

## Experiment: Status and Challenges

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### Outline

1. General
2. Hadronic Vacuum Polarization (HVP)
3. How real is the accuracy?
4. Hadronic LbL
5. Conclusions

## General

Major achievements coming from:

### 1. Energy Frontier:

- LHC and Higgs discovery
- (before that) Tevatron studied  $t$  quark physics and QCD
- LEP and Standard Model success

### 2. Intensity/Precision Frontier:

- E821 –  $a_\mu$ ;  $a_e$  and  $\alpha$
- $\phi$  and B factories –  $R$  studies, CPV,  
exotic  $c\bar{c}$  and  $b\bar{b}$  states
- Proton radius

## Muon Anomalous Magnetic Moment

$$\vec{\mu} = g \frac{e}{2m} \vec{s}, \quad a = (g - 2)/2.$$

In Dirac theory for pointlike particles  $g = 2$ ,  
higher-order effects or new physics  $\Rightarrow g \neq 2$

Any significant difference of  $a_\mu^{\text{exp}}$  from  $a_\mu^{\text{th}}$  indicates  
New Physics beyond the Standard Model.

$a_\mu$  is much more sensitive to new physics effects than  $a_e$ :  
the gain is usually  $\sim (m_\mu/m_e)^2 \approx 4.3 \cdot 10^4$ .

$$a_\mu^{\text{th}} = a_\mu^{\text{SM}} + a_\mu^{\text{NP}}, \quad a_\mu^{\text{SM}} = a_\mu^{\text{QED}} + a_\mu^{\text{EW}} + a_\mu^{\text{had}}.$$

## Experimental Status of $a_l$

$$a_e = 1159652180.73(28) \times 10^{-12} \quad 0.24 \times 10^{-9}$$

D. Hanneke et al., PRL 100, 120801 (2008)  
QED test or  $\alpha$  determination

$$a_\mu = 116592080(63) \times 10^{-11} \quad 0.54 \times 10^{-6}$$

G.W. Bennett et al. (E821), PRD 73, 072003 (2006)  
Sensitive test of the Standard Model

$$a_\tau = -0.018(17) \text{ or } -0.052 < a_\tau < 0.013 \text{ 95%CL}$$

J. Abdallah et al. (DELPHI), EPJ C 35, 159 (2004)  
Theory:  $117721(5) \times 10^{-8}$ , SE, M. Passera, MPL A 22, 159 (2007)

## Update of the Experimental Value of $a_\mu$

E821 at BNL (2006):

$$a_{\mu^+}^{\text{exp}} = (11659204 \pm 6 \pm 5) \times 10^{-10}$$
$$a_{\mu^-}^{\text{exp}} = (11659215 \pm 8 \pm 3) \times 10^{-10}$$

Their average assuming CPT and with account of correlations:

$$a_\mu^{\text{exp}} = (11659208.9 \pm 5.3 \pm 3.3) \times 10^{-10}$$

These values take into account the newest CODATA value  
for the  $\mu/p$  magnetic ratio  $\lambda = 3.183345137 \pm 85$ .

The induced change in  $a_\mu$  is  $+0.92 \times 10^{-10}$ .

P.J. Mohr, B.N. Taylor, and D.B. Newell, Rev. Mod. Phys. 80, 633 (2008)

## QED Contribution $a_\mu^{\text{QED}}$

$$\begin{aligned}
 a_\mu^{\text{QED}} \cdot 10^{10} = \sum C_i \left(\frac{\alpha}{\pi}\right)^i = & 11614097.3 \text{ (1-loop)} & 1 \text{ diagram} \\
 & + 41321.8 \text{ (2-loop)} & 9 \\
 & + 3014.2 \text{ (3-loop)} & > 100 \\
 & + 38.1 \text{ (4-loop)} & > 1000 \\
 & + 0.4 \text{ (5-loop)} & > 20000
 \end{aligned}$$

$\alpha^3$  terms known analytically (S. Laporta, E. Remiddi, 1993),

$\alpha^4$  terms – numerically (T. Kinoshita et al., 2003-2008),

$L \log \alpha^5$  (TK et al., 2005,2007; A.L. Kataev, 2006, K. Chetyrkin et al., 2008):

