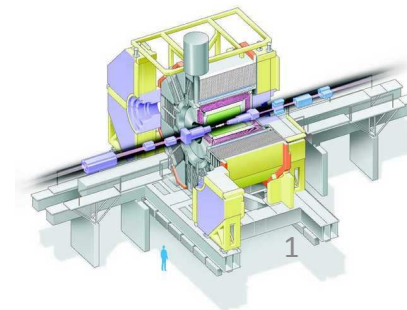
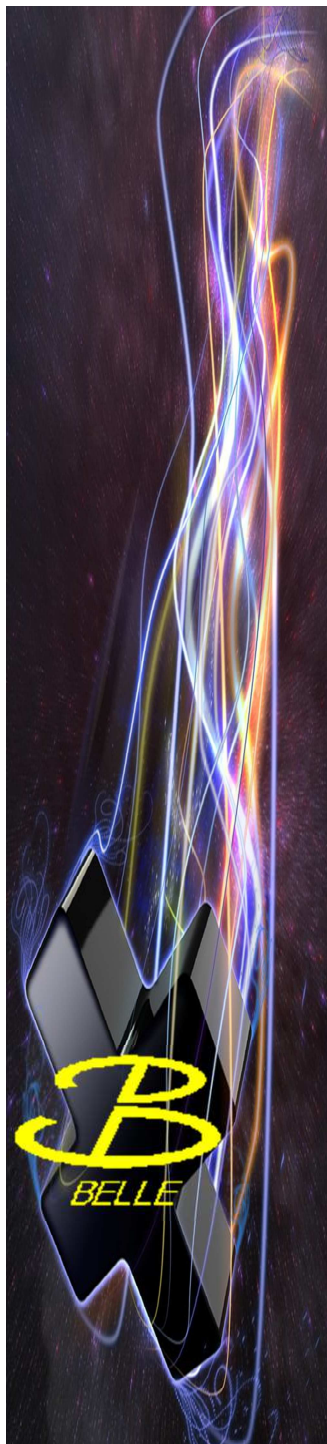




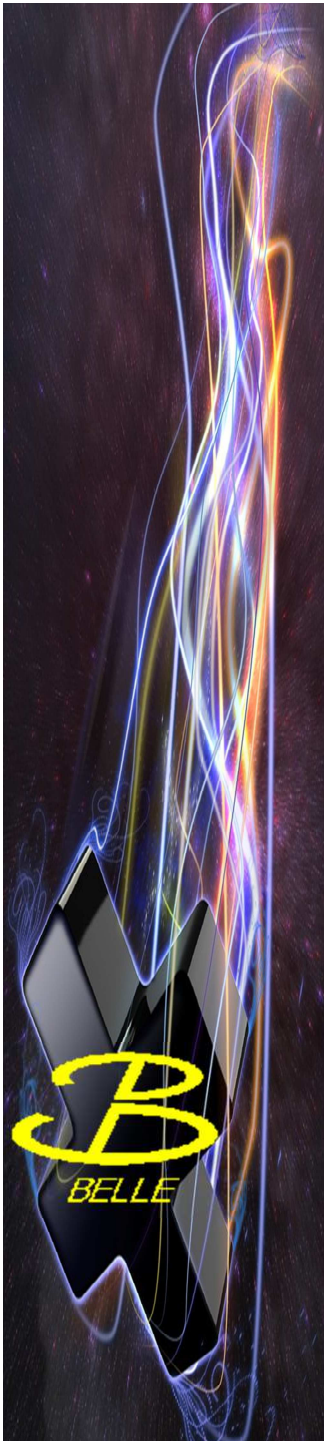
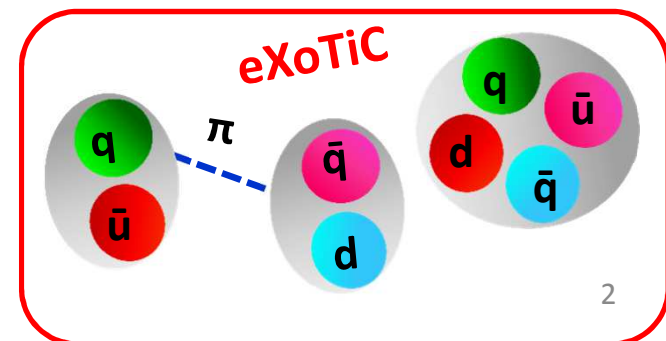
Studies of quarkonium and quarkonium-like exotic particles from Belle

Vishal Bhardwaj, NWU
(for Belle collaboration)

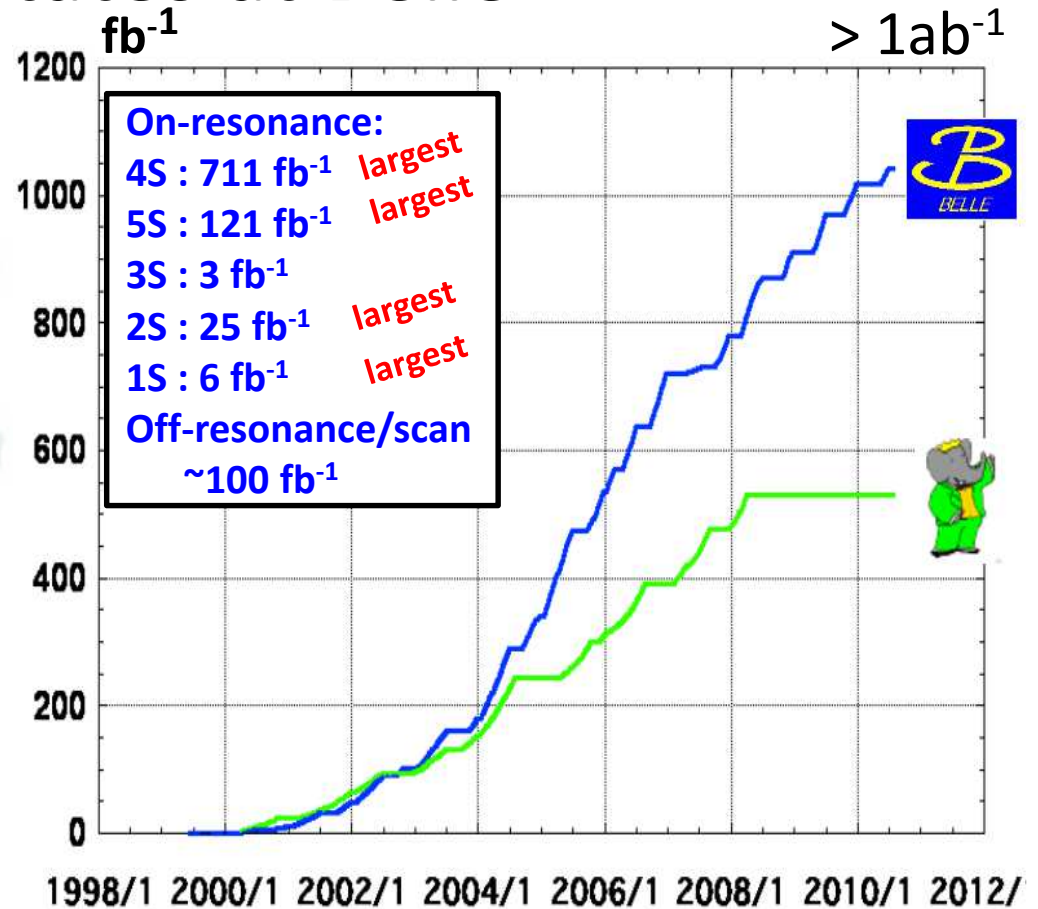
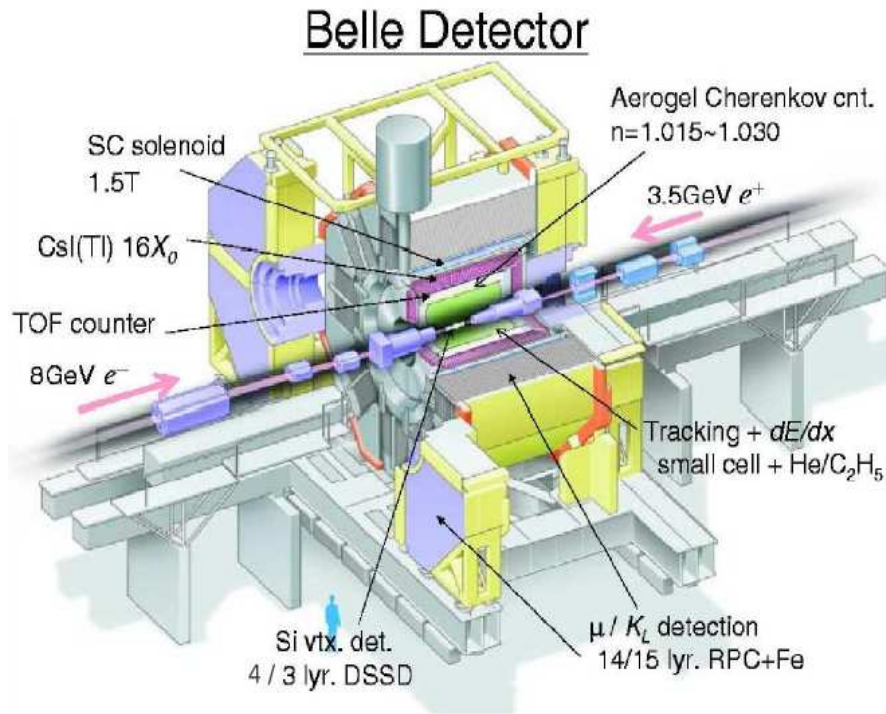


Outline

- Bottomonium (-like) family
 - $Z_b(10610)^+$ and $Z_b(10650)^+$ *eXoTiC*
 - Observation of neutral $Z_b(10610)^0$ *eXoTiC*
- Charmonium (-like) family
 - $Z(3895)^+$ *eXoTiC*
 - $Z(4430)^+$ *eXoTiC*
 - $X(3823)$
- Summary



qq̄ (-like) states at Belle



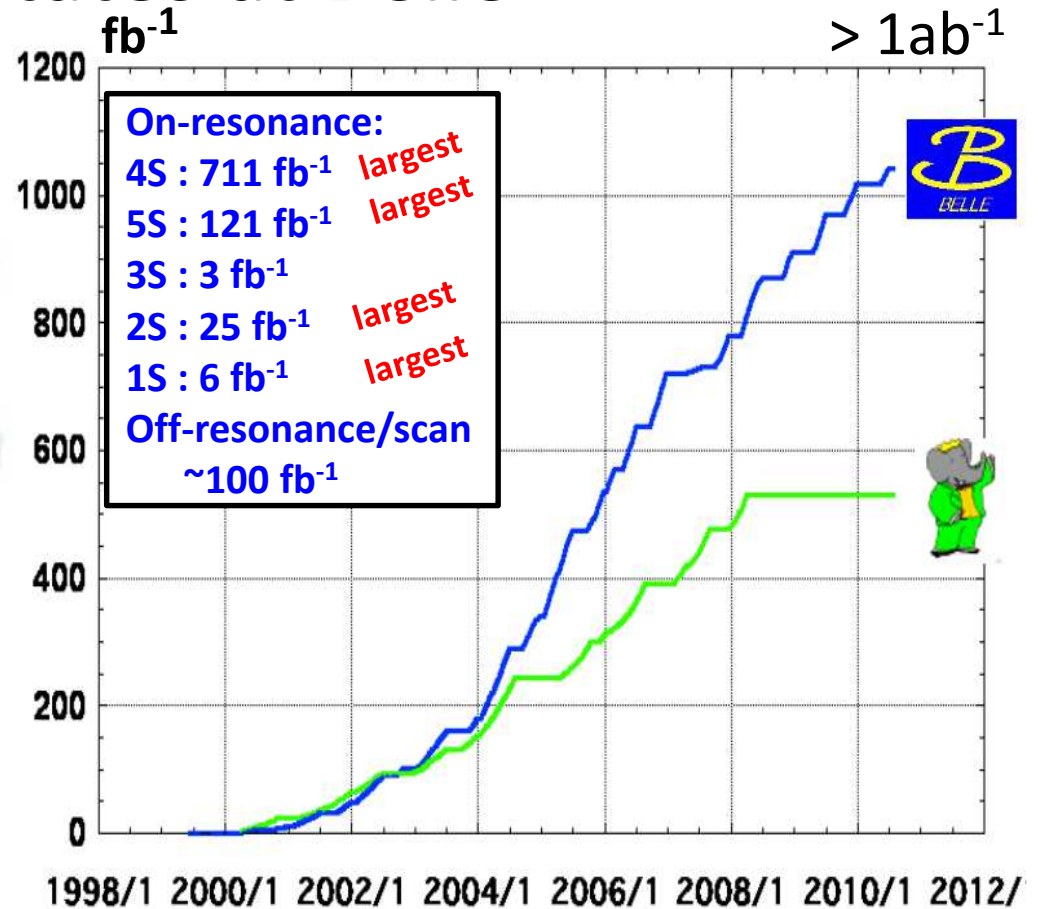
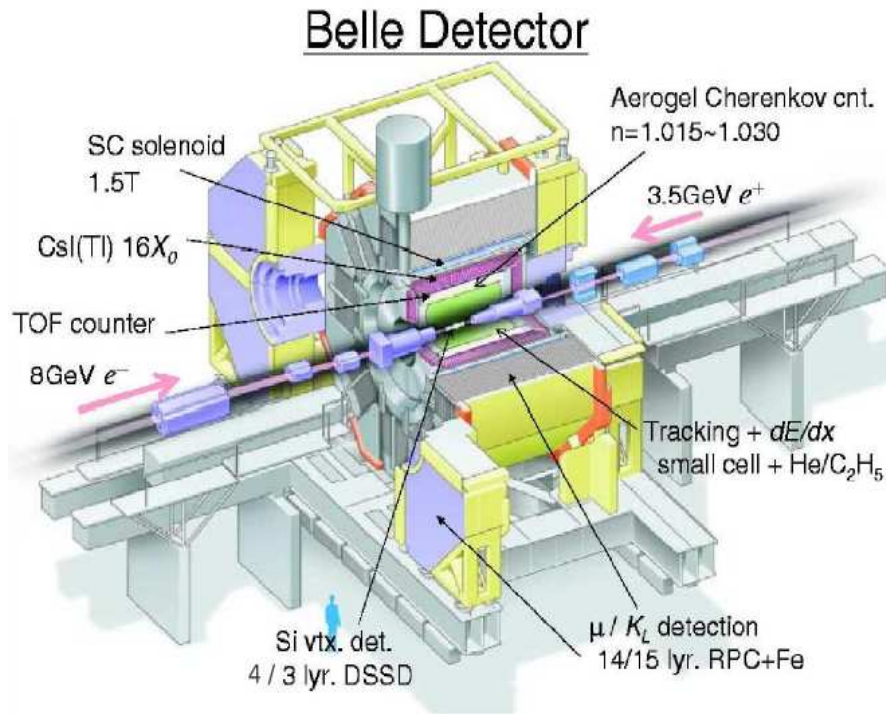
General purpose detector, built to test Standard Model mechanism for CP violation in B decays to charmonium ($B^0 \rightarrow J/\psi, \Psi', \chi_{c1} K^0$).

Contribution to charmonium (-like) states:

Belle, PRL 108, 171802 (2012)

$\eta_c(2S), X(3823), X(3872), Z(3895)^+, Y(3940), Z(3930), X(3940), X(3915), Y(4260), Y(4660), Z(4430)^+, Z_1(4050)^+, Z_2(4250)^+ \dots$

$q\bar{q}$ (-like) states at Belle



General purpose detector, built to test Standard Model mechanism for CP violation in B decays to charmonium ($B^0 \rightarrow J/\psi, \Psi', \chi_{c1} K^0$).

Contribution to bottomonium (-like) states:

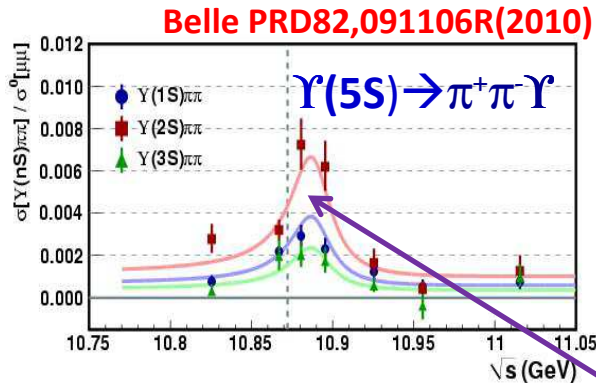
Belle, PRL 108, 171802 (2012)

$Y_b, \eta_b(2S), h_b(1P), h_b(2P), Z_b(10610)^+, Z_b(10610)^0, Z_b(10650)^+, \dots$

“ $\Upsilon(5S)$ ” more interesting than other Υ states

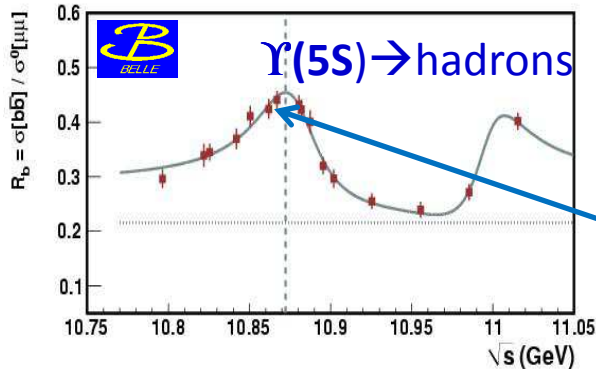
Anomalous large production of $\Upsilon(nS)\pi^+\pi^-$ was observed at the $\Upsilon(5S)$ by Belle with 21 fb⁻¹.

Belle, PRL100,112001(2008)



	$\Gamma(\text{MeV})$
$\Upsilon(5S) \rightarrow \Upsilon(1S)\pi^+\pi^-$	$0.59 \pm 0.04 \pm 0.09$
$\Upsilon(5S) \rightarrow \Upsilon(2S)\pi^+\pi^-$	$0.85 \pm 0.07 \pm 0.16$
$\Upsilon(5S) \rightarrow \Upsilon(3S)\pi^+\pi^-$	$0.52^{+0.20}_{-0.17} \pm 0.10$
$\Upsilon(2S) \rightarrow \Upsilon(1S)\pi^+\pi^-$	0.0060
$\Upsilon(3S) \rightarrow \Upsilon(1S)\pi^+\pi^-$	0.0009
$\Upsilon(4S) \rightarrow \Upsilon(1S)\pi^+\pi^-$	0.0019

x 10⁻²



$$M = (10889.6 \pm 1.8 \pm 1.5) \text{ MeV}$$

$$\Gamma = 54.7^{+8.5}_{-7.2} \pm 2.5 \text{ MeV}$$

$\sim 2\sigma$ discrepancies in the peak mass and width

$$M = (10865 \pm 8) \text{ MeV}$$

$$\Gamma = (110 \pm 13) \text{ MeV}$$

Nature of $\Upsilon(5S)$ is puzzling

Exotic resonance Y_b near $\Upsilon(5S)$ analogue of $Y(4260)$ resonance !

