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T. Han, Z. Liu and SS, to appear

Outline

- Introduction/Motivation
- Light neutralino dark matter
- A₁/H₁ funnel region
- sbottom coannihilation
- stau coannihilation
- Direct and indirect detections
- LHC observables
- Nearly degenerate sfermion signals at the ILC
- Sonclusion

















Dark Matter





• Relic density
$$M_{\rm WIMP} \lesssim \frac{g^2}{0.3} \ 1.8 \ {\rm TeV}$$

• Connection of WIMP dark matter to TeV scale new physics

• DM mass, coupling, relic density: model dependent



- Relic density $M_{\rm WIMP} \lesssim \frac{g^2}{0.3} \ 1.8 \ {\rm TeV}$
- Connection of WIMP dark matter to TeV scale new physics
- DM mass, coupling, relic density: model dependent

How light a WIMP dark matter can be?
 preserve WIMP DM properties
 satisfy current experimental constraints

Light Dark Matter

Direct detection





• consistent observations among all approaches



Complementarity

• consistent observations among all approaches





• consistent observations among all approaches





$$M_{\tilde{N}^{0}} = \begin{pmatrix} M_{1} & 0 & -g_{1} \frac{v_{d}}{\sqrt{2}} & g_{1} \frac{v_{u}}{\sqrt{2}} \\ M_{2} & g_{2} \frac{v_{d}}{\sqrt{2}} & -g_{2} \frac{v_{u}}{\sqrt{2}} \\ & 0 & -\mu \\ & * & 0 \end{pmatrix}$$

$$\tilde{\chi}_1^0 = N_{11}\tilde{B} + N_{12}\tilde{W}^0 + N_{13}\tilde{H}_d^0 + N_{14}\tilde{H}_u^0 +$$



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• lightest neutralino LSP in MSSM as good dark matter candidate



Ightest neutralino LSP in MSSM as good dark matter candidate



Ightest neutralino LSP in MSSM as good dark matter candidate



Han, Liu and Natarajan , 1303.3040

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Han, Liu and Natarajan , 1303.3040 $\frac{8}{8}$

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Ightest neutralino LSP in MSSM as good dark matter candidate



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Draper et. al. , 1009.3963 Arbey et. al. , 1205.2557,...

	Models	DM (< 40 GeV)	Annihilation
Co-ann	MSSM & NMSSM	Bino/Singlino	$\tilde{\chi}_1^0 \tilde{\chi}_1^0 \to f\bar{f}; \ \tilde{\chi}_1^0 \tilde{f} \to Vf; \ \tilde{f}\tilde{f}' \to ff'$
Funnel	NMSSM	Singlino/Bino	$\tilde{\chi}_1^0 \tilde{\chi}_1^0 \to a_1, h_1 \to SM$
			·

- Study properties of those solutions
- Direct and indirect detection
- Observational aspects at colliders
 - via SM-like Higgs
 - light Higgses
 - light sfermion

NMSSM Higgs Sector

• Type II Two Higgs Doublet Model plus singlet S

$$W_{\text{NMSSM}} = Y_u \hat{u}^c \hat{H}_u \hat{Q} + Y_d \hat{d}^c \hat{H}_d \hat{Q} + Y_e \hat{e}^c \hat{H}_d \hat{L} + \lambda \hat{\mathcal{S}} \hat{H}_u \hat{H}_d + \frac{1}{3} \kappa \hat{\mathcal{S}}^3$$
$$V_{H,Soft} = m_{H_u}^2 H_u^{\dagger} H_u + m_{H_d}^2 H_d^{\dagger} H_d + M_S^2 |\mathcal{S}|^2 + \left(\lambda A_\lambda (H_t^T \epsilon H_d) \mathcal{S} + \frac{1}{3} \kappa A_\kappa \mathcal{S}^3 + c.c.\right)$$

