



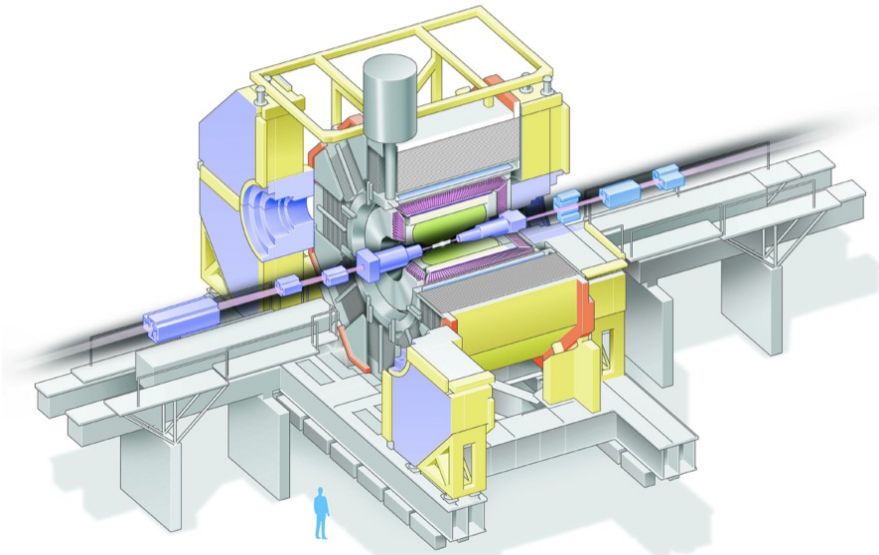
CP asymmetry studies from Belle for the CKM angle Φ_3

Minakshi Nayak (IIT Madras)

On behalf of Belle Collaboration

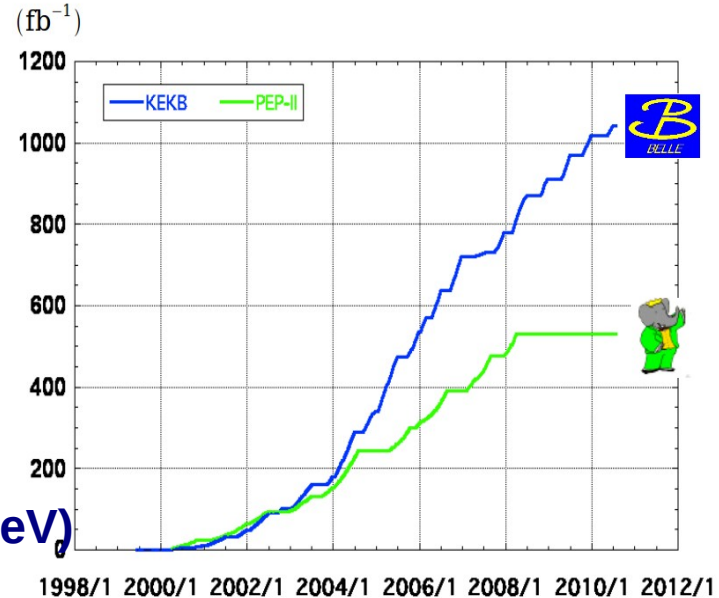
19th International Symposium on Particles, Strings and Cosmology (PASCOS 2013)

KEKB contributing to φ_3 determination.



KEKB asymmetric e^+e^- collider (3.5 on 8 GeV)

Integrated luminosity of B factories



$> 1 \text{ ab}^{-1}$
On resonance:
Y(5S): 121 fb^{-1}
Y(4S): 711 fb^{-1}
Y(3S): 3 fb^{-1}
Y(2S): 25 fb^{-1}
Y(1S): 6 fb^{-1}
Off reson./scan:
 $\sim 100 \text{ fb}^{-1}$

$\sim 550 \text{ fb}^{-1}$
On resonance:
Y(4S): 433 fb^{-1}
Y(3S): 30 fb^{-1}
Y(2S): 14 fb^{-1}
Off resonance:
 $\sim 54 \text{ fb}^{-1}$

KEK peak luminosity $2.11 \times 10^{34} \text{ cm}^{-2}\text{s}^{-1}$ (world record!)

Belle total data sample: 1000 fb^{-1}

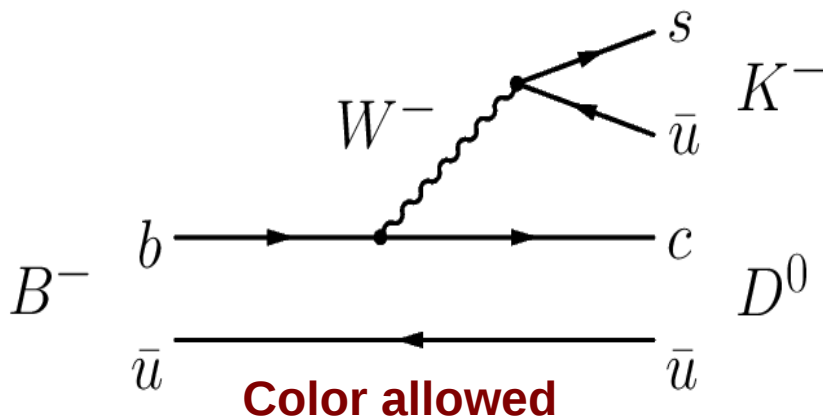
Y(4S) data sample : 711 fb^{-1} ($\sim 772 \text{ M } B\bar{B}$ pairs)

Belle data taking period: 1999 - 2010
Aim was to measure $\sin(2\varphi_1)$!

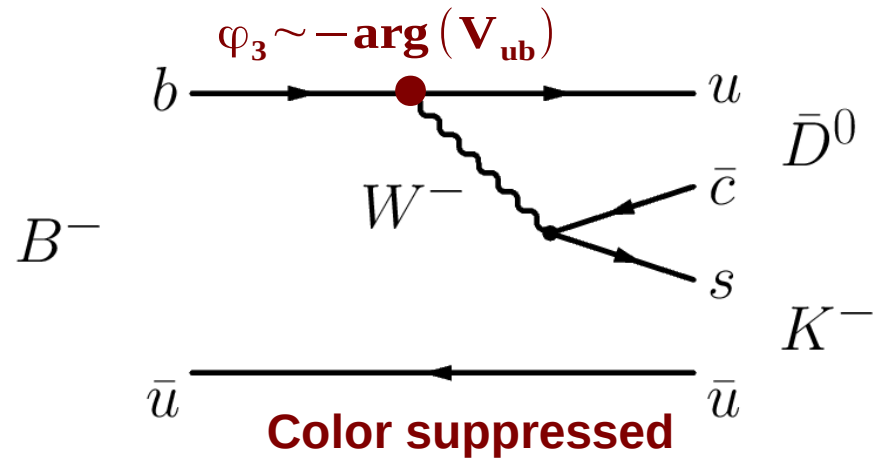
φ_3 measurements from $B^\pm \rightarrow DK^\pm$ decay

$$\varphi_3 \equiv \arg \left(\frac{V_{ud} V_{ub}^*}{-V_{cd} V_{cb}^*} \right) \sim -\arg(V_{ub})$$

Determination of Φ_3 via interference between $B^- \rightarrow D^0 K^-$ and $B^- \rightarrow \bar{D}^0 K^-$ using tree level B decay



$$B^- \rightarrow D^0 K^- \sim V_{cb} V_{us}^* \sim A\lambda^3$$



$$B^- \rightarrow \bar{D}^0 K^- \sim V_{ub} V_{cs}^* \sim A\lambda^3 (\rho + i\eta)$$

No loop contribution to $B \rightarrow DK$ decay.
Theoretically clean way to determine φ_3

Methods for φ_3 measurements from $B^\pm \rightarrow DK^\pm$ decay

Reconstruction of $D (D^0/\bar{D}^0)$ final states using

- CP eigenstates such as K^+K^- , $\pi^+\pi^-$, $K_S\pi^0$
GLW method (Gronau - London - Wyler) PLB 253, 483 (1991),
PLB 265, 172 (1991)
- Doubly - Cabibbo suppressed D decays such as $K\pi$, $K\pi\pi^0$
ADS method (Atwood - Dunietz - Soni) PRD 63, 036005 (2001)
- Three- body decays such as $D \rightarrow K_S\pi^+\pi^-$, $K_S K^+K^-$
GGSZ (Dalitz) method (Giri - Grossman - Soffer - Zupan)
GGSZ is the most accurate

