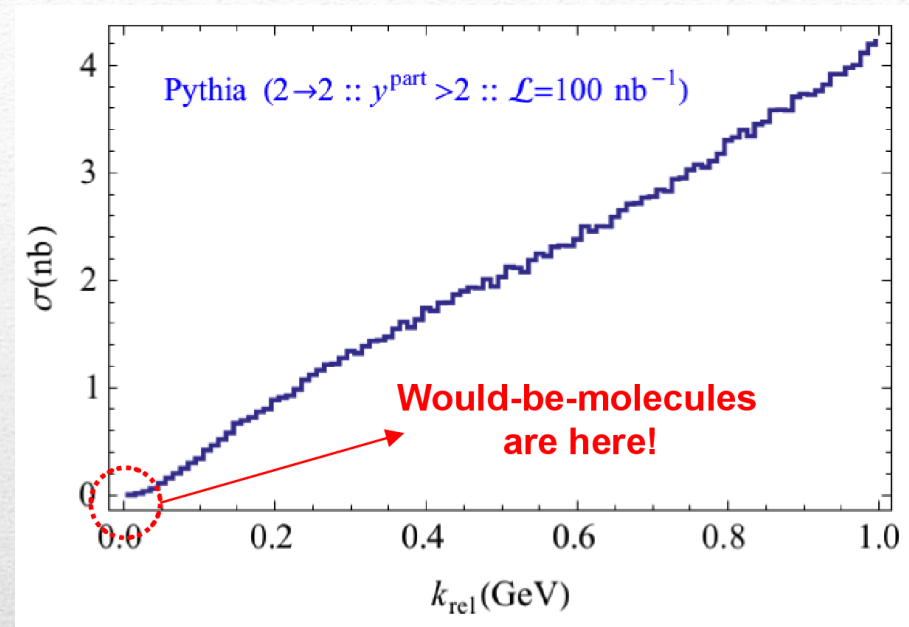
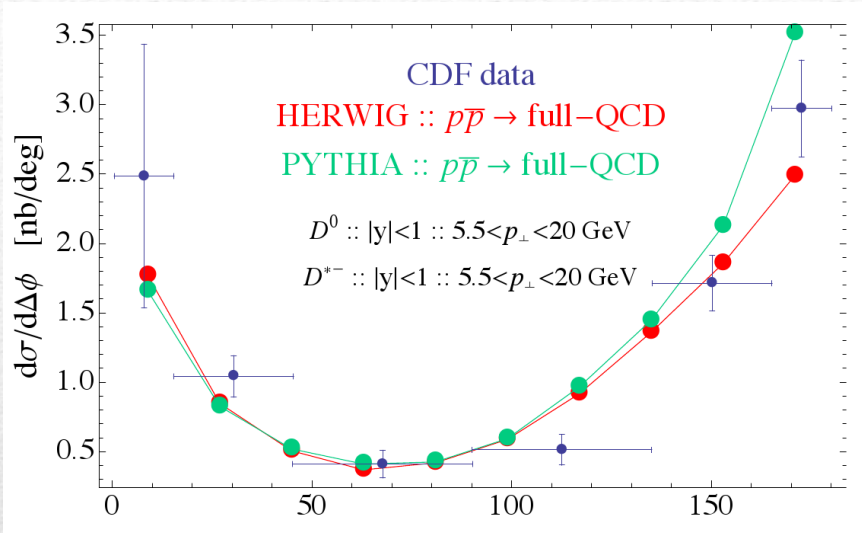
$$\left( \begin{array}{l} \text{binding energy reported in Kamal Seth's talk is } E_B \approx -0.013 \pm 0.192 \text{ MeV:} \\ \sqrt{\langle k^2 \rangle} \approx 30 \text{ MeV}, \sqrt{\langle r^2 \rangle} \approx 30 \text{ fm} \end{array} \right)$$

to compare with deuteron:  $E_B = -2.2$  MeV

$$\sqrt{\langle k^2 \rangle} \approx 80 \text{ MeV}, \sqrt{\langle r^2 \rangle} \approx 4 \text{ fm}$$

We assume  $k_{max} \sim \sqrt{\langle k^2 \rangle} \approx 50$  MeV, some other choices are commented later

# 2009 results

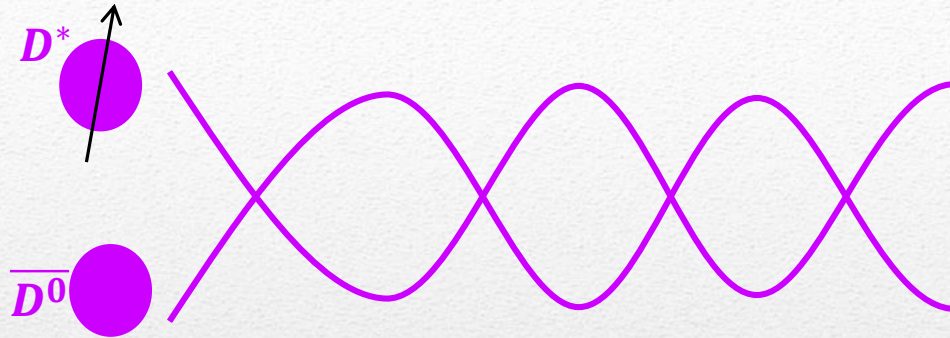


We tune our MC to reproduce CDF distribution of  $\frac{d\sigma}{d\Delta\phi} (p\bar{p} \rightarrow D^0 D^{*-})$

We get  $\sigma(p\bar{p} \rightarrow DD^* | k < k_{max}) \approx 0.1 \text{ nb}$  @  $\sqrt{s} = 1.96 \text{ TeV}$

Experimentally  $\sigma(p\bar{p} \rightarrow X(3872)) \approx 30 - 70 \text{ nb}!!!$

# Estimating $k_{max}$ (again)

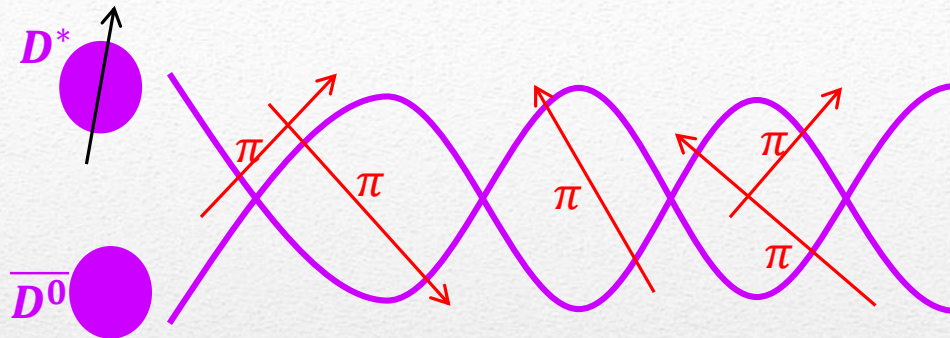


A solution can be FSI (rescattering of  $DD^*$ ), which allow  $k_{max}$  to be as large as  $5m_\pi \sim 700$  MeV

$$\sigma(p\bar{p} \rightarrow DD^* | k < k_{max}) \approx 230 \text{ nb} > \sigma_{exp}(p\bar{p} \rightarrow X(3872))$$

Artoisenet and Braaten PRD81 (2010) 114018

# Estimating $k_{max}$ (again)



A solution can be FSI (rescattering of  $DD^*$ ), which allow  $k_{max}$  to be as large as  $5m_\pi \sim 700$  MeV

$$\sigma(p\bar{p} \rightarrow DD^* | k < k_{max}) \approx 230 \text{ nb} > \sigma_{exp}(p\bar{p} \rightarrow X(3872))$$

Artoisenet and Braaten PRD81 (2010) 114018

However, the applicability of Watson theorem is challenged by the presence of pions that interfere with  $DD^*$  propagation

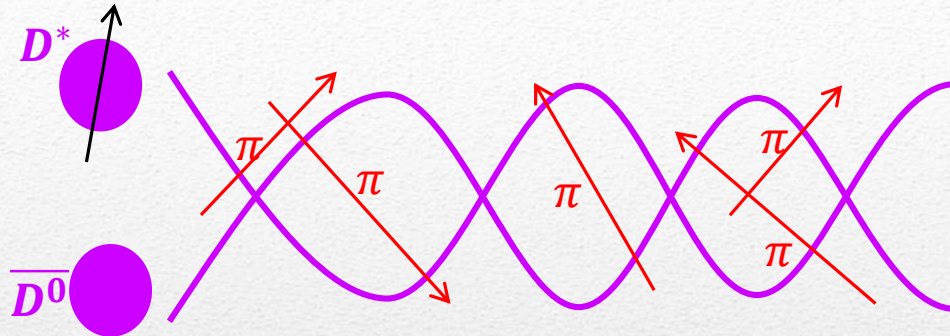
Bignamini, Grinstein, Piccinini, Polosa, Sabelli PLB684 (2010) 228-230

FSI saturate unitarity bound? Influence of pions small?