• SSB

$$H_u = \begin{pmatrix} H_u^+ \\ H_u^0 \end{pmatrix} \xrightarrow{} v_u/\sqrt{2} \qquad H_d = \begin{pmatrix} H_d^0 \\ H_d^- \end{pmatrix} \xrightarrow{} v_d/\sqrt{2} \qquad S \rightarrow v_s/\sqrt{2} \\ H_d^- \end{pmatrix} \qquad (\mu = \lambda v_s/\sqrt{2})$$

$$v_u^2 + v_d^2 = v^2 = (246 \text{GeV})^2$$
$$\tan \beta = v_u / v_d$$

after EWSB, 7 physical Higgses CP-even Higgses: H₁, H₂, H₃ CP-odd Higgs: A₁, A₂ Charged Higgses: H[±]

$$M_{\tilde{N}^0} = \begin{pmatrix} M_1 & 0 & -g_1 \frac{v_d}{\sqrt{2}} & g_1 \frac{v_u}{\sqrt{2}} \\ M_2 & g_2 \frac{v_d}{\sqrt{2}} & -g_2 \frac{v_u}{\sqrt{2}} \\ & 0 & -\mu \\ & * & 0 \end{pmatrix}$$

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$$\tilde{\chi}_1^0 = N_{11}\tilde{B} + N_{12}\tilde{W}^0 + N_{13}\tilde{H}_d^0 + N_{14}\tilde{H}_u^0 + N_{15}\tilde{S}$$

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• Bino-like LSP

$$N_{11} \approx 1, \quad N_{15} \approx 0,$$

 $N_{13} \approx \frac{m_Z s_W}{\mu} s_\beta, \quad N_{14} \approx -\frac{m_Z s_W}{\mu} c_\beta,$



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Singlino-like LSP

 $\begin{array}{l} N_{11} \approx 0, \quad N_{15} \approx 1 \\ N_{13} \approx -\frac{\lambda v}{\mu} c_{\beta}, \quad N_{14} \approx -\frac{\lambda v}{\mu} s_{\beta} \end{array}$

NMSSMTools4

	General	Sbottom	Stau	H_1, A_1 -funnel
$m_{A_{ m tree}}$	[0,3000]			
$\tan \beta$	[1,55]			
μ	[100, 500]			
$ A_{\kappa} $	[0,1000]			
λ	[0,1]			[0.01, 0.6]
κ	[0,1]	either $\kappa \in [2, 30]\lambda/(2\mu)$		
$ M_1 $	[0,500]	or Λ	$I_1 \in [2, 30]$], or both
M_{Q3}, M_{U3}	[0, 3000]			
$ A_t $	[0,4000]			
M_{D3}	[0,3000]	[0,80]		3000
$ A_b $	[0,4000]		0	
M_{L3}, M_{E3}	[0,3000]	3000	[0,500]	3000
$ A_{\tau} $	[0,4000]	0	[0,2000]	0

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	General	Sbottom	Stau	H_1, A_1 -funnel
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M_{L3}, M_{E3}	[0,3000]	3000	[0,500]	3000
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General	Sbottom	Stau	H_1, A_1 -funnel	
[0,3000]				
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[0,3000]				
[0,4000]				
[0,3000]	[0,80]		3000	
[0,4000]	_	— 0		
[0,3000]	3000	[0,500]	3000	
[0,4000]	0	[0,2000]	0	
	$\begin{array}{c} \text{General} \\ [0,3000] \\ [1,55] \\ [100,500] \\ [0,1000] \\ [0,1] \\$	GeneralSbottom $[0,3000]$ — $[1,55]$ — $[100,500]$ — $[0,1000]$ — $[0,1000]$ — $[0,1]$ eith $[0,1]$ eith $[0,500]$ or A $[0,3000]$ — $[0,3000]$ — $[0,3000]$ $[0,80]$ $[0,3000]$ $[0,80]$ $[0,3000]$ $[0,80]$ $[0,3000]$ $[0,80]$ $[0,4000]$ 0	GeneralSbottomStau $[0,3000]$ —— $[1,55]$ —— $[100,500]$ —— $[0,1000]$ —— $[0,1]$ 0— $[0,1]$ $(0,1]$ $(0,1]$ $[0,1]$ $(0,1]$ $(0,1]$ $[0,1]$ $(0,1]$ $(0,1]$ $[0,1]$ $(0,1]$ $(0,1]$ $[0,1]$ $(0,1]$ $(0,1]$ $[0,1]$ $(0,1]$ $(0,1]$ $[0,1]$ $(0,1]$ $(0,1]$ $[0,1]$ $(0,1]$ $(0,1]$ $[0,3000]$ $(0,200]$ $[0,3000]$ $(0,2000]$ $[0,3000]$ $(0,2000]$ $[0,4000]$ $(0,2000]$	