Different B decay modes: DK , D^*K PRD 68, 054018 (2003)

different hadronic factors (r_B , δ_B) for each B decay mode

Extraction of Φ_3 by combining information from all measurements

Latest preliminary and published results from Belle

GLW analysis and results

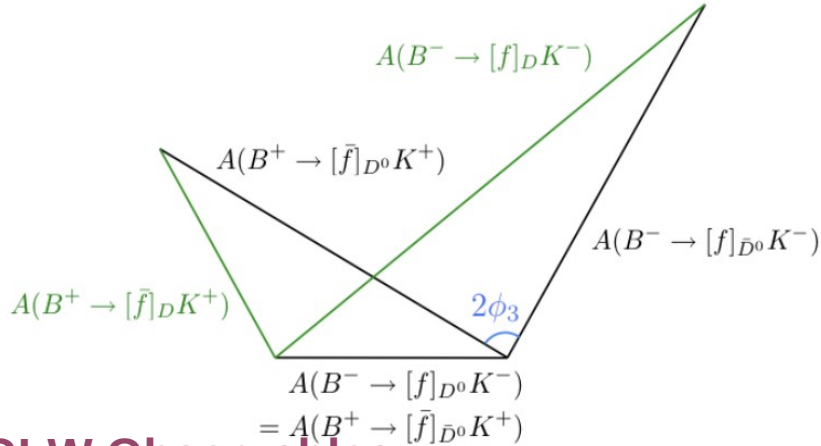
ADS analysis and results

Dalitz analysis and results

Combined Dalitz, ADS & GLW results

GLW and ADS Observables:

GLW Amplitude Triangles:



GLW Observables:

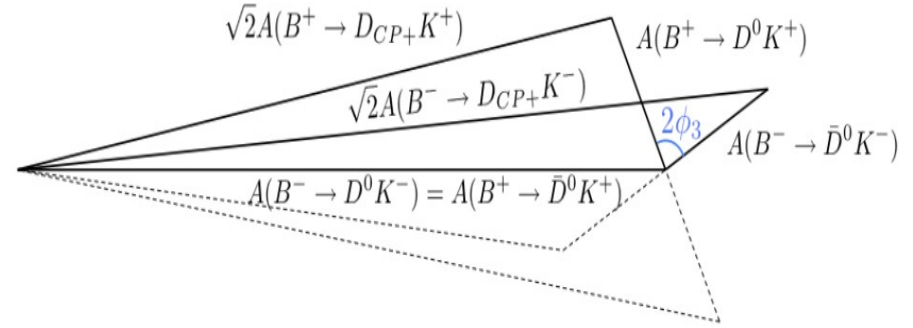
$$\begin{aligned} \mathcal{R}_{CP\pm} &\equiv \frac{\mathcal{B}(B^- \rightarrow D_{CP\pm} K^-) + \mathcal{B}(B^+ \rightarrow D_{CP\pm} K^+)}{\mathcal{B}(B^- \rightarrow D^0 K^-) + \mathcal{B}(B^+ \rightarrow \bar{D}^0 K^+)} \\ &= 1 + r_B^2 \pm 2r_B \cos \delta_B \cos \phi_3, \\ \mathcal{A}_{CP\pm} &\equiv \frac{\mathcal{B}(B^- \rightarrow D_{CP\pm} K^-) - \mathcal{B}(B^+ \rightarrow D_{CP\pm} K^+)}{\mathcal{B}(B^- \rightarrow D_{CP\pm} K^-) + \mathcal{B}(B^+ \rightarrow D_{CP\pm} K^+)} \\ &= \pm 2r_B \sin \delta_B \sin \phi_3 / \mathcal{R}_{CP\pm}, \end{aligned}$$

$$r_B = \left| \frac{A(B^- \rightarrow \bar{D}^0 K^-)}{A(B^- \rightarrow D^0 K^-)} \right|$$

$\delta_B = \text{strong phase}$

Input parameters

ADS Amplitude Triangles:



ADS Observables:

$$\begin{aligned} \mathcal{R}_{\text{ADS}} &\equiv \frac{\mathcal{B}(B^- \rightarrow [f]_D K^-) + \mathcal{B}(B^+ \rightarrow [\bar{f}]_D K^+)}{\mathcal{B}(B^- \rightarrow [\bar{f}]_D K^-) + \mathcal{B}(B^+ \rightarrow [f]_D K^+)} \\ &= r_B^2 + r_D^2 + 2r_B r_D \cos(\delta_B + \delta_D) \cos \phi_3, \\ \mathcal{A}_{\text{ADS}} &\equiv \frac{\mathcal{B}(B^- \rightarrow [f]_D K^-) - \mathcal{B}(B^+ \rightarrow [\bar{f}]_D K^+)}{\mathcal{B}(B^- \rightarrow [f]_D K^-) + \mathcal{B}(B^+ \rightarrow [\bar{f}]_D K^+)} \\ &= 2r_B r_D \sin(\delta_B + \delta_D) \sin \phi_3 / \mathcal{R}_{\text{ADS}}, \end{aligned}$$

$$r_D = \left| \frac{A(D^0 \rightarrow f)}{A(\bar{D}^0 \rightarrow f)} \right|$$

$\delta_D = \text{strong phase}$

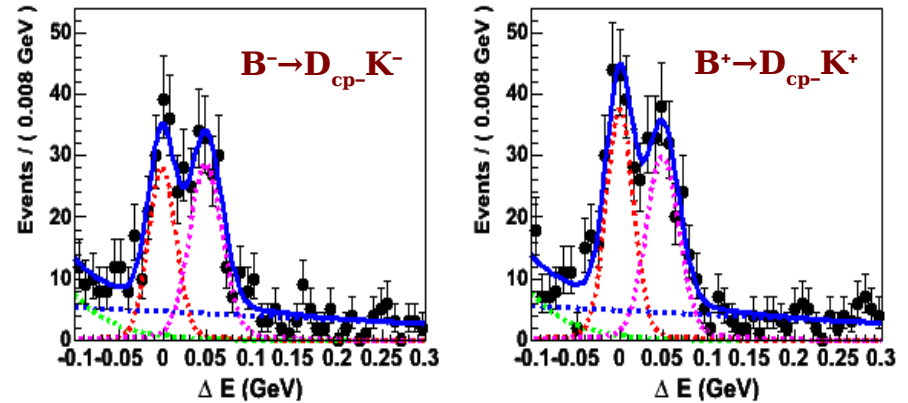
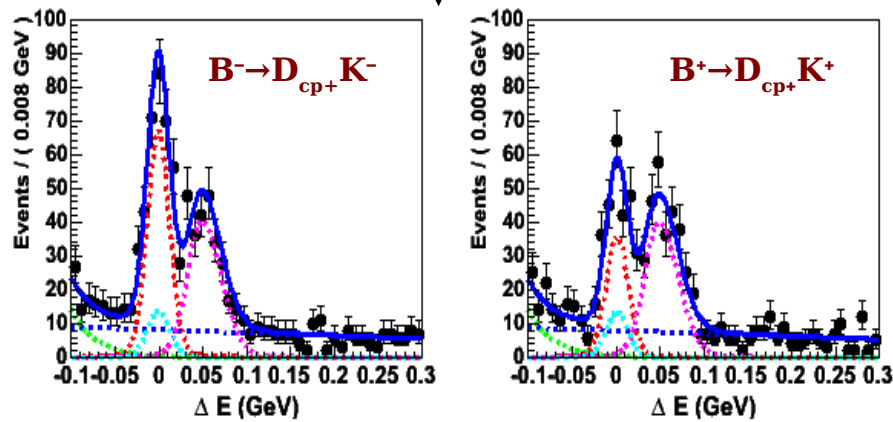
Additional Input from charm

Preliminary GLW results from Belle

Preliminary (LP2011) 772 M BB

$B \rightarrow DK, D \rightarrow KK, \pi\pi$ (CP+)

$B \rightarrow DK, D \rightarrow K_s \eta, K_s \pi^0$ (CP-)



