



Measurements of the CPV γ angle

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on behalf of the **LHCb Collaboration**

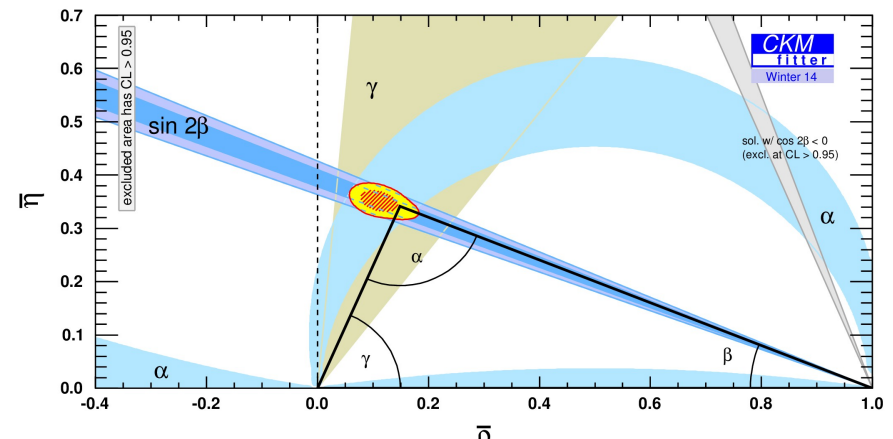
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ON HYPERONS, CHARM AND BEAUTY HADRONS
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BEACH
BIRMINGHAM 2014

γ a standard candle to probe new physics

- γ is the least known CKM parameter:
 - BaBar: $(69^{+17}_{-16})^\circ$ [PRD 87(2013)052015]
 - Belle: $(68^{+15}_{-14})^\circ$ [arXiv:1301.2033]
 - LHCb: $(67 \pm 12)^\circ$ [LHCb-CONF-2013-006]
 - CKM Fitter: $(66.5^{+1.3}_{-2.5})^\circ$ (global fit)

$$\gamma = \arg \left(-\frac{V_{ud}V_{ub}^*}{V_{cd}V_{cb}^*} \right) \approx \arg(-V_{ub}^*)$$



Constraint with only the angle measurements

- The only angle measurable from **tree processes** (loops negligible).
- **Theoretically clean** : $\delta\gamma/\gamma \lesssim \mathcal{O}(10^{-7})$ [JHEP 1401(2014)051].

➔ Excellent **Standard Model reference** to probe New Physics.
Need a better precision from direct measurement.

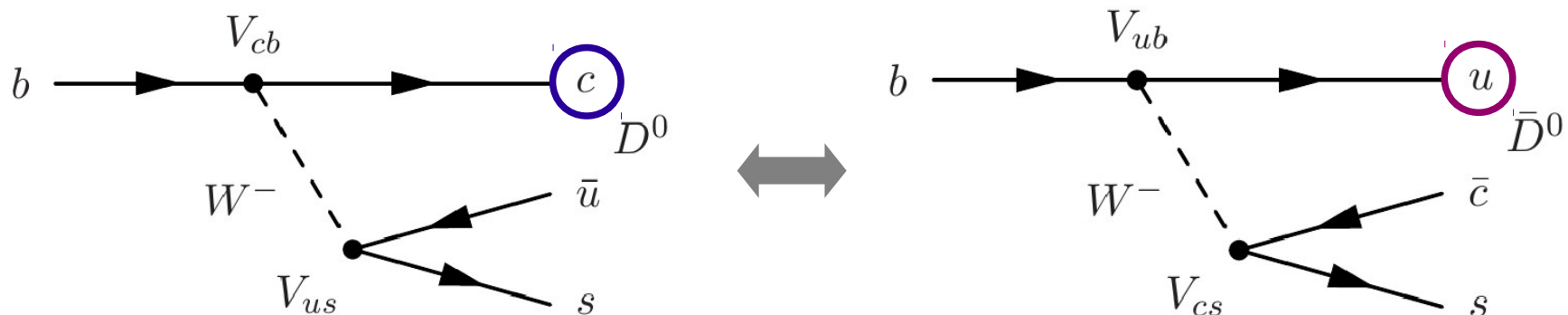
Today's menu

Four recent LHCb results (to be submitted to journals soon):

- $B^\pm \rightarrow D(K_s^0 \pi^+ \pi^-) K^\pm$, Amplitude analysis, Model-dependent (1 fb^{-1}).
[\[LHCb-PAPER-2014-017\]](#)
- $B^\pm \rightarrow D(K_s^0 h^+ h^-) K^\pm$, Amplitude analysis, Model-independent (3 fb^{-1}).
[\[LHCb-PAPER-2014-041\]](#)
- $B^0 \rightarrow DK^{*0}$, Counting analysis (3 fb^{-1}).
[\[LHCb-PAPER-2014-028\]](#)
- $B_s^0 \rightarrow D_s K^\pm$, Time dependent analysis (1 fb^{-1}).
[\[LHCb-PAPER-2014-038\]](#)

Time integrated measurements

- Interference between $b \rightarrow c\bar{u}s$ and $b \rightarrow u\bar{c}s$.



- D^0 and \bar{D}^0 must decay to the same final state:

- Counting Analysis : ADS ($D \rightarrow K\pi$), GLW ($D \rightarrow hh$)

$$A_{B^\pm} = A_D + e^{i(\delta_B \pm \gamma)} A_{\bar{D}}$$

[PLB253(1991)483,
PLB265(1991)172]
[PRL78(1997)3257,
PRD63(2001)036005]

- Dalitz plot analysis: GGSZ

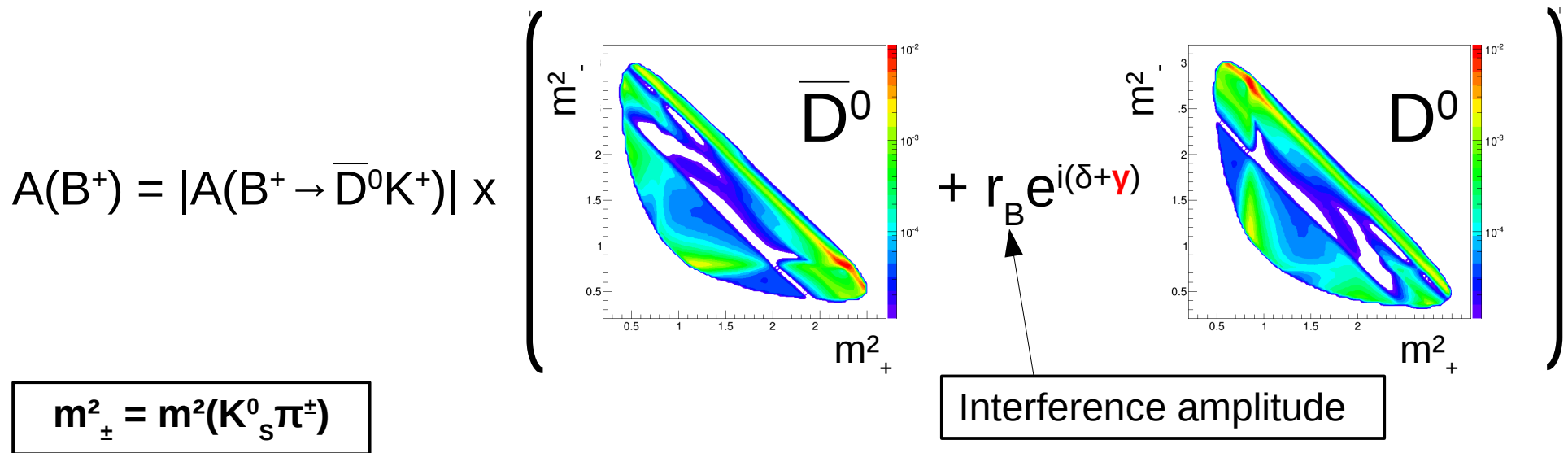
$$A_{B^\pm}(\mathcal{D}) = A_D(\mathcal{D}) + e^{i(\delta_B \pm \gamma)} A_{\bar{D}}(\mathcal{D})$$

↑
D meson phase space

[PRL78(1997)3257;
PRD68(2003)054018;
A. Bondar, Proceedings of
BINP special analysis
meeting on Dalitz analysis,
2002, unpublished]

Dalitz analysis of $B^\pm \rightarrow D(K_S^0 h^+ h^-)K^\pm$

- Large asymmetry in some regions of the Dalitz plot.
- To infer something on the weak phase γ , **strong phase variation** over the Dalitz plot must be known:
 - **Model Dependent** approach: use BaBar's model. [[PRL 105, 081803 \(2010\)](#)]
 - **Model Independent** approach: use CLEO-c measurements as inputs. [[PRD 82\(2010\)112006](#)]