Belle found twin charged states $Z_b(10610)^+$ and $Z_b(10650)^+$ having masses just above $B^*\bar{B}$ and $B^*\bar{B}^*$ thresholds. Belle, PRL108, 122001 (2012)

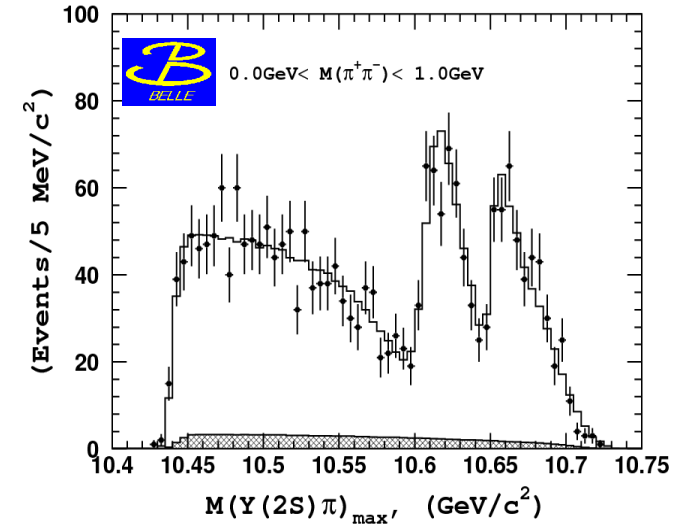
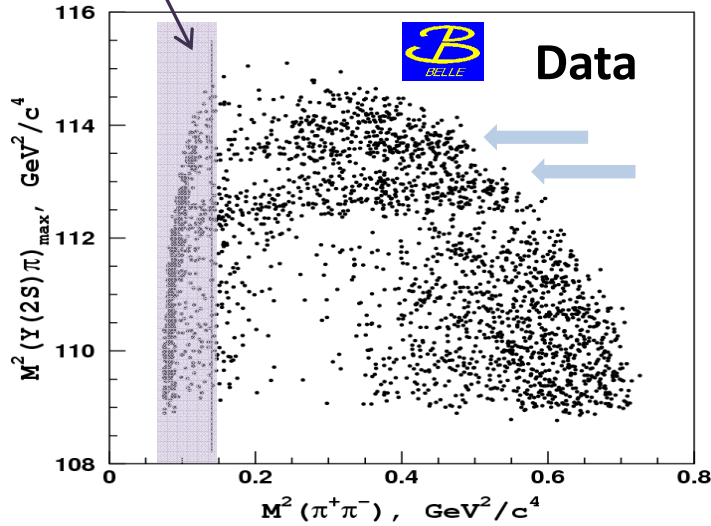
Measurement of J^P

preliminary

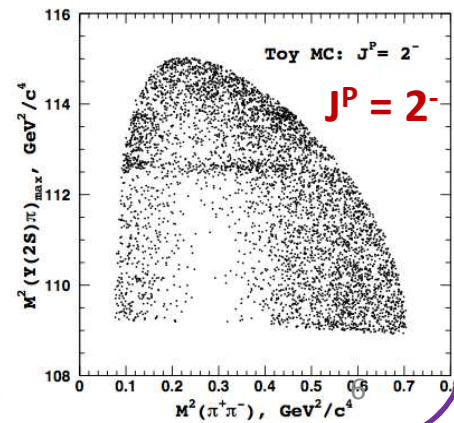
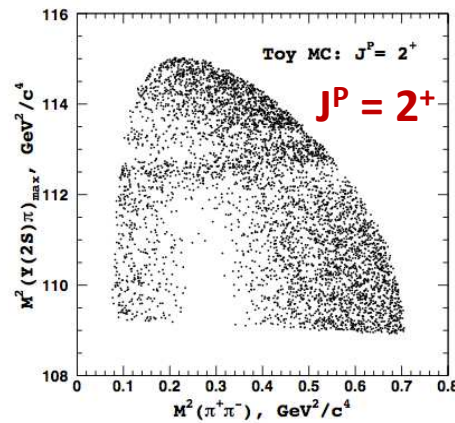
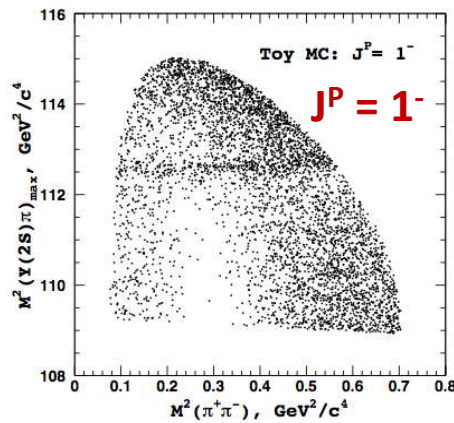
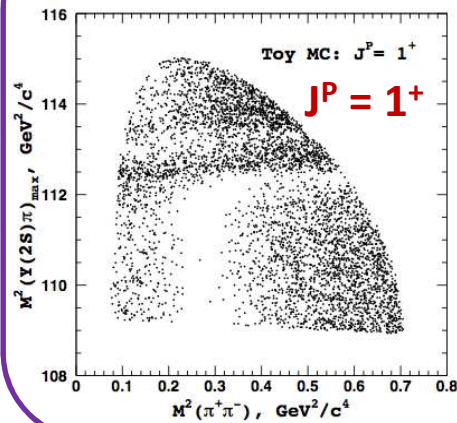
Full amplitude analysis of $e^+e^- \rightarrow \Upsilon(nS)\pi^+\pi^- \rightarrow \mu^+\mu^-\pi^+\pi^-$ (n=1,2,3)

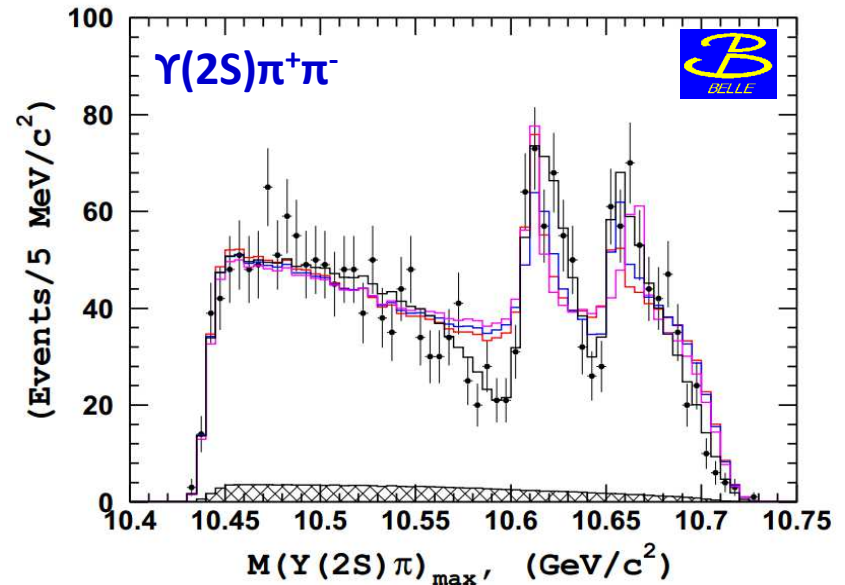
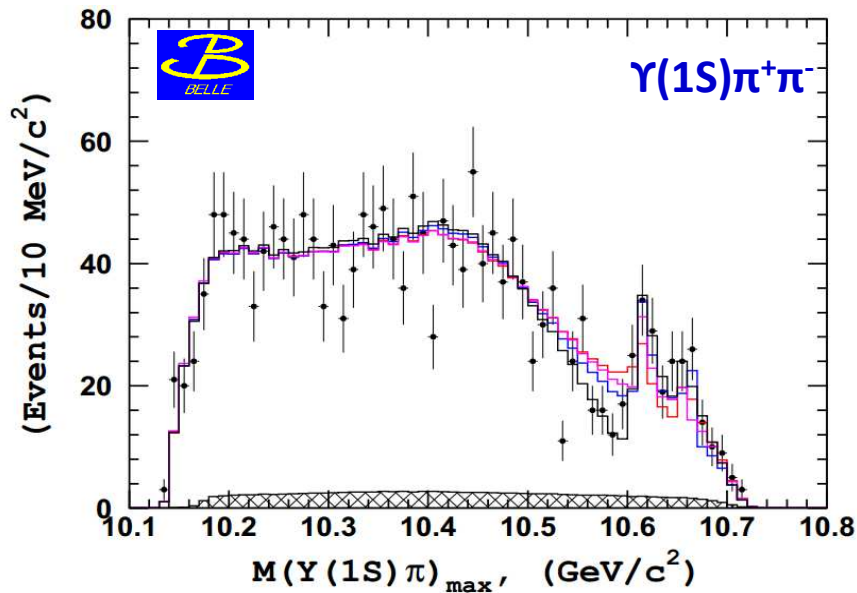
Excluded region with large background from photon conversions

$\Upsilon(5S) \rightarrow \Upsilon(2S)\pi^+\pi^-$

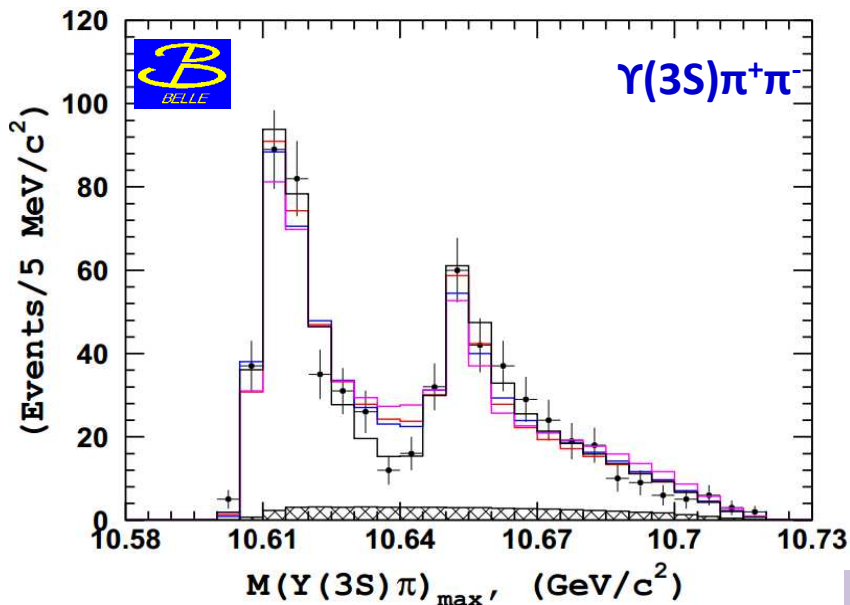


Toy MC with various J^P





1⁺
1⁻
2⁺
2⁻



J ^P Hypothesis \ Decay Mode	Y(1S)π ⁺ π ⁻	Y(2S)π ⁺ π ⁻	Y(3S)π ⁺ π ⁻
1 ⁺	0	0	0
1 ⁻	64	264	73
2 ⁺	41	207	87
2 ⁻	59	304	125

Highest sensitivity provided by e⁺e⁻ → Y(2S)ππ

Reject J^P=1⁻ and J^P=2[±] combinations at confidence level exceeding 7σ.

Spin parity of Z_b(10610) and Z_b(10650) is 1⁺

Nature of Z_b^+

$Z_b(10610)$

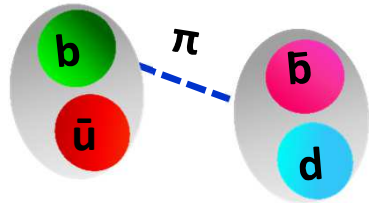
$M=10607.2\pm 2.0$ MeV
 $\Gamma=18.4\pm 2.4$ MeV

$Z_b(10650)$

$M=10652.2\pm 1.5$ MeV
 $\Gamma=11.5\pm 2.2$ MeV

PDG: $M_{\bar{B}} + M_{B^*} = 10604.8\pm 0.4$ MeV

PDG: $M_{\bar{B}^*} + M_{B^*} = 10650.4\pm 0.8$ MeV

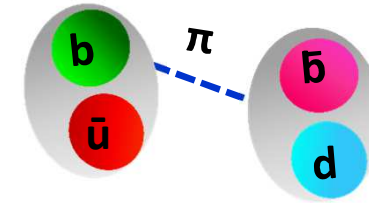


B^- B^{*0}

$$M_{Z_b(10610)} - (M_{B^-} + M_{B^{*0}}) = + 2.4 \pm 2.0 \text{ MeV}$$

Bondar et al. arXiv:1105.4473
Sun et al. PRD 84, 054002 (2011)
Zhang et al. PLB 704,312 (2011)
Ohkoda et al. PRD 86, 014004 (2012), ...

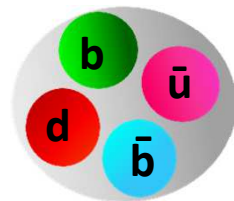
Molecular picture



B^{*-} B^{*0}

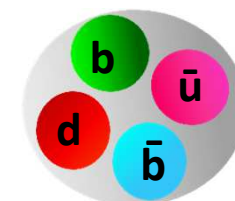
$$M_{Z_b(10650)} - 2M_{B^{*0}} = + 1.8 \pm 1.7 \text{ MeV}$$

Slightly unbound threshold resonances?



Karliner arXiv:0802.0649
Ali et al. PRD 85, 054011 (2012), ...

Tetraquark picture



Coupled channel resonance : *Dankiklin et al. PRD 85,034012 (2012)*

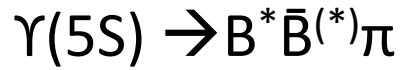
Cusp: *Bugg, Europhys. Lett.96,11002 (2011)*

+ others ...

I.S.P.E
PRD84,094003(2011)

If Z_b^+ is $B^* \bar{B}^{(*)}$ molecule, it should decay into $B^* \bar{B}^{(*)}$

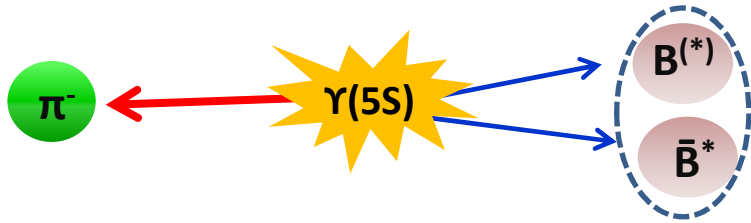
121 fb⁻¹



preliminary

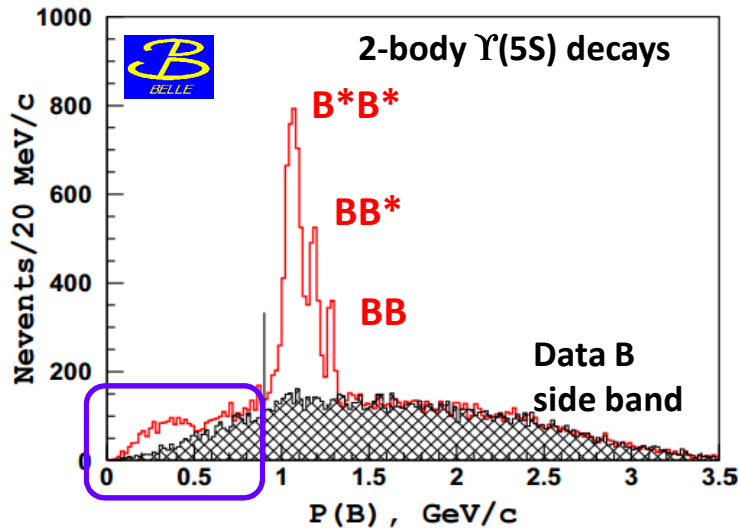
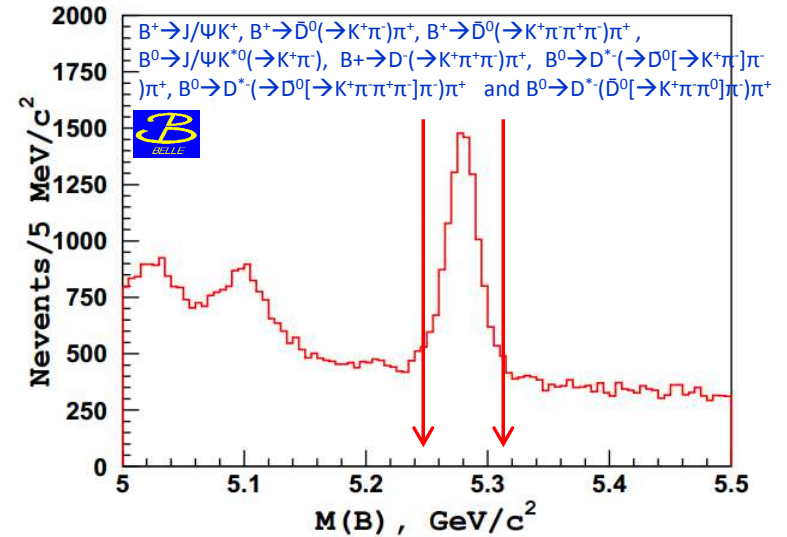
Belle, arXiv:1209.6450

Masses of Z_b(10610)⁺ and Z_b(10650)⁺ close to B \bar{B}^* and B^{* \bar{B}^* threshold}



Select events by using cut in M(B) and p(B)

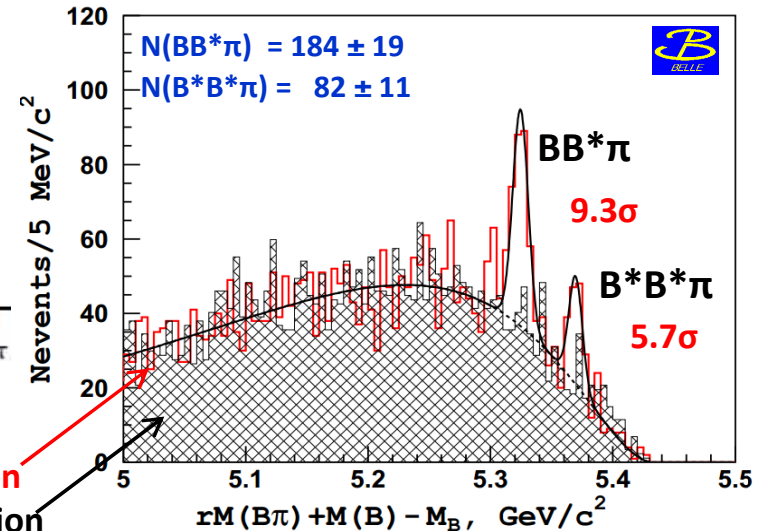
One B is fully reconstructed



3 body $\Upsilon(5S) \rightarrow B^{(*)} B^{(*)} \pi$ decays and rad. return to $\Upsilon(4S)$: $P(B) < 0.9$ GeV/c

