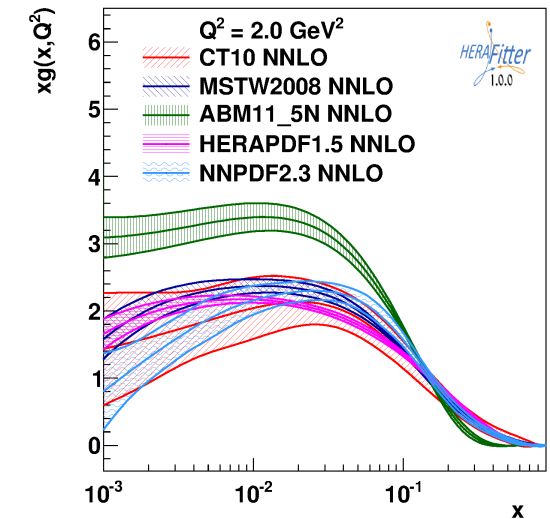


# HERAFitter

Open Source QCD Fit Platform  
to determine PDFs



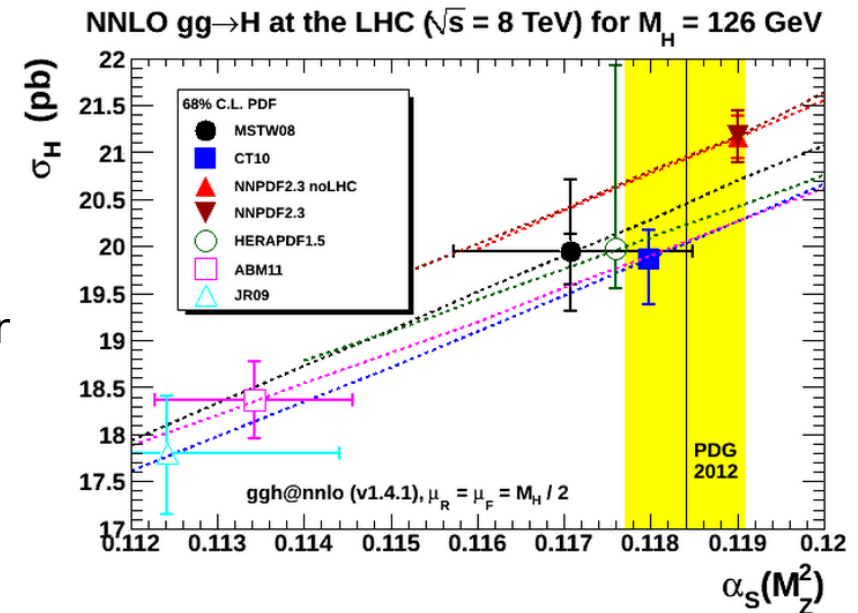
## Outline:

- Motivation
- Project Overview
- Functionality
- Application and Results

# Motivation

- PDFs are essential for precision physics at the LHC:
  - PDFs are one of the main theory uncertainties in Higgs production
  - PDF uncertainties also affect theory predictions for BSM high mass production
- PDF uncertainties arise from:
  - Precision of experimental data
  - Differences among several groups:
    - MSTW, CT, NNPDF, HERAPDF, ABM, JR
    - Current benchmarking of PDFs

10% differences among PDF groups for predictions for the Higgs cross section



G. Watt (November 2012)

→ **crucial to understand the theoretical differences**

[G. Watt, Nov 2012]

→ **important to provide accurate data for better PDF discrimination**

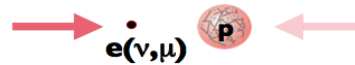
HERAFitter provides an ideal framework for

- Investigation of different methodologies in PDF fits
- Assess the impact of data on PDF → improve the sensitivity of new measurements to PDF

# Proton Structure

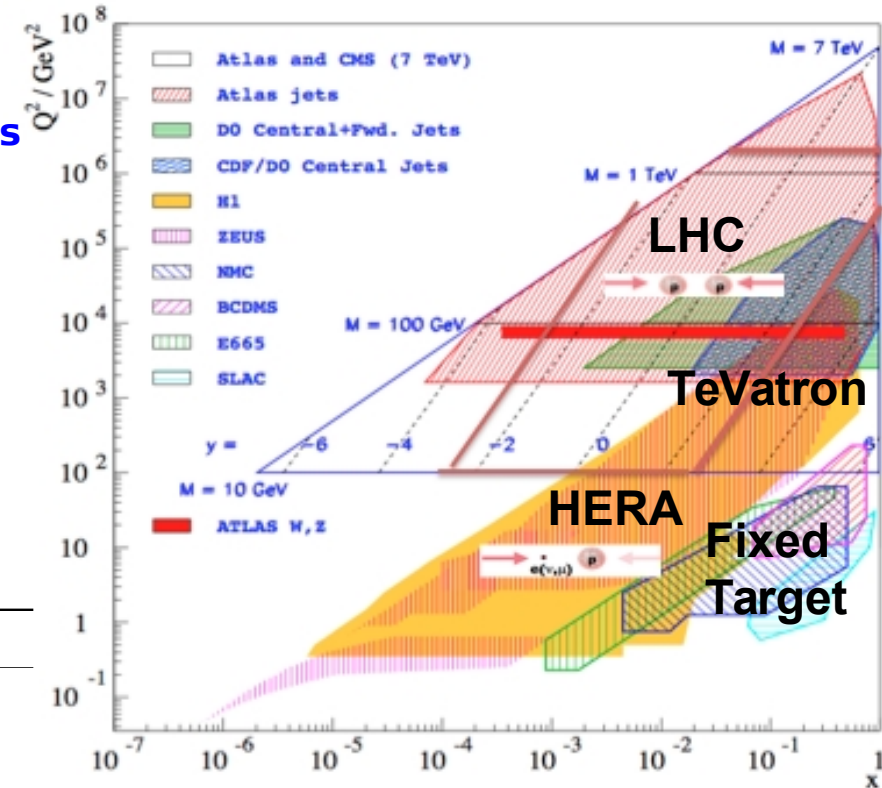
PDF determination relies on factorisation theorem:  
cross sections: PDFs  $\otimes$  hard scattering coefficients

Main constraint on PDFs comes from DIS data at HERA which probes linear combination of quarks:



$$F_2 \sim 0.44x(u + \bar{u} + c + \bar{c}) + 0.11x(d + \bar{d} + s + \bar{s} + b + \bar{b})$$

