

NNLOPS with POWHEG & *MINLO*

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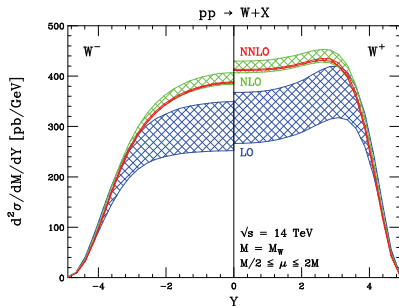
ZPW2014 on Monte Carlo Simulation
University of Zurich, 9 January 2014

- Quick introduction
 - MiNLO & NLOPS-merging
 - MiNLO: Multiscale Improved NLO [1206.3572]
 - NLOPS merging of X @ NLO and $X + 1$ jet @ NLO [1212.4504]
 - Matching NNLO with PS
 - NNLOPS simulation of Higgs production [1309.0017]
-
- News in POWHEG BOX [powhegbox.mib.infn.it]

Intro

Why NLO is important?

- first order where **rates are reliable**, and possible to attach **sensible theoretical uncertainties**
- **shapes** are, in general, **better described**
- sometimes corrections are sizeable, rates enhanced, etc.
- in these cases, NNLO is desirable (and lots of progress was done in 2013)



[Anastasiou et al., 0312266]

Limitations:

- Results are at the parton level only (5 final-state jets is the frontier)
- In regions where collinear emissions are important, they fail (no resummation)
 - ☞ desirable to **bring NLO accuracy into SMC**
 - * **not trivial**, because PS **already contains** R and V in LL approximation

However, POWHEG and MC@NLO solve this issue

- Choice of scale can become an issue when multijets in the final states
 - ☞ MiNLO originally thought to address this issue

Idea: *Modify $d\sigma_{\text{SMC}}$ in such a way that, expanding in α_s , one recovers the NLO cross section.*

[Nason '04]

$$B(\Phi_n) \Rightarrow \bar{B}(\Phi_n) = B(\Phi_n) + \frac{\alpha_s}{2\pi} \left[V(\Phi_n) + \int R(\Phi_{n+1}) d\Phi_r \right]$$

$$\Delta(t_m, t) \Rightarrow \Delta(\Phi_n; k_T) = \exp \left\{ -\frac{\alpha_s}{2\pi} \int \frac{R(\Phi_n, \Phi'_r)}{B(\Phi_n)} \theta(k'_T - k_T) d\Phi'_r \right\}$$

POWHEG “master formula” for the **hardest emission**:

$$d\sigma_{\text{POW}} = d\Phi_n \bar{B}(\Phi_n) \left\{ \Delta(\Phi_n; k_T^{\min}) + \Delta(\Phi_n; k_T) \frac{\alpha_s}{2\pi} \frac{R(\Phi_n, \Phi_r)}{B(\Phi_n)} d\Phi_r \right\}$$

+ *p_T -vetoing subsequent emissions*, to avoid double-counting.

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- inclusive observables: @NLO
- first hard emission: full tree level ME
- (N)LL resummation of collinear/soft logs

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☞ Notice: when doing $X + \text{jet(s)}$ @ NLO, $\bar{B}(\Phi_n)$ is **not finite** !

↪ need of a **generation cut** on Φ_n (or variants thereof)

↪ POWHEG for $H + 1$ jet **cannot be used** for inclusive Higgs production

MiNLO & NLOPS merging

MiNLO: Multiscale Improved NLO

[Hamilton,Nason,Zanderighi, 1206.3572]

- goal: method to a-priori choose scales in NLO computation
- relevant for processes with widely different scales (e.g. $X +$ jets close to Sudakov regions)

How?

- At LO, the CKKW procedure allows to take these effects into account: modify the LO weight $B(\Phi_n)$ in order to include (N)LL effects.