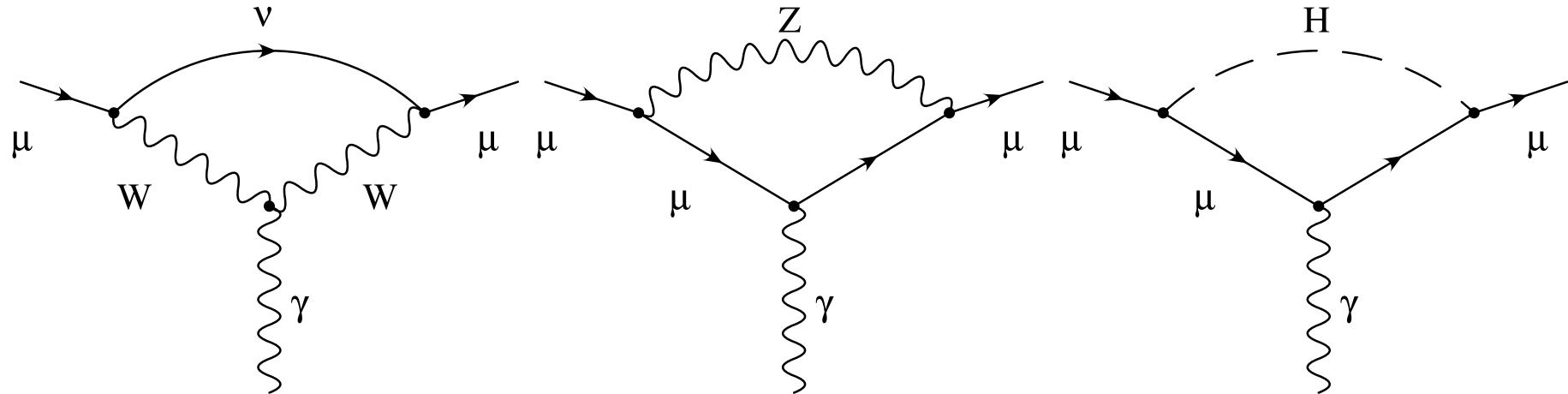
$$a_\mu^{\text{QED}} = (116584719.4 \pm 1.4) \cdot 10^{-11}.$$

From the latest value of  $a_e$  (D. Hanneke et al., 2008; T. Kinoshita, 2012):

$$\alpha^{-1} = 137.035999173(34), a_\mu^{\text{QED}} = (116584718.09 \pm 0.14 \pm 0.04) \cdot 10^{-11}.$$

The errors are due to: a/  $\mathcal{O}(\alpha^5)$ , b/  $\alpha$

## Electroweak contribution $a_\mu^{\text{EW}}$



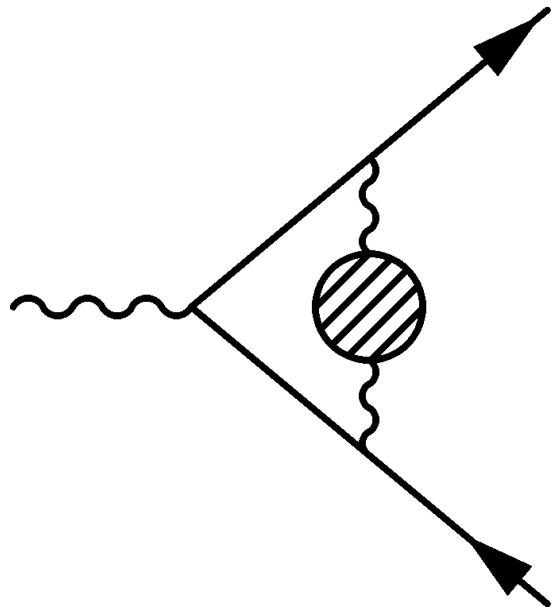
One-loop electroweak contributions

Authors	Year	$a_\mu^{\text{EW}}, 10^{-10}$
..., ..., ...	1972	19.5
A. Czarnecki et al.	1996	$15.2 \pm 0.4$
A. Czarnecki et al.	2002	$15.4 \pm 0.1 \pm 0.2$

The errors are due to: a/ hadr. loops, b/  $M_H, M_t$ , 3-loop effects.

### Hadronic contribution $a_\mu^{\text{had}}$

$$a_\mu^{\text{had}} = a_\mu^{\text{had,LO}} + a_\mu^{\text{had,HO}} + a_\mu^{\text{had,LBL}}$$

