

Rare and forbidden B and tau decays in Belle

24 July, 2014

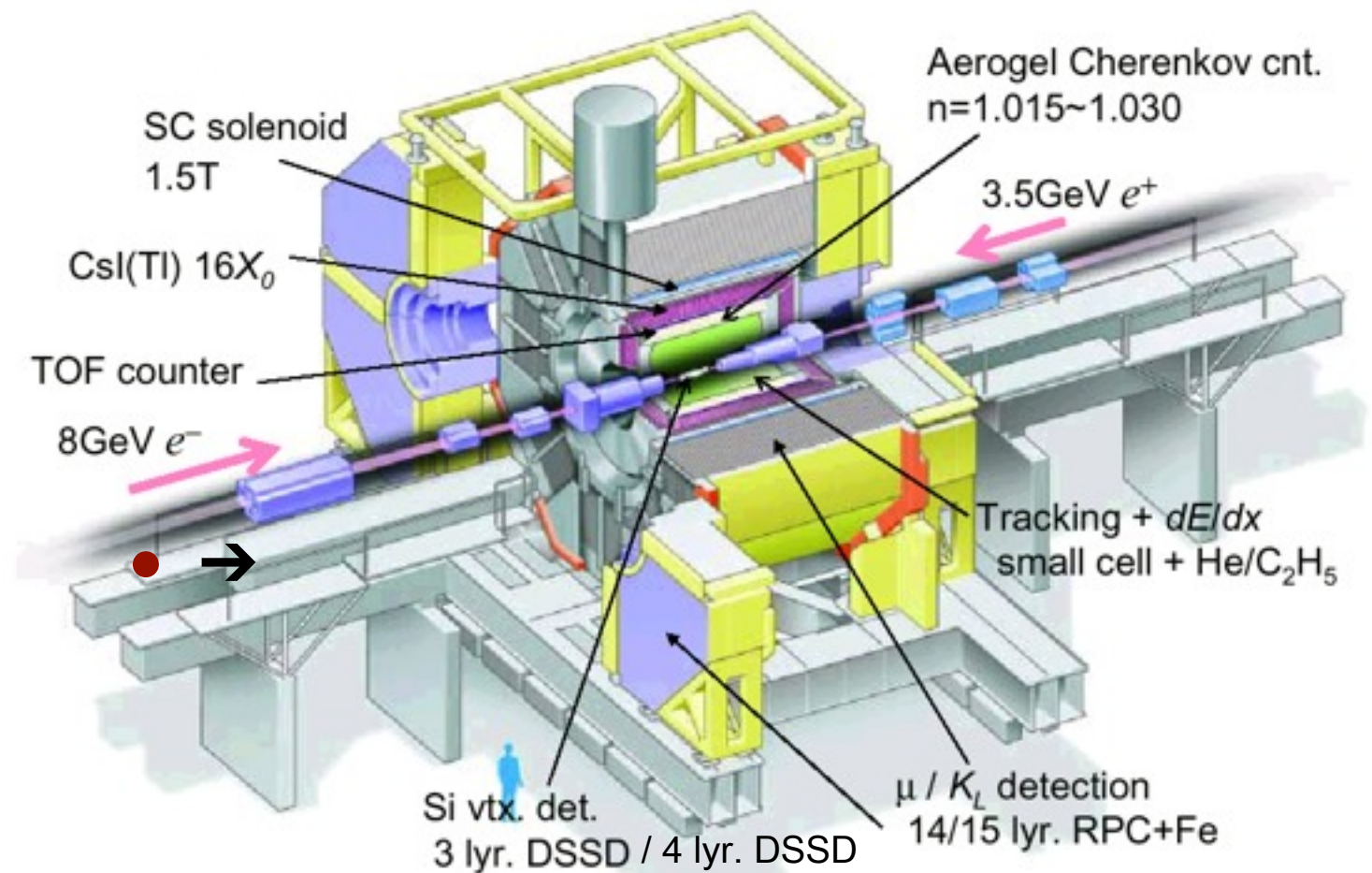
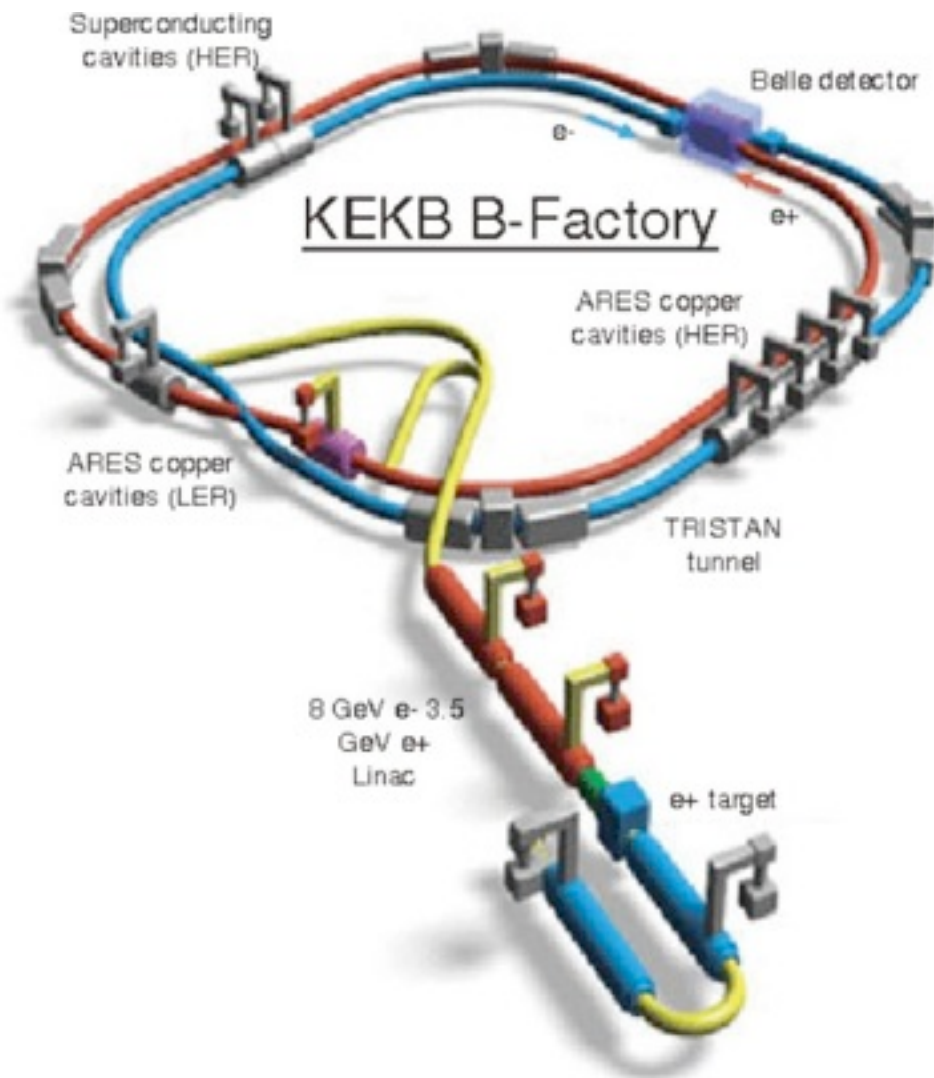
(on behalf of Belle Collaboration)



HyoJung Hyun
Kyungpook National University, Daegu, S. Korea

- KEKB and Belle Experiment
- Leptonic Decays : $B^+ \rightarrow e^+ \nu_e$ and $B^+ \rightarrow \mu^+ \nu_\mu$
- Search for Massive Neutral Leptons
 - $B^+ \rightarrow l^+ X^0$ (X^0 : something massive)
 - $B \rightarrow (X) l \nu_{\text{heavy}}$ (X : meson)
- Lepton Flavor Violation in Tau Decays : $\tau \rightarrow l^+ h h'$
- Summary

KEKB and Belle Experiment



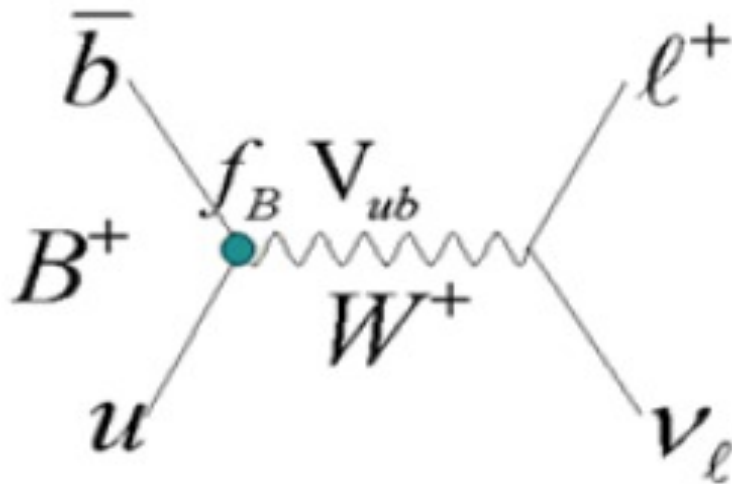
- 4π detector + known initial state \rightarrow perfect environment for studies of B decays with neutrinos in final state
- Collected full data set : $\sim 710 \text{ fb}^{-1}$ at $\Upsilon(4S)$ $\rightarrow 772 \times 10^6$ BB-bar pairs

$$\mathbf{B^+ \rightarrow e^+ \nu_e \text{ and } B^+ \rightarrow \mu^+ \nu_\mu}$$

Y. Yook, et al., arXiv:1406.6356v1

$B^+ \rightarrow l^+ \nu_l$

Physics Motivation



SM Predictions:

$$\mathcal{B}(B \rightarrow e\nu) \sim 10^{-11}$$

$$\mathcal{B}(B \rightarrow \mu\nu) \sim 10^{-7}$$

$$\mathcal{B}(B \rightarrow \tau\nu) \sim 10^{-4}$$

Helicity suppressed in the SM

$$\mathcal{B}(B^+ \rightarrow l^+ \nu_l) = \frac{G_F^2 m_B m_l^2}{8\pi} \left(1 - \frac{m_l^2}{m_B^2}\right)^2 f_B^2 |V_{ub}|^2 \tau_B$$

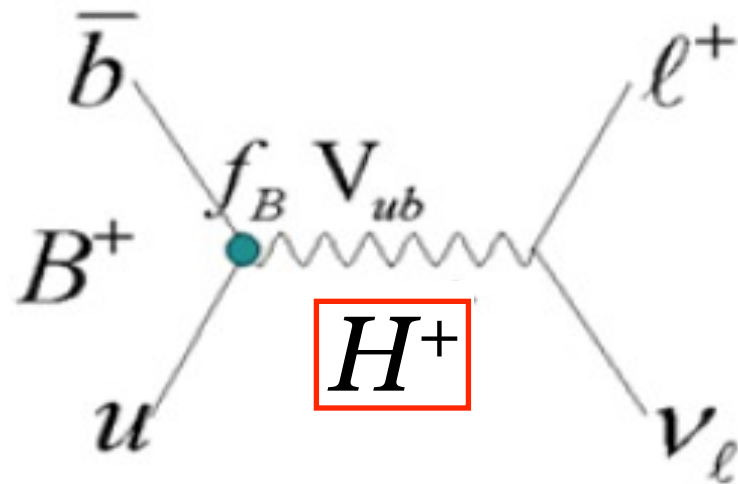
Origin of uncertainty

$|V_{ub}|$ given by a fit to the full CKM unitarity triangle
 f_B given from lattice QCD calculations

- A clean process for the measurement of $f_B^2 \cdot |V_{ub}|^2$ within the SM
- Evidence of $B^+ \rightarrow \tau^+ \nu$ from Belle and BABAR experiments
 - $[0.72^{+0.27}_{-0.25} \text{ (stat)} \pm 0.11 \text{ (syst)}] \times 10^{-4}$ PRL 110, 131801 (2013)
 - $[1.8^{+0.9}_{-0.8} \text{ (stat)} \pm 0.4 \text{ (bkg. syst)} \pm 0.2 \text{ (other syst)}] \times 10^{-4}$ PRD 77, 011107(R) (2008)

$B^+ \rightarrow l^+ \nu_l$

Physics Motivation

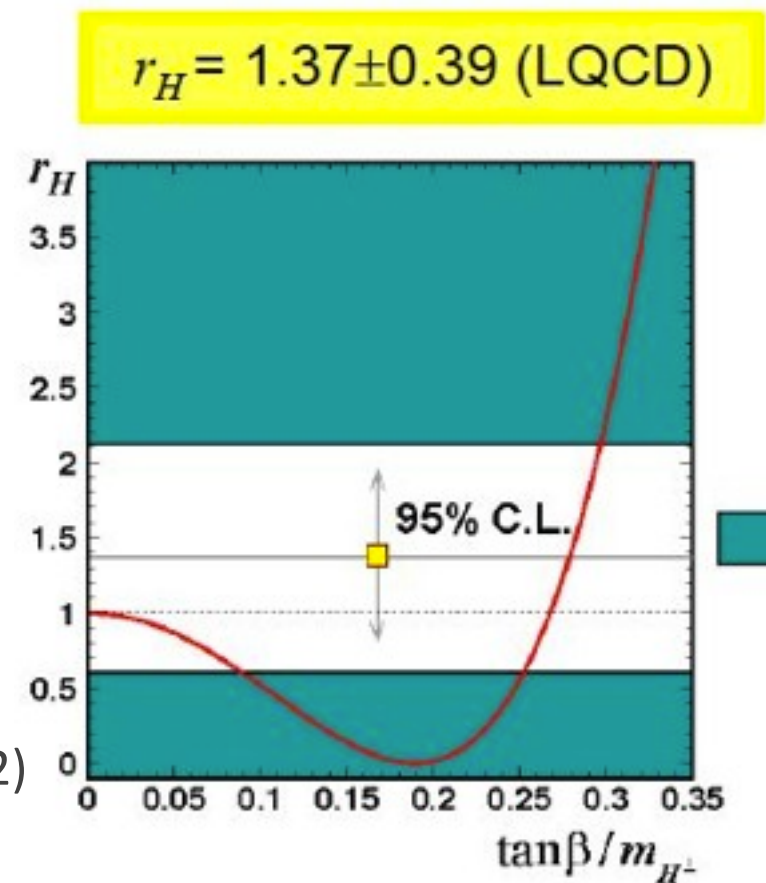


- New Physics (NP) contributions might interfere with SM and modify SM expectation
- Most prominent: H^\pm from 2-Higgs-Doublet-Models (2HDM) in MSSM

$$\mathcal{B}(B^+ \rightarrow l^+ \nu_l)_{2HDM} = \mathcal{B}(B^+ \rightarrow l^+ \nu_l)_{SM} \times \left(1 - \tan^2 \beta \frac{m_B^2}{m_H^2} \right)^2$$

$$R^{ll'} = \mathcal{B}(B^+ \rightarrow l^+ \nu_l) / \mathcal{B}(B^+ \rightarrow l'^+ \nu_{l'})$$

Physics Report 516, 1 (2012)

