

Theoretical status of triple Higgs coupling studies at the LHC

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Outline



Introduction

- SM Higgs pair production at the LHC
- Status of the studies of the triple Higgs coupling in the SM
- BSM studies of the triple Higgs coupling

Outlook

Motivation: probing the Brout-Englert-Higgs potential



• From the scalar potential before EWSB: with a scalar SU(2)-doublet field ϕ , $Y_{\phi} = 1$:



 $V(\phi) = -m^2 |\phi|^2 + \lambda |\phi|^4$



Motivation: probing the Brout-Englert-Higgs potential



■ Quartic Higgs coupling: not accessible at current or foreseen collider energies (≤ 100 TeV) [Plehn, Rauch, Phys.Rev. D72 (2005) 053008]

• Triple Higgs coupling: the ultimate probe of the shape of the SM Brout-Englert-Higgs potential

• BSM physics: triple Higgs coupling can depend on gauge parameters (for example in SUSY) and be enhanced

Historical recap: the early studies



- Early studies at lepton colliders:
 - Studies at a 2 TeV e^+e^- collider: SM triple Higgs coupling could be measured with a 10% accuracy for a light Higgs, in $\nu_e \bar{\nu}_e HH$ and W^+W^-HH modes (VBF modes) [Boudjema, Chopin, Z.Phys. C73 (1996) 85]
 - Complementary SM and MSSM studies: in addition to weak boson fusion, associated Higgs production with a weak gauge boson and triple Higgs production; 500 GeV e⁺e⁻ collider could be enough for a 20% accuracy on the triple Higgs coupling [Djouadi, Kilian, Muhlleimer, Zerwas, Eur.Phys.J. C10 (1999) 27]
- Early studies at the LHC:
 - First study at the LHC: theoretical predictions for HH production in the main channels, in the SM and MSSM [Djouadi, Kilian, Muhlleitner, Zerwas, Eur.Phys.J. C10 (1999) 45]
 - Comprehensive analysis of the $b\bar{b}\gamma\gamma$ channel: with a very high luminosity (6000 fb⁻¹) $\lambda = 0$ can be excluded at 90% CL

[Baur, Plehn, Rainwater, Phys.Rev.Lett. 89 (2002) 151801; Phys.Rev. D67 (2003) 033003; Phys.Rev. D69 (2004) 053004]

SM Higgs pair production at the LHC



SM Higgs pair production at the LHC

Gluon fusion: the largest cross section

LO inclusive cross section known exactly (*t* + *b* loops) [Eboli *et al*, Phys.Lett. B197 (1987) 269; Glover, v.d. Bij, Nucl.Phys. B309 (1988) 282; Dicus, Kao, Willenbrock, Phys.Lett. B203 (1988) 457; Plehn, Spira, Zerwas, Nucl.Phys. B479 (1996) 46]

QCD corrections to inclusive rate in the low energy limit $\sqrt{s} \ll m_t$: NLO corrections [Dawson, Dittmaier, Spira, Phys.Rev. D58 (1998) 115012] + NNLO corrections (new in 2013!), +20% on top of

NLO rate [De Florian, Mazzitelli, Phys.Lett. B724 (2013) 306; Phys.Rev.Lett. 111 (2013) 201801]



NLO (NNLO) K-factor $\simeq 2$ (2.3)

\sqrt{s} [TeV]	$\sigma^{ m NLO}$ [fb]	$\sigma^{ m NNLO}$ [fb]
8	8.2	9.8
14	33.9	40.2
33	207.3	242
100	1417.8	1638

NNLL resummation: $\simeq +20 - 30\%$ on top of NLO cross section, scale dependence stabilized

[Shao, C.S. Li, H.T. Li, Wang, JHEP 1307 (2013) 169]

SM Higgs pair production at the LHC

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Gluon fusion: theoretical uncertainties