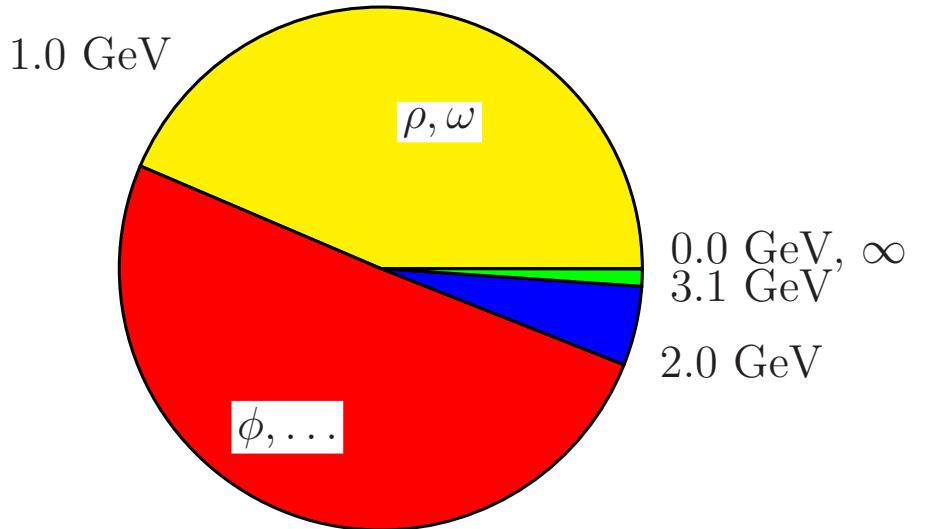
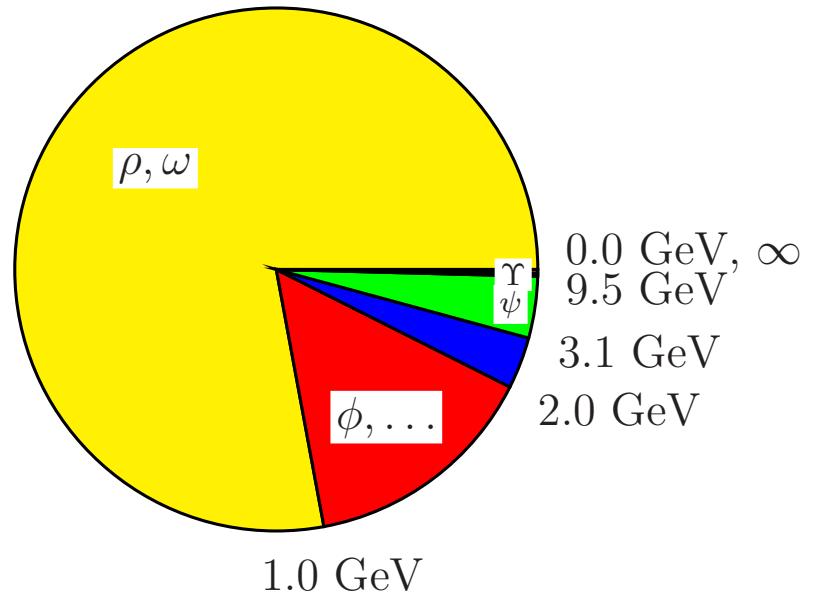


$a_\mu^{\text{had,LO}} = \left(\frac{\alpha m_\mu}{3\pi}\right)^2 \int_{4m_\pi^2}^\infty ds \frac{R(s) \hat{K}(s)}{s^2}$ , C. Bouchiat, L. Michel, Bouchiat, 1961; M. Gourdin, E. de Rafael, 1969

$$R(s) = \frac{\sigma(e^+ e^- \rightarrow \text{hadrons})}{\sigma(e^+ e^- \rightarrow \mu^+ \mu^-)},$$

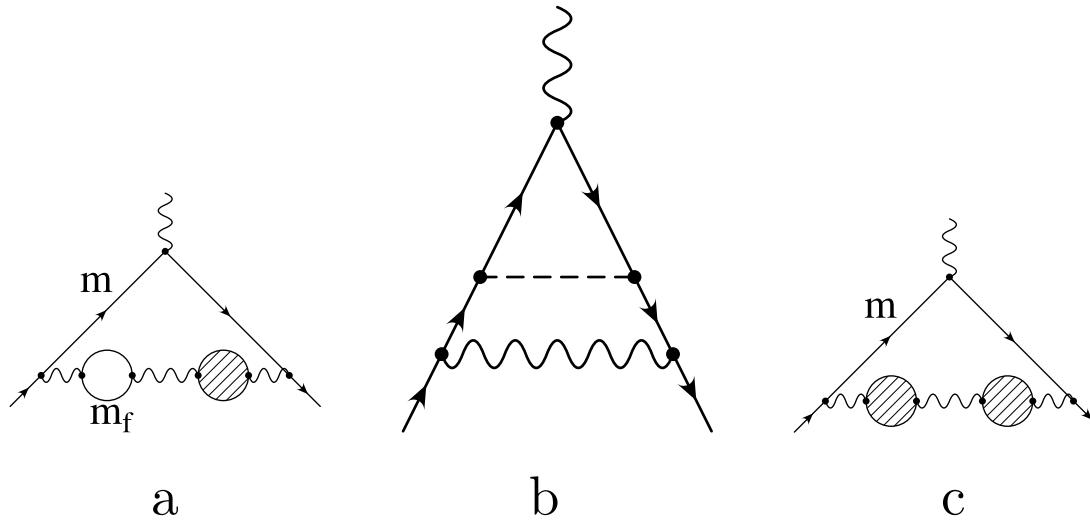
$\hat{K}(s)$  grows from 0.63 at  $s = 4m_\pi^2$  to 1 at  $s \rightarrow \infty$ ,  
 $1/s^2$  emphasizes low energies, particularly  $e^+ e^- \rightarrow \pi^+ \pi^-$ .  
 $a_\mu^{\text{had,LO}} \sim 700 \cdot 10^{-10} \Rightarrow$  accuracy better than 1% needed