Artoisenet and Braaten PRD83 (2011) 014019

---

# Estimating $k_{max}$ (again)



A solution can be FSI (rescattering of  $DD^*$ ) which allow  $k$

Guo, Meissner, Wang, Yang, JHEP 1405, 138; EPJC74 9, 3063;  
CTP 61 354

use  $E_{max} = M_X + \Gamma_X$  for above-threshold unstable states

(2010) 114018

Howe

With different choices, 2 orders of magnitude uncertainty,  
limits on predictive power

e of

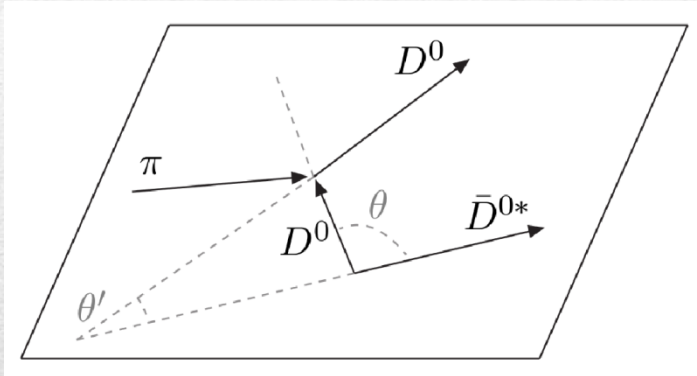
FSI saturate unitarity bound? Influence of pions small?

Artoisenet and Braaten PRD83 (2011) 014019



# A new mechanism?

In a more **billiard-like** point of view, the comoving pions can **elastically interact** with  $D(D^*)$ , and **slow down** the pairs  $DD^*$



Esposito, Piccinini, AP, Polosa JMP 4, 1569

The mechanism also implies:  $D$  mesons actually **“pushed”** inside the potential well (the **classical 3-body problem!**)

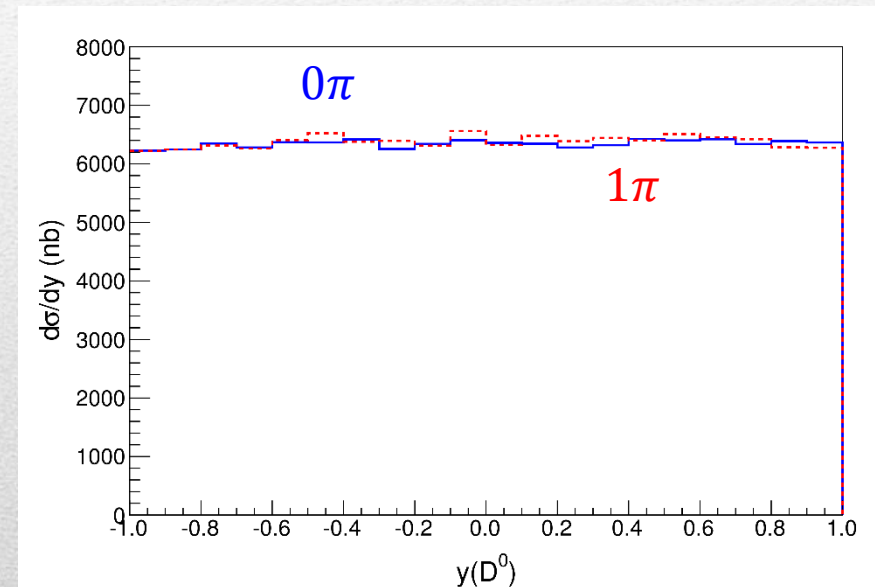
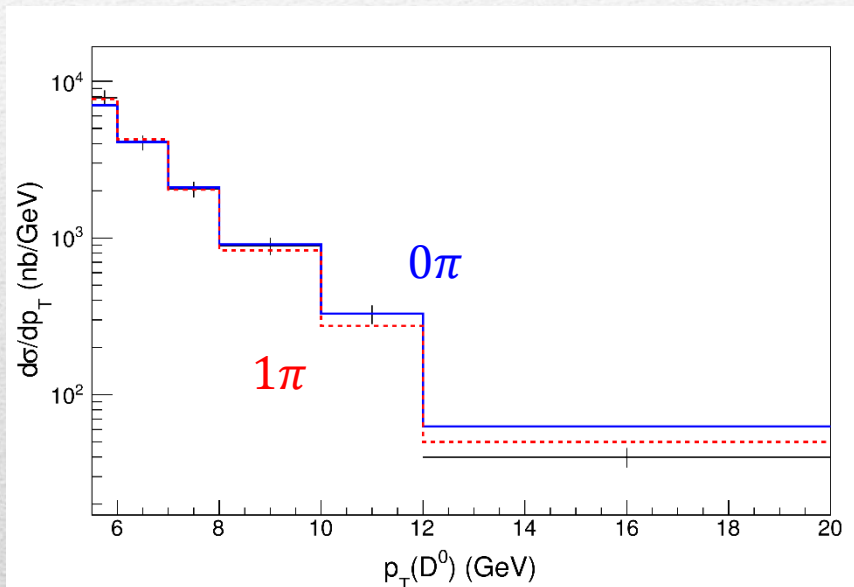
$X(3872)$  is a **real, negative energy bound state** (stable)

It also explains a small width  $\Gamma_X \sim \Gamma_{D^*} \sim 100$  keV

# Tuning pions

This picture could spoil existing meson distributions used to tune MC  
We verify this is not the case up to an overall  $K$  factor

Guerrieri, Piccinini, AP, Polosa, PRD90, 034003

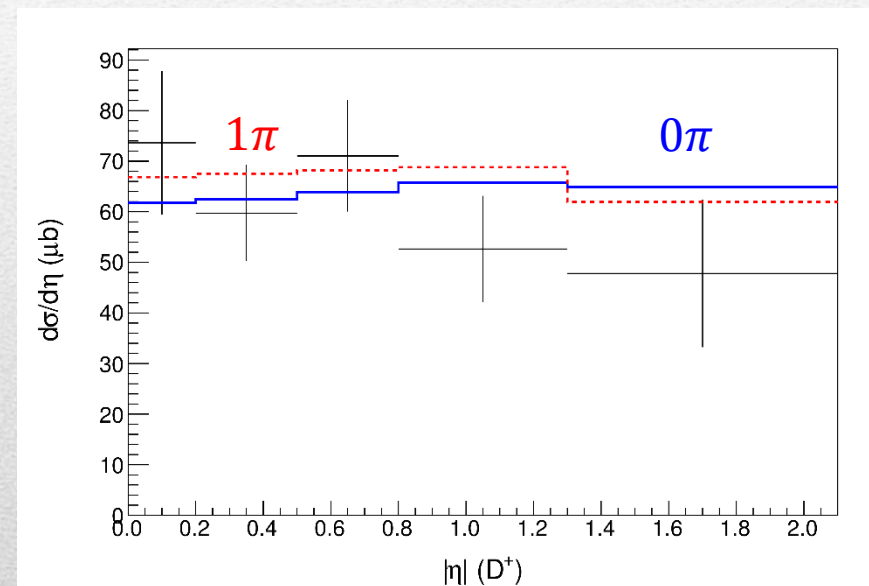
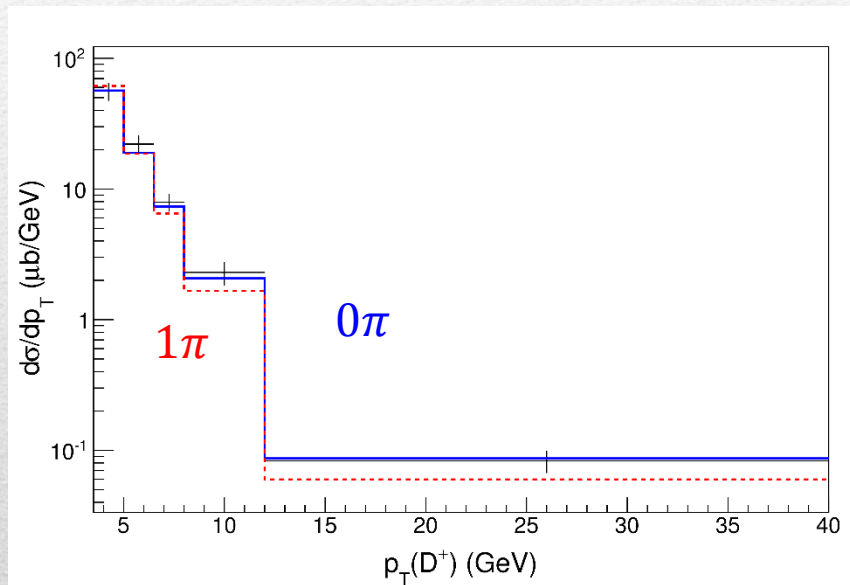


Neither at CDF...

