

Top theory

What role for precision in top-quark physics?

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Plan

Theory status

- Top-quark pair-production
- Single top-quark production
- Electroweak effects
- Asymmetries

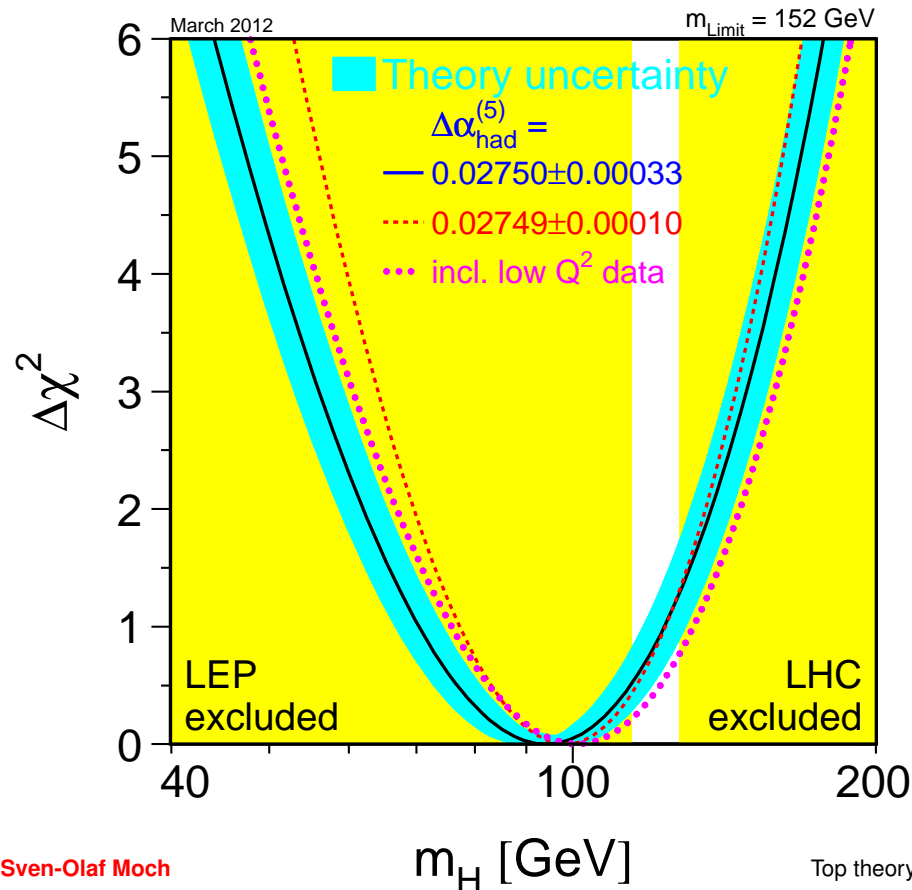
Big question

- Top-quark mass

Why precision?

Long history of indirect searches for new physics

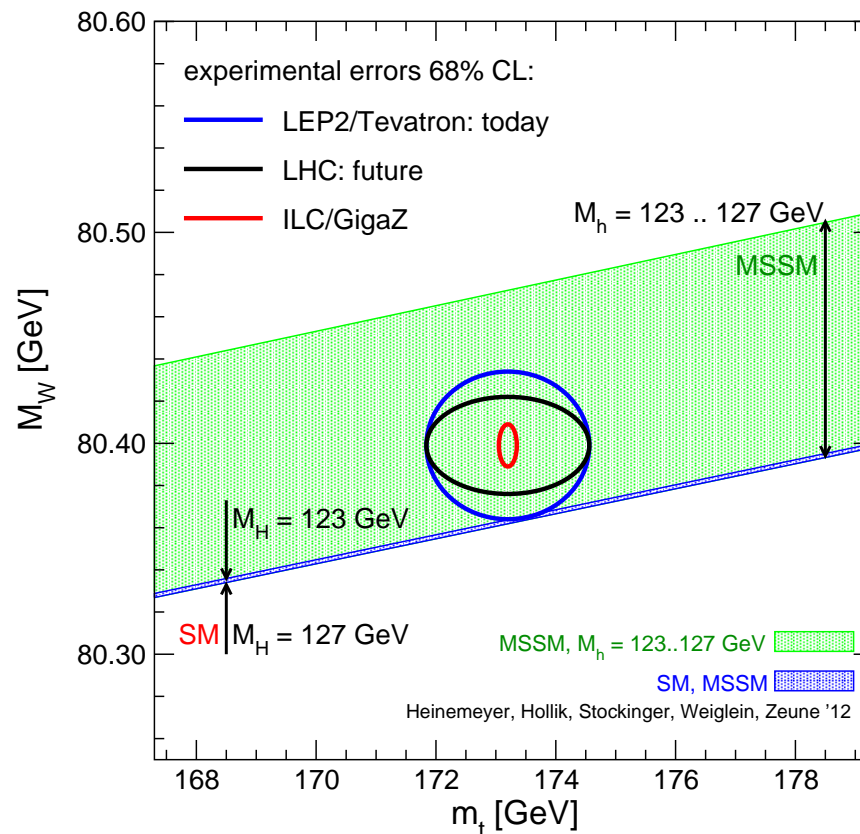
- In absence of direct evidence for new physics look for deviations in precision measurements
- Constraints for parameter space through precision tests
 - e.g., LEP electroweak precision data predicts low Higgs mass M_H



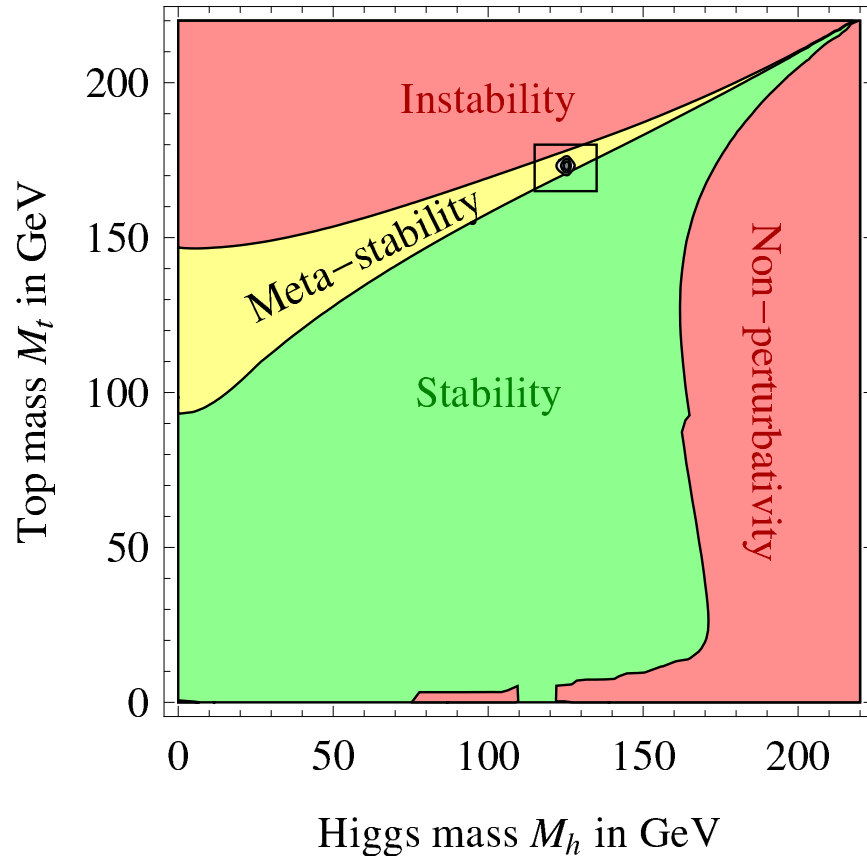
After the Higgs boson discovery

Electroweak precision fits

- Extension to MSSM Heinemeyer, Hollik, Stöckinger, Weiglein, Zeune '12
- Relations for radiative corrections known through two loops
 - need for precise input parameters: M_W and top-quark mass m_t



Electroweak vacuum stability



Bezrukov, Kalmykov, Kniehl, Shaposhnikov '12;
Degrassi, Di Vita, Elias-Miro, Espinosa,
Giudice et al. '12;
Alekhin, Djouadi, S.M. '12; Masina '12;
Buttazzo, Degrassi, Giardino, Giudice, Sala,
Salvio, Strumia '13;
[many people]

- Phase diagram if Standard Model extrapolated up to Planck scale M_P
 - relation between Higgs mass m_H and top quark mass m_t
 - condition of absolute electroweak vacuum stability dependent on m_t
- Precision on m_t decisive for “fate of universe”

