

Charm CPV and Mixing at Belle

BEACH 2014 @Birmingham
July 21-26, 2014

Byeong Rok Ko (Korea University)
for the Belle Collaboration

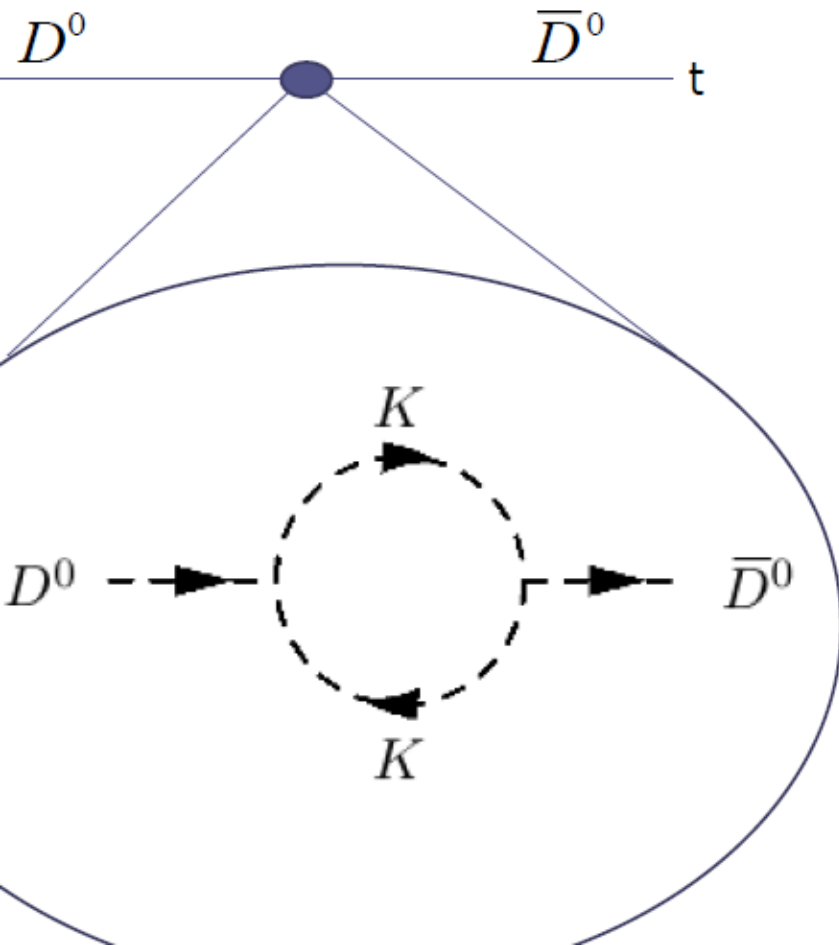
◦ Introduction

- CPV in charm decays
 - Very small in the Standard Model (SM), $< O(0.1\%)$
 - $O(1\%)$ CPV in charm decays would signal new physics

CP violation in charm decays
provides a unique probe
to search for beyond the SM

◦ Introduction

- Charm mixing



- SM re-scattering dominates
→ SM prediction of the mixing rate is quite difficult

**Probe to search
for BSM**

- Independent observations of the mixing from LHCb, CDF and Belle

Contents

◦ Introduction

1) Mixing in $D^0 \rightarrow K^+ \pi^-$

2) Mixing and indirect CPV in $D^0 \rightarrow K_S^0 \pi^+ \pi^-$

3) Time-integrated CPV in $D^0 \rightarrow \pi^0 \pi^0$

(also update CPV in $D^0 \rightarrow K_S^0 \pi^0$)

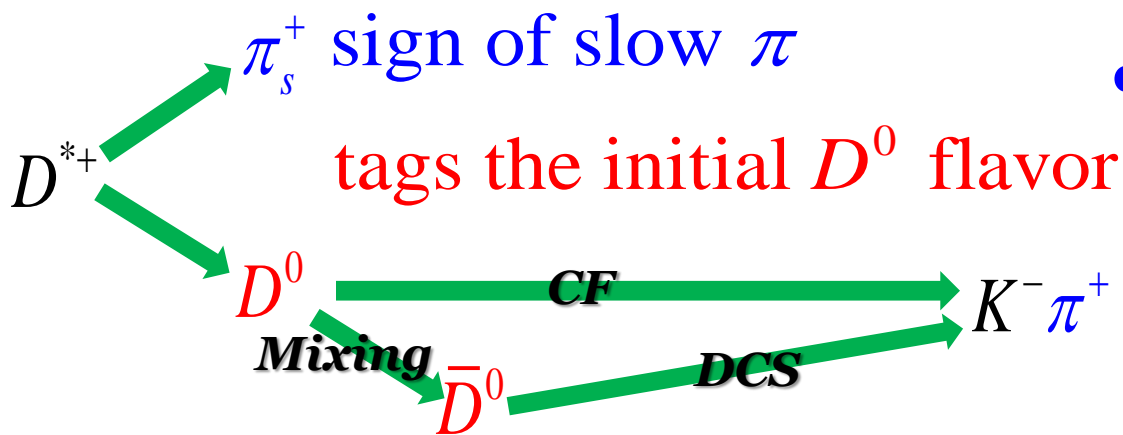
◦ Summary

1) Mixing in $D^0 \rightarrow K^+ \pi^-$

-time-dependent ratio of $D^0 \rightarrow K^+ \pi^-$ (WS) to $D^0 \rightarrow K^- \pi^+$ (RS) decay rates

(the role of RS : cancel most of experimental effects out)

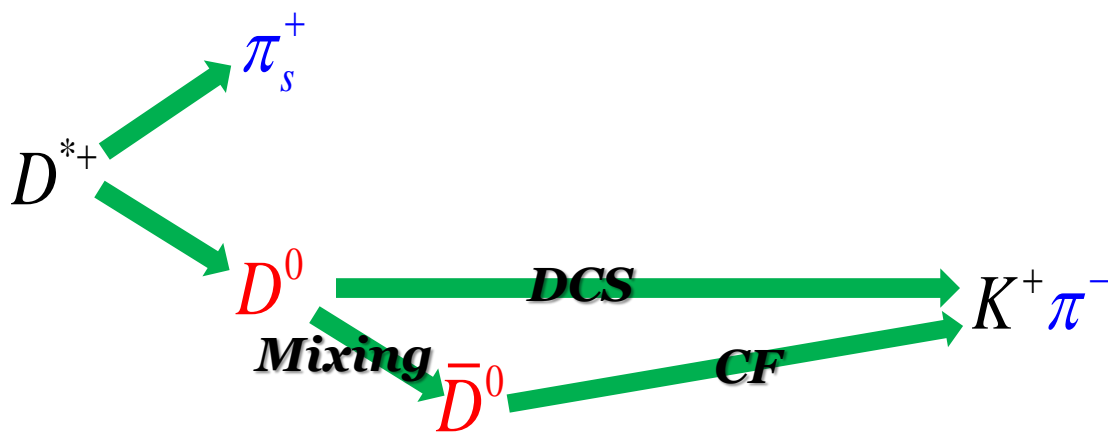
-have to use **tagged D^0** from D^{*+} decay to identify WS and RS



$$\bullet \mathcal{A}_{RS} = \mathcal{A}_{CF} + \mathcal{A}_{DCS} \mathcal{A}_{Mixing} \approx \mathcal{A}_{CF}$$

: effectively CF decays

$$(\because \mathcal{A}_{CF} \square \mathcal{A}_{DCS} \approx \mathcal{A}_{Mixing})$$



$$\bullet \mathcal{A}_{WS} = \mathcal{A}_{DCS} + \mathcal{A}_{CF} \mathcal{A}_{Mixing}$$

$$= \mathcal{A}_{CF} \left(\mathcal{A}_{DCS} / \mathcal{A}_{CF} + \mathcal{A}_{Mixing} \right)$$

: coherent sum of
DCS and Mixing

1) Mixing in $D^0 \rightarrow K^+ \pi^-$

-time-dependent ratio of $D^0 \rightarrow K^+ \pi^-$ (WS) to $D^0 \rightarrow K^- \pi^+$ (RS) decay rates

(the role of RS : cancel most of experimental effects out)

-have to use **tagged** D^0 from D^{*+} decay to identify WS and RS

• time-dependent decay rates π^+ sign of slow π

D^{*+} Under No tags and small mixing

$$\bullet \mathcal{A}_{RS} = \mathcal{A}_{CF} + \mathcal{A}_{DCS} \mathcal{A}_{Mixing} \approx \mathcal{A}_{CF}$$

: effectively CF decays

$$\Gamma_{RS}(\tilde{t}/\tau) \approx |\mathcal{A}_{CF}|^2 e^{-\tilde{t}/\tau} \quad (\because \mathcal{A}_{CF} \square \mathcal{A}_{DCS} \approx \mathcal{A}_{Mixing})$$

$$\Gamma_{WS}(\tilde{t}/\tau) \approx |\mathcal{A}_{CF}|^2 e^{-\tilde{t}/\tau}$$

$$D^{*+} \left(\underbrace{R_D}_{DCS} + \underbrace{\sqrt{R_D} y'}_{\text{Interference}} \frac{\tilde{t}}{\tau} + \underbrace{\frac{x'^2 + y'^2}{4}}_{\text{Mixing}} \left(\frac{\tilde{t}}{\tau} \right)^2 \right)$$

$\rightarrow K^+ \pi^-$ (CF)
 $\rightarrow K^- \pi^+$ (DCS)

$$\bullet \mathcal{A}_{WS} = \mathcal{A}_{DCS} + \mathcal{A}_{CF} \mathcal{A}_{Mixing} = \mathcal{A}_{CF} \left(\mathcal{A}_{DCS} / \mathcal{A}_{CF} + \mathcal{A}_{Mixing} \right)$$

: coherent sum of
DCS and Mixing

1) Mixing in $D^0 \rightarrow K^+ \pi^-$

-time-dependent ratio of $D^0 \rightarrow K^+ \pi^-$ (WS) to $D^0 \rightarrow K^- \pi^+$ (RS) decay rates
(the role of RS : cancel most of experimental effects out)