# Tuning pions

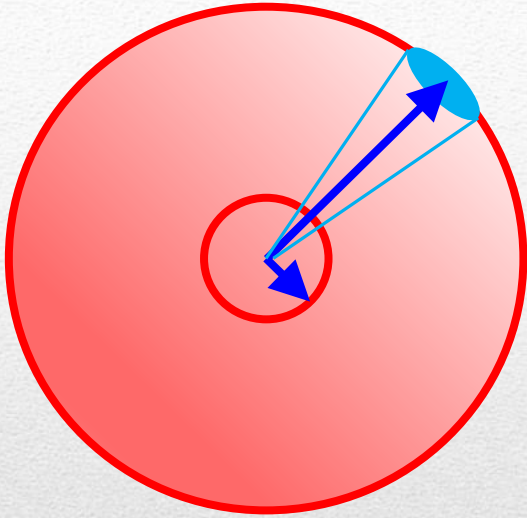
This picture could spoil existing meson distributions used to tune MC  
We verify this is not the case up to an overall  $K$  factor

Guerrieri, Piccinini, AP, Polosa, PRD90, 034003

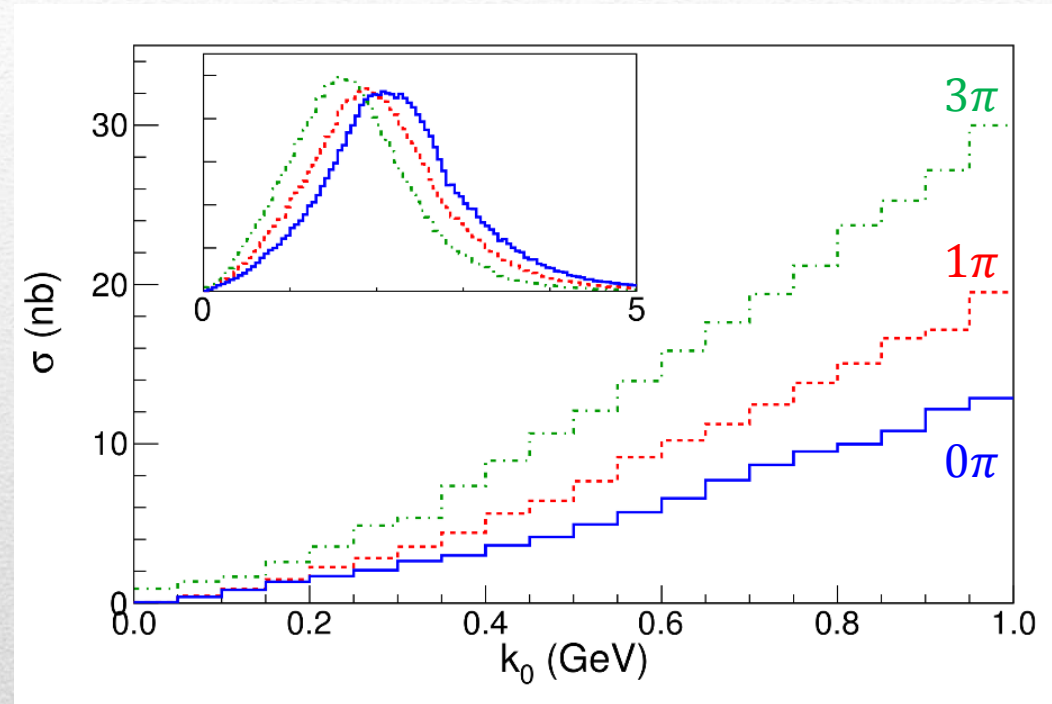


...nor at ATLAS

# Results



By comparing hadronization times of heavy and light mesons, we estimate up to  $\sim 3$  collisions can occur before the heavy pair to fly apart



We get  $\sigma(p\bar{p} \rightarrow X(3872)) \sim 5$  nb,  
**still not sufficient** to explain all the experimental cross section

# $X(3872) \sim$ Deuteron?

Guerrieri, Piccinini, AP, Polosa, PRD90, 034003

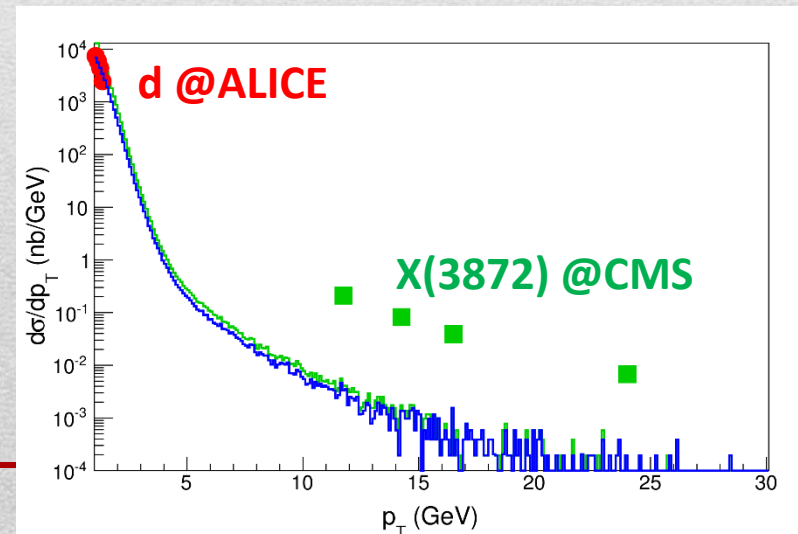
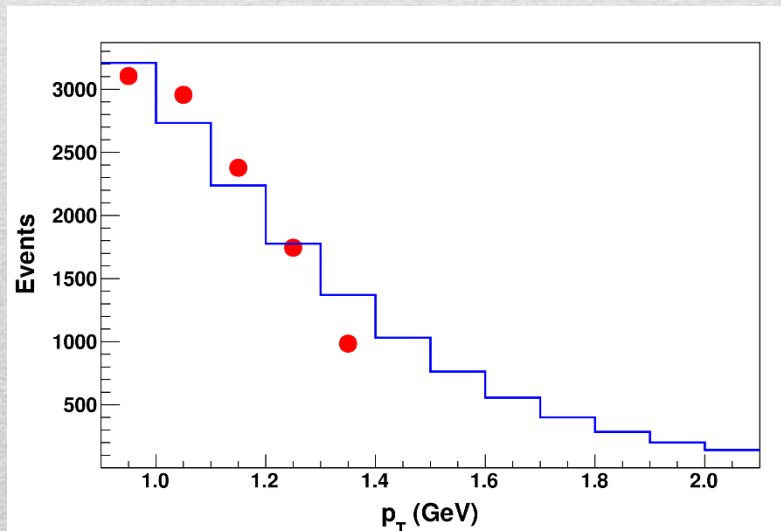
If  $X(3872)$  is a deuteron-like molecule, we can compare production cross sections

We use antideuteron ALICE data and use MC simulations to extrapolate at high  $p_T$

Since  $p_{Tmin} \sim 1$  GeV, total cross section is exploding, we cannot normalize data we choose a  $K$  factor to fit data: *no dependence on  $k_{max}$*