Top-quark pair-production

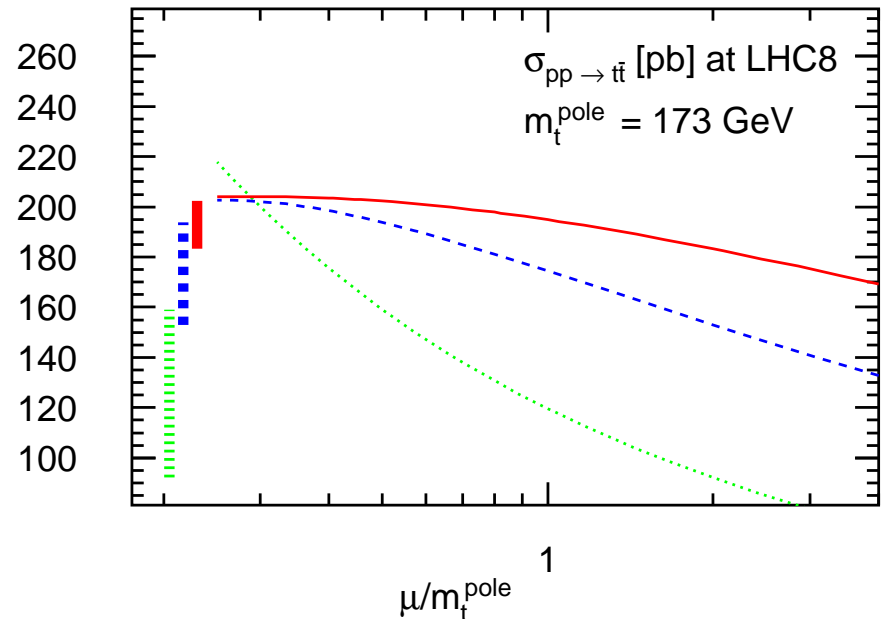
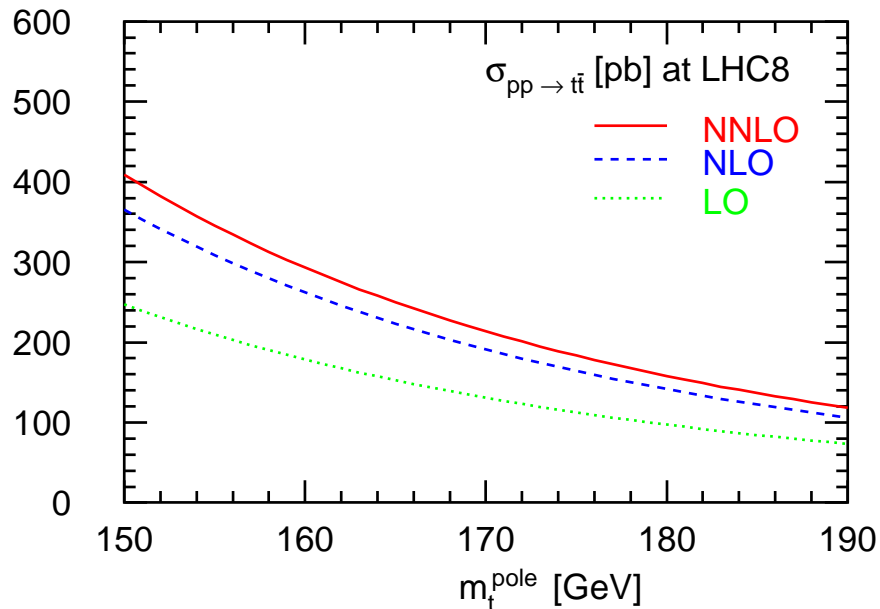
Rates and shapes

- Requirements for precision of theory predictions
 - driven by accuracy of experimental data
 - QCD corrections at least to NLO in QCD
- NNLO QCD corrections mandatory if data accuracy of $\mathcal{O}(10\%)$ or better
 - inclusive cross section for top-quark pairs at LHC8
 - expected for differential distributions in run II
- Electroweak corrections become important as well, since order $\alpha_s^2 \sim \alpha_{EW}$

Total cross section

Exact result at NNLO in QCD

Czakon, Fiedler, Mitov '13



- NNLO perturbative corrections (e.g. at LHC8)
 - K -factor (NLO \rightarrow NNLO) of $\mathcal{O}(10\%)$; scale stability of $\mathcal{O}(\pm 5\%)$
- Beyond NNLO
 - theory improvements with soft gluon resummation [many people]
 - K -factor (NNLO \rightarrow resummed) small; scale stability further improved

Top-quark mass from total cross section

- Intrinsic limitation of sensitivity in total cross section

$$\left| \frac{\Delta\sigma_{t\bar{t}}}{\sigma_{t\bar{t}}} \right| \simeq 5 \times \left| \frac{\Delta m_t}{m_t} \right|$$

- QCD factorization for cross section

$$\sigma_{pp \rightarrow X} = \sum_{ij} f_i(\mu^2) \otimes f_j(\mu^2) \otimes \hat{\sigma}_{ij \rightarrow X}(\alpha_s(\mu^2), Q^2, \mu^2, m_X^2)$$

- joint dependence on non-perturbative parameters:
parton distribution functions f_i , strong coupling α_s , masses m_X

Correlations are essential

- Cross section at LHC has correlation of m_t , $\alpha_s(M_Z)$ and gluon PDF

$$\sigma_{t\bar{t}} \sim \alpha_s^2 m_t^2 g(x) \otimes g(x)$$

- effective parton $\langle x \rangle \sim 2m_t/\sqrt{s} \sim 2.5 \dots 5 \cdot 10^{-2}$
- fit with fixed values of m_t and $\alpha_s(M_Z)$ carries significant bias
Czakon, Mangano, Mitov, Rojo '13
- fit with PDF re-weighting and fixed values of m_t insufficient
Beneke, Falgari, Klein, Piclum, Schwinn, Ubiali, Yan '12

Going differential

Shapes

- NNLO QCD corrections mandatory if data accuracy of $\mathcal{O}(10\%)$ or better
- Case for:
 - inclusive cross section for top-quark pairs at LHC8
 - expected for differential distributions in run II

Strategy

- In absence of complete NNLO QCD predictions can resort to approximations
- Exploit Sudakov resummation of soft gluon emission
 - physical cross sections convolution with parton luminosity dominated by threshold logarithms
- Approximate NNLO results in (semi-inclusive) kinematics
Kidonakis, Sterman '96; . . . ; Ahrens, Ferroglia, Neubert, Pecjak, Yang '11; Kidonakis '12; Ferroglia, Pecjak, Yang '13
- Upshot: single variable differential distributions in p_T^t , y^t , $m_{t\bar{t}}$ available

Going differential

Boosted Top Quark Pair Production in Soft
Collinear Effective Theory *A. Ferroglia*

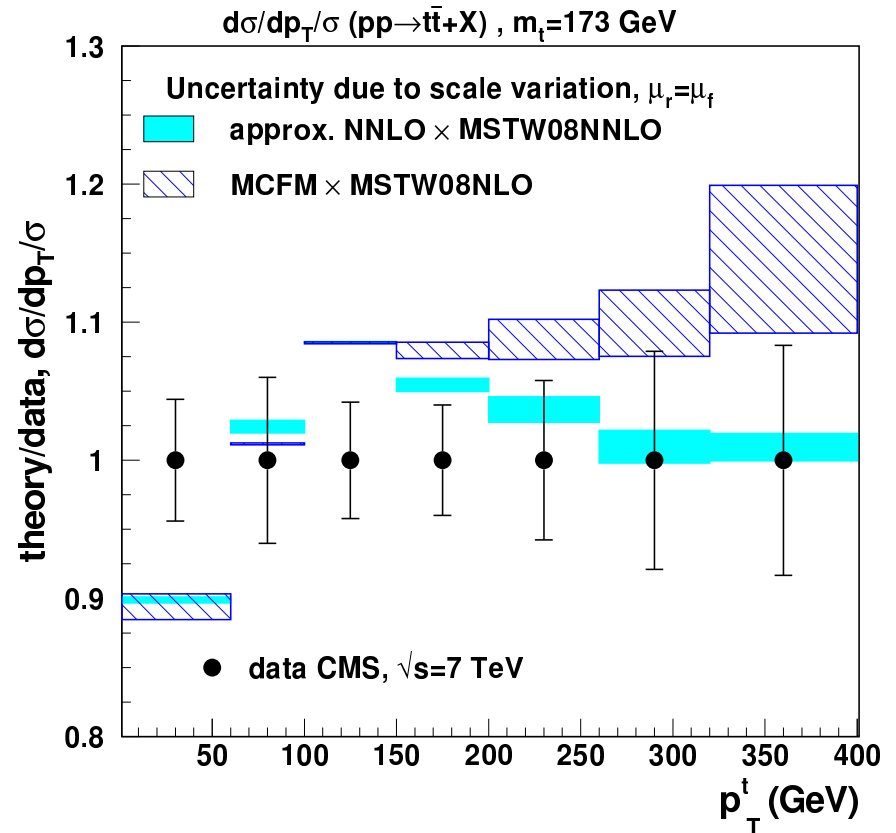
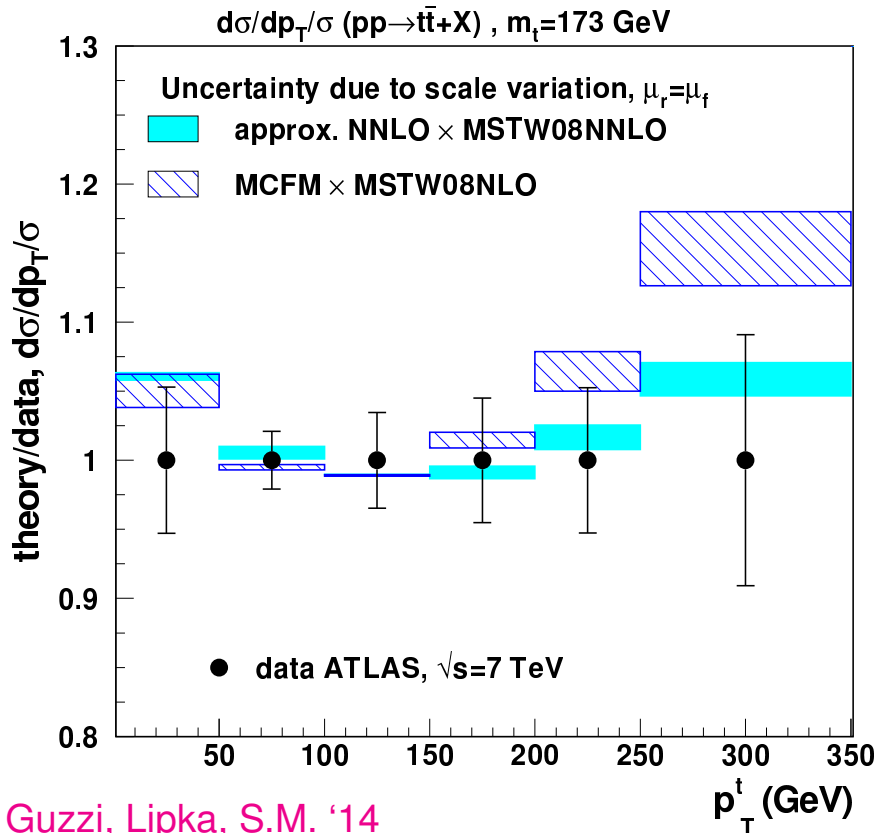
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Distributions at (approximately) NNLO



Guzzi, Lipka, S.M. '14

- Approximate NNLO results show trend in right direction for comparison with data
- Great opportunity for high statistics measurements in run II
 - fast and reliable numerical codes are essential (interface to fastNLO or Applgrid)