**No flavour decomposition of the sea**



Measurement at LHC	PDF sensitivity
Jets	high x quarks and gluons (alphas)
Inclusive W, Z and asymmetries	quark flavour separation (u,d,s)
Low and high mass Drell-Yan	quarks at low and high x (u,d)
W + charm	Direct sensitivity to s-quark
Isolated photons	medium - x gluons
Single top	u,d and b quark
ttbar (total, differential)	Medium-x gluon (alphas)
W,Z production with jets	Medium-x gluon
Z+b production	sensitive to b-quark

Coverage in x is essential  
QCD evolution is in  $Q^2$

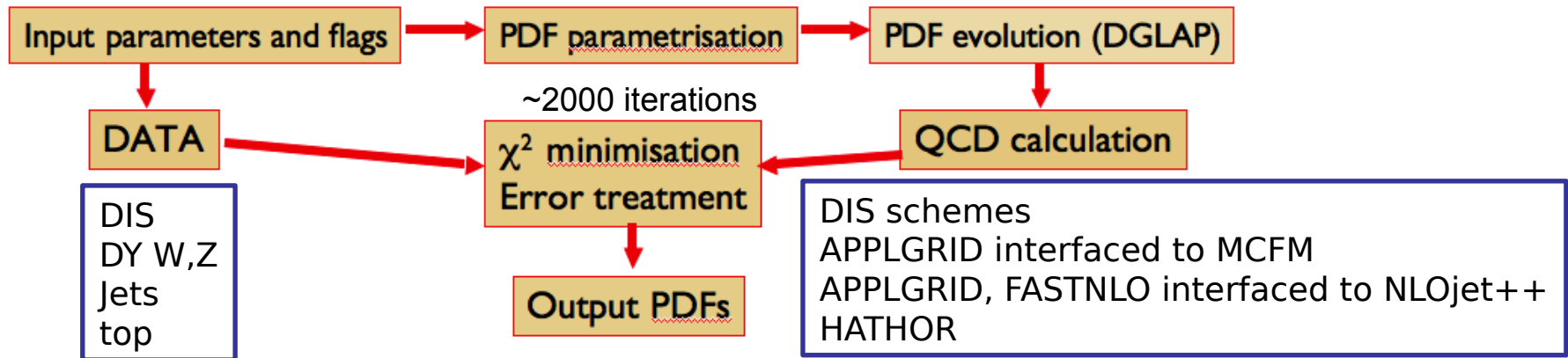
LHC provides new observables and precise measurements to better constraint

- Flavour decomposition of the sea
- Gluon PDF



# Schematics of PDFs determination

Flow diagram of PDF determination in QCD fit

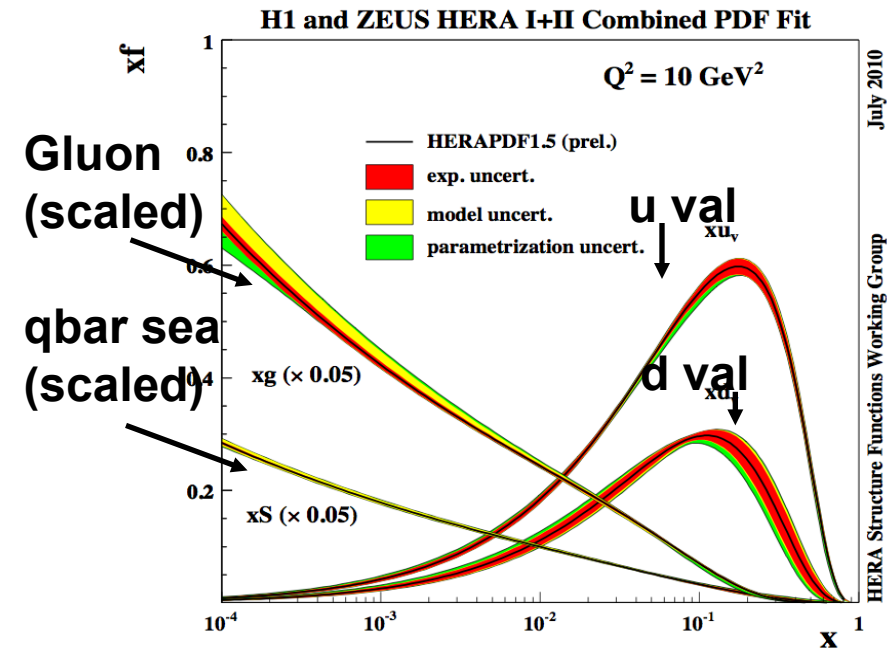


## Data

- Important to provide uncertainties correlation

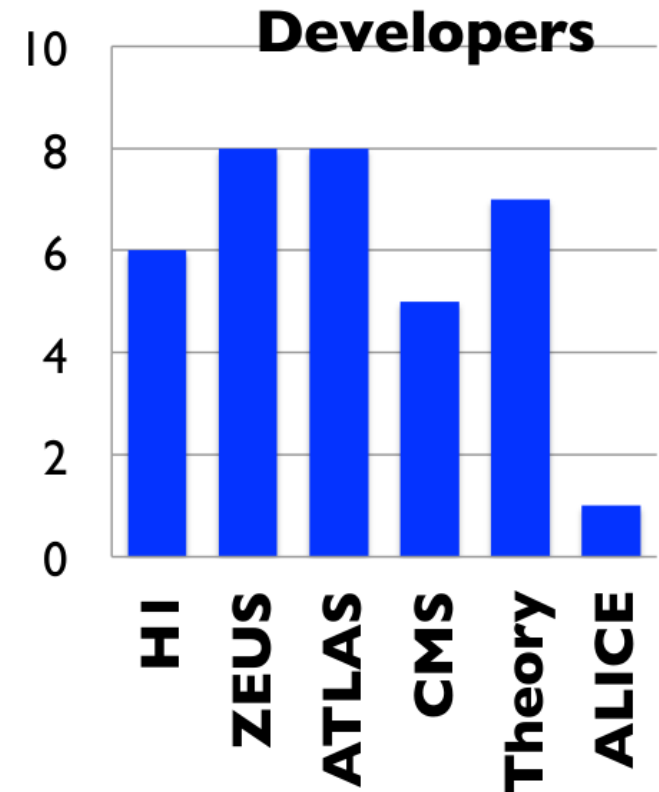
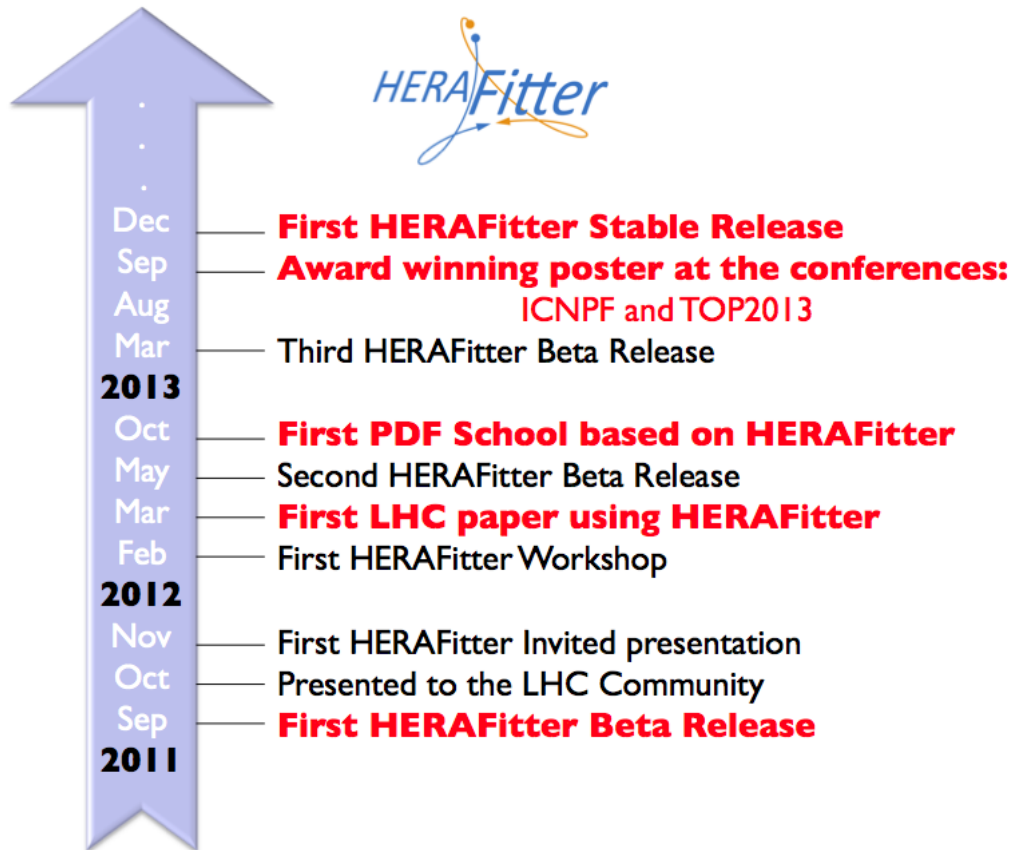
## Theory