B is combined with π and recoil mass to $(B\pi)$ combination is calculated

$$rM(B\pi) = \sqrt{E_{\text{cms}}^2 - P_{B\pi}^2}$$



Right sign B π combination

Wrong sign B π combination

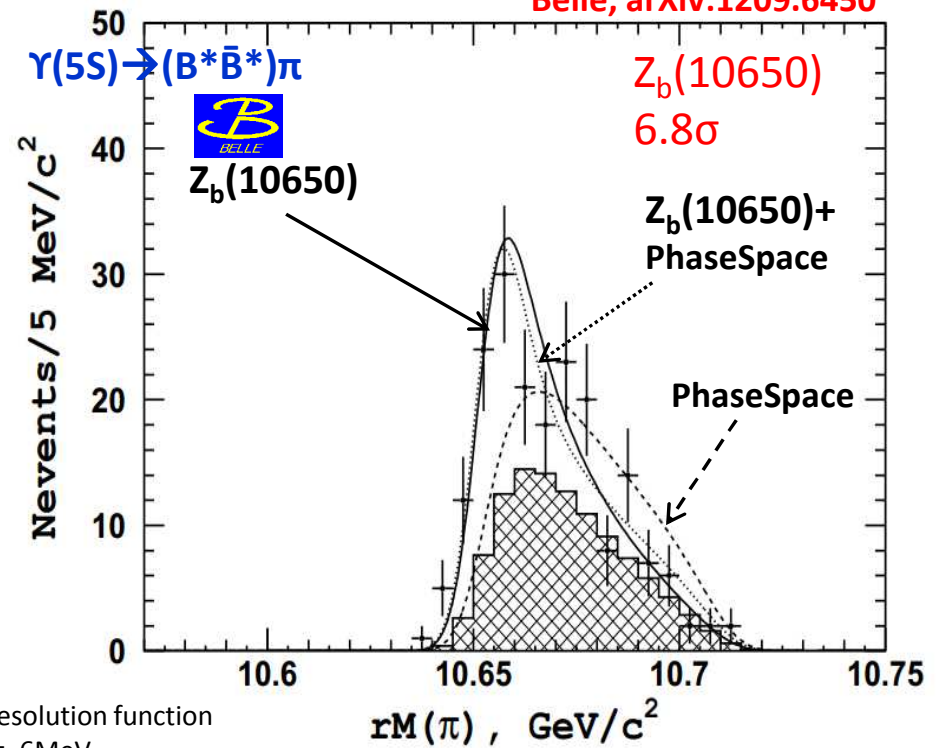
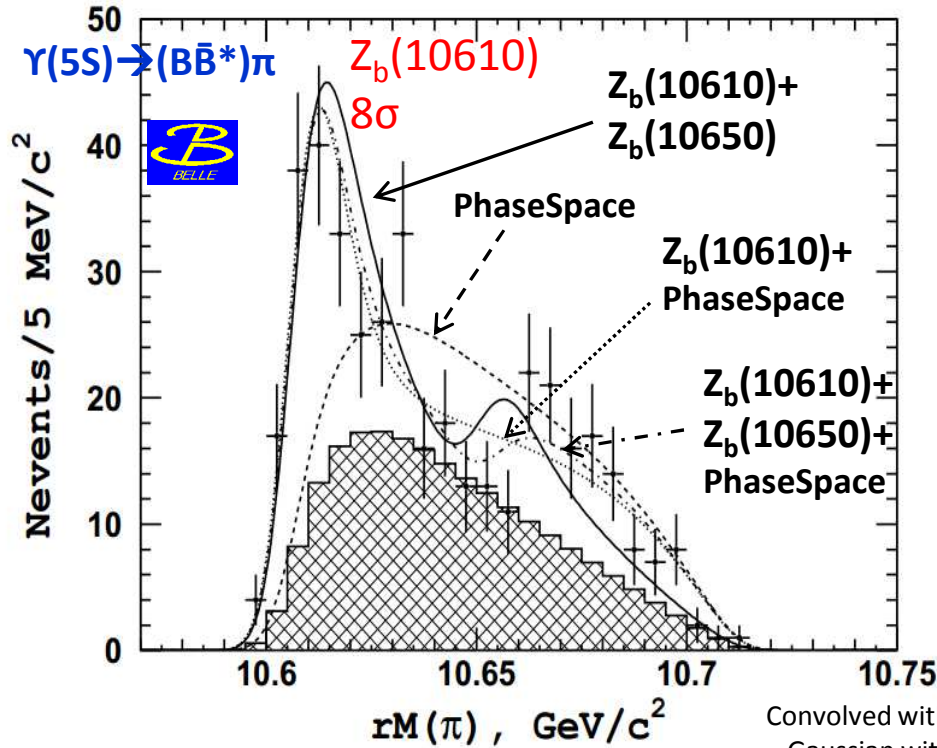
Look at recoil mass of (π) to see if there is Z_b peak.

preliminary

Recoil mass of (π) in $\Upsilon(5S) \rightarrow B^* \bar{B}^{(*)} \pi$

121 fb⁻¹

Belle, arXiv:1209.6450



Convolved with resolution function
= Gaussian with $\sigma=6\text{MeV}$

Channel\Fraction(%)	$Z_b(10610)^+$	$Z_b(10650)^+$
$\Upsilon(1S)\pi^+$	0.32 ± 0.09	0.24 ± 0.07
$\Upsilon(2S)\pi^+$	4.38 ± 1.21	2.40 ± 0.63
$\Upsilon(3S)\pi^+$	2.15 ± 0.56	1.64 ± 0.40
$h_b(1P)\pi^+$	2.81 ± 1.10	7.43 ± 2.70
$h_b(2P)\pi^+$	4.34 ± 2.07	14.8 ± 6.22
$B\bar{B}^*$	86.0 ± 3.6	-
$B^*\bar{B}^*$	-	73.4 ± 7.0

- $Z_b(10610)^+$ in $B\bar{B}^*$ and $Z_b(10650)^+$ seen in $B\bar{B}^*/B^*\bar{B}^*$.
- $B^{(*)}B^*$ dominant mode of Z_b decays

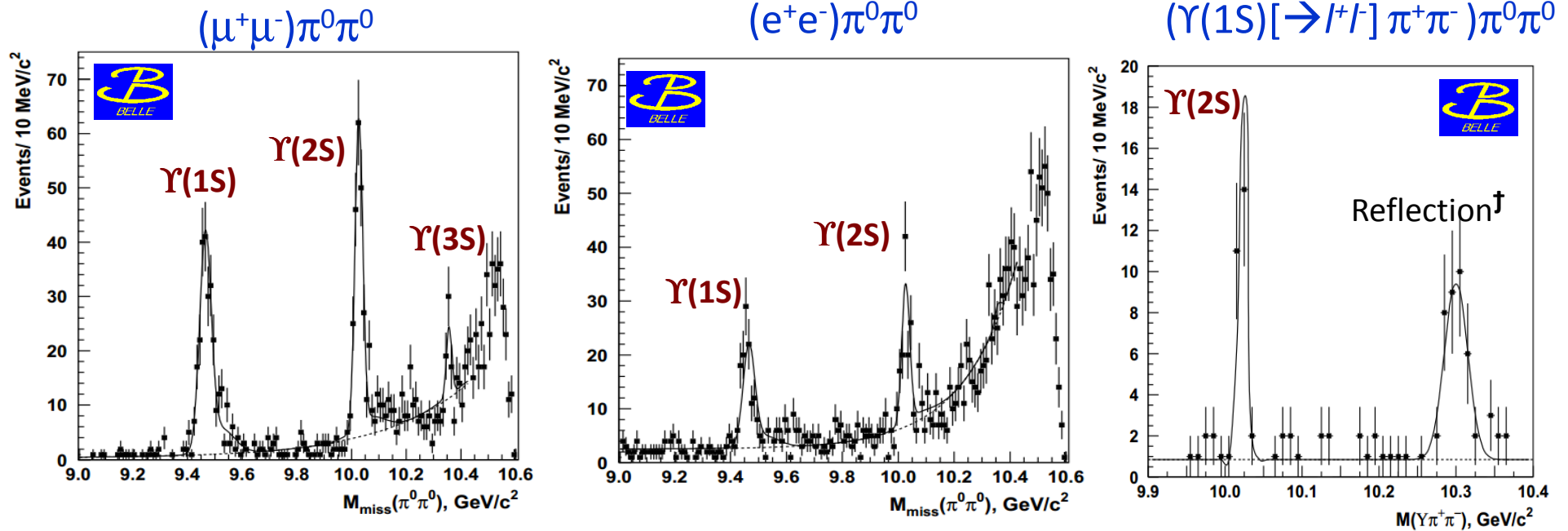
Support molecular picture ?

Is there neutral partner ?

$\Upsilon(5S) \rightarrow \Upsilon(nS)\pi^0\pi^0$

Belle, PRD88, 052016 (2013)

$\Upsilon(1,2,3S) \rightarrow \mu^+\mu^-, e^+e^-, \Upsilon(2S) \rightarrow \Upsilon(1S)\pi^+\pi^-$



$$\sigma[e^+e^- \rightarrow \Upsilon(5S) \rightarrow \Upsilon(1S)\pi^0\pi^0] = (1.16 \pm 0.06 \pm 0.10) \text{ pb}$$

$$\sigma[e^+e^- \rightarrow \Upsilon(5S) \rightarrow \Upsilon(2S)\pi^0\pi^0] = (1.87 \pm 0.11 \pm 0.23) \text{ pb}$$

$$\sigma[e^+e^- \rightarrow \Upsilon(5S) \rightarrow \Upsilon(3S)\pi^0\pi^0] = (0.98 \pm 0.24 \pm 0.19) \text{ pb}$$

Consistent with $\frac{1}{2}$ of $\Upsilon(nS)\pi^+\pi^-$

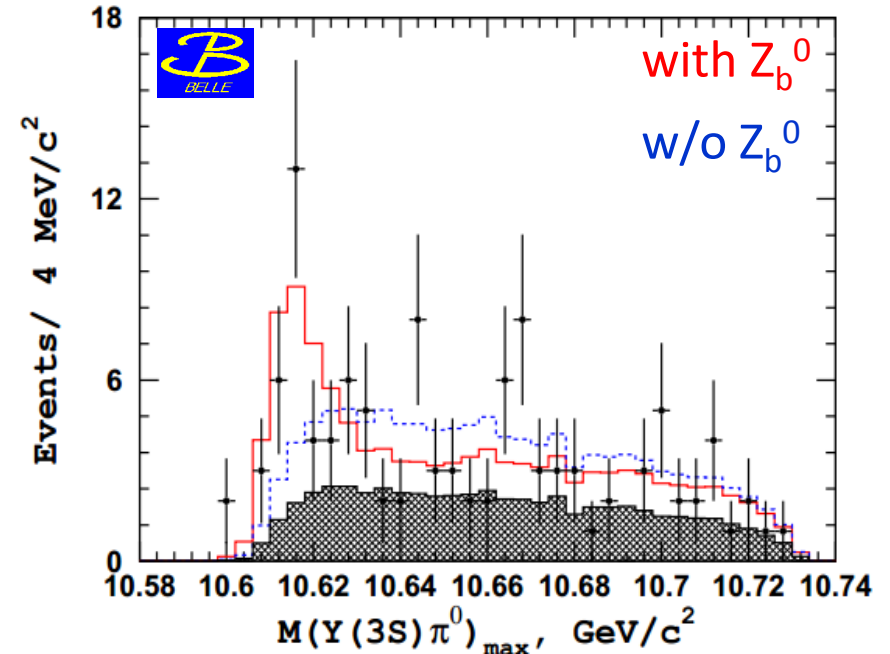
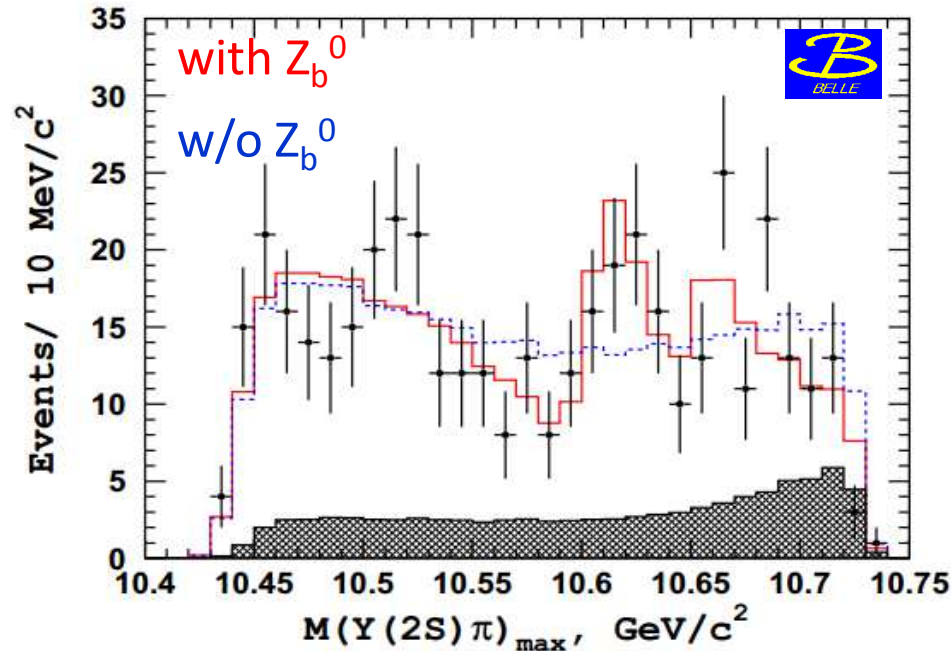
† due to cross-feed from $\Upsilon(5S) \rightarrow \Upsilon(2S)[\rightarrow \Upsilon(1S)\pi^0\pi^0]\pi^+\pi^-$

Neutral Z_b^0 in $\Upsilon(5S) \rightarrow \Upsilon(nS)\pi^0\pi^0$

Belle, PRD88, 052016 (2013)

Dalitz analysis

$$M = A_{Z_1} + A_{Z_2} + A_{f_0} + A_{f_2} + a^{\text{NR}}$$



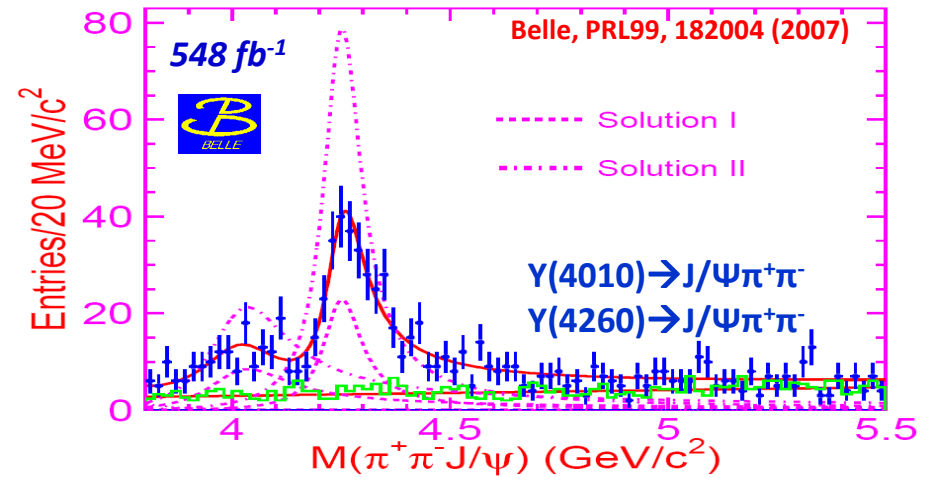
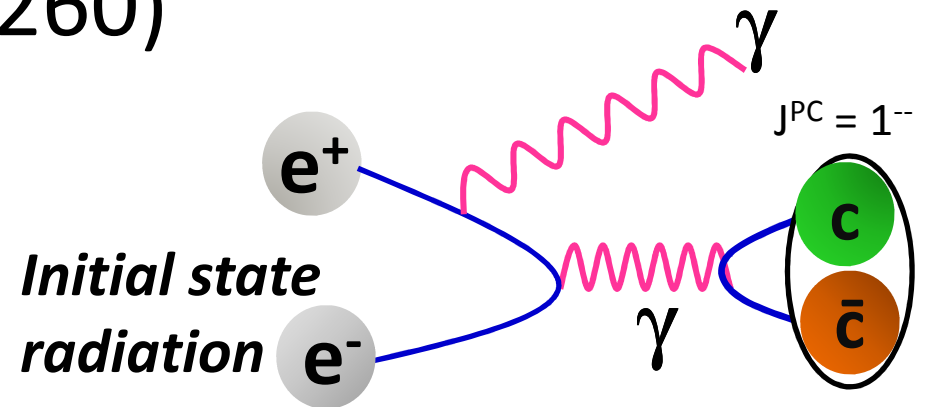
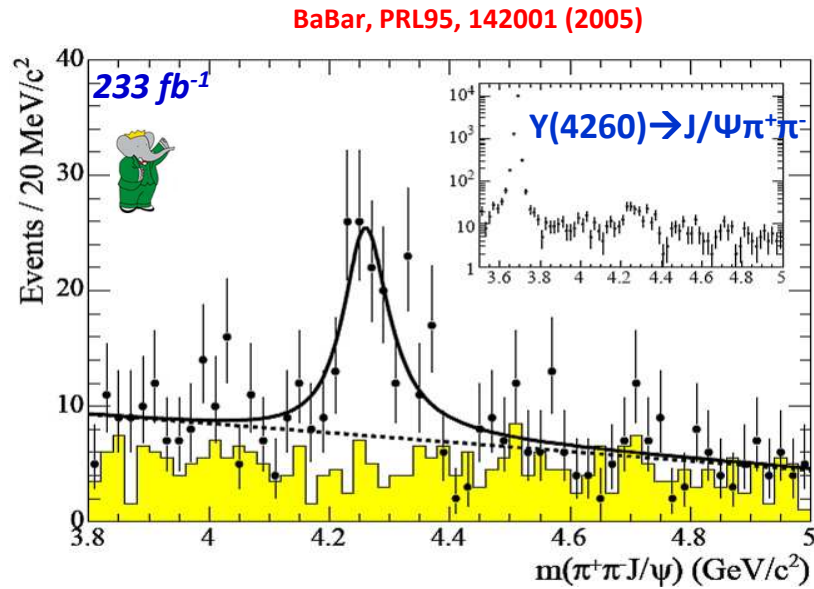
$Z_b(10650)^0$ is included in the fit

- ❖ Z_b^0 resonant structure observed in $\Upsilon(2S)\pi^0\pi^0$ and $\Upsilon(3S)\pi^0\pi^0$.
- ❖ Statistical significance of $Z_b(10610)^0$ is 6.5σ (including systematics).
- ❖ Our data consistent with existence $Z_b(10650)^0$, but available statistics insufficient for observation of it.
- ❖ $Z_b(10610)^0$ mass from fit : $10609 \pm 4 \pm 4 \text{ MeV}/c^2$

$$M[Z_b(10610)^+] = 10607.2 \pm 2.0 \text{ MeV}/c^2$$

First observation of $Z_b(10610)^0$

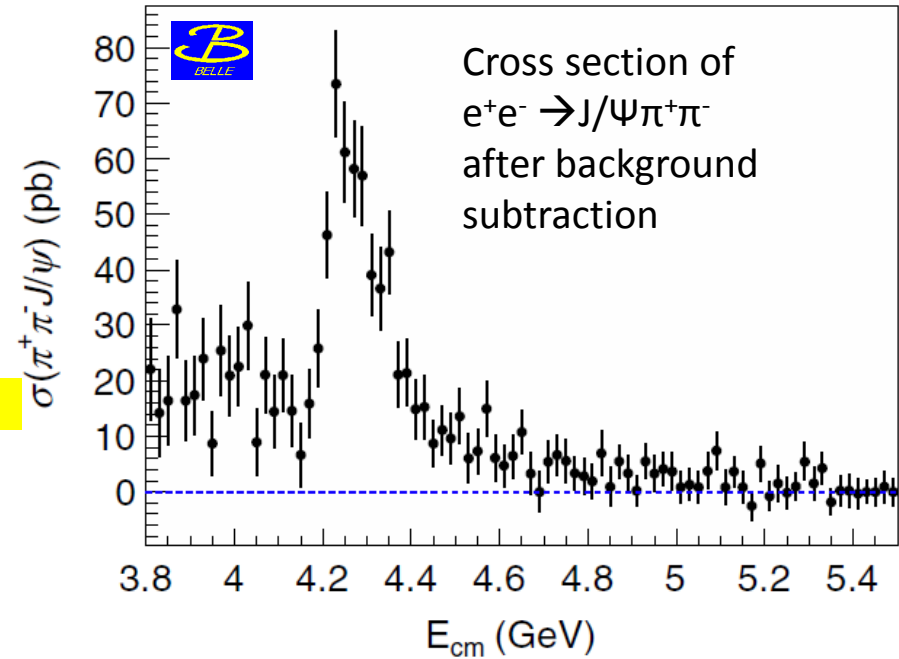
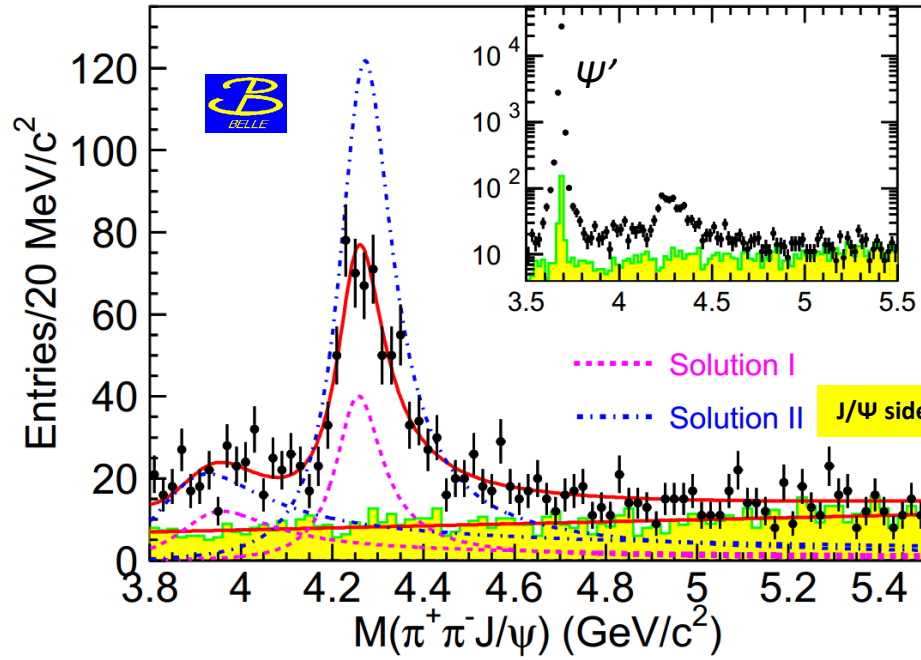
Y(4260)