Tools 4 you: available codes

Total cross section

- NNLO QCD corrections and soft gluon resummation
 - Hathor Aliev, Lacker, Langenfeld, Moch, Uwer, Wiedermann [arXiv:1007.1327]
 - Top++ Czakon, Mitov [arXiv:1112.5675]
 - TOPIX Beneke, Falgari, Klein, Piclum, Schwinn, Ubiali, Yan [arXiv:1206.2454]

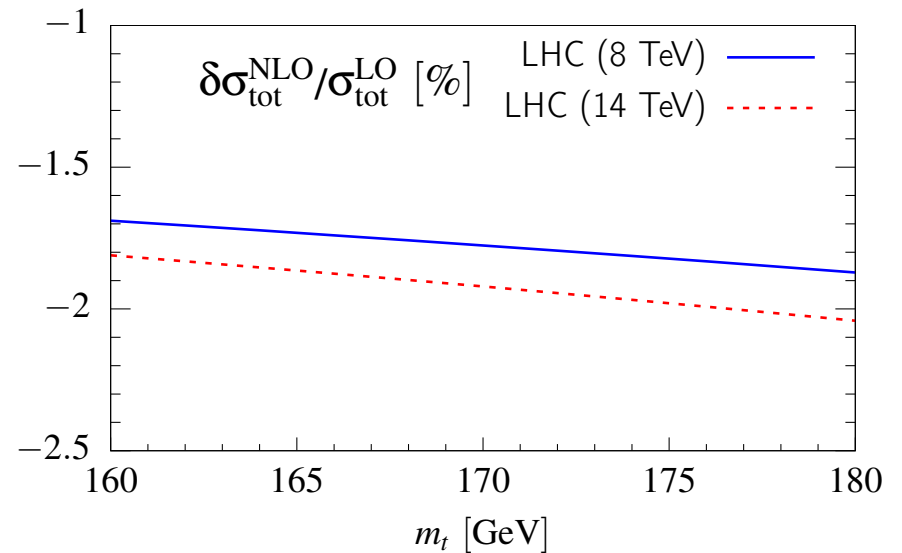
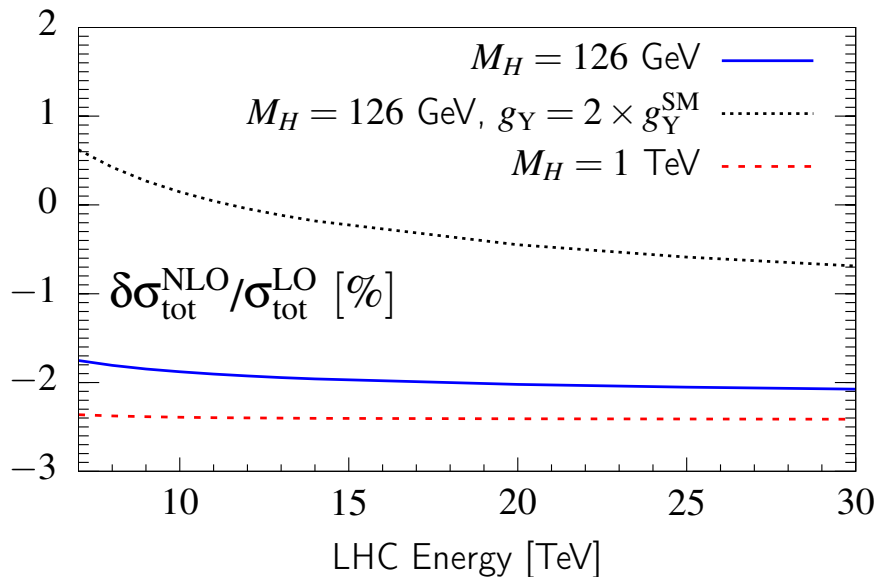
Differential distributions

- NLO QCD corrections (in association with jets, leptons, . . .)
- Fixed order with on-shell top-quarks or decays
 - MCFM Campbell, Ellis [arXiv:1204.1513]
- Matched to parton shower
 - MC@NLO Frixione, Webber [hep-ph/0305252]
 - POWHEG-BOX Alioli, Nason, Oleari, Re [arXiv:1002.2581]
with contributions of [many people]
 - aMC@NLO Alwall, Frederix, Frixione, Hirschi, Maltoni, Mattelaer, Shao, Stelzer, Torrielli, Zaro [arXiv:1405.0301]

Electroweak corrections

- Electroweak corrections (ratio of σ_{EW}/σ_{LO})

Beenakker, Denner, Hollik, Mertig, Sack, Wackerath '94; Bernreuther, Fucker '05;
Kühn, Scharf, Uwer '06

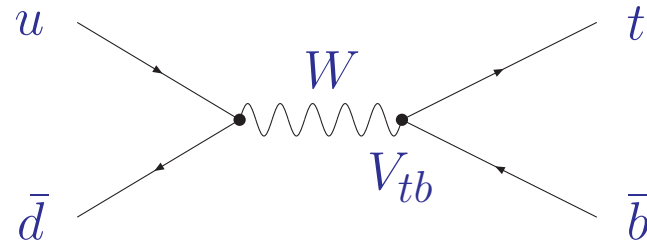


- Left: σ_{EW}/σ_{LO} as function of total cms energy (effect depends on Higgs mass and Higgs-Yukawa coupling)
- Right: σ_{EW}/σ_{LO} as function of top-quark mass: $\mathcal{O}(2\%)$ with respect to σ_{LO} negative contribution to total cross section
- New:** NLO EW corrections now included in update of Hathor (v2.1)
Kühn, Scharf, Uwer '13

Single top-quark production

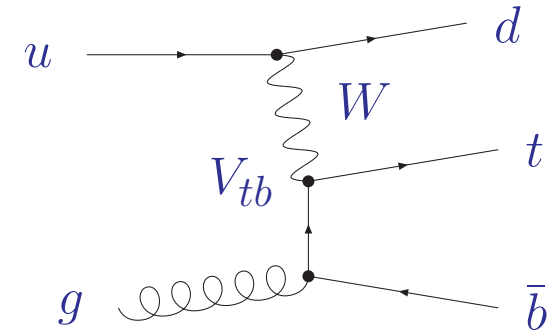
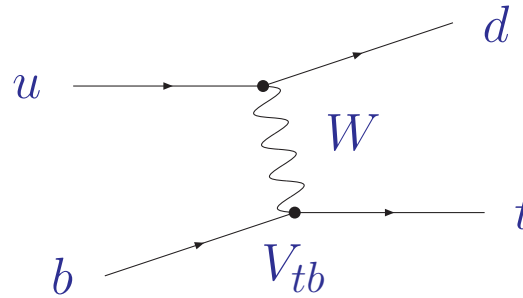
- Study of charged-current weak interaction of top quark

- s -channel production



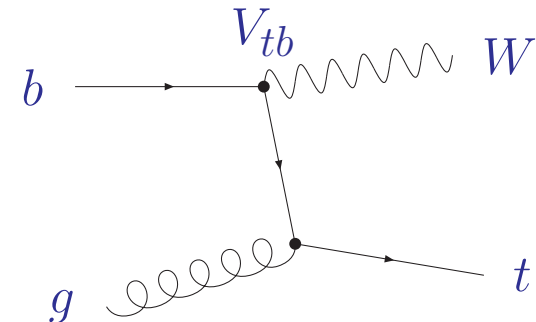
- t -channel production

- bg -channel at NLO enhanced by gluon luminosity



- Wt -production

- contributes at LHC (small at Tevatron)



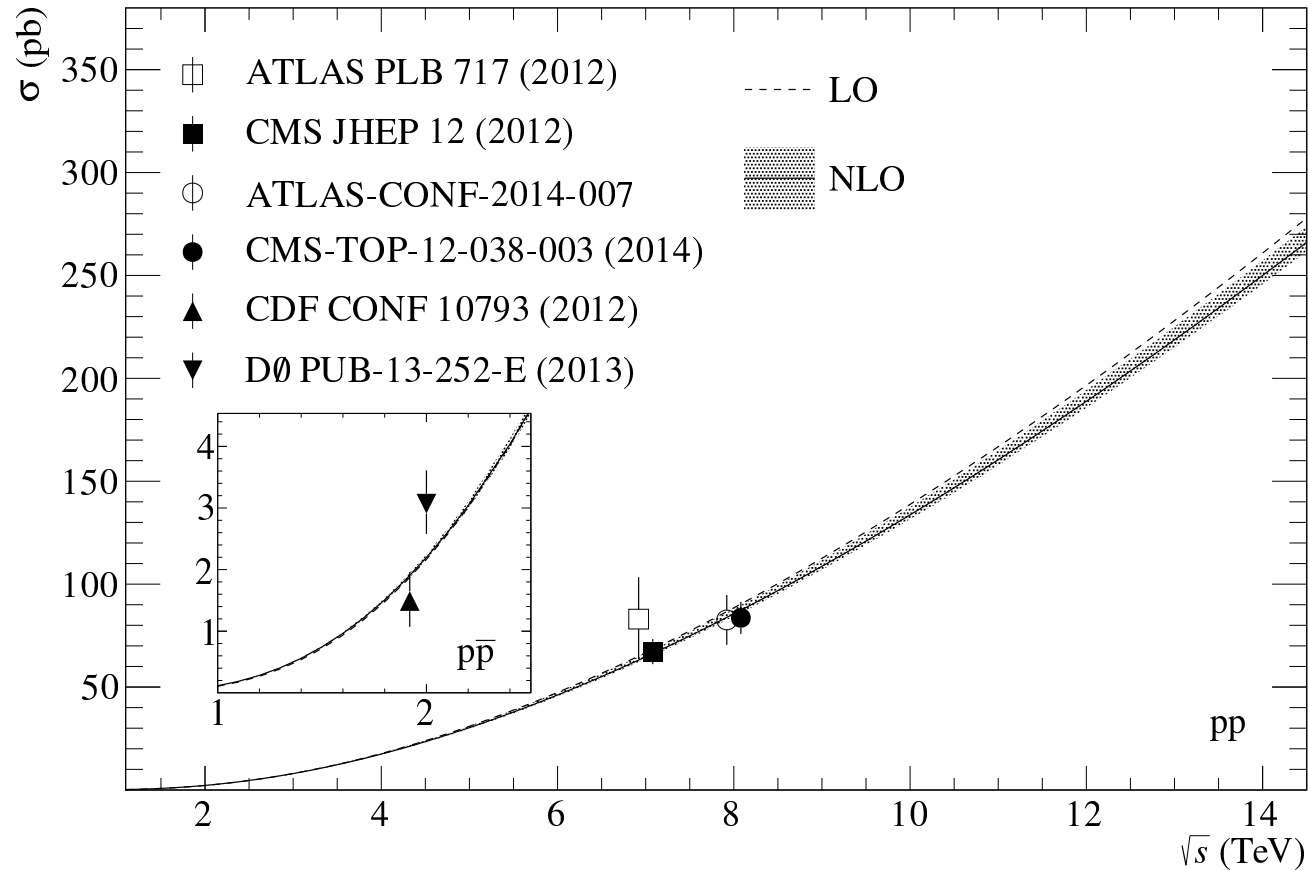
Theory status

- QCD corrections known
 - complete NLO Harris, Laenen, Phaf, Sullivan, Weinzierl '02; Sullivan '04; Campbell, Frederix, Maltoni, Tramontano '09; [+ many people]
 - implementations merged with parton shower
 - in MC@NLO Frixione, Laenen, Motylinski, Webber, White '09
 - in POWHEG Aioli, Nason, Oleari, Re '09
 - approximate NNLO corrections Kidonakis '11, '13