⇒ “Use CKKW” on top of NLO computation that potentially involves many scales

Next-to-Leading Order accuracy needs to be preserved

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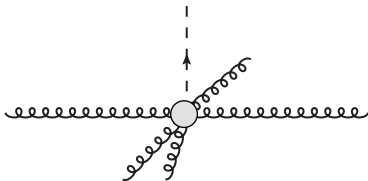
- 1 Scale dependence shows up at NNLO [“scale compensation”]:

$$O(\mu') - O(\mu) = \mathcal{O}(\alpha_S^{n+2}) \quad \text{if } O \sim \alpha_S^n \quad \text{at LO}$$

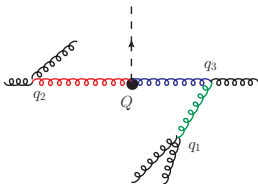
- 2 Away from soft-collinear regions, exact NLO recovered:

$$O_{\text{MiNLO}} = O_{\text{NLO}} + \mathcal{O}(\alpha_S^{n+2}) \quad [\text{i.e. } \alpha_S^n \text{ \& } \alpha_S^{n+1} \text{ reproduce plain NLO}]$$

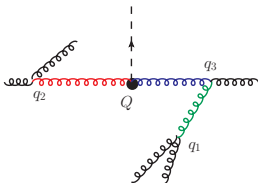
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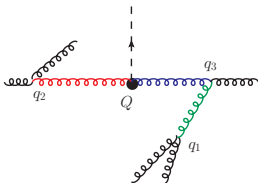


- Evaluate α_S at nodal scales

$$\alpha_S^n(\mu_R) B(\Phi_n) \Rightarrow \alpha_S(q_1) \alpha_S(q_2) \dots \alpha_S(q_n) B(\Phi_n)$$

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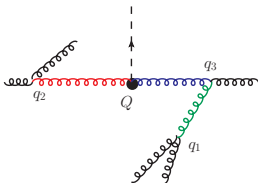
- Sudakov FFs in internal and external lines of Born “skeleton”

$$B(\Phi_n) \Rightarrow B(\Phi_n) \times \{\Delta(Q_0, Q)\Delta(Q_0, q_i)\dots\}$$

* Upon expansion, $\mathcal{O}(\alpha_S^{n+1})$ (log) terms are introduced, and need to be removed

$$B(\Phi_n) \Rightarrow B(\Phi_n) \left(1 - \Delta^{(1)}(Q_0, Q) - \Delta^{(1)}(Q_0, q_i) + \dots \right)$$

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$X + \text{jets}$ cross-section finite **without generation cuts**

$\leftrightarrow \bar{B}$ with MiNLO prescription: ideal starting point for NLOPS (POWHEG) for $X + \text{jets}$

Example, in 1 line: $H + 1$ jet

- Pure NLO:

$$d\sigma = \bar{B} d\Phi_n = \alpha_S^3(\mu_R) \left[B + \alpha_S^{(\text{NLO})} V(\mu_R) + \alpha_S^{(\text{NLO})} \int d\Phi_{\text{rad}} R \right] d\Phi_n$$

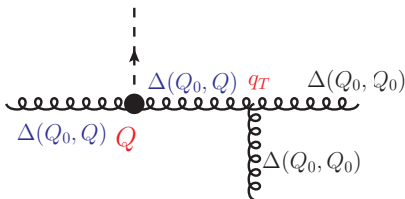
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- MiNLO:

$$\bar{B} = \alpha_S^2(M_H) \alpha_S(q_T) \Delta_g^2(q_T, M_H) \left[B \left(1 - 2\Delta_g^{(1)}(q_T, M_H) \right) + \alpha_S^{(\text{NLO})} V(\bar{\mu}_R) + \alpha_S^{(\text{NLO})} \int d\Phi_{\text{rad}} R \right]$$

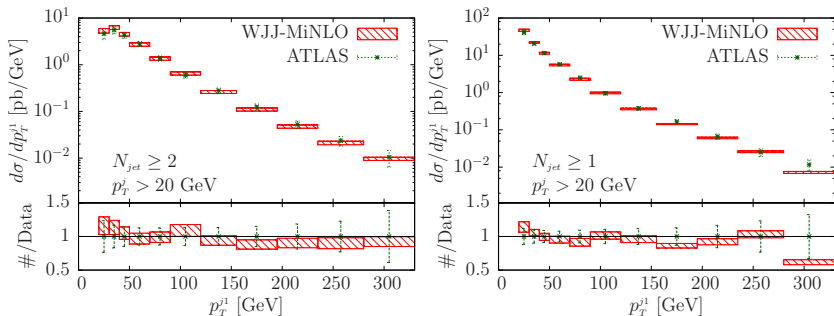


$$* \bar{\mu}_R = (M_H^2 q_T)^{1/3}$$

$$* \log \Delta_f(q_T, Q) = - \int_{q_T^2}^{Q^2} \frac{dq^2}{q^2} \frac{\alpha_S(q^2)}{2\pi} \left[A_f \log \frac{Q^2}{q^2} + B_f \right]$$

$$* \Delta_f^{(1)}(q_T, Q) = -\alpha_S^{(\text{NLO})} \frac{1}{2\pi} \left[\frac{1}{2} A_{1,f} \log^2 \frac{Q^2}{q_T^2} + B_{1,f} \log \frac{Q^2}{q_T^2} \right]$$

$$* \mu_F = Q_0 (= q_T)$$



- ☞ Start from $W + 2$ jets @ NLO, good agreement with data also when requiring $N_{jet} \geq 1$!