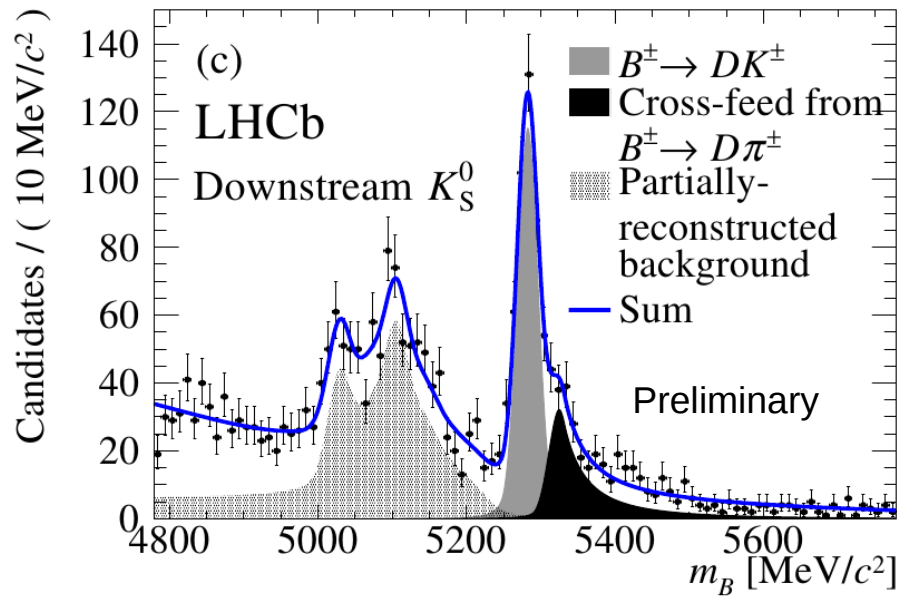


$B^\pm \rightarrow D(K_S^0 h^+ h^-)K^\pm$ Model Dependent - Method

$B \rightarrow DK$

K_S decay inside Vertex Detector: 217

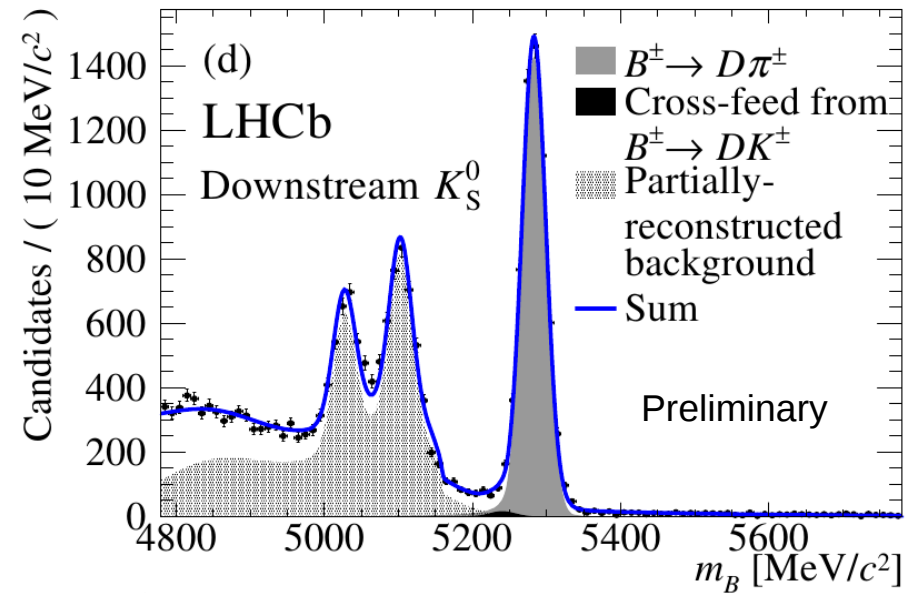
K_S decay outside Vertex Detector: 420



$B \rightarrow D\pi$

K_S decay inside Vertex Detector: 2906

K_S decay outside Vertex Detector: 5960



[LHCb-PAPER-2014-017]

- Fit simultaneously $B \rightarrow DK$ & $B \rightarrow D\pi$

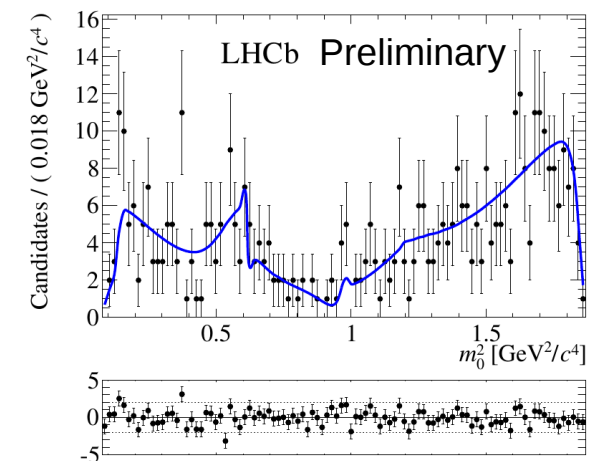
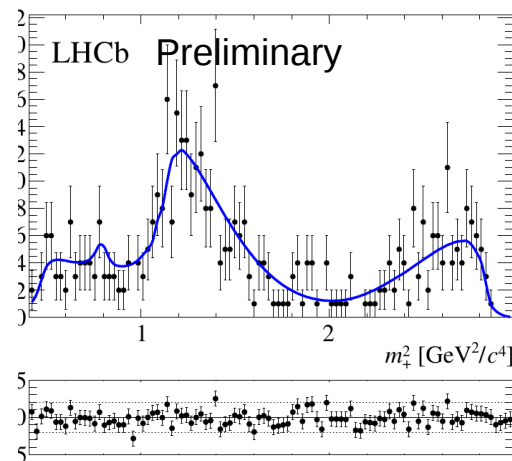
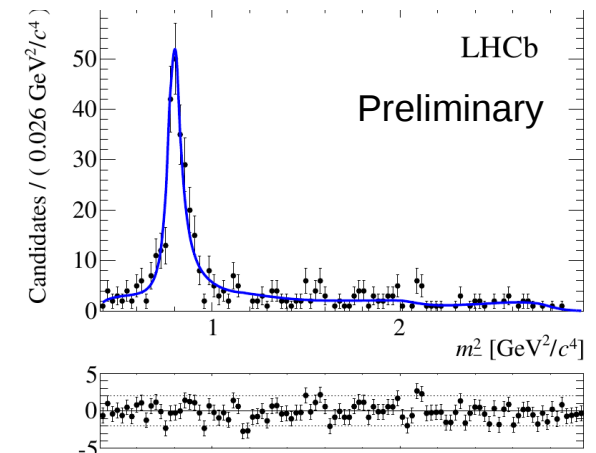
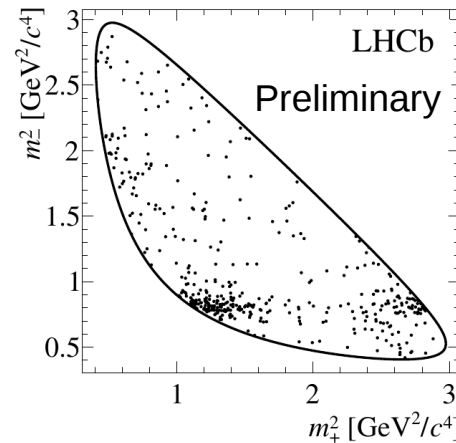
1) **Mass fit** (phase-space integrated): fix signal and background yields.

2) **Dalitz fit**: extract r_B , γ and δ_B from cartesian coordinates.

$$\begin{aligned}x_\pm &= r_B \cos(\delta_B \pm \gamma) \\y_\pm &= r_B \sin(\delta_B \pm \gamma)\end{aligned}$$

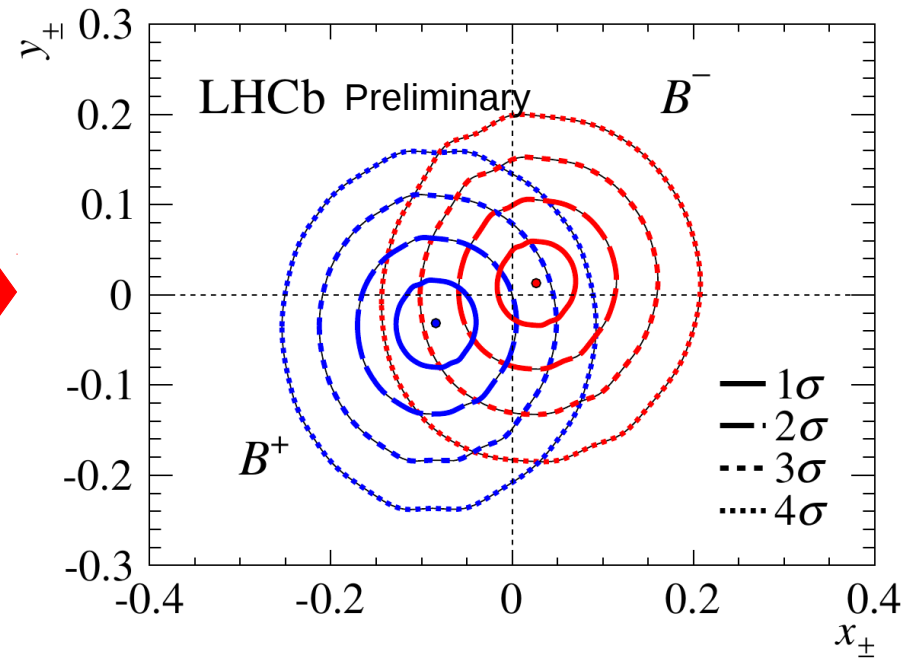
$B^\pm \rightarrow D(K_S^0 h^+ h^-)K^\pm$ MD – Dalitz fit

- D strong phase variation evaluated with an **amplitude model** (BaBar latest).
- $B \rightarrow D\pi$ determine the **efficiency on the Dalitz plot** (assuming no CPV).
- Use only $D \rightarrow K_S^0 \pi\pi$ (1 fb^{-1}).