- Need fast tools to perform PDF fits:  
APPLGRID, FASTNLO  
→ grid techniques relying on factorisation theorem



# HERAFitter Project

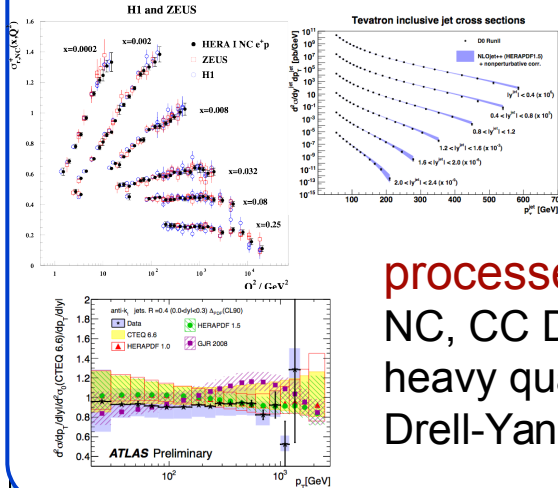
Dec 2013 → First Stable Release HERAFitter 1.0.0



- **Unique framework to address PDF theoretical differences**
- **Provides means to the experimentalists to assess impact of new data**

# HERAFitter 1.0.0 in a glance

## experimental input



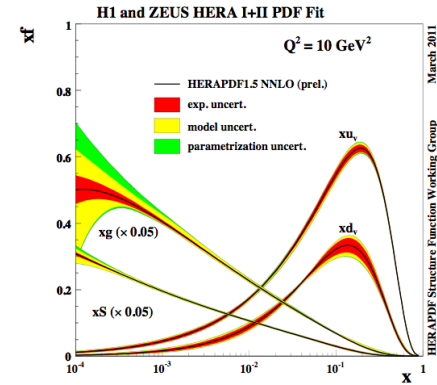
**experiments:**  
HERA, Tevatron,  
LHC, fixed target

**processes:**  
NC, CC DIS, jets, diffraction,  
heavy quarks (c,b,t)  
Drell-Yan, W production

## theoretical calculations/tools

Heavy quark schemes: MSTW, CTEQ, ABM  
 Jets, W, Z production: fastNLO, Applgrid  
 Top production NNLO (Hathor)  
 QCD Evolution DGLAP (QCDNUM)  
 kT factorisation  
 Alternative tools NNPDF reweighting  
 Other models Dipole model  
 + Different error treatment models  
 + Tools for data combination (HERAaverager)

HERAFitter



PDF or uPDF or DPDF

$\alpha_S$  (MZ), mc, mb, mt,  
fs,..

Theory predictions

Benchmarking

Comparison of schemes

# Heavy Flavour Schemes in DIS

For the DIS process, several schemes are available for heavy quark treatments:

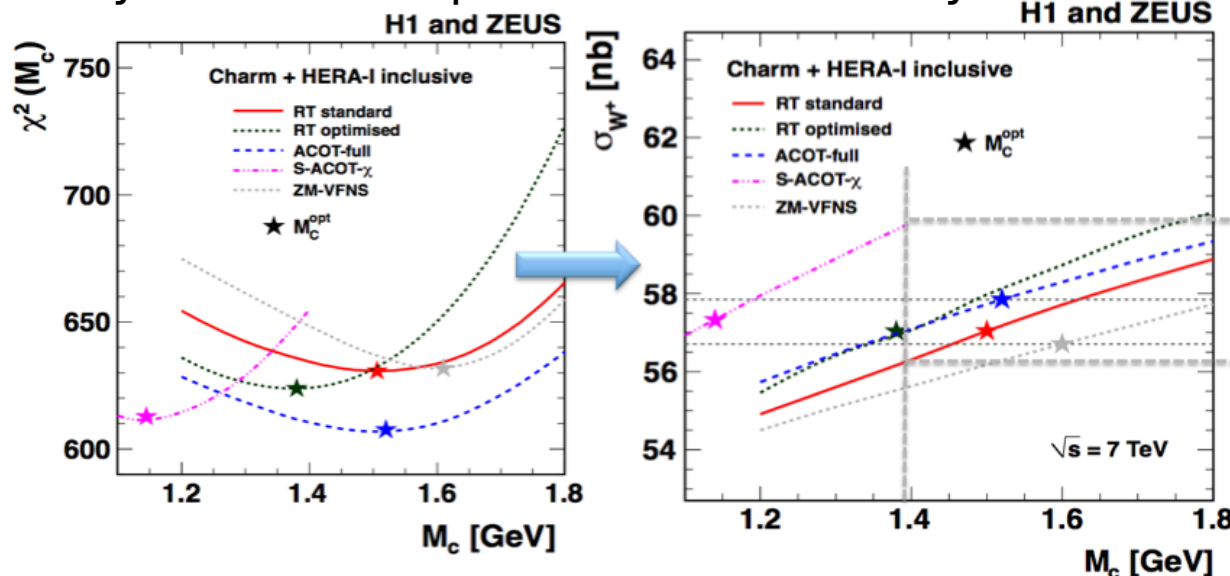
- **VFNS (Variable Flavour Number Schemes):**