This is not possible with a standard NLO...

- Accuracy of $\text{BJ}+\text{MiNLO}$ for inclusive observables carefully investigated
- $\text{BJ}+\text{MiNLO}$ describes inclusive boson observables at order α_S (relative to $B + 0j$ at LO)
- However, to reach genuine NLO when inclusive, higher terms must be of relative order α_S^2 , *i.e.*

$$O_{\text{BJ}+\text{MiNLO}} = O_{\text{B@NLO}} + \mathcal{O}(\alpha_S^{m+2})$$

if O is inclusive ($\text{B@LO} \sim \alpha_S^m$).

- “Original MiNLO” contains **ambiguous** $\mathcal{O}(\alpha_S^{m+3/2})$ terms.
- Possible to improve $\text{BJ}+\text{MiNLO}$ such that NLO $B + 0j$ ($\text{NLO}^{(0)}$) is recovered, without spoiling NLO accuracy for $B + 1j$ ($\text{NLO}^{(1)}$).
 - proof based on careful comparisons of general resummation formula with MiNLO ingredients
 - need to include B_2 in MiNLO -Sudakovs
 - need to evaluate $\alpha_S^{(\text{NLO})}$ in $\text{BJ}+\text{MiNLO}$ at scale q_T , and $\mu_F = q_T$

Effectively it is like if we merged $\text{NLO}^{(0)}$ and $\text{NLO}^{(1)}$ samples, **without merging** different samples (no merging scale used).

“Improved” MiNLO & NLOPS merging

- Resummation formula

$$\frac{d\sigma}{dq_T^2 dy} = \sigma_0 \frac{d}{dq_T^2} \left\{ [C_{ga} \otimes f_a](x_A, q_T) \times [C_{gb} \otimes f_b](x_B, q_T) \times \exp S(q_T, Q) \right\} + R_f$$

- If $C_{ij}^{(1)}$ included and R_f is LO⁽¹⁾, then upon integration we get NLO⁽⁰⁾
- Take derivative, then compare with MiNLO :

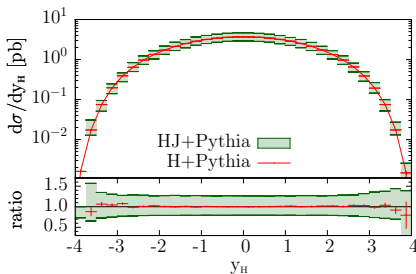
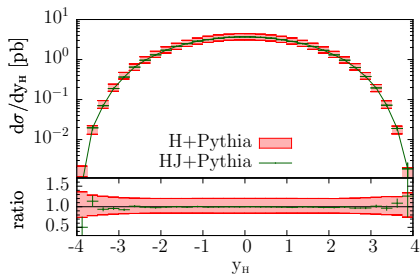
$$\sim \sigma_0 \frac{1}{q_T^2} [\alpha_S, \alpha_S^2, \alpha_S^3, \alpha_S^4, \alpha_S L, \alpha_S^2 L, \alpha_S^3 L, \alpha_S^4 L] \exp S(q_T, Q) + R_f \quad L = \log(Q^2/q_T^2)$$

- **highlighted terms** are needed to reach NLO⁽⁰⁾:

$$\int^{Q^2} \frac{dq_T^2}{q_T^2} L^m \alpha_S^n(q_T) \exp S \sim (\alpha_S(Q^2))^{n-(m+1)/2}$$

- if I don't include B_2 in MiNLO Δ_g , I miss a term $(1/q_T^2) \alpha_S^2 B_2 \exp S$
- upon integration, violate NLO⁽⁰⁾ by a term of relative $\mathcal{O}(\alpha_S^{3/2})$
- “wrong” scale in $\alpha_S^{(\text{NLO})}$ in MiNLO produces again same error

Alternative proof also available in the paper.