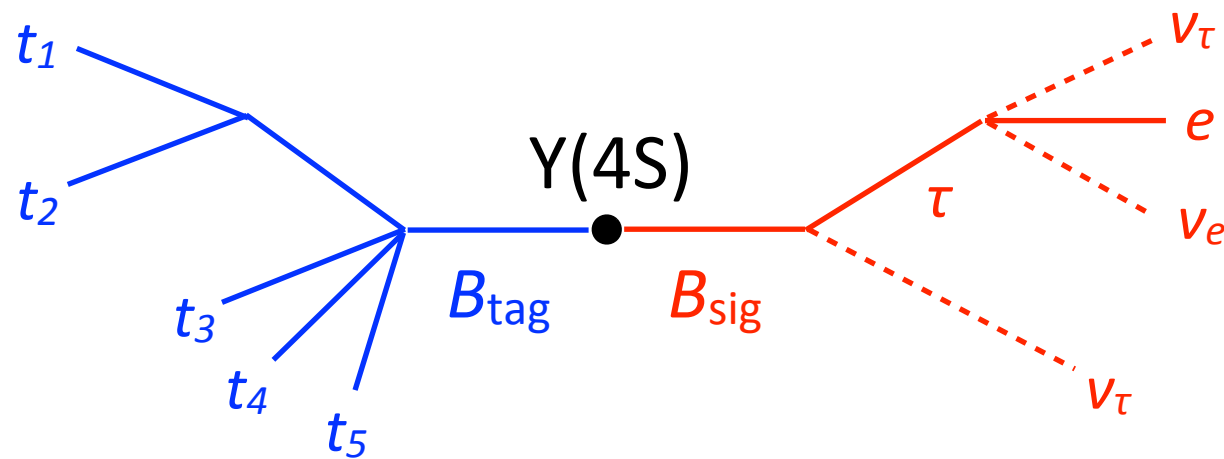


- In NP models with MFV (Minimal Flavor Violation), the ratios are expected to be nearly unmodified from SM expectations V. Cirigliano et al., Nucl. Phys. B 728, 121 (2005)
- In GUT model, the ratios $R^{e\mu}$ and $R^{e\tau}$ may increase to more than one order of magnitude above SM expectation due to the enhancement of the electron mode A. Filipuzzi and G. Isidori, Eur. Phys. J. C64, 55 (2009)

$$B^+ \rightarrow l^+ \nu_l$$

Hadronic Tagging Method

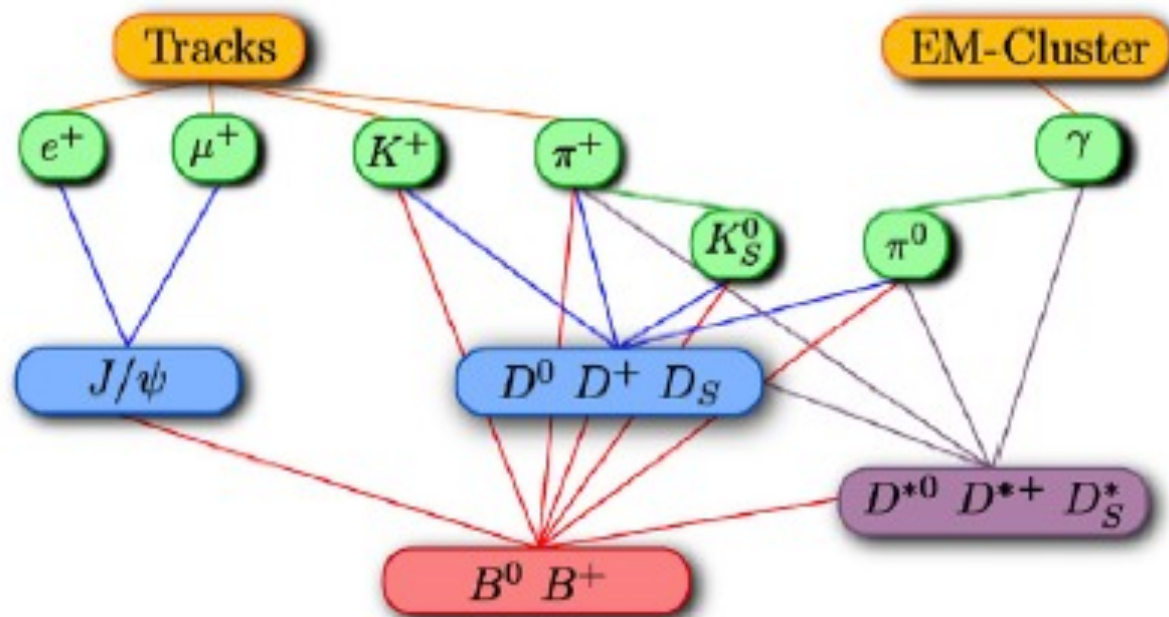
M. Feindt et al., NIMA 654, 432 (2011)



Tag side: the other B meson, reconstructed by the full reconstruction method

Signal side: the decay of physics interest

Exemplary fully reconstructed event

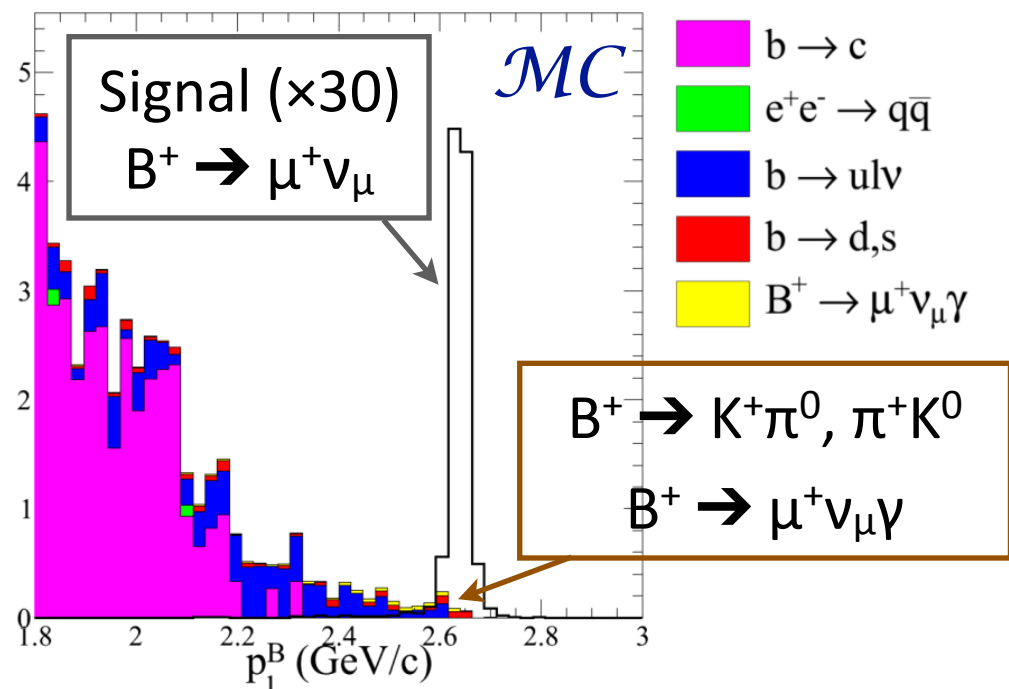
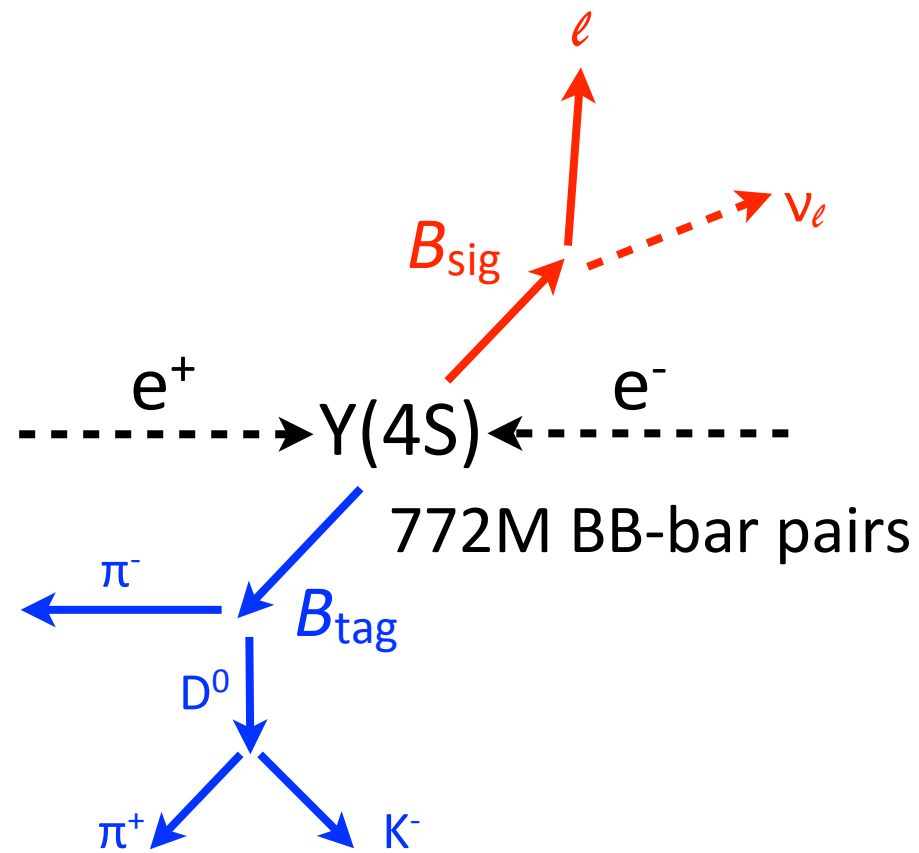


four stages of the full reconstruction

- Complete tagging of a B in $Y(4S) \rightarrow BB\text{-bar}$ decays
- full reconstruction of a B_{tag} in a hadronic channel:
 - taking over 1000 decay chains into account
 - B.F. ($Y(4S) \rightarrow BB\text{-bar}$) $\sim 96\%$
- Constrain the charge, flavour, four-momentum of B_{tag} and B_{sig}
- Results in high purity and increased efficiency, $\sim 0.28\%$ (old method: 0.14%)
- Good suppression of $e^+e^- \rightarrow qq\text{-bar}$ ($q = u, d, s, c$)
- Good ways to reconstruct modes with invisible particle



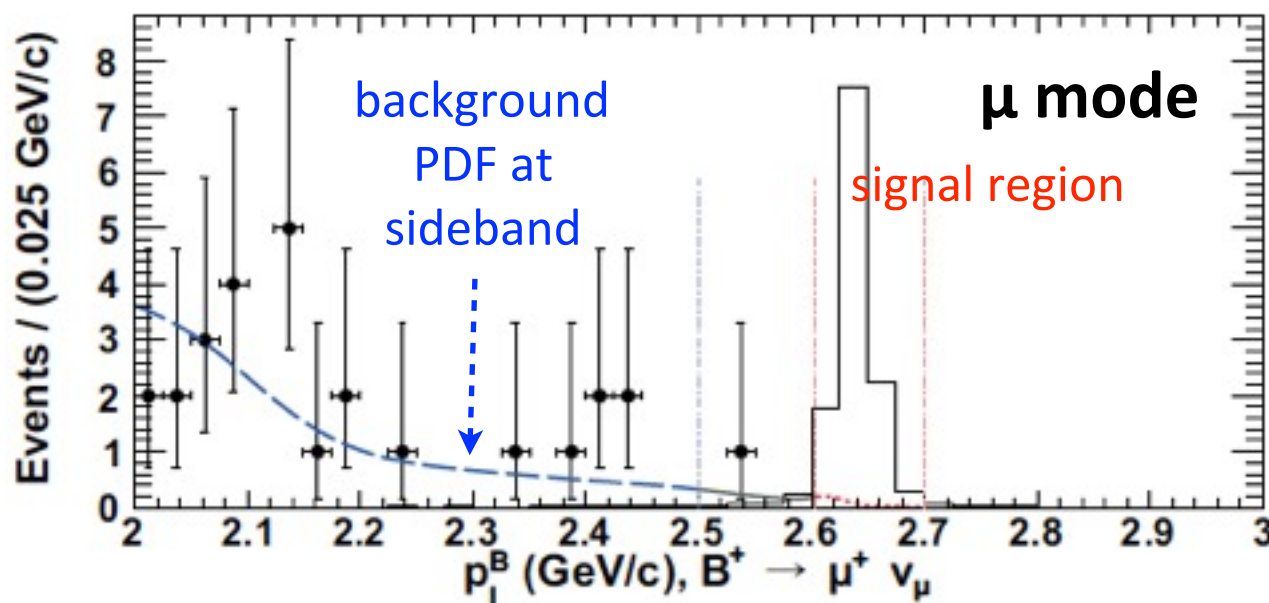
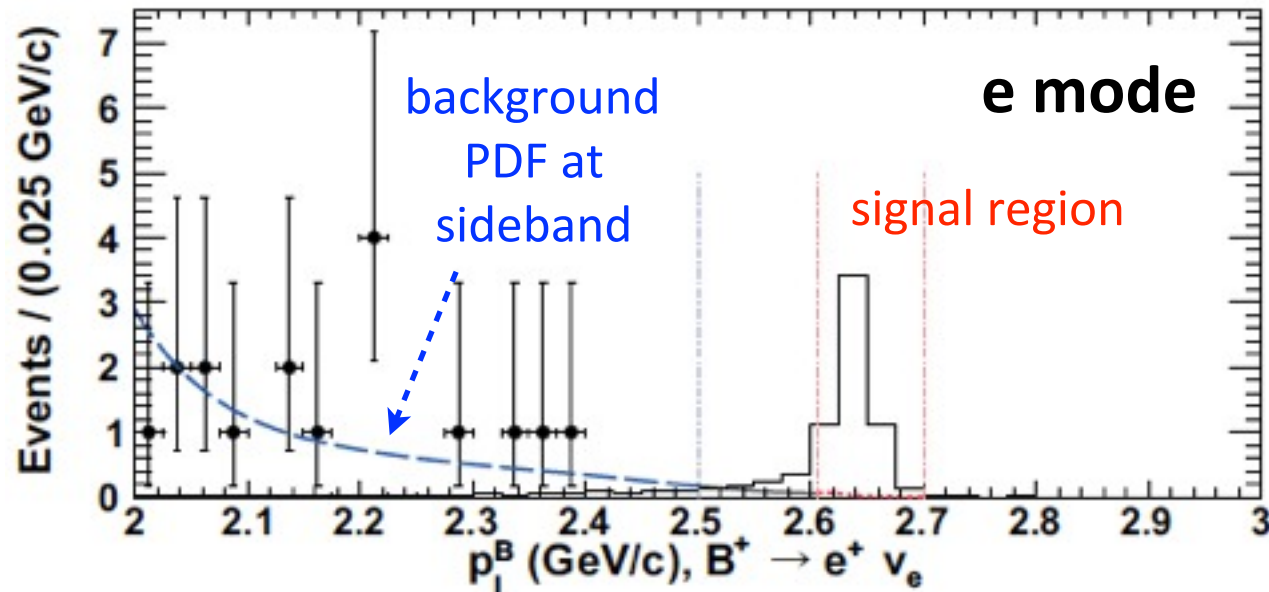
Analysis Strategy



- On signal side, one single track (e or μ) required
- 2-body decay: clear signature in B_{sig} rest frame
- Signal extraction variable: p_l^B
(lepton momentum at the rest frame of B_{sig})
- Sharp-peaking near 2.64 GeV/c
- Very clean signal with low BG
- Background estimation:
 - Fit the sideband of p_l^B (2-2.5 GeV/c)
 \rightarrow extrapolate the BG into the signal region
 ($\sim 2.6-2.7$ GeV/c)
 - Dedicated MC modeling for peaking BG at signal region

$B^+ \rightarrow l^+ \nu_l$

Signal Extraction



- No signal events observed
 \rightarrow Upper limit is calculated using Feldman-Cousins method

$$\mathcal{B}(B^+ \rightarrow l^+ \nu) < \frac{S_{90}}{2\varepsilon_s N_{B^+ B^-}}$$

$B \rightarrow l\nu$	ε_s [%]	N_{bkg}	N_{obs}
$e\nu$	0.086	0.10 ± 0.04	0
$\mu\nu$	0.102	$0.26^{+0.09}_{-0.08}$	0

$\mathcal{B}(B \rightarrow e\nu) < 3.4 \times 10^{-6}$
 $\mathcal{B}(B \rightarrow \mu\nu) < 2.7 \times 10^{-6}$ @ 90% C.L.