**3 orders of magnitude smaller** than CMS  $X(3872)$  data!

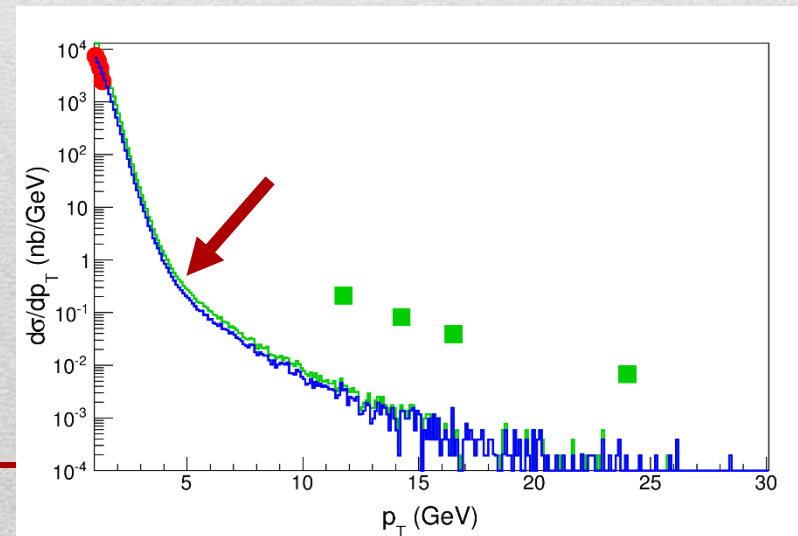
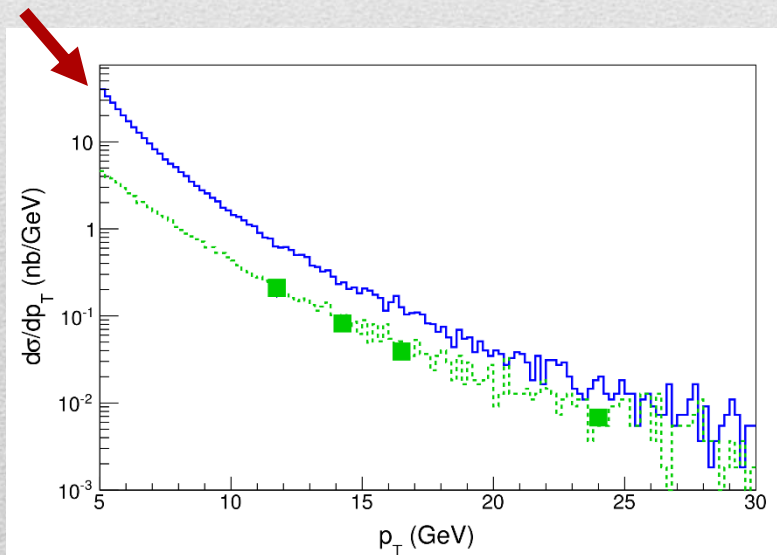
Are they similar objects?



# $X(3872) \sim$ Deuteron?

Guerrieri, Piccinini, AP, Polosa, PRD90, 034003

We can go backwards by normalizing to CMS  $X(3872)$  data prediction for antideuteron is **much larger** than previous one



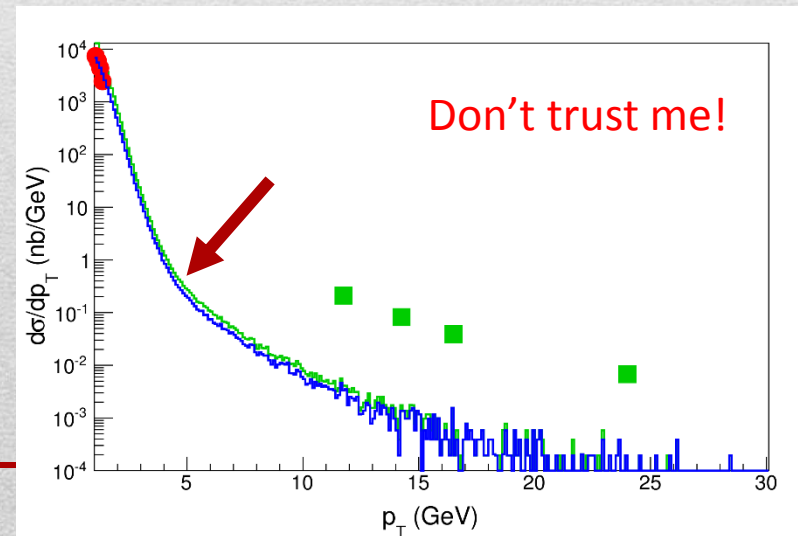
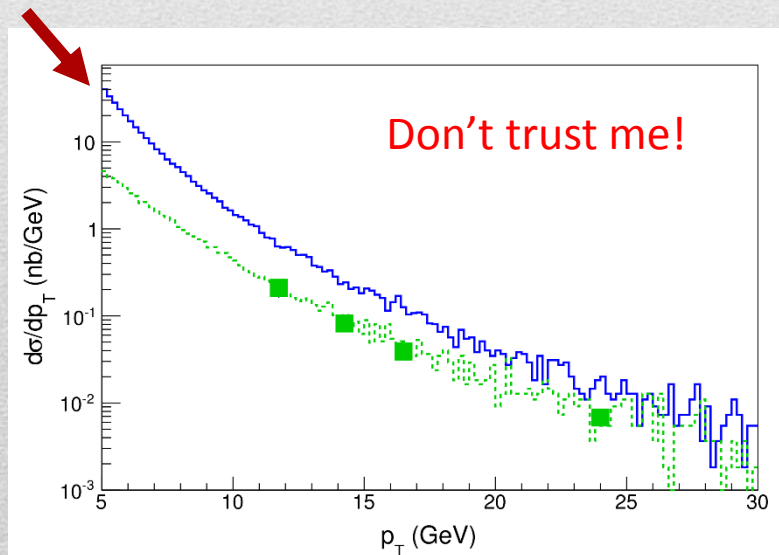
# $X(3872) \sim$ Deuteron?

Guerrieri, Piccinini, AP, Polosa, PRD90, 034003

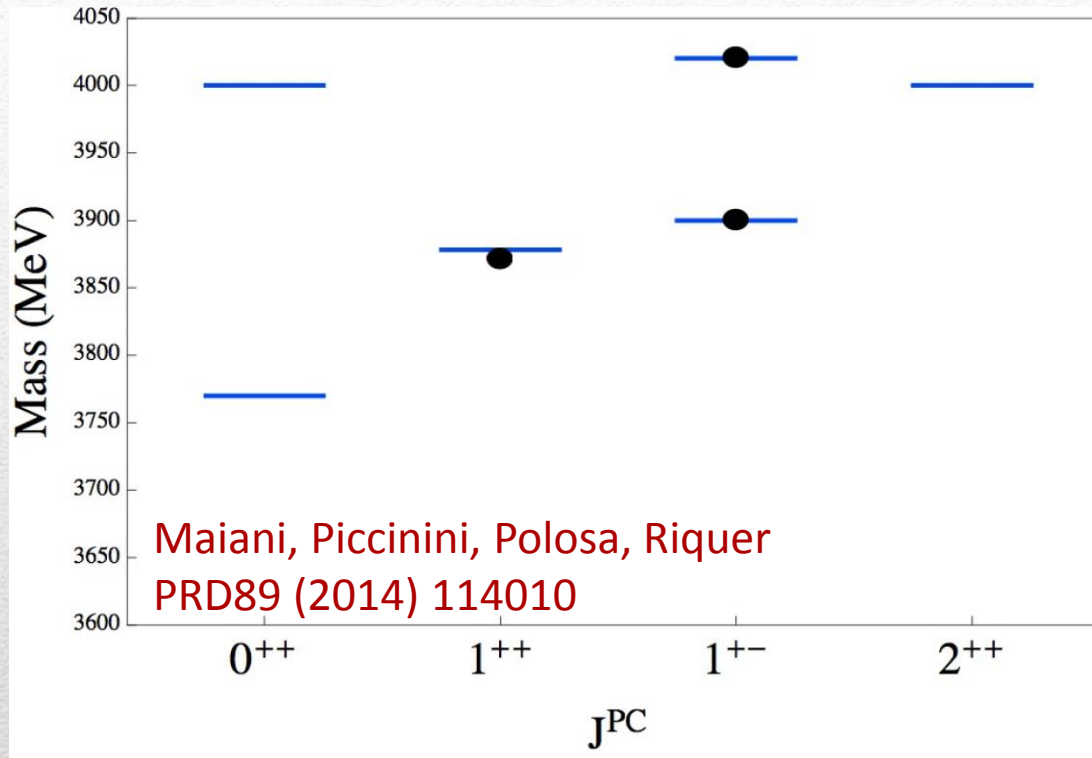
We can go backwards by normalizing to CMS  $X(3872)$  data prediction for antideuteron is **much larger** than previous one

Do not trust MC!  
We want data!!!