	Name	Process	M (MeV/c ²)	Γ (MeV)
BaBar(233 fb ⁻¹)	Y(4260)	J/ψππ	4259±8 ⁺² ₋₆	88±23 ⁺⁶ ₋₄
Belle (548 fb ⁻¹)	Y(4260)	J/ψππ	4247 ± 12 ⁺¹⁷ ₋₃₂	108 ± 19 ± 10
Belle (548fb ⁻¹)	Y(4010) ?	J/ψππ	4008 ± 40 ⁺¹¹⁴ ₋₂₈	226 ± 44 ± 87

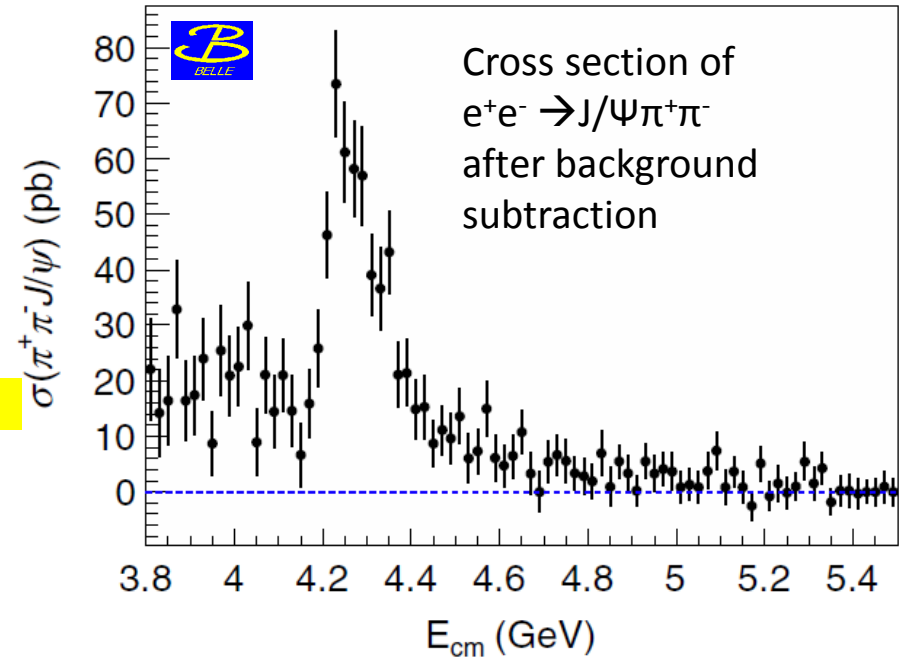
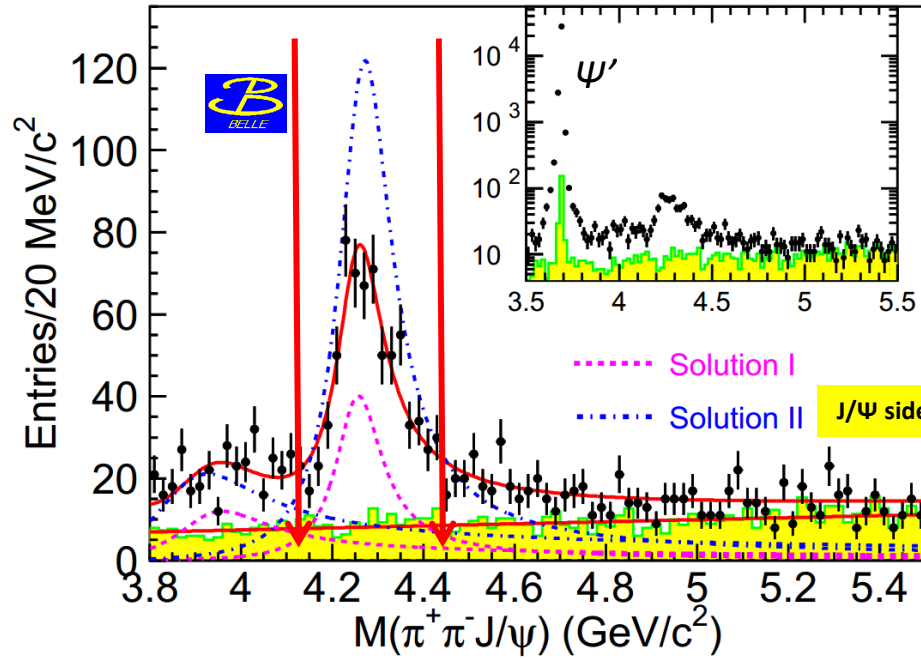
Also confirmed by CLEO-c and CLEOIII !

Revisit Y @ Belle

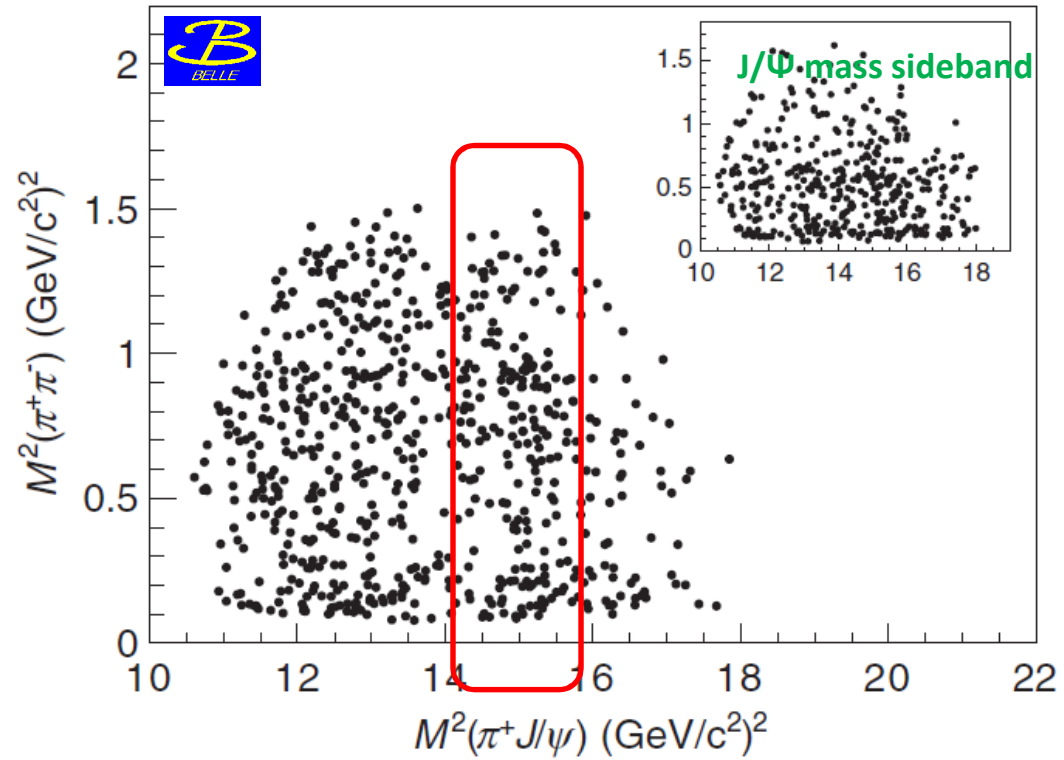


Parameters	Solution I	Solution II
$M(R_1)$	$3890.8 \pm 40.5 \pm 11.5$	
$\Gamma_{\text{tot}}(R_1)$	$254.5 \pm 39.5 \pm 13.6$	
$\Gamma_{ee} \mathcal{B}(R_1 \rightarrow \pi^+ \pi^- J/\psi)$	$(3.8 \pm 0.6 \pm 0.4)$	$(8.4 \pm 1.2 \pm 1.1)$
$M(R_2)$	$4258.6 \pm 8.3 \pm 12.1$	
$\Gamma_{\text{tot}}(R_2)$	$134.1 \pm 16.4 \pm 5.5$	
$\Gamma_{ee} \mathcal{B}(R_2 \rightarrow \pi^+ \pi^- J/\psi)$	$(6.4 \pm 0.8 \pm 0.6)$	$(20.5 \pm 1.4 \pm 2.0)$
ϕ	$59 \pm 17 \pm 11$	$-116 \pm 6 \pm 11$

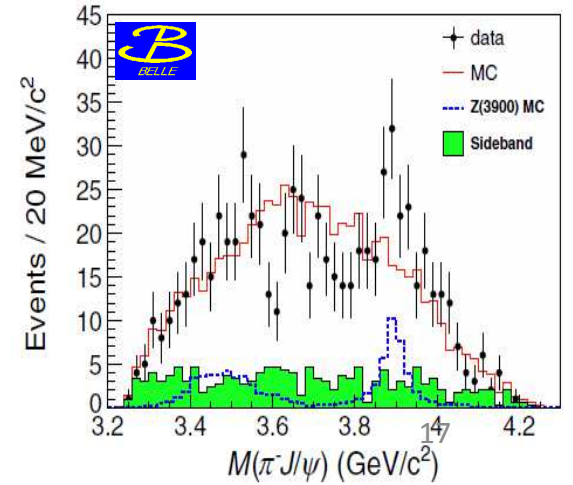
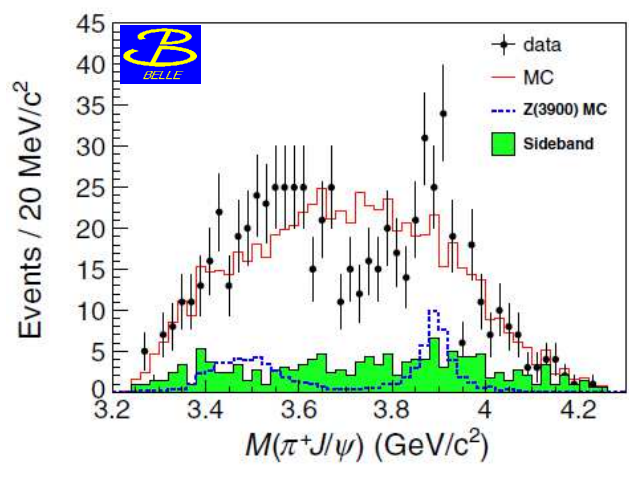
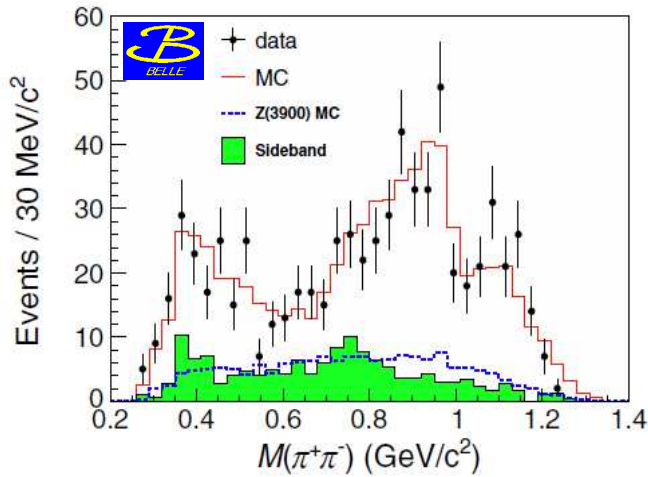
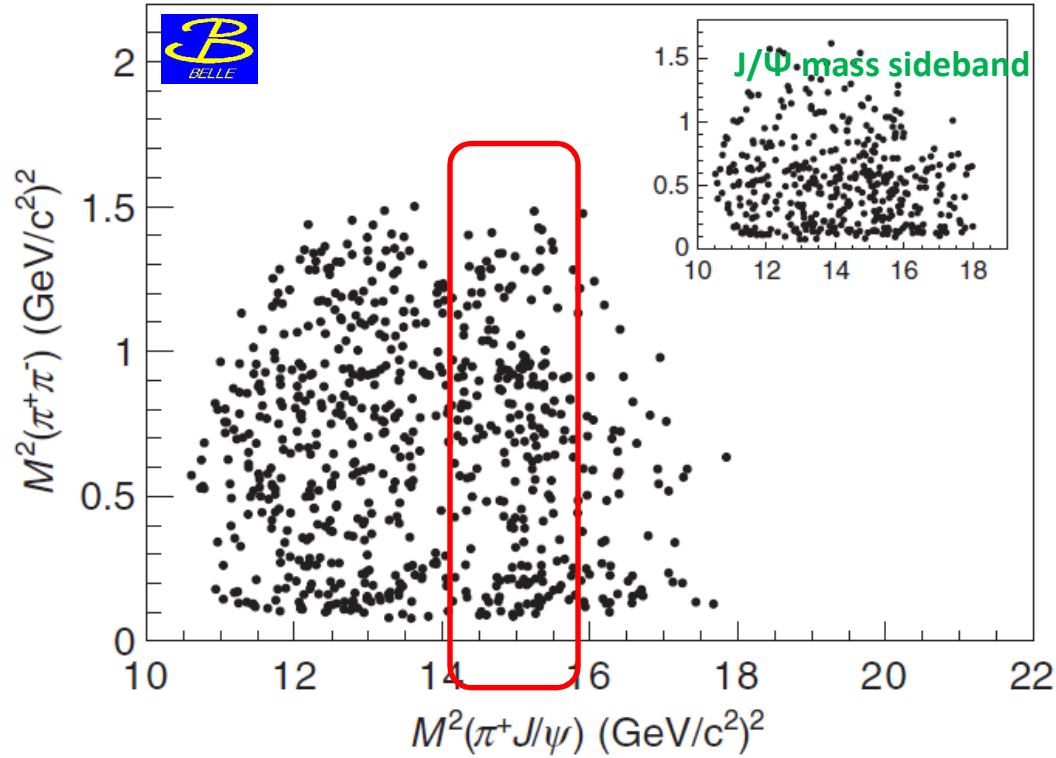
Revisit Y @ Belle



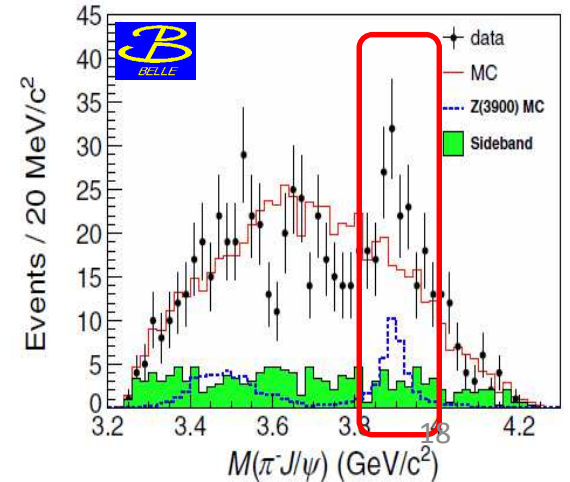
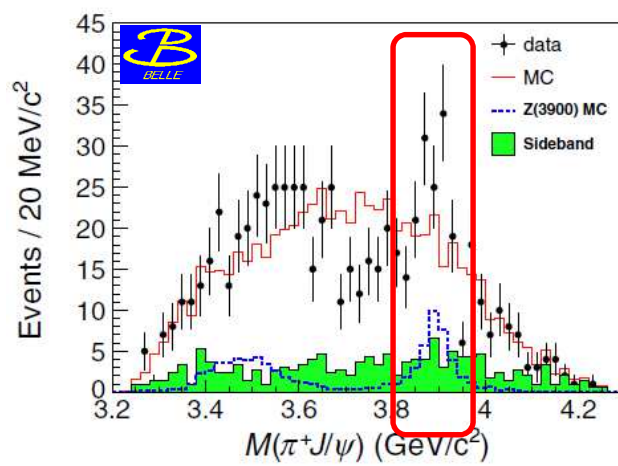
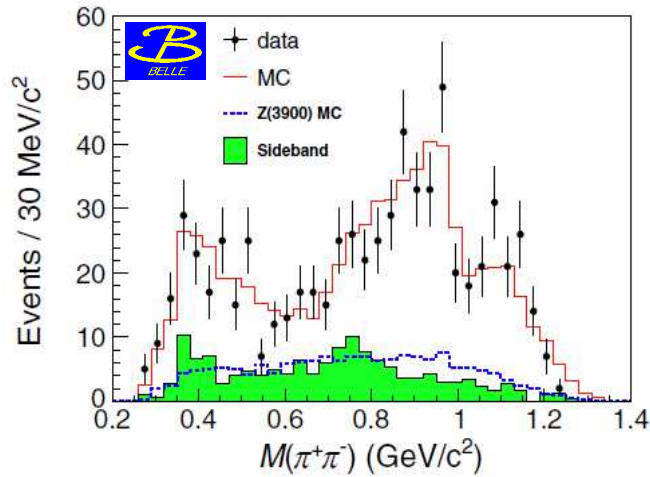
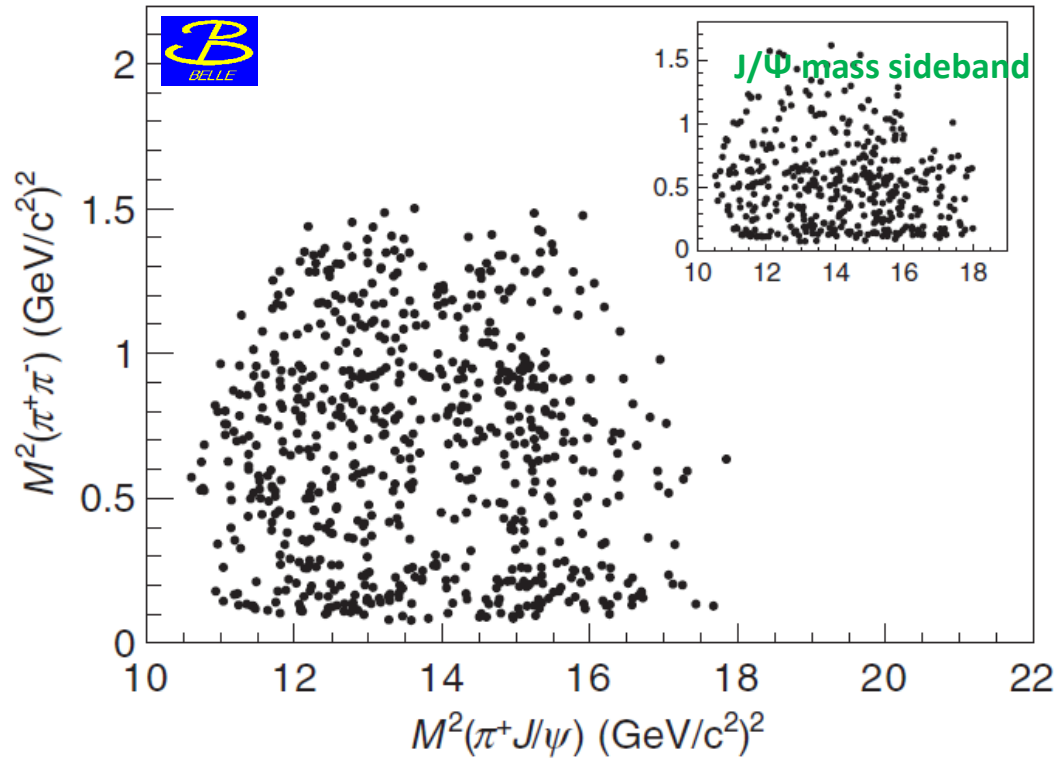
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ϕ	$59 \pm 17 \pm 11$	$-116 \pm 6 \pm 11$