Blue: total
 Red: signal peaks at 0
 Magenta: $D\pi$ peaks at 0.05
 Green: BB
 Dotted blue: qq
 Cyan: peaking BG (KKK contribution)

$$R_{CP^+} = 1.03 \pm 0.07 \pm 0.03$$

$$R_{CP^-} = 1.13 \pm 0.09 \pm 0.05$$

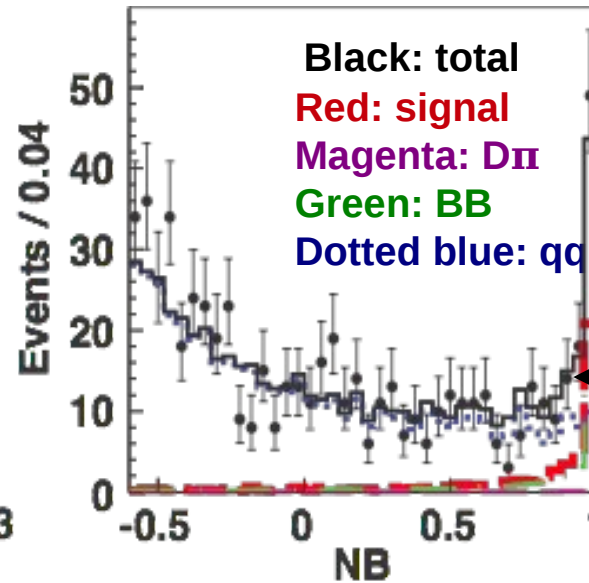
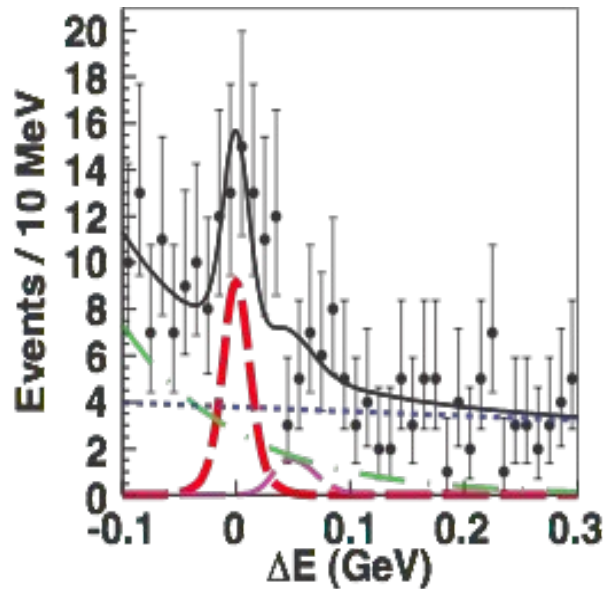
$$A_{CP^+} = +0.29 \pm 0.06 \pm 0.02$$

$$A_{CP^-} = -0.12 \pm 0.06 \pm 0.01$$

Published ADS results from Belle

Results from $B \rightarrow DK$, $D \rightarrow K \pi$ mode using 772 M $B \bar{B}$ pair events.

PRL 106, 231803 (2011)



Signal peaks at 1

More detail on
continuum suppression is
discussed in later slides

This was the first evidence of suppressed DK signal
obtained with a significance of 4.2σ

$$R_{DK} = [1.63_{-0.41}^{+0.44} (\text{stat})_{-0.13}^{+0.07} (\text{syst})] \times 10^{-2}$$

$$A_{DK} = [-0.39_{-0.28}^{+0.26} (\text{stat})_{-0.03}^{+0.04} (\text{syst})]$$

Preliminary ADS results from Belle

Preliminary (LP2011) 772 M B \bar{B}

Results from $B \rightarrow [K \pi]_{D\pi^0}, D^* \rightarrow D \pi^0 / D \gamma$ mode using 772 M B \bar{B} events

$D^* \rightarrow D \gamma$ signal seen at 3.5σ

Ratio to favored mode:

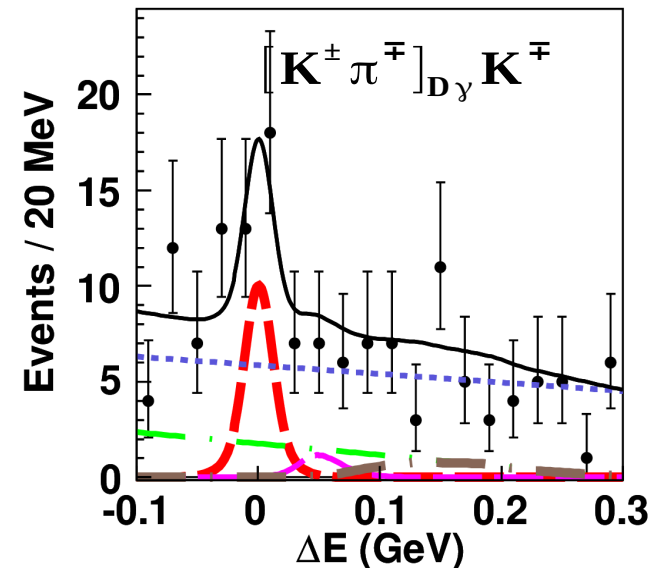
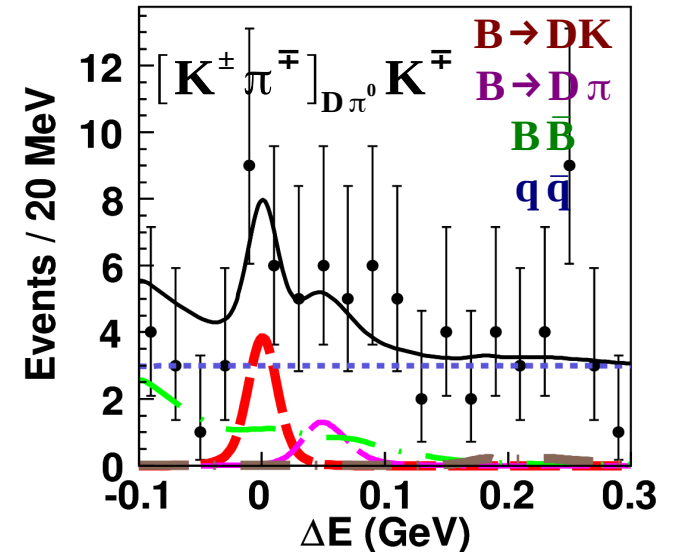
$$R_{D\pi^0} = (1.0_{-0.7}^{+0.8} (\text{stat})_{-0.2}^{+0.1} (\text{syst})) \times 10^{-2}$$

$$R_{D\gamma} = (3.6_{-1.2}^{+1.4} (\text{stat}) \pm 0.2 (\text{syst})) \times 10^{-2}$$

Asymmetry:

$$A_{D\pi^0} = (0.4_{-0.7}^{+1.1} (\text{stat})_{-0.3}^{+0.2} (\text{syst}))$$

$$A_{D\gamma} = (-0.51_{-0.29}^{+0.33} (\text{stat}) \pm 0.8 (\text{syst}))$$



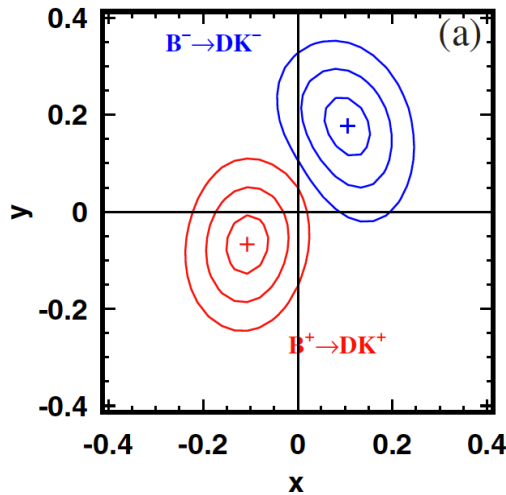
Review of GGSZ results from Belle:

Model dependent analysis

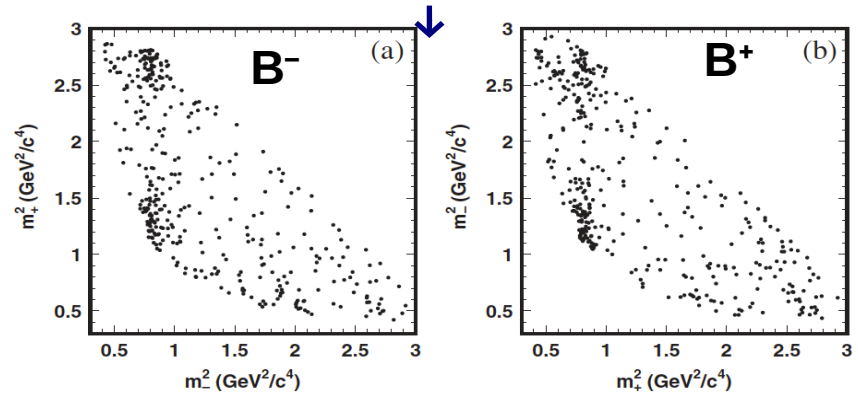
PRD81, 112002 (2010),

657M BB

$$x_{\pm} = r_B \cos(\delta_B \pm \gamma), \quad y_{\pm} = r_B \sin(\delta_B \pm \gamma)$$



Dalitz plot for $B^{\pm} \rightarrow [K_s \pi \pi]_D K^{\pm}$

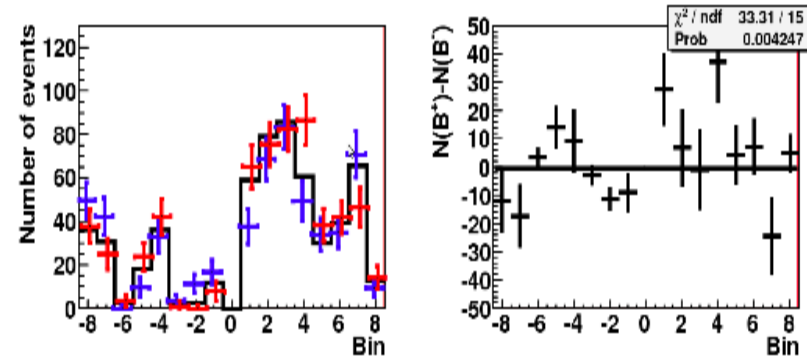


Model independent analysis

(Dividing Dalitz plot in to several bins)