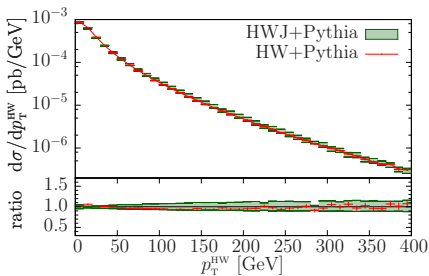
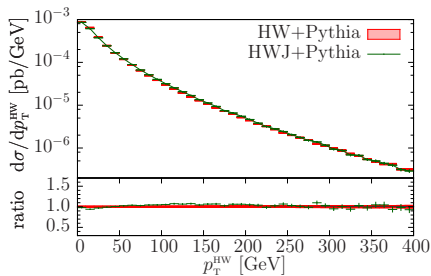


- “H+Pythia”: standalone POWHEG ($gg \rightarrow H$) + PYTHIA (PS level) [7pts band, $\mu = m_H$]
- “HJ+Pythia”: HJ-MiNLO* + PYTHIA (PS level) [7pts band, μ from MiNLO]

✓ very good agreement (both value and band)

👉 Notice: band is $\sim 20 - 30\%$

[Luisoni et al., 1306.2542]



- ✓ good agreement (notice that in HWJ-MinLO this observable is NLO)
- scale dependence in HW-POWHEG inherited from fully-inclusive cross-section (no `hfact` used).
- and there is a Sudakov peak (not noticeable in these plots)

NNLO Higgs production matched with PS

- HJ-MiNLO* differential cross section $(d\sigma/dy)_{\text{HJ-MiNLO}}$ is NLO accurate

$$W(y) = \frac{\left(\frac{d\sigma}{dy}\right)_{\text{NNLO}}}{\left(\frac{d\sigma}{dy}\right)_{\text{HJ-MiNLO}}} = \frac{c_2\alpha_S^2 + c_3\alpha_S^3 + c_4\alpha_S^4}{c_2\alpha_S^2 + c_3\alpha_S^3 + d_4\alpha_S^4} \simeq 1 + \frac{c_4 - d_4}{c_2}\alpha_S^2 + \mathcal{O}(\alpha_S^3)$$

- thus, reweighting each event with this factor, we get NNLO+PS
 - * obvious for y_H , by construction
 - * α_S^4 accuracy of HJ-MiNLO* in 1-jet region not spoiled, because $W(y) = 1 + \mathcal{O}(\alpha_S^2)$
 - * if we had $\text{NLO}^{(0)} + \mathcal{O}(\alpha_S^{2+3/2})$, 1-jet region spoiled because

$$[\text{NLO}^{(1)}]_{\text{NNLOPS}} = \text{NLO}^{(1)} + \mathcal{O}(\alpha_S^{4.5})$$

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* Variants for W are possible:

$$W(y, p_T) = h(p_T) \frac{\int d\sigma_A^{\text{NNLO}} \delta(y - y(\Phi))}{\int d\sigma_A^{\text{MiNLO}} \delta(y - y(\Phi))} + (1 - h(p_T))$$

$$d\sigma_A = d\sigma h(p_T), \quad d\sigma_B = d\sigma (1 - h(p_T)), \quad h = \frac{(\beta m_H)^2}{(\beta m_H)^2 + p_T^2}$$

- * $h(p_T)$ controls where the NNLO/NLO K-factor is spread
- * with above W , we get $(d\sigma/dy)_{\text{NNLOPS}} = (d\sigma_A/dy)_{\text{NNLO}} + (d\sigma_B/dy)_{\text{HJ-MiNLO}}$

In 1309.0017, we used

$$W(y, p_T) = h(p_T) \frac{\int d\sigma^{\text{NNLO}} \delta(y - y(\Phi)) - \int d\sigma_B^{\text{MiNLO}} \delta(y - y(\Phi))}{\int d\sigma_A^{\text{MiNLO}} \delta(y - y(\Phi))} + (1 - h(p_T))$$

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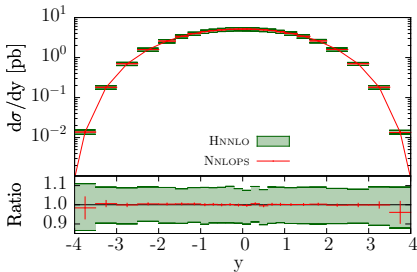
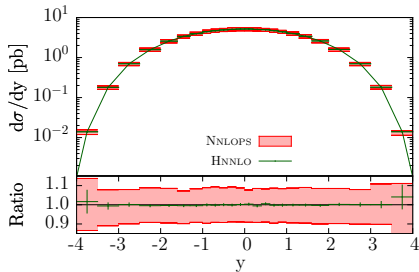
- we get exactly $(d\sigma/dy)_{\text{NNLOPS}} = (d\sigma/dy)_{\text{NNLO}}$ (no α_s^5 terms)
- we use $h(p_T^{j1})$