$B^\pm \rightarrow D(K_s^0 h^+ h^-)K^\pm$ MD - Results

	stat.	syst. exp.	syst. Dalitz model
x_-	$+0.027 \pm 0.044$	$+0.010 \pm 0.001,$ -0.008	$\pm 0.001,$
y_-	$+0.013 \pm 0.048$	$+0.009 \pm 0.003,$ -0.007	$\pm 0.003,$
x_+	-0.084 ± 0.045	$\pm 0.009 \pm 0.005,$	
y_+	-0.032 ± 0.048	$+0.010 \pm 0.008,$ -0.009	



$$\gamma = (84^{+49}_{-42})^\circ$$

Preliminary

- Model systematics:
 - test several alternative models.
- Leading experimental systematics:
 - Efficiency.
 - Background descriptions uncertainties.
- Results consistent with the 1fb^{-1} model independent analysis.
- To be improved with 3fb^{-1} .

$B^\pm \rightarrow D(K_S^0 h^+ h^-)K^\pm$ model independent - Method -

- D strong phase variation measured by CLEO-c in a particular binning scheme.
- Analysis = **counting experiment in each bins of the Dalitz plot.**

$$N_{\pm i}^+ = h_{B^+} \left[F_{\mp i} + (x_+^2 + y_+^2) F_{\pm i} + 2\sqrt{F_i F_{-i}} (x_+ c_{\pm i} \mp y_+ s_{\pm i}) \right]$$

D from B+ events falling in bin $\pm i$

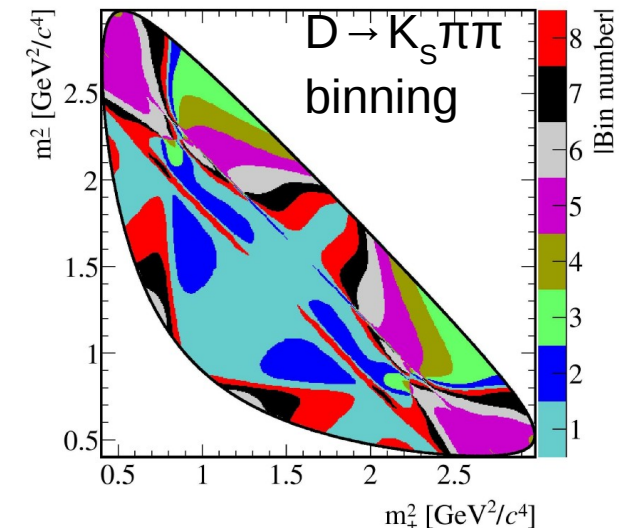
Fraction of pure D^0 events in a given bin, taking into account the signal efficiency profile

CLEO-c inputs

c_i and s_i are the averaged cosine and sine of the strong phase difference in bin i .

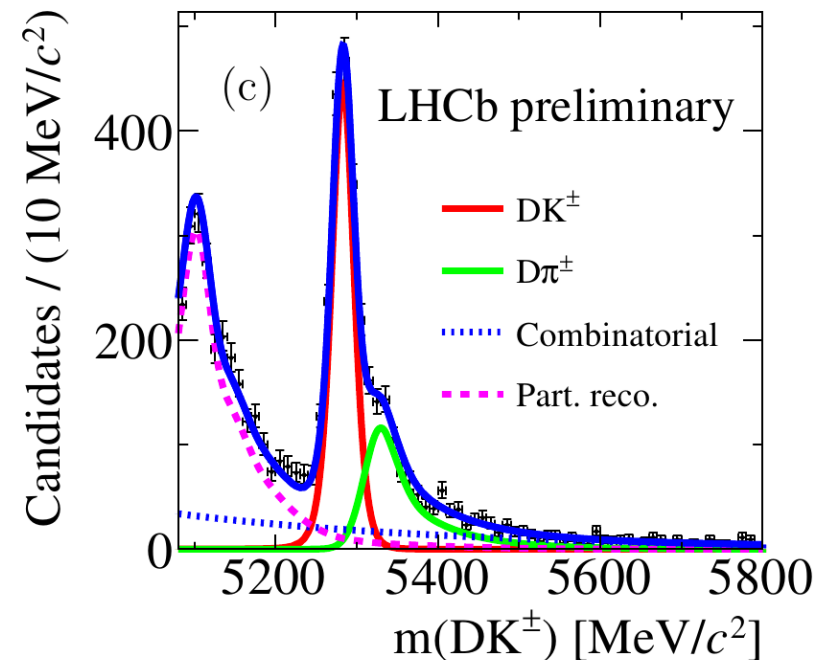
F_i are determine with $B^0 \rightarrow D^*(D^0 \pi^+) \mu \nu$ LHCb data.
(efficiency correction from MC)

Simultaneous mass fit in every bins to extract x_\pm and y_\pm .

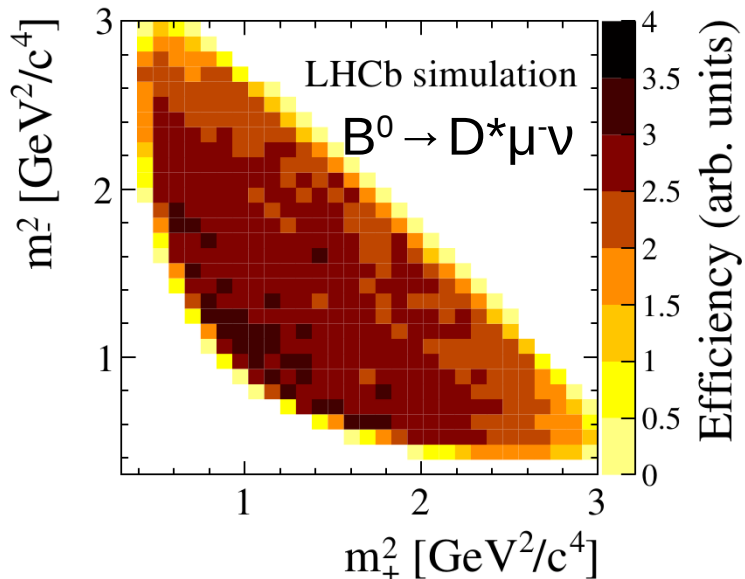
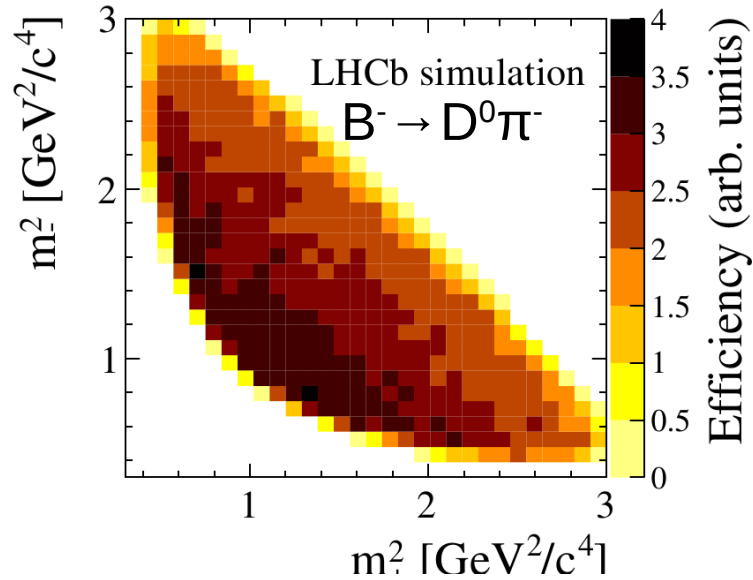


Mass fit

- First, mass fit over the full phase space:
 - Total DK candidates ~ 2600
 - Split data into $K_S\pi\pi$ and $K_S KK$, and K_S position decay.
 - Purity $\sim 75\%$ in signal region.
- Fix all mass model PDF for the second fit in each Dalitz bin which determines x_{\pm} and y_{\pm} .



$B^0 \rightarrow D^*(D^0\pi^+)\mu^-\nu$ efficiency discrepancy



- $B^0 \rightarrow D^*\mu^-\nu$ excellent proxy to determine the F_i :
 - High purity and statistics.
 - D^0 is tagged from the D^* slow pion.
- Small efficiency discrepancy observed between $B^\pm \rightarrow Dh^\pm$ and $B^0 \rightarrow D^*\mu^-\nu$, in the MC.
- **F_i determination:**
 - Fit $B^0 \rightarrow D^*\mu^-\nu$ data \rightarrow yields in dalitz bins.
 - Correct these yields with the MC.