ALICE data are preliminary  
MC is not reliable in the  $p_T \sim 1$  GeV  
Dependence on hadronization models  
Different fragmentation functions to be considered



# Tetraquark



The pattern of  $X(3872)$ ,  $Z_c(3900)$ ,  $Z_c'(4020)$ , is understood

Prediction for radial excitation  $Z(4430)$  ✓

A full nonet for each level is expected ✗

We need a mechanism that disfavors the formation of the unobserved states



# Feshbach resonances

Braaten and Kusunoki, PRD69, 074005

Papinutto, Piccinini, AP, Polosa, Tantalò arXiv:1311.7374

Guerrieri, Piccinini, AP, Polosa, PRD90, 034003

In cold atoms there is a mechanism that occurs when two atoms can interact with **two potentials**, resp. with **continuum** and **discrete** spectrum

Meson-meson (molecule) potential

$$H_P \psi_P = E_P \psi_P$$

(continuum levels)

Open charm  
threshold

*e.g. DD\**

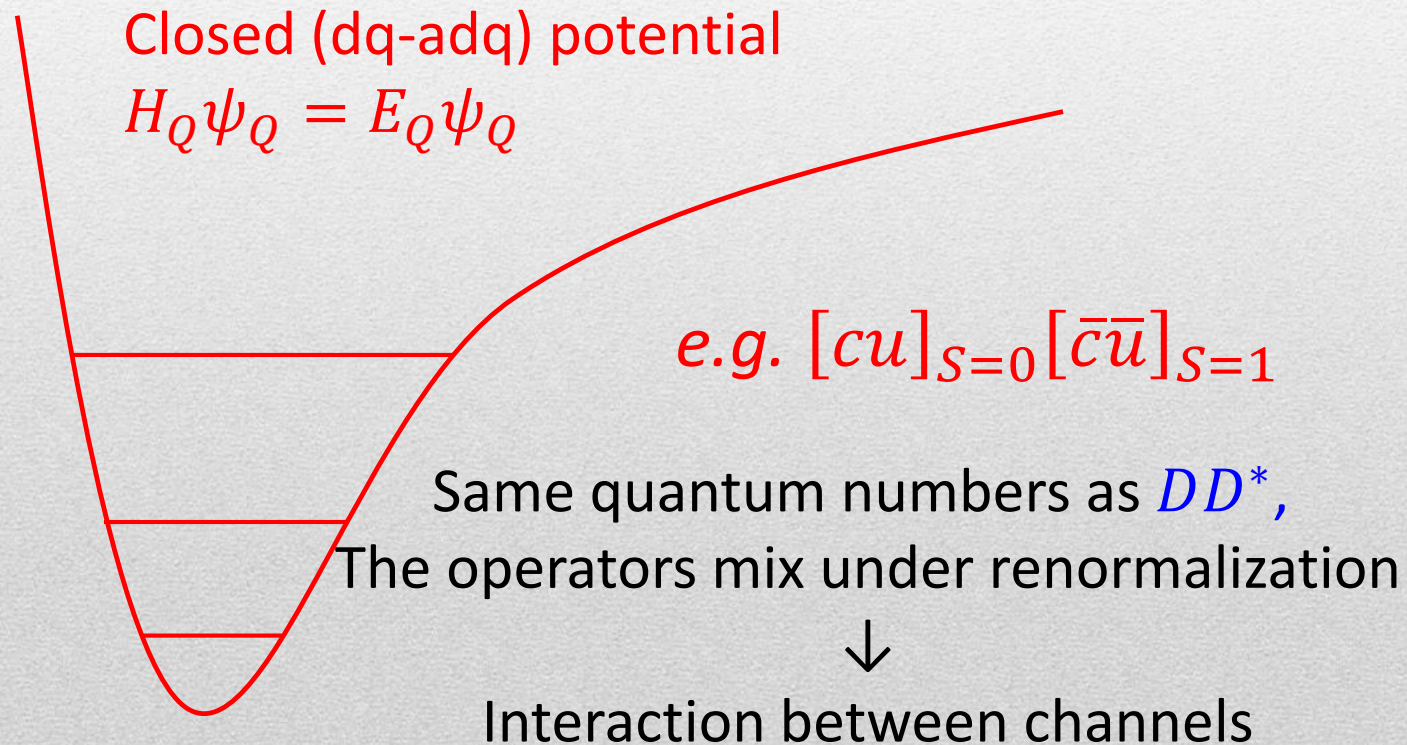
# Feshbach resonances

Braaten and Kusunoki, PRD69, 074005

Papinutto, Piccinini, AP, Polosa, Tantalò arXiv:1311.7374

Guerrieri, Piccinini, AP, Polosa, PRD90, 034003

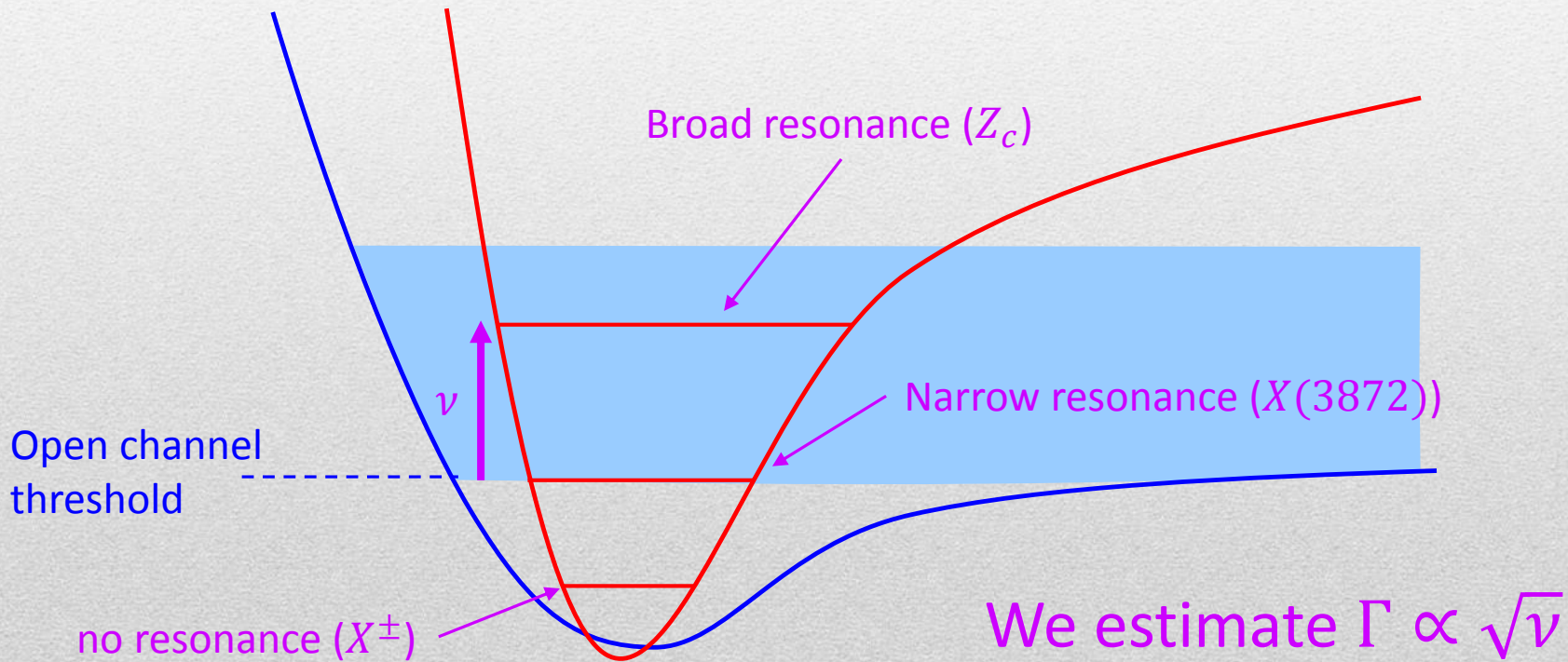
In cold atoms there is a mechanism that occurs when two atoms can interact with **two potentials**, resp. with **continuum** and **discrete** spectrum