## Contributions of Various Energy Ranges to $a_\mu^{\text{had,LO}}$



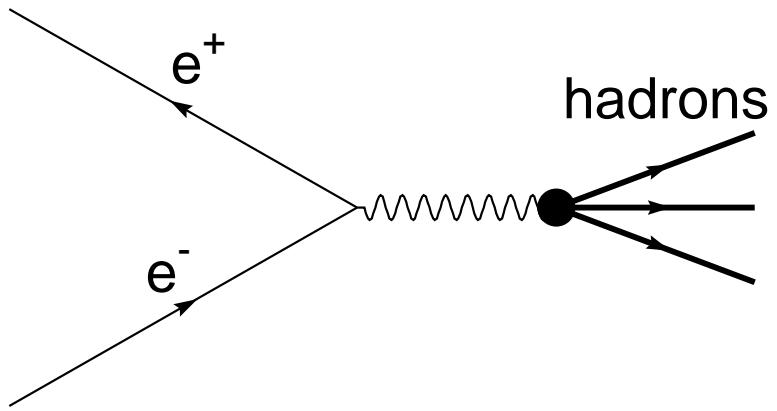
More than 72% of  $a_\mu^{\text{had,LO}}$  come from  $e^+e^- \rightarrow \pi^+\pi^-$  and  
more than 90% from the energy range below 2 GeV

## Higher Order Hadronic Contributions $a_\mu^{\text{had,HO}}$

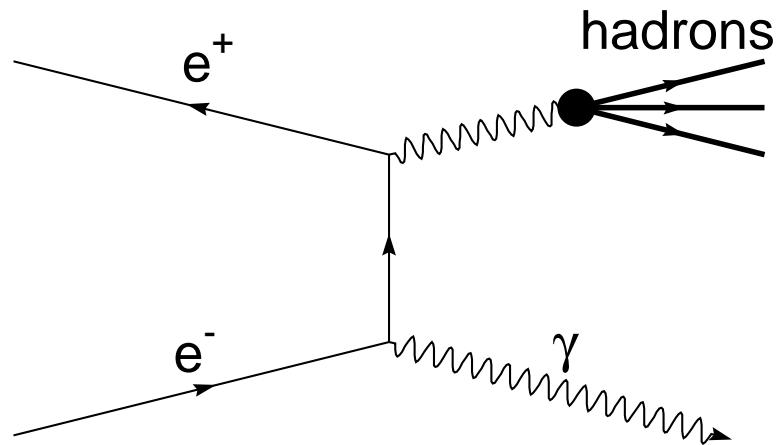


The contributions of all 3 graphs can be calculated in terms of the  $\int R(s)G(s)ds/s^{2(3)}$ , where  $G(s)$  is a smooth function of  $s$ , so that the low energy range again dominates the integral. Several calculations agree. The recent value is (F. Jegerlehner and R. Szafron, 2011):

$$a_\mu^{\text{had,HO}} = (-9.98 \pm 0.10) \cdot 10^{-10}.$$

**Scan and ISR**

Scan



ISR

Scan can provide larger data samples at fixed energy

ISR benefits from the same systematics and flat acceptance,  
but may suffer from more complicated radiative effects,  
a broad range of collision energies

## Relation of Scan and ISR Center-of-mass Energy

If the nominal c.m. energy of the collider is  $\sqrt{s}$  and initial electron or positron emit a photon with energy  $E_\gamma$ , the effective c.m. energy of the collision is

$$\sqrt{s'} = \sqrt{s - 2E_\gamma\sqrt{s}}$$

$\sqrt{s}$ , GeV	$\sqrt{s'}$ , GeV	$E_\gamma$ , GeV
1.02 ( $m_\phi$ )	0.770 ( $m_\rho$ )	0.22
10.58 ( $m_{\Upsilon(4S)}$ )	0.770 ( $m_\rho$ )	5.26
10.58 ( $m_{\Upsilon(4S)}$ )	3.1 ( $m_{J/\psi}$ )	4.84