NMSSMTools4

			-	
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$m_{A_{ m tree}}$	[0, 3000]			
aneta	$[1,\!55]$			
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M_{D3}	[0,3000]	[0,80]		3000
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M_{L3}, M_{E3}	[0,3000]	3000	[0,500]	3000
$ A_{\tau} $	[0,4000]	0	[0,2000]	0

NMSSMTools4

[01		
	General	Sbottom	Stau	H_1, A_1 -tunnel
$m_{A_{ m tree}}$	[0, 3000]			
$\tan eta$	$[1,\!55]$			
μ	[100, 500]			
$ A_{\kappa} $	[0,1000]			
λ	[0,1]			[0.01, 0.6]
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Experimental Constraints

- Theoretical constraints such as Vacuum stability.
- Collider Higgs search limits from the LEP, the Tevatron and the LHC.
- LEP, Tevatron and LHC constrains on searches of supersymmetric particles, such as charignos, leptons and squarks;
- 2σ window of the SM-like Higgs boson mass: 122.7 128.7 GeV (including linearly added estimated theoretical uncertainties of ± 2 GeV).
- 2σ window of the SM-like Higgs bosons cross sections for $\gamma\gamma$, ZZ, W^+W^- , $\tau^+\tau^$ and $b\bar{b}$ different production modes.
- Z boson invisible width and hadronic width as in Eq. (2.11) and Eq. (2.12).
- B-physics constrains, including $b \to s\gamma$, $B_s \to \mu^+\mu^-$, $B \to \chi_s\mu^+\mu^-$ and $B^+ \to \tau^+\nu_\tau$, as well as Δm_s , Δm_d , $m_{\eta_b(1S)}$ and $\Upsilon(1S) \to a\gamma$, $h\gamma$.

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Constraints for Low Mass

• Light neutralino LSP: invisible Z decay with

 $Z \tilde{\chi}_{1}^{0} \tilde{\chi}_{1}^{0}$ coupling $N_{14}^{2} - N_{13}^{2}$

 $\Delta \Gamma_{inv} < 2.0 ~{\rm MeV}$

- Bino LSP:
$$\mu > 140$$
 GeV

- Singlino LSP: μ/λ > 540 GeV



Constraints for Low Mass

• Light sfermion: total Z decay width

 $\Delta \Gamma_{tot} < 4.7 \ {\rm MeV}$

$$Z\tilde{f}_1\tilde{f}_1: g_f^L \cos^2\theta_{\tilde{f}} + g_f^R \sin^2\theta_{\tilde{f}} \quad \tan^2\theta_{\tilde{f}}^{min} = -g_f^L/g_f^R$$

- sbottom: mostly right-handed
- stau: even mixture of left and right-handed



Dark Matter Properties

$$0.0947 \ (0.001) < \Omega_{\tilde{\chi}^0_1} h^2 < 0.142,$$



funnel

sb-coann

stau-coann





















Indirect Detection



Indirect Detection



Indirect Detection





Observation of a SM-like Higgs poses strong constraints

- mixture from other Higgses
- new decay modes open: $\tilde{\chi}_1^0 \tilde{\chi}_1^0$, $A_1 A_1$, $H_1 H_1$, $\tilde{\tau}_1^+ \tilde{\tau}_1^-$ and $\tilde{b}_1 \tilde{b}_1^*$
- light sbottom/stau appears in Hgg, Hyy



SM Higgs



SM Higgs





Dark matter production via Higgs portal



$H \rightarrow XX$



• Coupling and Decay: singlet like





Production: < 10% SM rate</p>





 \odot Light sbottom with compressed spectrum: small Δm

- $\Delta m > m_b$: prompt sbottom decay
- - △m < m_b: prompt, displaced vertex, R-hadron, ...
 depend on the flavor structure

• LEP limits

\tilde{f}	$m_{min}({ m GeV})$	Ref.	Condition
	76	DELPHI $[50]$	$\tilde{b} \to \tilde{\chi}^0 b$, all $\theta_{\tilde{b}}$, $\Delta m > 7 \text{ GeV}$
$ \tilde{b}$	89	ALEPH $[48]$	$\tilde{b} \to \tilde{\chi}^0 b$, all $\theta_{\tilde{b}}, \Delta m > 10 \text{ GeV}$
	$390 \sim 645$	ATLAS $[51, 52]$	$\tilde{b} \to \tilde{\chi}_1^0 b$, simplified, $m_{\tilde{\chi}_1^0} < 60$ GeV for $m_{\tilde{b}} > 100$ GeV
	•		