Treatment of heavy quarks

- Scheme with $n_l = 4$ light flavors + heavy quark of mass m_b at low scales
 - no mass singularities for $m_b, m_t \gg \Lambda_{QCD}$, no (evolving) PDFs
- Scheme with $n_l = 5$ light flavors
 - b PDF for $Q \gg \gg m_b$ generated perturbatively

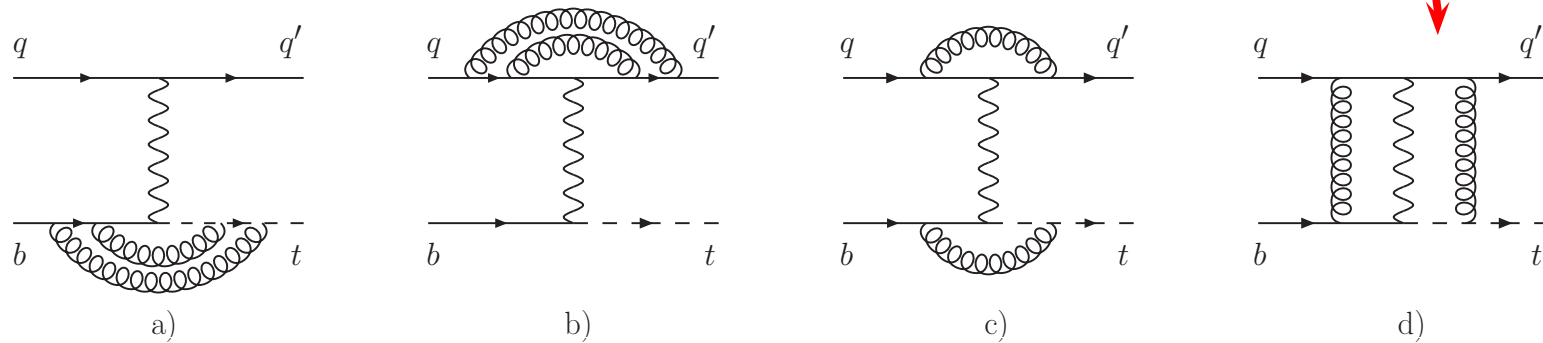
Single top-quark t -channel production



- **New:** Approximate NNLO QCD corrections in Hathor v2.0
Kant, Kind, Kintscher, Lohse, Martini, Mölbitz, Rieck, Uwer [to appear]

QCD corrections at NNLO

- **New:** computation of NNLO QCD corrections Brucherseifer, Caola, Melnikov '14
 - fully differential, with cuts on p_T
- QCD corrections treated in structure function approach
 - non-factorizable contributions neglected (neglected diagrams $\mathcal{O}(1/N_c^2)$ suppressed)

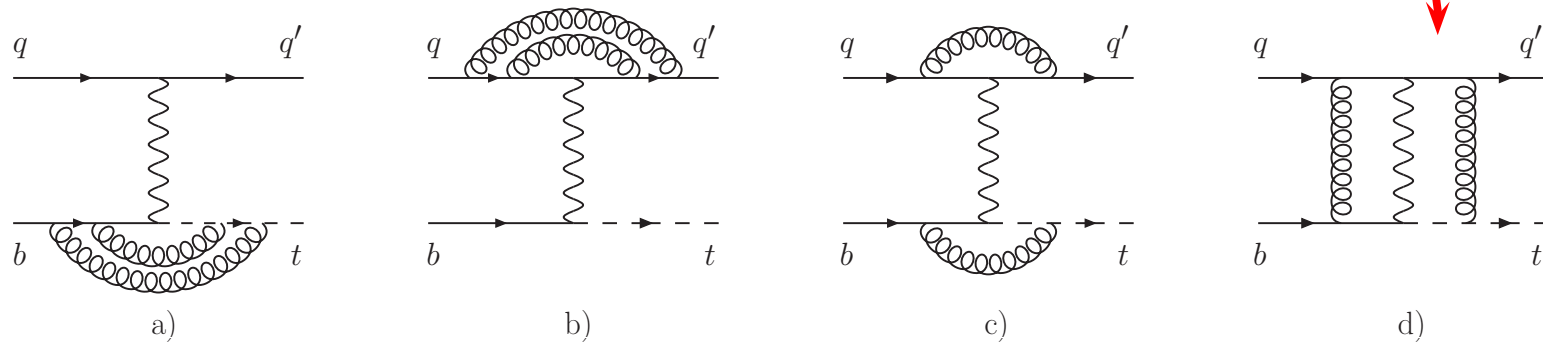


- QCD corrections to t -channel single top quark production at LHC8

p_{\perp}	$\sigma_{\text{LO}}, \text{pb}$	$\sigma_{\text{NLO}}, \text{pb}$	δ_{NLO}	$\sigma_{\text{NNLO}}, \text{pb}$	δ_{NNLO}
0 GeV	$53.8^{+3.0}_{-4.3}$	$55.1^{+1.6}_{-0.9}$	+2.4%	$54.2^{+0.5}_{-0.2}$	-1.6%
20 GeV	$46.6^{+2.5}_{-3.7}$	$48.9^{+1.2}_{-0.5}$	+4.9%	$48.3^{+0.3}_{-0.02}$	-1.2%
40 GeV	$33.4^{+1.7}_{-2.5}$	$36.5^{+0.6}_{-0.03}$	+9.3%	$36.5^{+0.1}_{+0.1}$	-0.1%
60 GeV	$22.0^{+1.0}_{-1.5}$	$25.0^{+0.2}_{+0.3}$	+13.6%	$25.4^{-0.1}_{+0.2}$	+1.6%

QCD corrections at NNLO

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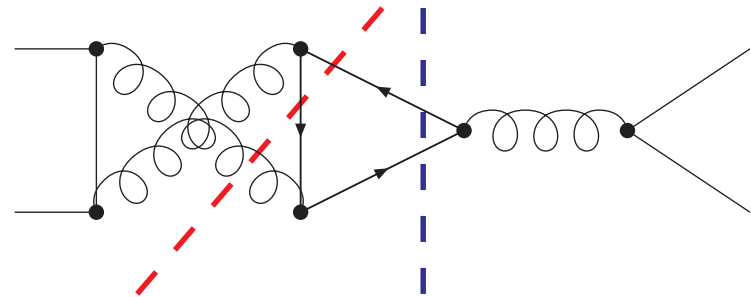
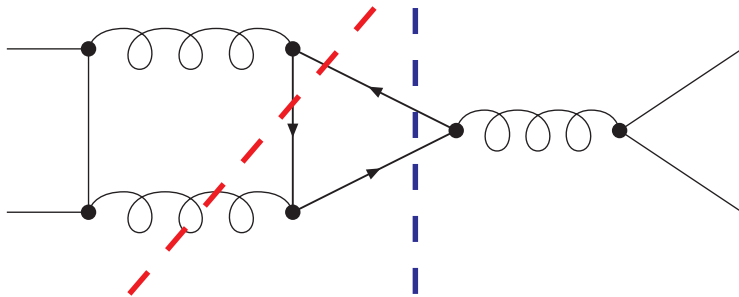


- QCD corrections to t -channel single anti-top quark production at LHC8

p_{\perp}	$\sigma_{\text{LO}}, \text{pb}$	$\sigma_{\text{NLO}}, \text{pb}$	δ_{NLO}	$\sigma_{\text{NNLO}}, \text{pb}$	δ_{NNLO}
0 GeV	$29.1^{+1.7}_{-2.4}$	$30.1^{+0.9}_{-0.5}$	+3.4%	$29.7^{+0.3}_{-0.1}$	-1.3%
20 GeV	$24.8^{+1.4}_{-2.0}$	$26.3^{+0.7}_{-0.3}$	+6.0%	$26.2^{-0.01}_{-0.1}$	-0.4%
40 GeV	$17.1^{+0.9}_{-1.3}$	$19.1^{+0.3}_{+0.1}$	+11.7%	$19.3^{-0.2}_{+0.1}$	+1.0%
60 GeV	$10.8^{+0.5}_{-0.7}$	$12.7^{+0.03}_{+0.2}$	+17.6%	$12.9^{-0.2}_{+0.2}$	+1.6%

Charge asymmetry

- Top-quark charge asymmetry arises from interference between real emission and virtual contributions
 - interference term does not contribute to total cross section (Furry's theorem)
- Asymmetric contribution for un-integrated $t\bar{t}$ phase space
 - virtual corrections
 - real corrections