Model independent results (3 fb⁻¹)

Most precise measurement of x and y to date:

$$x_+ = (-7.7 \pm 2.4 \pm 1.0 \pm 0.4) \times 10^{-2}$$

$$x_- = (2.5 \pm 2.5 \pm 1.0 \pm 0.5) \times 10^{-2}$$

$$y_+ = (-2.2 \pm 2.5 \pm 0.4 \pm 1.0) \times 10^{-2}$$

$$y_- = (7.5 \pm 2.9 \pm 0.5 \pm 1.4) \times 10^{-2}$$

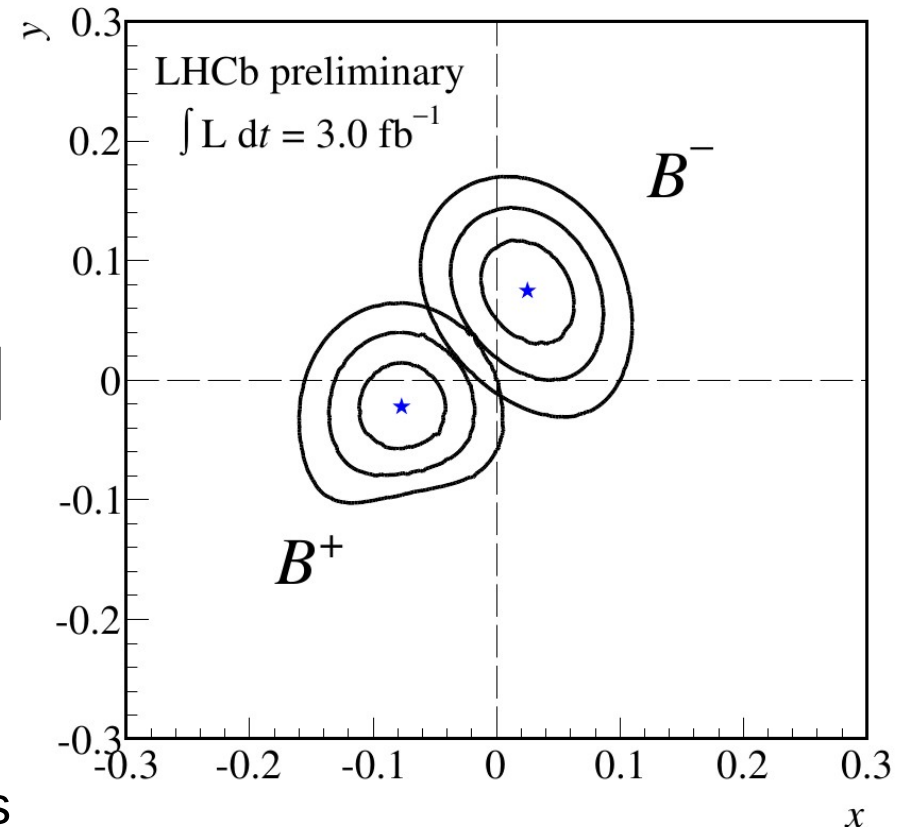
stat.

Exp. Syst.

Cleo input Syst.

Compare to 1fb⁻¹ measurement:

- Higher statistics = smaller statistical error.
- Experimental systematic error reduced with the new $B^0 \rightarrow D^* \mu \nu$ control mode (prev. it was $B^\pm \rightarrow D \pi^\pm$, assuming no CPV).
- Smaller D strong phase systematic thanks to increased sample size.

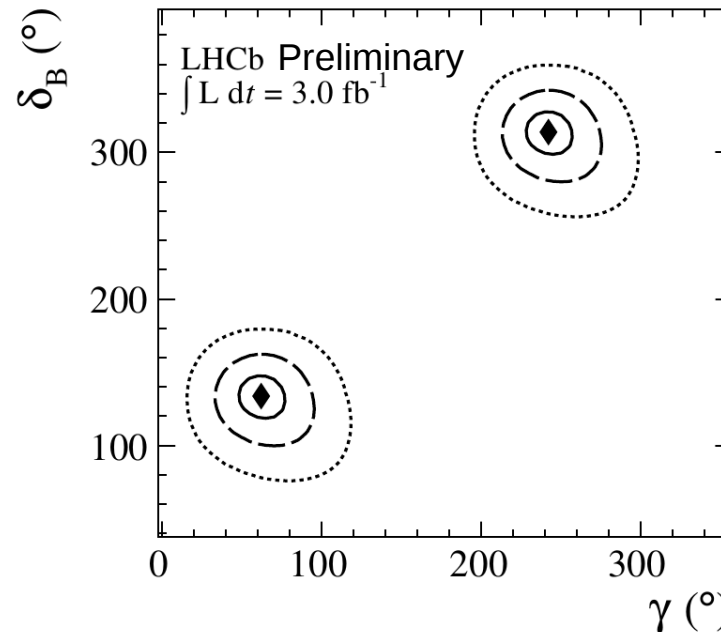
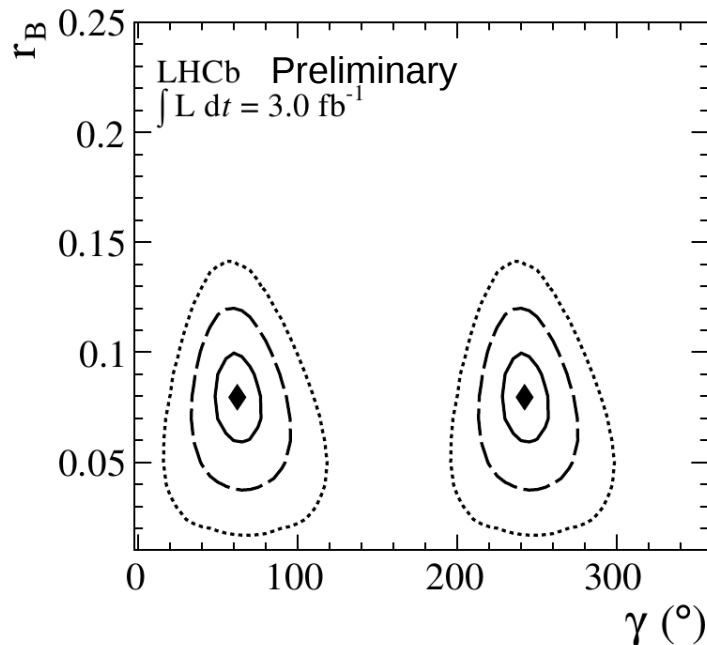


Results on polar coordinates

- Confidence intervals with stat+syst uncertainty on x and y.
- 1 fb^{-1} result : $(44^{+43}_{-38})^\circ$
- **Precision reach the B factories separate γ combination result.**

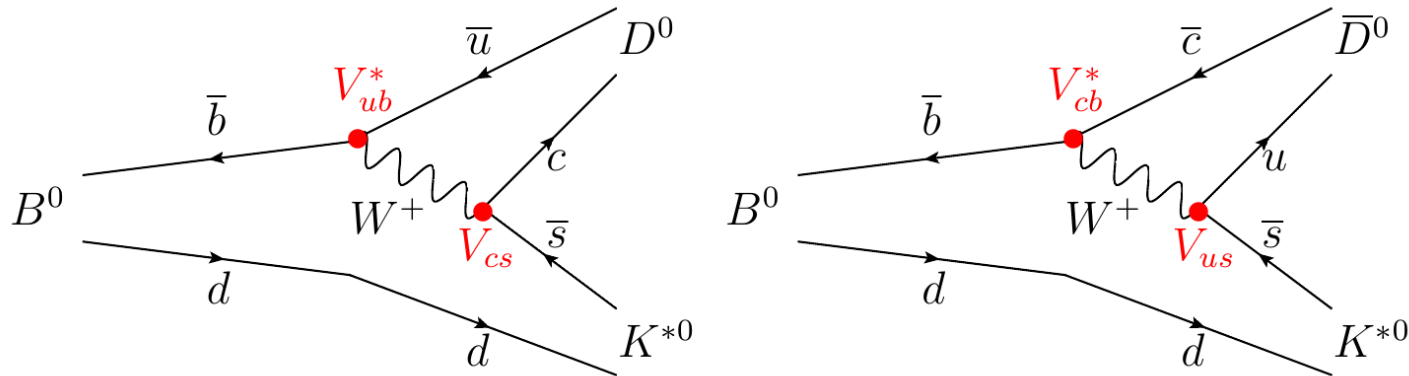
$$r_B = 0.080^{+0.019}_{-0.021}$$
$$\gamma = (62^{+15}_{-14})^\circ$$
$$\delta_B = (134^{+14}_{-15})^\circ$$

Preliminary

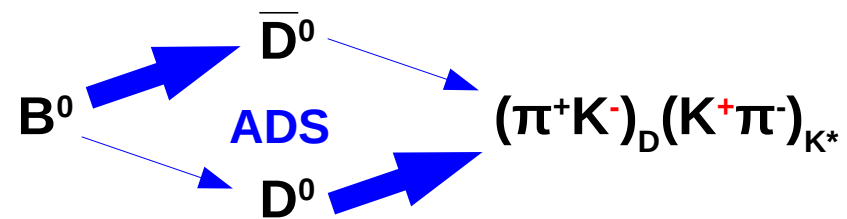
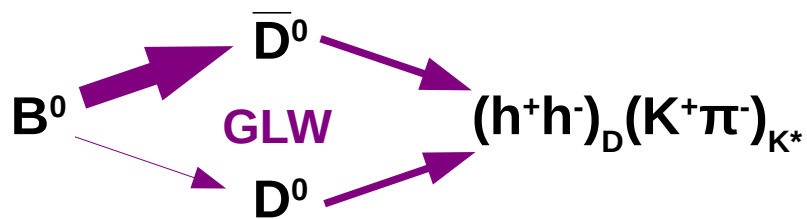


2D projections of confidence regions (all uncertainties included)

$B^0 \rightarrow DK^{*0}$



- Both diagrams colour suppressed: **larger r_B than in $B \rightarrow DK$** .
 - Expect better sensitivity to gamma.
 - Experimentally more challenging.
- **Self-tagged decay** thanks to $K^{*0} \rightarrow K^+\pi^-$.
- So far only the 2-body modes available (3 fb^{-1}).