## How Is $R$ Measured at Low Energy ( $\sqrt{s} < 2$ GeV)?

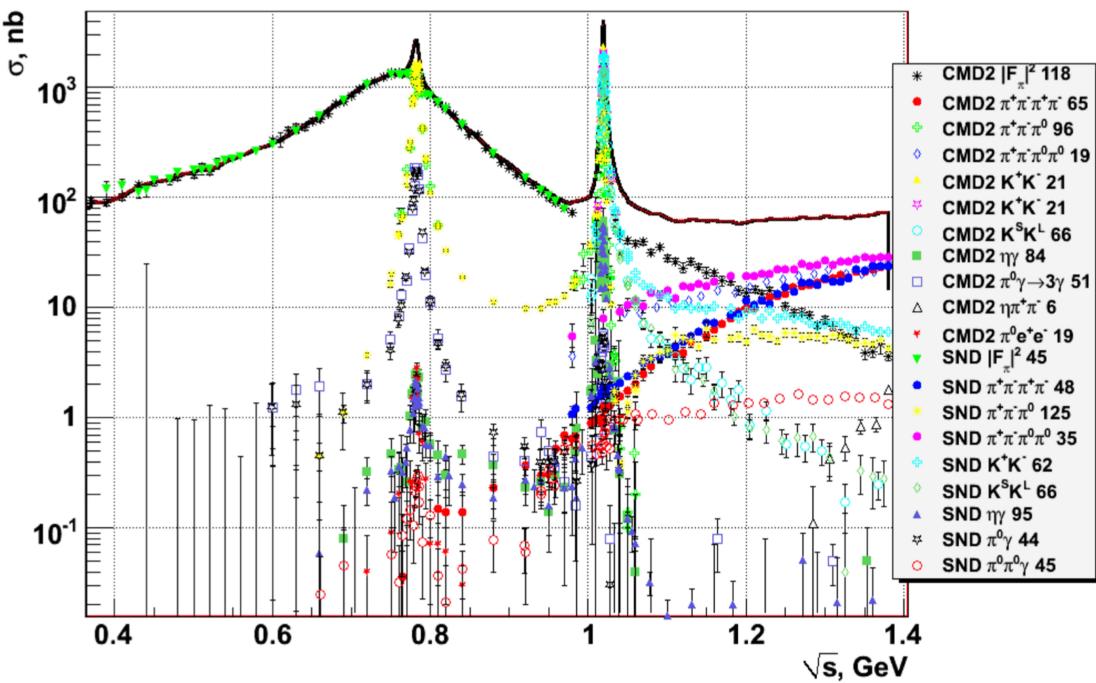
- The cross section rapidly changes with energy because one is far from asymptotics and there are many resonances
- There is no good theoretical model to find  $\epsilon$
- Exclusive approach: specific final states studied separately  $(\pi^+\pi^-, K^+K^-, K_SK_L, , n\pi, K\bar{K}m\pi, p\bar{p}, n\bar{n}, \dots)$
- The cross sections measured summed
- Important not to miss some final states

## *R* Measurement at Low Energies (< 5 GeV)

The main players in the field:

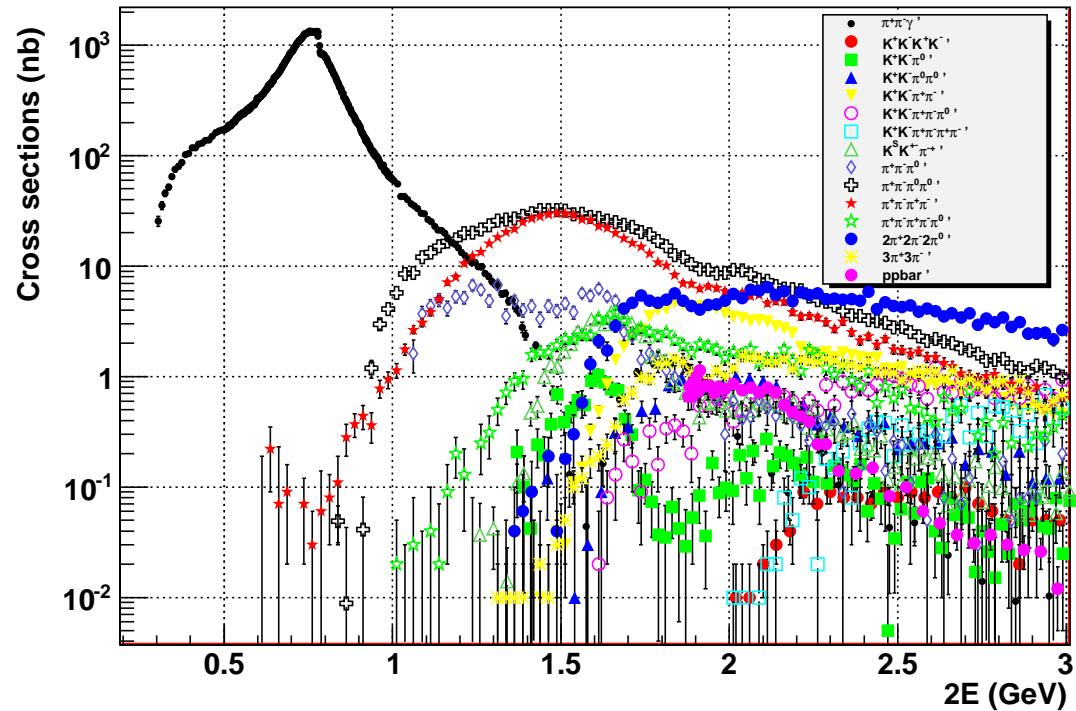
- Novosibirsk – scan (CMD-2/SND at VEPP-2M,  $0.36 < \sqrt{s} < 1.4$  GeV, CMD-3/SND at VEPP-2000,  $2m_\pi < \sqrt{s} < 2.0$  GeV)
- Frascati – ISR (KLOE/KLOE-2 at DAFNE,  $2m_\pi < \sqrt{s} < 1.02$  GeV)
- Beijing – scan/ISR (BESII at  $2.0 < \sqrt{s} < 5.0$  GeV, BESIII at  $2m_\pi < \sqrt{s} < 4.6$  GeV)
- SLAC – ISR (BaBar at PEPII,  $2m_\pi < \sqrt{s} < 5$  GeV)
- KEK – ISR (Belle at KEKB,  $2m_\pi < \sqrt{s} < 5$  GeV, BelleII at SuperKEKB,  $2m_\pi < \sqrt{s} < 5$  GeV)

## Current Status of $R$ Below 2 GeV – Scan



Syst. errors: (0.6-1.0)% for  $\pi^+\pi^-$ , (5-15)% for multibody states  
 Cross sections vary by 4-5 orders!

## Current Status of $R$ Below 2 GeV – ISR



Syst. errors: 0.5% for  $\pi^+\pi^-$ , (2-15)% for multibody states  
 BaBar - all energies, Belle mainly in the charm region

## Progress of Data-driven $a_\mu^{\text{had,LO}}$

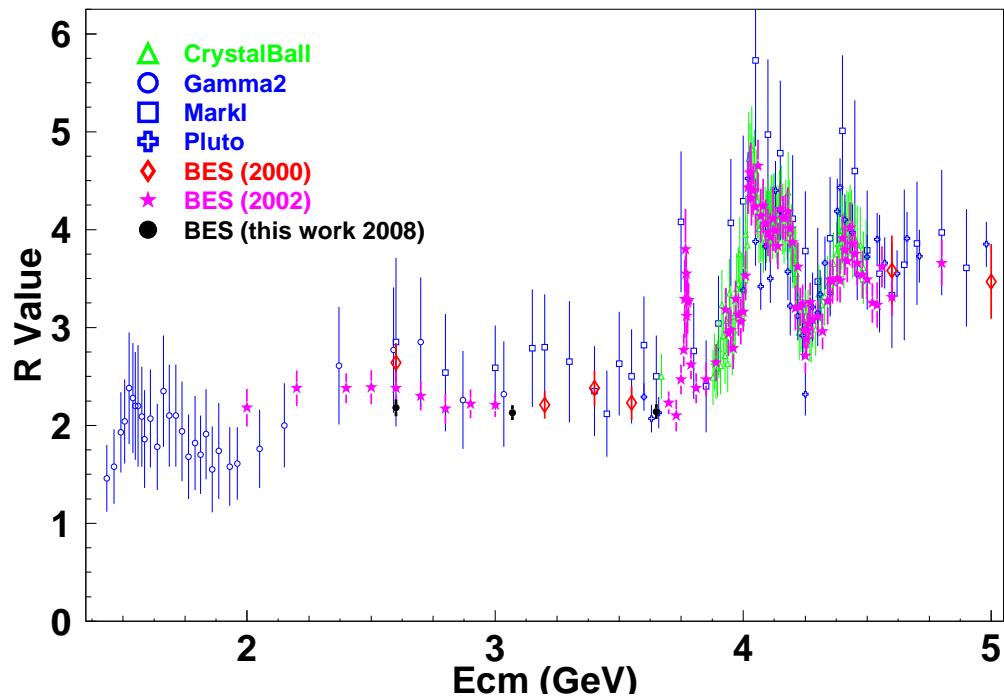
Author	Date	$a_\mu^{\text{had,LO}}, 10^{-10}$
V. Barger	1975	$663 \pm 85$
SE, FJ	1994	$702 \pm 15$
M. Davier, SE, ...	2003	$696.3 \pm 7.2$
FJ, A. Nyffeler	2009	$690.6 \pm 5.3$
M. Davier et al.	2011	$692.3 \pm 4.2$