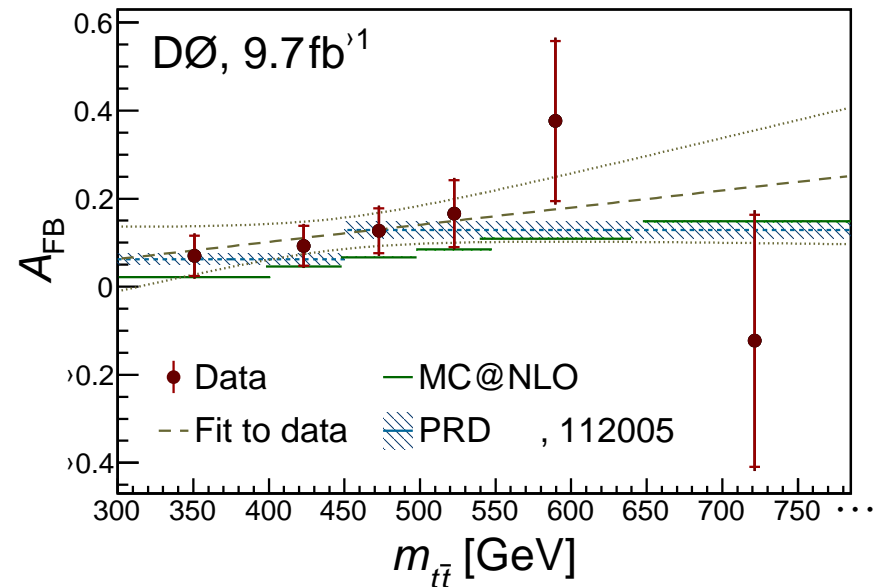
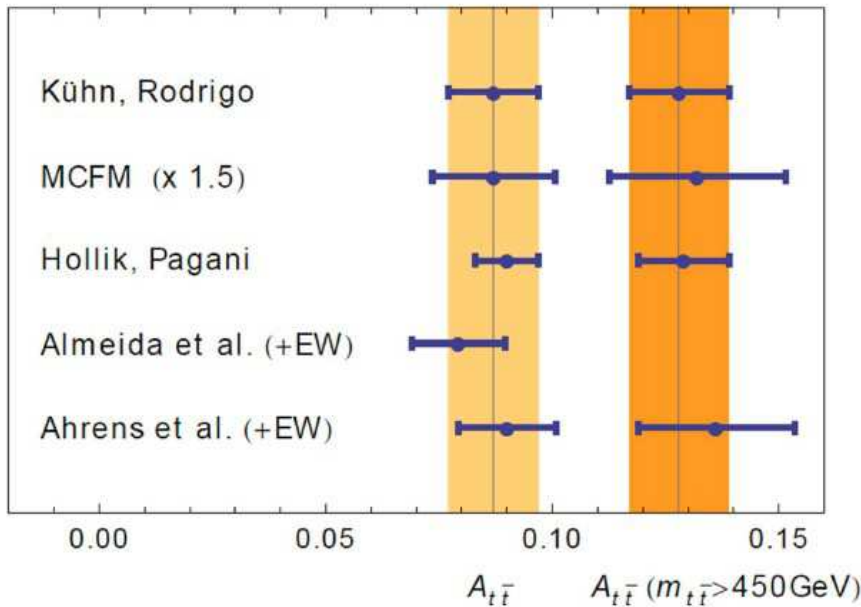
- Asymmetry is genuine quantum effect
 - theory predictions effectively leading order only
 - interpretation requires good understanding of the quantum level

Forward-backward asymmetry at Tevatron

Top properties at the Tevatron *G. Petrillo*

- Top-quark forward-backward asymmetry A_{FB} definitions at Tevatron with $\Delta y_{t\bar{t}} = y_t - y_{\bar{t}}$

$$A_{FB}^{t\bar{t}} = \frac{N(\Delta y_{t\bar{t}} > 0) - N(\Delta y_{t\bar{t}} < 0)}{N(\Delta y_{t\bar{t}} > 0) + N(\Delta y_{t\bar{t}} < 0)}$$



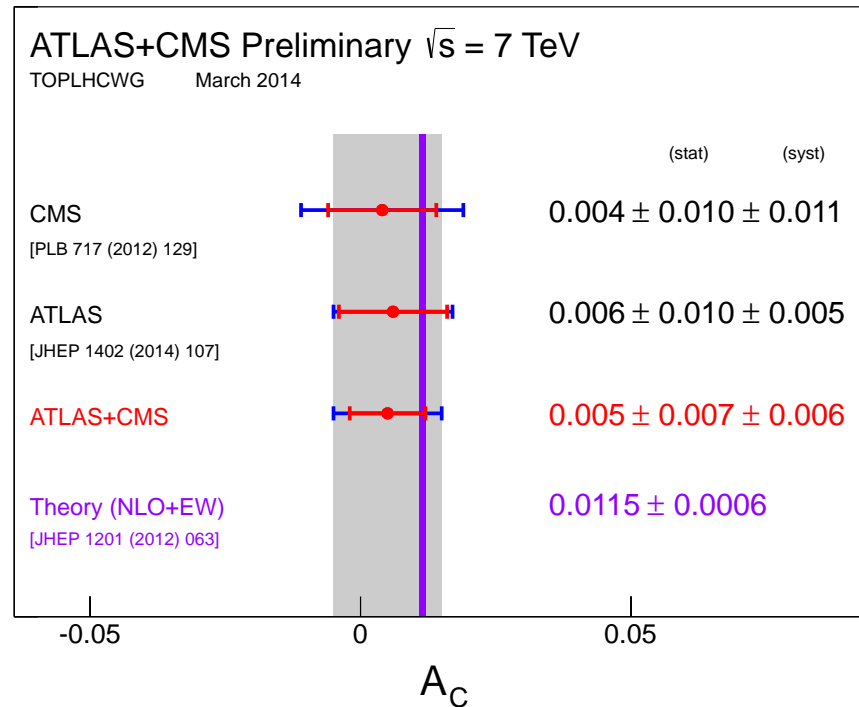
- Consistent picture from theory predictions include QCD+EW corrections *Kühn, Rodrigo '11*; *Hollik, Pagani '11* or soft gluon resummation *Almeida, Sterman, Vogelsang '08*; *Ahrens, Ferroglia, Neubert, Pecjak, Yang '11*
- Two-loop QCD corrections needed for assessment of theory uncertainty

Charge asymmetry at LHC

- Top-quark charge asymmetry A_C at LHC with $\Delta|y| = |y_t| - |y_{\bar{t}}|$

$$A_C = \frac{N(\Delta|y| > 0) - N(\Delta|y| < 0)}{N(\Delta|y| > 0) + N(\Delta|y| < 0)}$$

- no forward backward charge asymmetry, because initial state at LHC is P symmetric



Top quark properties and mass with CMS
K. Ecklund

- Consistency with theory predictions, but again two-loop QCD corrections needed

Top quark mass

What is the value of the top quark mass ?

$$m_t = ?$$

Quark masses in Standard Model

- Higgs boson gives mass to matter fields via Higgs-Yukawa coupling
 - large top quark mass m_t

QCD

- Classical part of QCD Lagrangian

$$\mathcal{L} = -\frac{1}{4} F_{\mu\nu}^a F_b^{\mu\nu} + \sum_{\text{flavors}} \bar{q}_i (i\not{D} - m_q)_{ij} q_j$$

- field strength tensor $F_{\mu\nu}^a$ and matter fields q_i, \bar{q}_j
- covariant derivative $D_{\mu,ij} = \partial_\mu \delta_{ij} + ig_s (t_a)_{ij} A_\mu^a$
- Formal parameters of the theory (no observables)
 - strong coupling $\alpha_s = g_s^2 / (4\pi)$
 - quark masses m_q

Challenge

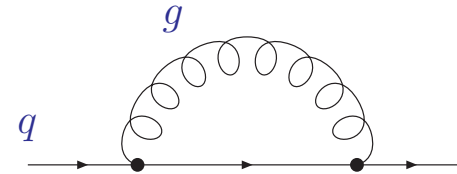
- Suitable observables for measurements of α_s, m_q, \dots
 - comparison of theory predictions and experimental data

Quark mass renormalization

Pole mass

- Based on (unphysical) concept of top-quark being a free parton

$$\not{p} - m_q - \Sigma(p, m_q) \Big|_{p^2 = m_q^2}$$



- heavy-quark self-energy $\Sigma(p, m_q)$ receives contributions from regions of all loop momenta – also from momenta of $\mathcal{O}(\Lambda_{QCD})$
- Ambiguity Δm_q in definition of pole mass up to corrections $\mathcal{O}(\Lambda_{QCD})$
Bigi, Shifman, Uraltsev, Vainshtein '94; Beneke, Braun '94; Smith, Willenbrock '97
 - lattice QCD bound: $\Delta m_q \geq 0.7 \cdot \Lambda_{QCD} \simeq 200 \text{ MeV}$ Bauer, Bali, Pineda '11

Short distance mass

- Short distance masses (\overline{MS} , 1S Hoang, Teubner '99, PS Beneke '98, ...) probe at scale of hard interaction: $m_{\text{pole}} = m_{\text{short distance}} + \delta m$
- \overline{MS} mass definition $m(\mu_R)$ realizes running mass (scale dependence)
- Conversion between m_{pole} and \overline{MS} mass $m(\mu_R)$ in perturbation theory
Gray, Broadhurst, Gräfe, Schilcher '90; Chetyrkin, Steinhauser '99; Melnikov, v. Ritbergen '99