- ▾ RT-VFNS schemes (RT Standard, RT Optimal) – as used by MSTW group (as well as variants based on k-factors RT FAST, RT OPT FAST)
- ▾ Zero Mass VFNS [qcdnum, ACOT variant]
- ▾ ACOT Full, ACOT Chi, ACOT ZM, they are all based on k-factors – as used by CT group

- **FFNS (Fixed Flavour Number Scheme)**

- ▾ via QCDNUM
- ▾ Via Openqcdrad-1.6 – as used by ABM

Variety of scheme options was studied by HERA in F2 charm HERA combined paper



[Eur. Phys. J. C73 (2013) 2311]

Spread in predictions for W and Z is reduced significantly when predictions are evaluated at the optimal  $M_c$  determined from F2 charm

# Chi square definitions

- Typical measurements sensitive to PDFs are precise, with statistical uncertainties below 10%, so they follow normal distribution which allows use of chi square minimization for determining optimal PDF parameters.
- The HERAFitter package allows for various types of data uncertainty treatment:
  - ▽ Various chi square representations:

- **Simple form:**

$$\chi_{\text{exp}}^2(\mathbf{m}, \mathbf{b}) = \sum_i \frac{[m^i - \sum_j \gamma_j^i m^i b_j - \mu^i]^2}{(\delta_{i,\text{stat}} \mu^i)^2 + (\delta_{i,\text{uncor}} \mu^i)^2} + \sum_j b_j^2.$$

- **Scaled form:**

$$\chi_{\text{exp}}^2(\mathbf{m}, \mathbf{b}) = \sum_i \frac{[m^i - \sum_j \gamma_j^i m^i b_j - \mu^i]^2}{\delta_{i,\text{stat}}^2 \mu^i (m^i - \sum_j \gamma_j^i m^i b_j) + (\delta_{i,\text{uncor}} m^i)^2} + \sum_j b_j^2 + \text{log penalty}$$

- **Mixed form (covariance and nuisance parameter):**

$$\chi_{\text{exp}}^2(\mathbf{m}, \mathbf{b}) = \sum_{ij} \left( m^i - \sum_l \Gamma_l^i(m^i) b_l - \mu^i \right) C_{\text{stat. } ij}^{-1}(m^i, m^j) \left( m^j - \sum_l \Gamma_l^j(m^j) b_l - \mu^j \right) + \sum_l b_l^2.$$



# Experimental Uncertainties

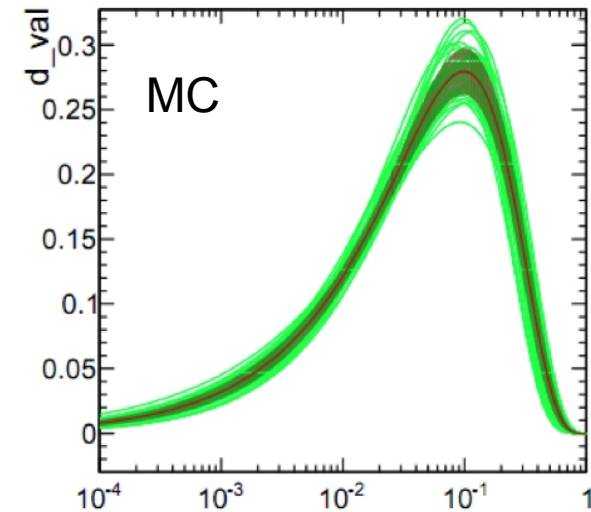
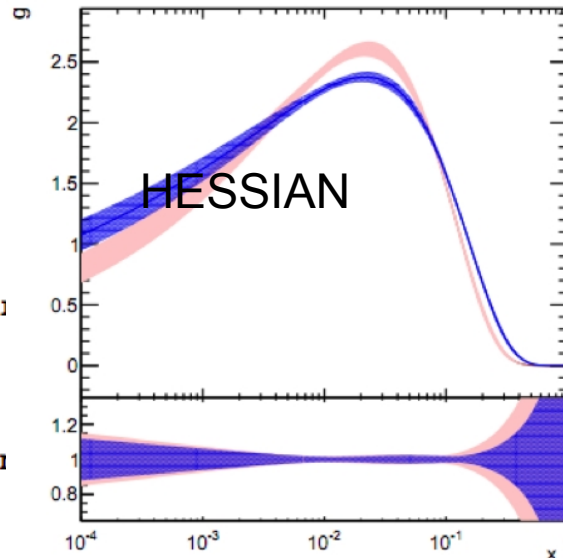
HERAFitter provides various methods for the treatment of experimental uncertainties

- Asymmetric Hessian errors
- Monte Carlo errors

&MCErrors

```
lRAND = False
lRANDDATA = True
ISeedMC = 123456
! --- Choose what distribution for the
! STATYPE (SYS_TYPE) = 1 gauss
! STATYPE (SYS_TYPE) = 2 uniform
! STATYPE (SYS_TYPE) = 3 lognormal
! STATYPE (SYS_TYPE) = 4 poisson ( $\alpha$ )
STATYPE = 1
SYSTYPE = 1
```

&End



- Monte Carlo Method for error estimation compared to Hessian error propagation:
  - Benchmarking exercise with NNPDF group [arXiv:0901.2504]
  - Regularisation methods: constrain PDFs with a flexible parametrisation style
    - Data Driven Regularisation (as used by NNPDF) fit and control samples
    - External Regularisation based on a penalty term in chisq