Impressive progress due to the new data

## How Is $R$ Measured at High Energy ( $2 < \sqrt{s} < 5$ GeV)?

- Inclusive approach: all multihadronic events selected
- Background determined ( $\tau$  decays,  $\gamma\gamma$ , QED)
- $\int \mathcal{L} dt$  found
- $\epsilon$  found from MC (LUND, PYTHIA, LUARLW)
- Radiative corrections applied: ISR (PHOKHARA), FSR (PHOTOS)

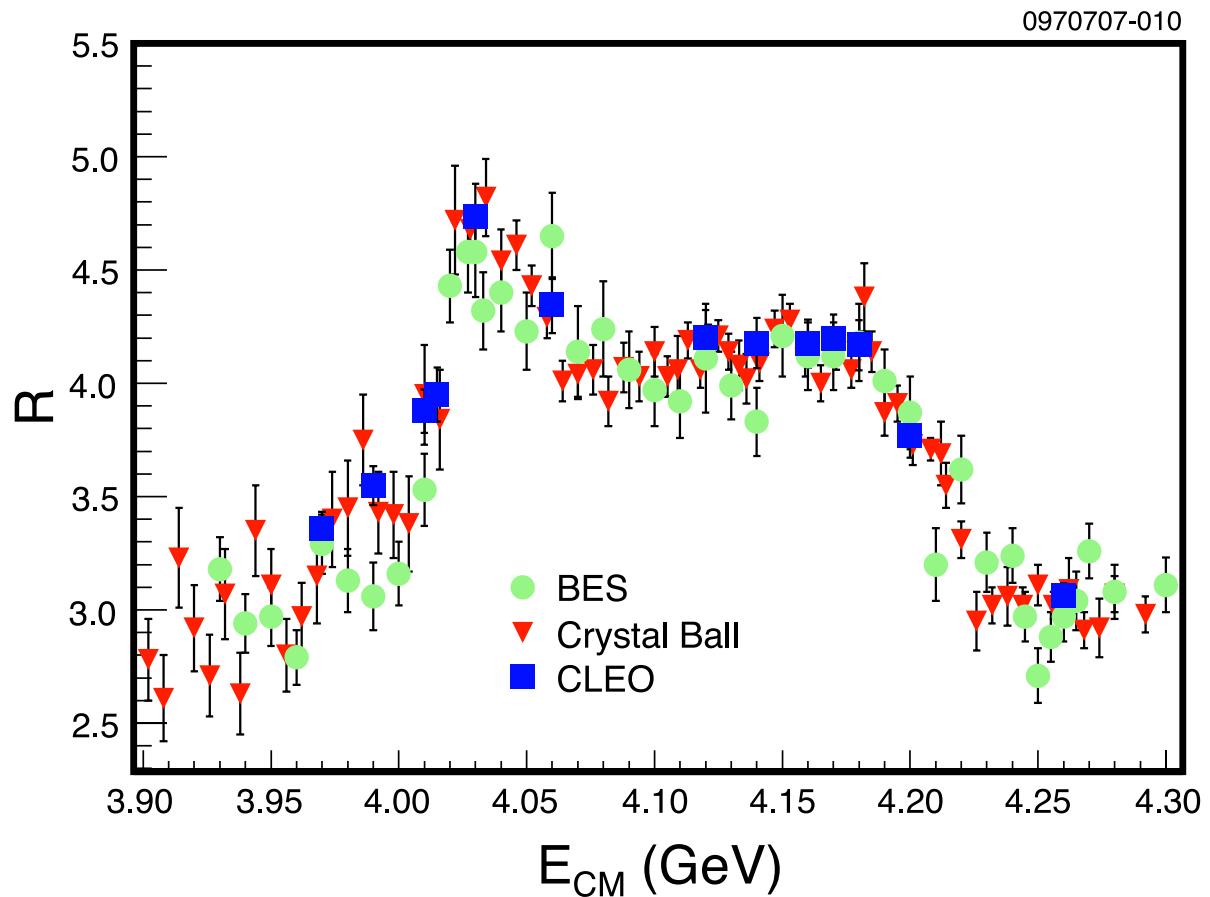
## $R$ Measurement Below 5 GeV



Dominated by BES: stat. errors (3-5)%, syst. errors (5-8)%

J.Z. Bai et al., Phys.Rev.Lett. 84 (2000) 594, Phys.Rev.Lett. 88 (2002) 101802;  
M. Ablikim et al., Phys.Rev.Lett. 97 (2006) 262001, Phys.Lett. B677 (2009) 239