# Feshbach resonances

We add an interaction Hamiltonian  $H_{QP}$  so that

$$a \simeq a_P + C \sum \frac{|\langle \psi_i | H_{QP} | \psi_{th} \rangle|^2}{E_{th} - E_i} \simeq a_{NR} - C \frac{|\langle \psi_{res} | H_{QP} | \psi_{th} \rangle|^2}{\nu}$$



# Feshbach resonances

We impose a cutoff on  $\nu < 100$  MeV

$X(3872)$  should be a  $I = 0$  state, but  $M(1^{++}) < M(D^{*+}D^-)$

**No charged component, isospin violation!**

If we assume  $\Gamma = A\sqrt{\nu}$ , we can use  $Z_c(3900)$  as input to extract  $A = 10 \pm 5$  MeV<sup>1/2</sup>

This value is **compatible for all resonances** (**caveat**: still large errors...)

Open channel	$M_{4q}$ (MeV)	$\nu$ (MeV)	$\Gamma$ (MeV)	$I^G J^{PC}$	name
$D^{*0}\bar{D}^0$	3872	0	0	$1^- 1^{++}$	$X(3872)$
$D^{*+}\bar{D}^0$	3900	24	53	$1^+ 1^{+-}$	$Z_c(3900)$
$D^{*+}\bar{D}^0$	4025	8	24	$1^+ 1^{+-}$	$Z'_c(4025)$
$\eta_c(2S)\rho^+$	4475	75	>150	$1^+ 1^{+-}$	$Z(4430)$
$B^{*+}\bar{B}^0$	10610	3	18	$1^+ 1^{+-}$	$Z_b(10610)$
$B^{*+}\bar{B}^{*0}$	10650	1.8	11	$1^+ 1^{+-}$	$Z'_b(10650)$

We remark that  $\Gamma(Z'_b)/\Gamma(Z_b) \approx 0.63$ ,  $\sqrt{\nu(Z'_b)/\nu(Z_b)} \approx 0.77$

# Production & Feshbach?

Going back to  $pp(\bar{p})$  collisions, we can imagine hadronization to produce a state

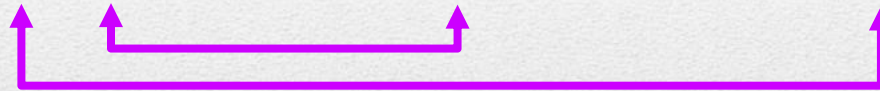
$$|\psi\rangle = \alpha|[qQ][\bar{q}\bar{Q}]\rangle_c + \beta|(\bar{q}q)(\bar{Q}Q)\rangle_o + \gamma|(\bar{q}Q)(\bar{Q}q)\rangle_o$$

If  $\beta, \gamma \gg \alpha$ , an initial tetraquark state is not likely to be produced  
The open channel mesons **fly apart** (see MC simulations)

# Production & Feshbach?

Going back to  $pp(\bar{p})$  collisions, we can imagine hadronization to produce a state

$$|\psi\rangle = \alpha|[qQ][\bar{q}\bar{Q}]\rangle_c + \beta|(\bar{q}q)(\bar{Q}Q)\rangle_o + \gamma|(\bar{q}Q)(\bar{Q}q)\rangle_o$$



If Feshbach mechanism is at work, an open state can resonate in a closed one

No prompt production without Feshbach resonances!

For example, we compare the at-threshold  $X(3872)$  with the below-threshold  $Y(4260)$   
 CMS  $X(3872)$  data: [JHEP 1304, 154](#)

$$\frac{\sigma(pp \rightarrow X(3872)) \times BR(X(3872) \rightarrow J/\psi \pi^+ \pi^-)}{\sigma(pp \rightarrow Y(4260)) \times BR(Y(4260) \rightarrow J/\psi \pi^+ \pi^-)} \sim 10^2$$

# Conclusions

The study of exotic resonances in heavy quark sector  
is still puzzling

- Measurement of **prompt production cross sections** could improve our understanding of hadronization
- Explore **new production mechanisms** having predictive power for at- and above-threshold states
- Feshbach mechanism could help in **reducing the number of states** predicted by tetraquark picture, and in **adding some interesting features** of molecular description

**Thank you**

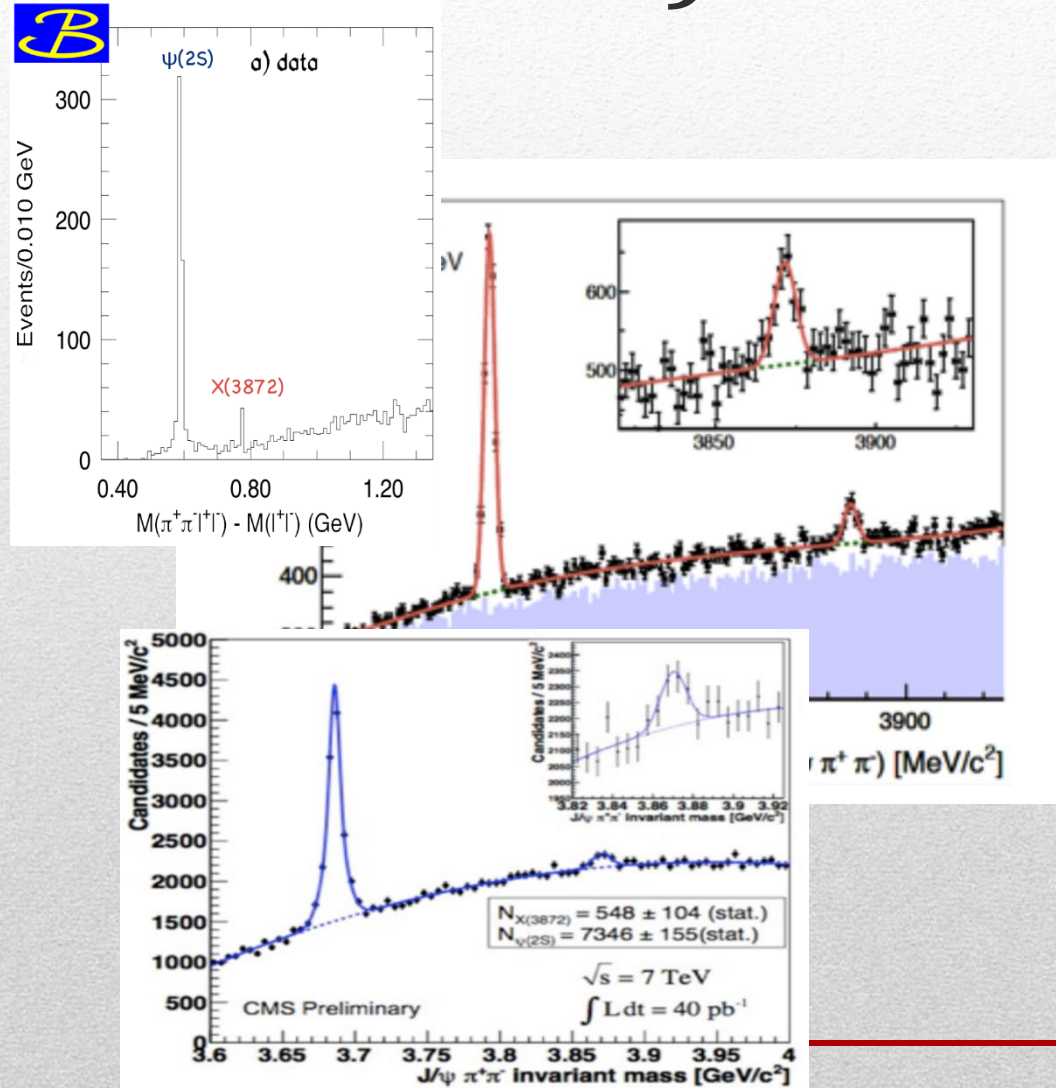
---

BACKUP

---



# X(3872)



- **Very close** to  $DD^*$  threshold
- **Too narrow** for an above-threshold charmonium
- **Isospin violation** too big  

$$\frac{\Gamma(X \rightarrow J/\psi \omega)}{\Gamma(X \rightarrow J/\psi \rho)} \sim 0.8 \pm 0.3$$
- **Mass prediction** not compatible with  $\chi_{c1}(2P)$