Intermediate state in $\Upsilon(4260) \rightarrow J/\psi \pi \pi$ 

Intermediate state in $\Upsilon(4260) \rightarrow J/\psi \pi \pi$

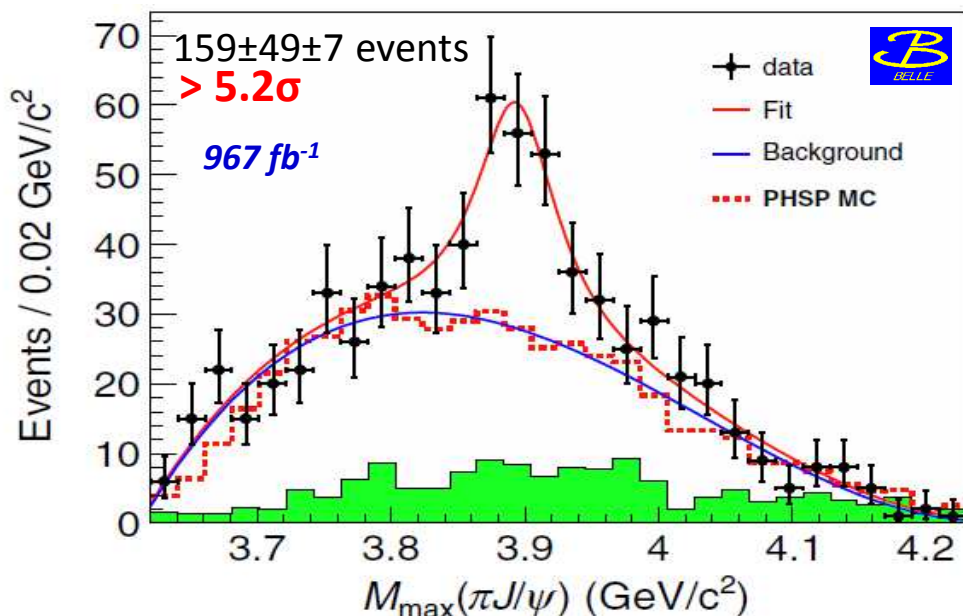


Intermediate state in $\Upsilon(4260) \rightarrow J/\psi \pi \pi$



Belle PRL110, 252002 (2013)

Observation of $Z(3895)^+$



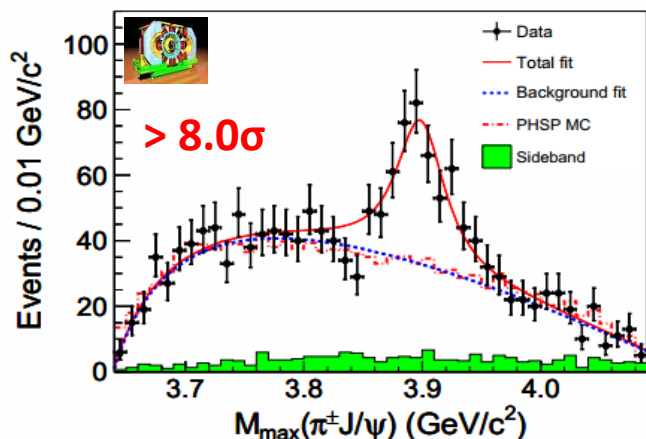
Measured properties

- Mass = $(3894.5 \pm 6.6 \pm 4.5) \text{ MeV}/c^2$
- Width = $(63 \pm 24 \pm 26) \text{ MeV}/c^2$

$$\frac{BR[Y(4260) \rightarrow Z(3895)^\pm \pi^\mp]}{BR[Y(4260) \rightarrow J/\psi \pi^+ \pi^-]} = (29.0 \pm 8.9)\%$$

Test hypothesis that interference between S and D waves in $\pi^+ \pi^-$ system might produce structure similar to the enhancement.

➤ Partial waves alone cannot produce $J/\psi \pi^\pm$ invariant mass peak near $3.9 \text{ GeV}/c^2$.



BESIII PRL110, 252001 (2013)

Measured by BES III

- Mass = $(3899.0 \pm 3.6 \pm 4.9) \text{ MeV}/c^2$
- Width = $(46 \pm 10 \pm 20) \text{ MeV}/c^2$

$$\frac{BR[Y(4260) \rightarrow Z(3900)^\pm \pi^\pm]}{BR[Y(4260) \rightarrow J/\psi \pi^+ \pi^-]} = (21.5 \pm 3.3)\%$$

T. Xiao, *et al.* arXiv:1304.3036 ¹⁹

Using CLEO data, T. Xiao *et al.* has also confirmed Z^+ and claim for an evidence for neutral Z !

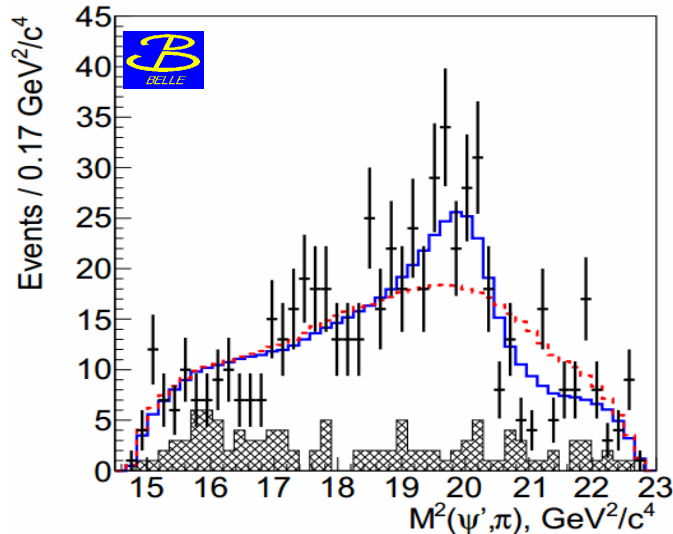
Quantum number of Z(4430)⁺

B⁰ → (Ψ'π⁺)K⁻ decay mode

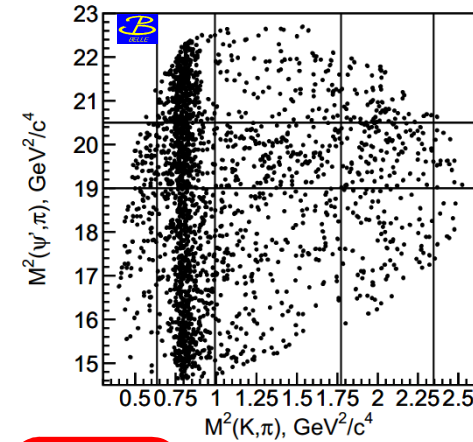
Amplitude analysis in 4D space is performed

M(Kπ), M(Ψ'π), Ψ' helicity and angle between Ψ' and K*

Projection of the fit results with K* veto



Mass and width consistent with previous Belle result

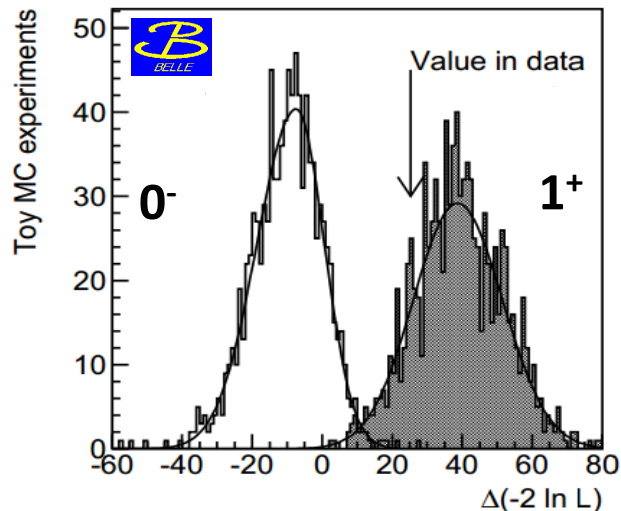


J ^P	0 ⁻	1 ⁻	1 ⁺	2 ⁻	2 ⁺
Mass, MeV/c ²	4479±16	4477±4	4485±20	4478±22	4384±19
Width, MeV	110±50	22±14	200±40	83±25	52±28
Significance	4.5σ	3.6σ	6.4σ	2.2σ	1.8σ

1⁺ hypothesis is favored

Exclusion levels calculated from toy MC

- 0⁻ not excluded
- 1⁺ is favored over 0⁻ by 2.9σ
- 1⁻, 2⁻ and 2⁺ are excluded at levels of 5.5σ, 4.3σ and 5.4σ

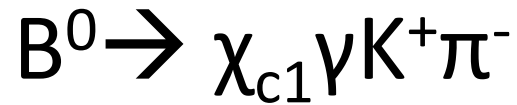


$$BR(B^0 \rightarrow \Psi' K^+ \pi^-) = (5.80 \pm 0.39) \times 10^{-4}$$

$$BR(B^0 \rightarrow \Psi' K^*(892)) = (5.55^{+0.22+0.41}_{-0.23-0.84}) \times 10^{-4}$$

$$BR(B^0 \rightarrow Z(4430) K^+) \times BR(Z(4430)^- \rightarrow \Psi' \pi^-) = 6.0^{+1.7+2.5}_{-2.0-1.4} \times 10^{-5}$$

711 fb⁻¹



Belle, PRL 111, 032001 (2013)

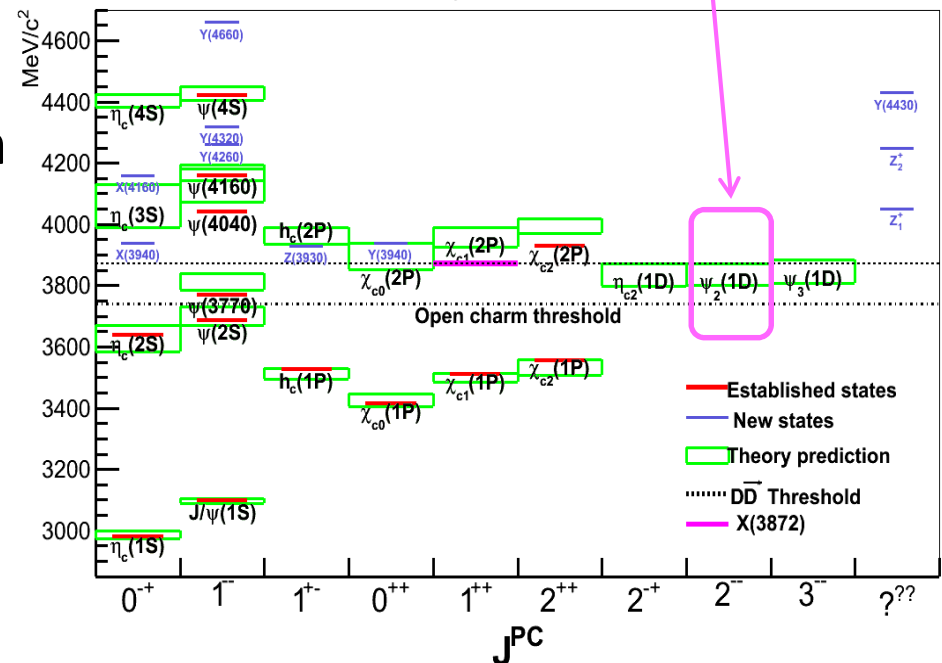
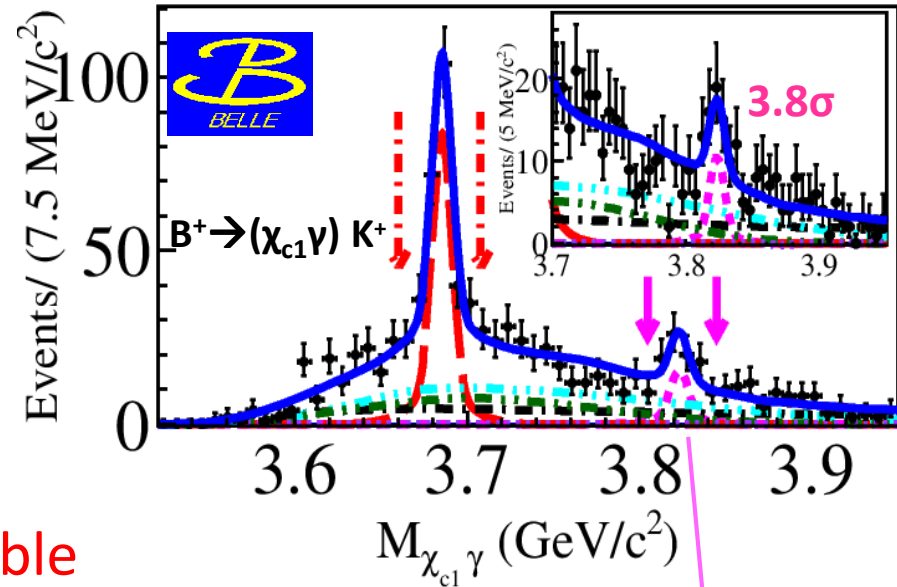
Belle found a narrow peak
 $X(3823) \rightarrow \chi_{c1} \gamma$ in $B^+ \rightarrow (\chi_{c1} \gamma) K^+$

Its narrow width and properties
suggest, it to be Ψ_{2D} ($2^-, 1^3D_2 c\bar{c}$)
charmonium state.

If so, it is suppressed in $B^+ \rightarrow \Psi_{2D} K^+$
But one can expect it to have reasonable
 $BR(B^+ \rightarrow \Psi_{2D} K^+ \pi^-)$

$B^0 \rightarrow \chi_{cJ} \gamma K^+ \pi^-$ useful mode to search
for $X(3823)$.

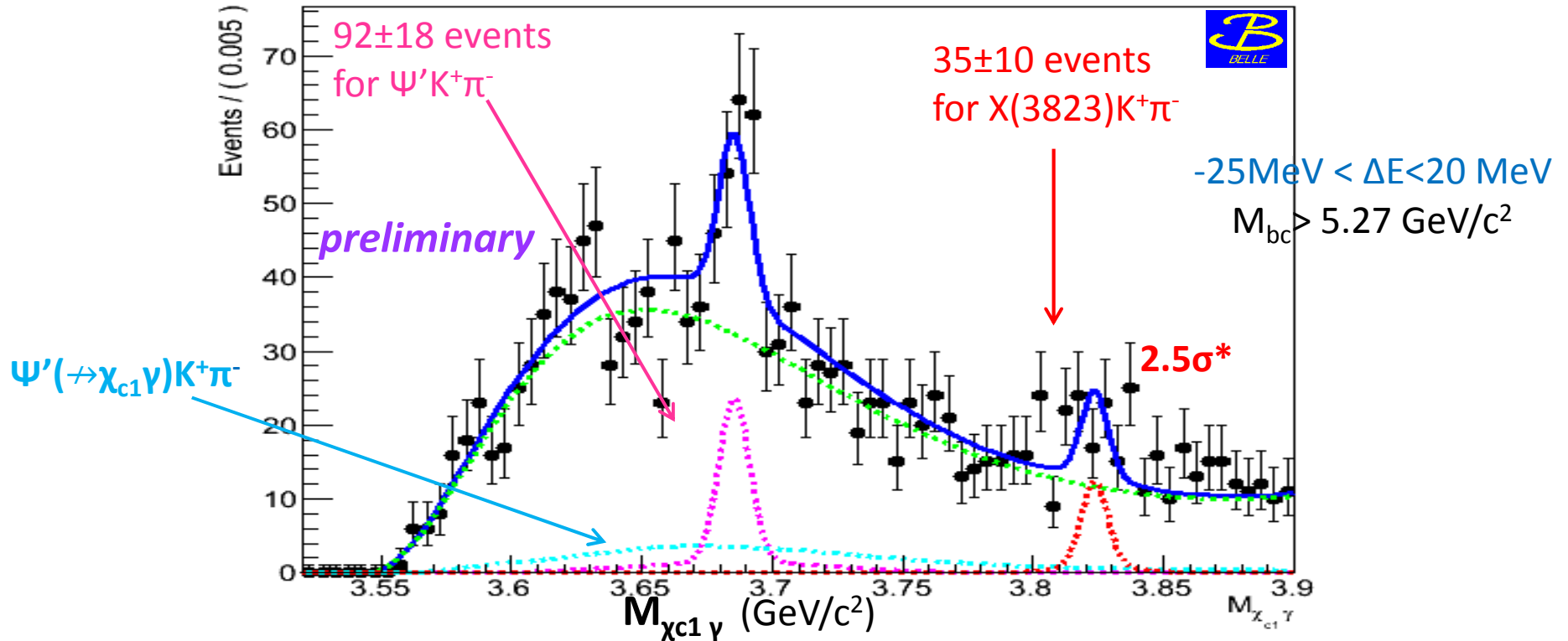
- -25 MeV < ΔE < 20 MeV
- E_γ scaled ($\Delta E=0$) to improve the resolution of $M_{\chi_{c1, c2} \gamma}$.
- Search for $X(3823)$ and other new state in $M_{\chi_{c1, c2} \gamma}$



NEW

Fit to X(3823)

$B^0 \rightarrow \chi_{c1} \gamma K^+ \pi^-$



Resolution fixed from Belle previous study of $B^+ \rightarrow (\chi_{c1} \gamma) K^+$ study

$$\frac{BR^\dagger(B^0 \rightarrow X(3823) K^+ \pi^-)}{BR(B^+ \rightarrow X(3823) K^+)} = 2.5 \pm 1.0 \text{ (stat. only)}$$

- o Large $BR(B \rightarrow X(3823) K^+ \pi^-)$, suggest its J to be 2.

*with systematic inclusion

† assumed efficiency for three body decay and one consider the central value

Summary

Bottomonium (-like)

- J^P of Z_b favored to be 1^+
- $Z_b(10610)^+$ and $Z_b(10650)^+$ decay to $B^{(*)}\bar{B}^*$
- First observation of neutral $Z_b(10610)^0$ in $\Upsilon(2S,3S)\pi^0$

Charmonium (-like)

- $\Upsilon(4260)$ is found to decay into $Z(3895)^+ \pi^-$ and further $Z(3895)^+$ decay into $J/\Psi\pi^+$
- J^P of $Z(4430)^+$ preferred as 1^+
- Hint of large $BR(B \rightarrow X(3823) K^+\pi^-)$, suggest its J to be 2

Belle is quite active in finding new quarkonium (-like) states and also in solving their mystery.