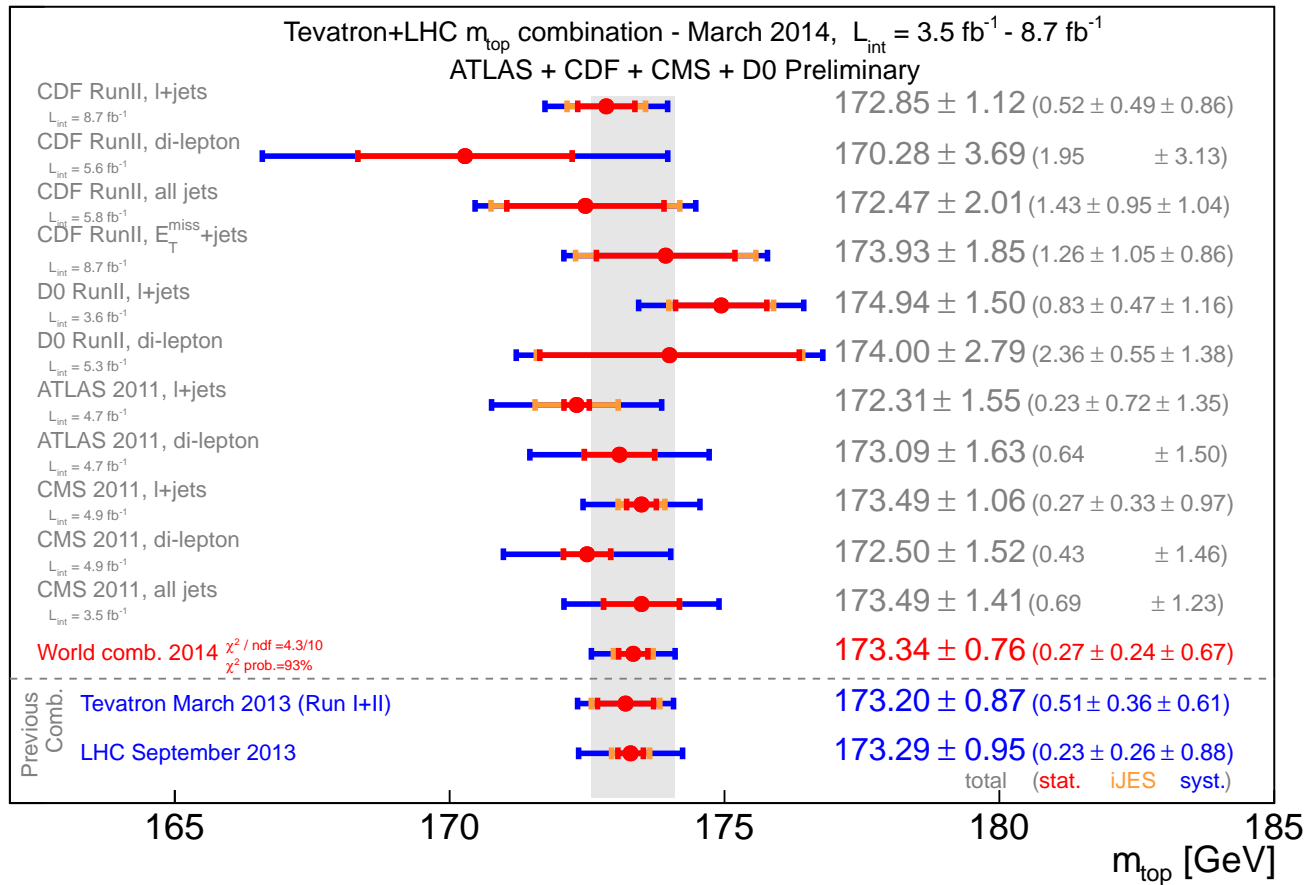
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What is the value of the top quark mass ?

$$m_t = ?$$

Some Answers

Top quark properties in ATLAS F. Derue



World combination

Experiment: ATLAS, CDF, CMS & D0 coll. 1403.4427

$$m_t = 173.34 \pm 0.76 \text{ GeV}$$

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In all measurements considered in the present combination, the analyses are calibrated to the Monte Carlo (MC) top-quark mass definition.

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Theory:

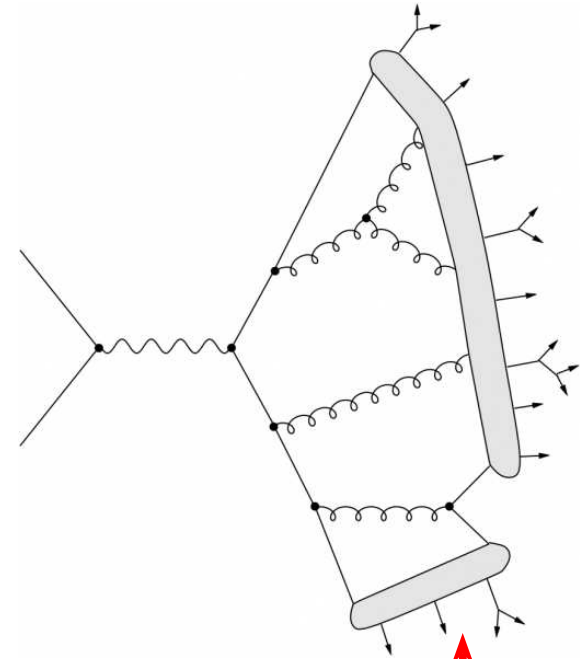
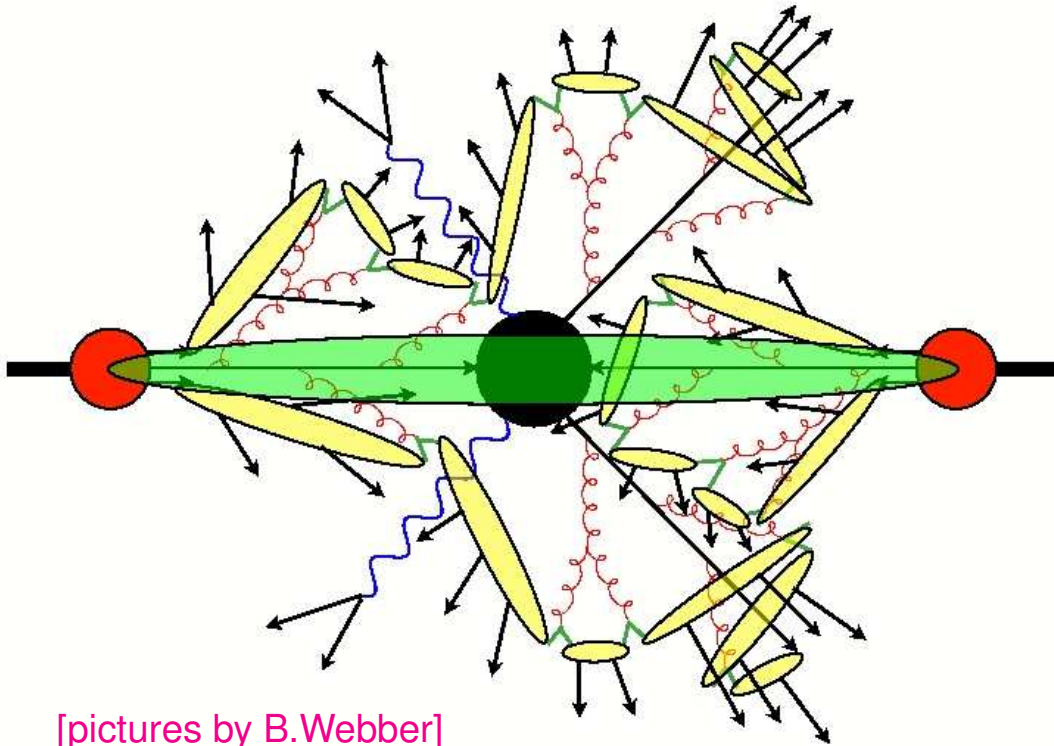
That is, we can state as the final result for the likely relation between the top quark mass measured using a given Monte Carlo event generator ("MC") and the pole mass as

$$m_{\text{pole}} = m_{\text{MC}} + Q_0 [\alpha_s(Q_0)c_1 + \dots]$$

where $Q_0 \sim 1 \text{ GeV}$ and c_1 is unknown, but presumed to be of order 1 and, according to the argument above, presumed to be positive.

A. Buckley et al. arXiv:1101.2599

Monte Carlo mass

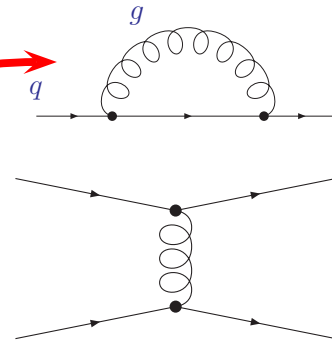


[pictures by B. Webber]

- Intuition tells, that Monte Carlo mass is pole mass due to kinematics
 $E_q^2 - p^2 = m_q^2$
- Quantum mechanics considers particles in potential
 - heavy quarks interact with potential due to gluon field
- String hadronization model based on potential energy of heavy-quark pair (colored sources)

Static energy of heavy-quark

- Consider static energy E_{stat} of heavy-quark pair
 - well-defined problem in perturbation theory at large scales R
 - use lattice at small scales
- QCD corrections to static energy receives from
 - heavy-quark self-energy $\Sigma(p, m_q)$
 - heavy-quark potential $V(R)$



- Renormalon ambiguities in QCD corrections can cancel between $\Sigma(p, m_q)$ and $V(R)$

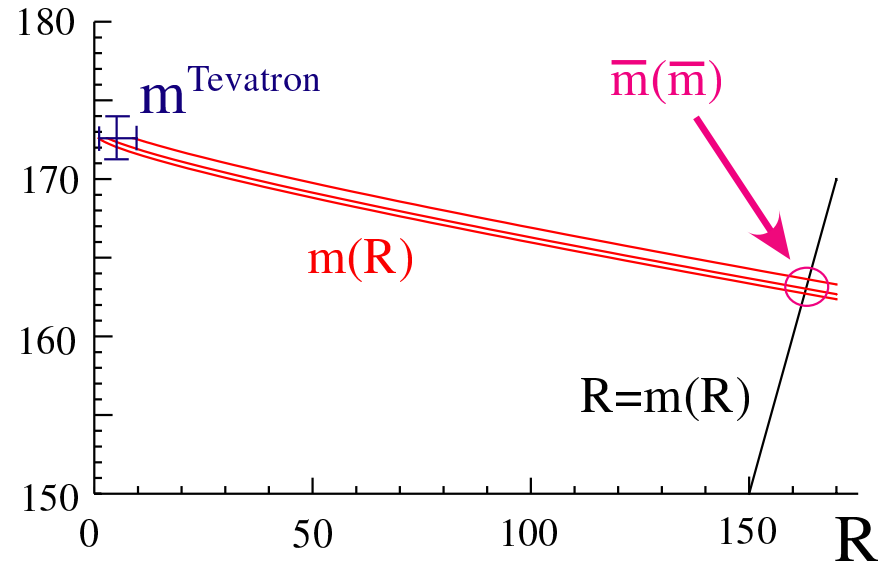
$$\begin{aligned} E_{\text{stat}} &= 2m_q + 2\Sigma(m_q, m_q) + V(R) \\ &= 2m_{\text{pole}} + V(R) \\ &= 2m^{\text{MSR}}(R) + \left(2\Sigma^{\text{fin}}(R, R) + V(R)\right) \end{aligned}$$

- Extraction of a short-distance mass $m^{\text{MSR}}(R)$ from the quarkonium spectrum is free of an ambiguity of order $\mathcal{O}(\Lambda_{QCD})$