# Quantitative Comparison between data and theory

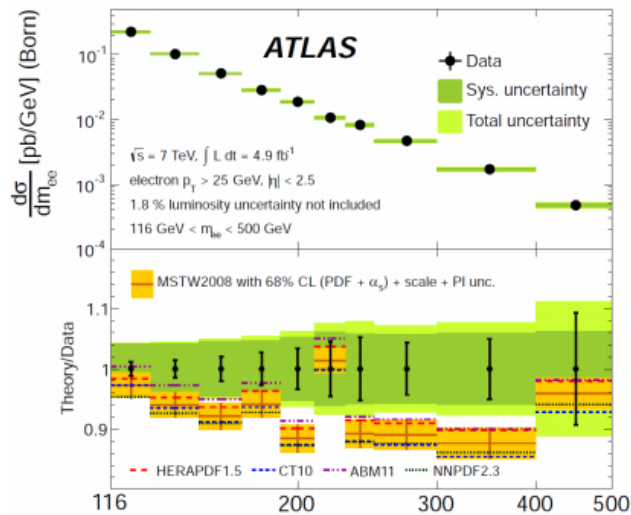
HERAFitter provides a quantitative assessment of level of agreement between data and theory by taking into account theoretical and experimental uncertainties

$$\chi^2 = \sum_i \left( \frac{\mu_i - m_i \left[ 1 + \sum_j b_j^{\text{exp}} \gamma_{ji}^{\text{exp}} + \sum_j b_j^{\text{theo}} \gamma_{ji}^{\text{theo}} \right]}{\Delta_i} \right)^2 + \sum_j (b_j^{\text{exp}})^2 + \sum_j (b_j^{\text{theo}})^2$$

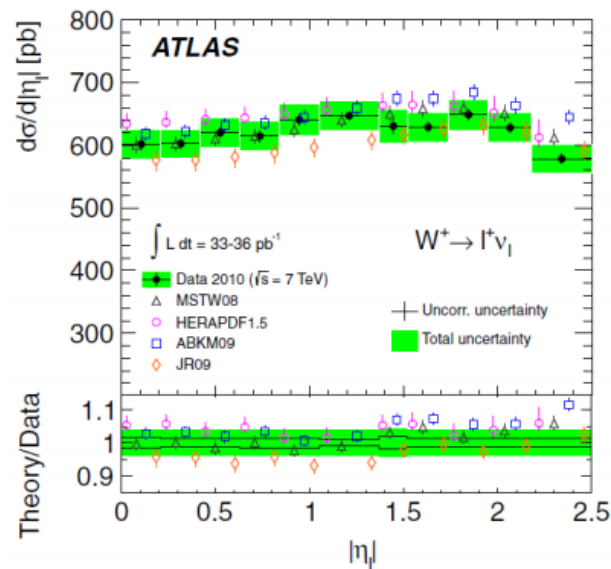
Ex: 30 points from ATLAS  
WZ 2010 vs NNLO predictions

PDF set	Central PDF	With PDF uncertainties
CT10	34.1	32.0
MSTW08	72.0	49.7
HERAPDF1.5eig	43.1	39.2

Used in ATLAS publications:



Phys. Lett. B 725 (2013) 223

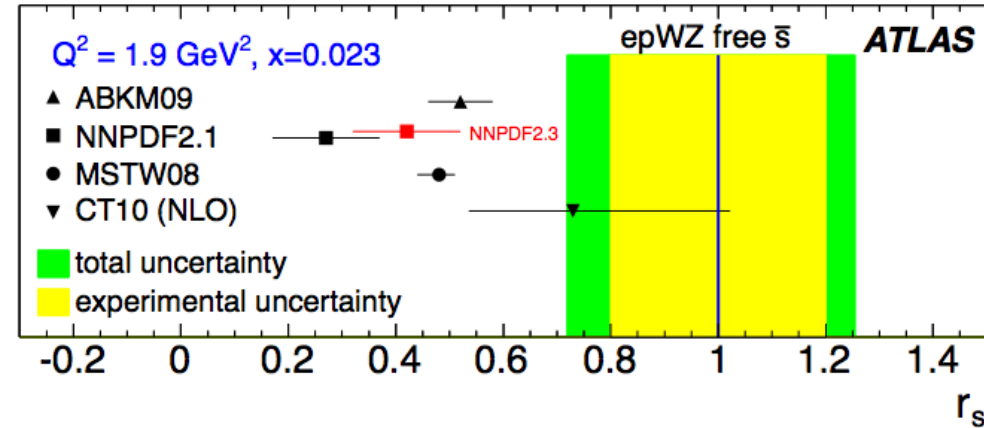


Phys. Rev. D 85 (2012) 072004

# Determination of the strange quark in the proton

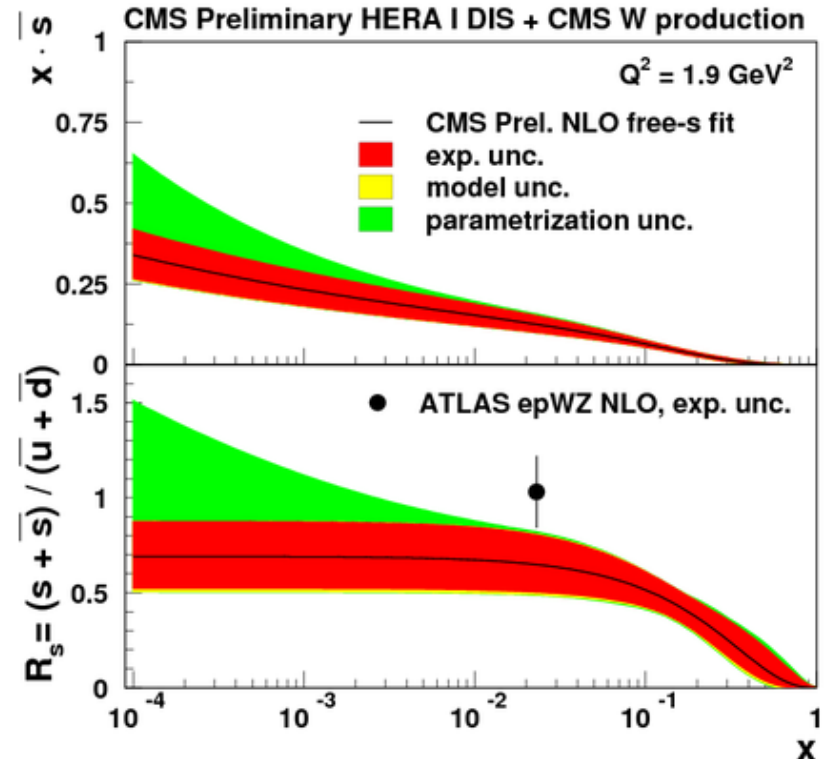
- Using  $W^+$ ,  $W^-$ ,  $Z$  (35/pb) inclusive cross sections - ATLAS [PRL 109 (2012) 012001] (kinematic region probed is at  $x \sim 0.01$ )
  - NNLO QCD Analysis
  - ATLAS-epWZ-EIG.LHgrid available in lhapdf**

$$r_s = 1.00 \pm 0.20_{\text{exp}} \pm 0.07_{\text{mod}}^{+0.10}_{-0.15} \alpha_S \pm 0.08_{\text{th.}}^{+0.06}_{-0.07}$$