Other results, I didn't cover

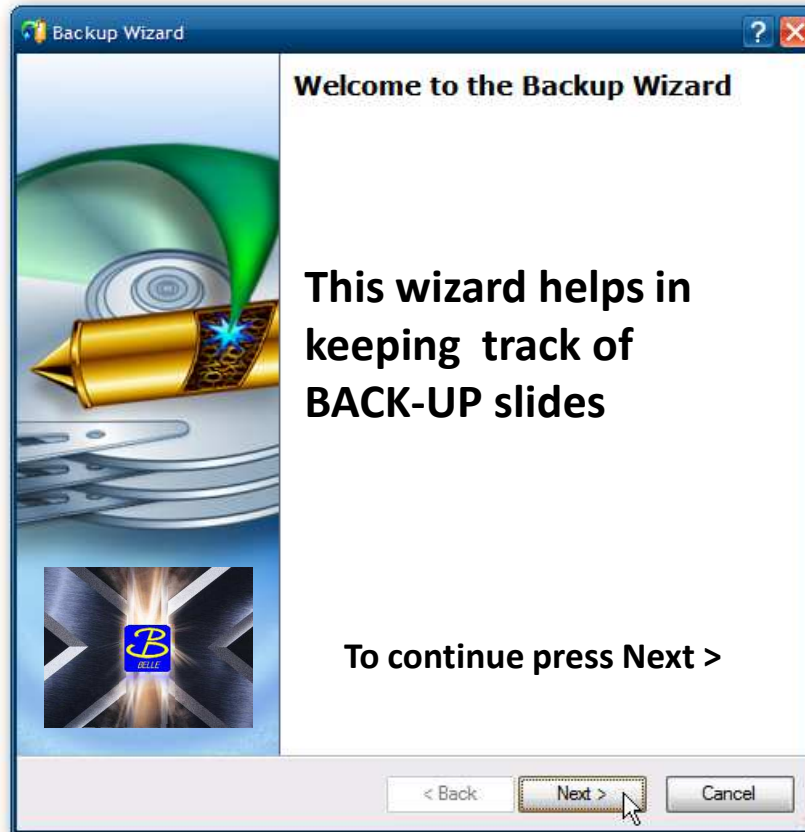
- Observation of $h_b(1P,2P) \rightarrow \eta_b(1S)\gamma$ **Belle PRL 109 232002(2012)**
- First evidence for $\eta_b(2S)$ **Belle PRL 109, 232002 (2012)**
- Disconfirmation of $X_{bb}(9975)$ by Belle. **Belle, PRL 111, 112001 (2013)**
- Search for C-odd partner of $X(3872)$ in $B \rightarrow (J/\Psi\eta)K$ **Belle, arXiv:1310.2704**
- Search for C-odd partner of $X(3872) \rightarrow \chi_{cJ}\gamma$ **Belle PRL 111, 032001 (2013)**
- Search for $X(3872)$ and χ_{c1}' in $\chi_{c1}\pi\pi K$. **E.Panzenboeck(Belle), Hadron 2013**
- Observation of $B \rightarrow X(3872)K\pi$. **A.Bala(Belle), Hadron2013**
- Observation of $\Psi(4040)$ and $\Psi(4160)$ decay into $\eta J/\Psi$ **Belle PRD 87, 051101(R) (2013)**
- Hadronic transitions $\Upsilon(2S) \rightarrow (\eta, \pi^0)\Upsilon(1S)$ **Belle, PRD 87, 011104(R) (2013)**
- Search for an H-dibaryon with mass near $2m_\Lambda$ in $\Upsilon(1S)$ and $\Upsilon(2S)$ decays **Belle, PRL 110, 222002 (2013)**

Visit archive of belle results

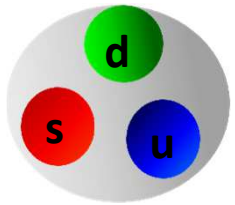
http://belle.kek.jp/bdocs/b_journal.html



Thank you



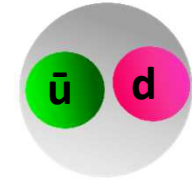
QCD : real particles are color singlet



Baryons are red-blue-green triplets

$\Lambda = usd$

Mesons are color-anticolor pairs

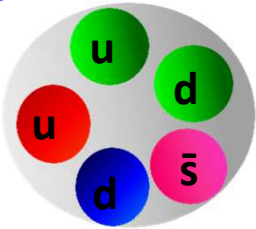


$\pi = \bar{u}d$

Other possible combinations of quarks and gluons :

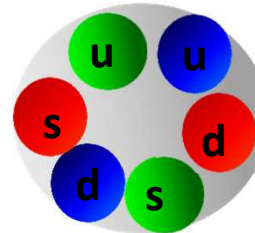
Pentaquark

$S = +1$
Baryon



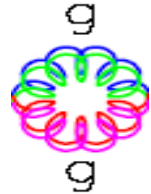
H di-Baryon

Tightly bound
6 quark state



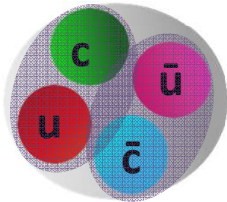
Glueball

Color-singlet multi-gluon bound state



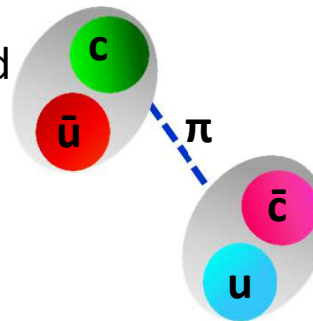
Tetraquark

Tightly bound
diquark &
anti-diquark

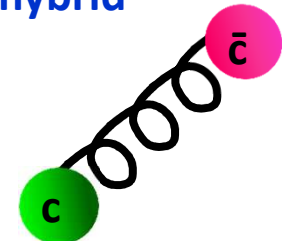


Molecule

loosely bound
meson-
antimeson
"molecule"



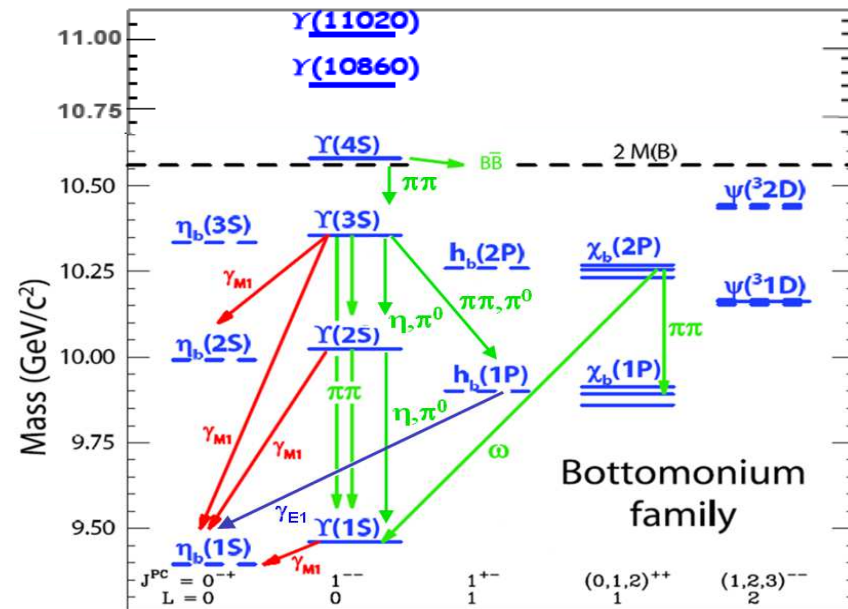
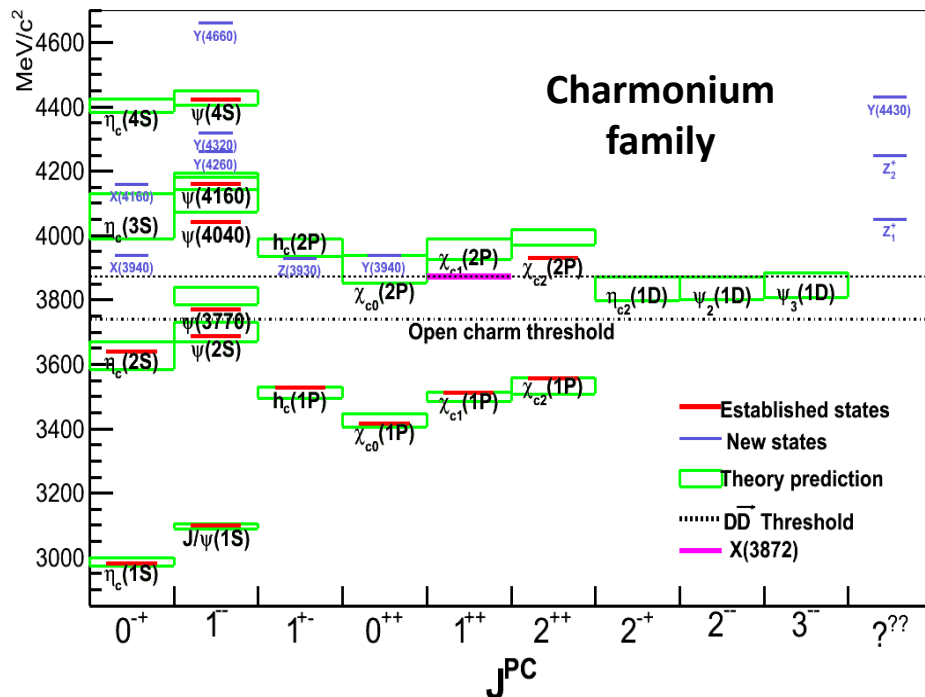
$q\bar{q}$ -gluon hybrid
mesons



Search for exotic states

Basic strategy follow:

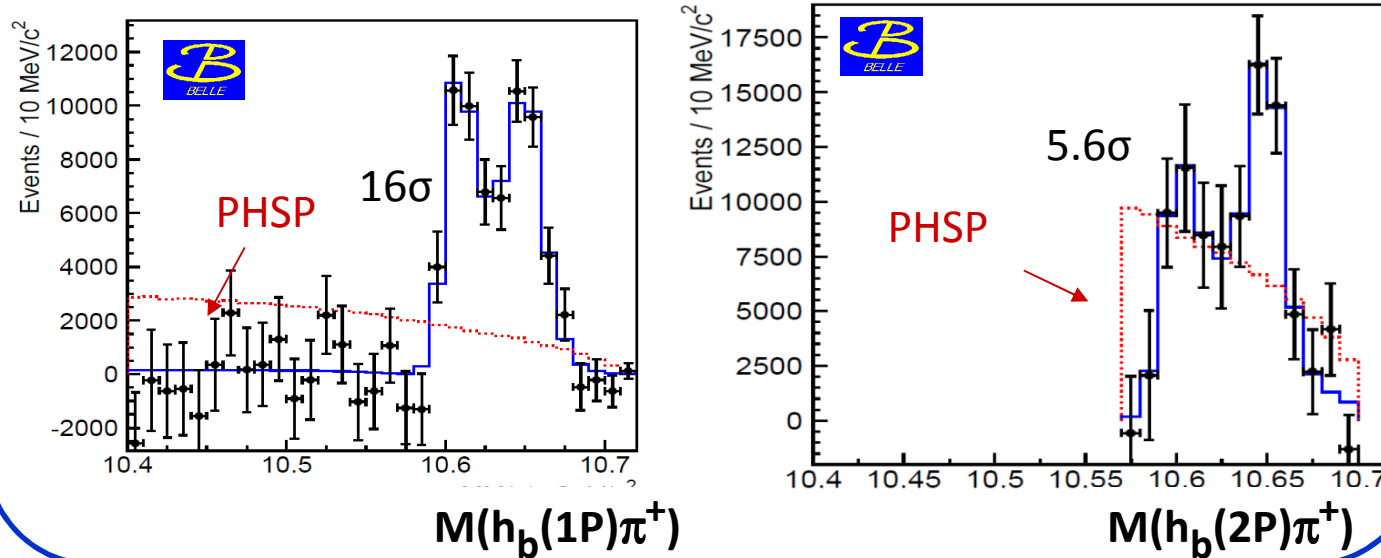
- Search for meson decaying into $c\bar{c}$ or similar state and study its properties.
- Observed particle found state among the expected states and also show expected properties then standard particle.
- If properties can't be easily explained, most probably exotic state



Resonant structure in $\Upsilon(5S) \rightarrow [(b\bar{b})\pi^+]\pi^-$

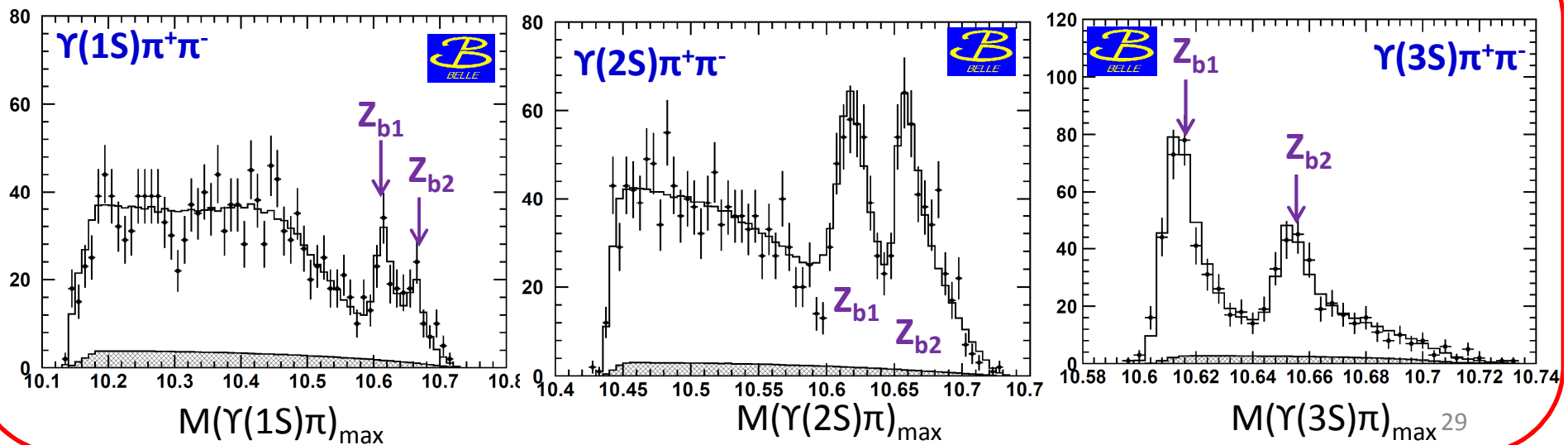
measure $\Upsilon(5S) \rightarrow h_b \pi \pi$ yield in bins of $MM(\pi)$

Belle, PRL108, 122001 (2012)



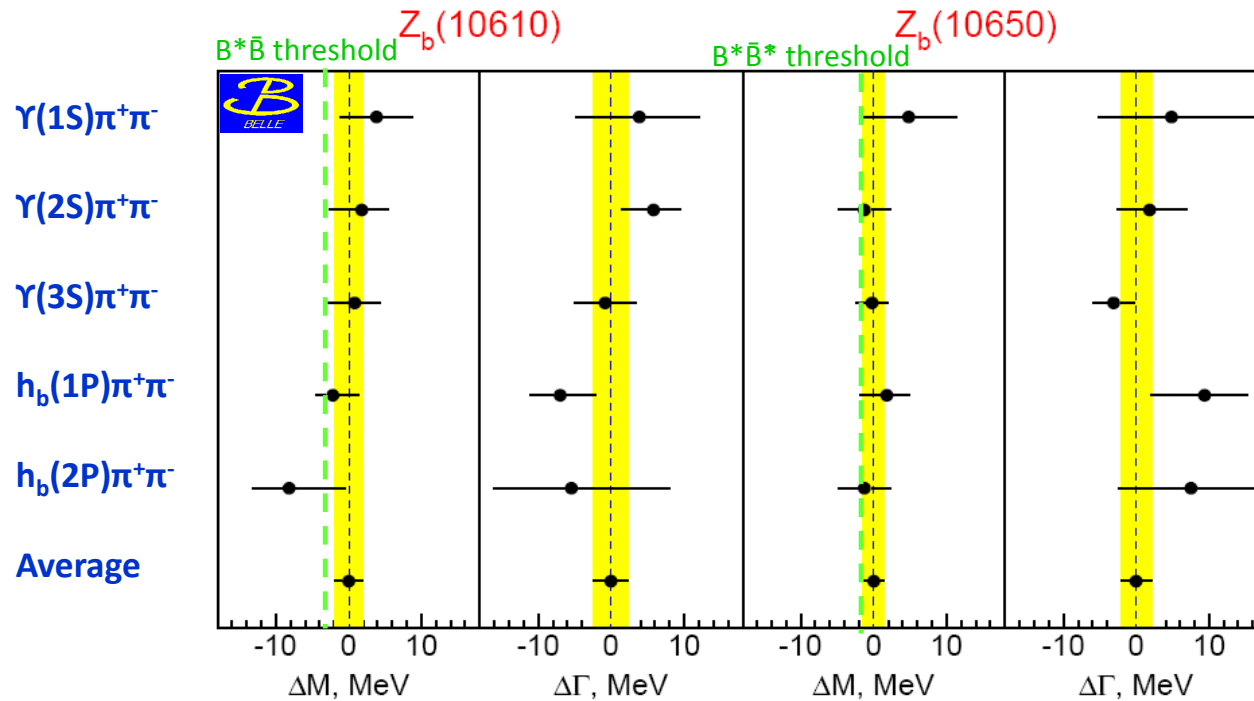
Two charged states observed $Z_b(10610)$ and $Z_b(10650)$!

Dalitz plot analysis of $\Upsilon(5S) \rightarrow \Upsilon(nS)\pi\pi$



$Z_b(10610)$ & $Z_b(10650)$

Belle, PRL108, 122001 (2012)