PRD85, 112014 (2012),

772M BB



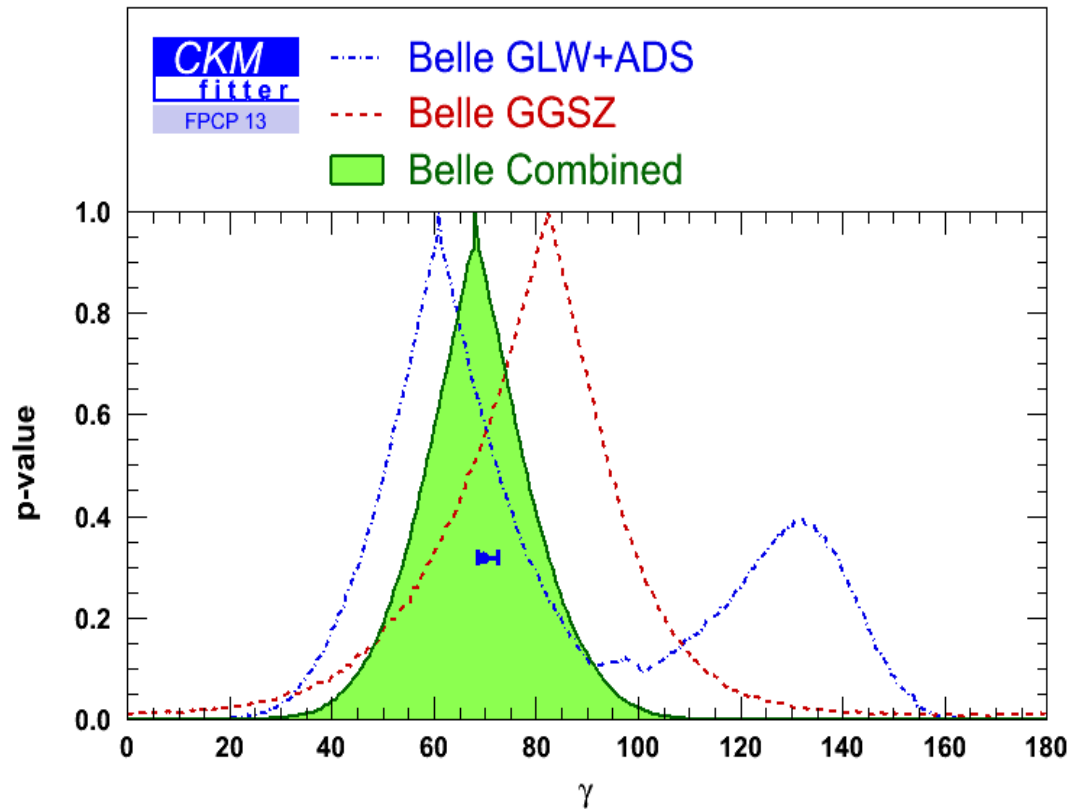
Parameter	$B^+ \rightarrow DK^+$ mode	$B^+ \rightarrow D^* K^+$ mode
ϕ_3	$(80.8^{+13.1}_{-14.8} \pm 5.0 \pm 8.9)^\circ$	$(73.9^{+18.9}_{-20.2} \pm 4.2 \pm 8.9)^\circ$
r	$0.161^{+0.040}_{-0.038} \pm 0.011^{+0.050}_{-0.010}$	$0.196^{+0.073}_{-0.072} \pm 0.013^{+0.062}_{-0.012}$
δ	$(137.4^{+13.0}_{-15.7} \pm 4.0 \pm 22.9)^\circ$	$(341.7^{+18.6}_{-20.9} \pm 3.2 \pm 22.9)^\circ$

combining both B modes:

$$\varphi_3 = (78.4^{+10.8}_{-11.6} \pm 3.6 (\text{syst.}) \pm 8.9 (\text{model}))^\circ$$

$$\varphi_3 = (77.3^{+15.1}_{-14.9} \pm 4.1 \pm 4.3)^\circ$$

Determination of φ_3 via GGSZ, ADS and GLW methods using Belle $D^0 K$ and $D^{*0} K$ results



combined result from Belle

$$\varphi_3 = (68 \pm 14)^\circ$$

New results from Belle

$B^\pm \rightarrow [K\pi\pi^0]_D K^\pm$ decay using ADS method

PRD 88, 091104(R) 2013

ADS $B^\pm \rightarrow [K\pi\pi^0]_D K^\pm$ analysis by Belle

observables measured:

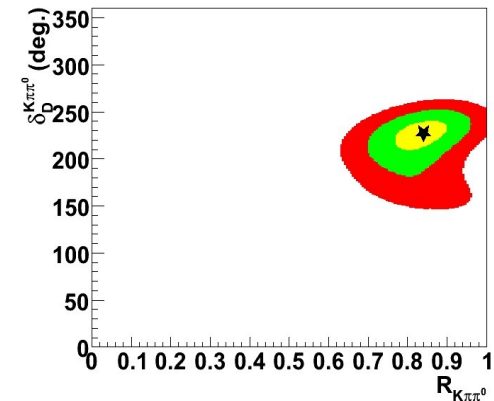
$$\begin{aligned}
 R_{ADS} &= \frac{B(B^- \rightarrow [K^+\pi^-\pi^0]_D K^-) + B(B^+ \rightarrow [K^-\pi^+\pi^0]_D K^+)}{B(B^- \rightarrow [K^-\pi^+\pi^0]_D K^-) + B(B^+ \rightarrow [K^+\pi^-\pi^0]_D K^+)} \\
 &= r_B^2 + r_D^2 + 2r_B r_D R_{K\pi\pi^0} \cos\phi_3 \cos(\delta_B + \delta_D^{K\pi\pi^0}), \\
 A_{ADS} &= \frac{B(B^- \rightarrow [K^+\pi^-\pi^0]_D K^-) - B(B^+ \rightarrow [K^-\pi^+\pi^0]_D K^+)}{B(B^- \rightarrow [K^+\pi^-\pi^0]_D K^-) + B(B^+ \rightarrow [K^-\pi^+\pi^0]_D K^+)} \\
 &= \frac{2r_B r_D R_{K\pi\pi^0} \sin\phi_3 \sin(\delta_B + \delta_D^{K\pi\pi^0})}{r_B^2 + r_D^2 + 2r_B r_D R_{K\pi\pi^0} \cos\phi_3 \cos(\delta_B + \delta_D^{K\pi\pi^0})}
 \end{aligned}$$

Here $R_{K\pi\pi^0}$ and $\delta_D^{K\pi\pi^0}$ are the coherence factor and average strong – phase difference for $D^0 \rightarrow K\pi\pi^0$ decay

CLEO measurements :

$$R_{K\pi\pi^0} = 0.84 \pm 0.07, \delta_D^{K\pi\pi^0} = (227_{-17}^{+14})^\circ.$$

Phys. Rev. D 80, 031105(R) (2009)

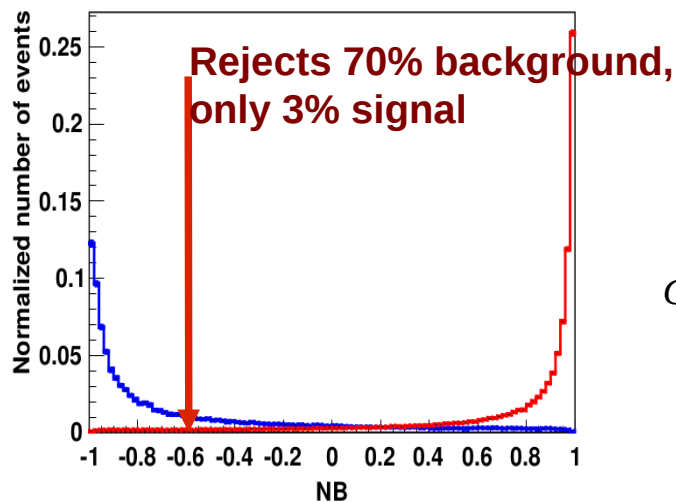


Main challenge of selection is Continuum Suppression

Continuum suppression via neural network output
(combining event topology parameters as inputs):

Nine topological variables used.