Hoang, Smith, Stelzer, Willenbrock '98

Conversion of Monte Carlo mass to pole mass

- Running of $m^{\text{MSR}}(R)$ mass
Hoang, Stewart '08



Strategy

- Identify Monte Carlo mass with short distance mass at low scale $\mathcal{O}(1)$ GeV
 $m^{\text{MC}} \rightarrow m^{\text{MSR}}(R)$ with $R \simeq 1 \dots 9 \text{ GeV}$
- Choice 1: run $m^{\text{MSR}}(R)$ from low scale to $R = m_t$: $m^{\text{MSR}}(R) \rightarrow m(m)$ and convert from $m(m)$ to pole mass [arXiv:1405.4781]

$m^{\text{MSR}}(1)$	$m^{\text{MSR}}(3)$	$m^{\text{MSR}}(9)$	$\bar{m}(\bar{m})$	m_{11p}^{pl}	m_{21p}^{pl}	m_{31p}^{pl}
173.72	173.40	172.78	163.76	171.33	172.95	173.45

- Choice 2: convert from $m^{\text{MSR}}(R)$ at low scale directly to pole mass

$m^{\text{MSR}}(1)$	$m^{\text{MSR}}(3)$	$m^{\text{MSR}}(9)$	m_{11p}^{pl}	m_{21p}^{pl}	m_{31p}^{pl}
173.72	173.40	172.78	173.72	173.87	173.98

Conversion of Monte Carlo mass to pole mass

Summary

$$m_{\text{pole}} = 173.34 \pm 0.76 \text{ GeV (exp)} + \Delta m(\text{th})$$

with

$$\Delta m(\text{th}) = \pm 0.7 \text{ GeV} (m^{\text{MC}} \rightarrow m^{\text{MSR}}(3\text{GeV})) + 0.5 \text{ GeV} (m(m) \rightarrow m_{\text{pole}})$$

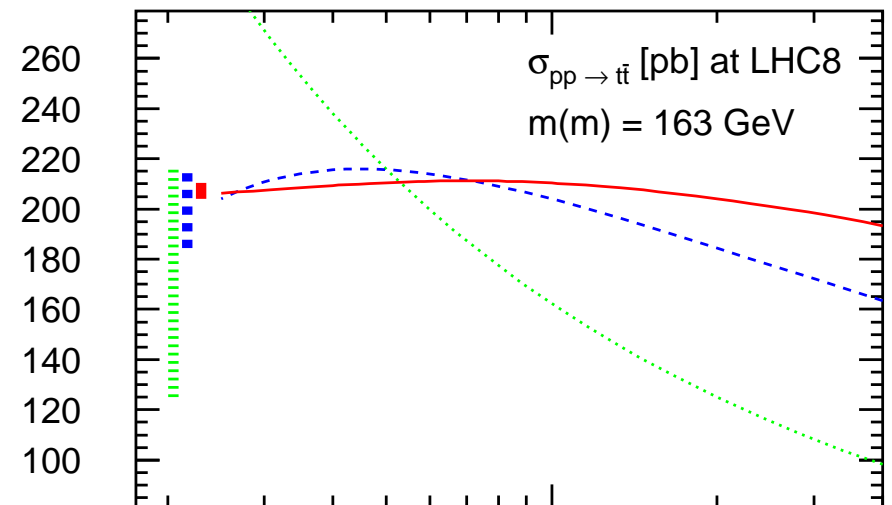
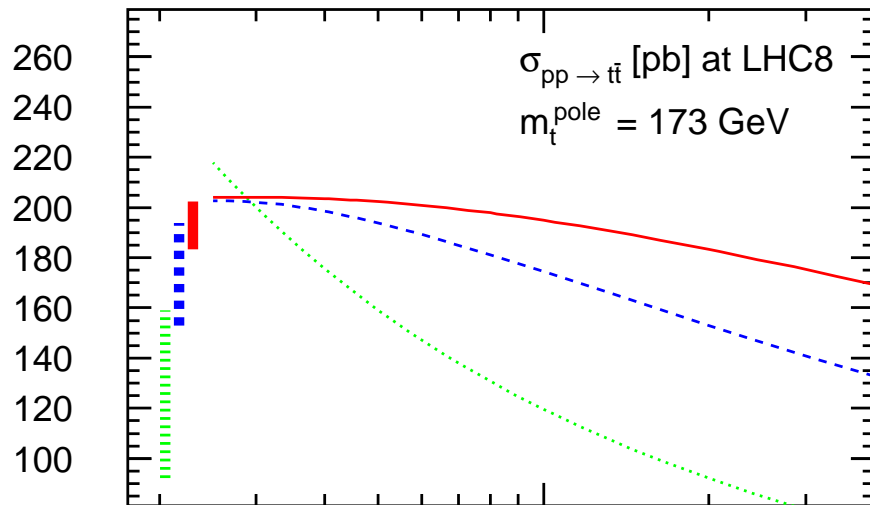
Alternative mass measurements

- Rates and shapes of distributions offer possibility for top mass determination with well-defined renormalization scheme
- Requirements:
 - theory predictions at least to NLO in QCD
 - sufficient sensitivity to m_t (kinematics)
- Observables (examples):
 - inclusive cross section
 - shapes of distributions; e.g., m_{lb} distribution or jet rates

Total cross section with running mass

Comparison pole mass vs. $\overline{\text{MS}}$ mass

Dowling, S.M. '13



pole mass

μ/m_t^{pole}

1

$\mu/m(m)$

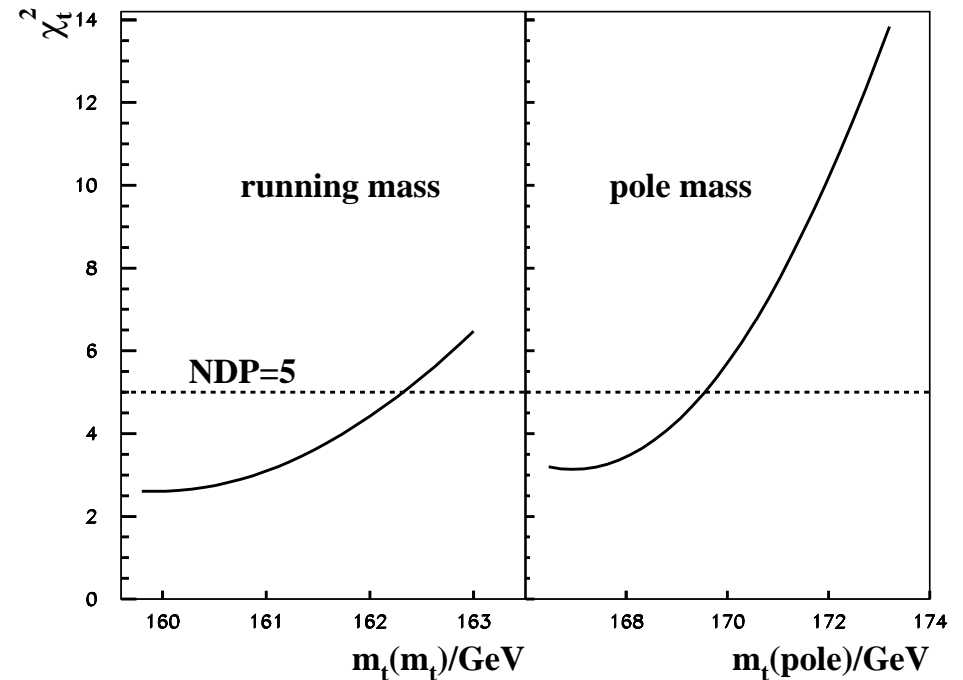
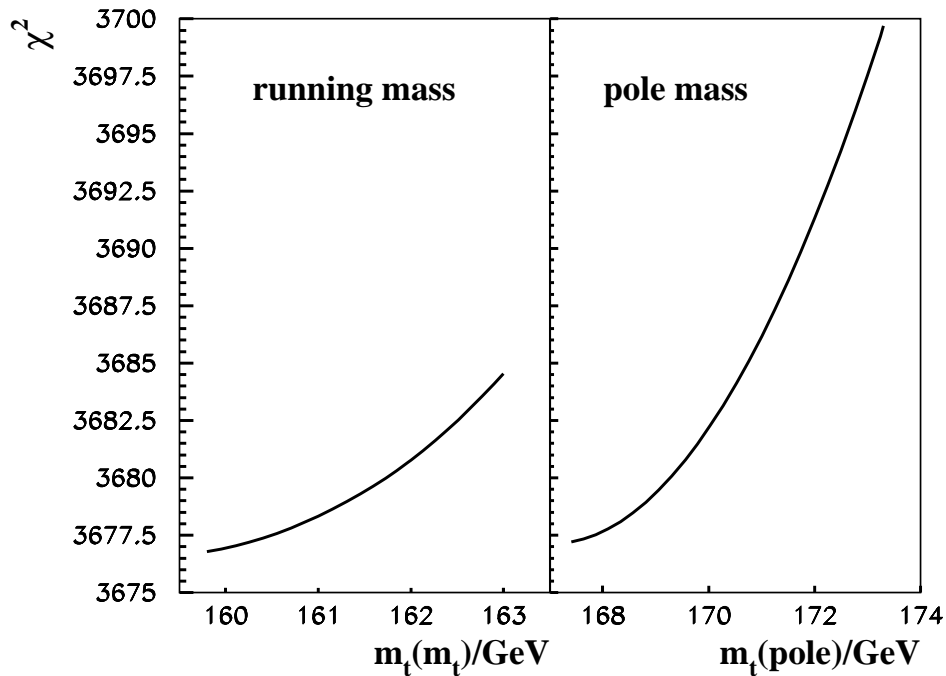
1

$\overline{\text{MS}}$ mass

- NNLO cross section with running mass significantly improved
 - good apparent convergence of perturbative expansion
 - small theoretical uncertainty from scale variation