$Z_b(10610)$

$M=10607.2\pm 2.0$ MeV
 $\Gamma=18.4\pm 2.4$ MeV

PDG: $M_{\bar{B}} + M_{B^*} = 10604.8\pm 0.4$ MeV

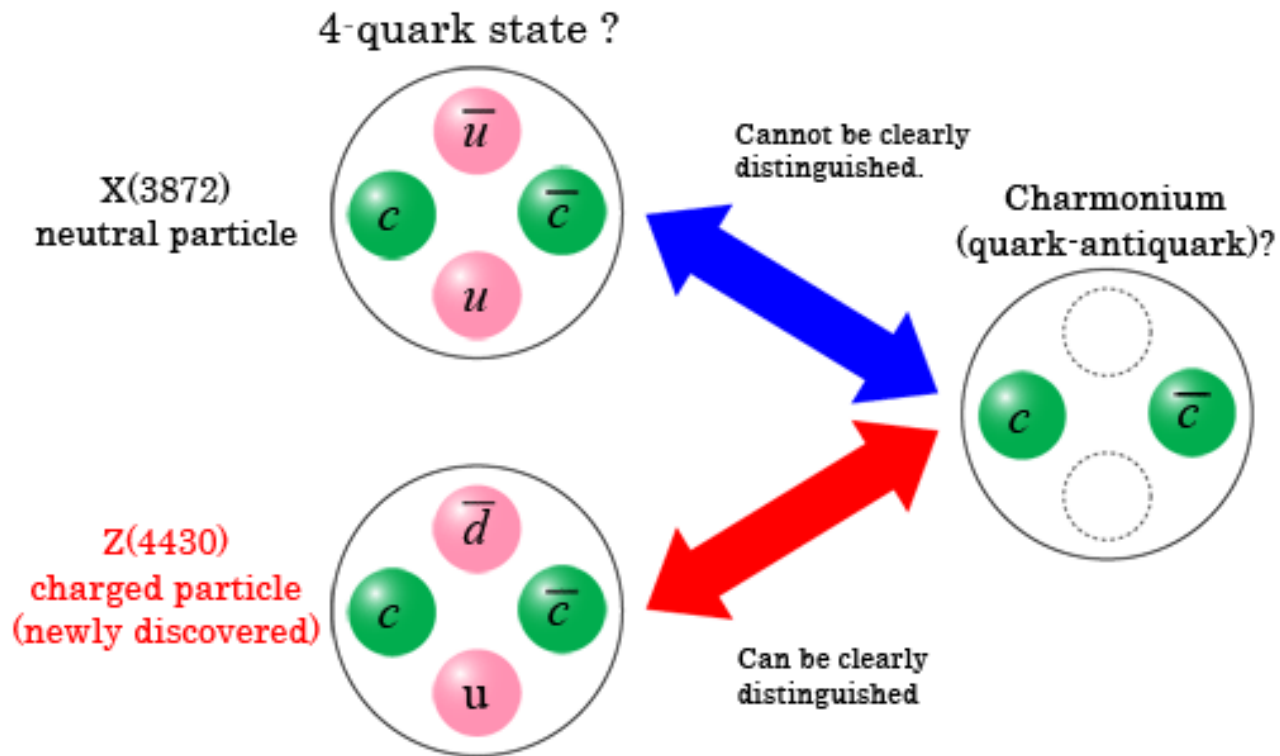
$Z_b(10650)$

$M=10652.2\pm 1.5$ MeV
 $\Gamma=11.5\pm 2.2$ MeV

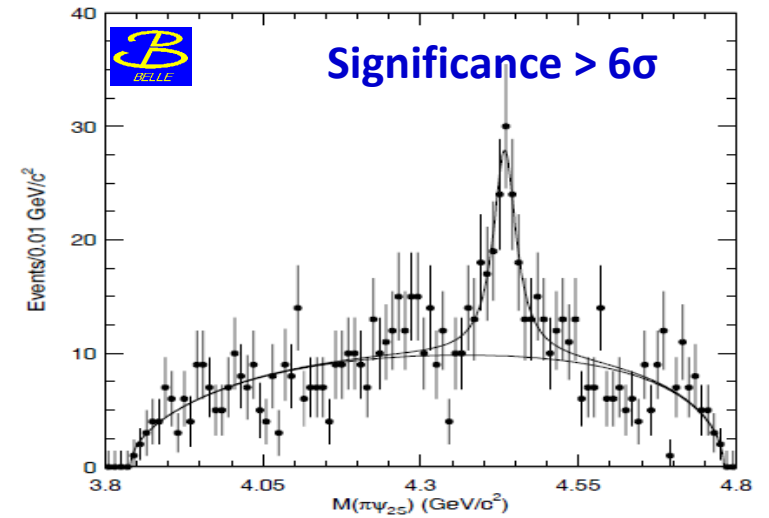
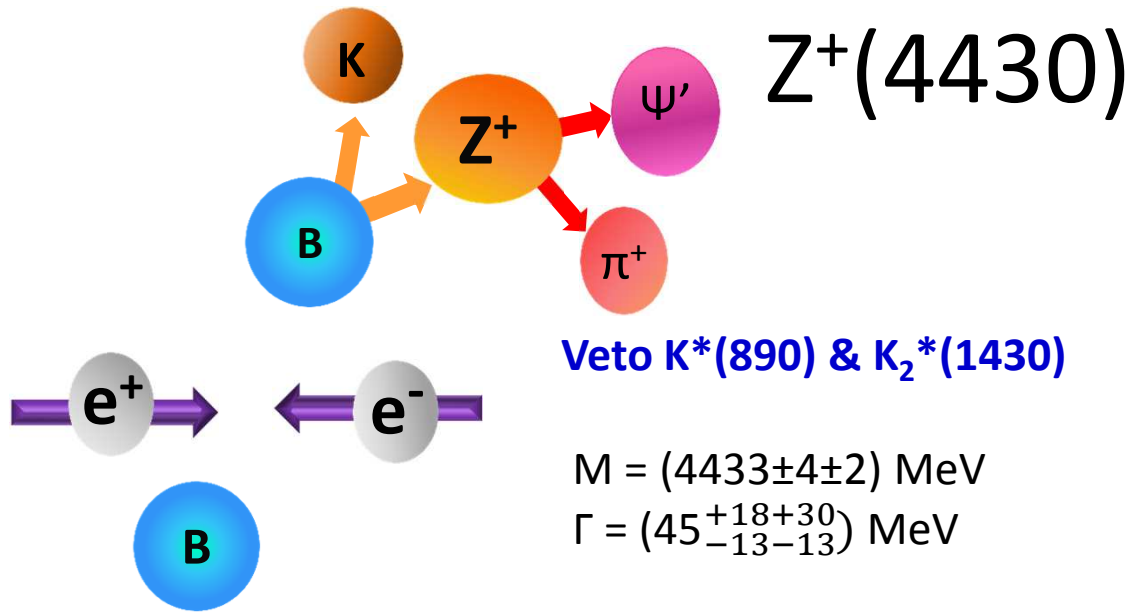
PDG: $M_{\bar{B}^*} + M_{B^*} = 10650.4\pm 0.8$ MeV

Parameters are consistent between the five states.
 Masses just above $B^*\bar{B}$ and $B^*\bar{B}^*$ thresholds.

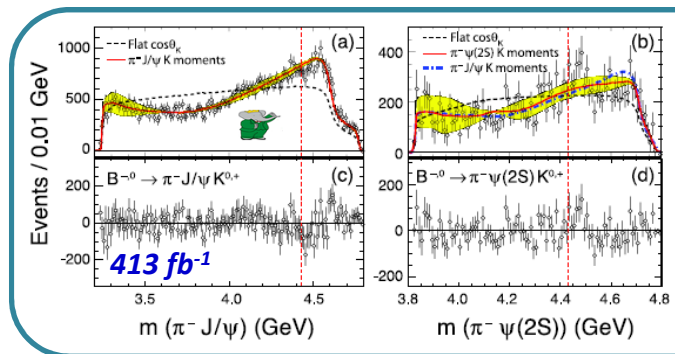
Charged $c\bar{c}$ -like states



Belle, PRL 100, 142001 (2007)



$$\text{BR}(\bar{B}^0 \rightarrow K^- Z(4430)^+) \times \text{BR}(Z(4430)^+ \rightarrow \Psi' \pi^+) = (4.1 \pm 1.0 \pm 1.4) \times 10^{-5}$$



BaBar didn't find conclusive evidence for the $Z(4430)^+$
 $\text{BR}(\bar{B}^0 \rightarrow K^- Z(4430)^+) \times \text{BR}(Z(4430)^+ \rightarrow \Psi' \pi^+) < 3.1 \times 10^{-5}$

BaBar data (due to less statistics) doesn't refute the Belle observation of $Z^+(4430)$

BaBar, PRD79, 112001 (2009)

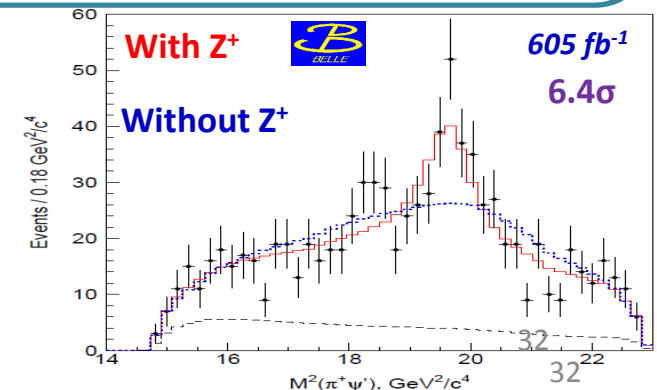
Re-analysis by Belle using sophisticated Dalitz fit

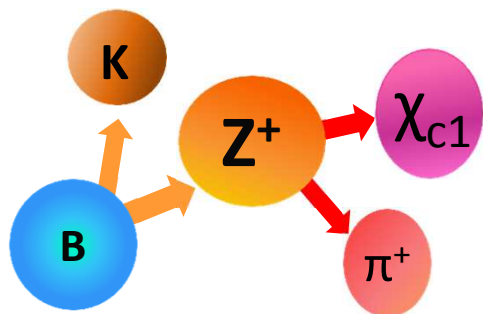
$$M = (4443^{+15+17}_{-12-13}) \text{ MeV}$$

$$\Gamma = (109^{+86+57}_{-43-52}) \text{ MeV}$$

Belle, PRD80, 031104 (2009)

$$\text{BR}(\bar{B}^0 \rightarrow K^- Z(4430)^+) \times \text{BR}(Z(4430)^+ \rightarrow \Psi' \pi^+) = (3.2^{+1.8+5.3}_{-0.9-1.6}) \times 10^{-5}$$





$Z_1^+(4050)$ & $Z_2^+(4250)$

Belle, PRD80, 031104 (2009)

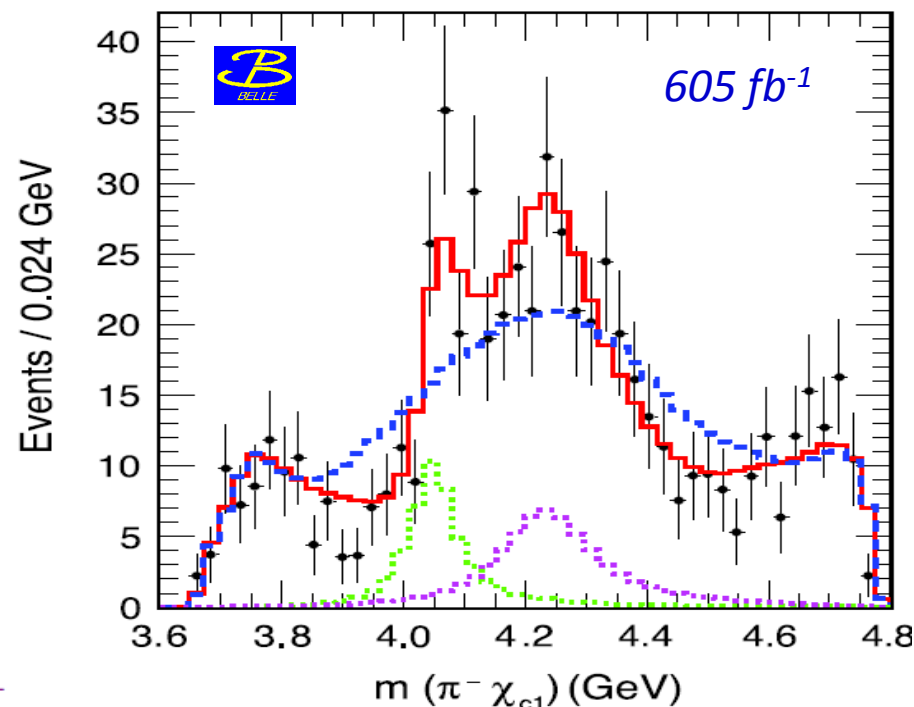
Isobar model :

$\chi_{c1}\pi^-$ resonance+ known $K\pi^+$

Without two Z^+ resonance

With two Z^+ resonance

Two resonance preferred at $> 5\sigma$

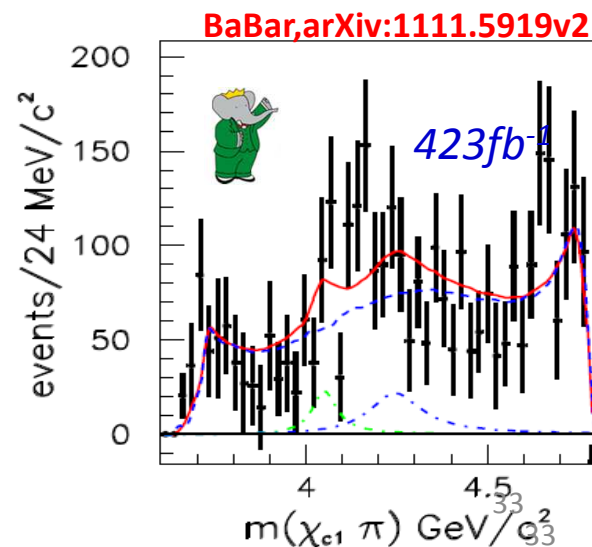


Z_1^+

Z_2^+

	Z_1^+	Z_2^+
M (MeV)	$4051 \pm 14_{-41}^{+20}$	$4248_{-29-35}^{+44+180}$
Γ (MeV)	82_{-17-22}^{+21+47}	$177_{-39-61}^{+54+316}$
$B_{\bar{B}^0} \times B_{Z^+} (\times 10^{-5})$	$(3.1_{-0.9-1.7}^{+1.5+3.7})$	$(4.0_{-0.9-0.5}^{+2.3+19.7})$

BaBar didn't find any strong evidence (in their search).
However, they are limited by less statistics.

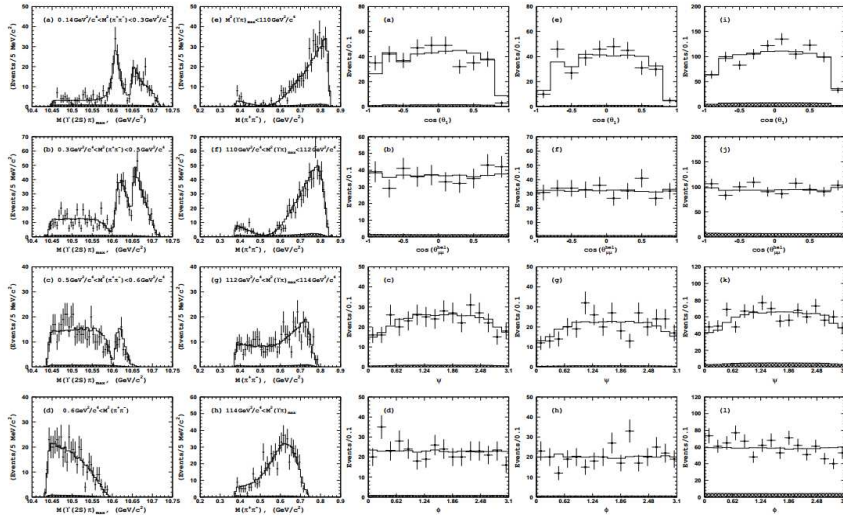


Measurement of J^P

Full amplitude analysis of $e^+e^- \rightarrow \Upsilon(nS)\pi^+\pi^- \rightarrow \mu^+\mu^-\pi^+\pi^-$ ($n=1,2,3$)

Amplitude analysis performed in 6D space :

- $M(\Upsilon(nS)\pi)_{\max}$
- $M(\pi^+\pi^-)$
- θ_1 : angle between prompt π and beam axis in c.m. frame
- $\theta_{\mu\mu}^{\text{hel}}$: angle between $\Upsilon(nS)$ momentum in Z_b rest frame and μ^+ momentum in $\Upsilon(nS)$ rest frame.
- ϕ angle between plane formed by π system and $\Upsilon(nS)$ decay plane in Z_b rest frame
- Ψ angle between plane formed by prompt pion and beam axis and the Z_b decay plane calculated in Z_b rest frame.



$J^P = 0^+$ and 0^- combinations are forbidden because of the observed decay channels $Z_b \rightarrow \Upsilon(nS)\pi$ and $Z_b \rightarrow h_b(mP)\pi$

FIG. 8: A detailed comparison of fit results (open histogram) with experimental data (points with error bars) for $\Upsilon(2S)\pi^+\pi^-$ events in the signal region. Hatched histogram shows the background component.

Charmonium

Bound state of c and \bar{c}

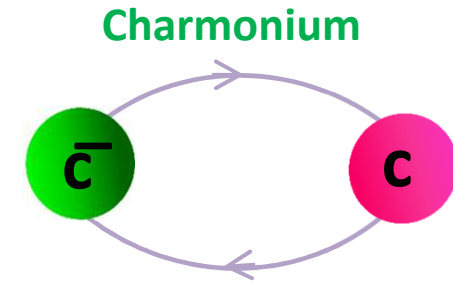
Spin : $\frac{1}{2}$ and $\frac{1}{2} = 0,1$

Orbital angular momentum: $L = 0,1,2,\dots$

Parity (P) = $(-1)^{L+1}$

Charge Conjugation (C) = $(-1)^{L+S}$

Total Spin : $\vec{J} = \vec{L} + \vec{S}$



$$V(r) = -\frac{4\alpha_s}{3r} + kr$$

(Cornell potential)

Quark model quantum numbers

$L=0, S=0 : J=0$	$J^{PC}=0^{-+}$
$L=0, S=1 : J=1$	$J^{PC}=1^{--}$
$L=1, S=0 : J=1$	$J^{PC}=1^{+-}$
$L=1, S=1 : J=0,1,2$	$J^{PC} = 0^{++} 1^{++} 2^{++}$
$L=2, S=0 : J=1$	$J^{PC}= 2^{-+}$
$L=2, S=1 : J=1,2,3$	$J^{PC}=1^{--} 2^{--} 3^{--}$

and so on..

Spectrum based on this, with spin-orbital, spin-spin and tensor term.

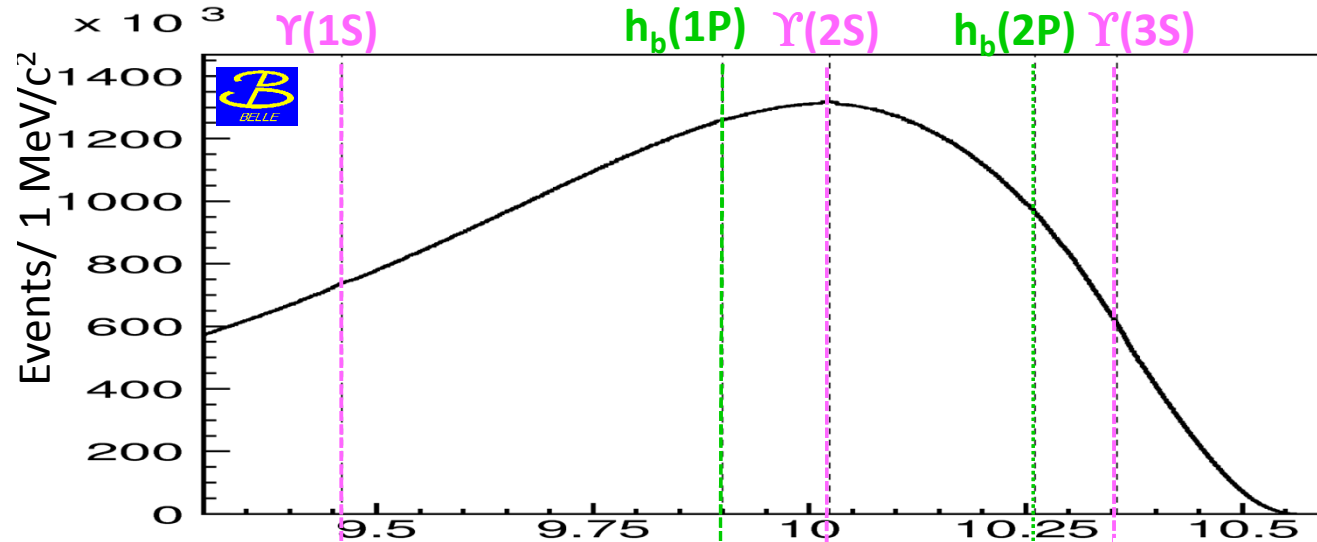
Exotic quantum number
 $0^+, 0^-, 1^+, 2^+$ and so on..

States not easily accommodated, candidates for exotic nature.