ATLAS limits: 2b+MET,bbj+MET





recast ATLAS sbottom search results for light sbottom m_{sb}=20 GeV, m_x=14 GeV, prompt decay

		SRA C	SRB bbjME	
$ \not\!$		$> 150 {\rm ~GeV}$		> 250 GeV
$P_T(j_1)$		$> 130 {\rm ~GeV}$		> 150 GeV
$P_T(j_2)$		$> 50 { m GeV}$		> 30 GeV
$P_T(j_3)$	Ve	eto if > 50 Ge	V	> 30 GeV
$\Delta \phi (ot\!$				> 2.5
b tagging	ta	gged b jet j_1 ,	j_2	$j_2,\ j_3$
$\Delta \phi_{min}$		> 0.4		> 0.4
$\not\!$	<i>₽</i>	$r/m_{eff}(2) > 0$.25	$E_T/m_{eff}(3) > 0.25$
m_{bb}		$> 200 {\rm ~GeV}$		
$H_{T,3}$				$< 50 { m GeV}$
$m_{ m CT}$	$\geq 250 \text{ GeV} \mid \geq 300 \text{ GeV} \mid \geq 350 \text{ GeV}$			
95% C.L. upper limit	0.45 0.37 0.26			13
σ_{vis} (fb)	0.45 0.57 0.20			1.0
σ_{sig} (fb)	0.20	0.19	0.17	137
S. Su				20



recast ATLAS sbottom search results for light sbottom m_{sb}=20 GeV, m_x=14 GeV, prompt decay

		SRA k	SRB bbjME				
		Lepton veto					
$\not\!$		$> 150 {\rm ~GeV}$		$> 250 \mathrm{GeV}$			
$P_T(j_1)$		> 130 GeV		> 150 GeV			
$P_T(j_2)$		$> 50 {\rm GeV}$		$> 30 \mathrm{GeV}$			
$P_T(j_3)$	V	eto if > 50 Ge	eV	$> 30 \mathrm{GeV}$			
$\Delta \phi (E_T, i_t)$				> 2.5			
b tag <mark>:⊚ ∆m ></mark>	b tag \odot $\Delta m > m_b$ (prompt sb decay): ruled out j_2, j_3						
$\Delta \phi_n$ a Am s	m: dener	nds on the	decay life	> 0.4			
E_T/m_{e_j}				$\tau_{ff}(3) > 0.25$			
m_{bb}		> 200 GeV					
$H_{T,3}$				$< 50 { m GeV}$			
$m_{ m CT}$	$\geq 250 \text{ GeV}$	$\geq 300 \text{ GeV}$	$\geq 350 \mathrm{GeV}$				
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S Su				70			



• LEP limit

L	1		- ^1 ~]
	81.9	DELPHI [50]	$\Delta m > 15 \text{ GeV}, \text{ all } \theta_{\tilde{\tau}}, \tilde{\tau} > 45 \text{ GeV}$
$ _{\tilde{\tau}}$	$35 \sim 45$	ALEPH [53, 54]	$Z \rightarrow \ell \ell$ (acoplanar), right-handed, $\Delta m > 2 \sim 5$ GeV
	35	ALEPH [53, 54]	$Z \rightarrow \text{invisible, right-handed, all } \Delta m$
	$20 \sim 44$	ALEPH [53, 54]	Z-decoupling, $\Delta m > 2 \sim 15 \text{ GeV}$
	•		

- LHC limit with stau from neutralino/chargino decay
 not applicable with large MT2 cut of 90-110 GeV
- ττ(j) + MET search difficult with WW(j)+MET background.

light stau difficult at LHC as well.



bbγ+MET, ττγ+MET
 i



Conclusion

light neutralino dark matter (2 - 40 GeV)

	A1/H1 funnel	sb-coann	stau-coann
DM	Bino/Singlino	Bino	Bino/Singlino
light particle	m _{A1/H1} ~2m _X singlet-like	m _{sb} ~m _X ∆m < m _b	m _{stau} ∼m _X m _{stau} >30 GeV
relic	✓	✓	✓
direct detection	1		1
indirect detection	1	✓	1
via SM Higgs	1	✓	1
LHC	✓	×	×
ILC	1	✓	1