Run details:

- results are for 8 TeV LHC
- scale choices: NNLO input with $\mu = m_H/2$, HJ-MiNLO “core scale” m_H (other powers are at q_T)
- PDF: everywhere MSTW8NNLO
- NNLO always from HNNLO
- events reweighted at the LH level
- plots after k_T -ordered PYTHIA 6 at the PS level (hadronization and MPI switched off)

- NNLO with $\mu = m_H/2$, HJ-MiNLO “core scale” m_H
- $(7_{\text{Mi}} \times 3_{\text{NN}})$ pts scale var. in NNLOPS, 7pts in NNLO

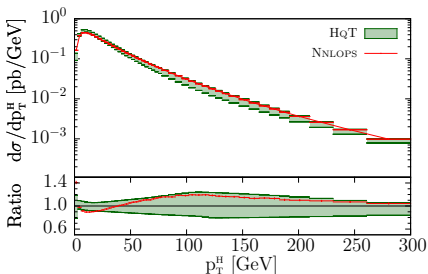
[NNLO from HNNLO, Catani, Grazzini]



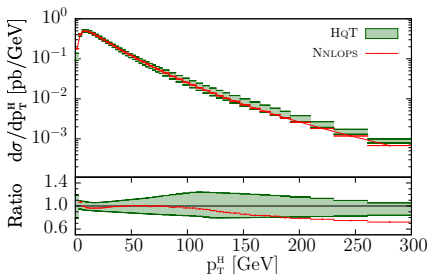
👉 Notice: band is 10%

[Until and including $\mathcal{O}(\alpha_S^4)$, PS effects don't affect y_H (first 2 emissions controlled properly at $\mathcal{O}(\alpha_S^4)$ by MiNLO+POWHEG)]

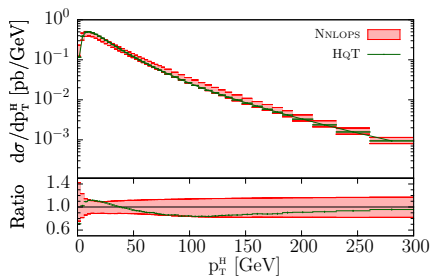
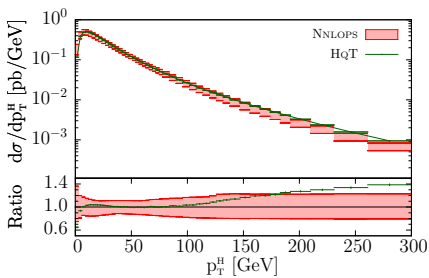
$\beta = \infty$ (W indep. of p_T)



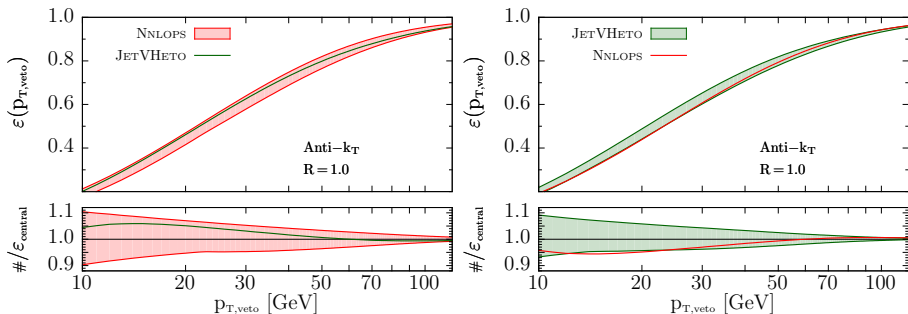
$\beta = 1/2$



- HqT: NNLL+NNLO, $\mu_R = \mu_F = m_H/2$ [7pts], $Q_{\text{res}} \equiv m_H/2$
- ✓ $\beta = 1/2$ & ∞ : uncertainty bands of HqT contain NNLOPS at low-/moderate p_T
- $\beta = 1/2$: HqT tail harder than NNLOPS tail ($\mu_{\text{HqT}} < \mu_{\text{MINLO}}$)
- $\beta = 1/2$: very good agreement with HqT resummation [“~ expected”, since $Q_{\text{res}} \equiv m_H/2$]