-have to use **tagged D^0** from D^{*+} decay to identify WS and RS

•time-dependent decay rates

under No CPV and small mixing

$$\Gamma_{\text{RS}}(\tilde{t}/\tau) \approx |\mathcal{A}_{\text{CF}}|^2 e^{-\tilde{t}/\tau}$$

$$\Gamma_{\text{WS}}(\tilde{t}/\tau) \approx |\mathcal{A}_{\text{CF}}|^2 e^{-\tilde{t}/\tau}$$

$$\times \left(\underbrace{R_D}_{\text{DCS}} + \underbrace{\sqrt{R_D} y'}_{\text{Interference}} \frac{\tilde{t}}{\tau} + \underbrace{\frac{x'^2 + y'^2}{4}}_{\text{Mixing}} \left(\frac{\tilde{t}}{\tau} \right)^2 \right)$$

$$\bullet \mathcal{A}_{\text{RS}} = \mathcal{A}_{\text{CF}} + \mathcal{A}_{\text{DCS}} \mathcal{A}_{\text{Mixing}} \approx \mathcal{A}_{\text{CF}}$$

$$\left\{ \begin{array}{l} \tilde{t} : \text{decay time, } \tau : D^0 \text{ lifetime} \\ R_D = \left(\frac{|\mathcal{A}_{\text{DCS}}|^2}{|\mathcal{A}_{\text{CF}}|^2} \right) \approx \mathcal{A}_{\text{Mixing}}^2 \\ x' = x \cos \delta + y \sin \delta \\ y' = x \sin \delta - y \cos \delta \\ x = \frac{(m_1 - m_2) \Gamma}{2\Gamma} = \mathcal{A}_{\text{CF}} \left(\frac{\mathcal{A}_{\text{DCS}}}{\mathcal{A}_{\text{CF}} + \mathcal{A}_{\text{Mixing}}} \right) \\ y = \frac{(\Gamma_1 - \Gamma_2)}{2\Gamma} \\ \Gamma = 1/\tau \\ \delta : \text{relative strong phase} \\ \text{between } \mathcal{A}_{\text{DCS}} \text{ and } \mathcal{A}_{\text{CF}} \end{array} \right.$$

Mixing

parameters

coherent sum of
DCS and Mixing

1) Mixing in $D^0 \rightarrow K^+ \pi^-$

- taking a ratio of the two decay rates

$$R(\tilde{t}/\tau) = \frac{\Gamma_{\text{WS}}(\tilde{t}/\tau)}{\Gamma_{\text{RS}}(\tilde{t}/\tau)} \approx R_D + \sqrt{R_D} y' \frac{\tilde{t}}{\tau} + \frac{x'^2 + y'^2}{4} \left(\frac{\tilde{t}}{\tau} \right)^2$$

*Note $e^{-\tilde{t}/\tau}$ cancel out

- extracting

R_D , y' , and x'^2 from $R(\tilde{t}/\tau)$
 → done by CDF and LHCb

1) Mixing in $D^0 \rightarrow K^+ \pi^-$

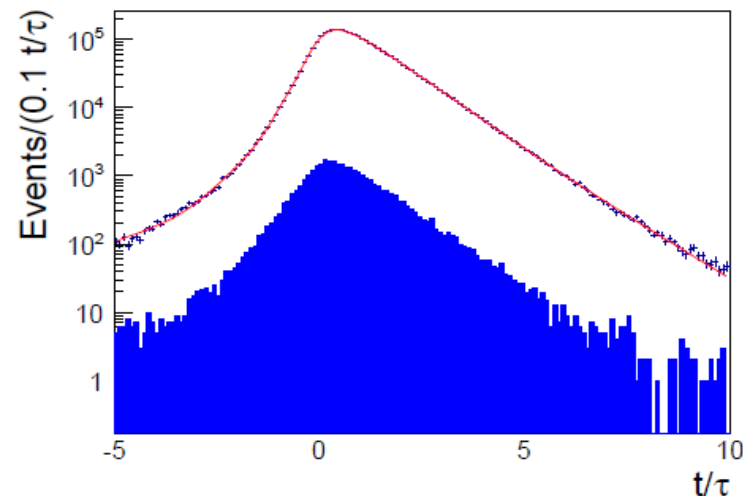
PRL 112, 111801 (2014)

- taking a ratio of the two decay rates

$$R(\tilde{t}/\tau) = \frac{\Gamma_{\text{WS}}(\tilde{t}/\tau)}{\Gamma_{\text{RS}}(\tilde{t}/\tau)} \approx R_D + \sqrt{R_D} y' \frac{\tilde{t}}{\tau} + \frac{x'^2 + y'^2}{4} \left(\frac{\tilde{t}}{\tau} \right)^2$$

* Note $e^{-\tilde{t}/\tau}$ cancel out

- RS decay time at Belle



t resolution : $\sim 0.3 t/\tau \sim 120$ fs
 most of events : $\sim 1.0 t/\tau \sim 400$ fs
 take into account the t
 resolution using convolution

- extracting

R_D , y' , and x'^2 from $R(\tilde{t}/\tau)$
 \rightarrow done by CDF and LHCb

- the ratio with convolution

$$R(t/\tau) = \frac{\int_{-\infty}^{+\infty} \Gamma_{\text{WS}}(\tilde{t}/\tau) \mathcal{R}(t/\tau - \tilde{t}/\tau) d(\tilde{t}/\tau)}{\int_{-\infty}^{+\infty} \Gamma_{\text{RS}}(\tilde{t}/\tau) \mathcal{R}(t/\tau - \tilde{t}/\tau) d(\tilde{t}/\tau)}$$

- \mathcal{R} : 4 Gaussians from RS decay time

* Note $e^{-\tilde{t}/\tau}$ does not cancel out

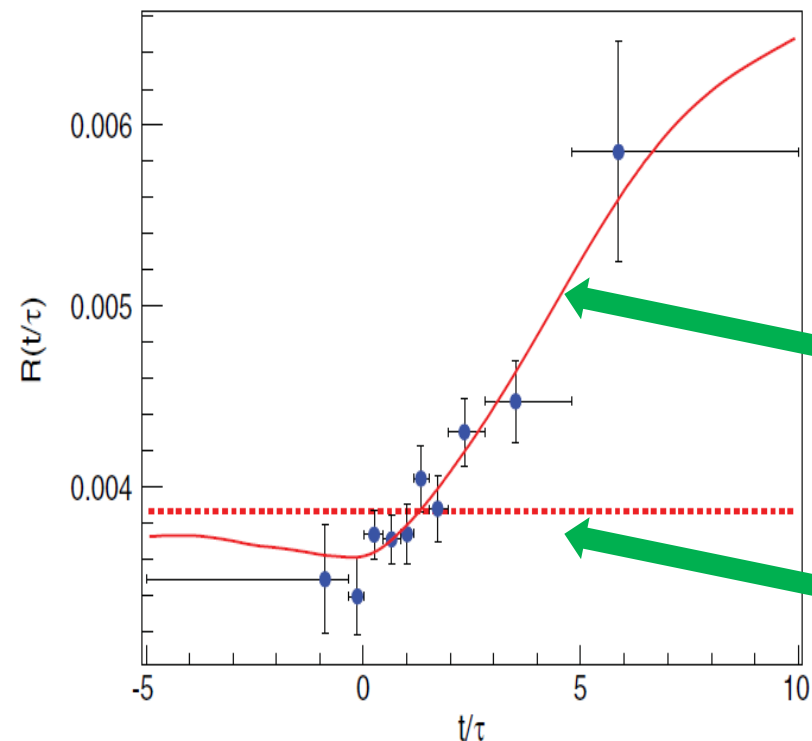
*complicate functional form

- extracting R_D , y' , and x'^2

from $R(t/\tau)$, not from $R(\tilde{t}/\tau)$ for Belle

1) Mixing in $D^0 \rightarrow K^+ \pi^-$

PRL 112, 111801 (2014)



Test hypothesis (χ^2/DOF)	Parameters	Fit results (10^{-3})
Mixing (4.2/7)	R_D y' x'^2	3.53 ± 0.13 4.6 ± 3.4 0.09 ± 0.22
No mixing (33.5/9)	R_D	3.864 ± 0.059

$$\bullet \Delta\chi^2 = \chi^2_{\text{Mixing}} - \chi^2_{\text{No Mixing}} = 29.3$$

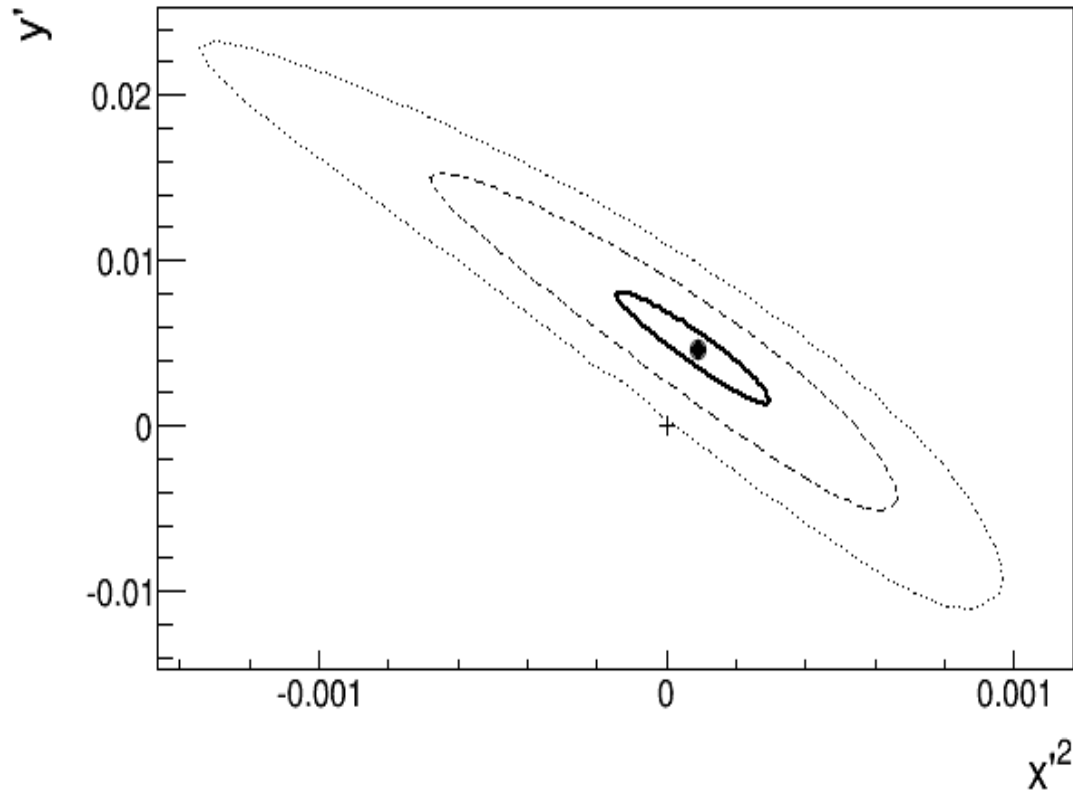
→ 5.1 standard deviations

from No mixing hypothesis

• First observation of
 $D^0 - \bar{D}^0$ mixing
in e^+e^- collisions

1) Mixing in $D^0 \rightarrow K^+ \pi^-$

PRL 112, 111801 (2014)