- $gg \rightarrow HH$ affected by sizeable uncertainties:
 - Scale uncertainty: calculated at NLO with $\frac{1}{2}\mu_0 \leq \mu_R$, $\mu_F \leq 2\mu_0$, $\mu_0 = M_{HH}$ $\Delta^{\text{scale}} \simeq +20\%(+12\%)/-17\%(-10\%)$ at $\sqrt{s} = 8(100)$ TeV
 - PDF uncertainty: gluon PDF at high-x less constrained, $\alpha_s(M_Z^2)$ uncertainty $\Delta_{90\% CL}^{PDF+\alpha_s} \simeq \pm 9\% (\simeq \pm 6\% \text{ at } 100 \text{ TeV})$ uncertainty
 - EFT approximation: NLO correction only known in a top mass expansion (new 2013!) ⇒ estimate of ±10% uncertainty [Grigo, Hoff, Melnikov, Steinhauser, Nucl.Phys. B875 (2013) 1]



Total uncertainty: $\simeq \pm 40\%$ ($\simeq \pm 30\%$ at 100 TeV) [J.B. *et al*, JHEP 1304 (2013) 151] With recent NNLO calculation, scale uncertainty reduced to $\pm 9\%(\pm 6\%)$ at 8 (100) TeV

[De Florian, Mazzitelli, Phys.Rev.Lett. 111 (2013) 201801]

SM Higgs pair production at the LHC

Vector boson fusion at NLO

 $pp \rightarrow qq \rightarrow qq WW/ZZ \rightarrow qqHH$: the second production channel at the LHC





LO inclusive cross section known for a while [Keung, Mod.Phys.Lett. A2 (1987) 765; Eboli *et al*, Phys.Lett. B197 (1987) 269; Dicus, Kao, Willenbrock, Phys.Lett. B203 (1988) 457; Dobrovolskaya, Novikov, Z.Phys. C52 (1991) 427]

QCD corrections: NLO corrections to inclusive rates and differential distributions [J.B. et al, JHEP 1304 (2013) 151] implemented in VBFNLO (and now publicly available!) [Arnold et al

Comput.Phys.Comm. 180 (2009) 1661; J.B. et al, arXiv:1404.3940



 $\simeq +7\%$ correction (similar to single Higgs case)

\sqrt{s} [TeV]	$\sigma^{ m NLO}$ [fb]
8	0.49
14	2.01
33	12.05
100	79.55

SM Higgs pair production at the LHC

Vector boson fusion: theoretical uncertainties



$qq \rightarrow HHqq$ is a clean process:

- Scale uncertainty: calculated at NLO with $\frac{1}{2}\mu_0 \leq \mu_R, \mu_F \leq 2\mu_0, \mu_0 = Q_{W/Z}$; $\Delta^{\text{scale}} \simeq +3\%(+2\%)/-2\%(-1\%)$ at $\sqrt{s} = 8(33)$ TeV Good precision compared to LO $\Delta^{\text{scale}} \simeq \pm 10\%$
- PDF uncertainty: total $\Delta_{90\% CL}^{PDF+\alpha_s} \simeq +7\%/-4\%$ ($\simeq +5\%/-4\%$ at 33 TeV)



Total uncertainty: $\simeq +8\%/-5\%$ (14 TeV) [J.B. *et al*, JHEP 1304 (2013) 151]

NNLO QCD corrections in the structure function approach: +0.5% on top of the NLO result, scale uncertainty at the percent level [L. Liu-Sheng *et al*, Phys.Rev. D89 (2014) 073001]

SM Higgs pair production at the LHC

Monte Carlo tools and parton shower



Progress in 2014: Monte-Carlo tools including parton shower:

- $gg \rightarrow HH$ merged to 1 jet: HERWIG++ implementation of HH + 1j production with real radiation merged to parton shower $\Rightarrow 10\%$ theoretical uncertainty on the efficiencies of the cuts, much better than unmerged samples [Maierhöfer, Papaefstathiou, JHEP 1403 (2014) 126]
- All main processes interfaced with parton shower in the aMC@NLO framework: fully differential predictions at NLO for all channels [Frederix et al, Phys.Lett. B732 (2014) 142]



SM Higgs pair production at the LHC

Status of the studies of the *HHH* coupling in the SM

Parton level analysis: overview of the main channels



Where to look for HH production? production cross section small \Rightarrow use $H \rightarrow b\bar{b}$ decay channel at least once to retain some signal; foreseen luminosity at the LHC of 3000 fb⁻¹