Previous measurements @ 90% C.L.

Hadronic Tagging

$$\mathcal{B}(B \rightarrow e\nu) < 5.2 \times 10^{-6}$$

$$\mathcal{B}(B \rightarrow \mu\nu) < 5.6 \times 10^{-6} \text{ 342 fb}^{-1}$$

BABAR PRD 77, 091104 (2008)

Loose Tagging

$$\mathcal{B}(B \rightarrow e\nu) < 9.8 \times 10^{-7} \text{ 253 fb}^{-1}$$

Belle PLB 647, 67 (2007)

$$\mathcal{B}(B \rightarrow \mu\nu) < 1.0 \times 10^{-6} \text{ 426 fb}^{-1}$$

BABAR PRD 79, 091101 (2009)

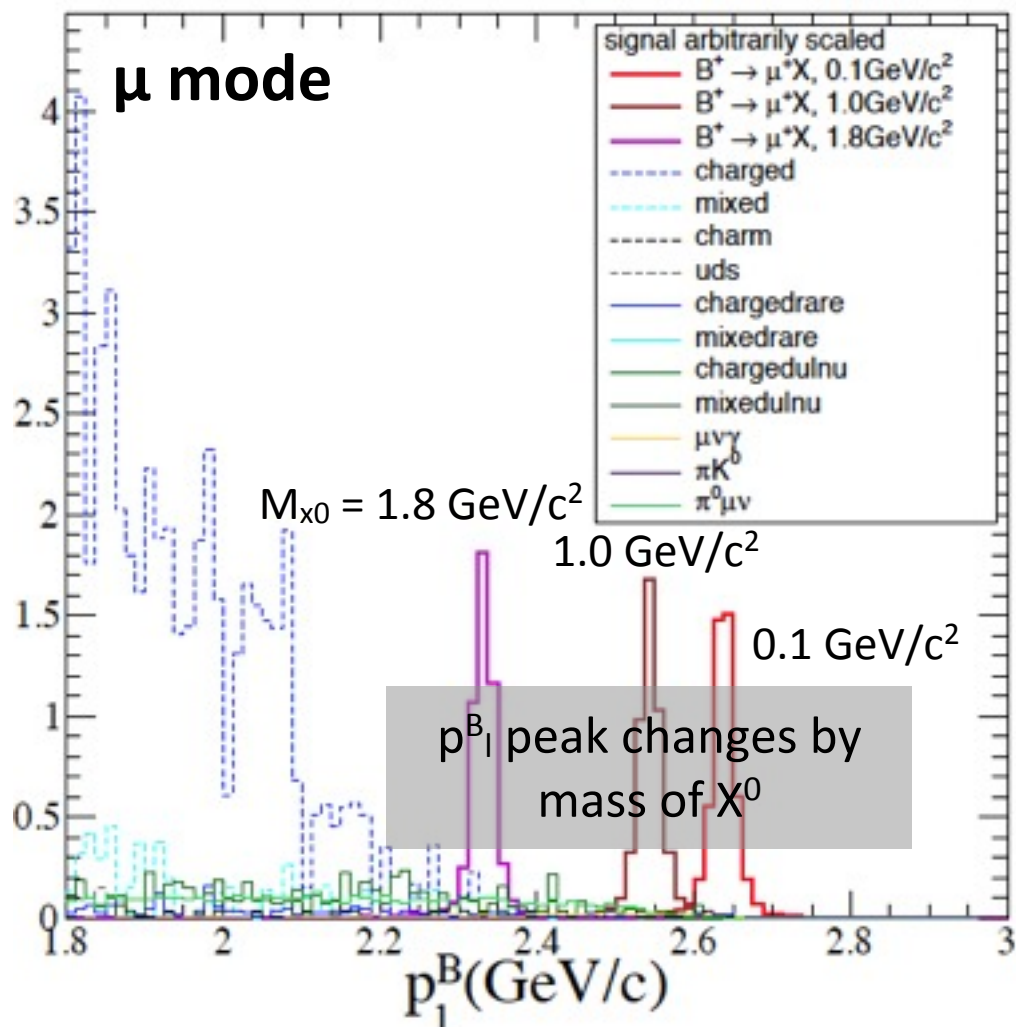
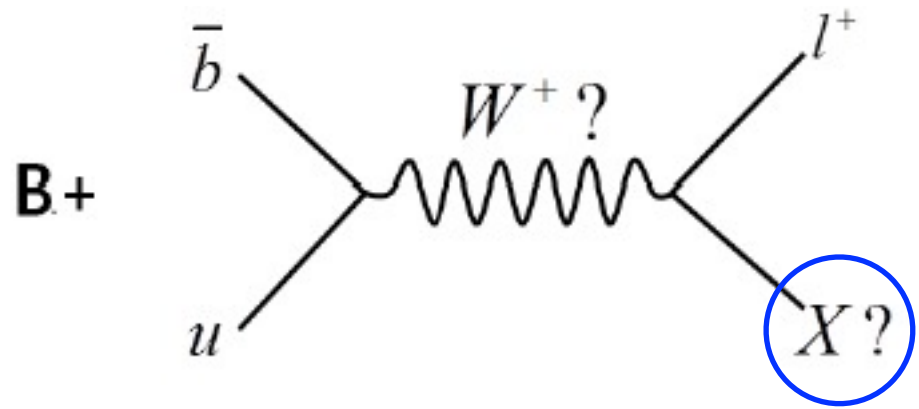
Search for Massive Neutral Lepton

$B^+ \rightarrow l^+ X^0$: search for massive invisible particle X^0

$B \rightarrow (X)l^+ \nu_{\text{heavy}}$: search for heavy neutrino

D. Liventsev, et al., PRD 87, 071102(R) (2013)

$B^+ \rightarrow l^+ X^0$



- Search for **new** neutrino-like, heavy fermion X^0
- Covered mass range: $0.1 \text{ GeV}/c^2 \sim 1.8 \text{ GeV}/c^2$ in steps of $0.1 \text{ GeV}/c^2$
- Similar to $B \rightarrow l\nu$ analysis
 - except: looser momentum cut and looser impact parameter selection

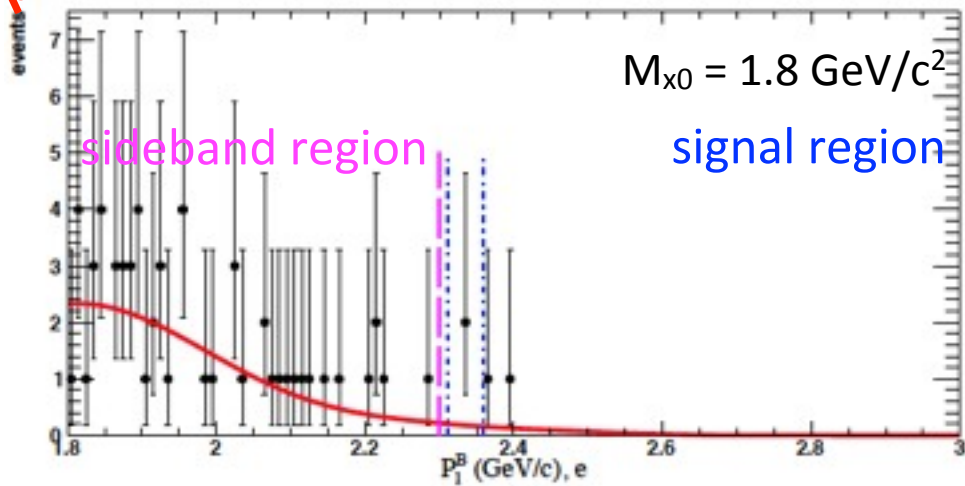
mode	p_l^{lab}	dz [cm]	dr [cm]
$B^+ \rightarrow l^+ X$	$p_l^{\text{lab}} > 1.0 \text{ GeV}/c$	$ dz < 2.0$	$dr < 0.5$
$B^+ \rightarrow l^+ \nu$	$p_l^{\text{lab}} > 1.8 \text{ GeV}/c$	$ dz < 1.5$	$dr < 0.05$

- Similar systematics
- p_l^B also shows good separation
- Signal region optimized to lowest expected upper limit

$B^+ \rightarrow I^+ X^0$

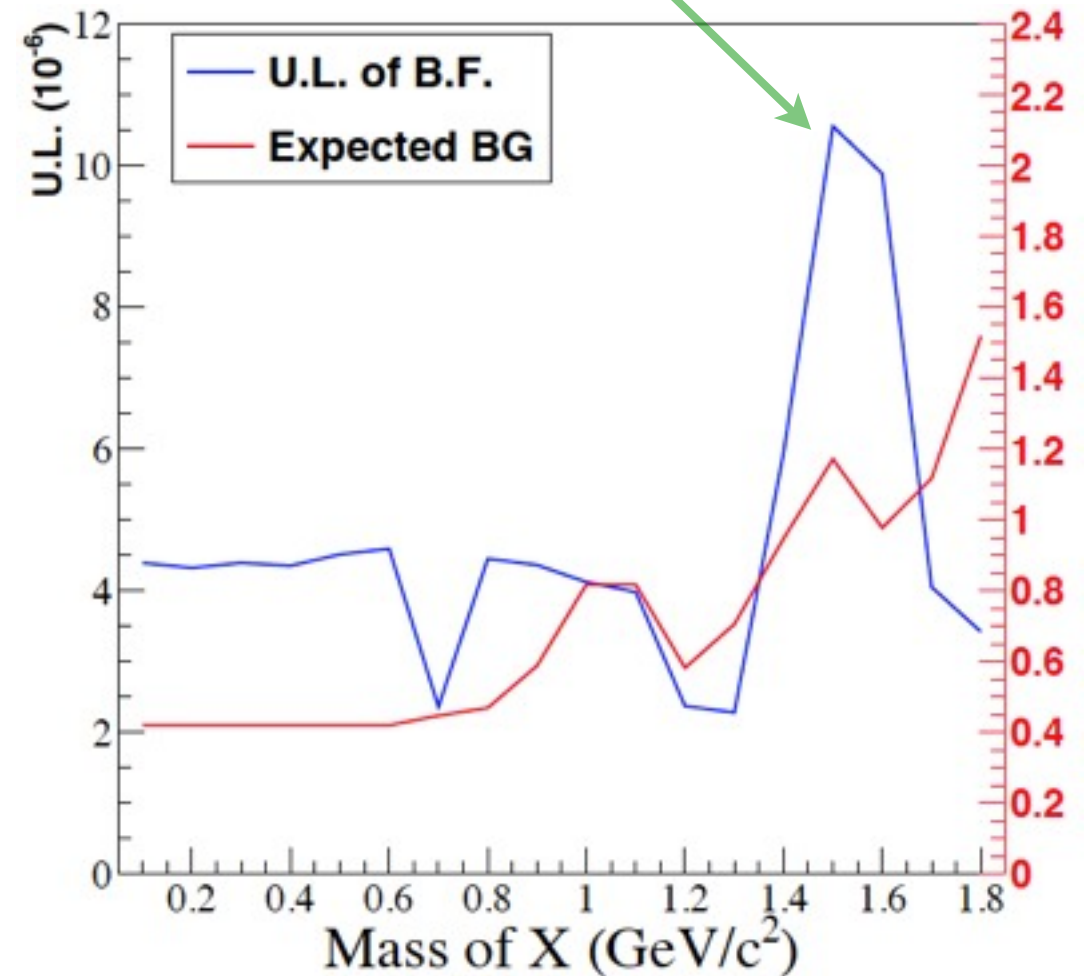
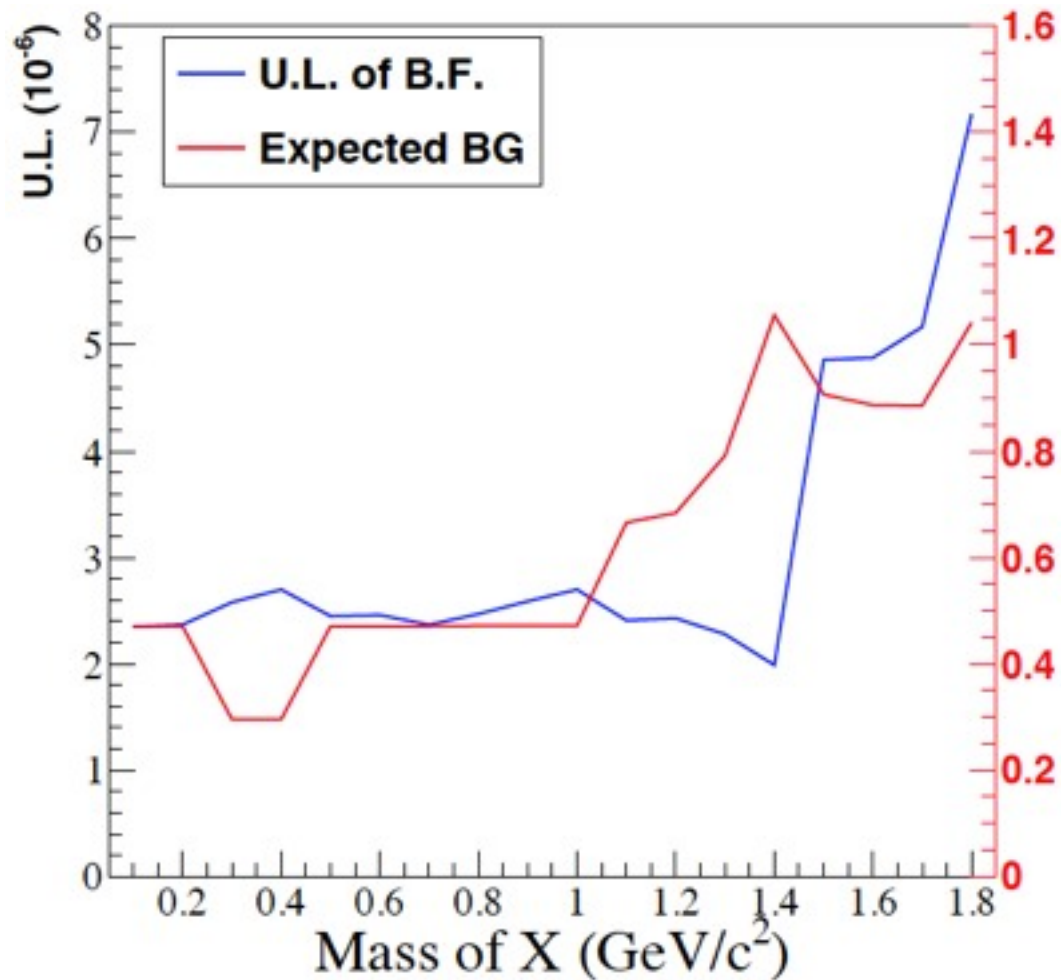
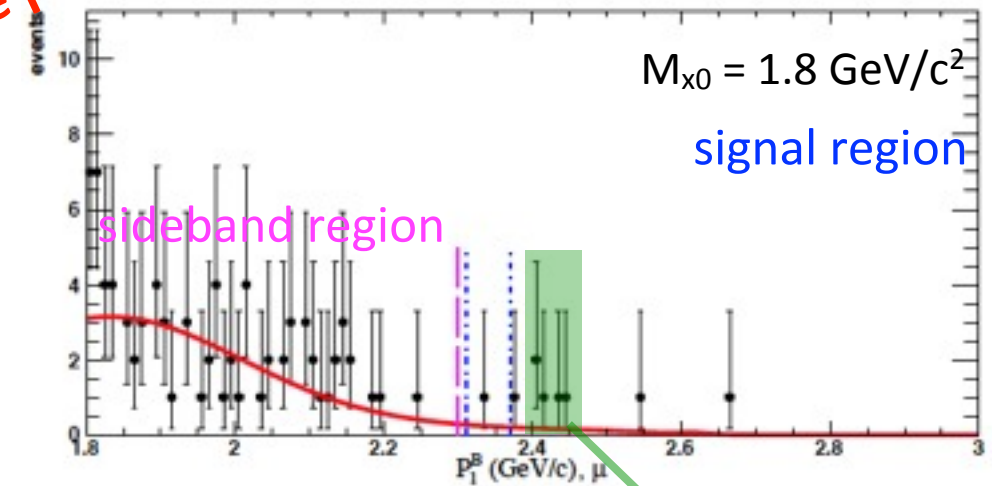
Belle preliminary