CPV observables

Several observables sensitive to γ can be built, for instance:

- Asymmetries in $D \rightarrow$ CP eigenstates (KK or $\pi\pi$):

$$\mathcal{A}_d^{hh} \equiv \frac{\Gamma(\bar{B}^0 \rightarrow D(h^+h^-)\bar{K}^{*0}) - \Gamma(B^0 \rightarrow D(h^+h^-)K^{*0})}{\Gamma(\bar{B}^0 \rightarrow D(h^+h^-)\bar{K}^{*0}) + \Gamma(B^0 \rightarrow D(h^+h^-)K^{*0})} = \frac{2r_B \kappa \sin \delta_B \sin \gamma}{1 + r_B^2 + 2r_B \kappa \cos \delta_B \cos \gamma}$$

- Ratio with the DCS decay $D^0 \rightarrow K^+\pi^-$ and CF $D^0 \rightarrow K^-\pi^+$:

$$\mathcal{R}_d^+ \equiv \frac{\Gamma(B^0 \rightarrow D(\pi^+K^-)K^{*0})}{\Gamma(B^0 \rightarrow D(K^+\pi^-)K^{*0})} = \frac{r_B^2 + r_D^2 + 2r_B r_D \kappa \cos(\delta_B + \delta_D + \gamma)}{1 + r_B^2 r_D^2 + 2r_B r_D \kappa \cos(\delta_B - \delta_D + \gamma)}$$

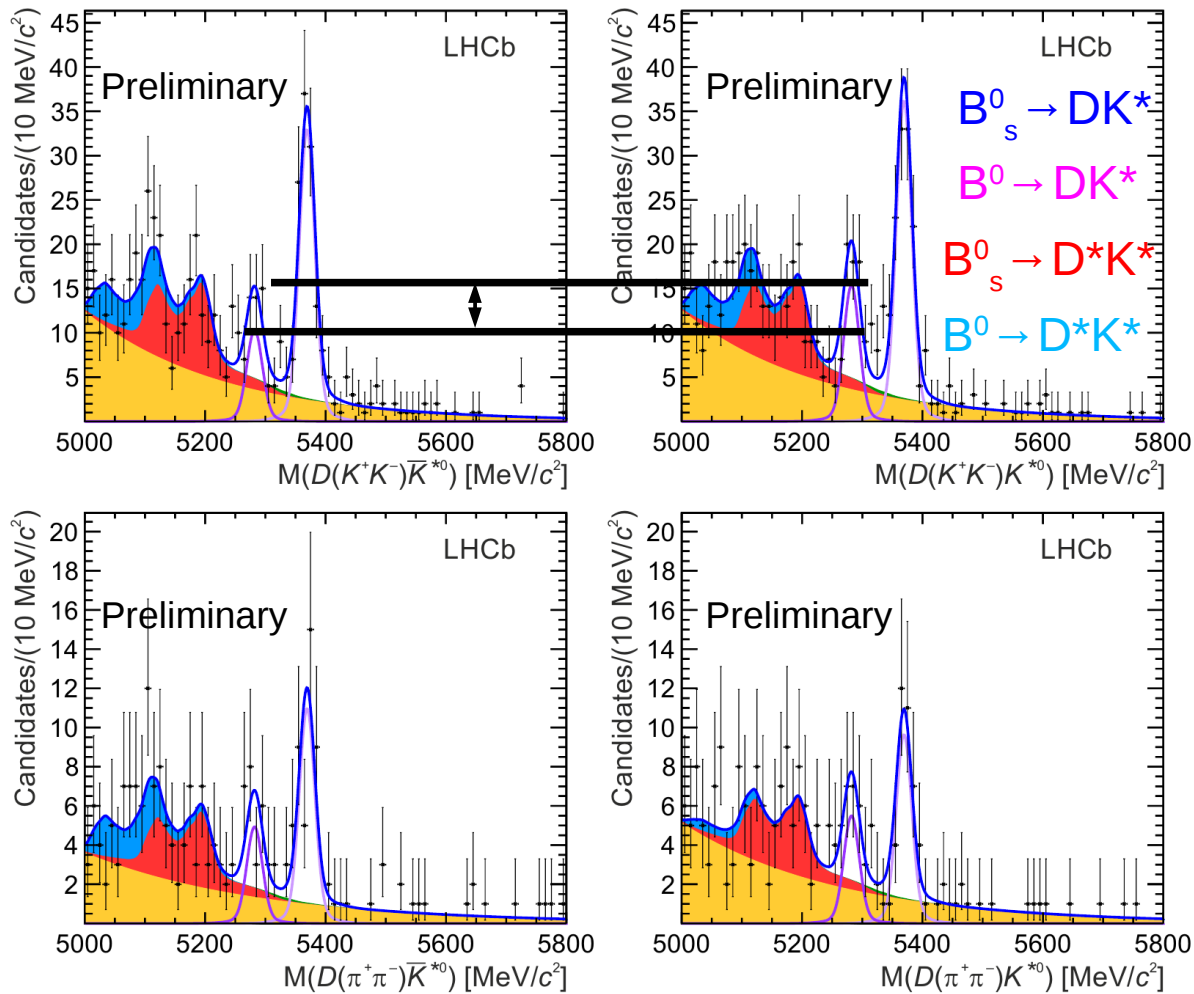
$$\mathcal{R}_d^- \equiv \frac{\Gamma(\bar{B}^0 \rightarrow D(\pi^-K^+)\bar{K}^{*0})}{\Gamma(\bar{B}^0 \rightarrow D(K^-\pi^+)\bar{K}^{*0})} = \frac{r_B^2 + r_D^2 + 2r_B r_D \kappa \cos(\delta_B + \delta_D - \gamma)}{1 + r_B^2 r_D^2 + 2r_B r_D \kappa \cos(\delta_B - \delta_D - \gamma)}$$

κ is the coherence factor taking into account the effect of the $B^0 \rightarrow DK^+\pi^-$ non resonant contribution in the K^{*0} signal region.

$B^0 \rightarrow D(hh)K^{*0}$

\bar{B}^0

B^0



- Signal significance:
 - KK : 8.6σ
 - $\pi\pi$: 5.8σ
- Production and efficiency asymmetries are taken into account

$$\mathcal{A}_d^{KK} = -0.20 \pm 0.15 \pm 0.02$$

$$\mathcal{A}_d^{\pi\pi} = -0.09 \pm 0.22 \pm 0.02$$

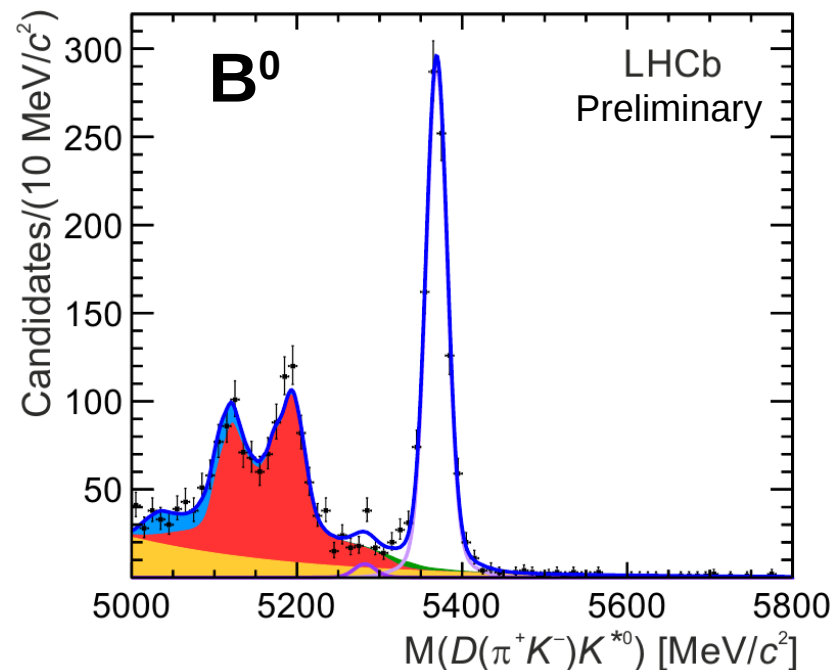
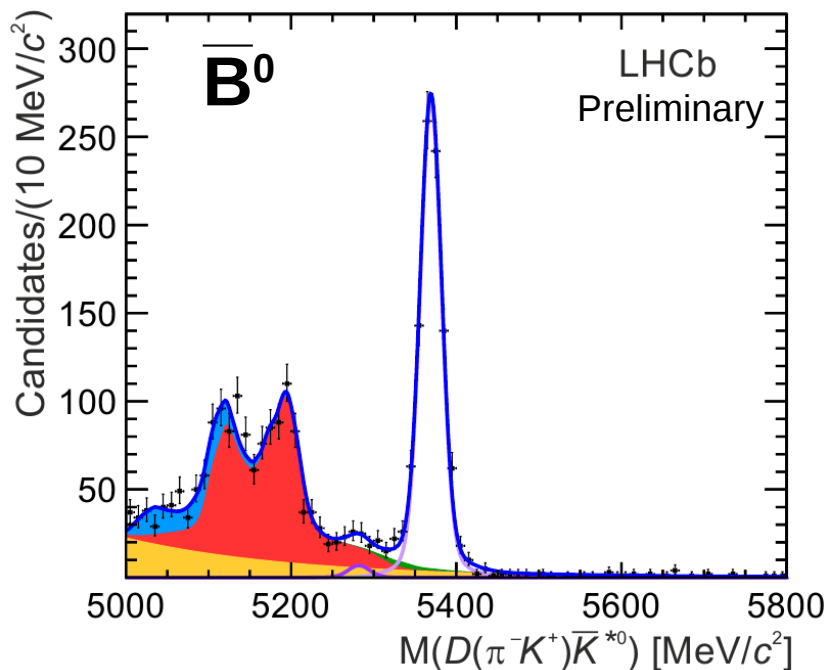
Preliminary