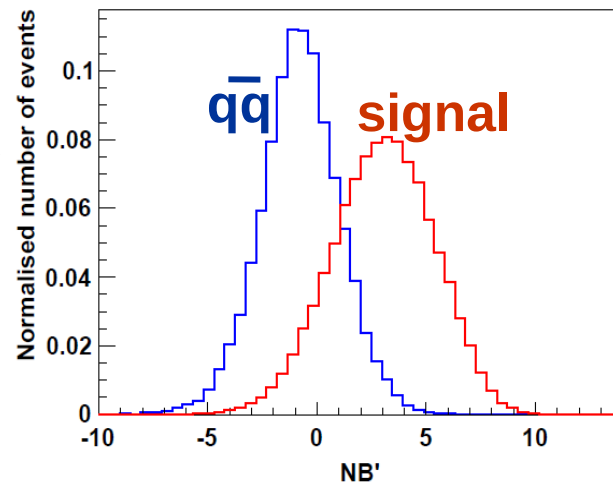
Network Output ↓



Transformed using ↓

$$C'_{NB} = \log \left(\frac{C_{NB} - C_{NB,min}}{C_{NB,max} - C_{NB}} \right)$$

Transformed Output
(To simplify fit using PDFs) ↓



Signal extraction via 2D fit between ΔE and C'_{NB}

Fit parameters :

– N_{sup} , N_{fav} , A_{ADS}

– N_{peak} , $N_{B\bar{B}}$, $N_{q\bar{q}}$

– PDF shape parameters ...

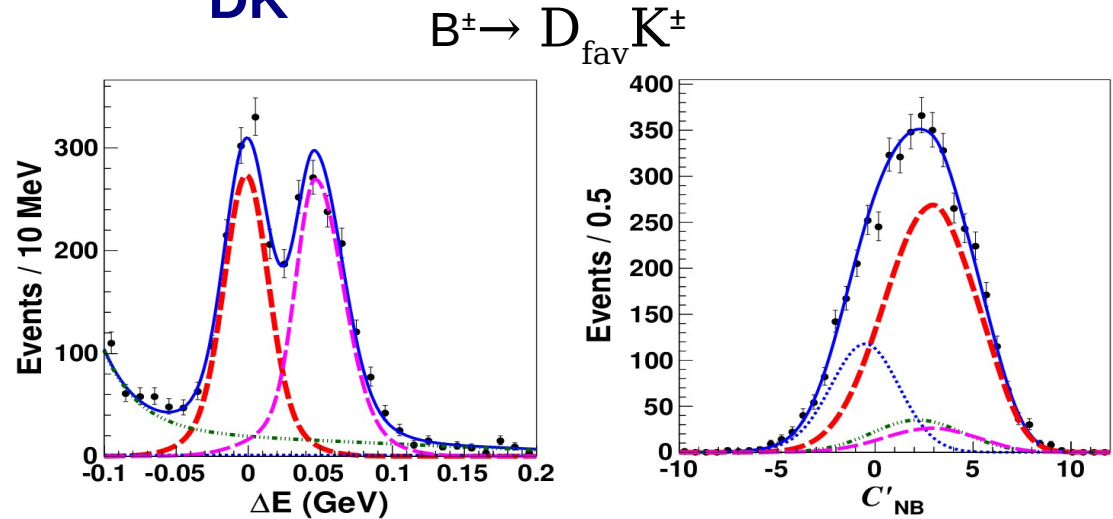
ADS $B^\pm \rightarrow [K\pi\pi^0]_D K^\pm$ result by Belle

PRD 88, 091104(R) 2013

R_{DK}

ΔE and C'_{NB} distributions: \rightarrow

Blue: total
 Red: DK signal
 Magenta: $D\pi$
 Green: $B\bar{B}$
 Dotted blue: $q\bar{q}$



Belle Result using 772 M $B\bar{B}$ pairs:

$$N_{sup} = 77 \pm 24$$

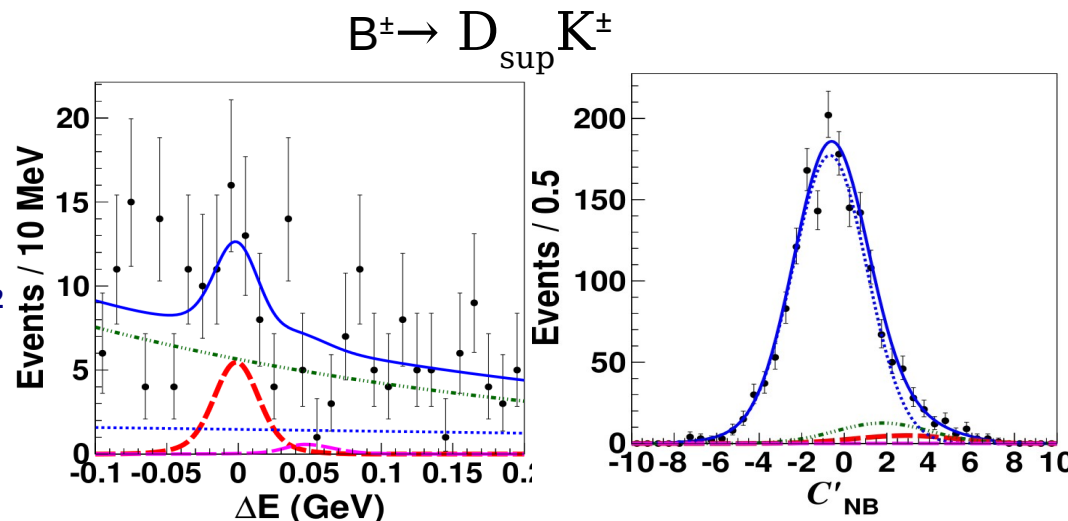
$$N_{fav} = 3871 \pm 90$$

Ratio to favored mode:

$$R_{DK} = (1.98 \pm 0.62 (\text{stat}) \pm 0.23 (\text{syst})) \times 10^{-2}$$

Babar Result using 474 M $B\bar{B}$ pairs:

$$R_{DK} = (0.91^{+0.82}_{-0.76} (\text{stat})^{+0.14}_{-0.37} (\text{syst})) \times 10^{-2}$$

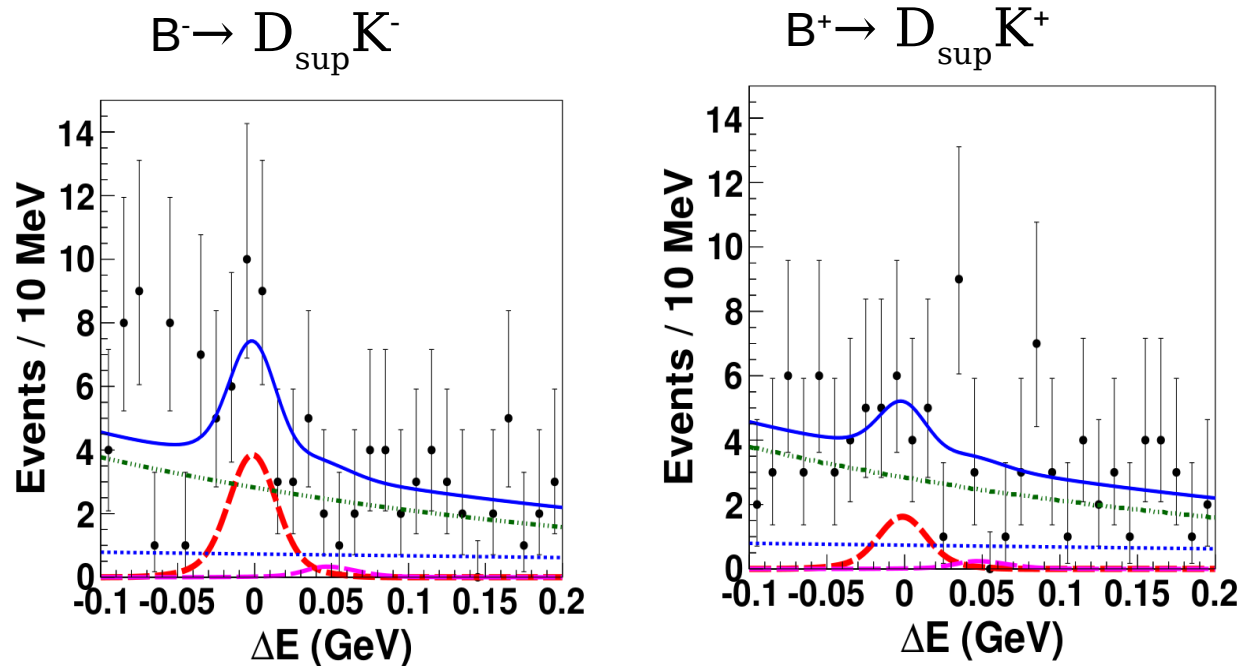


Suppressed DK signal significance 3.2σ

ADS $B^\pm \rightarrow [K\pi\pi^0]_D K^\pm$ result by Belle

PRD 88, 091104(R) 2013

A_{DK}



Belle Result using 772 million $B\bar{B}$ pairs :

$$R_{DK} = (1.98 \pm 0.62 (\text{stat}) \pm 0.23 (\text{syst})) \times 10^{-2}$$

$$A_{DK} = (0.41 \pm 0.30 (\text{stat}) \pm 0.05 (\text{syst}))$$

First $A_{DK}(D \rightarrow K\pi\pi^0)$ measurement !