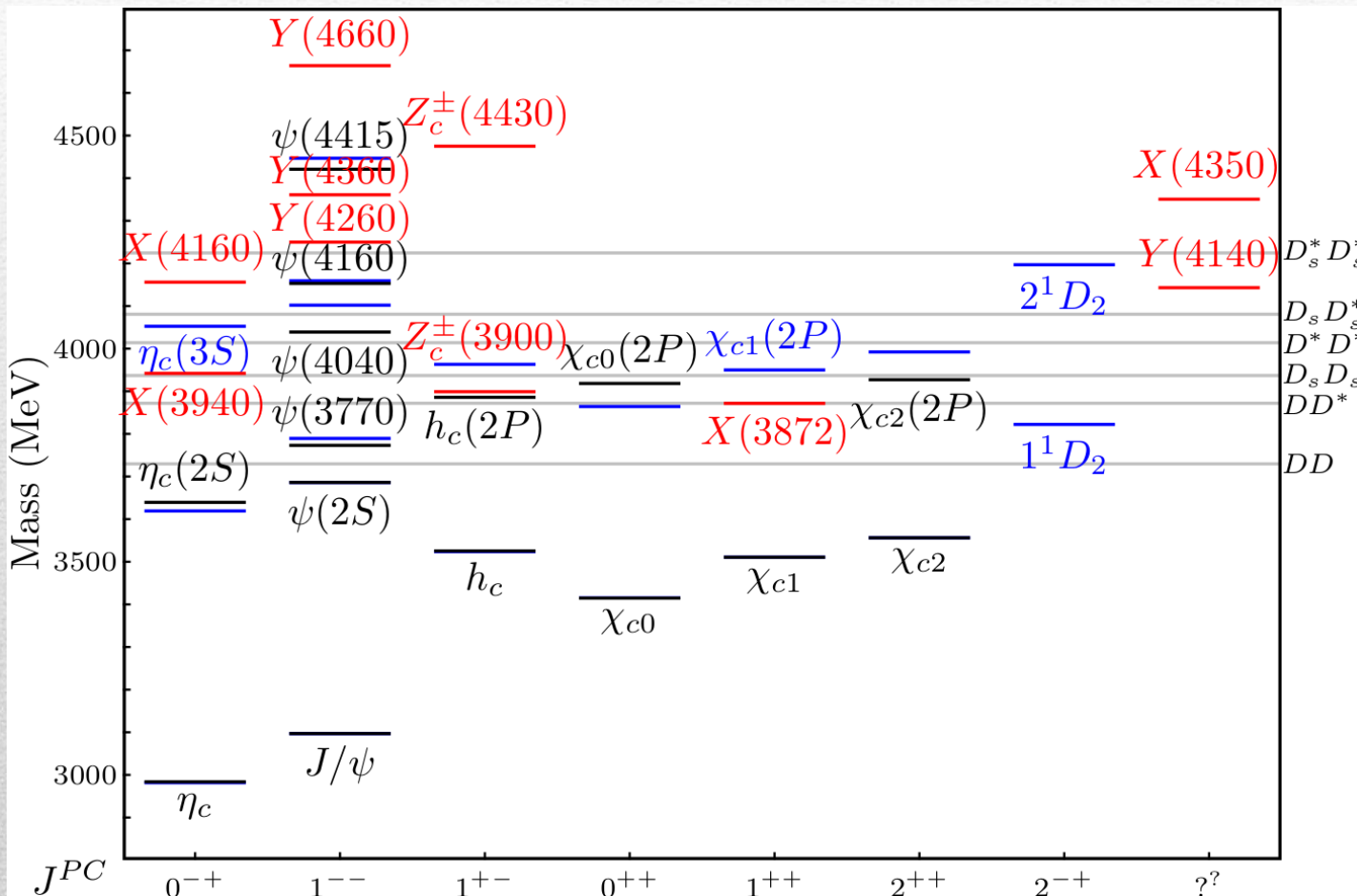
$$M = 3871.68 \pm 0.17 \text{ MeV}$$

$$M_X - M_{DD^*} = -0.14 \pm 0.22 \text{ MeV}$$

$$\Gamma < 1.2 \text{ MeV @90\%}$$

$$J^{PC} = 1^{++}$$

# Quarkonium orthodoxy?



A host of **unexpected resonances** have appeared

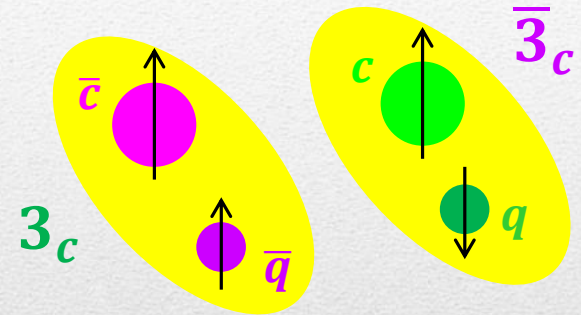
decaying into charmonium + light

**Hardly reconciled** with usual charmonium interpretation

# Tetraquark

One of the models is a compact  
**diquark-antidiquark bound state**

$$[cq]_{S=0}[\bar{c}\bar{q}]_{S=1} + h.c.$$



Maiani, Piccinini, Polosa, Riquer PRD71 014028

Faccini, Maiani, Piccinini, AP, Polosa, Riquer PRD87 11, 111102

We can evaluate mass spectrum in a constituent quark model

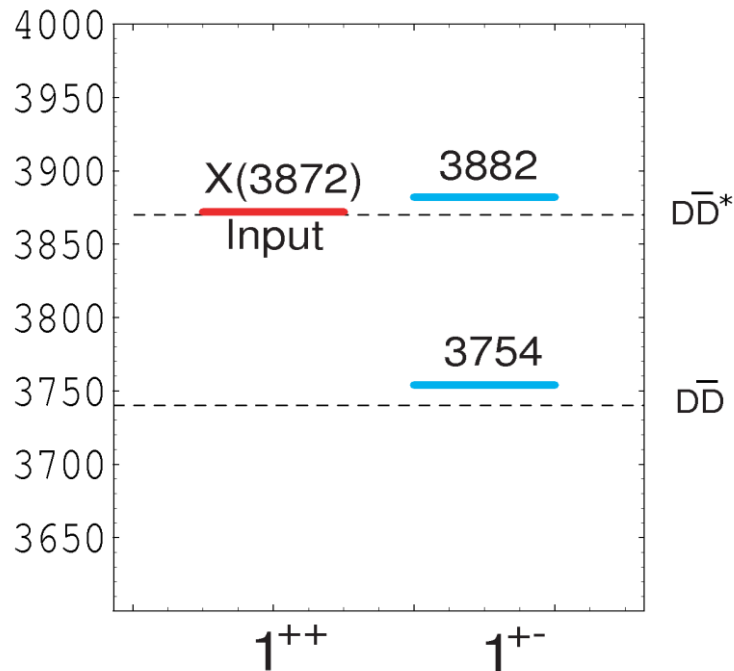
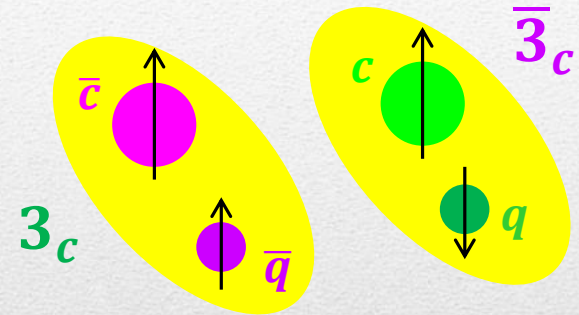
$$H = -2 \sum_{i < j} \kappa_{ij} \vec{S}_i \cdot \vec{S}_j \frac{\lambda_i^a}{2} \frac{\lambda_j^a}{2}$$

# Tetraquark

One of the models for the **X(3872)** is a compact **diquark-antidiquark bound state**