e mode



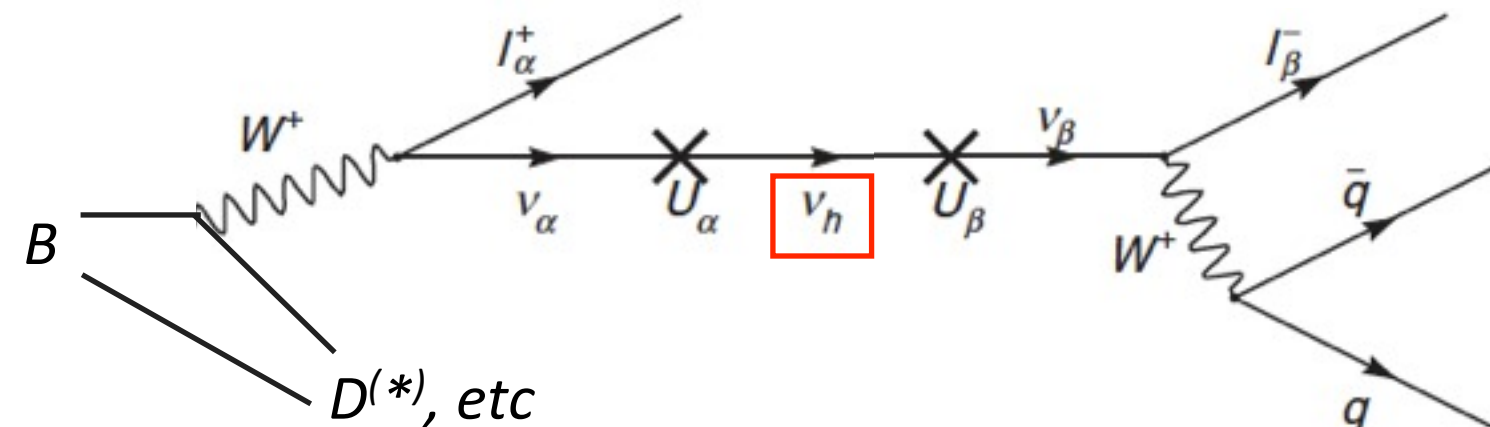
Belle preliminary

μ mode



$B \rightarrow (X)l\nu_h$

- $m_\nu > 0$ from experimental data while SM assumes 0 mass
- Heavy neutrinos (ν_h) are assumed in many models beyond the SM
- ν_h interacts only by mixing with a left-handed neutrino by a unitary transformation
- Search for $B \rightarrow (X)l_2^+\nu_h$
 - if ν_h is Majorana, $\nu_h \rightarrow l_1^+\pi^-$ or $l_1^-\pi^+$
 - if ν_h is Dirac, $\nu_h \rightarrow l_1^-\pi^+$
- Search range of heavy neutrino : $0.5 \text{ GeV}/c^2 \leq M(\nu_h) \leq 5.0 \text{ GeV}/c^2$
- Approach separately for large and small $M(\nu_h)$
 - $M(\nu_h) < 2.0 \text{ GeV}/c^2$: look for $X = D$ or D^* using recoil mass
 - $M(\nu_h) > 2.0 \text{ GeV}/c^2$: look for $X = D^{(*)}$, light meson, nothing

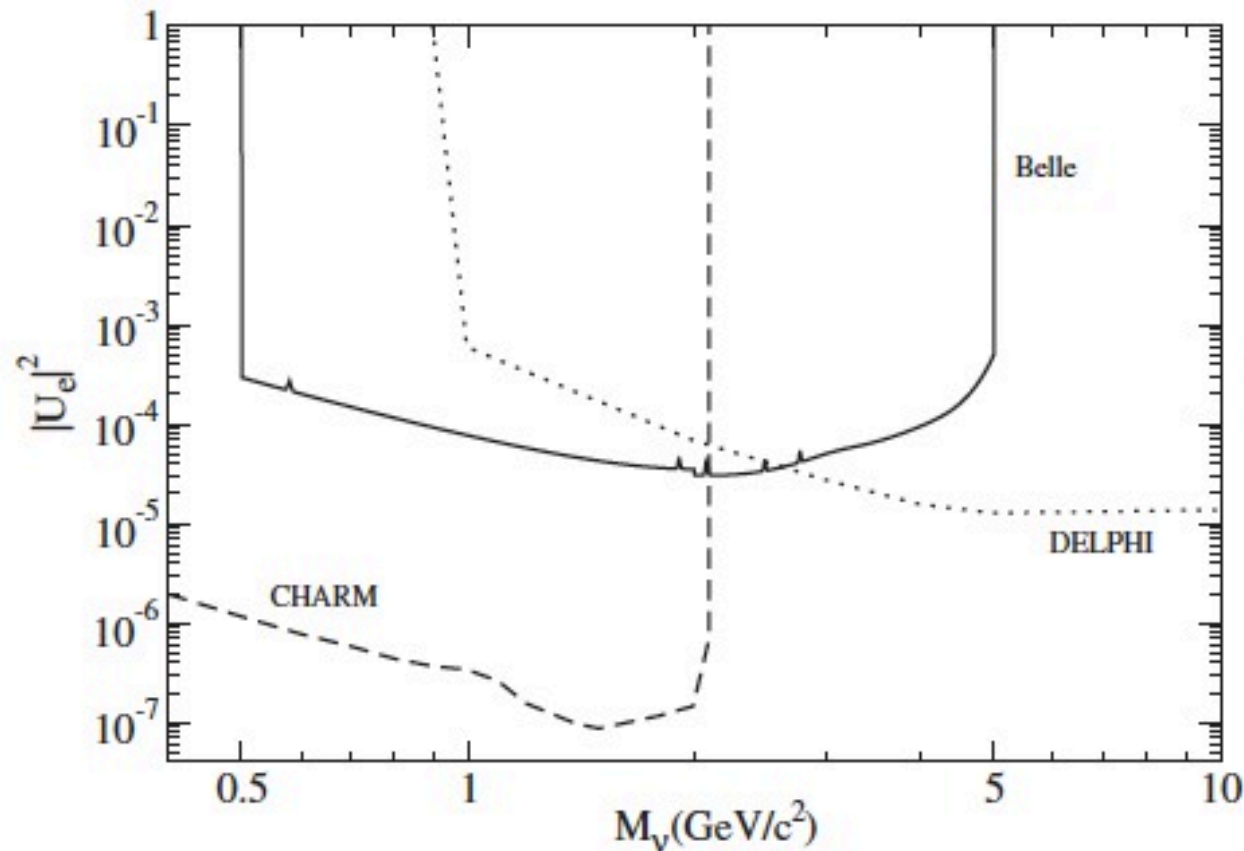


Heavy neutrino production and decay diagram

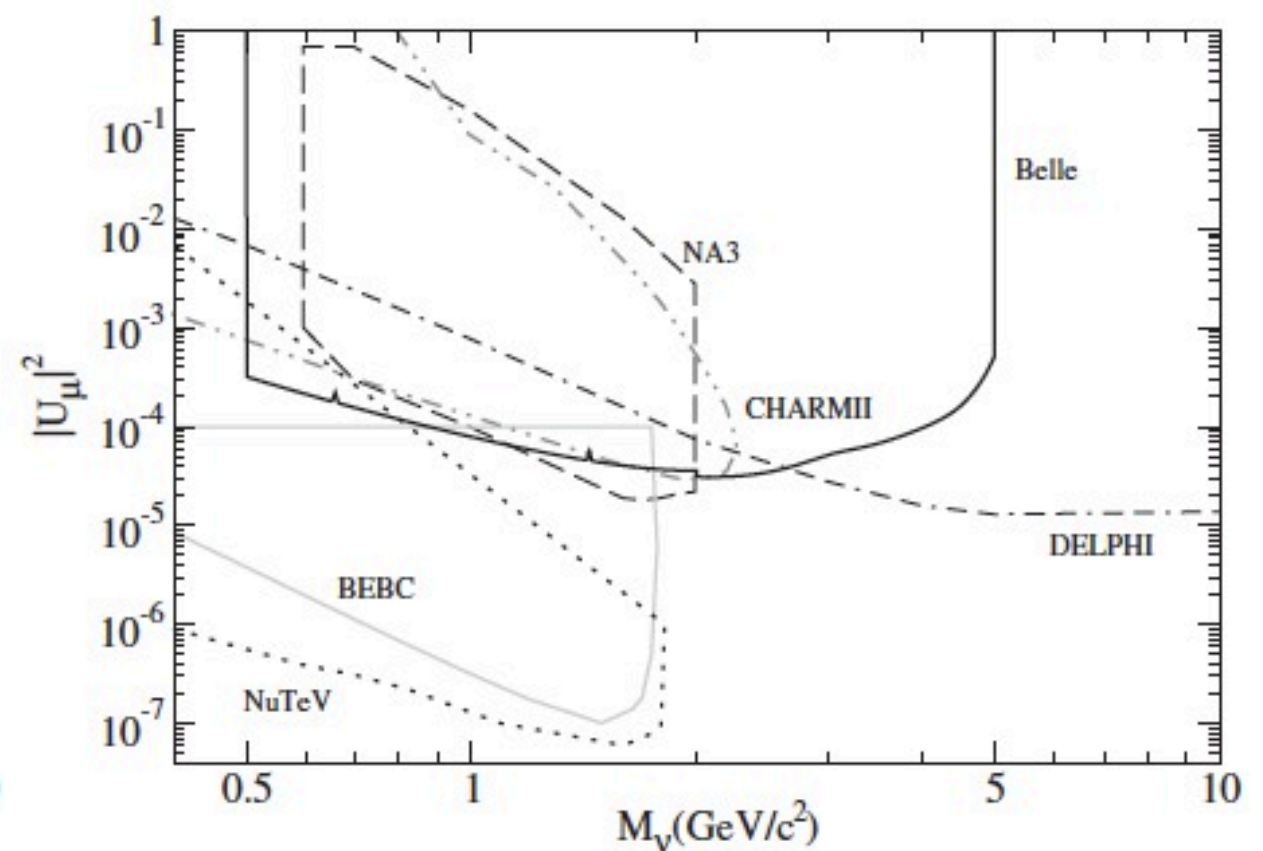
- Background suppression
 - QED background : by $N(\text{track}) > 4$
 - Decays with similar topology : by strict lepton ID, vertex quality, and distance $l-\pi$ vertex
 - Combinatorial background : by distance btw the closest associated hit in SVD/CDC to vertex of ν_h

$B \rightarrow (X)l\nu_h$

$|U_e|^2$



$|U_\mu|^2$



- Upper limits on $\nu_h - \nu_l$ mixing ($|U_l|$) are obtained in the range $0.5 \text{ GeV}/c^2 \leq M(\nu_h) \leq 5.0 \text{ GeV}/c^2$
- Corresponding upper limit for the product branching fraction (for $M(\nu_h) = 2 \text{ GeV}/c^2$)

$$\mathcal{B}(B \rightarrow (X)l\nu_h) \times \mathcal{B}(\nu_h \rightarrow l\pi^+) < 7.2 \times 10^{-7} \text{ for } l = e \text{ or } \mu$$

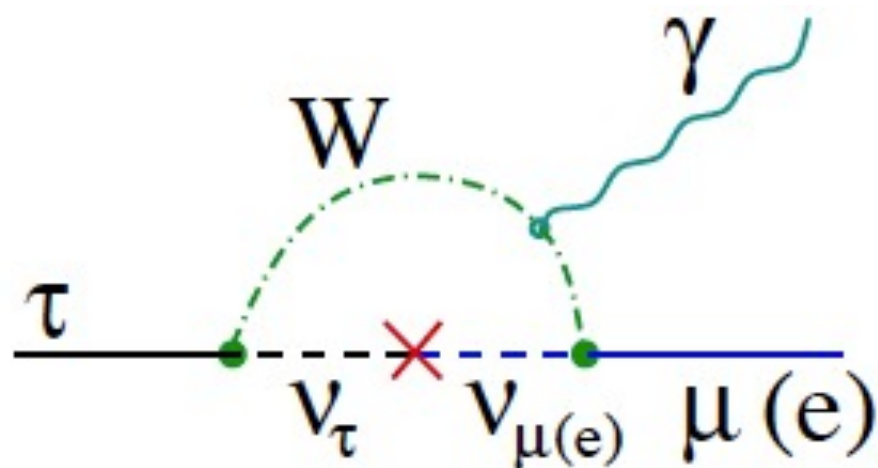
Lepton Flavor Violation in Tau Decays

$$\tau \rightarrow l^+ h h'$$

l : electron or muon, $h^{(\prime)}$: charged pion or kaon

Y. Miyazaki, et al., PLB 719 (2013) 346

Lepton Flavor Violation in Tau Decays



Model	$B(\tau \rightarrow \mu\gamma)$	$B(\tau \rightarrow \mu\mu)$
mSUGRA+seesaw	10^{-8}	10^{-9}
SUSY+SO(10)	10^{-8}	10^{-10}
SM+seesaw	10^{-9}	10^{-10}
Non-universal Z'	10^{-9}	10^{-8}
SUSY+Higgs	10^{-10}	10^{-8}

- Probability of LFV decays of charged lepton is extremely small in the SM

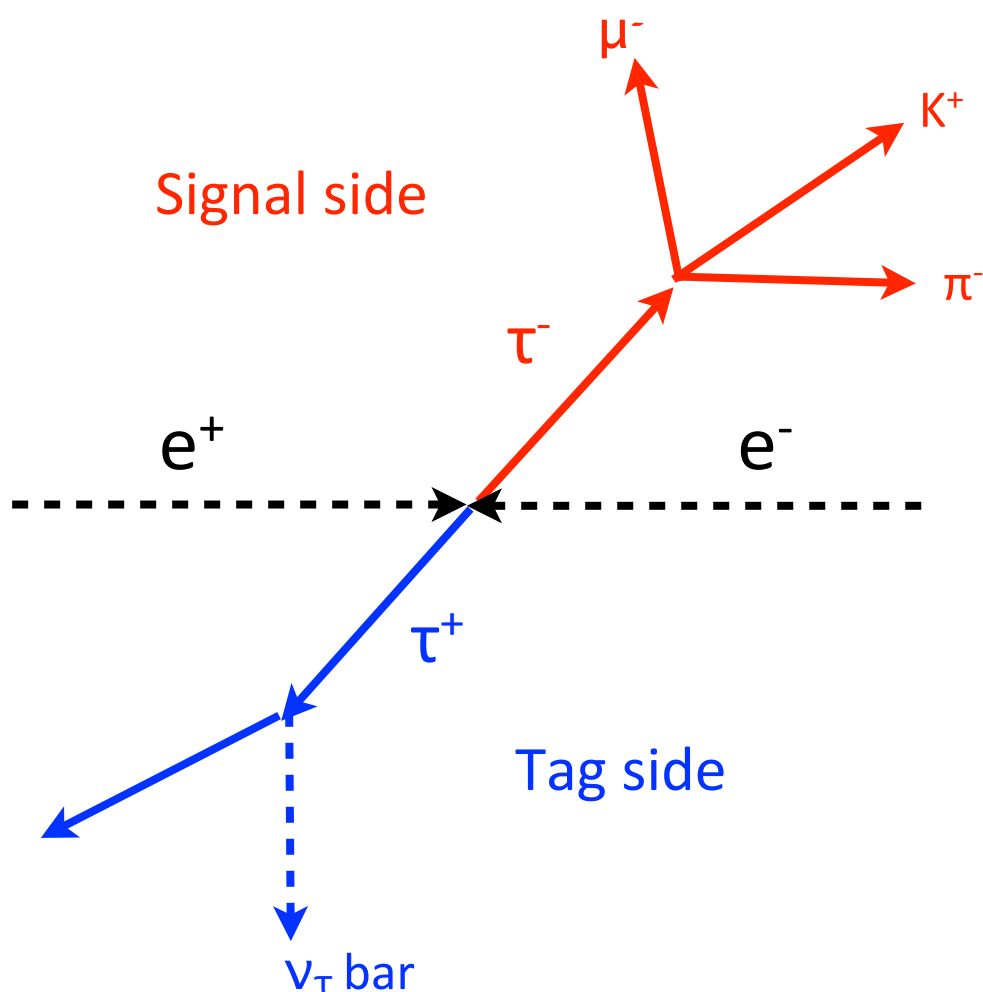
$$\mathcal{B}(\tau \rightarrow l\nu) \sim \left(\frac{\Delta m_\nu^2}{m_W^2} \right)^2 < 10^{-54}$$