$\beta = \infty$ (W indep. of p_T)

 $\beta = 1/2$


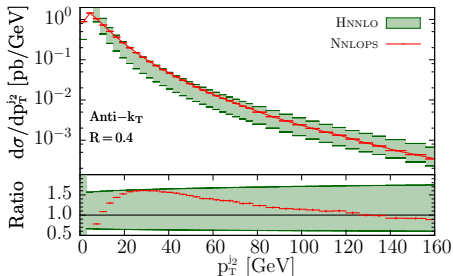
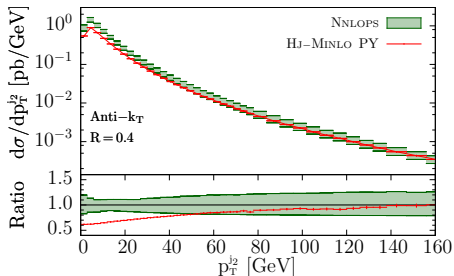
- HqT: NNLL+NNLO, $\mu_R = \mu_F = m_H/2$ [7pts], $Q_{\text{res}} \equiv m_H/2$
- $\beta = 1/2$: NNLOPS tail \rightarrow NLOPS tail [$W(y, p_T \gg m_H) \rightarrow 1$]
 larger band (affected just marginally by NNLO, so it's \sim genuine NLO band)



$$\epsilon(p_{T,\text{veto}}) = \frac{\Sigma(p_{T,\text{veto}})}{\sigma_{\text{tot}}} = \frac{1}{\sigma_{\text{tot}}} \int d\sigma \theta(p_{T,\text{veto}} - p_T^{j1})$$

- JetVHeto: NNLL resum, $\mu_R = \mu_F = m_H/2$ [7pts], $Q_{\text{res}} \equiv m_H/2$, (a)-scheme only
- nice agreement, differences never more than 5-6 %

☞ Separation of $H \rightarrow WW$ from $t\bar{t}$ bkg: x-sec binned in N_{jet}
 0-jet bin \Leftrightarrow jet-veto accurate predictions needed !



- This is LO (and $\mu_{\text{NNLO}} = m_H$)
- as expected, at high k_T , NNLOPS reproduces the underlying HJ-MiNLO (which for j_2 means HJ-POWHEG)
- at small p_T ($\lesssim m_H/2$), effect of $W(p_T, j_1)$ noticeable (j_1 just harder than j_2)
- scale variation in NNLOPS greatly underestimated (usual effect with POWHEG in “NLO-jet” region; here even more pronounced, since NNLO-reweighted)

POWHEG-BOX status update

POWHEG BOX: technical improvements

- * V2 ready, new processes and new developments there.
- * `MINLO` will be the default for X +jets processes.

Automation:

- **Interface to MadGraph 4** [Frederix]: automatically builds subprocesses list, B , B_{ij} , $B^{\mu\nu}$, R and large- N Born color structures.
 - Used to build the code for Hj and Hjj [Campbell, Ellis, Frederix, Nason, Oleari], with virtuals from MCFM.
- **interface to GoSam** [Luisoni, Nason, Oleari, Tramontano]: automatically write the code for 1-loop amplitudes, and interface it via BLHA
 - Used to study VH and VHj

PDF and scale uncertainties:

- Generate MC samples for different scale choices, and, even more, for different PDFs, is very time consuming
- Primitive reweighting facility now superseded by new mechanism [Hamilton,Nason,ER]
 - we need some feedback

Complicated processes & parallelization:

- Possible to run `POWHEG BOX` in parallel. Not only event generation, but also grid computation.
- details in repository [Parallel-grids]

- EW processes ($VVjj$, $\ell\ell jj$)
- last month: $ZZjj$, also with anomalous couplings

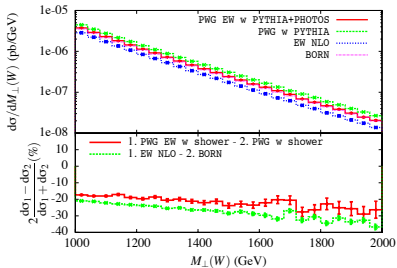
[Jaeger, Zanderighi, ...]
[Jaeger, Karlberg, Zanderighi, '13]