4 interesting final states a priori:

- *bbW*(→ ℓν)*W*(→ ℓν): difficult because of MET, not promising [J.B. et al, JHEP 1304 (2013) 151]
- bbW(→ ℓν)W(→ 2j): difficult because of MET, but less than above, worth doing it?
- $b\bar{b}\gamma\gamma$: rates very small, lots of fake photon identification, still promising?
- $b\bar{b}\tau\tau$: rates small, but quite promising and under consideration by experimental collaborations

see also CMS projections at HL-LHC [CMS Collaboration, arXiv:1307.7135] and ATLAS projections [ATLAS Collaboration, ATL-PHYS-PUB-2012-004, 2013-007, 2013-014]

Remark: analyses presented in the following have been performed using the $gg \rightarrow HH$ production channel, HH + 2j (using also VBF process) analyses have just started

[Dolan, Englert, Greiner, Spannowsky, Phys.Rev.Lett. 112, 101802 (2014)]

Triple Higgs coupling sensitivity in the production channels



How sensitive are the three main channels to the HHH coupling?

- VBF mode is the most sensitive channel
- Identical shape when increasing the center-of-mass energy but reduced sensitivity



[J.B. et al, JHEP 1304 (2013) 151; see also Djouadi, Kilian, Mühlleitner, Zerwas, Eur.Phys.J. C10 (1999) 45-49]

Status of the studies of the triple Higgs coupling in the SM J. Baglio – *HHH* coupling at the LHC: theory status

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Signal analysis in $b\bar{b} au au$ final state [Dolan, Englert, Spannowsky, JHEP 1210

(2012) 112]



Jet substructure analysis, the major improvement : fatjet analysis with boosted kinematics to distinguish in jet substructure the signal from large QCD backgrounds

[Butterworth, Davison, Rubin, Salam, Phys.Rev.Lett. 100 (2008) 242001]

the idea: define a large cone size ("fatjet") and then work backward through the jet to define and separate softer subjets

Cut strategy: kinematic acceptance cuts + boosted topology cuts + Fat jet cuts

Results with a SHERPA/MADEVENT+HERWIG++ simulation:

 $S/B\simeq 0.5, 95$ signal events for 1000 fb $^{-1}$

• Adding one jet in the final state (*hhj* $\rightarrow b\bar{b}\tau\tau j$): with the same techniques, $S/B \simeq 1.5$

• With the addition of kinematic bounding variables: 60% accuracy in trilinear Higgs coupling determination at 3 ab⁻¹ [Barr, Dolan, Engler, Spannowsky, Phys.Lett. B728 (2014) 308]

• With kinematic acceptance cuts + boosted topology cuts only and more optimistic $M_{\tau\tau}$ window: [J.B. *et al.*, JHEP 1304 (2013) 151]

Optimistic expected significance at 14 TeV, $\mathcal{L} = 3000 (300)$ fb⁻¹: S/ $\sqrt{B} = 9.37 (2.97)$, 330 (33) signal events

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Optimistic expected significance at 14 TeV, $\mathcal{L}=3000~(300)~\text{fb}^{-1}\text{:}$ $S/\sqrt{B}=9.37~(2.97),\,330~(33)$ signal events

Signal analysis in $bar{b}\gamma\gamma$ final state [J.B. *et al*, JHEP 1304 (2013) 151]



Parton level analysis: Pythia 6 using $gg \rightarrow HH$ matrix elements from HPAIR, rates rescaled to (N)NLO through *K*-factors, tag efficiency of 70% (*b*), fake photons with a rough detector simulation (Delphes)

Cut strategy: kinematic acceptance cuts + boosted topology cuts



Rough detector level expected significance at 14 TeV, ${\cal L}=3000~fb^{-1}$: $S/\sqrt{B}=6.46,47$ signal events

See also a study at high energy LHC (33 and 100 TeV) in [Yao, arXiv:1308.6302]