$B^0 \rightarrow D(\pi K)K^{*0}$

- Combined signal significance: 2.9σ

$$\mathcal{R}_d^+ = 0.06 \pm 0.03 \pm 0.01$$
$$\mathcal{R}_d^- = 0.06 \pm 0.03 \pm 0.01$$

Preliminary



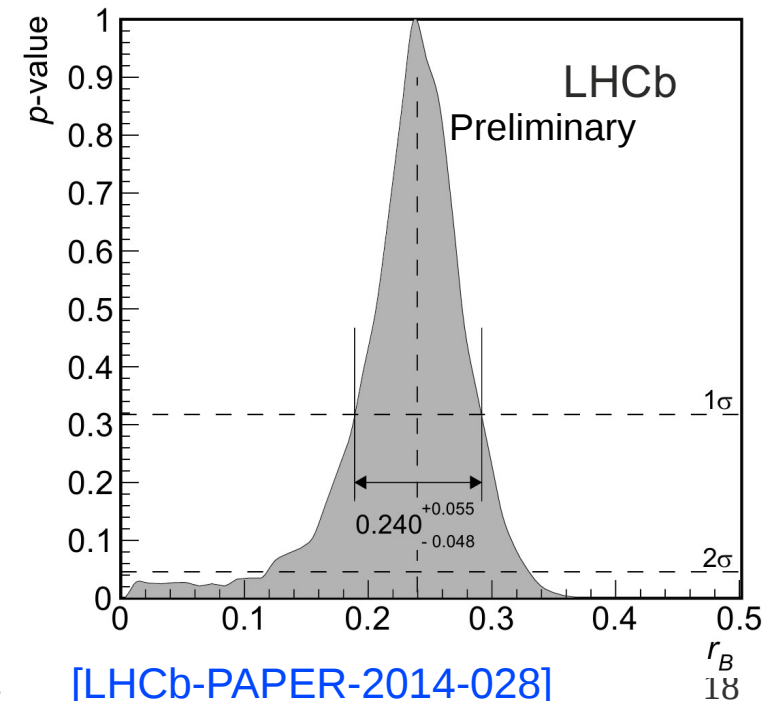
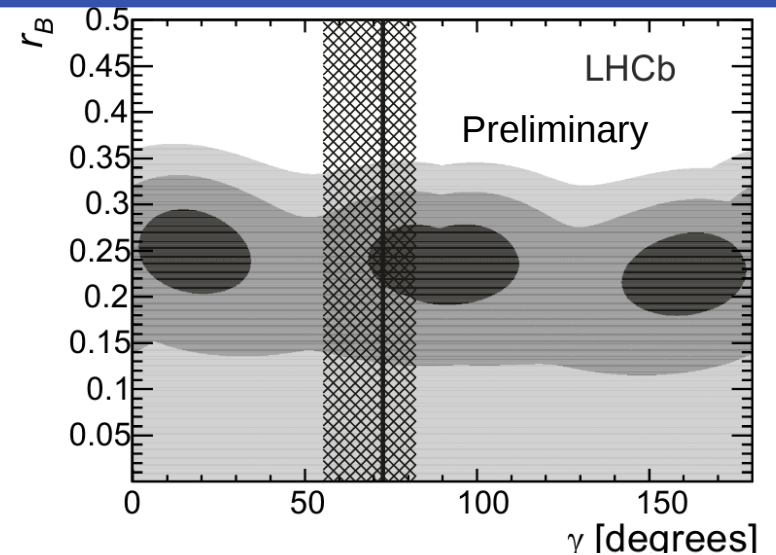
Implication on the value of r_B

- Frequentist scan of (r_B, γ, δ_B) .
- $\kappa = 0.95 \pm 0.03$ from a simulation study with a realistic model of $B^0 \rightarrow DK\pi$.
- r_B estimation at a 68.3% CL:

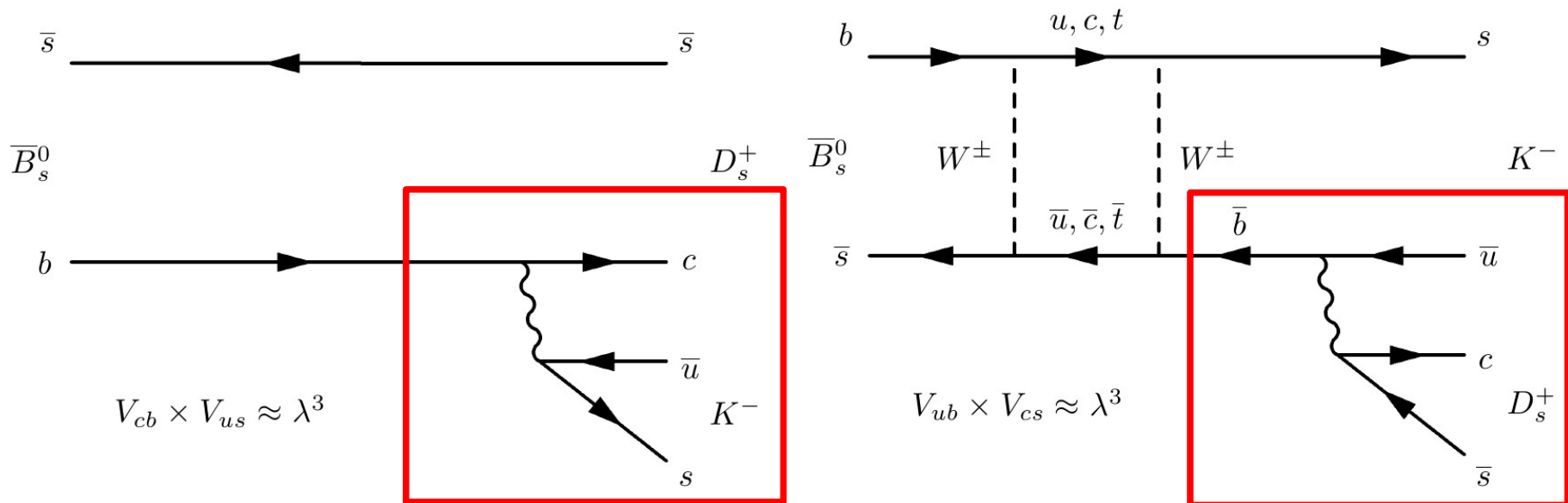
$$r_B = 0.240^{+0.055}_{-0.048}$$

Preliminary

- **Most precise measurement to date.**
- High r_B value : encouraging for a better γ measurement.



$B_s^0 \rightarrow D_s K^\pm$



- CP violation in the **mixing and decay**.
- Same tree level process as presented previously.
- **Time dependent** measurement (more complex).
- **Measure ($\gamma - 2\beta_s$)**
- Assume $\Phi_s = -2\beta_s$ and use as external input the Φ_s measurement from $B_s^0 \rightarrow J/\psi\Phi$ (much better precision).

CP violation observables

- A_f = decay amplitude of B_s^0 to final state f
- $\lambda_f = (q/p)(\bar{A}_f/A_f)$

Time dependent decay rate:

$$\frac{d\Gamma_{B_s^0 \rightarrow f}(t)}{dt} = \frac{1}{2}|A_f|^2(1 + |\lambda_f|^2)e^{-\Gamma_s t} \left[\cosh\left(\frac{\Delta\Gamma_s t}{2}\right) - A_f^{\Delta\Gamma} \sinh\left(\frac{\Delta\Gamma_s t}{2}\right) + C_f \cos(\Delta m_s t) - S_f \sin(\Delta m_s t) \right]$$

$$\frac{d\Gamma_{\bar{B}_s^0 \rightarrow f}(t)}{dt} = \frac{1}{2}|A_f|^2 \left| \frac{p}{q} \right|^2 (1 + |\lambda_f|^2)e^{-\Gamma_s t} \left[\cosh\left(\frac{\Delta\Gamma_s t}{2}\right) - A_f^{\Delta\Gamma} \sinh\left(\frac{\Delta\Gamma_s t}{2}\right) - C_f \cos(\Delta m_s t) + S_f \sin(\Delta m_s t) \right]$$