- DM+monojet

[Haisch, Kahlhoefer, ER]

- NLO QCD and NLO EW, for DY

[Bernaciak, Wackerroth'12 - Barze et al'12-'13]



- we started looking into problem with top p_T in $t\bar{t}$

- MiNLO & improved MiNLO:
 - original motivation: assign scales and Sudakov FF in $B + n$ jets NLO computations
 - ideal as starting point for POWHEG
 - $B + 1$ jet “improved” MiNLO allows to merge NLO⁽⁰⁾ and NLO⁽¹⁾ samples, **without the need of a merging scale**
 - ☞ merging for higher multiplicity requires further study
 - NNLOPS:
 - MiNLO allows to define a procedure to reach NNLOPS
 - **Shown first results for Higgs production**
 - ☞ NNLOPS doable for DY and $H + V$; more to learn ?
-
- Progress in POWHEG BOX:
 - list of processes steadily increasing
 - towards automation (via interfaces to MG4 / GoSam / ...?)
 - several technical improvements to keep up with theoretical and experimental needs
 - ↔ V2 essentially ready

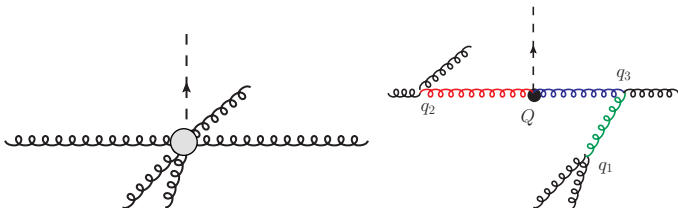
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Thanks for your attention!

Backup 1: CKKW in a nutshell

- ME weight $B(\Phi_n) \Rightarrow$ “most-likely” shower history (via k_T -algo): $Q > q_3 > q_2 > q_1 \equiv Q_0$



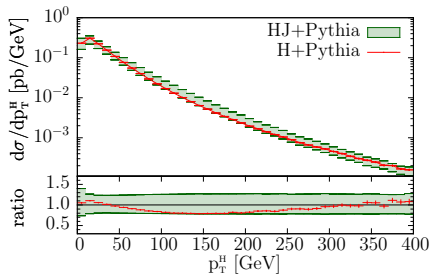
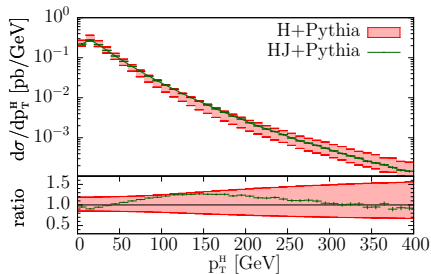
- New weight:

$$\alpha_S^5(Q)B(\Phi_3) \rightarrow \alpha_S^2(Q)B(\Phi_3) \frac{\Delta_g(Q_0, Q)}{\Delta_g(Q_0, q_2)} \frac{\Delta_g(Q_0, Q)}{\Delta_g(Q_0, q_3)} \frac{\Delta_g(Q_0, q_3)}{\Delta_g(Q_0, q_1)}$$
$$\Delta_g(Q_0, q_2)\Delta_g(Q_0, q_2)\Delta_g(Q_0, q_3)\Delta_g(Q_0, q_1)\Delta_g(Q_0, q_1)$$
$$\alpha_S(q_1)\alpha_S(q_2)\alpha_S(q_3)$$