Others channels, more improvements



• Using ratio of cross sections: similar structure for higher-order corrections in $\sigma(gg \rightarrow H)$ and $\sigma(gg \rightarrow HH) \Rightarrow$ uncertainties on their ratio C_{HH} much more reduced $\Delta^{\mu}C_{HH} \simeq \pm 2\%$, $\Delta^{\text{PDF}}C_{HH} \simeq \pm 2\%$ [Goertz, Papaefstahiou, Yang, Zurita, JHEP 1306 (2013) 016]

Very promising confidence interval of $\simeq +30\%/-20\%$ on the reduced triple Higgs coupling $\lambda = \lambda_{HHH}/\lambda_{HHH}^{\rm SM}$ when the three previous search channels are naively combined

- Multivariate analysis in $b\bar{b}\gamma\gamma$: improved significance and probe of λ_{HHH} within 40% uncertainty at LHC 14 TeV with 3 ab⁻¹ [Barger, Everett, Jackson, Shaughnessya, Phys.Lett. B728 (2014) 433]
- Signal analysis in $b\bar{b}W(\rightarrow \ell\nu)W(\rightarrow jj)$ final state: a cut-based analysis with jet substructure technique and then improved with BDT multivariate analysis \Rightarrow promising result of $S/\sqrt{S+B} = 2.4$ with 9 events at 600 fb⁻¹
- New from April 2014, 4b analysis! with jet substructure analysis, set a 95% CL limit $\lambda_{HHH} \leq 1.2$ at 3 ab⁻¹ [de Lima, Papaefstathiou, Spannowsky, arXiv:1404.7139]

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BSM studies of the triple Higgs coupling

Triple Higgs couplings in the 2HDM of type II



Disclaimer: this is one (biased) example of the various BSM studies on the market

Two-Higgs Doublet Model (2HDM): SM + 1 additional Higgs doublet \Rightarrow **5 Higgs bosons:** 2 CP-even *h/H*, 1 CP-odd *A*, 2 charged H^{\pm} (CP-conserving case) Type II \Leftrightarrow 1 Higgs doublet coupling to up-type fermion, the other to down-type fermions (example: the MSSM)

Using latest exp contraints and th constraints: *hhh* coupling cannot be enhanced, non standard triple Higgs couplings can reach $5 \times g_{bhh}^{SM}$ at 2σ [J.B, Eberhardt, Nierste, Wiebusch, arXiv:1403.1264]



Large enhancement in $\sigma(gg \rightarrow hh)$ due to resonant H production possible

[J.B, Eberhardt, Nierste, Wiebusch, arXiv:1403.1264]

See also [Moretti et al, JHEP 0502 (2005) 024; Arhrib et al, JHEP 0908 (2009) 035; Arhrib, Ferreira, Rui Santos, JHEP 1403 (2014) 053]

BSM studies of the triple Higgs coupling

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A (short) selection of other BSM studies

Disclaimer: there has been a lot of activities in *HH* production regarding to BSM theories in the past few years. I apologize here for the missing papers, this is a limited selection

Strong sector and anomalous Higgs couplings [Contino et al, JHEP 1005 (2010) 089, JHEP 1208 (2012) 154;

Kribs, Martin, Phys.Rev. D86 (2012) 095023]

- Anomalous ttH coupling effects [Nishiwaki, Niyogi, Shivaji, JHEP 1404 (2014) 011]
- MSSM studies: 1.45 enhancement factor for $gg \rightarrow H_{\rm SM-like}H_{\rm SM-like}$ in the most fouried promotes space ratio and for $gg \rightarrow H_{\rm SM-like}$ with the most fourier space ratio and for the space ratio and the space ratio

favored parameter space region, see [Cao, Heng, Shang, Wan, Yang, JHEP 1304 (2013) 134]

- NMSSM studies:
 - 0.7 to 2.4 enhancement factor for gg → H_{SM-like} H_{SM-like} in the most favored parameter space region [Cao, Heng, Shang, Wan, Yang, JHEP 1304 (2013) 134]
 - sizeable enhancement in $\sigma \times BR$ predictions in $gg \to h_i h_j \to b\bar{b}\tau\tau$, $b\bar{b}\gamma\gamma$ for 1 SM-like Higgs boson and a lighter Higgs state [Ellwanger, JHEP 1308 (2013) 077]
 - One-loop corrections to trilinear Higgs couplings in the real NMSM [Nhung, Mühlleitner, Streicher, Walz, JHEP 1311 (2013) 181]