- Many models beyond the SM predict LFV decays with the branching fractions up to $\leq 10^{-8}$. As a result, observation of LFV is a clear signature of New Physics
- τ lepton is a good tool to search for the LFV decays due to the enhanced couplings to the new particles as well as large number of LFV decay modes
- Study of the different τ LFV decay modes allows us to test various NP models

$\tau \rightarrow l^+ h h'$

Data Set and Method

Process	σ [nb]
$e^+e^- \rightarrow qq\text{-bar}$ ($q = u, d, s, c$)	3.39
$e^+e^- \rightarrow bb\text{-bar}$	1.05
$e^+e^- \rightarrow \tau^+\tau^-(\gamma)$	0.919



- **854 fb⁻¹ data sample used**
 - collected at or below Y(4S) and Y(5S) resonances
- **In total of 14 modes** were investigated
 - 8 LFV $\tau^- \rightarrow l^+ h h'$ and 6 lepton-number-violating $\tau^- \rightarrow l^+ h h'$ decays
(l : electron or muon, h, h' : pions or Kaons)
- **Blind analysis performed**
 - Search for signal events on the M_{inv} vs. ΔE plane
($M_{\text{inv}} \approx M_{\tau}$, $\Delta E = E_{\text{LFV}} - E_{\text{beam}} \approx 0$)
- Tag one τ by its 1-prong decay ($B_{1\text{-prong}} \sim 85\%$), the other τ is required to produce the LFV final state
- **Background suppression**
 - Opening angle btw missing momentum (\mathbf{p}_{miss}) and charged track on the tag side : $\cos\theta^{\text{CM}}_{\text{tag-miss}}$
 - Selection on the thrust : T
 - Missing mass :
$$m^2_{\text{miss}} = E^2_{\text{miss}} - \mathbf{p}^2_{\text{miss}} = (E_{\text{total}} - E_{\text{vis}})^2 - \mathbf{p}^2_{\text{miss}}$$

- One event in the signal region was found for $\tau^- \rightarrow \mu^+ \pi^- \pi^-$ and $\tau^- \rightarrow \mu^- \pi^+ K^-$, no events for the other 12 modes
- For all modes the number of observed signal events agree with the number of expected background events

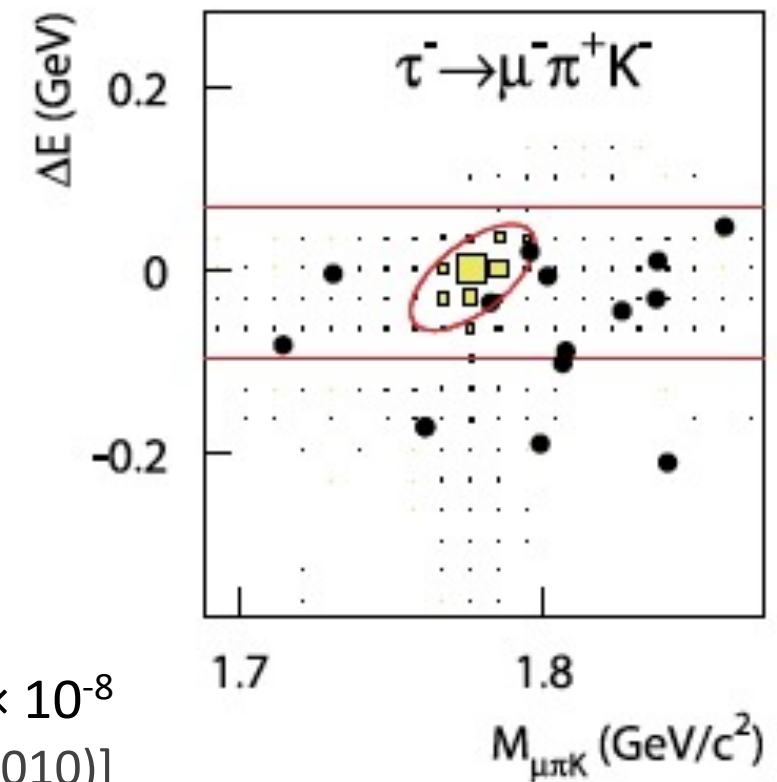
$$\mathcal{B}(\tau \rightarrow l h h') < \frac{S_{90}}{2N_{\tau\tau}\epsilon}$$

S_{90} : the number of signal events including systematic uncertainty

$N_{\tau\tau}$: the number of $\tau^+\tau^-$ pairs, 782×10^6

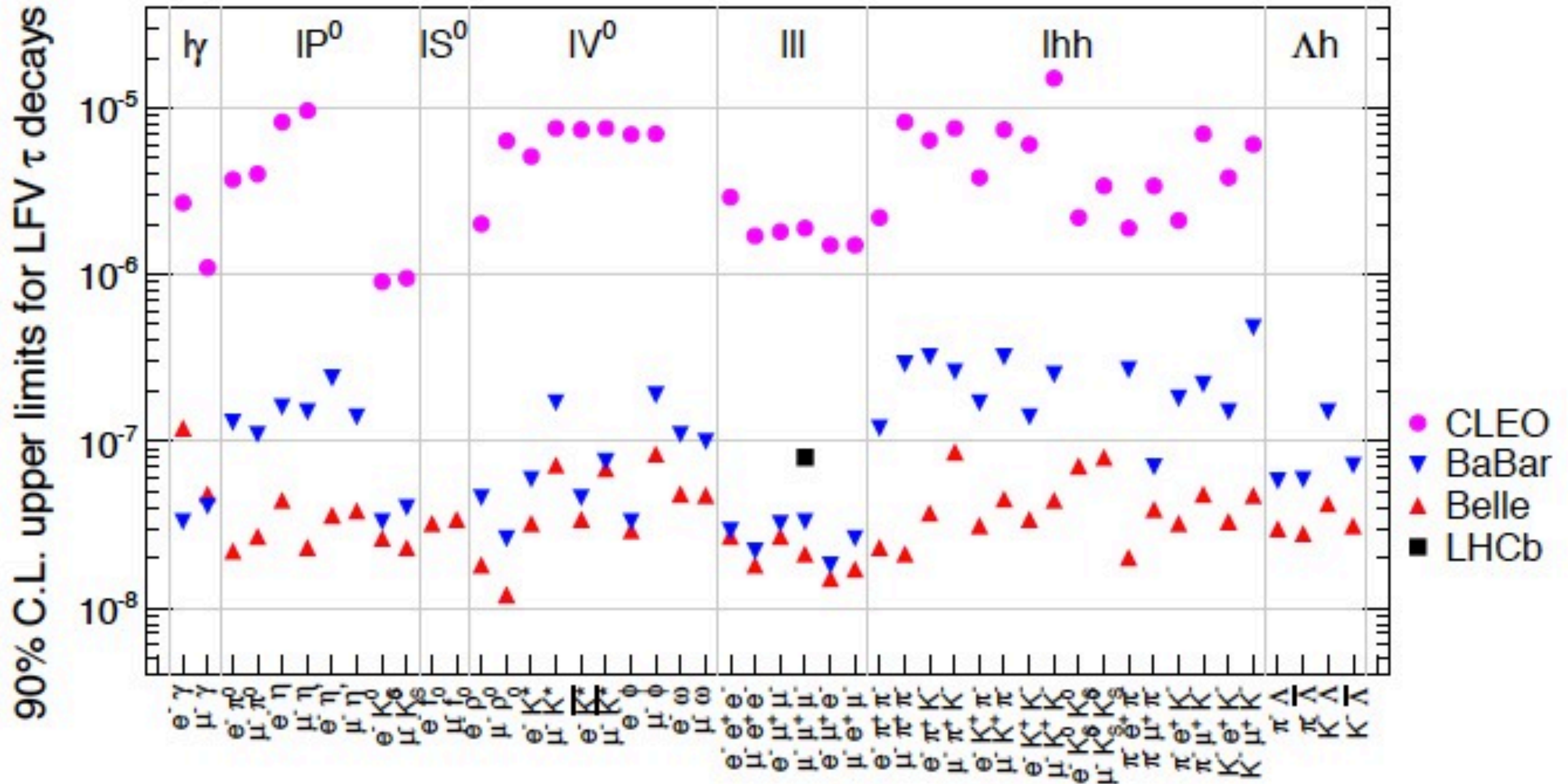
ϵ : signal efficiency

- Obtained upper limits at 90% C.L.: $\mathcal{B}(\tau \rightarrow l h h') < (2.0 \sim 8.6) \times 10^{-8}$
previous result with 671 fb^{-1} : $(3.3 \sim 16) \times 10^{-8}$
[Y. Miyazaki et al., Phys. Lett. B 682, 355 (2010)]



Mode	ϵ (%)	N_{BG}	σ_{syst} (%)	N_{obs}	S_{90}	\mathcal{B} (10^{-8})
$\tau^- \rightarrow \mu^- \pi^+ \pi^-$	5.83	0.63 ± 0.23	5.7	0	1.87	2.1
$\tau^- \rightarrow \mu^+ \pi^- \pi^-$	6.55	0.33 ± 0.16	5.6	1	4.01	3.9
$\tau^- \rightarrow e^- \pi^+ \pi^-$	5.45	0.55 ± 0.23	5.7	0	1.94	2.3
$\tau^- \rightarrow e^+ \pi^- \pi^-$	6.56	0.37 ± 0.19	5.5	0	2.10	2.0
$\tau^- \rightarrow \mu^- K^+ K^-$	2.85	0.51 ± 0.19	6.1	0	1.97	4.4
$\tau^- \rightarrow \mu^+ K^- K^-$	2.98	0.25 ± 0.13	6.2	0	2.21	4.7
$\tau^- \rightarrow e^- K^+ K^-$	4.29	0.17 ± 0.10	6.7	0	2.29	3.4
$\tau^- \rightarrow e^+ K^- K^-$	4.64	0.06 ± 0.06	6.5	0	2.39	3.3
$\tau^- \rightarrow \mu^- \pi^+ K^-$	2.72	0.72 ± 0.28	6.2	1	3.65	8.6
$\tau^- \rightarrow e^- \pi^+ K^-$	3.97	0.18 ± 0.13	6.4	0	2.27	3.7
$\tau^- \rightarrow \mu^- K^+ \pi^-$	2.62	0.64 ± 0.23	5.7	0	1.86	4.5
$\tau^- \rightarrow e^- K^+ \pi^-$	4.07	0.55 ± 0.31	6.2	0	1.97	3.1
$\tau^- \rightarrow \mu^+ K^- \pi^-$	2.55	0.56 ± 0.21	6.1	0	1.93	4.8
$\tau^- \rightarrow e^+ K^- \pi^-$	4.00	0.46 ± 0.21	6.2	0	2.03	3.2

Results on LFV of τ decays



48 different LFV modes were studied at Belle
The world best upper limits were obtained

Recently, first U.L. for BNV and LNV τ decays
with protons is obtained from LHCb

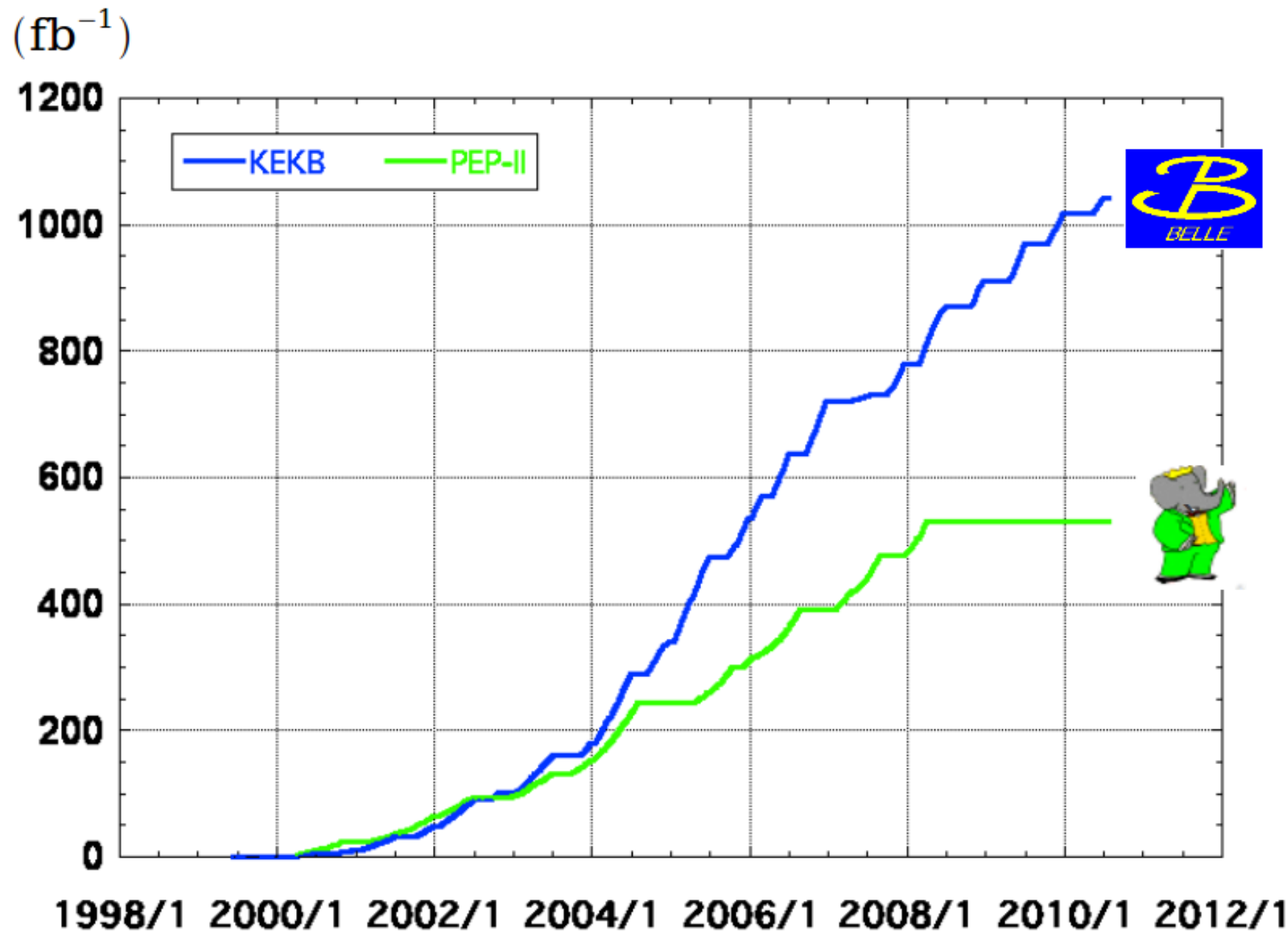
R. Aaij, et al., PLB 724, 36 (2013)