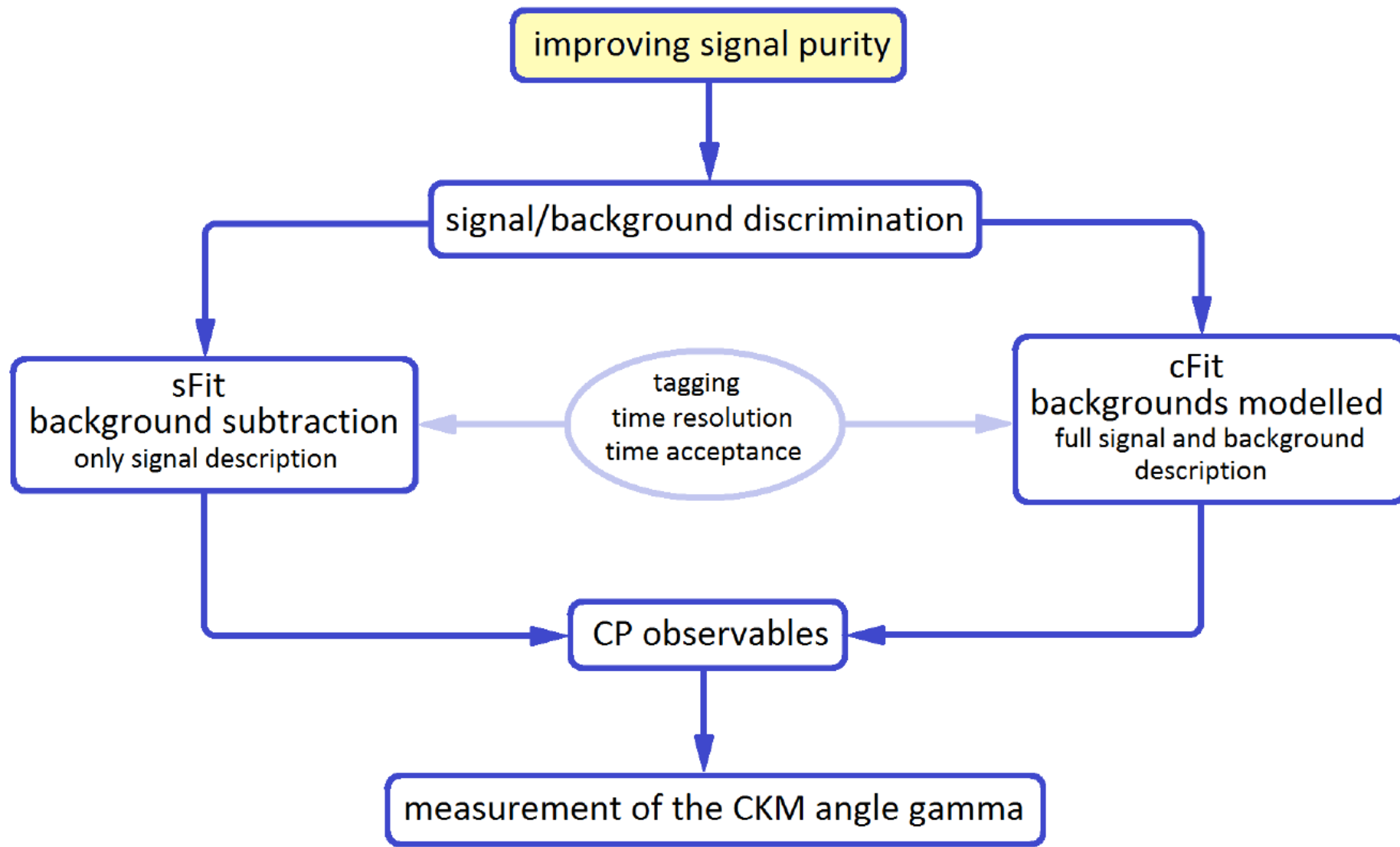
CP observables:

$$C_f = \frac{1 - r_{D_s K}^2}{1 + r_{D_s K}^2},$$

$$A_f^{\Delta\Gamma} = \frac{2r_{D_s K} \cos(\delta - (\gamma - 2\beta_s))}{1 + r_{D_s K}^2}, \quad A_{\bar{f}}^{\Delta\Gamma} = \frac{2r_{D_s K} \cos(\delta + (\gamma - 2\beta_s))}{1 + r_{D_s K}^2},$$

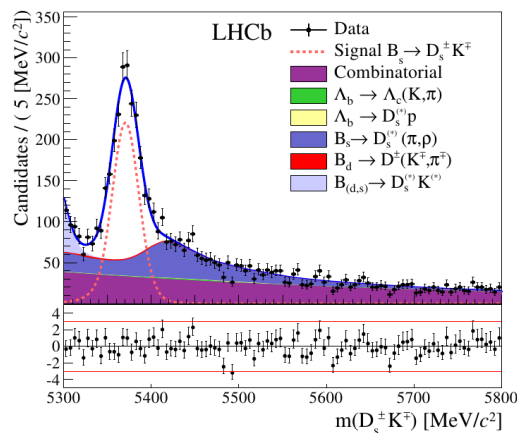
$$S_f = \frac{2r_{D_s K} \sin(\delta - (\gamma - 2\beta_s))}{1 + r_{D_s K}^2}, \quad S_{\bar{f}} = \frac{2r_{D_s K} \sin(\delta + (\gamma - 2\beta_s))}{1 + r_{D_s K}^2}.$$

Strategy

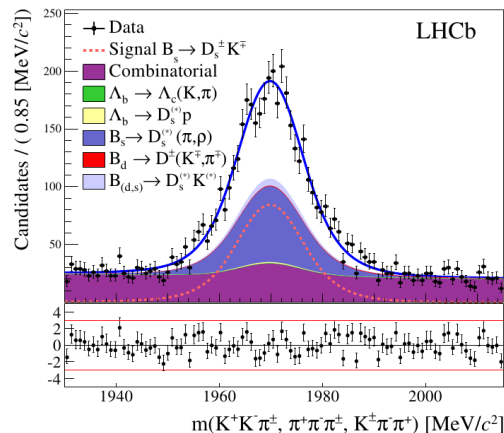


Signal/Background discrimination

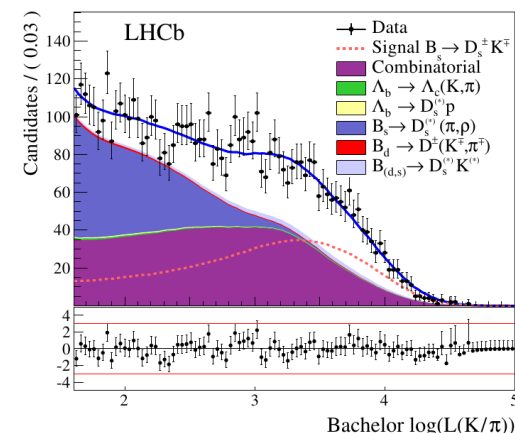
$D_s K$ mass



$KK\pi, K\pi\pi, \pi\pi\pi$ mass



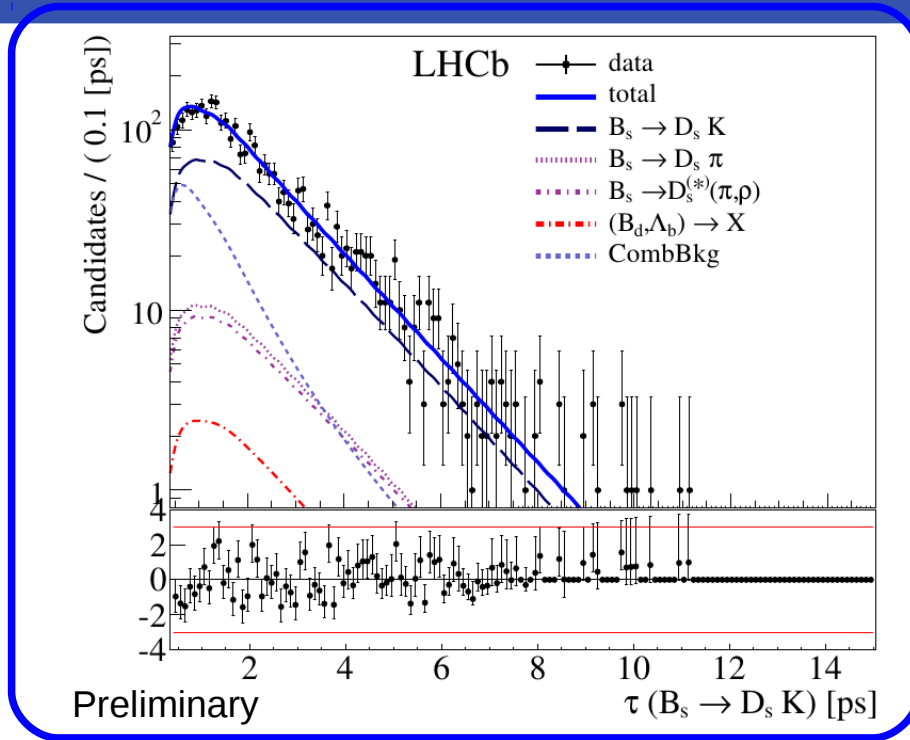
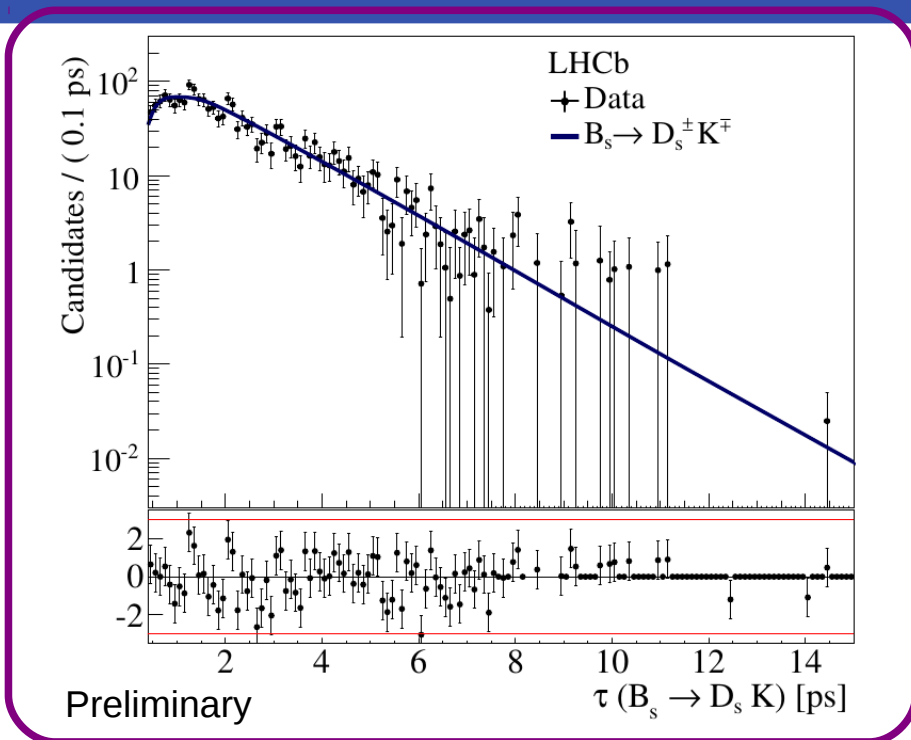
K bachelor ID