• Resonant new physics in *HH* production:

- generic new physics [Dolan, Englert, Spannowsky, Phys.Rev. D87 (2013) 5, 055002]
- new Higgs states analysis [Liu, Wang, Zhu, arXiv:1310.3634; Arhrib, Ferreira, Rui Santos, JHEP 1403 (2014) 053; J.B., Eberhardt, Nierste, Wiebusch, arXiv:1403.1264]
- jet substructure technique, case study of massive KK graviton [Gouzevitch et al, JHEP 1307 (2013) 148]
- SM + 2 singlets: large enhancement in $gg \rightarrow H_{\rm SM}H_{\rm SM}$ [Ahriche, Arhrib, Nasri, JHEP 1402 (2014) 042]
- Distinguishing BSM models with *hhh* couplings: combined analysis of λ_{hhh} and λ_{hVV} through their ratio can help to distinguish between several BSM physics models [Efrati, Nir, arXiv:1401.0935]
- Exotics: pair production with color-octet scalars [Heng, Shang, Zhu, JHEP 1402 (2014) 083], Minimal Dilaton Model [Cao, He, Wu, Zhang, Zhu, JHEP 1401 (2014) 150], etc.

BSM studies of the triple Higgs coupling



Summary and outlook



Trilinear Higgs coupling at the LHC:

- Major news from 2012: the observation of a scalar particle at the LHC compatible with the SM Higgs boson
- Higgs couplings measurements era has began:
 HHH coupling of utmost importance for the scalar potential measurements
- HH production channels status: 2013 has seen major improvements in the QCD corrections
 - VBF process now at NLO (total rates and differential distributions) and NNLO in the approximation of the structure function, Higgs-strahlung at NNLO (total rates)

 \Rightarrow total theoretical uncertainty <10% in VHH and VBF channels

- Gluon fusion channel at NNLO+NNLL in the infinite top mass limit for the total rate, top mass expansion at NLO \Rightarrow scale uncertainty down to $\pm 8\%$ at 14 TeV
- HH Parton level analysis: jet substructure technique is the 2013 major improvement $b\bar{b}\tau\tau$ channel really promising even already at $\mathcal{L} = 300 \text{ fb}^{-1}$ $b\bar{b}\gamma\gamma$ may also be very interesting at $\mathcal{L} = 3000 \text{ fb}^{-1}$
- **BSM activities:** lots of studies on the market, large enhancements in the triple Higgs couplings and/or SM-like *hh* production are possible
- Stay tuned, more to come with improvements towards a full NLO calculation for gg → HH including the differential distributions!

Thank you!



More details on the analyses presented



• Signal analysis in $b\bar{b}\tau\tau$:

Main backgrounds considered:

- continuum production: $pp \to b\bar{b}\tau\tau$; $b\tau^+\nu_\tau \bar{b}\tau^-\bar{\nu}_\tau$ (mainly from $t\bar{t}$ production)
- ► $ZH \rightarrow b\bar{b}\tau\tau$ production

Define the subjet separation in the fat jet: using mass-drop condition,

$$m_{j_1} \leq 0.66 m_j \& \min(p_{T,j_1}^2, p_{T,j_2}^2) / m_j^2 \Delta R_{j_1,j_2}^2 > 0.09$$

 τ reconstruction efficiency of 80%

• Signal analysis in $b\bar{b}\gamma\gamma$:

Main backgrounds considered:

- continuum production: $pp \rightarrow b\bar{b}\gamma\gamma$
- ► $t\bar{t}H$ production with $H \to \gamma\gamma$ and $t \to W^+ b$ decays, $ZH \to b\bar{b}\gamma\gamma$ production

• Signal analysis in $b\bar{b}W(\rightarrow \ell\nu)W(\rightarrow jj)$:

Main backgrounds considered:

- ▶ largest background: $pp \rightarrow t\bar{t}$ with semi-leptonic decays
- ► $W(\rightarrow \ell \nu)b\bar{b} + 2j$ production, $H(\rightarrow WW)b\bar{b}$ production and H + jj with misidentified jets