- A study of decays with neutrinos in the final state is possible using the hadronic tagging method
- Most stringent limits on $B^+ \rightarrow l^+ \nu$ are obtained
 - $\mathcal{B}(B \rightarrow e \nu) < 3.4 \times 10^{-6}$ @90% C.L.
 - $\mathcal{B}(B \rightarrow \mu \nu) < 2.7 \times 10^{-6}$ @90% C.L.
- Performed **search for heavy neutral lepton-like particles**
 - $B^+ \rightarrow l^+ X^0$, where X^0 can be any invisible (and possibly massive) fermion particle and in preliminary results, the upper limits are $O(10^{-6})$ for $0.1 \text{ GeV}/c^2 < M_x < 1.8 \text{ GeV}/c^2$
 - U.L. on mixing of $\nu_h - \nu_l$ is set in the mass range of $0.5 \text{ GeV}/c^2 \sim 5.0 \text{ GeV}/c^2$
- Up to now, no hints for NP contribution from leptonic B decays
- We studied 48 different **LFV modes in tau decays**, 46 of them were analyzed with almost full data sample and obtained upper limits on the branching fractions are of the order of 10^{-8}



BACKUP SLIDES

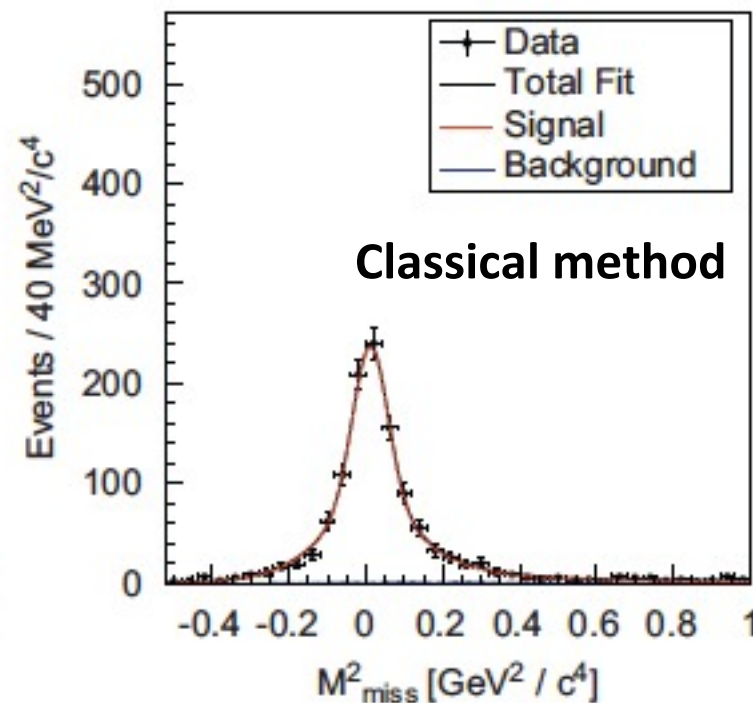
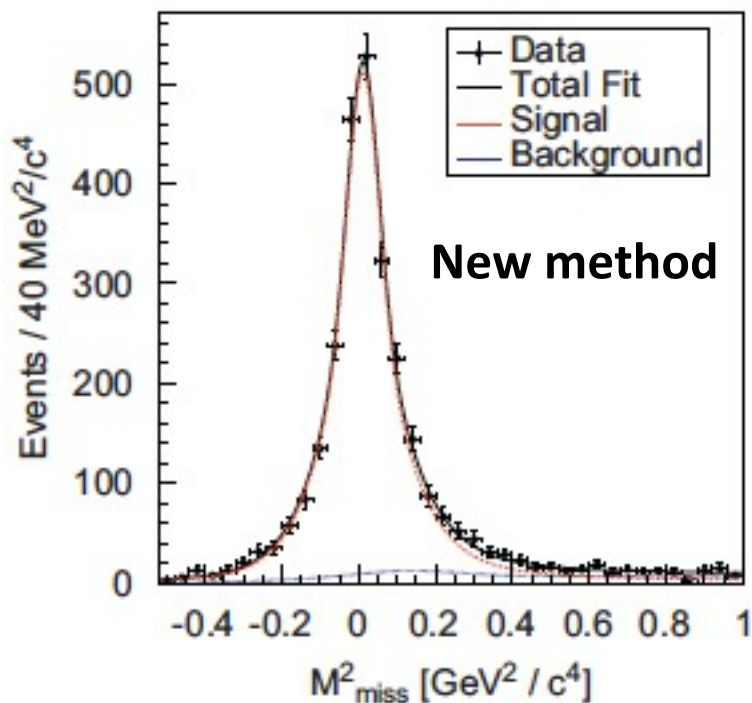
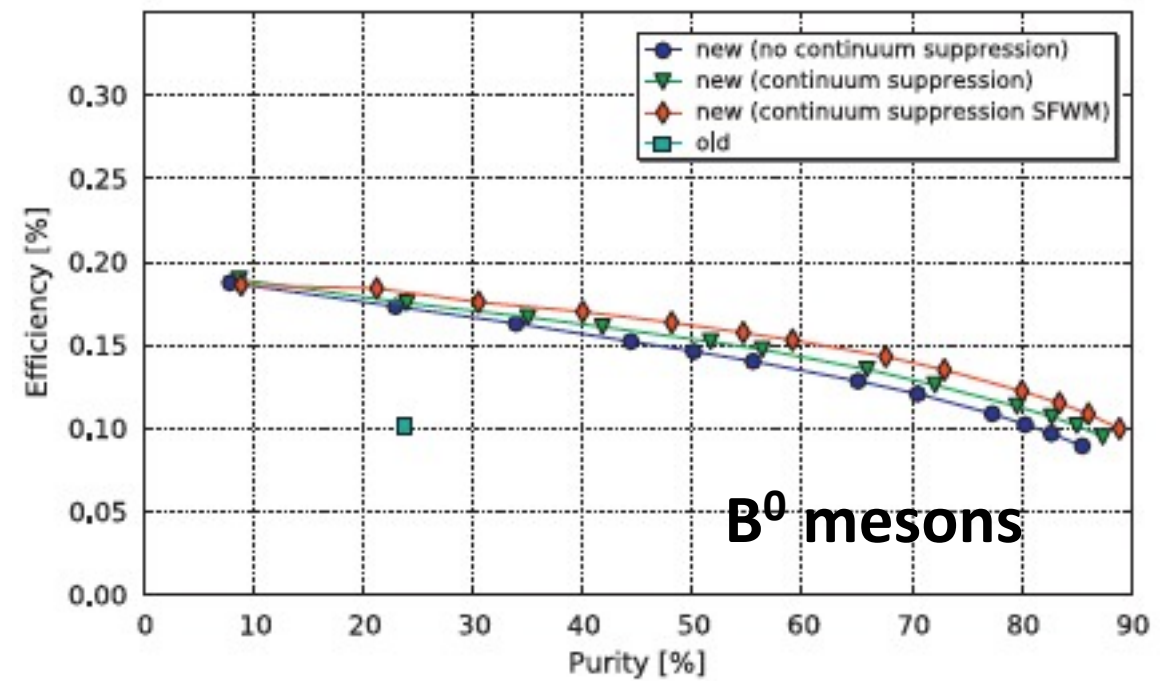
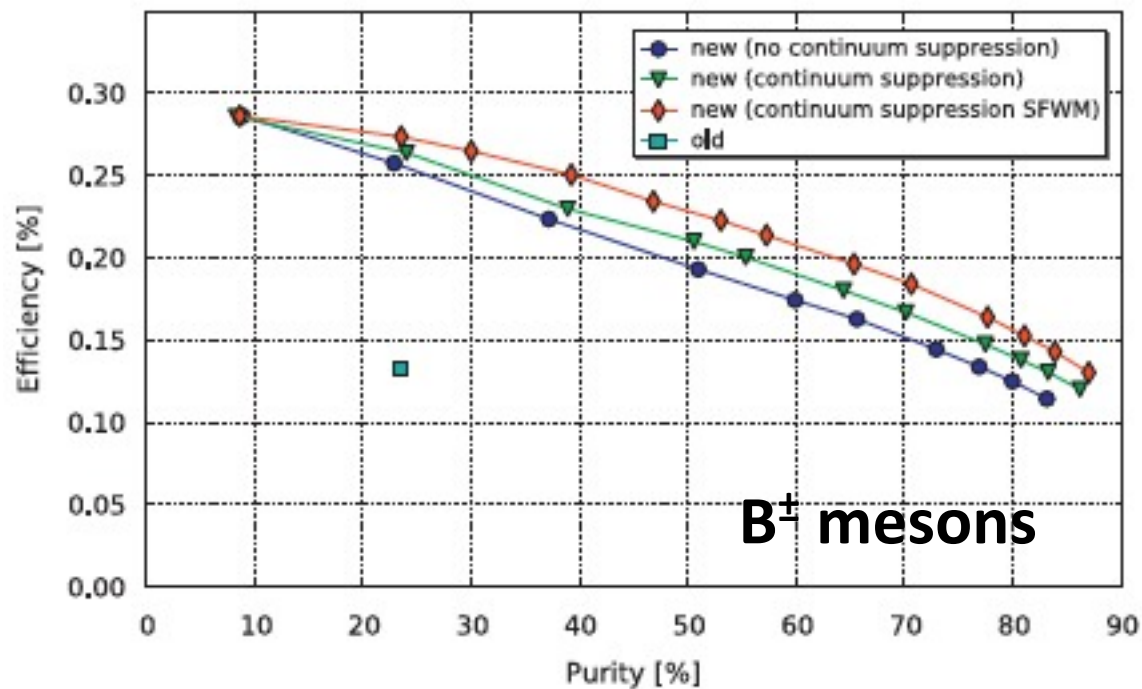
Integrated luminosity of B factories



$> 1 \text{ ab}^{-1}$
On resonance:
 $Y(5S): 121 \text{ fb}^{-1}$
 $Y(4S): 711 \text{ fb}^{-1}$
 $Y(3S): 3 \text{ fb}^{-1}$
 $Y(2S): 25 \text{ fb}^{-1}$
 $Y(1S): 6 \text{ fb}^{-1}$
Off reson./scan:
 $\sim 100 \text{ fb}^{-1}$

$\sim 550 \text{ fb}^{-1}$
On resonance:
 $Y(4S): 433 \text{ fb}^{-1}$
 $Y(3S): 30 \text{ fb}^{-1}$
 $Y(2S): 14 \text{ fb}^{-1}$
Off resonance:
 $\sim 54 \text{ fb}^{-1}$

B tagging Purity-Efficiency

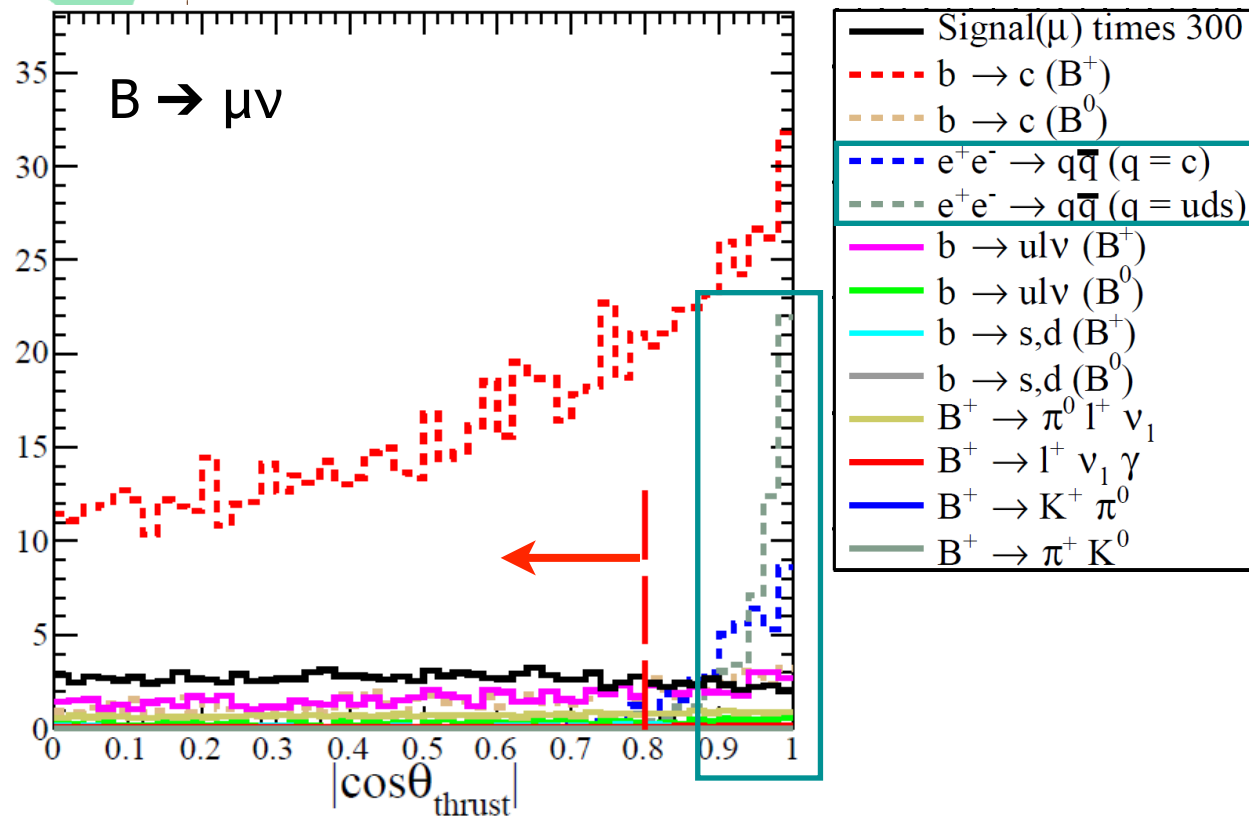
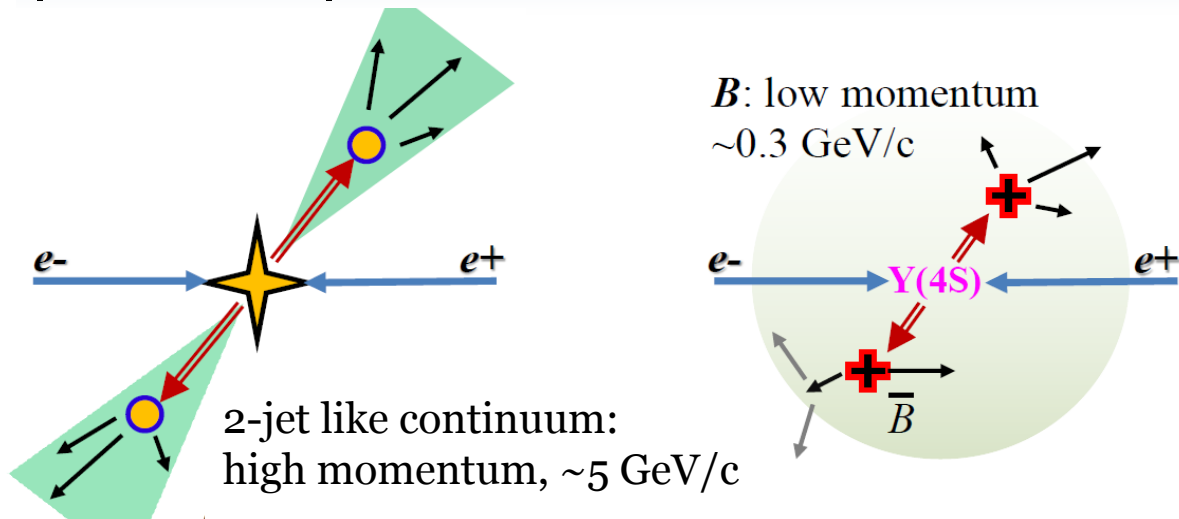