All preliminary

- Consider 3 D_s decays: $KK\pi, K\pi\pi, \pi\pi\pi$.
- Simultaneous 3D fit of $B_s^0 \rightarrow D_s K^\pm$ and $B_s^0 \rightarrow D_s \pi^\pm$.
 - $m(B_s), m(D_s)$ and **PID variable** on the K/π from the B (bachelor).
- Discrimination of signal and background.
- Signal weights determination.

Decay Time fit result



Parameter	<i>sFit</i> fitted value	<i>cFit</i> fitted value
C_f	$0.52 \pm 0.25 \pm 0.04$	$0.53 \pm 0.25 \pm 0.04$
$A_f^{\Delta\Gamma}$	$0.29 \pm 0.42 \pm 0.17$	$0.37 \pm 0.42 \pm 0.20$
$A_{\bar{f}}^{\Delta\Gamma}$	$0.14 \pm 0.41 \pm 0.18$	$0.20 \pm 0.41 \pm 0.20$
S_f	$-0.90 \pm 0.31 \pm 0.06$	$-1.09 \pm 0.33 \pm 0.08$
$S_{\bar{f}}$	$-0.36 \pm 0.34 \pm 0.06$	$-0.36 \pm 0.34 \pm 0.08$

- Leading syst.: acceptance, $\Gamma_s, \Delta\Gamma_s$.
- **Excellent agreement.**

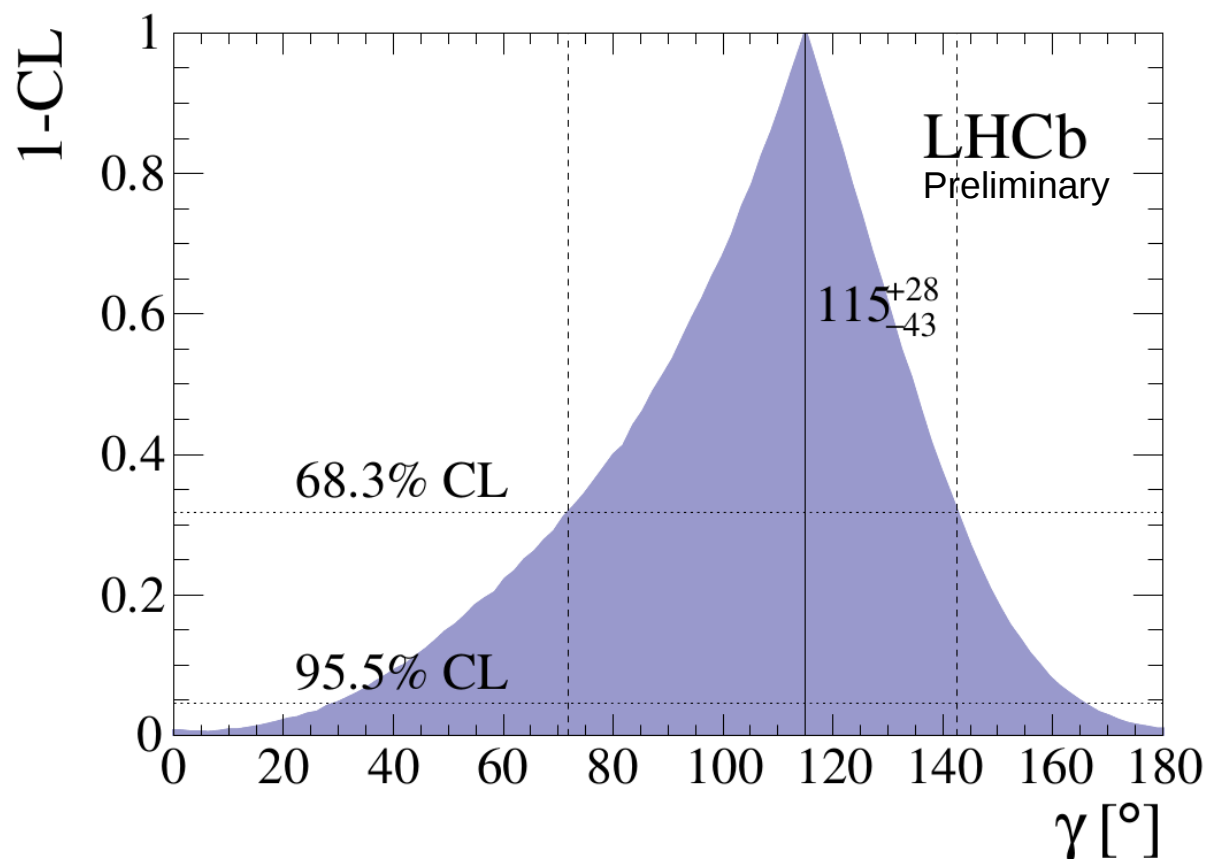
Interpretation on γ angle

- Take cfit results to make 68% CL.
- Statistical+Systematics (and Correlation) taken into account.
- Use only 1 fb^{-1} .

$$\gamma = (115^{+28}_{-43})^\circ,$$
$$\delta = (3^{+19}_{-20})^\circ,$$
$$r_{D_s K} = 0.53^{+0.17}_{-0.16},$$

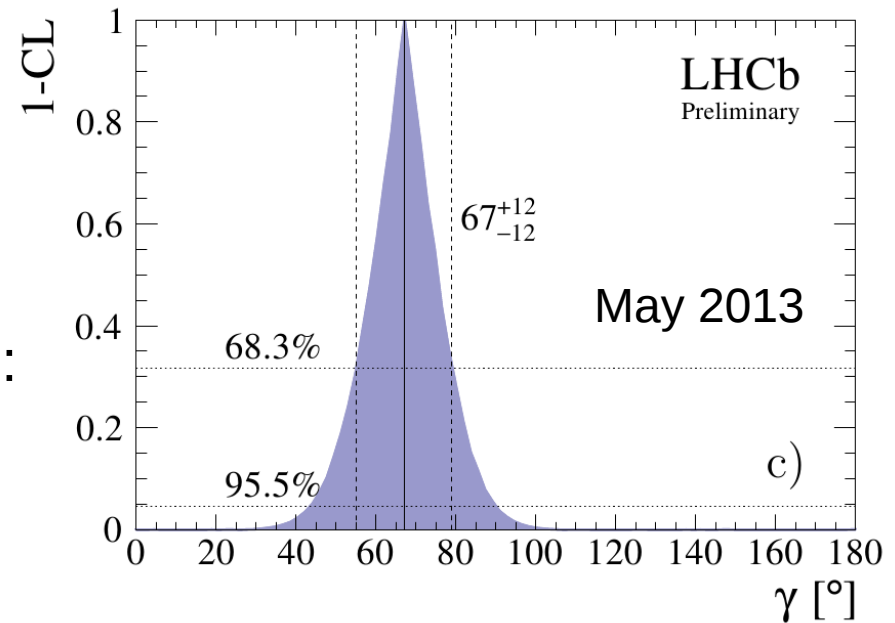
Preliminary

**World first
measurement of γ
from $B_s^0 \rightarrow D_s K^\pm$!**



Perspectives

- The updated GGSZ 3fb^{-1} improved significantly from the previous ($2+1\text{fb}^{-1}$).
- $B^0 \rightarrow DK^{*0}$ and $B_s \rightarrow D_s K$ will contribute to reduce the uncertainty.
- Other $B \rightarrow DK$, $B \rightarrow DX$ analysis carried on:
 - updating from 1fb^{-1} to 3fb^{-1} .
 - New D decays.
- γ from loop measurement coming soon.



Stay tune for the next LHCb γ combination!

BACKUP

$B_s^0 \rightarrow D_s K^\pm$ time fit inputs

- **Tagging:**
 - Combination of OS and SS tagging.
 - Efficiency for tagging an event : 67.53%
 - Effective tagging power: 5.07%
- **Time acceptance:**
 - Taken from $B_s^0 \rightarrow D_s \pi^\pm$ (with simulation correction).
- **Time resolution:**
 - Use per event error, with average resolution of 47 fs.
- **External inputs:**
 - $\Gamma_s, \Delta\Gamma_s, \Gamma_d, \Gamma_{\Lambda b}$ and Δm_s fixed from other measurements