Correlation coefficient		
R_D	y'	x'^2
1	-0.865	+0.737
	1	-0.948
		1

- 1 (line), 3 (dashed-line), and 5 (dots) standard deviations from the best fit (point)
- + : no mixing

the best fit (point) :
5 σ away from No mixing

2) Mixing and indirect CPV in $D^0 \rightarrow K_S^0 \pi^+ \pi^-$

-time-dependent Dalitz fit

•time-dependent decay matrix elements

$$\begin{aligned}
 \mathcal{M}(m_+^2, m_-^2, t) &= g_+(t) \mathcal{A}(m_+^2, m_-^2) + \frac{q}{p} g_-(t) \bar{\mathcal{A}}(m_+^2, m_-^2) \\
 \bar{\mathcal{M}}(m_+^2, m_-^2, t) &= g_+(t) \bar{\mathcal{A}}(m_+^2, m_-^2) + \frac{p}{q} g_-(t) \mathcal{A}(m_+^2, m_-^2)
 \end{aligned}
 \left\{ \begin{array}{l} m_{\pm}^2 = m_{K_S^0 \pi^{\pm}}^2 \\ \mathcal{M}, \mathcal{A} \text{ for } D^0 \text{ decay} \\ \bar{\mathcal{M}}, \bar{\mathcal{A}} \text{ for } \bar{D}^0 \text{ decay} \end{array} \right.$$

2) Mixing and indirect CPV in $D^0 \rightarrow K_S^0 \pi^+ \pi^-$

-time-dependent Dalitz fit

•time-dependent decay matrix elements

$$\begin{aligned} \mathcal{M}(m_+^2, m_-^2, t) &= g_+(t) \mathcal{A}(m_+^2, m_-^2) + \frac{q}{p} g_-(t) \bar{\mathcal{A}}(m_+^2, m_-^2) \\ \bar{\mathcal{M}}(m_+^2, m_-^2, t) &= g_+(t) \bar{\mathcal{A}}(m_+^2, m_-^2) + \frac{p}{q} g_-(t) \mathcal{A}(m_+^2, m_-^2) \end{aligned} \quad \left\{ \begin{array}{l} m_{\pm}^2 = m_{K_S^0 \pi^{\pm}}^2 \\ \mathcal{M}, \mathcal{A} \text{ for } D^0 \text{ decay} \\ \bar{\mathcal{M}}, \bar{\mathcal{A}} \text{ for } \bar{D}^0 \text{ decay} \end{array} \right.$$

◦ t -independent part

$$\mathcal{A}(m_+^2, m_-^2) = \sum a_j e^{i\delta_j} A_j(m_+^2, m_-^2)$$

$$\bar{\mathcal{A}}(m_+^2, m_-^2) = \sum \bar{a}_j e^{i\bar{\delta}_j} A_j(m_+^2, m_-^2)$$

a_j and δ_j from the fit

$A_j(m_+^2, m_-^2)$: known

$$\left\{ \begin{array}{l} a_j, \delta_j \text{ for } D^0 \text{ decay} \\ \bar{a}_j, \bar{\delta}_j \text{ for } \bar{D}^0 \text{ decay} \end{array} \right.$$

2) Mixing and indirect CPV in $D^0 \rightarrow K_S^0 \pi^+ \pi^-$

-time-dependent Dalitz fit

- time-dependent decay matrix elements

$$\mathcal{M}(m_+^2, m_-^2, t) = g_+(t) \mathcal{A}(m_+^2, m_-^2) + \frac{q}{p} g_-(t) \bar{\mathcal{A}}(m_+^2, m_-^2)$$

$$\bar{\mathcal{M}}(m_+^2, m_-^2, t) = g_+(t) \bar{\mathcal{A}}(m_+^2, m_-^2) + \frac{p}{q} g_-(t) \mathcal{A}(m_+^2, m_-^2)$$

◦ t -independent part

$$\mathcal{A}(m_+^2, m_-^2) = \sum a_j e^{i\delta_j} A_j(m_+^2, m_-^2)$$

$$\bar{\mathcal{A}}(m_+^2, m_-^2) = \sum \bar{a}_j e^{i\bar{\delta}_j} A_j(m_+^2, m_-^2)$$

a_j and δ_j from the fit

$A_j(m_+^2, m_-^2)$: known

$$\begin{cases} a_j, \delta_j & \text{for } D^0 \text{ decay} \\ \bar{a}_j, \bar{\delta}_j & \text{for } \bar{D}^0 \text{ decay} \end{cases}$$

◦ t -dependent part

$$g_{\pm}(t) = \frac{1}{2} \left(e^{-i\lambda_1 t} \pm e^{-i\lambda_2 t} \right),$$

$$\lambda_i = m_i - \frac{i\Gamma_i}{2}$$

m_i and Γ_i : D_i mass and width

- \mathcal{M}^2 (\sim decay rates) contains

$$\left. \frac{q}{p} = \left| \frac{q}{p} \right| e^{i\phi} \right\} \text{CPV parameters } \left| \frac{q}{p} \right| \text{ and } \phi = \arg \left(\frac{q}{p} \right)$$

$$\left. \begin{array}{l} e^{-\Gamma t} \cos(x\Gamma t) \\ e^{-\Gamma t} \sin(x\Gamma t) \\ e^{[(-1 \pm y)\Gamma t]} \end{array} \right\} \text{the mixing parameters } x \text{ and } y$$

–obtain them simultaneously

2) Mixing and indirect CPV in $D^0 \rightarrow K_S^0 \pi^+ \pi^-$

-time-dependent Dalitz fit

- time-dependent decay matrix elements

$$\mathcal{M}(m_+^2, m_-^2, t) = g_+(t) \mathcal{A}(m_+^2, m_-^2) + \frac{q}{p} g_-(t) \bar{\mathcal{A}}(m_+^2, m_-^2)$$

$$\bar{\mathcal{M}}(m_+^2, m_-^2, t) = g_+(t) \bar{\mathcal{A}}(m_+^2, m_-^2) + \frac{p}{q} g_-(t) \mathcal{A}(m_+^2, m_-^2)$$

◦ t -independent part

$$\mathcal{A}(m_+^2, m_-^2) = \sum a_j e^{i\delta_j} A_j(m_+^2, m_-^2)$$

$$\bar{\mathcal{A}}(m_+^2, m_-^2) = \sum \bar{a}_j e^{i\bar{\delta}_j} A_j(m_+^2, m_-^2)$$

- t -integrated Dalitz fits to D^0 and \bar{D}^0 separately $\Rightarrow a_j \approx \bar{a}_j$ and $\delta_j \approx \bar{\delta}_j$

$A_j(m_+^2, m_-^2)$: known
 \rightarrow assume No direct CPV, $\mathcal{A}(m_+^2, m_-^2) = \bar{\mathcal{A}}(m_+^2, m_-^2)$

\rightarrow Search for indirect CPV

$\left\{ \begin{array}{l} a_j, \delta_j \text{ for } D^0 \text{ decay} \\ \bar{a}_j, \bar{\delta}_j \text{ for } \bar{D}^0 \text{ decay} \end{array} \right. \begin{array}{l} |q/p| \neq 1 : \text{CPV in mixing} \\ \arg(q/p) \neq 0 : \text{CPV in the interference between mixing and decay} \end{array}$

◦ t -dependent part

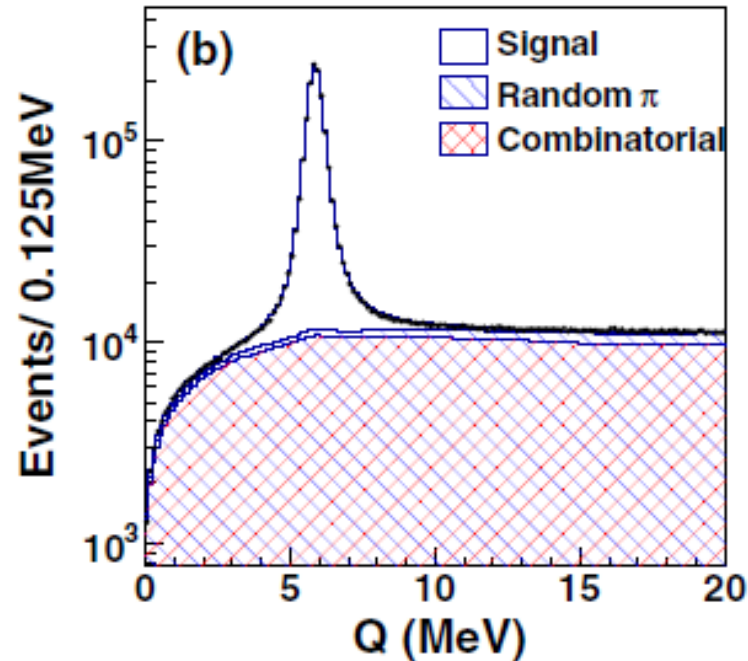
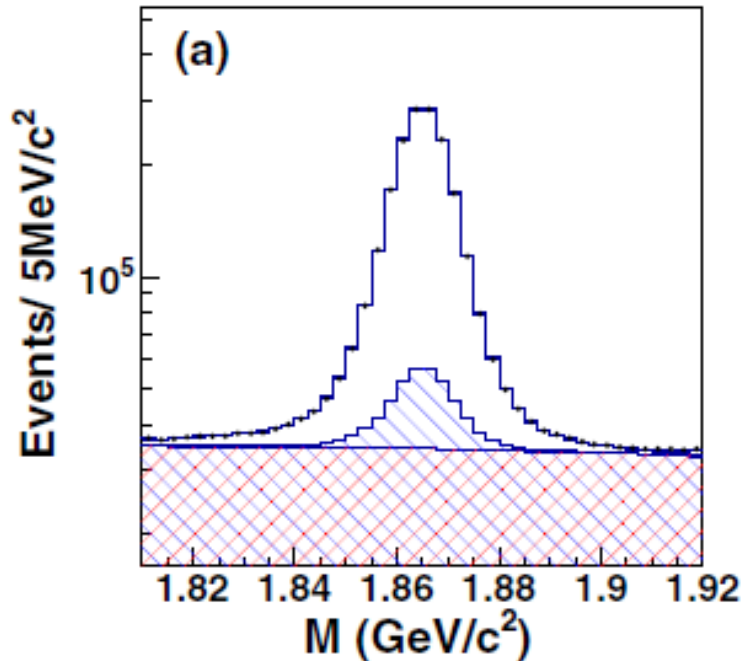
$$g_{\pm}(t) = \frac{1}{2} \left(e^{-i\lambda_1 t} \pm e^{-i\lambda_2 t} \right),$$

$$\lambda_i = m_i - \frac{i\Gamma_i}{2}$$

m_i and Γ_i : D_i mass and width

2) Mixing and indirect CPV in $D^0 \rightarrow K_S^0 \pi^+ \pi^-$

PRD 89, 091103 (2014)



• signal PDF:
gaussian and
asymmetric
gaussian

• signal PDF: $(M = M_{K_S^0 \pi^+ \pi^-})$

triple-gaussian

◦ signal region

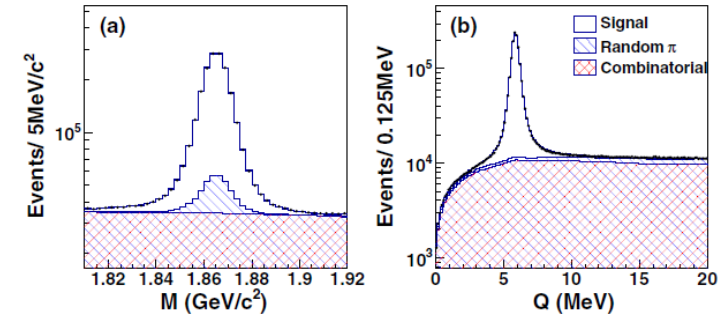
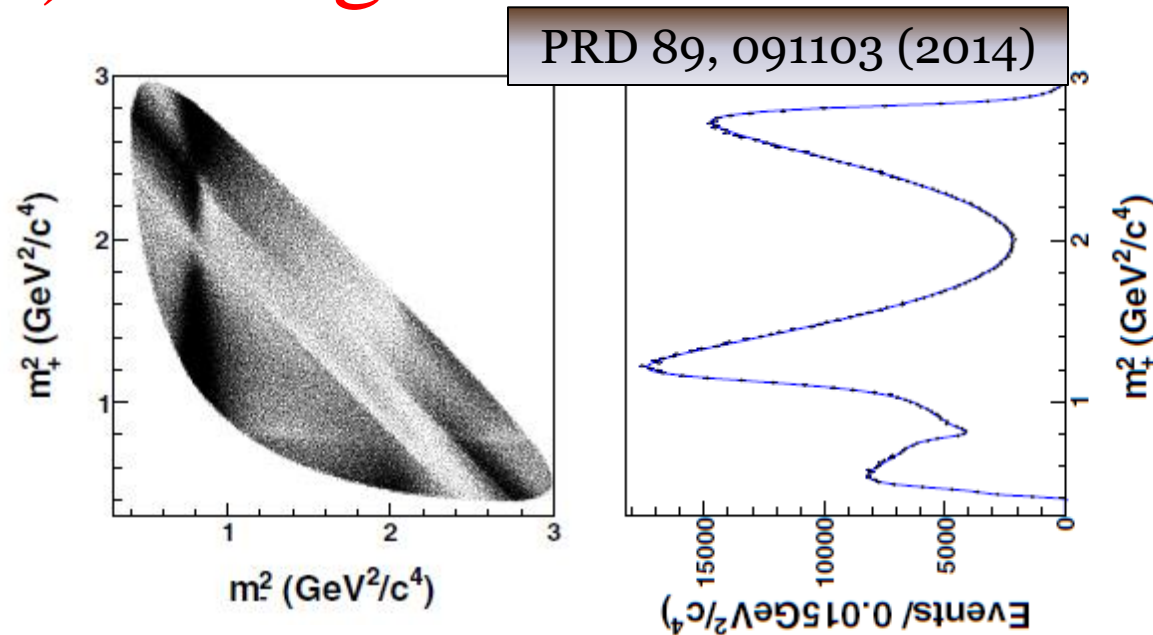
$$|M - m_{D^0}| < 15 \text{ MeV} \quad \Rightarrow$$

$$5.75 \text{ MeV} < Q < 5.95 \text{ MeV}$$

$$(Q = M_{K_S^0 \pi^+ \pi^- \pi_s^+} - M_{K_S^0 \pi^+ \pi^-} - m_{\pi_s^+})$$

- $\sim 1.2\text{M}$ signals
- $\sim 96\%$ purity

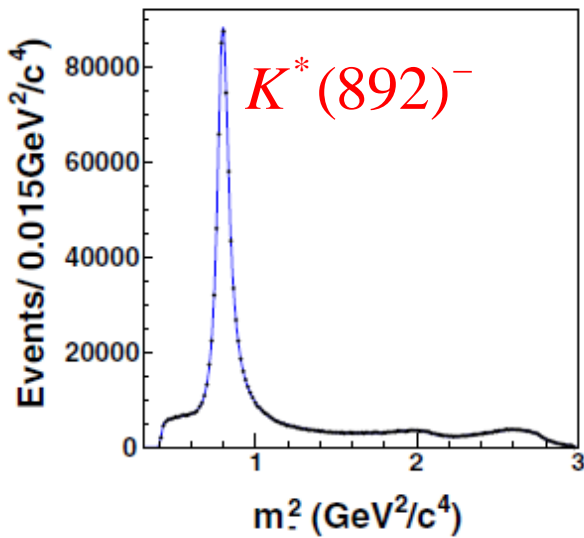
2) Mixing and indirect CPV in $D^0 \rightarrow K_S^0 \pi^+ \pi^-$



○ signal region

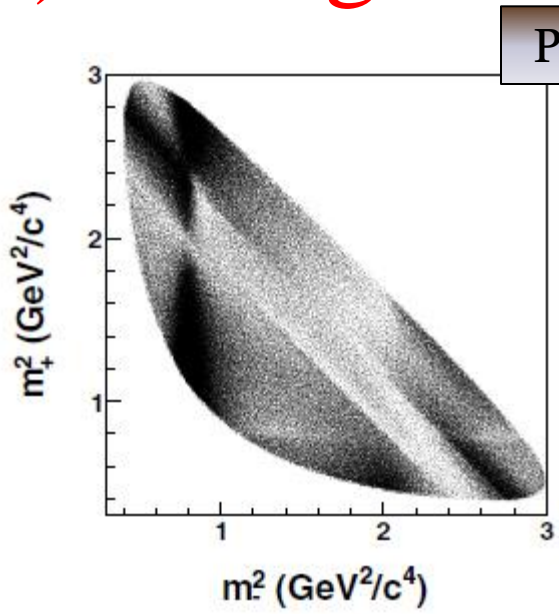
$$|M - m_{D^0}| < 15 \text{ MeV}$$

$$5.75 \text{ MeV} < Q < 5.95 \text{ MeV}$$

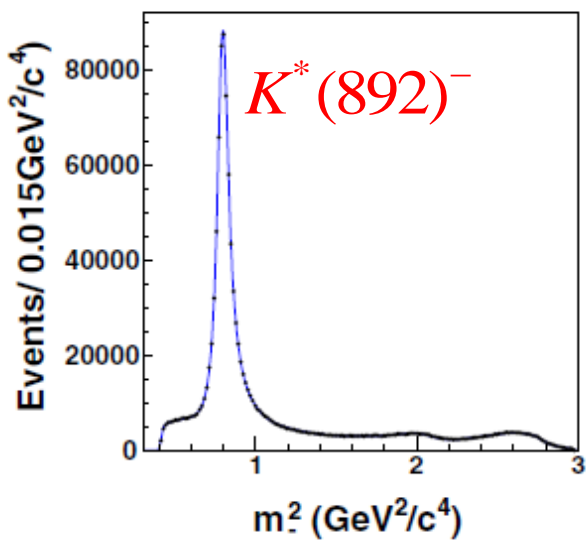
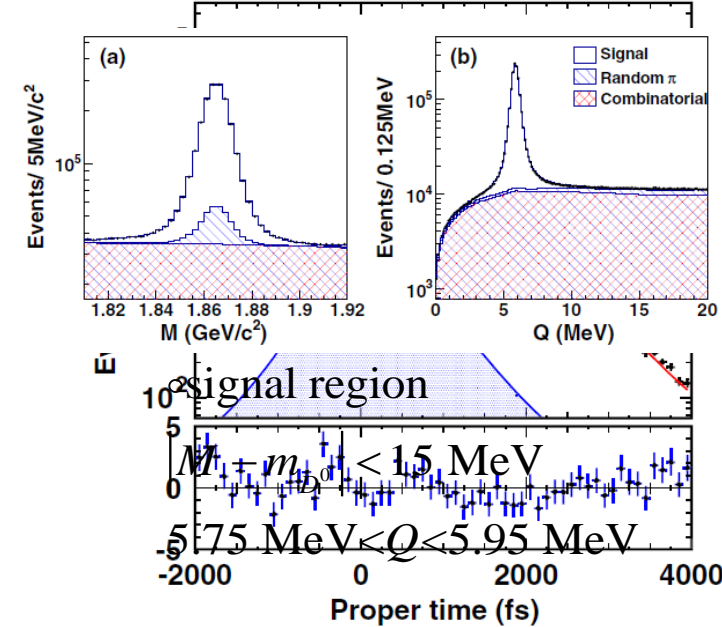
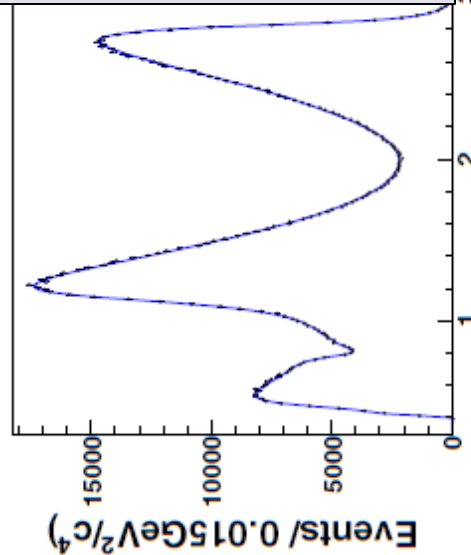


- best model found to be ;
 12 relativistic Breit-Wigner's
 (P- and D-waves)
 + K-matrix ($\pi\pi$ S-wave)
 + LASS ($K\pi$ S-wave)
 without non-resonant decay

2) Mixing and indirect CPV in $D^0 \rightarrow K_S^0 \pi^+ \pi^-$



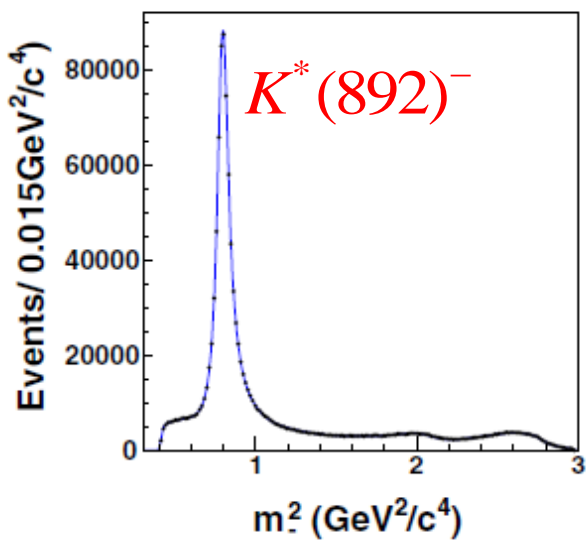
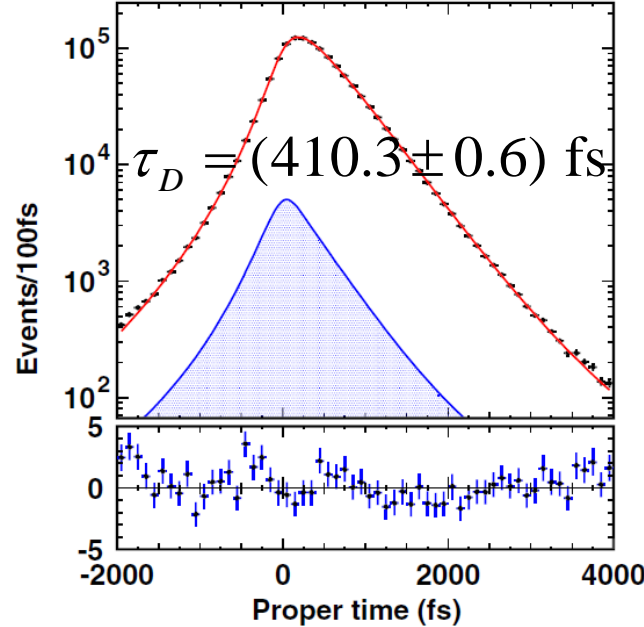
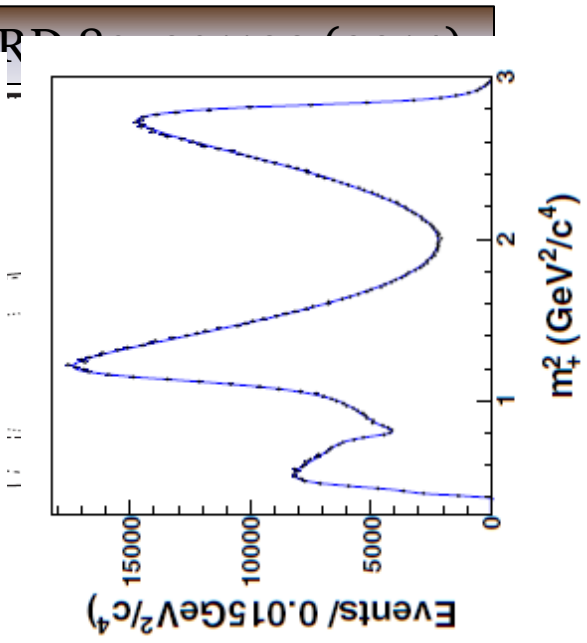
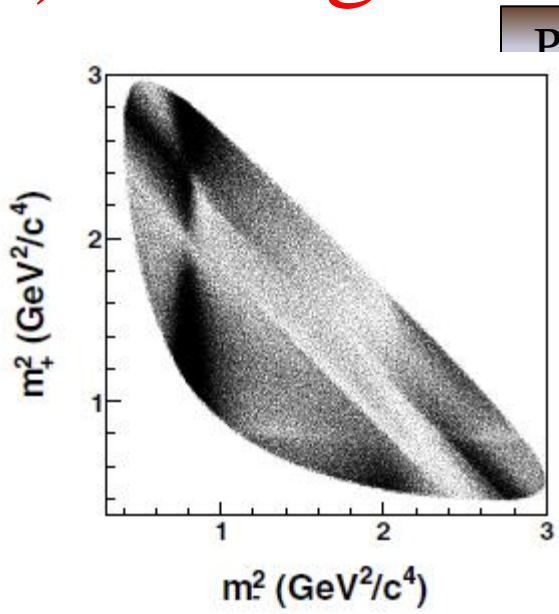
PRD 89, 091103 (2014)



Fit type	Parameter	Fit result
No CPV	$x(\%)$	$0.56 \pm 0.19^{+0.03+0.06}_{-0.09-0.09}$
	$y(\%)$	$0.30 \pm 0.15^{+0.04+0.03}_{-0.05-0.06}$
CPV	$x(\%)$	$0.56 \pm 0.19^{+0.04+0.06}_{-0.08-0.08}$
	$y(\%)$	$0.30 \pm 0.15^{+0.04+0.03}_{-0.05-0.07}$
[q/p]	$ q/p $	$0.90^{+0.16+0.05+0.06}_{-0.15-0.04-0.05}$
	$\arg(q/p)(^\circ)$	$15 \pm 11 \pm 3^{+3}_{-4}$

- best model found to be ;
- 12 relativistic Breit-Wigner's (P- and D-waves)
- + K-matrix ($\pi\pi$ S-wave)
- + LASS ($K\pi$ S-wave)
- without non-resonant decay

2) Mixing and indirect CPV in $D^0 \rightarrow K_S^0 \pi^+ \pi^-$



0.05 0.01 0.015

No CPV

CPV

1 fit

2 fit

Parameter	Fit result
$x(\%)$	$0.56 \pm 0.19^{+0.03+0.06}_{-0.09-0.09}$
$y(\%)$	$0.30 \pm 0.15^{+0.04+0.03}_{-0.05-0.06}$
$x(\%)$	$0.56 \pm 0.19^{+0.04+0.06}_{-0.08-0.08}$
$y(\%)$	$0.30 \pm 0.15^{+0.04+0.03}_{-0.05-0.07}$
$ q/p $	$0.90^{+0.16+0.05+0.06}_{-0.15-0.04-0.05}$
$\arg(q/p)(^\circ)$	$-6 \pm 11 \pm 3^{+3}_{-4}$

3) Time-integrated CPV in $D^0 \rightarrow \pi^0 \pi^0$

- $A_{CP}^{D^0 \rightarrow f} \equiv \frac{\Gamma(D^0 \rightarrow f) - \Gamma(\bar{D}^0 \rightarrow \bar{f})}{\Gamma(D^0 \rightarrow f) + \Gamma(\bar{D}^0 \rightarrow \bar{f})}$, Γ : partial decay width (also update CPV in $D^0 \rightarrow K_s^0 \pi^0$)

- $f \in \{\pi^0 \pi^0, K_s^0 \pi^0\}$: D^0 flavor from soft π in $D^{*+} \rightarrow D^0 \pi_s^+$ decay

- $A_{rec}^{D^{*+} \rightarrow D^0 \pi_s^+} = \frac{N_{rec}^{D^{*+} \rightarrow D^0 \pi_s^+} - N_{rec}^{D^{*-} \rightarrow D^0 \pi_s^-}}{N_{rec}^{D^{*+} \rightarrow D^0 \pi_s^+} + N_{rec}^{D^{*-} \rightarrow D^0 \pi_s^-}} \approx A_{CP}^{D^0 \rightarrow f} + A_{\varepsilon}^{\pi_s^+} + A_{prod}^{D^{*+}} (\because A_{\varepsilon}^{D^0} = 0)$

- $A_{CP}^{D \rightarrow f}$: CP asymmetry in $D \rightarrow f$

- $A_{\varepsilon}^{\pi_s^+}$: soft π detection asymmetry

- $A_{prod}^{D^{*+}}$: Forward-backward asymmetry, depending on $\cos \theta_{D^{*+}}^*$

3) Time-integrated CPV in $D^0 \rightarrow \pi^0 \pi^0$

• $A_{CP}^{D^0 \rightarrow f} \equiv \frac{\Gamma(D^0 \rightarrow f) - \Gamma(\bar{D}^0 \rightarrow \bar{f})}{\Gamma(D^0 \rightarrow f) + \Gamma(\bar{D}^0 \rightarrow \bar{f})}$, Γ : partial decay width (also update CPV in $D^0 \rightarrow K_S^0 \pi^0$)

• $f \in \{\pi^0 \pi^0, K_S^0 \pi^0\}$: D^0 flavor from soft π in $D^{*+} \rightarrow D^0 \pi_s^+$ decay

• $A_{rec}^{D^{*+} \rightarrow D^0 \pi_s^+} = \frac{N_{rec}^{D^{*+} \rightarrow D^0 \pi_s^+} - N_{rec}^{D^{*-} \rightarrow D^0 \pi_s^-}}{N_{rec}^{D^{*+} \rightarrow D^0 \pi_s^+} + N_{rec}^{D^{*-} \rightarrow D^0 \pi_s^-}} \approx A_{CP}^{D^0 \rightarrow f} + A_{\varepsilon}^{\pi_s^+} + A_{prod}^{D^{*+}} (\because A_{\varepsilon}^{D^0} = 0)$

, $A_{CP}^{D \rightarrow f}$: CP asymmetry in $D \rightarrow f$

, $A_{\varepsilon}^{\pi_s^+}$: soft π detection asymmetry use the correction in PRL 106, 211801 (2011)
from tagged and untagged $D^0 \rightarrow K^- \pi^+$ decays

, $A_{prod}^{D^{*+}}$: Forward-backward asymmetry, depending on $\cos \theta_{D^{*+}}^*$
decouple from $A_{CP}^{D^0 \rightarrow f}$ using antisymmetry of $A_{FB}^{D^{*+}}$ in $\cos \theta_{D^{*+}}^*$

3) Time-integrated CPV in $D^0 \rightarrow \pi^0 \pi^0$

- $A_{CP}^{D^0 \rightarrow f} \equiv \frac{\Gamma(D^0 \rightarrow f) - \Gamma(\bar{D}^0 \rightarrow \bar{f})}{\Gamma(D^0 \rightarrow f) + \Gamma(\bar{D}^0 \rightarrow \bar{f})}$, Γ : partial decay width (also update CPV in $D^0 \rightarrow K_S^0 \pi^0$)

- $f \in \{\pi^0 \pi^0, K_S^0 \pi^0\}$: D^0 flavor from soft π in $D^{*+} \rightarrow D^0 \pi_s^+$ decay

- $A_{rec}^{D^{*+} \rightarrow D^0 \pi_s^+} = \frac{N_{rec}^{D^{*+} \rightarrow D^0 \pi_s^+} - N_{rec}^{D^{*-} \rightarrow D^0 \pi_s^-}}{N_{rec}^{D^{*+} \rightarrow D^0 \pi_s^+} + N_{rec}^{D^{*-} \rightarrow D^0 \pi_s^-}} \approx A_{CP}^{D^0 \rightarrow f} + A_{\varepsilon}^{\pi_s^+} + A_{prod}^{D^{*+}} (\because A_{\varepsilon}^{D^0} = 0)$

- $A_{CP}^{D \rightarrow f}$: CP asymmetry in $D \rightarrow f$

- $A_{\varepsilon}^{\pi_s^+}$: soft π detection asymmetry use the correction in PRL 106, 211801 (2011)
from tagged and untagged $D^0 \rightarrow K^- \pi^+$ decays

- $A_{prod}^{D^{*+}}$: Forward-backward asymmetry, depending on $\cos \theta_{D^{*+}}^*$
decouple from $A_{CP}^{D^0 \rightarrow f}$ using antisymmetry of $A_{FB}^{D^{*+}}$ in $\cos \theta_{D^{*+}}^*$

- For $f = K_S^0 \pi^0$

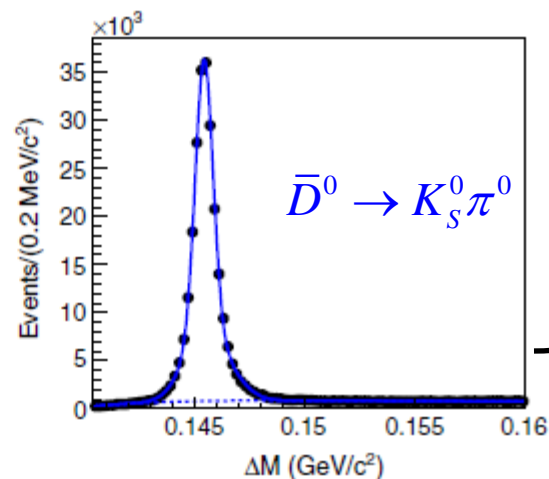
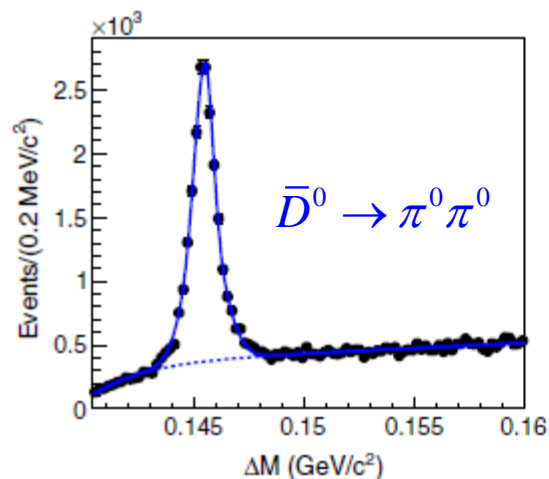
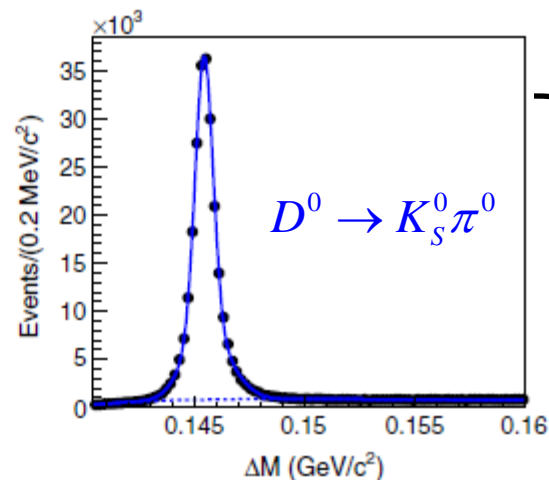
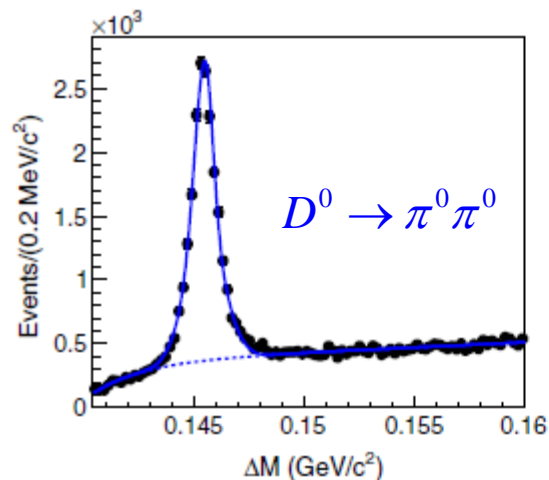
- $A_{\varepsilon}^{\bar{K}^0}$ ($\sigma(\bar{K}^0 N) \neq \sigma(K^0 N)$) according to PRD 84, 111501 (2011)

- $A_{CP}^{\bar{K}^0}$ (experiment dependent CPV in \bar{K}^0) according to JHEP, 04 (2012) 002

3) Time-integrated CPV in $D^0 \rightarrow \pi^0 \pi^0$

PRL 112, 211601 (2014)

(also update CPV in $D^0 \rightarrow K_S^0 \pi^0$)



34460 ± 273

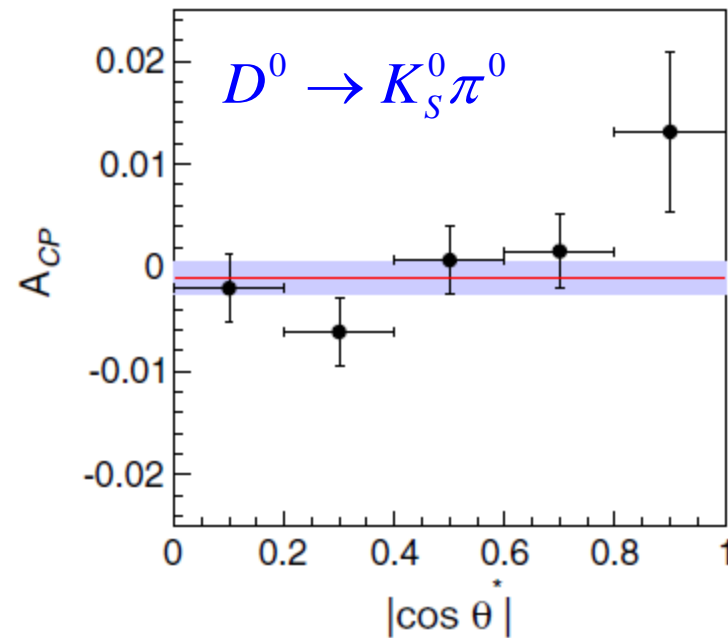
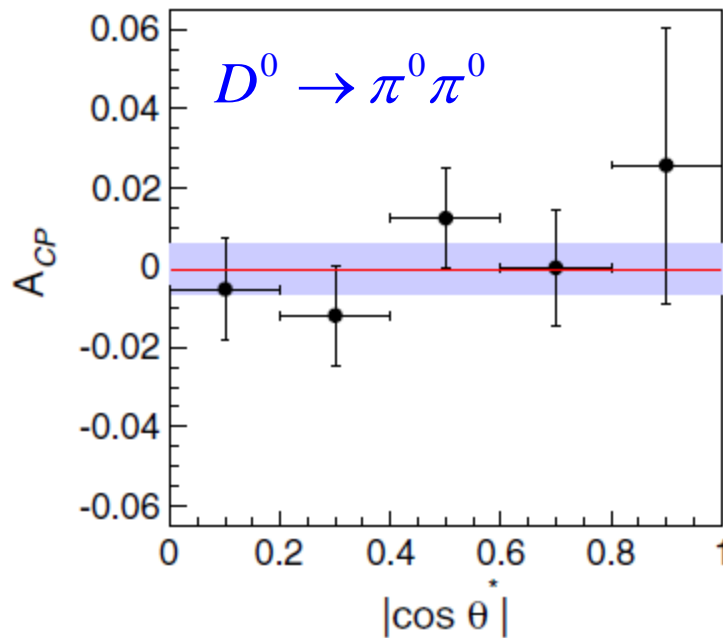
466814 ± 773

□ signal PDF: gaussian and asymmetric gaussian

3) Time-integrated CPV in $D^0 \rightarrow \pi^0 \pi^0$

PRL 112, 211601 (2014)

(also update CPV in $D^0 \rightarrow K_S^0 \pi^0$)



$$A_{CP}(D^0 \rightarrow \pi^0 \pi^0) = (-0.03 \pm 0.64 \pm 0.10)\%$$

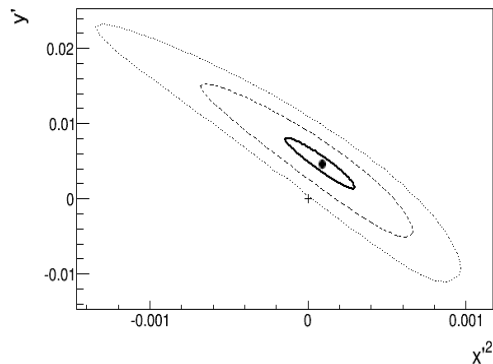
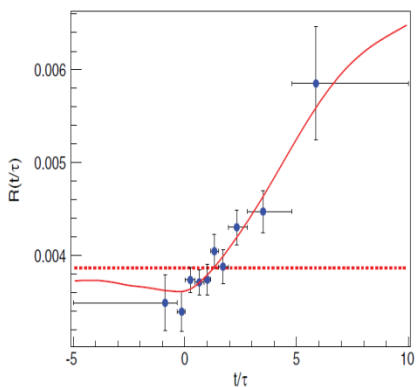
$$A_{CP}(D^0 \rightarrow K_S^0 \pi^0) = (-0.21 \pm 0.16 \pm 0.07)\%$$

- consistent with No CPV
- most precise measurements to date

Summary

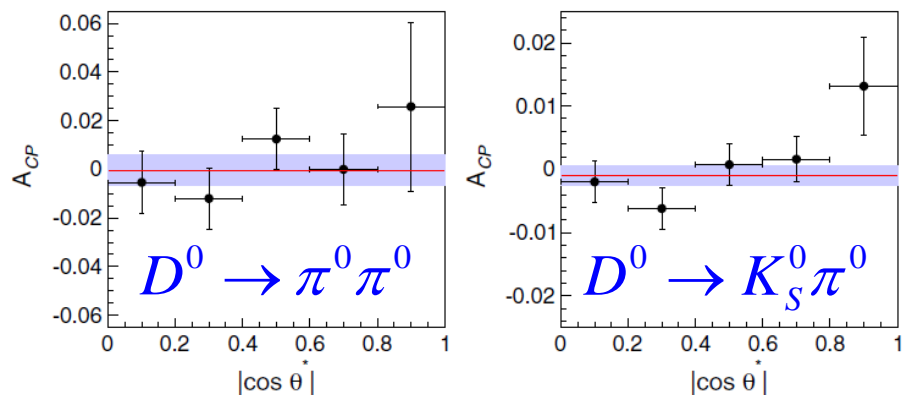
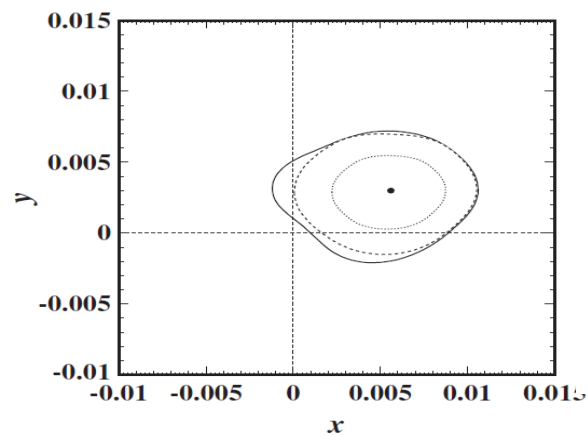
Charm CPV and Mixing at Belle

first observation
in e^+e^- collisions



most precise
in a single
experiment

$x(\%)$	$0.56 \pm 0.19^{+0.04+0.06}_{-0.08-0.08}$
$y(\%)$	$0.30 \pm 0.15^{+0.04+0.03}_{-0.05-0.07}$
$ q/p $	$0.90^{+0.16+0.05+0.06}_{-0.15-0.04-0.05}$
$\arg(q/p)(^\circ)$	$-6 \pm 11 \pm 3^{+3}_{-4}$



significantly improved

$$A_{CP} \text{ in } D^0 \rightarrow \pi^0 \pi^0$$

BACKUP

• $D^0 - \bar{D}^0$ Mixing

$$|D^0\rangle = \frac{1}{2p}(|D_1\rangle + |D_2\rangle)$$

$$|\bar{D}^0\rangle = \frac{1}{2q}(|D_1\rangle - |D_2\rangle)$$

$|D^0\rangle$ and $|\bar{D}^0\rangle$: flavor eigenstates, **physical observable**

$|D_1\rangle$ and $|D_2\rangle$: mass eigenstates, **finite masses and widths**

$p^2 + q^2 = 1$ under CPT symmetry

$p = q = 1/\sqrt{2}$ under CP symmetry

$$|D^0(t)\rangle = g_+(t)|D^0\rangle + \frac{q}{p}g_-(t)|\bar{D}^0\rangle$$

$$g_{\pm}(t) = \frac{1}{2}(e^{-i\lambda_1 t} \pm e^{-i\lambda_2 t}), \quad \lambda_i = m_i - \frac{i\Gamma_i}{2}$$

$$|\bar{D}^0(t)\rangle = g_+(t)|\bar{D}^0\rangle + \frac{p}{q}g_-(t)|D^0\rangle$$

m_i and Γ_i : D_i mass and width

$\Rightarrow D^0 - \bar{D}^0$ Mixing

described by **the mixing parameters**

$$x = \frac{m_1 - m_2}{\Gamma} \quad \text{and} \quad y = \frac{\Gamma_1 - \Gamma_2}{2\Gamma}, \quad \Gamma = \frac{\Gamma_1 + \Gamma_2}{2}$$

•CP Violation

□ partial decay widths

$$\Gamma(D^0(t) \rightarrow f) = \left| \langle f | H | D^0(t) \rangle \right|^2 \quad \langle f | H | D^0(t) \rangle = g_+(t) \langle f | H | D^0 \rangle + \frac{q}{p} g_-(t) \langle f | H | \bar{D}^0 \rangle$$

$$\Gamma(\bar{D}^0(t) \rightarrow \bar{f}) = \left| \langle \bar{f} | H | \bar{D}^0(t) \rangle \right|^2 \quad \langle \bar{f} | H | \bar{D}^0(t) \rangle = g_+(t) \langle \bar{f} | H | \bar{D}^0 \rangle + \frac{p}{q} g_-(t) \langle \bar{f} | H | D^0 \rangle$$

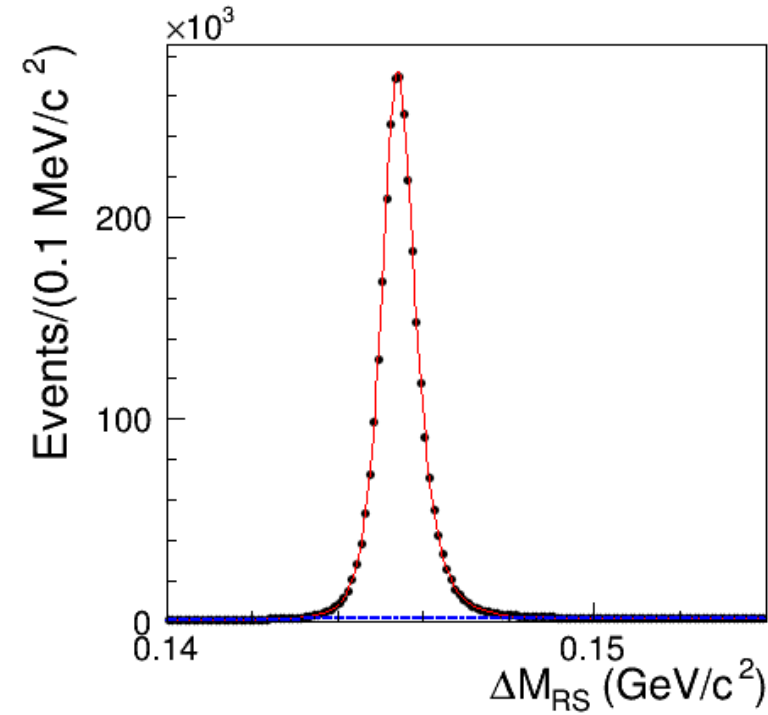
$$\square \Gamma(D^0(t) \rightarrow f) \neq \Gamma(\bar{D}^0(t) \rightarrow \bar{f}) \Rightarrow \text{CP Violation}$$

1) $\left| \langle f | H | D^0 \rangle / \langle \bar{f} | H | \bar{D}^0 \rangle \right| \neq 1$: different decay amplitudes

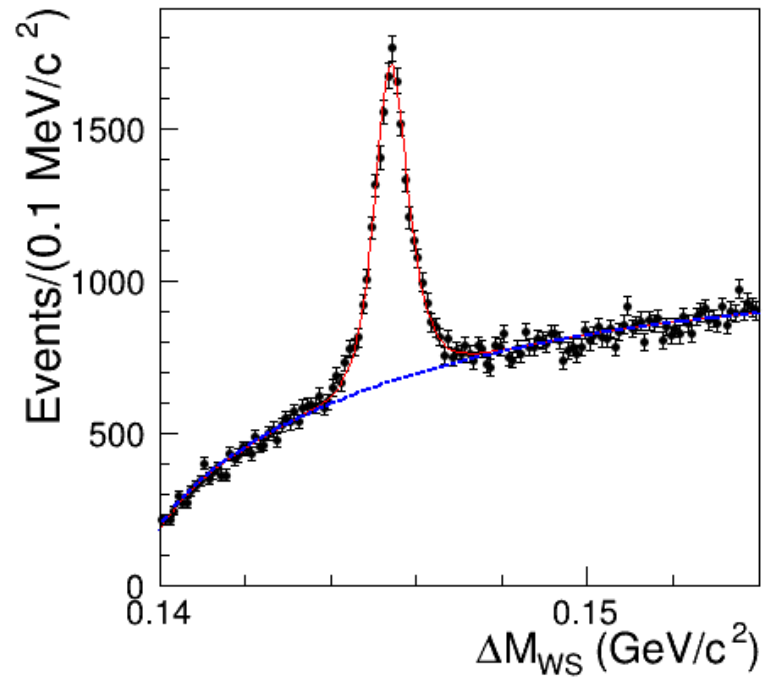
2) $|q/p| \neq 1$: different mixing rates

3) $\arg(q/p) \neq 0$: different interferences

Time-integrated results



nSIG (RS)



nSIG (WS)

data (976 fb⁻¹)

2980710 ± 1885

11478 ± 177

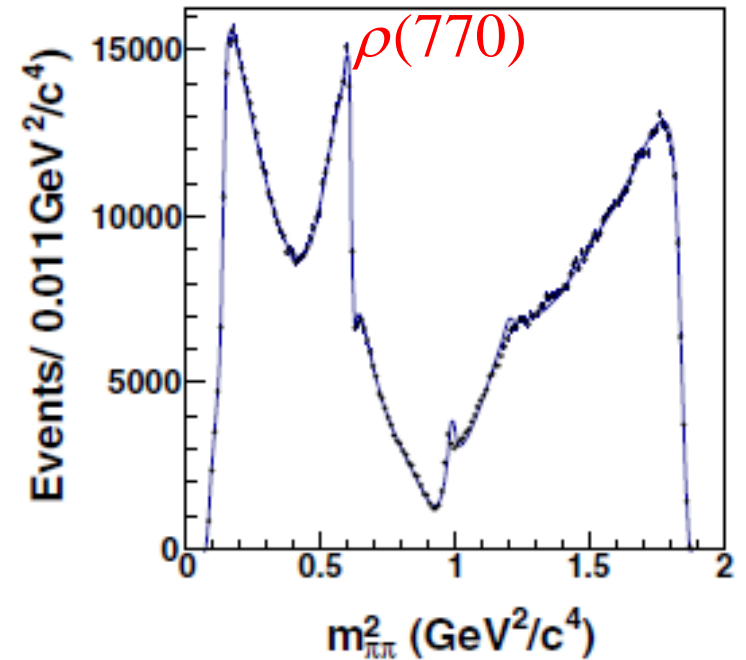
$$R_{WS} = (3.851 \pm 0.059) \times 10^{-3}$$

Resonance	Amplitude	Phase (deg)	Fit fraction
$K^*(892)^-$	1.590 ± 0.003	131.8 ± 0.2	0.6045
$K_0^*(1430)^-$	2.059 ± 0.010	-194.6 ± 1.7	0.0702
$K_2^*(1430)^-$	1.150 ± 0.009	-41.5 ± 0.4	0.0221
$K^*(1410)^-$	0.496 ± 0.011	83.4 ± 0.9	0.0026
$K^*(1680)^-$	1.556 ± 0.097	-83.2 ± 1.2	0.0016
$K^*(892)^+$	0.139 ± 0.002	-42.1 ± 0.7	0.0046
$K_0^*(1430)^+$	0.176 ± 0.007	-102.3 ± 2.1	0.0005
$K_2^*(1430)^+$	0.077 ± 0.007	-32.2 ± 4.7	0.0001
$K^*(1410)^+$	0.248 ± 0.010	-145.7 ± 2.9	0.0007
$K^*(1680)^+$	1.407 ± 0.053	86.1 ± 2.7	0.0013
$\rho(770)$	1 (fixed)	0 (fixed)	0.2000
$\omega(782)$	0.0370 ± 0.0004	114.9 ± 0.6	0.0057
$f_2(1270)$	1.300 ± 0.013	-31.6 ± 0.5	0.0141
$\rho(1450)$	0.532 ± 0.027	80.8 ± 2.1	0.0012

$\pi\pi$ S wave 0.1288

β_1	4.23 ± 0.02	164.0 ± 0.2
β_2	10.90 ± 0.02	15.6 ± 0.2
β_3	37.4 ± 0.3	3.3 ± 0.4
β_4	14.7 ± 0.1	-8.9 ± 0.3
f_{11}^{prod}	12.76 ± 0.05	-161.1 ± 0.3
f_{12}^{prod}	14.2 ± 0.2	-176.2 ± 0.6
f_{13}^{prod}	10.0 ± 0.5	-124.7 ± 2.1

$K\pi$ S wave	
M (MeV/ c^2)	1461.7 ± 0.8
Γ (MeV/ c^2)	268.3 ± 1.1
F	0.4524 ± 0.005
ϕ_F (rad)	0.248 ± 0.003
R	1(fixed)
ϕ_R (rad)	2.495 ± 0.009
a (GeV/ c^{-1})	0.172 ± 0.006
r (GeV/ c^{-1})	-20.6 ± 0.3
$K^*(892)$ Parameters	
$M_{K^*(892)}$ (MeV/ c^2)	893.68 ± 0.04
$\Gamma_{K^*(892)}$ (MeV/ c^2)	47.49 ± 0.06



Correlation coefficient

	x	y	$ q/p $	$\arg(q/p)$
x	1	0.054	-0.074	-0.031
y		1	0.034	-0.019
$ q/p $			1	0.044
$\arg(q/p)$				1

TABLE III. Summary of the contributions to experimental systematic uncertainty on the mixing and CPV parameters. The positive and negative errors are added in quadrature separately.

Source	No CPV		CPV			
	$\Delta x/10^{-4}$	$\Delta y/10^{-4}$	$\Delta x/10^{-4}$	$\Delta y/10^{-4}$	$ q/p /10^{-2}$	$\arg(q/p)/^\circ$
Best candidate selection	+1.0	+1.9	+1.3	+2.0	-2.3	+2.2
Signal and background yields	± 0.3	± 0.3	± 0.4	± 0.4	± 1.2	± 0.8
Fraction of wrong-tagged events	-0.7	-0.4	-0.5	+0.4	+1.1	+0.8
Time resolution of signal	-1.4	-0.9	-1.2	-0.8	+0.8	-1.2
Efficiency	-1.1	-2.1	-1.4	-2.2	+3.1	+1.3
Combinatorial PDF	+1.9 -4.8	+2.3 -3.9	+2.4 -4.1	+2.0 -4.4	+1.2 -2.9	+2.8 -2.3
$K^*(892)$ DCS/CF reduced by 5%	-7.3	+2.3	-6.9	+3.1	+3.3	-1.4
$K_2^*(1430)$ DCS/CF reduced by 5%	+1.7	-0.7	+2.2	-0.2	+1.1	+0.4
Total	+2.8 -8.9	+3.7 -4.6	+3.6 -8.3	+4.3 -5.1	+5.0 -4.0	+3.3 -3.0

TABLE IV. Summary of contributions to the modeling systematic uncertainty on the mixing and CPV parameters. The positive and negative errors are added in quadrature separately.

Source	No CPV		CPV			
	$\Delta x/10^{-4}$	$\Delta y/10^{-4}$	$\Delta x/10^{-4}$	$\Delta y/10^{-4}$	$ q/p /10^{-2}$	$\arg(q/p)/^\circ$
Resonance M & Γ	± 1.4	± 1.2	± 1.2	± 1.3	± 2.1	± 1.0
$K^*(1680)^+$ removal	-1.8	-3.0	-2.2	-2.8	+2.1	-1.2
$K^*(1410)^\pm$ removal	-1.2	-3.6	-1.7	-3.9	-1.3	+1.4
$\rho(1450)$ removal	+2.1	+0.3	+2.1	+0.5	-1.9	+0.9
Form factors	+4.0	+2.4	+4.3	+2.0	-2.4	-1.0
$\Gamma(q^2) = \text{constant}$	+3.3	-1.6	+4.1	-2.3	-1.6	+1.3
Angular dependence	-8.5	-3.9	-7.4	-3.6	+5.6	-3.2
K -matrix formalism	-2.2	+1.8	-3.5	+2.4	-3.6	+1.1
Total	+5.8 -9.1	+3.2 -6.4	+6.4 -8.4	+3.4 -6.9	+6.4 -5.1	+2.5 -3.7

- Obtaining A_{ε}^f from CPV free resonance data : depends on f
- Assume the same A_{FB} for all charmed mesons

◦ soft charged π : $D^{*+} \rightarrow D^0 \pi_s^+ \rightarrow K^- \pi^+ \pi_s^+$ and $D^0 \rightarrow K^- \pi^+$

$$* A_{CP}^{D \rightarrow f} = \left\{ A_{rec}^{D \rightarrow f_{corr}} (\cos \theta_D^*) + A_{rec}^{D \rightarrow f_{corr}} (-\cos \theta_D^*) \right\} / 2$$

$$* A_{FB}^D = \left\{ A_{rec}^{D \rightarrow f_{corr}} (\cos \theta_D^*) - A_{rec}^{D \rightarrow f_{corr}} (-\cos \theta_D^*) \right\} / 2$$