Missing mass distributions for $B^0 \rightarrow D^{*+} l^+ \nu_l$ decays of new and classical full reconstruction tool

$B^+ \rightarrow l^+ \nu_l$

Background Suppression

$|\cos\theta_{\text{thrust}}|$

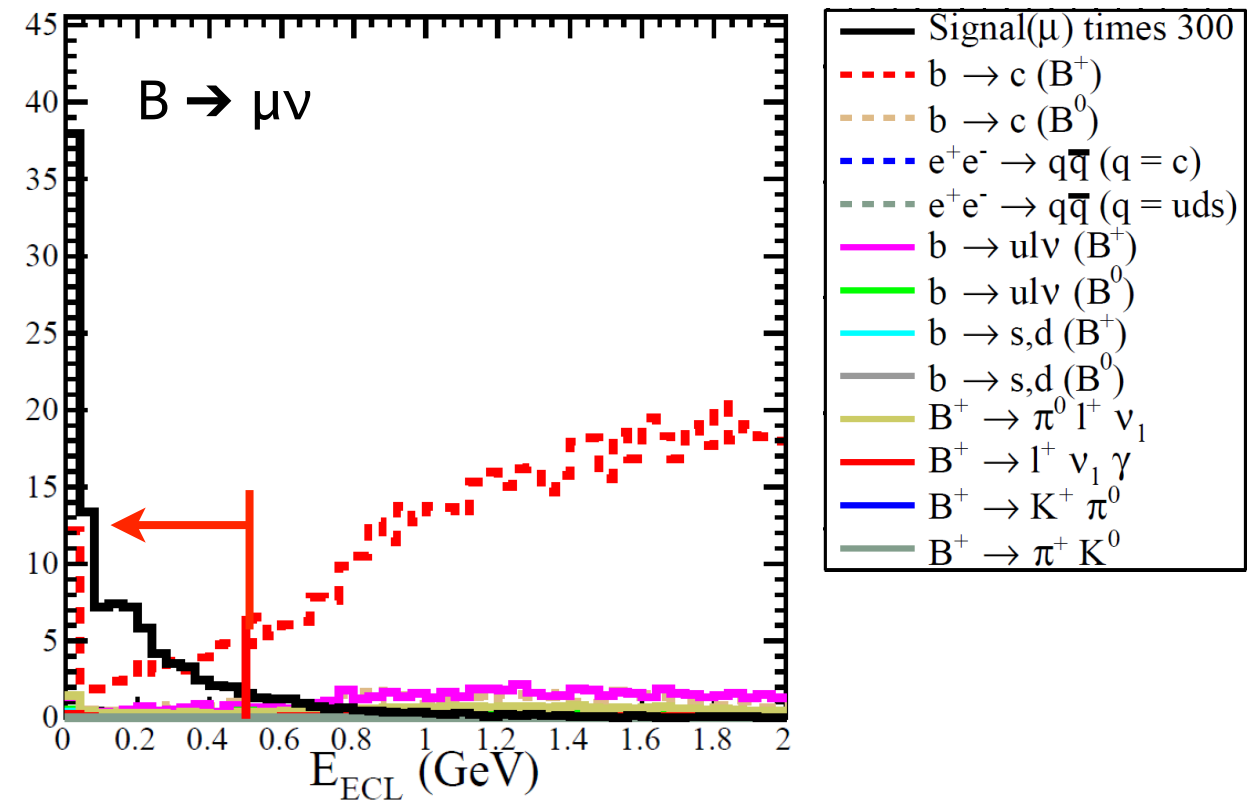


θ_{thrust} : angle between the thrust axis of B_{tag} particle and the lepton's momentum in CM frame

E_{ECL}

$$E_{\text{ECL}} = E_{\text{Total}} - E_{B_{\text{tag}}} - E_l$$

No extra energy deposits in the ECL
 (apart from the lepton and B_{tag})





Event Selection

Particle identity

$$L_e > 0.9$$

$$L_\mu > 0.9$$

Track quality

$$|dz| < 2.0 \text{ cm}$$

$$|dr| < 0.5 \text{ cm}$$

Continuum suppression

$$|\cos\theta_{\text{thrust}}| < 0.9 \text{ for e mode}$$

$$|\cos\theta_{\text{thrust}}| < 0.8 \text{ for } \mu \text{ mode}$$

Quality of tagged-B meson

$$|\Delta E| < 0.05 \text{ GeV}$$

$$M_{bc} > 5.27 \text{ GeV}/c^2$$

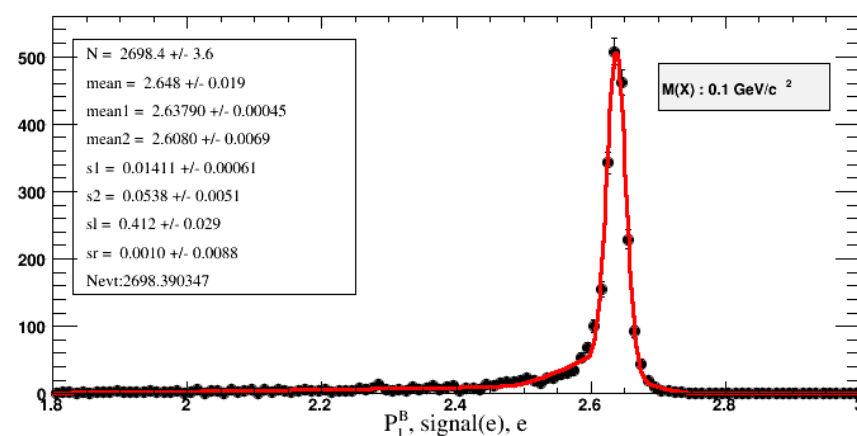
$$O_{NB} > 10^{-6}$$

E_{ECL} : remaining energy of ECL calorimeter

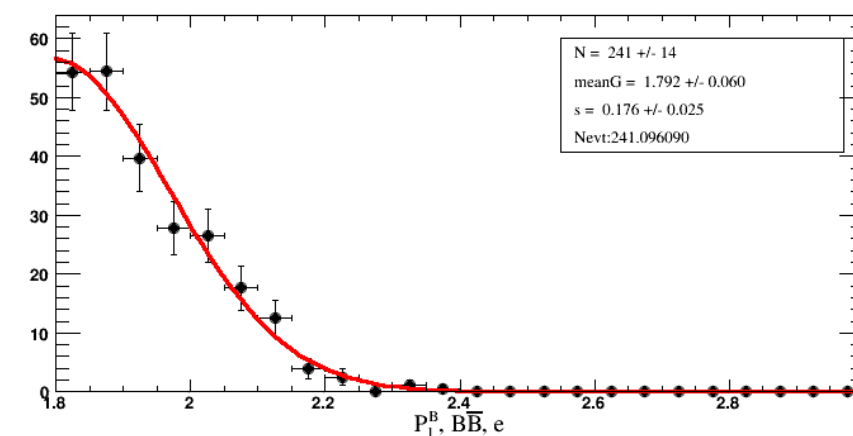
p_l^B : signal lepton's momentum in the signal B rest frame

p_l^B peak changes by mass of X^0

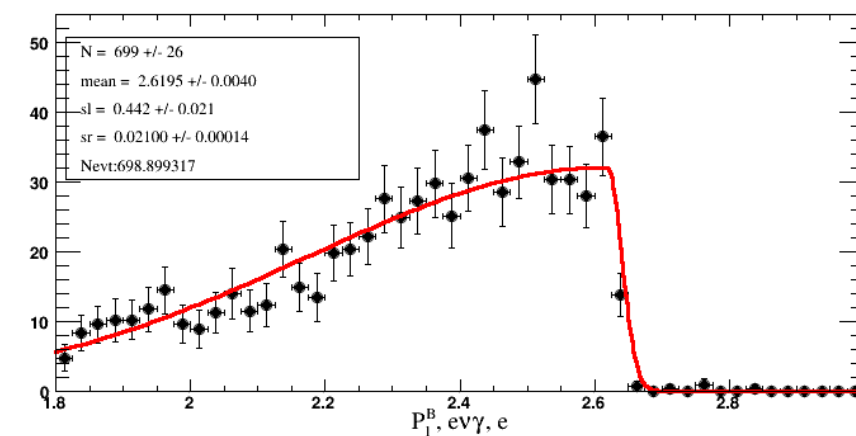
→ p_l^B cut should be optimized for each X^0 mass



Fitting signal



Fitting
background



Fitting
peaking background

$$B^+ \rightarrow I^+ X^0$$

Systematics

e mode

$M(X) (GeV/c^2)$	Statistical uncertainty	Total uncertainty
0.1	1.72%	6.1%
0.2	2.18%	6.2%
0.3	1.70%	6.1%
0.4	1.73%	6.1%
0.5	1.53%	6.0%
0.6	1.74%	6.1%
0.7	1.71%	6.1%
0.8	1.71%	6.1%
0.9	1.74%	6.1%
1.0	1.74%	6.1%
1.1	1.63%	6.0%
1.2	1.74%	6.1%
1.3	1.83%	6.1%
1.4	1.72%	6.1%
1.5	1.75%	6.1%
1.6	1.74%	6.1%
1.7	1.80%	6.1%
1.8	1.75%	6.1%

μ mode

$M(X) (GeV/c^2)$	Statistical uncertainty	Total uncertainty
0.1	1.78%	6.0%
0.2	1.80%	6.1%
0.3	1.80%	6.0%
0.4	1.81%	6.1%
0.5	1.87%	6.1%
0.6	1.88%	6.1%
0.7	1.82%	6.1%
0.8	1.80%	6.1%
0.9	1.83%	6.1%
1.0	1.83%	6.1%
1.1	1.79%	6.0%
1.2	1.83%	6.1%
1.3	1.84%	6.1%
1.4	1.82%	6.1%
1.5	1.82%	6.1%
1.6	1.82%	6.1%
1.7	1.83%	6.1%
1.8	1.81%	6.1%

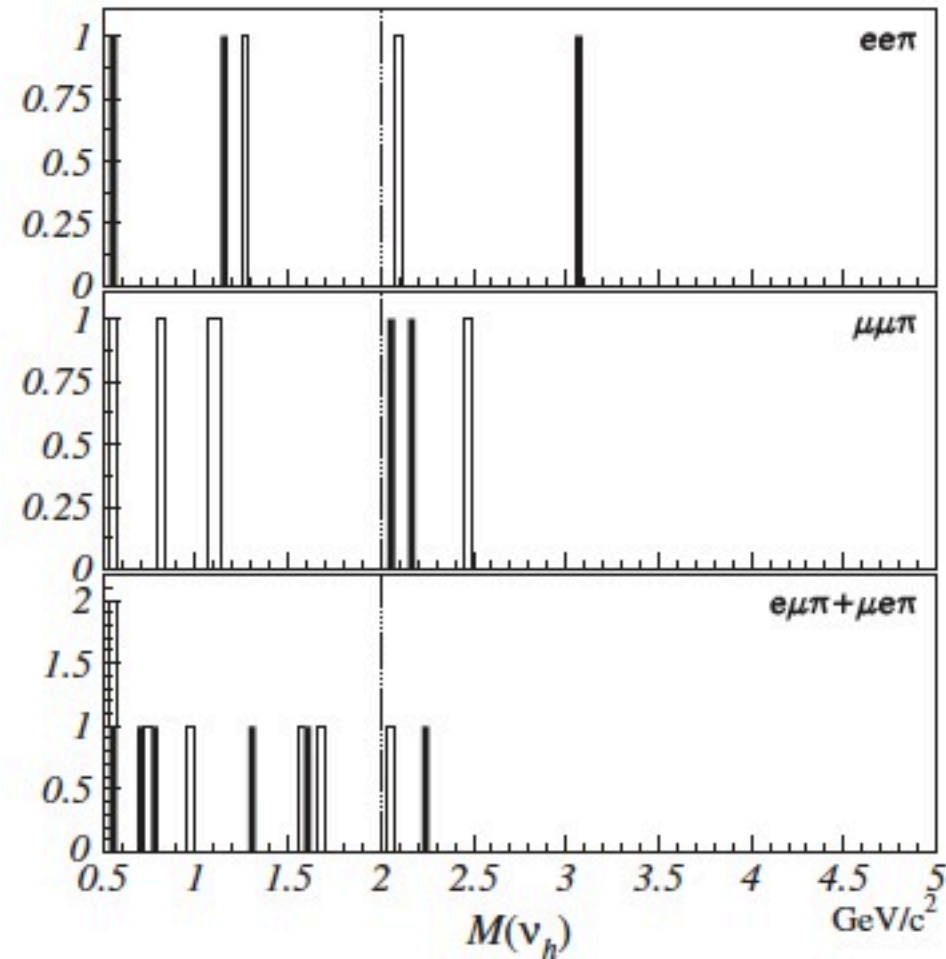
B → (X)lv_h

Signal Extraction

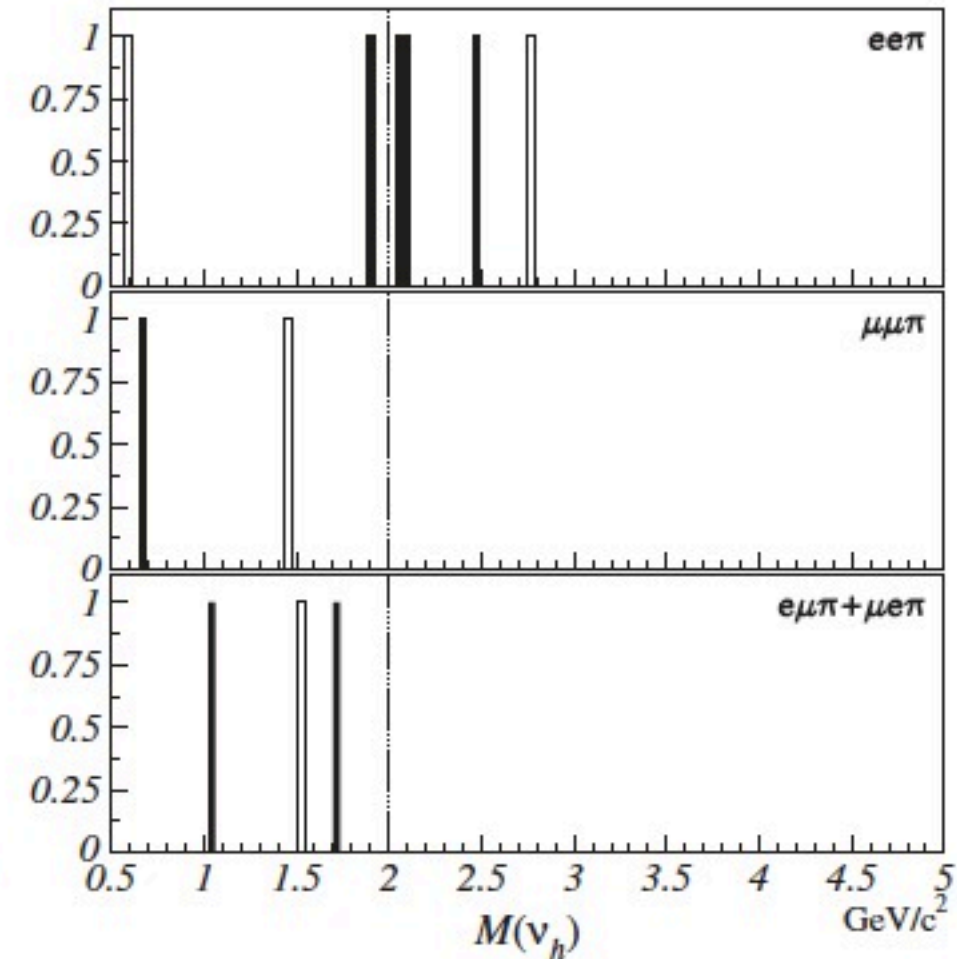
Obtained yield and expectation from MC

mode	MC expected	Data
$e\bar{e}\pi$	1.7 ± 0.7	6 ± 2.4
$\mu\bar{\mu}\pi$	2.3 ± 0.9	2 ± 1.4
$e\bar{\mu}\pi + \mu\bar{e}\pi$	4.0 ± 1.2	3 ± 1.7

generic MC (unscaled)



data



D. Gorbunov and M. Shaposhnikov, JHEP 0710, 015 (2007)

$$n(\nu_h) = 2N_{BB} \underbrace{B(B \rightarrow \nu_h)}_{\text{green}} \underbrace{B(\nu_h \rightarrow l\pi)}_{\text{purple}} \frac{m\Gamma}{p} \int \varepsilon(x) dx$$

$$= \underbrace{|U_\alpha|^2}_{\text{green}} \underbrace{|U_\beta|^2}_{\text{purple}} 2N_{BB} \underbrace{f_1(m)}_{\text{green}} \underbrace{f_2(m)}_{\text{purple}} \frac{m}{p} \int \varepsilon(x) dx$$