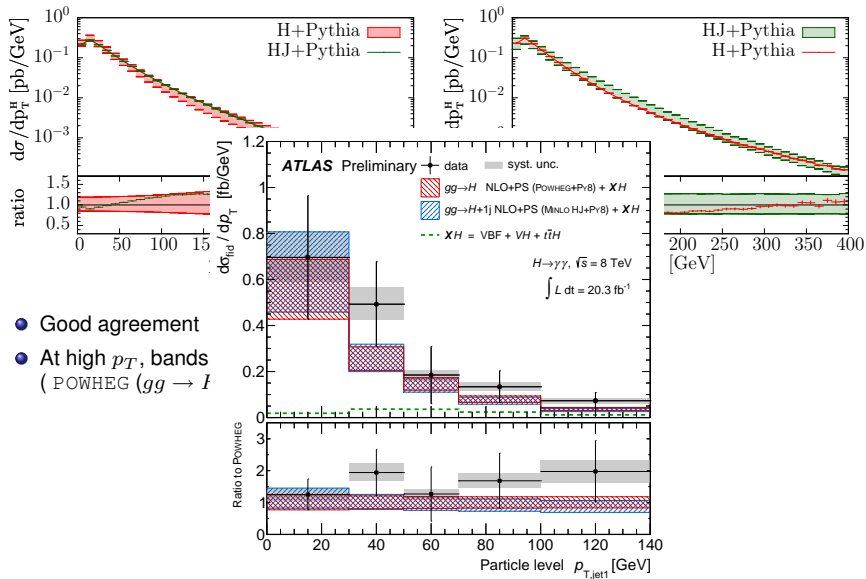
where typically

$$\log \Delta_f(q_T, Q) = - \int_{q_T^2}^{Q^2} \frac{dq^2}{q^2} \frac{\alpha_S(q^2)}{2\pi} \left[A_{1,f} \log \frac{Q^2}{q^2} + B_{1,f} \right]$$

- Fill phase space below Q_0 with **vetoed** shower



- Good agreement
- At high p_T , bands as expected (LO vs NLO)
(POWHEG ($gg \rightarrow H$) with $h_{\text{fact}} = m_H/1.2$, YR2)



- Good agreement
- At high p_T , bands (POWHEG ($gg \rightarrow H$))

MiNLO: All α_S in Born term are chosen with CKKW (local) scales q_1, \dots, q_n

$$\alpha_S^n(\mu_R)B \Rightarrow \alpha_S(q_1)\alpha_S(q_2)\dots\alpha_S(q_n)B$$

- Normal NLO structure ($\mu = \mu_R$):

$$\sigma(\mu) = \underbrace{\alpha_S^n(\mu)B}_{\text{Born}} + \underbrace{\alpha_S^{n+1}(\mu)\left(C + nb_0 \log(\mu^2/Q^2)B\right)}_{\text{Virtual}} + \underbrace{\alpha_S^{n+1}(\mu)R}_{\text{Real}}$$

- Explicit μ dependence of virtual term as required by RG invariance:

$$\alpha_S^n(\mu')B = \left[\alpha_S(\mu) - nb_0\alpha_S^{n+1}(\mu) \log(\mu'^2/\mu^2) \right] B + \mathcal{O}(\alpha_S^{n+2})$$

$$\text{Virtual}(\mu') = \text{Virtual}(\mu) + \alpha_S^{n+1}(\mu)nb_0 \log(\mu'^2/\mu^2) B + \mathcal{O}(\alpha_S^{n+2})$$

$$\Rightarrow \sigma(\mu') - \sigma(\mu) = \mathcal{O}(\alpha_S^{n+2})$$

- In MiNLO “scale compensation” kept if

$$\left(C + nb_0 \log(\mu_R^2/Q^2)B\right) \Rightarrow \left(C + nb_0 \log(\bar{\mu}_R^2/Q^2)B\right)$$

$$\text{with } \bar{\mu}_R^2 = (q_1 q_2 \dots q_n)^{2/n}$$

Few technicalities for original MiNLO:

- $\mu_F = Q_0$ (as in CKKW)
- Cluster with CKKW also V and R kinematics
 - Actual implementation uses FKS mapping for first cluster of Φ_{n+1}
 - Ignore CKKW Sudakov for 1st clustering of Φ_{n+1} (inclusive on extra radiation)
- Some freedom in choice of $\alpha_S^{(\text{NLO})}$ (entering V , R and $\Delta^{(1)}$):
 - * suggested average of LO α_S
 - * not free for “improved” MiNLO
- Used full NLL-improved Sudakovs (A_1, B_1, A_2)

Improved MiNLO: where are terms coming from when differentiating resum. formula?

$1/q_T^2$, always from integration in Sudakov

α_S from $C^{(0)} \times B_1, \dots$

α_S^2 from $C^{(0)} \times B_2, \dots$

...

$\alpha_S L$ from A_1 term in exponent

$\alpha_S L^2$ from A_2 term in exponent

...

p_T^H spectrum:

- “ $\mu_{\text{HJ-MiNLO}} = m_H, m_H, p_T$ ”
- At high p_T , $\mu_{\text{HJ-MiNLO}} = p_T$
- If $\beta = 1/2$, NNLOPS \rightarrow HJ-MiNLO at high p_T
- NNLO/NLO ~ 1.5 , because HNNLO with $\mu = m_H/2$, $\mu_{\text{HJ-MiNLO,core}} = m_H$