**NEW**

- Using  $W^+$ charm (5/fb) and  $W$  muon asymmetry (4.7/fb) - CMS [SMP-12-021]
- NLO QCD Analysis: determination of  $R_s(x)$

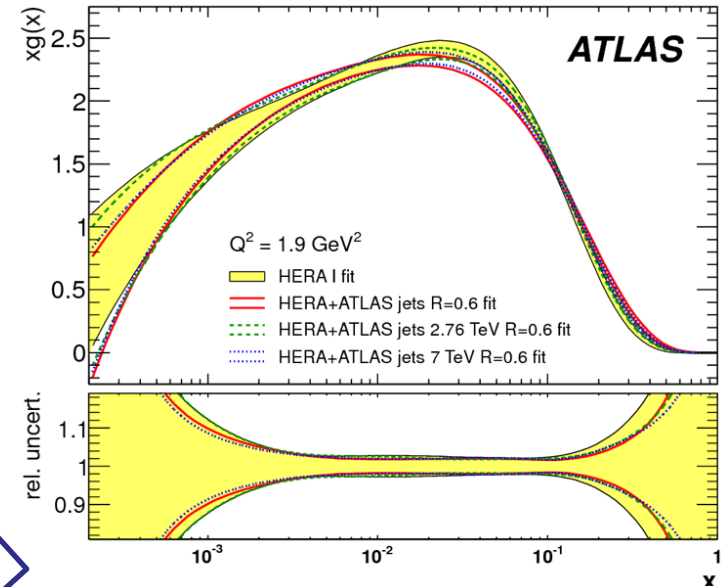


More details in Mark and Georg's talks

# Sensitivity to gluon and strong coupling:

Study sensitivity to the gluon PDF:

- Using ratio of jets at different beam energies - ATLAS [EPJC (2013) 73 2509]
  - ▽ Compare the gluon for PDF fit using just HERA I and a fit using HERA I + ATLAS 2.76, 7 TeV jet data (2010)



Using inclusive jet cross section at 7 TeV CMS data from 2011 (5/fb) [SMP-12-028]:

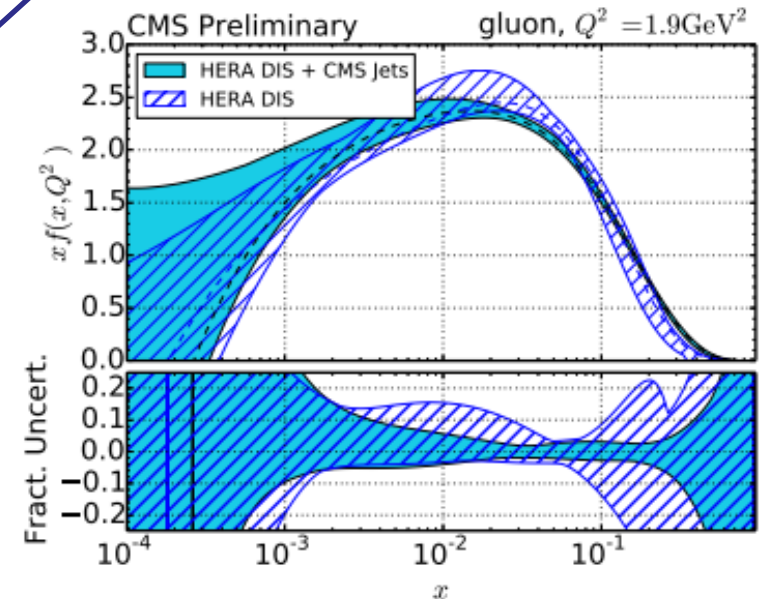
**NEW**

- ▽ PDFs are extracted and compared to fits using just HERA I and fits using HERA I + CMS 7 TeV jet data

Extraction of the strong coupling:

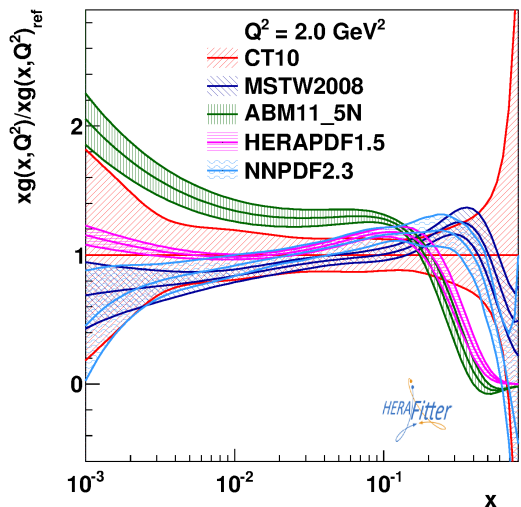
- From PDF and alphas simultaneous fit:

$$\alpha_s(M_Z) = 0.1192^{+0.0017}_{-0.0015}$$



More details in Mark and Georg's talks

# PDF Sensitivity study on prompt photon



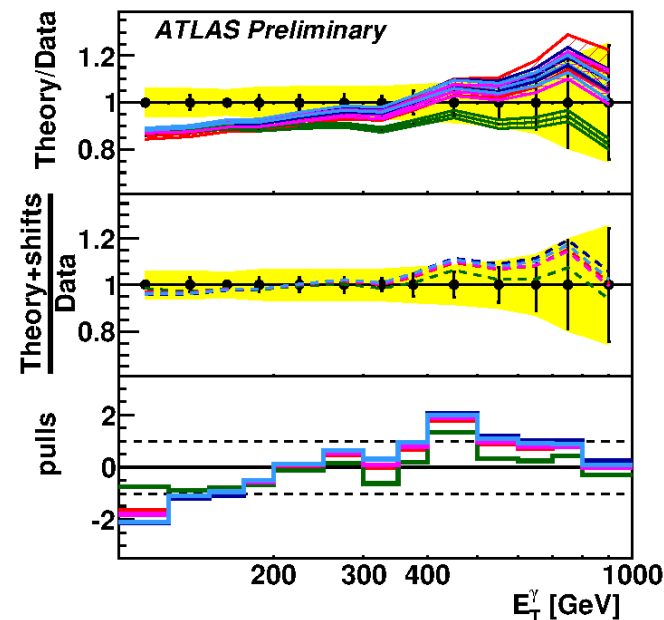
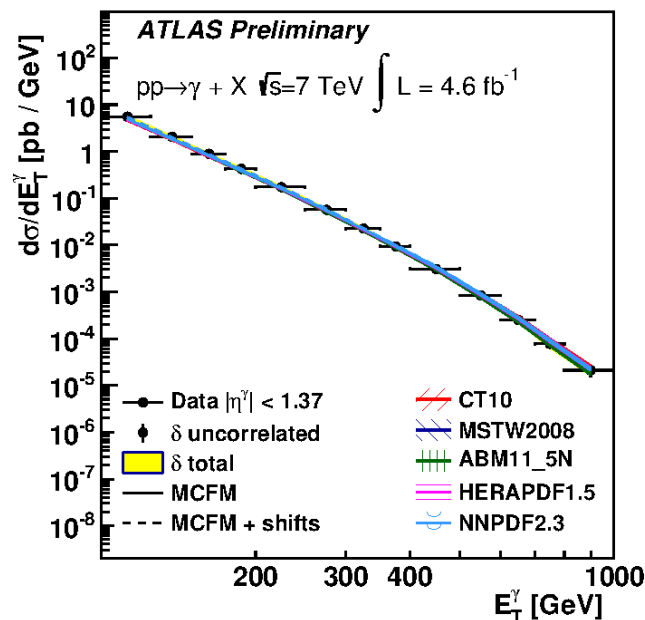
First result with stable release HERAFitter 1.0.0