Number of neutrinos detected
→ Expect upper limit of branching fraction

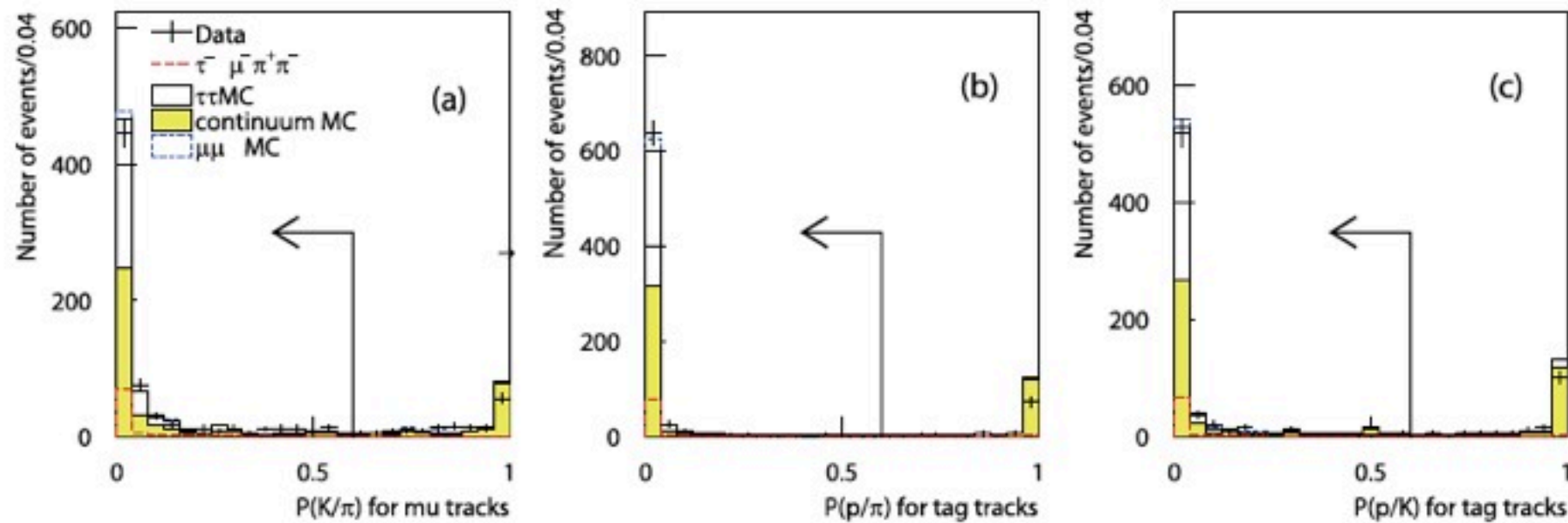


Fig. 1. (a) $\mathcal{P}(K/\pi)$ for muon tracks, (b) $\mathcal{P}(p/\pi)$ and (c) $\mathcal{P}(p/K)$ for hadronic tags, for $\tau^- \rightarrow \mu^- \pi^+ \pi^-$ candidate events. Signal MC ($\tau^- \rightarrow \mu^- \pi^+ \pi^-$) distributions are normalized arbitrarily while the background MC distributions are normalized to the data luminosity. The selected regions are indicated by arrows.

Table 1

Selection criteria for kaon identification $\mathcal{P}(K/\pi)$ and magnitude of thrust (T).

Mode	$\mathcal{P}(K/\pi)$	T
$\tau \rightarrow \mu \pi \pi$	—	$0.90 < T < 0.98$
$\tau \rightarrow \mu K \pi$	> 0.9	$0.92 < T < 0.98$
$\tau \rightarrow \mu K K$	> 0.8	$0.92 < T < 0.98$
$\tau \rightarrow e \pi \pi$	—	$0.90 < T < 0.97$
$\tau \rightarrow e K \pi$	> 0.8	$0.90 < T < 0.97$
$\tau \rightarrow e K K$	> 0.6	$0.90 < T < 0.98$

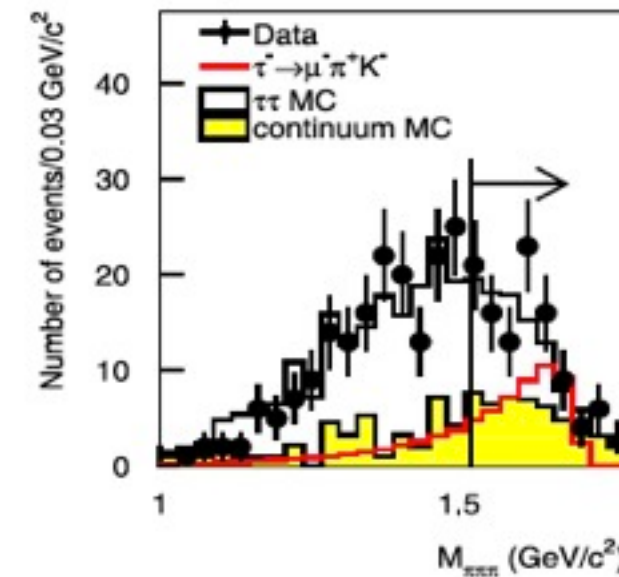
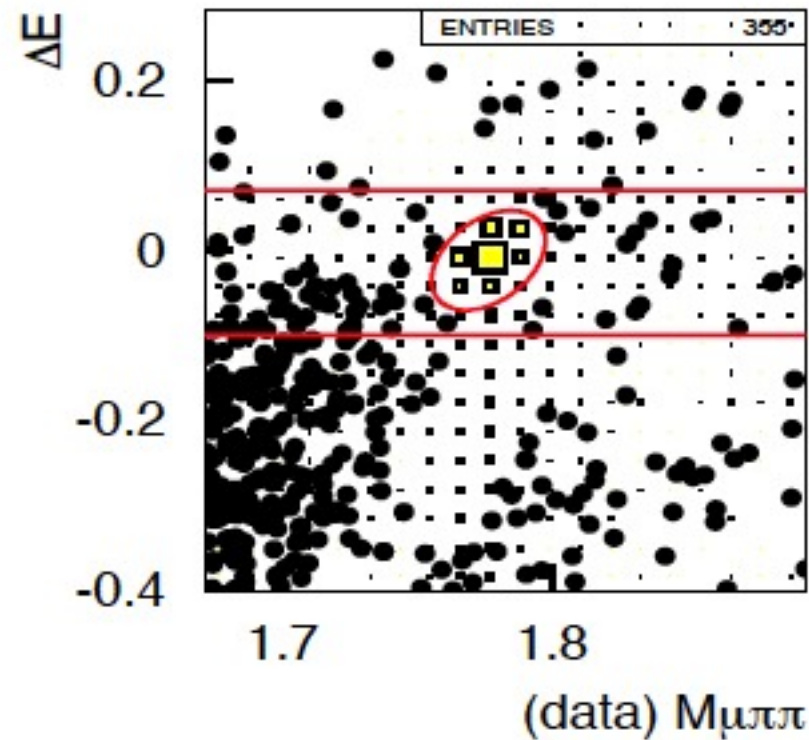
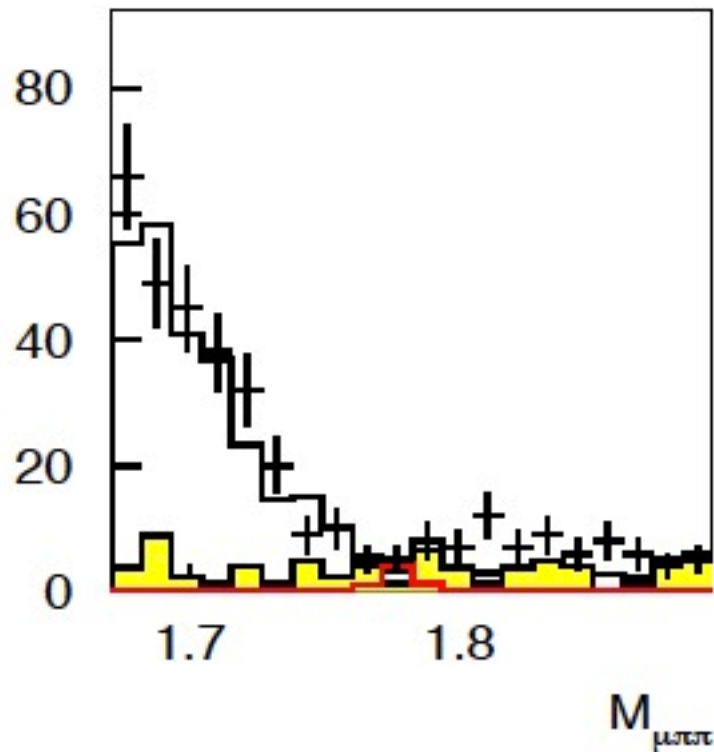
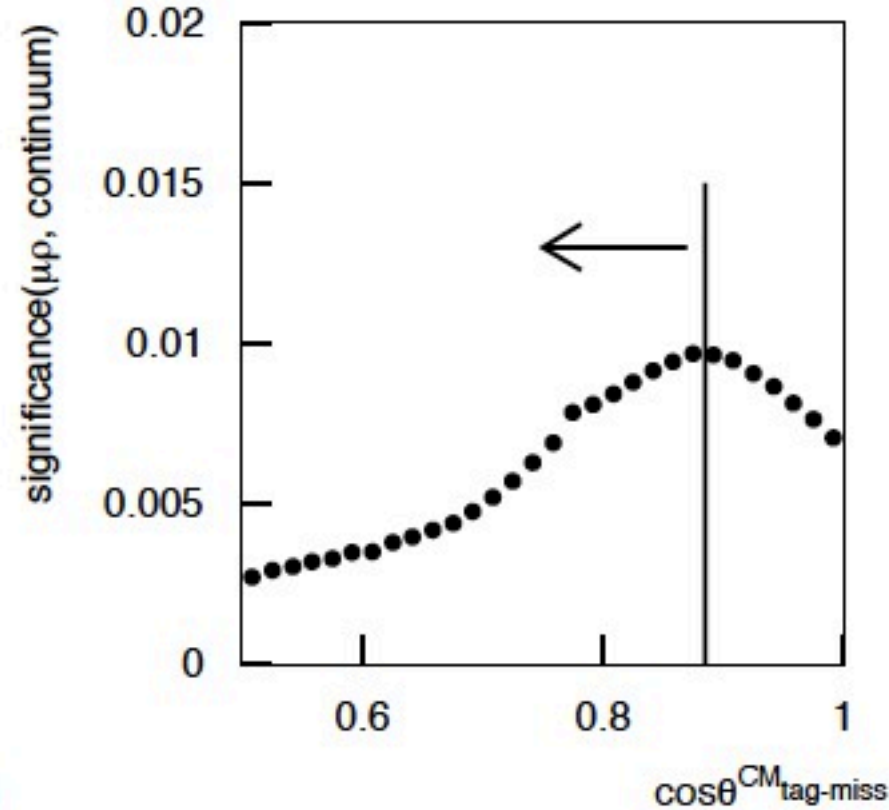
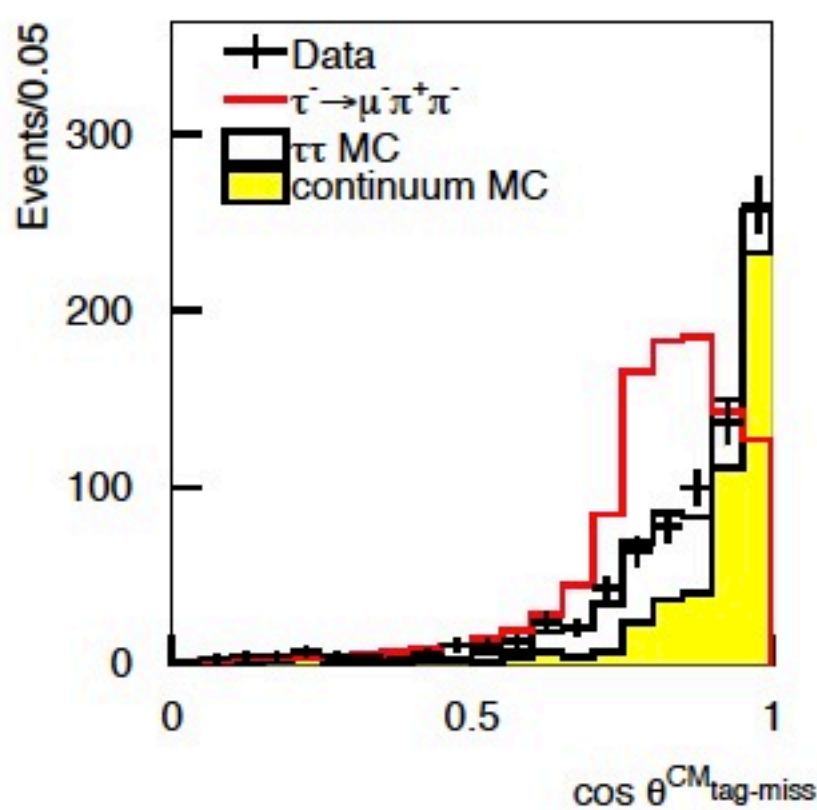


Fig. 2. Invariant mass distribution of three charged tracks on the signal side with the pion mass assigned to each track ($M_{\pi\pi\pi}$) for $\tau^- \rightarrow \mu^- \pi^+ K^-$ candidate events. Signal MC ($\tau^- \rightarrow \mu^- \pi^+ K^-$) distributions are normalized arbitrarily while the background MC distributions are normalized to the data luminosity. The selected regions are indicated by the arrow.

$\tau \rightarrow l^+ h h'$

Opening angle and Signal region



Invariant mass distribution and scatter plot btw $M_{\mu\pi\pi}$ and ΔE after continuum reduction selection for the $\mu\pi\pi$ mode.

red : signal MC
 open : generic $\tau\tau$ MC
 yellow filled : continuum MC
 crossed points : data