$\pi^+\pi^-$ recoil mass in $\Upsilon(5S) \rightarrow X \pi^+\pi^-$

121 fb⁻¹

Belle, PRL 108 032001

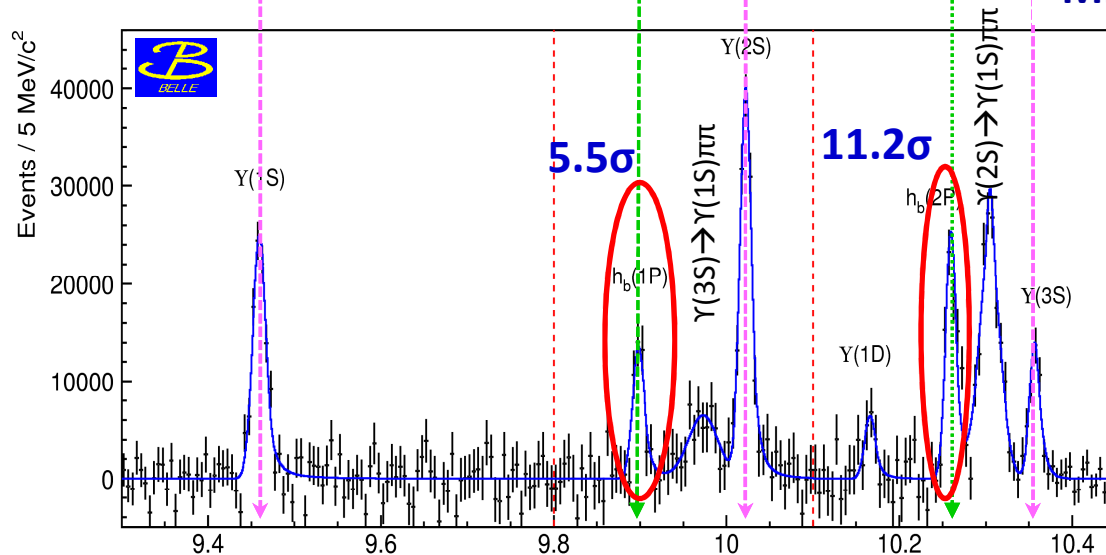


First observations

$h_b(1,2P)$

$J^{PC}=1^{+-}$

MM($\pi^+\pi^-$) spectrum



$h_b(1P)$,

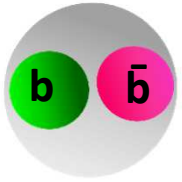
$M = (9898.25 \pm 1.06_{-1.07}^{+1.03}) \text{ MeV}$

$h_b(2P)$

$M = (10259.25 \pm 0.64_{-1.03}^{+1.04}) \text{ MeV}$

MM($\pi^+\pi^-$) residuals

MM($\pi^+\pi^-$) (GeV/c²)



$S=0, L=1,$
 $J^{PC}=1^{+-}$

$h_b(1P)$ & $h_b(2P)$

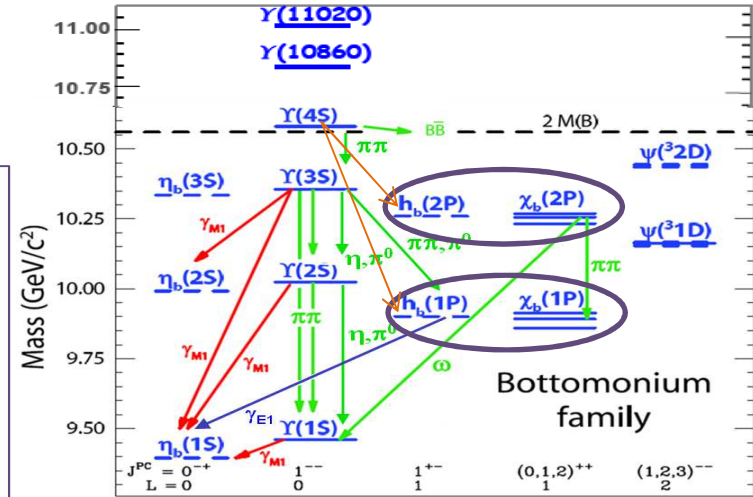
Expected mass $\approx (M_{\chi_{b0}} + 3 M_{\chi_{b1}} + 5 M_{\chi_{b2}}) / 9$

Hyperfine splitting :

$\Delta M_{HF} = M(\text{singlet}) - M(\text{triplet})$

$h_b(1P) \quad (1.7 \pm 1.5) \text{ MeV}/c^2$
 $h_b(2P) \quad (0.5^{+1.6}_{-1.2}) \text{ MeV}/c^2$

Deviation from
CoG of χ_{bj} mass
consistent with
zero as expected



Production ratio

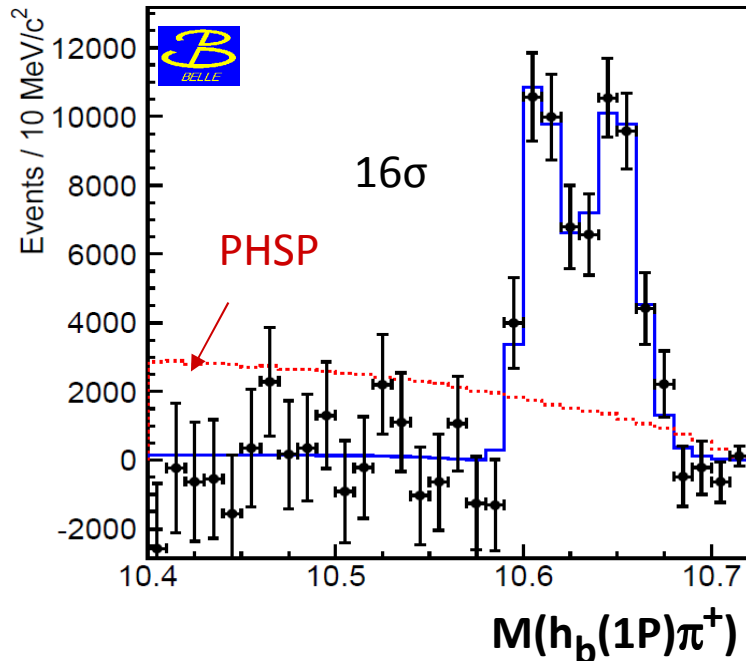
$$\begin{array}{c} \uparrow\downarrow \\ \uparrow\uparrow \end{array} \frac{\Gamma(Y(5S) \rightarrow h_b(nP)\pi^+\pi^-)}{\Gamma(Y(5S) \rightarrow Y(2S)\pi^+\pi^-)} = \begin{cases} 0.45 \pm 0.08^{+0.07}_{-0.12} & \text{for } h_b(1P) \\ 0.77 \pm 0.08^{+0.22}_{-0.17} & \text{for } h_b(2P) \end{cases}$$

Decay to h_b should be suppressed due to spin flip !

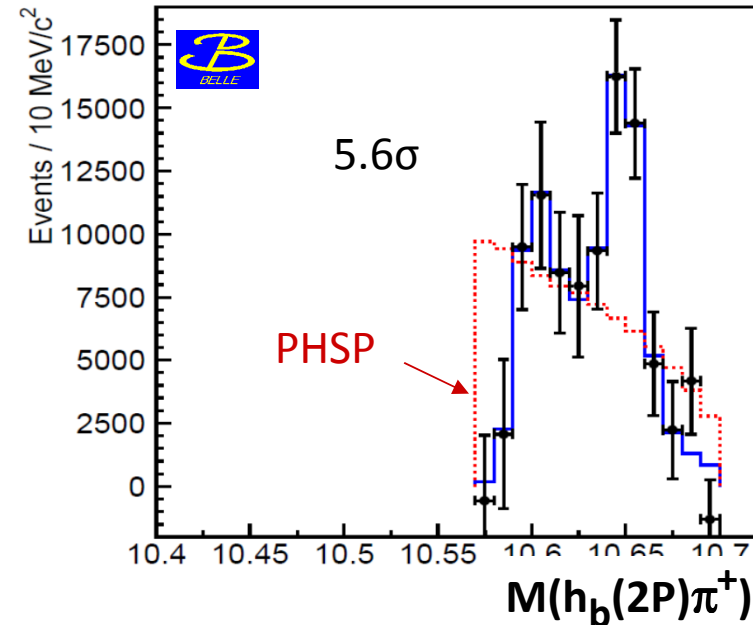
$Y(5S) \rightarrow h_b(nP)\pi^+\pi^-$ decay mechanism seems to be exotic

Resonant structure of $\Upsilon(5S) \rightarrow h_b(nP)\pi^+\pi^-$

measure $\Upsilon(5S) \rightarrow h_b\pi\pi$ yield in bins of $M(\pi\pi)$



Fit
MM(π) in
 $M(h_b\pi)$
bins



$$M_{Zb1} = (10605 \pm 2^{+3}_{-1}) \text{ MeV}$$

$$\Gamma = (11.4^{+4.5+2.1}_{-3.9-1.2}) \text{ MeV}$$

$$M_{Zb2} = (10654 \pm 3^{+1}_{-2}) \text{ MeV}$$

$$\Gamma = (20.9^{+5.4+2.1}_{-4.7-5.7}) \text{ MeV}$$

$\sim \bar{B} B^*$ threshold

$\sim \bar{B}^* B^*$ threshold

$$M_{Zb1} = (10599^{+6+5}_{-3-4}) \text{ MeV}$$

$$\Gamma = (13^{+10+2.1}_{-8-1.2}) \text{ MeV}$$

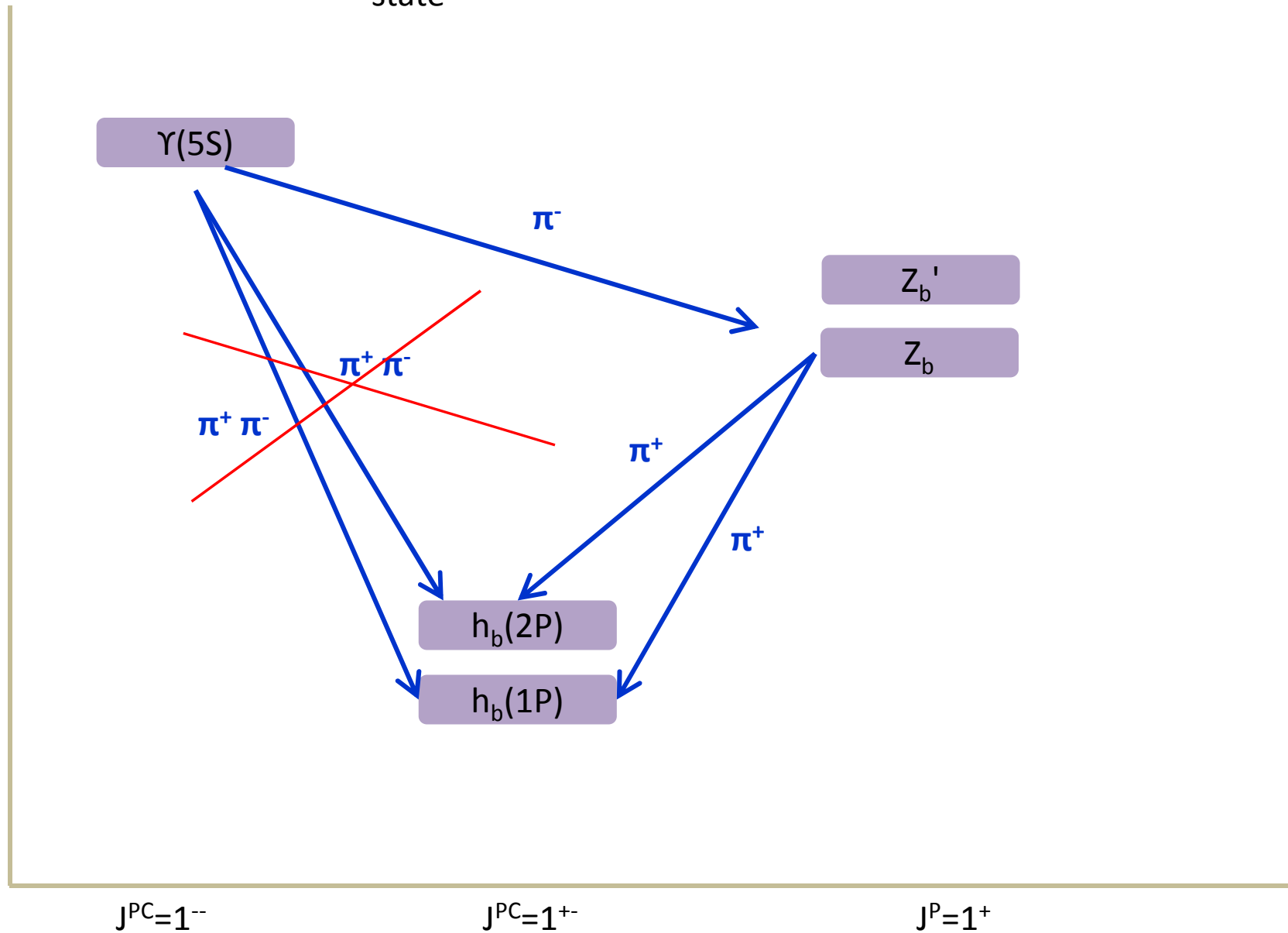
$$M_{Zb2} = (10651^{+2+3}_{-3-2}) \text{ MeV}$$

$$\Gamma = (19 \pm 7^{+11}_{-7}) \text{ MeV}$$

Resonance parameters are consistent for $h_b(1P)\pi\pi$ and $h_b(2P)\pi\pi$

Almost all $h_b(nP)$ are produced through $\Upsilon(5S) \rightarrow Z_b^+\pi^- \rightarrow h_b\pi^+\pi^-$

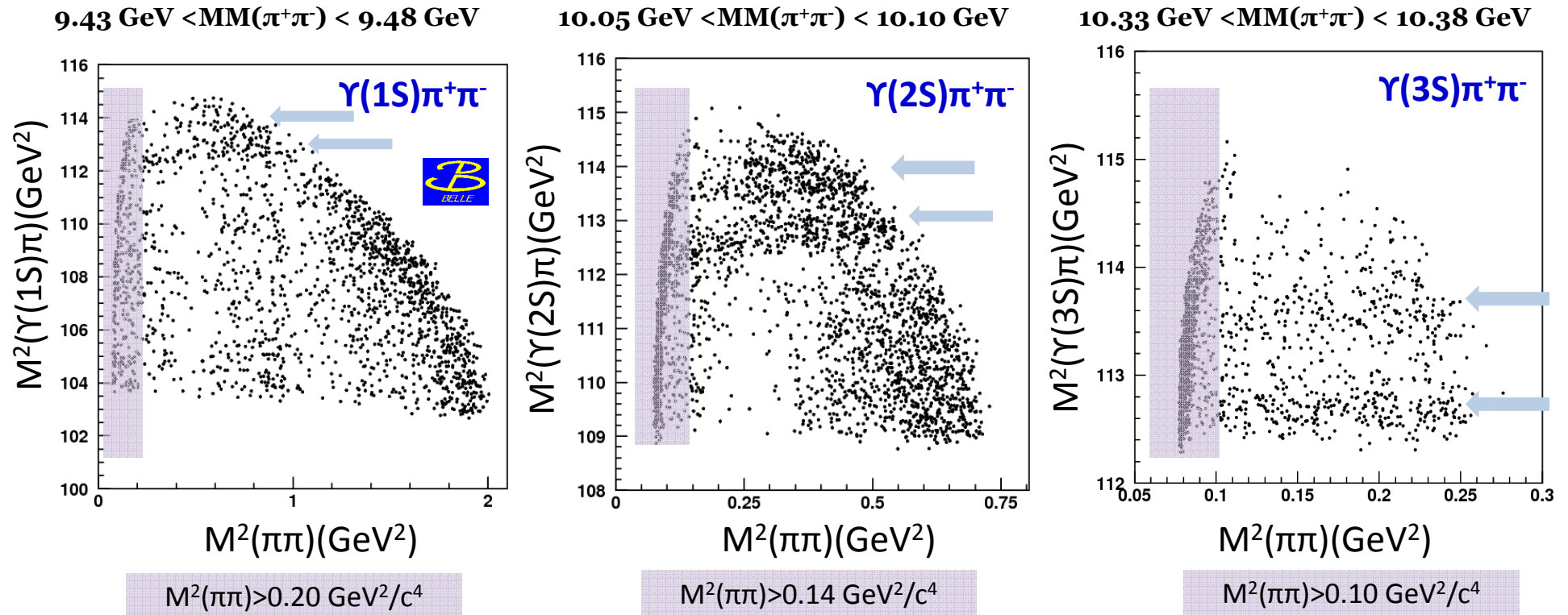
Instead, $\Upsilon(5S)$ decays via intermediate charged state



Z_b^+ should also be visible in
 $\Upsilon(5S) \rightarrow \Upsilon(nS)\pi^+\pi^-$

Resonant structure of $\Upsilon(5S) \rightarrow \Upsilon(nS) \pi^+ \pi^-$

Dalitz distribution



Excluded region with large background from photon conversions

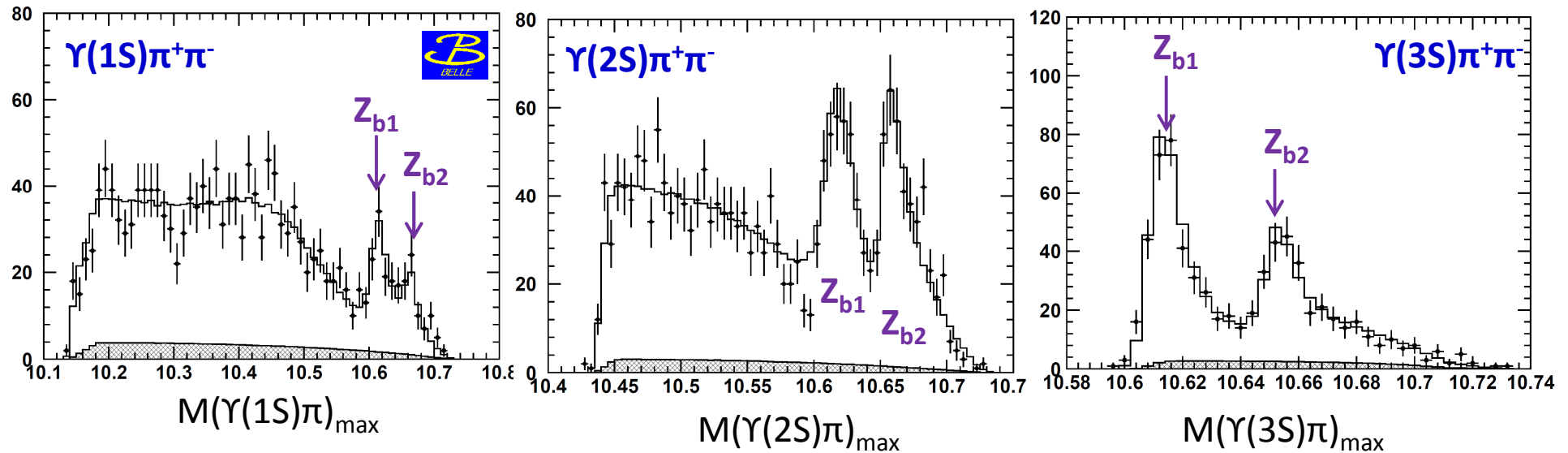
Signal amplitude parameterization:

$$S(s_1, s_2) = A(Z_{b1}) + A(Z_{b2}) + A(f_0(980)) + A(f_2(1275)) + A_{NR}$$

$$A_{NR} = C_1 + C_2 \cdot m^2(\pi\pi)$$

$A(Z_{b1}) + A(Z_{b2}) + A(f_2(1275)) \rightarrow$ Breit-Wigner
 $A(f_0(980)) \rightarrow$ Flatte

Fit result



$$M_{Z_{b1}} = (10611 \pm 4 \pm 3) \text{ MeV}$$

$$\Gamma = (22.3 \pm 7.7^{+3.0}_{-4.0}) \text{ MeV}$$

$$M_{Z_{b2}} = (10657 \pm 6 \pm 3) \text{ MeV}$$

$$\Gamma = (16.3 \pm 9.8^{+6.0}_{-2.0}) \text{ MeV}$$

$$M_{Z_{b1}} = (10609 \pm 2 \pm 3) \text{ MeV}$$

$$\Gamma = (24.2 \pm 3.1^{+2.0}_{-3.0}) \text{ MeV}$$

$$M_{Z_{b2}} = (10651 \pm 2 \pm 3) \text{ MeV}$$

$$\Gamma = (13.3 \pm 3.3^{+4.0}_{-3.0}) \text{ MeV}$$

$$M_{Z_{b1}} = (10608 \pm 2 \pm 3) \text{ MeV}$$

$$\Gamma = (17.6 \pm 3.0 \pm 3.0) \text{ MeV}$$

$$M_{Z_{b2}} = (10652 \pm 1 \pm 2) \text{ MeV}$$

$$\Gamma = (8.4 \pm 2.0 \pm 2.0) \text{ MeV}$$

Consistent peaks in all three channels