Assess:

- **Compatibility** between data and NLO predictions
- **Sensitivity** to the gluon PDF

HERAFitter 1.0.0 stable release provides automatic tools for:

- $\chi^2$  comparison with and without PDF uncertainties
- PDF plots
- Data plots



# Summary

- Successful releases of the HERAFitter package – an open source QCD Framework designed to help address the theoretical differences, but mostly provides means for various tests within experimental data analysis
  - HERAFitter platform has grown into a multi-functional QCD platform:
    - ▽ Various treatments for heavy flavours;
    - ▽ Various options for data uncertainties treatment;
    - ▽ Various parametrisation techniques;
    - ▽ Various physics cases.

**NEW**

Stable release available: [herafitter-1.0.0](#)

- [www.herafitter.org](http://www.herafitter.org)
- [herafitter-help@desy.de](mailto:herafitter-help@desy.de)

**We welcome new developments!**

# HERAFitter perspectives

A list of planned developments:

- **Theory (short and long terms):**
  - QED PDFs
  - Nuclear + proton PDFs.
  - Heavy Flavour scheme in QCDNUM, using fast convolution engine.
  - Improvements in Hathor cross-section calculation for fits, other ttbar codes
  - Addition of DiffTop – program to calculate differential cross sections
  - EW corrections.
  - DYNNLO in APPLGRID.
  - Photon's PDF.
  - Different evolution schemes:
    - ▽ e.g. matched to MC showering, mixed Dipole-DGLAP fits.
- **Data treatments:**
  - Alternative to MINUIT minimization package

# Results using HERAFitter

- Following PDF grids have been generated since the start of the project:
  - **HERAPDF1.0, HERAPDF1.5, ATLAS-epWZ12, LHeC-NLO**

- HERAFitter has been used in the following publications:



“ Determination of the strange quark density of the proton from ATLAS measurements of the W and Z cross sections” [[PRL 109 \(2012\) 012001](#)]

“ Measurements of the inclusive jet cross section in pp collisions at 2.76 TeV and comparison to the inclusive jet cross section at 7 TeV using the ATLAS detector” [[EPJC \(2013\) 73 2509](#)]

“ Measurement of the high-mass Drell-Yan differential cross-section in pp collisions at 7 TeV with the ATLAS detector” [[PLB 725 \(2013\) 223](#)]



“ Measurement of the muon charge asymmetry in pp W production at 7 TeV” [[SMP-12-021](#)]

“ PDF constraints and extraction of the strong coupling constant from the inclusive jet cross section at 7 TeV” [[SMP-12-08](#)]



“ Combination and QCD Analysis of Charm Production Cross Section Measurements in Deep Inelastic ep Scattering at HERA” [[EPJC \(2013\) 73 2311](#)]

“ Inclusive Deep Inelastic Scattering at High Q<sup>2</sup> with Longitudinally Polarised” [[JHEP 1209 \(2012\) 061](#)]



LHeC impact studies [[Journal of Phys. G 39 \(2012\)](#)]



“ Parton Distribution Uncertainties using Smoothness Prior” [[PLB 695 \(2011\) 238](#)]



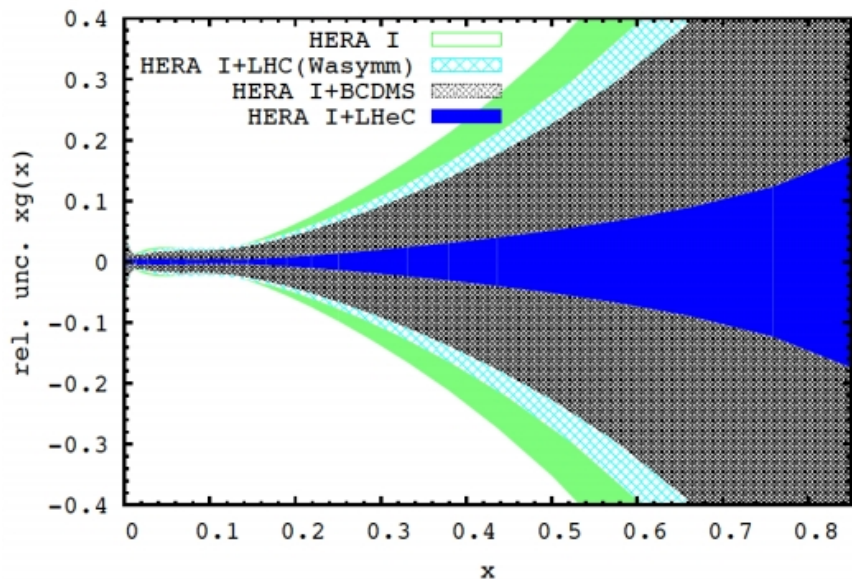
# Backup

# Impact studies of LHeC on PDFs

HERAFitter provides the possibility to perform impact studies using simulated data:

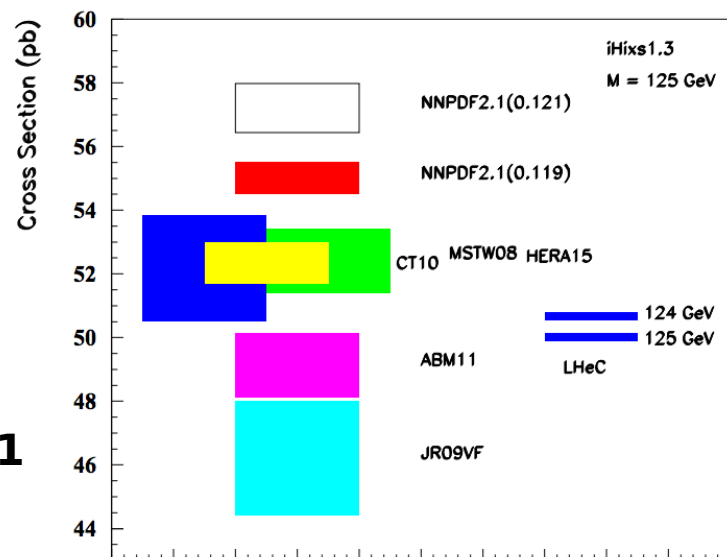
- LHeC can provide a complete PDF set with precise gluon, valence, and strong coupling:

LHeC promises per mille accuracy on alphas - using HERAFitter [Journal of Phys. G 39 (2012)]



case	cut [ $Q^2$ in GeV]	relative precision in %
HERA only (14p)	$Q^2 > 3.5$	1.94
HERA+jets (14p)	$Q^2 > 3.5$	0.82
LHeC only (14p)	$Q^2 > 3.5$	0.15
LHeC only (10p)	$Q^2 > 3.5$	0.17
LHeC only (14p)	$Q^2 > 20.$	0.25
LHeC+HERA (10p)	$Q^2 > 3.5$	0.11
LHeC+HERA (10p)	$Q^2 > 7.0$	0.20
LHeC+HERA (10p)	$Q^2 > 10.$	0.26

NNLO pp-Higgs Cross Sections at 14 TeV



14 TeV  $gg \rightarrow H$  total cross section at the LHC calculated for a variety of PDFs at 68% CL

- precision from LHeC can add a very significant constraint on the mass of the Higgs
- LHeC-NLO. LHgrid available since lhpdf v5.9.1**

# Low x Physics

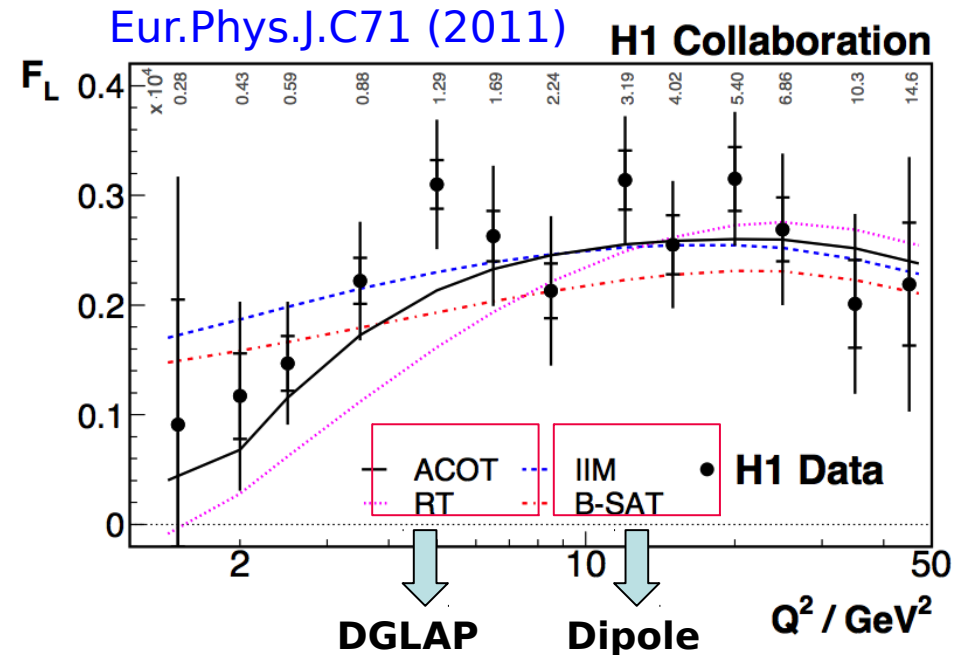
- As an alternative to DGLAP, HERAFitter includes also Dipole models:
  - Studied by the H1 collaboration in comparing different models on FL:

## ∇ Dipole Models implemented in HERAFitter:

- GBW model: first model
- IIM (based on BK-equation)
- BGK (based on GBW, but gluon evolved using DLGAP)

## ∇ DGLAP Models:

- RT as used by MSTW group
- ACOT as used by CTEQ group



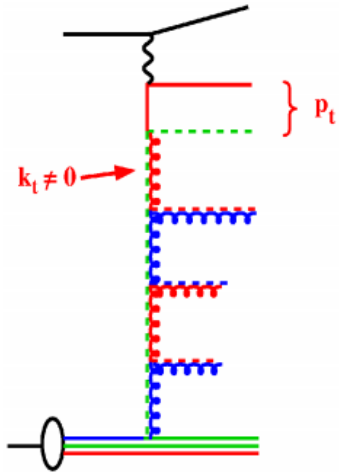
- Unintegrated PDFs based on the kT-factorisation (CCFM) evolution.

- applicable only to NC ep scattering

<https://www.herafitter.org/HERAFitter/HERAFitter/HERAFitterMeetings/Meeting2012-Oct-29?action=AttachFile&do=get&target=updf.pdf>

- Diffractive DIS PDF fits.

# uPDFs in HERAFitter



- $\frac{d\sigma}{dx dQ^2} = \int dx_g [dk_{\perp}^2 x_g \mathcal{A}_i(x_g, k_{\perp}^2, p)] \hat{\sigma}(x_g, k_{\perp}^2, x, Q^2)$
- $\hat{\sigma}(x_g, k_{\perp}^2, x, Q^2)$  is (off-shell,  $k_{\perp}$  dependent) hard scattering cross section
- uPDFs for gluons and quarks needed:
  - **Until now: only gluon uPDF determined**

- valence quarks: use starting distribution CTEQ6

- **method:**

$$\sigma_r(x, Q^2) = \int_0^1 dx_g \mathcal{A}(x_g, k_{\perp}, p) \hat{\sigma}(x, x_g, Q^2)$$

- **calculate**  $\int_{x/x'}^1 dx'' \tilde{\mathcal{A}}(x'', k_{\perp}, p) \cdot \hat{\sigma}(x, x' x'', Q^2)$  in a grid of  $x'', Q^2$

- **starting distribution:**  $\mathcal{A}_0(x) = N_g x^{-B_g} (1-x)^{C_g} (1-D_g x)$

- **calculate**  $\sigma_r(x, Q^2)$  by 1-dim Gauss integration (fast!)

- **external input:**

- kernel evolution grid for gluon
- evolved valence quark distribution (as uPDF)

- convolution of kernel with off-shell ME done in herafitter

# HERAFitter Perspectives

HERAFitter has a modular structure facilitating fast developments

- Many new developments are planned to be implemented in future releases:

