

# Charm spectroscopy at LHCb

**BEACH 2014 Birmingham**

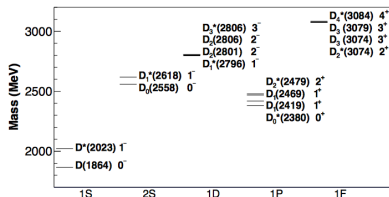
Stephen Ogilvy  
on behalf of the LHCb collaboration

University of Glasgow

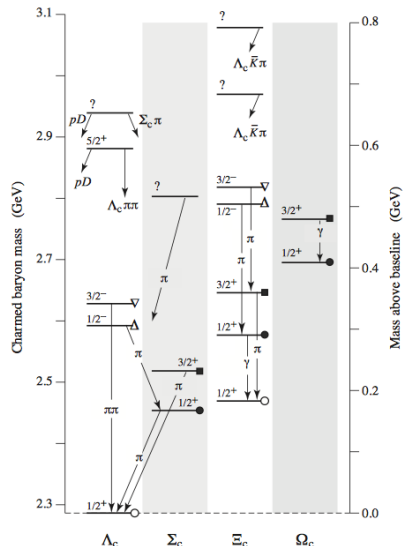


# Outline

- Quark model has enjoyed significant success in predicting charm spectra.
- Many charm states have been recently identified at various experiments.
  - But still many not found!
- And still some interesting tensions between theory and experiment.
- Today will present some LHCb results in the field.



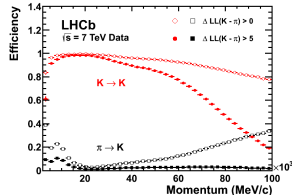
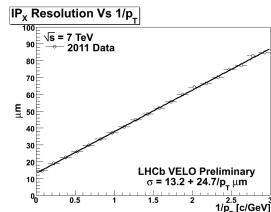
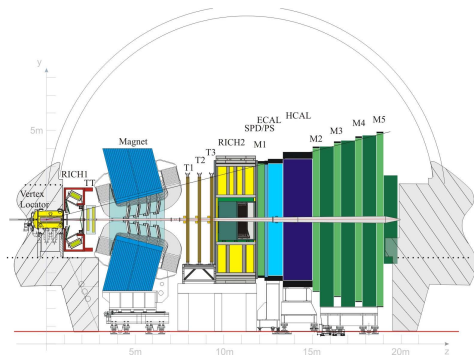
Meson  $c\bar{u}$  spectra - Phys. Rev. D32 (1985) 189



Baryon Spectra - Phys. Rev. D86, 010001 (2012)

# The LHCb Detector

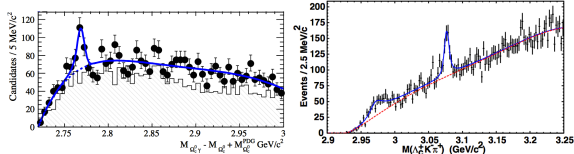
- Forward arm spectrometer designed for precision flavour measurements



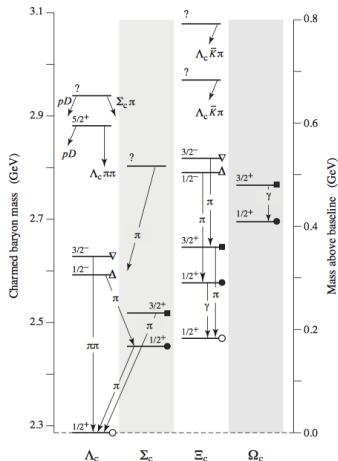
- VELO - powerful secondary vertex discrimination to trigger on heavy flavour decays
- Tracker momentum resolution:  $\Delta p/p = 0.4 \%$  at  $5 \text{ GeV}/c$  to  $0.6 \%$  at  $100 \text{ GeV}/c$
- RICH - daughter particle discrimination:  
Kaon ID efficiency  $\sim 95 \%$  for  $\sim 5 \%$   $\pi \rightarrow K$  mis-id probability

# Charm baryon overview

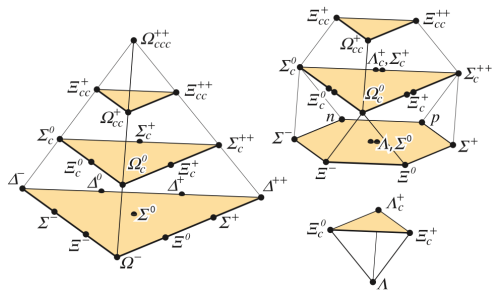
- Considerable progress in past 10 years on measuring charm baryon spectra.
- Variety of  $\Sigma_c$ ,  $\Omega_c$  and  $\Xi_c$  states identified by the B factories.
- Quark model has been very successful in predicting masses of singly charmed states, and mass splittings.
- One of the more interesting sagas in spectroscopy is the case of doubly-charmed production, and in searches for the  $\Xi_{cc}^{+}/++$ .



$\Omega_c(2770)^0$  at BaBar - Phys. Rev. Lett.  $\Xi_c(2980)$  and  $\Xi_c(3077)$  at BELLE - Phys. Rev. Lett. 97, 162001



Baryon Spectra - Phys. Rev. D86, 010001 (2012)

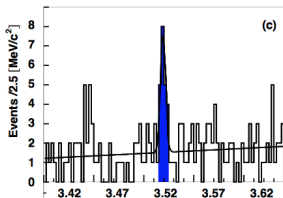


Phys. Rev. D86, 010001 (2012)

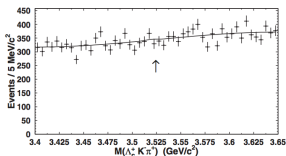
- Baryons with u,d,s,c form SU(4) multiplets
- Ground state baryons shown
- Three weakly decaying  $C = 2, J^P = 1/2^+$  states:
  - $\Xi_{cc}$  isodoublet ( $ccu, ccd$ )
  - $\Omega_{cc}$  singlet ( $ccs$ )

- Numerous predictions for  $\Xi_{cc}^{+}/^{++}$  masses and lifetimes:
  - $m(\Xi_{cc}^{+}/^{++})$ : 3500 – 3700 MeV/c<sup>2</sup> - Phys. Rev. D70 (2004) 094004
  - $\tau(\Xi_{cc}^{+}/^{++})$ : 100 – 250 fs - Eur. Phys. J. A45 (2010) 267
  - Production relative to  $\Lambda_c^+$  generally expected to be highly suppressed - e.g. Physics-Uspekhi 45 (2002), no. 5 455

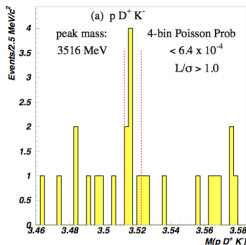
- SELEX reported signals in  $\Lambda_c^+ K^- \pi^+$  and  $p^+ D^+ K^-$  final states
  - $m(\Xi_{cc}^{+}/\Xi_{cc}^{++})$ :  $(3519 \pm 2)$  MeV/ $c^2$ ,  $\tau(\Xi_{cc}^{+}/\Xi_{cc}^{++})$ :  $< 30$  fs @ 90 % CL
  - SELEX calculate 20 % of their  $\Lambda_c$  produced in  $\Xi_{cc}^{+}/\Xi_{cc}^{++}$  decays



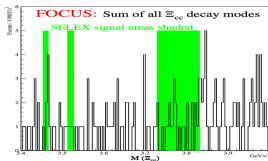
SELEX - Phys.Rev.Lett.89:112001



BELLE - PhysRevLett.97.162001

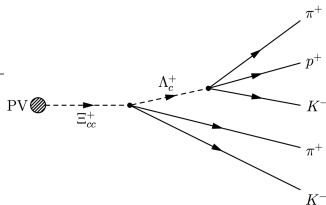


SELEX - Phys.Lett.B628:18-24



FOCUS - NuclPhysB 115:33-36

- Search for particle in decay  $\Xi_{cc}^+ \rightarrow \Lambda_c^+(pK^-\pi^+)K^-\pi^+$
- Using  $0.65 \text{ fb}^{-1}$  of 2011 data at  $\sqrt{s} = 7 \text{ TeV}$
- Measure production ratio relative to control channel  $\Lambda_c^+ \rightarrow pK^-\pi^+$ :



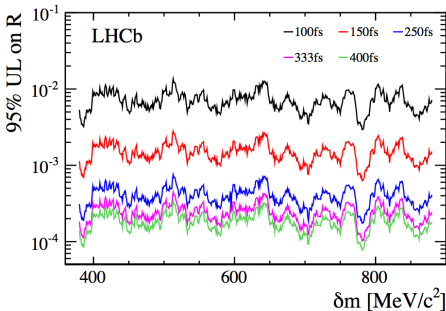
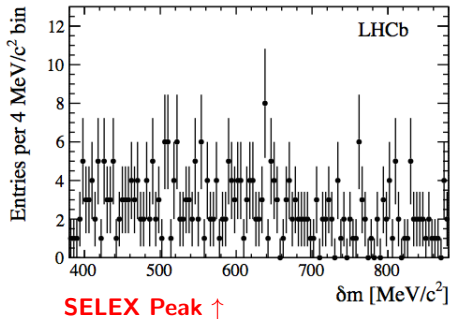
$$R \equiv \frac{\sigma(\Xi_{cc}^+) \mathcal{B}(\Xi_{cc}^+ \rightarrow \Lambda_c^+ K^- \pi^+)}{\sigma(\Lambda_c^+)} = \frac{N_{\text{signal}}}{N_{\text{control}}} \frac{\epsilon_{\text{control}}}{\epsilon_{\text{signal}}}$$

- Measured LHCb  $\Lambda_c$  cross-section at  $\sqrt{s} = 7 \text{ TeV} \approx 230 \text{ } \mu\text{b}$   
NUCL.PHYS.B871,1-20
- Predicted LHC  $\Xi_{cc}^{+/++}$  cross-section at  $\sqrt{s} = 7 \text{ TeV} \approx (30 - 900) \text{ nb}$ .
- Assume  $\mathcal{B}(\Xi_{cc}^+ \rightarrow \Lambda_c^+ K^- \pi^+) \approx \mathcal{B}(\Lambda_c^+ \rightarrow p^+ K^- \pi^+) \approx 5 \%$ 
  - expected value of  $R$  at LHCb is of order  $10^{-5} - 10^{-4}$

- Define:

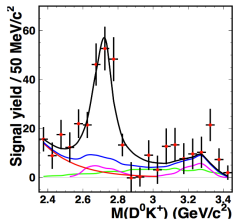
$$\delta m \equiv m(\Lambda_c^+ K^- \pi^+) - m_{meas}(\Lambda_c^+) - m(K^-) - m(\pi^+)$$

- Perform 2D fit in  $m(\Lambda_c)$  and  $\delta m$  to extract signal yields.
- No observed excess in  $\delta m$  spectrum in data.
- Calculate 95%  $CL_s$  ULs of  $R$  as function of  $\delta m$  for variety of lifetime hypotheses.

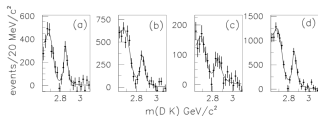


- 2011 analysis a strong proof of concept
- Prospects for 2011+2012 dataset look bright
- Full  $2.08 \text{ fb}^{-1}$  at  $\sqrt{s} = 8 \text{ TeV}$  available for analysis
- $\Lambda_c^+ \rightarrow pK^-\pi^+$  trigger and selection performance improved for 2012
- Now searching for  $\Xi_{cc}^{+}/^{++}$  in multiple final states
  - Notable inclusion:  $\Xi_{cc}^+ \rightarrow (D^+ \rightarrow K^-\pi^+\pi^+)p^+K^-$ .
  - High  $D^+$  lifetime (1 ps) vs.  $\Lambda_c^+$  (0.2 ps) - more efficient selections
- Updated analysis will have far greater sensitivity.

# Charm meson overview

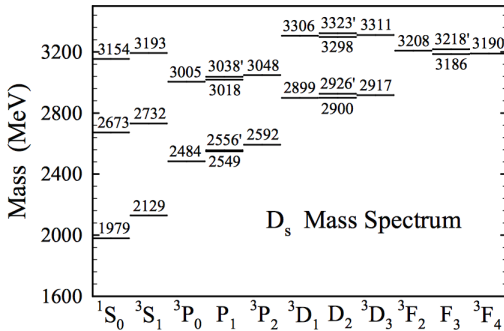


$D_{sJ}(2700)^+$  at Belle - Phys. Rev. Lett. 100, 092001



$D_{sJ}(2860)^+$  at BaBar - Phys Rev Lett. 1;97(22):222001

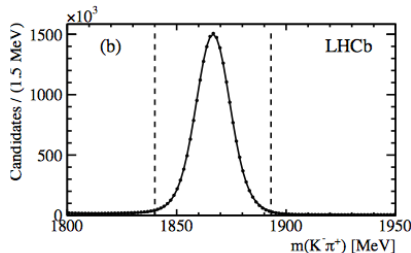
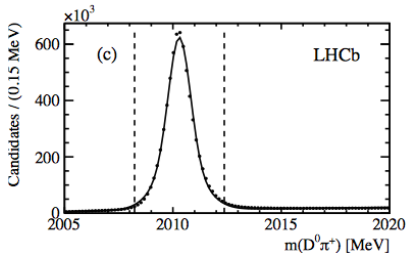
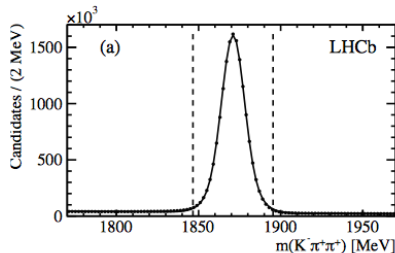
- Along with baryons, much recent progress in identifying charmed mesons.
- However, still many states missing which were predicted in 1980s.
- And some interesting tensions between theory and experiment - e.g. masses of  $D_{sJ}^*(2317)^+$  and  $D_{sJ}(2460)^+$  significantly lower than theory predictions.



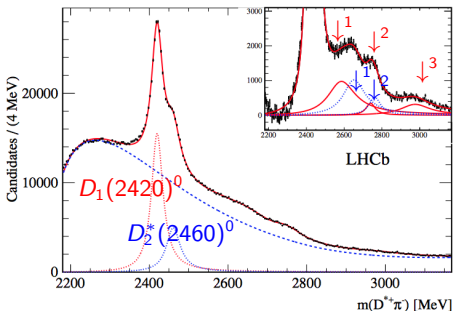
Predicted  $c\bar{s}$  spectra - Phys. Rev. D 89, 074023

# Charm meson spectroscopy at LHCb

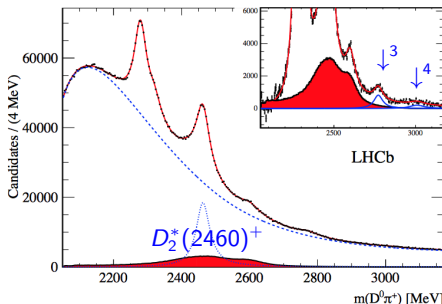
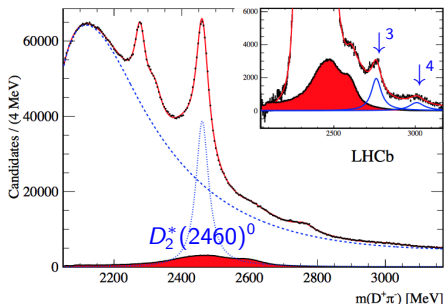
- Today present LHCb searches in the  $c\bar{u}$  and  $c\bar{s}$  meson spectra:
- Clean  $D$  reconstruction at LHCb.
- Candidates in  $D_J$  analysis:
  - $15.1 \times 10^6 D^+$
  - $20.4 \times 10^6 D^0$
  - $6.4 \times 10^6 D^{*+}$



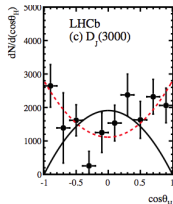
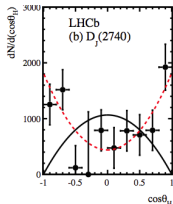
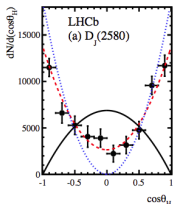
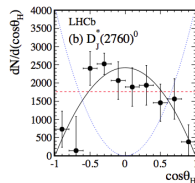
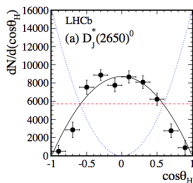
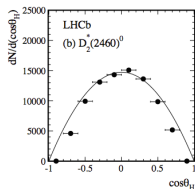
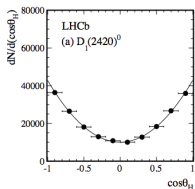
- Following on observations of a variety of excited charm mesons by BaBar (Phys. Rev. D82 111101), search in the final states:
  - $p\bar{p} \rightarrow D^+ \pi^- X$ ,  $p\bar{p} \rightarrow D^0 \pi^+ X$ ,  $p\bar{p} \rightarrow D^{*+} \pi^- X$ .
- Search uses full 2011 dataset:  $1.0 \text{ fb}^{-1}$  at  $\sqrt{s} = 7 \text{ TeV}$ .
- $D$  selections uses a variety of fiducial and kinematic cuts to increase purity.
- PID discrimination used to mitigate cross-feed.
- Aim to confirm previously observed states, and use high charms statistics at LHCb to search for new ones.



- $\downarrow^1 - D_J(2580)^0$ ,  $\downarrow^2 - D_J(2740)^0$ ,  
 $\downarrow^3 - D_J(3000)^0$
- $\downarrow^1 - D_J^*(2650)^0$ ,  $\downarrow^2 - D_J^*(2760)^0$
- $\downarrow^3 - D_J^*(2760)^+$ ,  $\downarrow^4 - D_J^*(3000)^+$

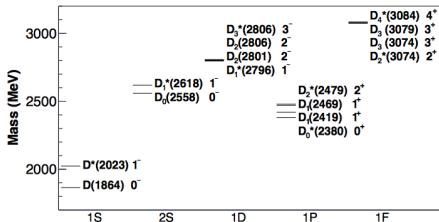


- Measure yields of each state as a function of helicity angle  $\cos \theta_H$ .
  - angle between the bachelor  $\pi^-$  and  $\pi^+$  from  $D^{*+}$  decay in the rest frame of the  $D^{*+} \pi^-$  rest frame.
- Tests for natural ( $J^P = 1^-, 2^+, 3^- \dots$ ) and unnatural ( $J^P = 1^+, 2^-, 3^+ \dots$ ) parity.
- Natural parity states:  $\frac{dN}{d \cos \theta_H} \propto \sin^2 \theta_H$ , unnatural parity  $\frac{dN}{d \cos \theta_H} \propto 1 + h \cos^2 \theta_H$

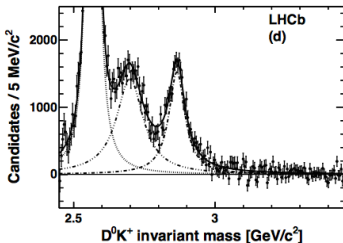
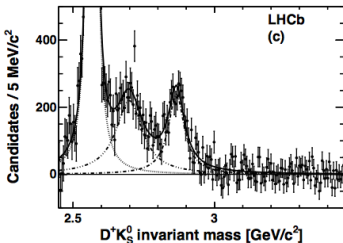
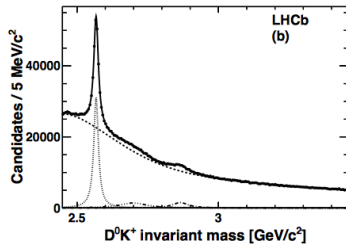
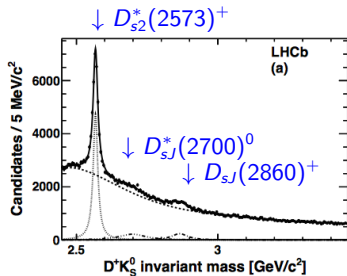


- Number of charm states identified in the final states  $p\bar{p} \rightarrow D^+ \pi^- X$ ,  $p\bar{p} \rightarrow D^0 \pi^+ X$ ,  $p\bar{p} \rightarrow D^{*+} \pi^- X$ .
  - Observe  $D_1(2420)^0$  in  $D^{*+} \pi^-$  final state,  $D_2^*(2460)$  resonance in  $D^+ \pi^-$ ,  $D^0 \pi^+$  and  $D^{*+} \pi^-$  final states - spin-parity assignments confirmed.
  - Observe two natural parity resonances -  $D_J^*(2650)^0$  and  $D_J^*(2760)^0$ .
  - Observe two unnatural parity resonances -  $D_J(2580)^0$  and  $D_J(2740)^0$ .
  - Observe further structure in  $D^{*+} \pi^-$  final state -  $D_J(3000)^0$  compatible with natural parity.
  - Also observe several structures in  $D^+ \pi^-$  and  $D^0 \pi^+$  final states -  $D_J^*(3000)^0$  and  $D_J^*(3000)^+$  - possible result of superposition of several 1F states.
- Identifications suggested by us and by the theory community - e.g. Phys.Rev.D88 (2013) 114003.

- $D_J^*(2650)^0$ :  $J^P = 1^-$ , 2S  $D_1^*(2618)$
- $D_J^*(2760)^+$ :  $J^P = 1^-$ , 1D  $D_1^*(2796)$
- $D_J(2740)^0$ :  $J^P = 2^-$ , 1D  $D_2(2801)$



- Current state of  $c\bar{s}$  spectroscopy - two S-wave and four P-wave states.
- Some tension with  $D_{sJ}^*(2317)^+$  and  $D_{sJ}(2460)^+$  states - found at higher masses than theory predicts.
- Among the observed high mass  $D_{sJ}$  structures, none currently reported in PDG tables.
- LHCb conducted analysis to help confirm existence of these states and to measure their parameters.
- Look for resonances in the final states:
  - $D^+ (K^- \pi^+ \pi^+) K_S^0 (\pi^+ \pi^-)$
  - $D^0 (K^- \pi^+) K^+$
- Again, full 2011 dataset used:  $1.0 \text{ fb}^{-1}$  at  $\sqrt{s} = 7 \text{ TeV}$ .



- Extracted yields:

Decay mode	$D_{s1}^*(2700)^+$	$D_{sJ}^*(2860)^+$
$D^+ K_S^0$	$6\,724 \pm 596$	$4\,825 \pm 347$
$D^0 K^+$	$45\,315 \pm 2\,186$	$31\,603 \pm 1\,257$

- Final extracted mass and width parameters:

$$\begin{aligned}m(D_{s1}^*(2700)^+) &= 2709.2 \pm 1.9(\text{stat}) \pm 4.5(\text{syst}) \text{ MeV}/c^2, \\ \Gamma(D_{s1}^*(2700)^+) &= 115.8 \pm 7.3(\text{stat}) \pm 12.1(\text{syst}) \text{ MeV}/c^2, \\ m(D_{sJ}^*(2860)^+) &= 2866.1 \pm 1.0(\text{stat}) \pm 6.3(\text{syst}) \text{ MeV}/c^2, \\ \Gamma(D_{sJ}^*(2860)^+) &= 69.9 \pm 3.2(\text{stat}) \pm 6.6(\text{syst}) \text{ MeV}/c^2.\end{aligned}$$

- All parameters agree with previous BaBar measurement, with factor 2 improvement in statistical sensitivity.
- Systematics remain dominant.
- Need decays from  $B_s$  to definitively assign spin-parity.
- Now have just this!

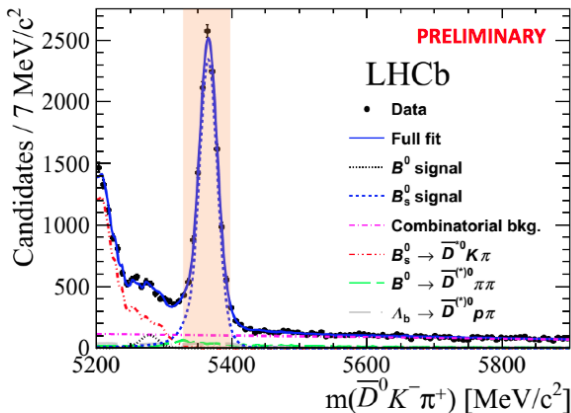
# Analysis overview

- Analysis of the resonance structure of  $B_s \rightarrow \bar{D}^0 K^- \pi^+$ 
  - **New results!**
  - Perform fit using Laura++ package – <http://laura.hepforge.org/>
  - Use candidates with  $\bar{D}^0 \rightarrow K^+ \pi^-$  from  $3\text{fb}^{-1}$  of LHCb data

**LHCb-PAPER-2014-035, LHCb-PAPER-2014-036**  
(to be submitted to PRL and PRD)
- Branching fractions of  $B_s^0 \rightarrow \bar{D}^0 K^- \pi^+$  and  $B^0 \rightarrow \bar{D}^0 K^+ \pi^-$  have been measured as  $(1.00 \pm 0.14) \times 10^{-3}$  and  $(9.0 \pm 1.3) \times 10^{-5}$  respectively
  - Uncertainties dominated by the uncertainty on the normalisation channel

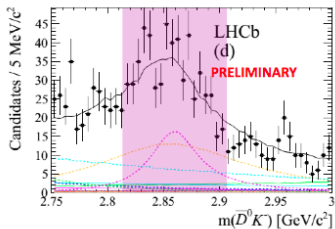
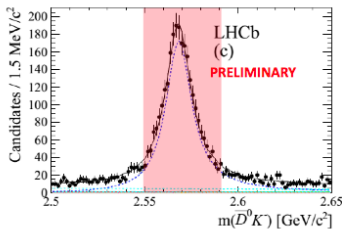
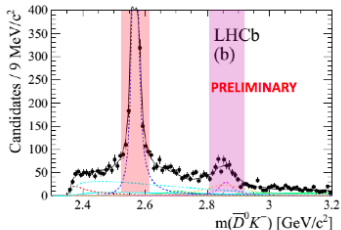
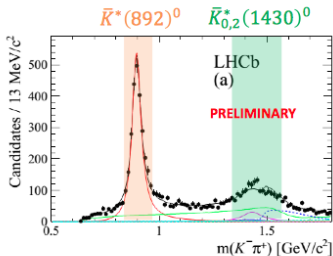
**Phys. Rev. D 87, 112009 (2013)**

# Fit to $B$ mass



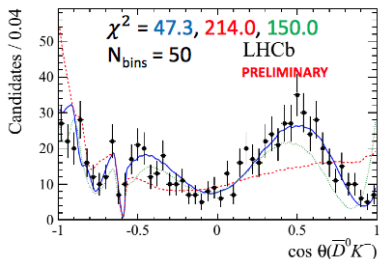
Fit to  $DK\pi$  mass distribution from  $3\text{fb}^{-1}$  of data showing the signal region ( $\pm 2.5\sigma$ ).  
 $\sim 11,000$  signal decays, 87% pure in the nominal signal window. Backgrounds due to combinatorial background (7.3%),  $B^0 \rightarrow D^{(*)0}\pi\pi$  (2.8%) and  $\Lambda_b \rightarrow D^{(*)0}p\pi$  (2.3%)

# Dalitz plot fit


 $D_{s2}^*(2573)^-$ 
 $D_{sJ}^*(2860)^-$

# $D_{SJ}^*(2860)^-$ states

- Various spin hypotheses tested for the  $m_{DK} \approx 2.86 \text{ GeV}/c^2$  region
- Spin-1 + spin-3 hypothesis offers best description of the data
- Spin-3 and spin-1 only hypotheses give poor descriptions of the DK helicity angle in the  $2.86 \text{ GeV}/c^2$  region



PRELIMINARY

Spin hypothesis	$\Delta\text{NLL}$	$\sqrt{2\Delta\text{NLL}}$	Masses and widths			
1+3	0	—				
0	141.0	16.8	2862	57		
0+1	113.2	15.0	2446	250*	2855	96
0+2	155.1	17.6	2870	61	2569	17*
0+3	105.1	14.5	2415	188*	2860	52
1	156.8	17.7	2866	92		
1+2	138.6	16.6	2851	99	3134	174*
2	287.9	24.0	3243	81*		
2	365.5	27.0	2569	17*		
2+3	131.2	16.2	2878	12	2860	56
3	136.5	16.5	2860	57		

 \* Indicates states that floated out of the  $2.86 \text{ GeV}/c^2$  region

# $D_{sJ}$ spectroscopy summary

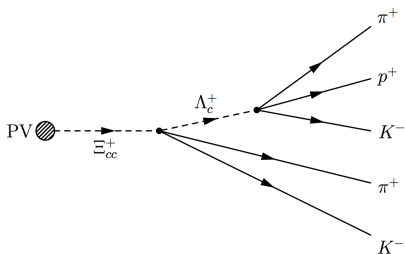
- $D_{sJ}^*(2700)^0$  and  $D_{sJ}(2860)^+$  resonances first observed by BaBar confirmed by LHCb.
- Precision on masses and decay widths are markedly improved.
- First time states observed in a hadronic environment.
- Angular analysis of  $B_s^0 \rightarrow \bar{D}K^- \pi^+$  decays have shown definitively that the  $D_{sJ}(2860)^+$  is composed of two resonances:
  - $D_{s1}^*(2860)^-$  and  $D_{s3}^*(2860)^-$ , required at greater than  $10 \sigma$  significance!
  - First observation of heavy-flavoured spin-3 state!

# Charm spectroscopy summary

- Charm spectroscopy remains an active area, with lots to still find and a few interesting tensions along the way.
- LHCb making contributions to knowledge of both charm mesons and baryons.
- Presented results of:
  - JHEP1312(2013)090 -  $\Xi_{cc}^{+}/^{++}$  search, placing upper limits on hadronic production relative to  $\Lambda_c^+$ .
  - JHEP09(2013)145 -  $D_J$  spectroscopy, identifying several new states and confirming parity assignments.
  - JHEP10(2012)151 -  $D_{sJ}$  spectroscopy, confirming the existence of the  $D_J^*(2760)^0$  and  $D_{sJ}(2860)^+$  states.
  - LHCb-PAPER-2014-035 - discovery of two  $D_{sJ}$  resonances in  $D_{sJ}(2860)^-$  structure: the  $D_{s1}^*(2860)^-$  and  $D_{s3}^*(2860)^-$ .
- Very active charm working group at LHCb carrying out a very wide variety of measurements.
- Expect more spectroscopy from us soon!

# BACKUP

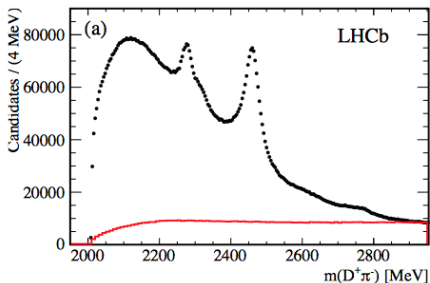
- Use same trigger requirements for control and signal based on  $\Lambda_c^+ \rightarrow pK^-\pi^+$  decay
  - One  $\Lambda_c$  daughter track must fire calorimeter hardware trigger
  - One  $\Lambda_c$  daughter track selected by inclusive software trigger
  - $\Lambda_c$  candidate reconstructed and accepted by dedicated  $\Lambda_c^+ \rightarrow pK^-\pi^+$  selection algorithm in software trigger - geometric and kinematic requirements, and using RICH PID info for proton.
- Offline reconstruction and selection based on PV displacement and particle identification requirements



- To make  $\Xi_{cc}^{+}/^{++}$  candidates:
  - Pair  $\Lambda_c$  with  $K$  and  $\pi$  at common vertex displaced from PV
  - Displacement cut reduces sensitivity to SELEX-like  $\Xi_{cc}^{+}/^{++}$   
Can be relaxed in future analyses
  - Artificial Neural Network final selection. Input variables chosen for minimal  $\Xi_{cc}^{+}/^{++}$  lifetime dependence

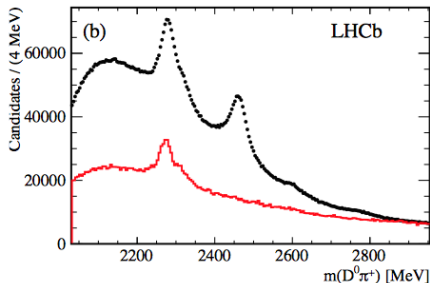
# $D_J$ meson decays - $D^+ \pi^-$ mass spectra

- Observed  $D^+ \pi^-$  mass spectra and wrong-mass spectra (red) shown.
  - Double peak structure at  $2300 \text{ MeV}/c^2$  from  $D_1(2420)^0$  and  $D_2^*(2460)^0$  cross feed when neutrals/photons not reconstructed.
  - Strong  $D_2^*(2460)^0$  signal, weak structures at  $2600 \text{ MeV}/c^2$  and  $2750 \text{ MeV}/c^2$ .
  - No structure in WM distribution.



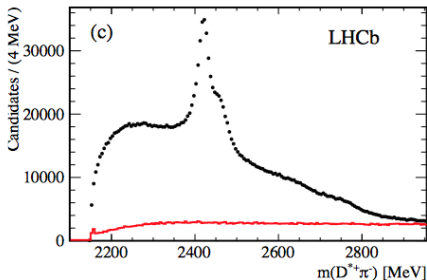
# $D_J$ meson decays - $D^0 \pi^+$ mass spectra

- Observed  $D^0 \pi^+$  mass spectra and wrong-mass spectra (red) shown.
  - Double peak structure at  $2300 \text{ MeV}/c^2$  from  $D_1(2420)^0$  and  $D_2^*(2460)^0$  cross feed when neutrals/photons not reconstructed.
  - Strong  $D_2^*(2460)^+$  signal, weak structures at  $2600 \text{ MeV}/c^2$  and  $2750 \text{ MeV}/c^2$ .
  - Structure in WM distribution at  $2300 \text{ /mevcc}$  due to cross feed from  $D_1(2420)^+ / D_2^*(2460)^+ \rightarrow \pi^- D^{*+} (D^0 \pi^+)$



# $D_J$ meson decays - $D^{*+} \pi^-$ mass spectra

- Observed  $D^{*+} \pi^-$  mass spectra and wrong-mass spectra (red) shown.
  - Dominated by  $D_1(2420)^0$  and  $D_2^*(2460)^0$  signals.
  - Structures evident in high mass region.
  - No WM structure.



Resonance	Final state	Mass (MeV)			Width (MeV)			Yields $\times 10^3$	Significance ( $\sigma$ )
$D_1(2420)^0$	$D^{*+}\pi^-$	2419.6 $\pm$ 0.1 $\pm$ 0.7			35.2 $\pm$ 0.4 $\pm$ 0.9			210.2 $\pm$ 1.9 $\pm$ 0.7	
$D_2^*(2460)^0$	$D^{*+}\pi^-$	2460.4 $\pm$ 0.4 $\pm$ 1.2			43.2 $\pm$ 1.2 $\pm$ 3.0			81.9 $\pm$ 1.2 $\pm$ 0.9	
$D_J^*(2650)^0$	$D^{*+}\pi^-$	2649.2 $\pm$ 3.5 $\pm$ 3.5			140.2 $\pm$ 17.1 $\pm$ 18.6			50.7 $\pm$ 2.2 $\pm$ 2.3	24.5
$D_J^*(2760)^0$	$D^{*+}\pi^-$	2761.1 $\pm$ 5.1 $\pm$ 6.5			74.4 $\pm$ 3.4 $\pm$ 37.0			14.4 $\pm$ 1.7 $\pm$ 1.7	10.2
$D_J(2580)^0$	$D^{*+}\pi^-$	2579.5 $\pm$ 3.4 $\pm$ 5.5			177.5 $\pm$ 17.8 $\pm$ 46.0			60.3 $\pm$ 3.1 $\pm$ 3.4	18.8
$D_J(2740)^0$	$D^{*+}\pi^-$	2737.0 $\pm$ 3.5 $\pm$ 11.2			73.2 $\pm$ 13.4 $\pm$ 25.0			7.7 $\pm$ 1.1 $\pm$ 1.2	7.2
$D_J(3000)^0$	$D^{*+}\pi^-$	2971.8 $\pm$ 8.7			188.1 $\pm$ 44.8			9.5 $\pm$ 1.1	9.0
$D_2^*(2460)^0$	$D^+\pi^-$	2460.4 $\pm$ 0.1 $\pm$ 0.1			45.6 $\pm$ 0.4 $\pm$ 1.1			675.0 $\pm$ 9.0 $\pm$ 1.3	
$D_J^*(2760)^0$	$D^+\pi^-$	2760.1 $\pm$ 1.1 $\pm$ 3.7			74.4 $\pm$ 3.4 $\pm$ 19.1			55.8 $\pm$ 1.3 $\pm$ 10.0	17.3
$D_J^*(3000)^0$	$D^+\pi^-$	3008.1 $\pm$ 4.0			110.5 $\pm$ 11.5			17.6 $\pm$ 1.1	21.2
$D_2^*(2460)^+$	$D^0\pi^+$	2463.1 $\pm$ 0.2 $\pm$ 0.6			48.6 $\pm$ 1.3 $\pm$ 1.9			341.6 $\pm$ 22.0 $\pm$ 2.0	
$D_J^*(2760)^+$	$D^0\pi^+$	2771.7 $\pm$ 1.7 $\pm$ 3.8			66.7 $\pm$ 6.6 $\pm$ 10.5			20.1 $\pm$ 2.2 $\pm$ 1.0	18.8
$D_J^*(3000)^+$	$D^0\pi^+$	3008.1 (fixed)			110.5 (fixed)			7.6 $\pm$ 1.2	6.6

- Look for resonances in the final states:
  - $D^+ (K^- \pi^+ \pi^+) K_S^0 (\pi^+ \pi^-)$
  - $D^0 (K^- \pi^+) K^+$
- Selection of candidates places variety of fiducial and kinematic constraints.
- PID discrimination used to mitigate cross-feed.
- Defining  $\theta$  as the angle between momentum of strange meson in  $DK$  system and momentum direction of  $DK$  system in lab frame - imposing  $\cos \theta > 0$  vetoes 90 % of combinatoric background.
- Further optimisation of the  $D_{s2}^*(2573)^+$  peak significance using decay kinematics.