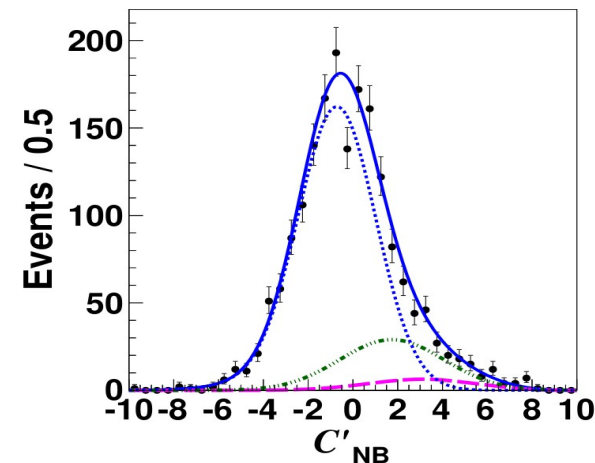
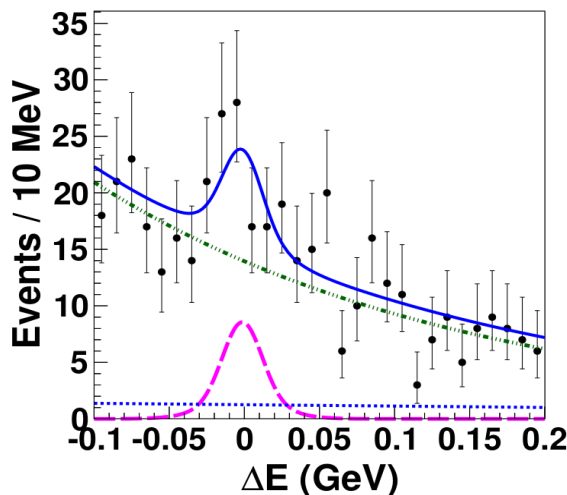
ADS $B^\pm \rightarrow [K\pi\pi^0]_D \pi^\pm$ result by Belle

PRD 88, 091104(R) 2013

$$B^\pm \rightarrow D_{\text{sup}} \Pi^\pm$$

ΔE and C' distributions: \rightarrow

Blue : total
 Magenta : $D\pi$ signal
 Green : $B\bar{B}$
 Dotted blue : $q\bar{q}$



Suppressed $D\pi$ signal significance 3.3σ

Small r_B . So, less sensitive to ϕ_3

$D\pi$ Results:

$$R_{D\pi} = (1.89 \pm 0.54 (\text{stat})_{-0.25}^{+0.22} (\text{syst})) \times 10^{-3}$$

$$A_{D\pi} = (0.16 \pm 0.27 (\text{stat})_{-0.04}^{+0.03} (\text{syst}))$$

First measurements!

D mixing corrections need to be taken in to account if above results are used to measure ϕ_3 (arXiv:1307.4384)

Conclusion:

*** Combined value of φ_3 measured by Belle : $(68 \pm 14)^\circ$**

*** New $[\mathbf{K} \pi \pi^0]_{\mathbf{D}}$ \mathbf{K} results :**

Suppressed signal seen with a significance of 3.2σ (including systematics)

$$\mathbf{R}_{\mathbf{DK}} = (1.98 \pm 0.62 (\text{stat}) \pm 0.23 (\text{syst})) \times 10^{-2}$$

$$\mathbf{A}_{\mathbf{DK}} = (0.41 \pm 0.30 (\text{stat}) \pm 0.05 (\text{syst}))$$

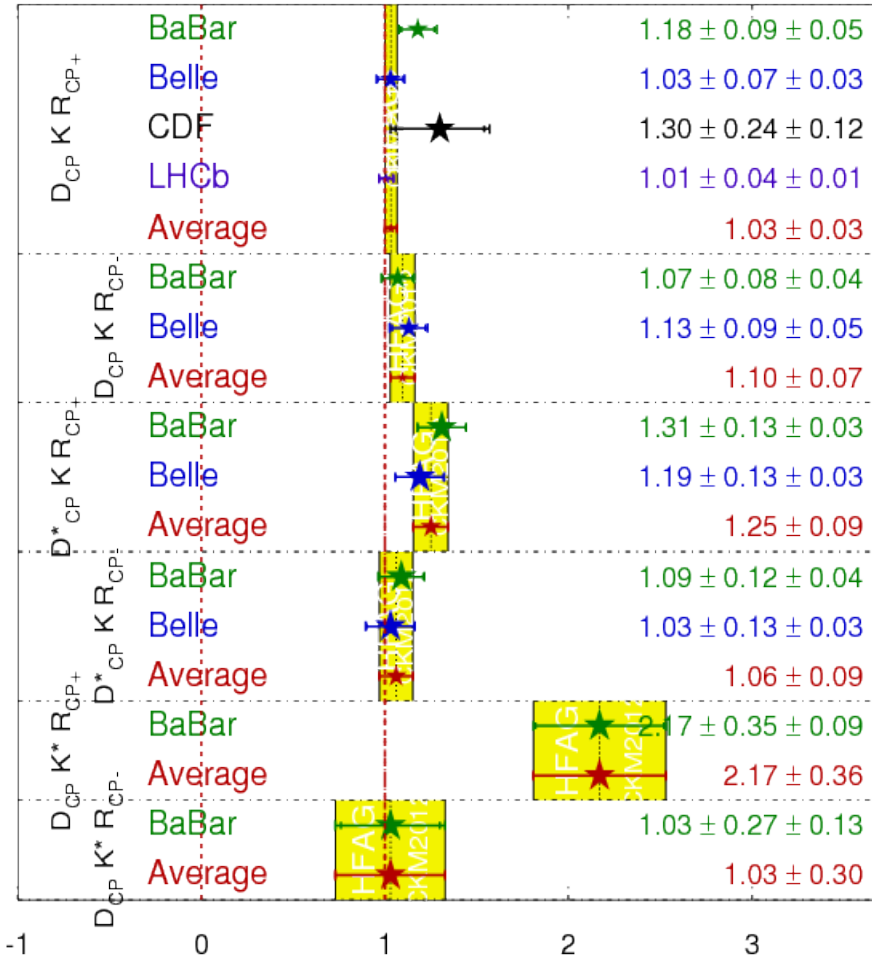
*** Several other analysis for measuring φ_3 using Belle full data sample are ongoing.**

THANK YOU!