Maiani, Piccinini, Polosa, Riquer PRD71 014028

$$H = \sum_i m_i - 2 \sum_{i < j} \kappa_{ij} \vec{S}_i \cdot \vec{S}_j \frac{\lambda_i^a}{2} \frac{\lambda_j^a}{2}$$



Constituent mass of the diquark is unknown

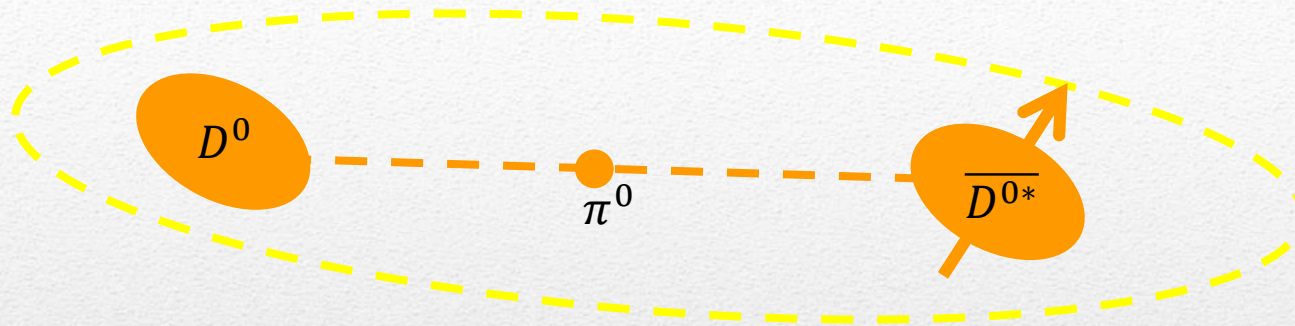


We can use  $X(3872)$  as the **seed to predict masses** of mesons made up of the same diquarks



$Z_c(3900)$  predicted + a lighter state

# Molecule



Tornqvist, Z.Phys. C61, 525 (1994)

A **deuteron-like meson pair**, the interaction is mediated by the exchange of light mesons

Two scales:  
 $R \sim 1$  fm radius of the mesons  
 $R \sim 10$  fm radius of the molecule

Good description of **decay patterns** and X(3872) **isospin violation** ✓

States appear close to thresholds ✓ (but Z(4430) ✗)

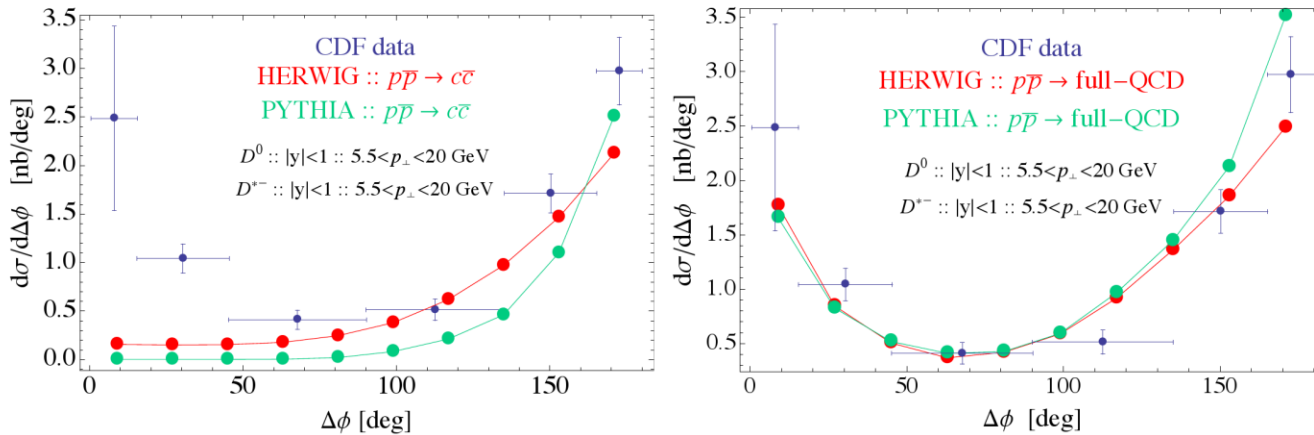
Binding energy is often **small**, or **positive** (repulsive interaction) ✗

# Tuning of MC

## Monte Carlo simulations

A. Esposito

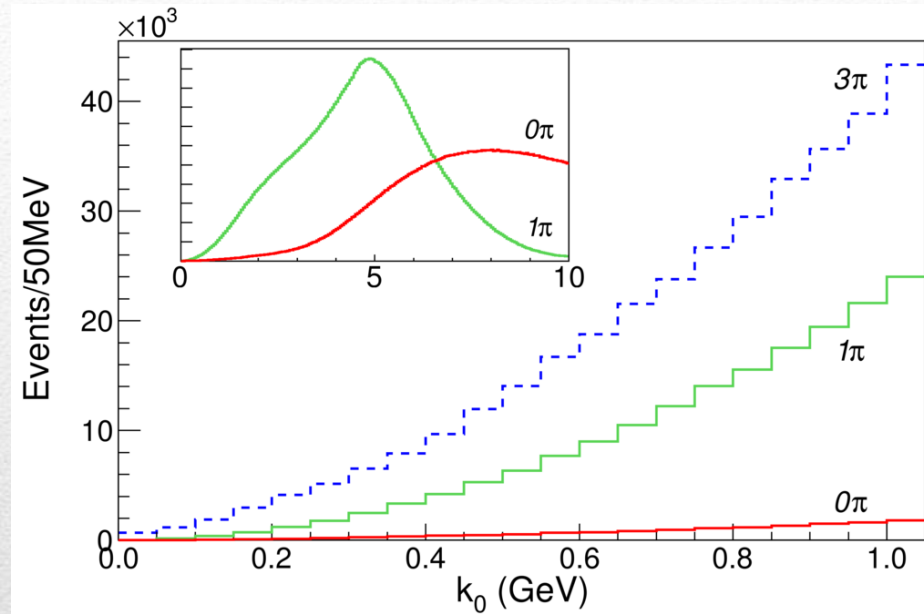
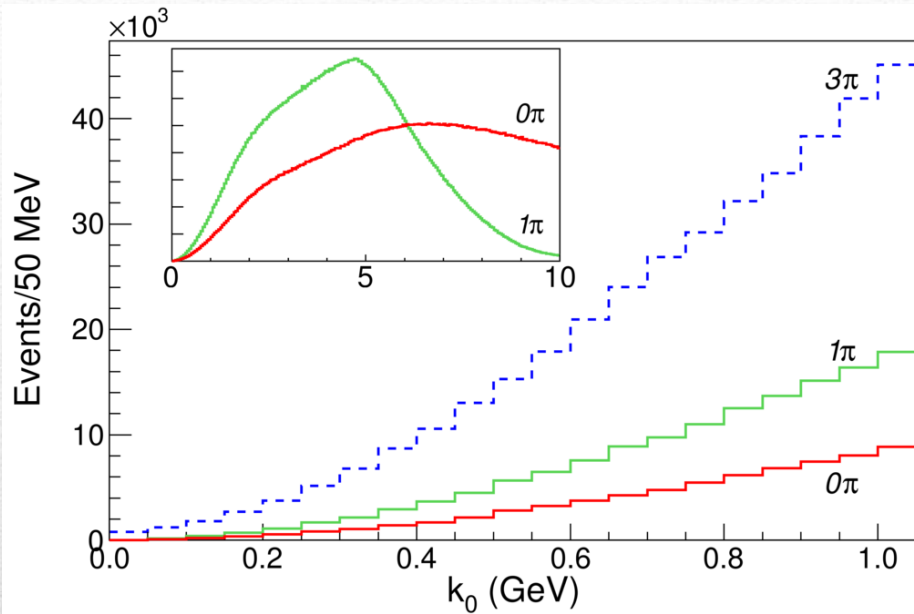
- We compare the  $D^0 D^{*-}$  pairs produced as a function of relative azimuthal angle with the results from CDF:



*The c-cbar run underestimate the low angles (low- $k_{\perp}$ ) region!*

Such distributions of charm mesons are available at Tevatron  
No distribution has been published (yet) at LHC

$$p\bar{p} \rightarrow c\bar{c}$$



#events	Herwig	Pythia
$0\pi$	10	3
$1\pi$	19	21
$3\pi$	802	814

The enhancement is impressive because first bins are almost empty