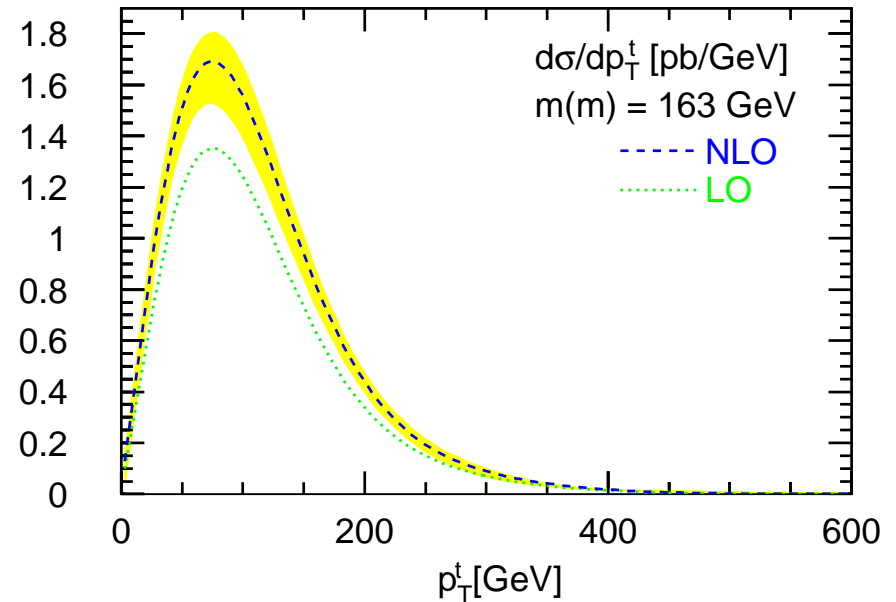
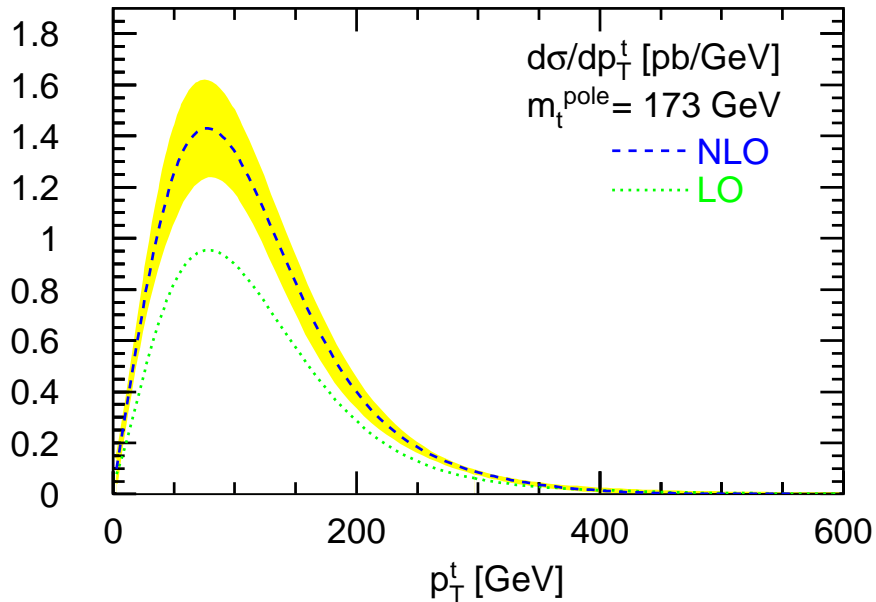
Top cross section data in ABM12 fit

- Fit with correlations
 - $g(x)$ and $\alpha_s(M_Z)$ already well constrained by global fit (no changes)
 - for fit with $\chi^2/NDP = 5/5$ obtain value of $m_t(m_t) = 162.3 \pm 2.3$ GeV (equivalent to pole mass $m_t = 171.2 \pm 2.4$ GeV) Alekhin, Blümlein, S.M. '13
 - χ^2 -profile steeper for pole mass (bigger impact of top-quark data and greater sensitivity to theoretical uncertainty at NNLO)



Differential cross sections

NLO in QCD



- Running mass for differential distributions show same features, e.g. p_T^t -distribution Dowling, S.M. '13

Top-quark pairs with one jet

- Mass measurement from shape of distribution for invariant mass of $t\bar{t} + 1\text{jet}$ system

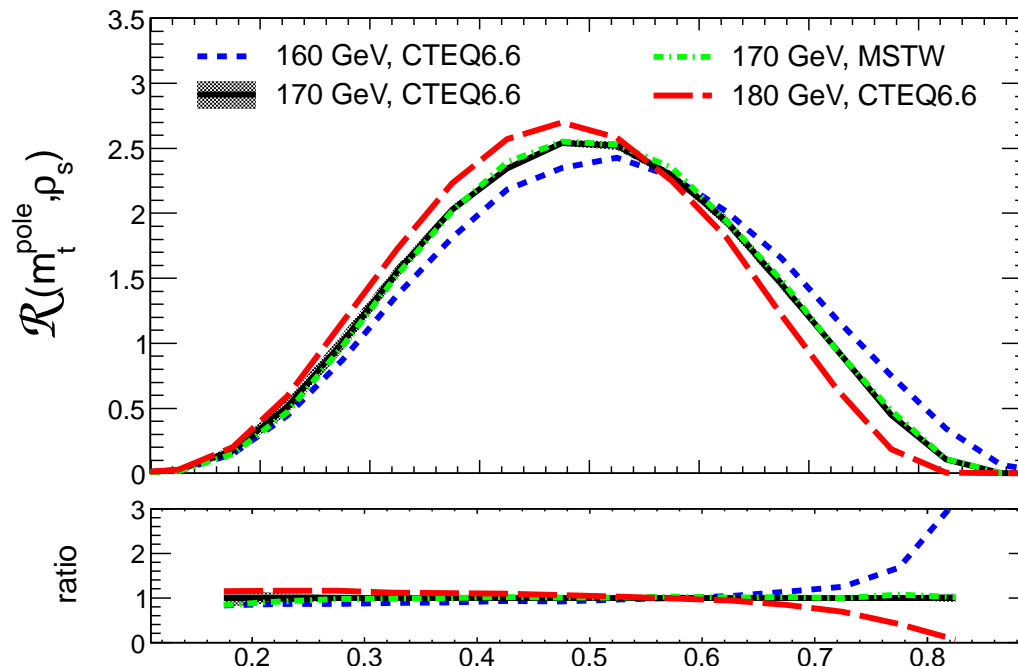
Alioli, Fernandez, Fuster, Irlles, S.M., Uwer, Vos '13

- variable $\rho_s = \frac{2 \cdot m_0}{\sqrt{s_{t\bar{t}+1\text{jet}}}}$ with fixed scale $m_0 = 170 \text{ GeV}$

- Normalized-differential $t\bar{t} + \text{jet}$ cross section

$$\mathcal{R}(m_t, \rho_s) = \frac{1}{\sigma_{t\bar{t}+1\text{jet}}} \frac{d\sigma_{t\bar{t}+1\text{jet}}}{d\rho_s}(m_t, \rho_s)$$

- significant mass dependence for $0.4 \leq \rho_s \leq 0.5$ and $0.7 \leq \rho_s$

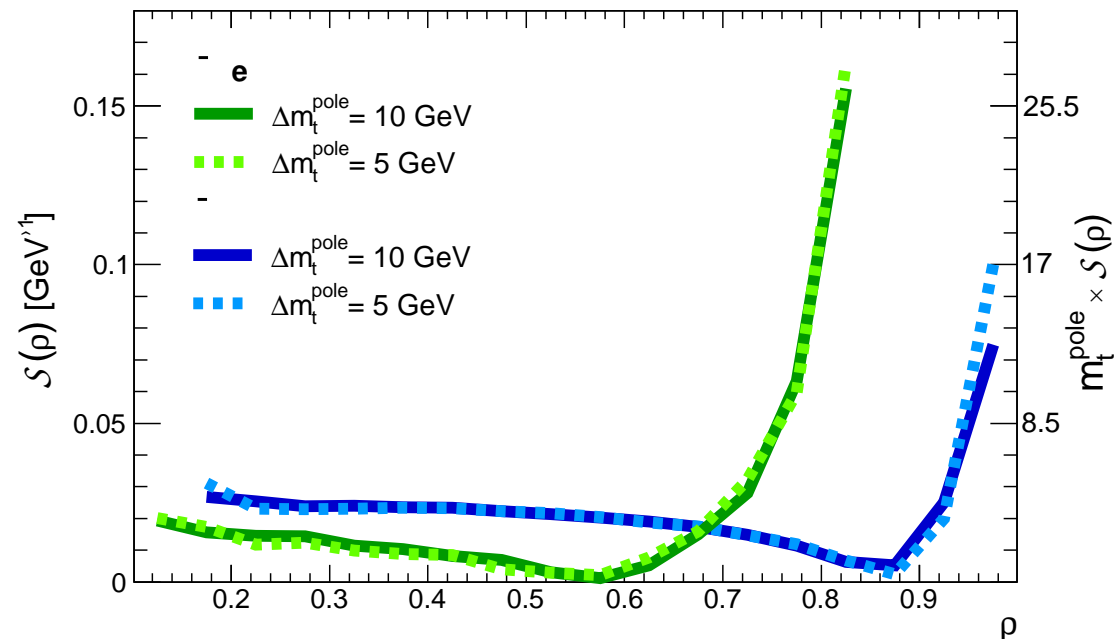


Mass sensitivity

- Differential cross section $\mathcal{R}(m_t, \rho_s)$
 - good perturbative stability, small theory uncertainties, small dependence on experimental uncertainties, ...
- Sensitivity to top-quark mass very good

$$\left| \frac{\Delta \mathcal{R}}{\mathcal{R}} \right| \simeq (m_t \mathcal{S}) \times \left| \frac{\Delta m_t}{m_t} \right|$$

- increased sensitivity for system $t\bar{t} + \text{jet}$ compared to $t\bar{t}$



Summary

Theory predictions for rates and shapes

- Precision predictions of inclusive and differential observables for LHC measurements
- QCD corrections at NNLO + electroweak corrections at NLO
- Quality of perturbative expansion depends on scheme for top-quark mass
- Short-distance masses $\overline{MS} m(m)$ or $m^{\text{MSR}}(R)$ show better convergence and scale stability

Top-quark mass

- Top quark mass is parameter of Standard Model Lagrangian
- Measurements of m_t require careful definition of observable
- Correlations in data analysis are important, e.g. with α_s and PDFs
- Relation of Monte Carlo mass m^{MC} to pole mass with additional theory uncertainty Δm_t

Future tasks

- Joint effort theory and experiment