GLW summary

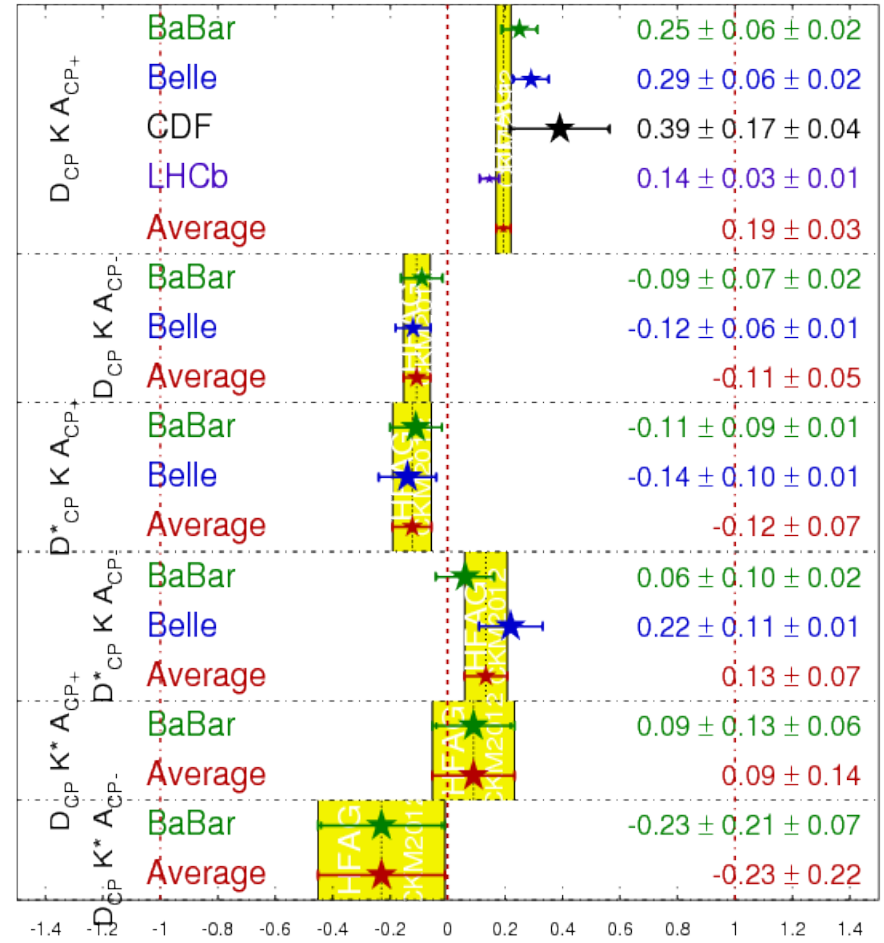
R_{CP} Averages

HFAG
CKM2012
PRELIMINARY



A_{CP} Averages

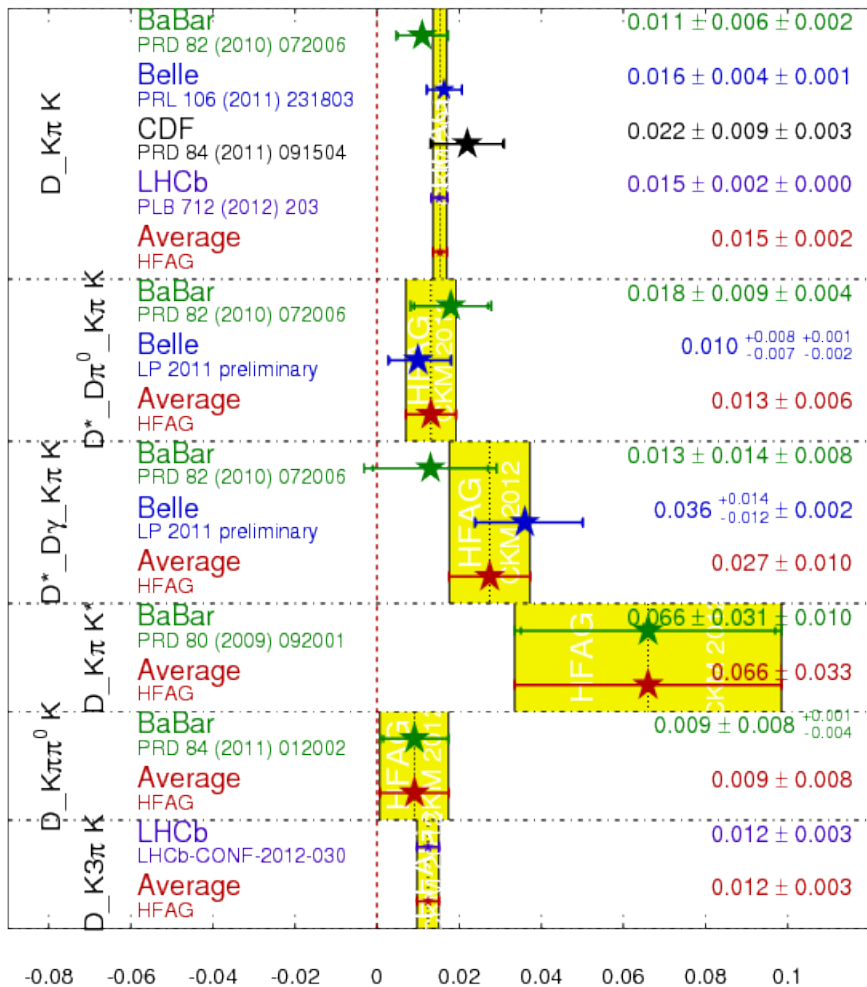
HFAG
CKM2012
PRELIMINARY



ADS summary

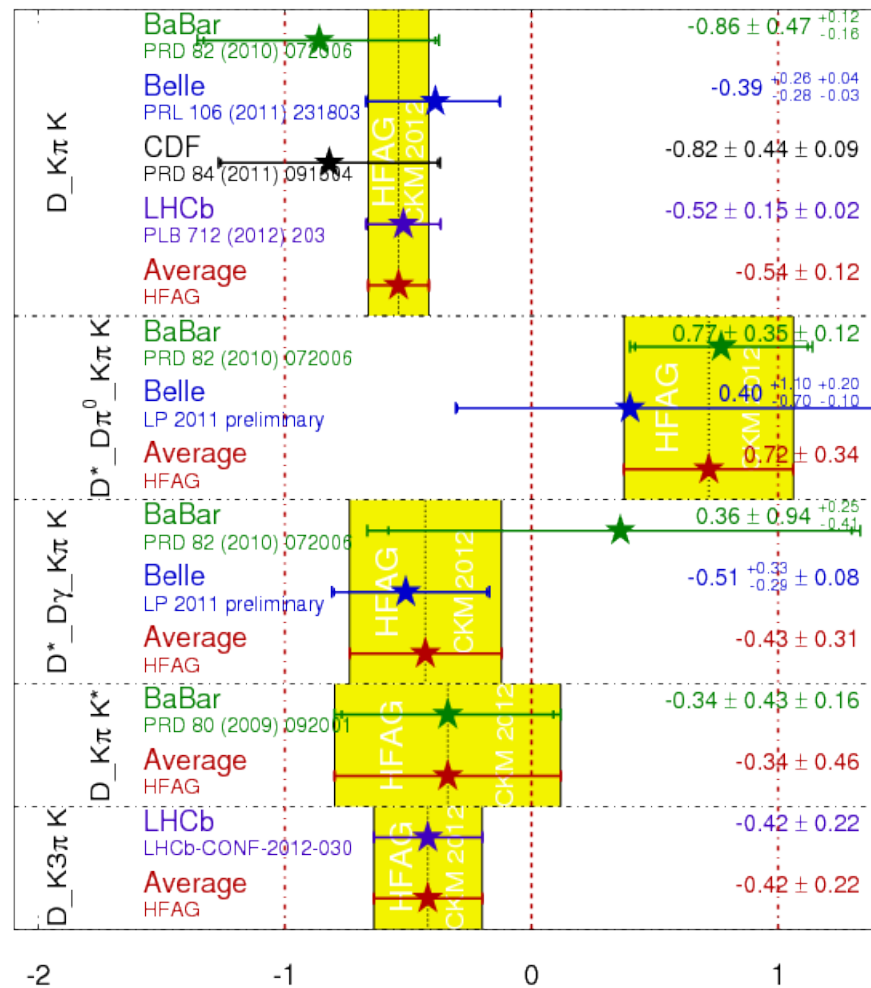
R_{ADS} Averages

HFAG
CKM 2012
PRELIMINARY



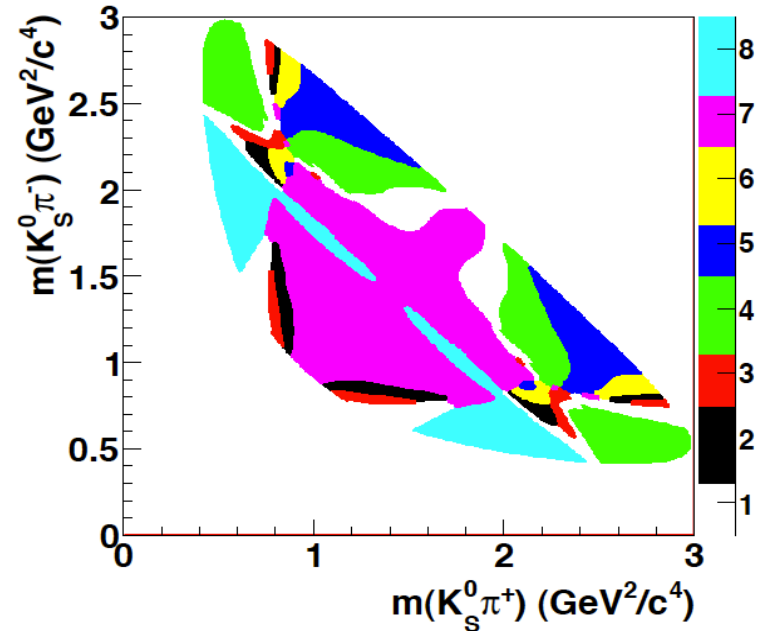
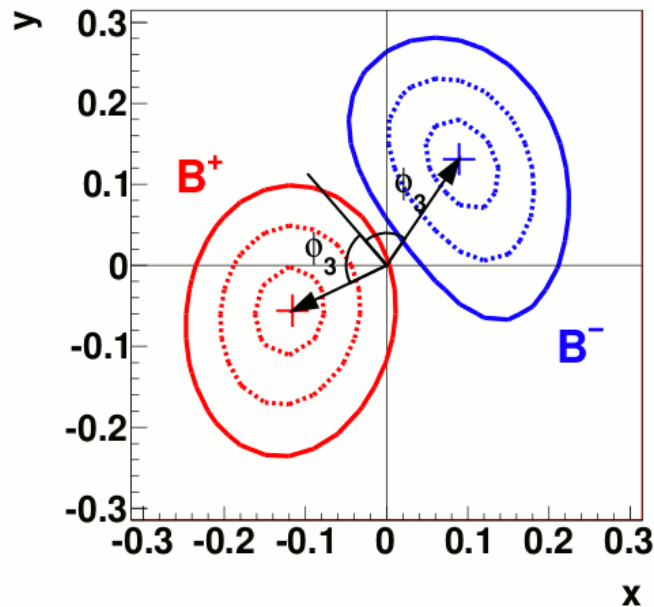
A_{ADS} Averages

HFAG
CKM 2012
PRELIMINARY



GGSZ results from Belle using Model-independent approach

PRD85, 112014 (2012),
772M BB



$$\phi_3 = (77.3^{+15.1}_{-14.9} \pm 4.1 \pm 4.3)^\circ$$

$$r_B = 0.145 \pm 0.030 \pm 0.010 \pm 0.011$$

$$\delta_B = (129.9 \pm 15.0 \pm 3.8 \pm 4.7)^\circ,$$

ADS $B^\pm \rightarrow [K\pi\pi^0]_D K^\pm$ analysis by Belle

selection Criteria:

- **Primary tracks:** $|dr| < 0.2 \text{ cm}$
 $|dz| < 1.5 \text{ cm}$
- **π selection:** $L(K/\pi) < 0.4$
- **K selection:** $L(K/\pi) \geq 0.6$
- **$E_\gamma > 50 \text{ MeV}$ in ECL**
- **$P_{\pi^0} > 0.4 \text{ GeV}/c$**
- **D^0 mass cut: $\pm 3\sigma$**
- **$M_{bc} = \pm 3\sigma$**
- **$\Delta E = E_{\text{beam}} - E_B : [-0.1, 0.2] \text{ GeV}$**

**Best candidate
selection: $X^2_{\min}(M_D, M_{bc})$**

BG vetoes:

✓ **$D^{*\pm}$ veto ($D^{*\pm} \rightarrow D^0\pi^\pm$) :**

$$\Delta M (D^{*\pm} - D^0) > 0.15 \text{ GeV}/c^2$$

✓ **double- mis-ID veto:**

$$(1.804 < M[K\pi\pi^0] < 1.885) \text{ GeV}/c^2$$

ADS $B^\pm \rightarrow [K\pi\pi^0]_D \pi^\pm$ result by Belle

$$R_{D\Pi}$$

$$B^\pm \rightarrow D_{\text{fav}} \Pi^\pm$$

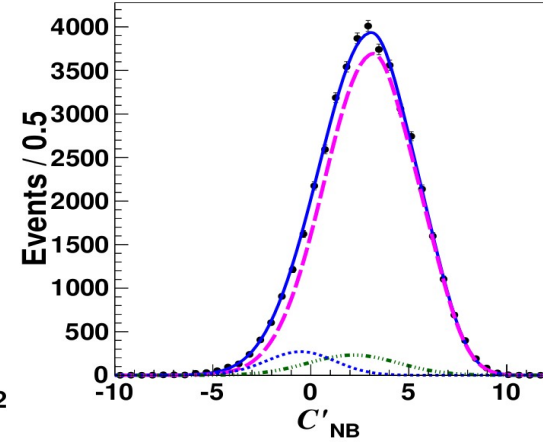
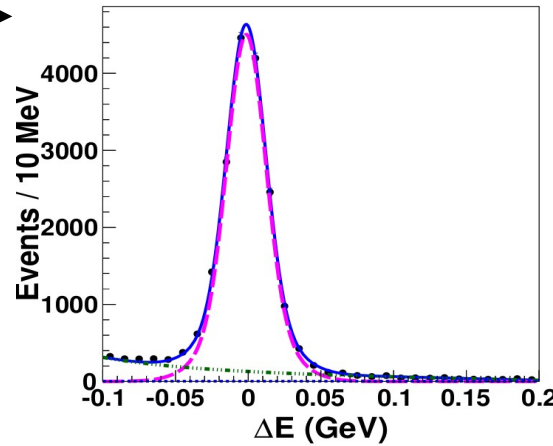
ΔE and C'_{NB} distributions: \rightarrow

Blue: total

Magenta: $D\Pi$ signal

Green: BB

Dotted blue: qq



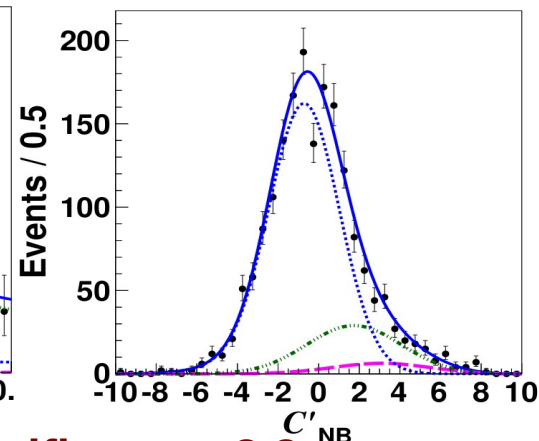
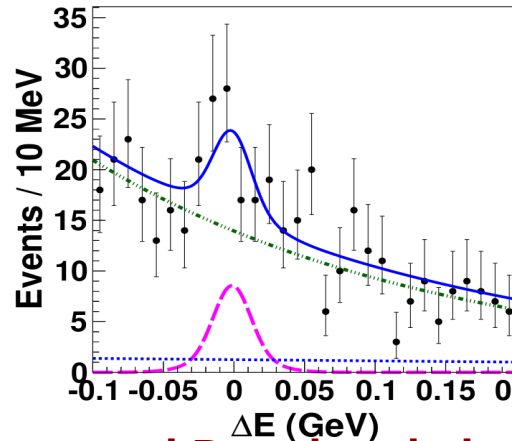
$$B^\pm \rightarrow D_{\text{sup}} \Pi^\pm$$

Belle Result using 772 M BB pairs:

$$N_{\text{sup}} = 94 \pm 27$$

$$N_{\text{fav}} = 49668 \pm 338$$

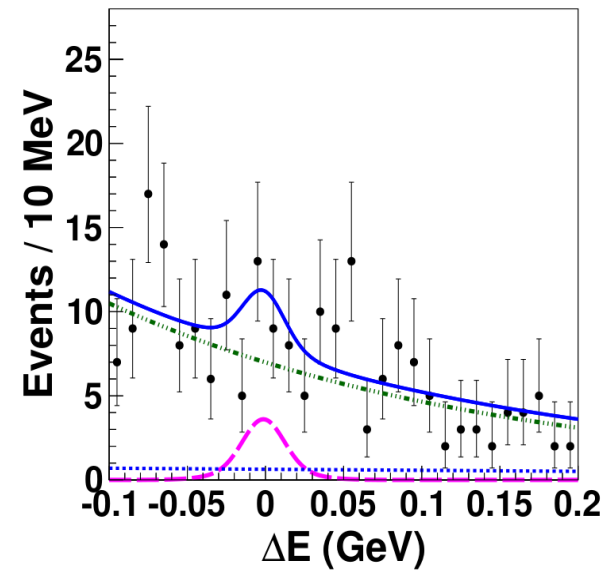
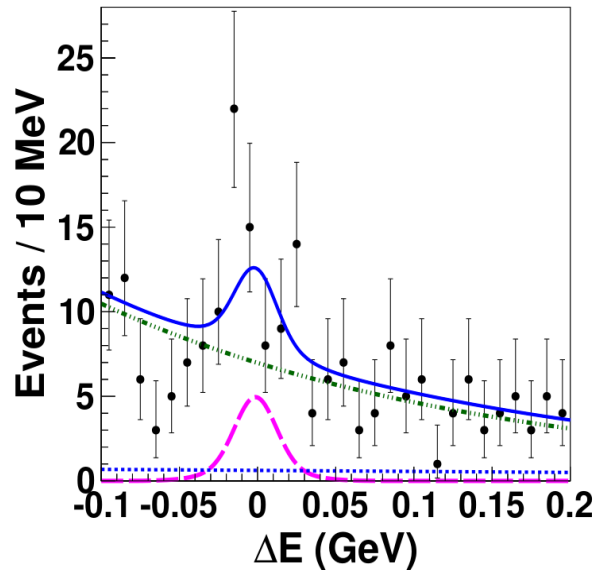
$$R_{D\Pi} = (1.89 \pm 0.54^{+0.22}_{-0.25}) \times 10^{-3}$$



Suppressed $D\Pi$ signal significance 3.3σ

ADS $B^\pm \rightarrow [K\pi\pi^0]_D K^\pm$ result by Belle

$$A_{D\Pi}$$



Belle Result using 772 M BB pairs:

$$R_{D\Pi} = (1.89 \pm 0.54^{+0.22}_{-0.25}) \times 10^{-3}$$

$$A_{D\Pi} = (0.16 \pm 0.27^{+0.03}_{-0.04})$$

First measurements!