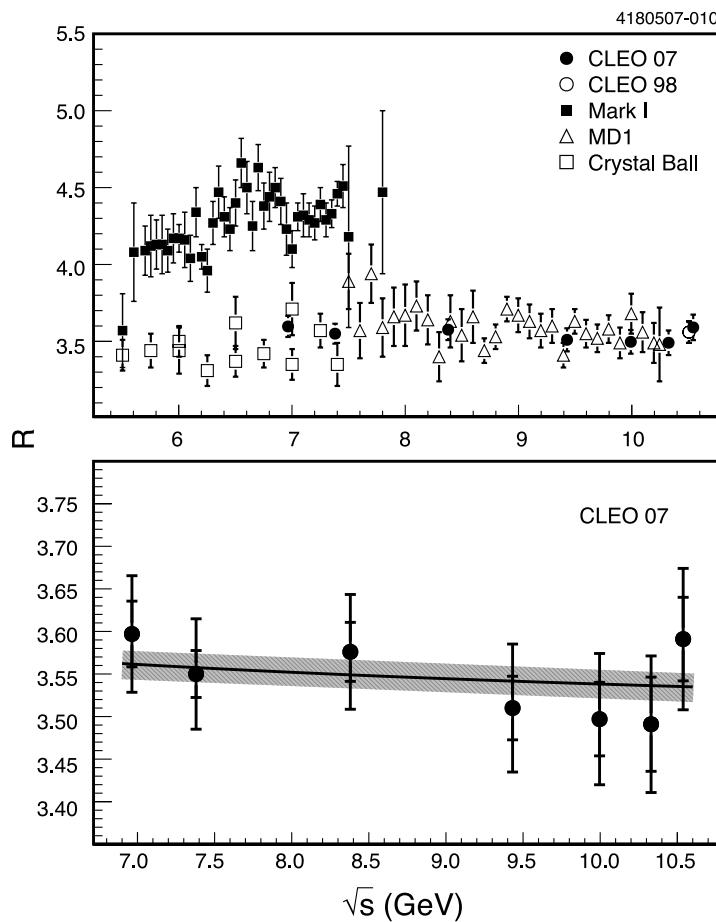
## *R* Measurement by CLEO – I



CLEO-c: syst. errors (5.2-6.1)%

D. Cronin-Hennessy et al., Phys. Rev. D80 (2009) 072001

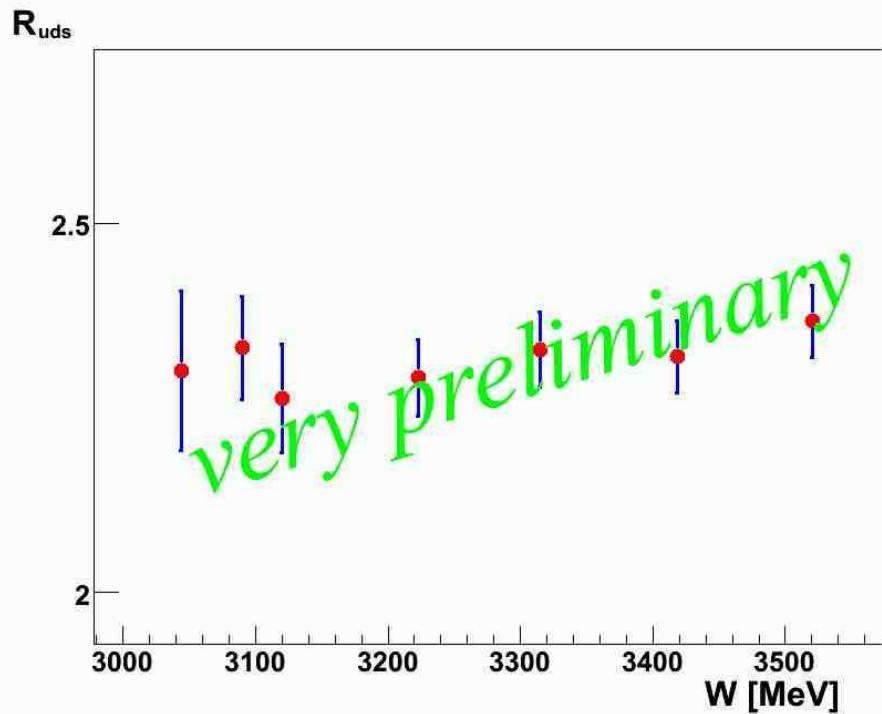
## *R* Measurement by CLEO – II



CLEO3: syst. errors (1.7-2.3)%

D. Besson et al., Phys. Rev. D76 (2007) 072008

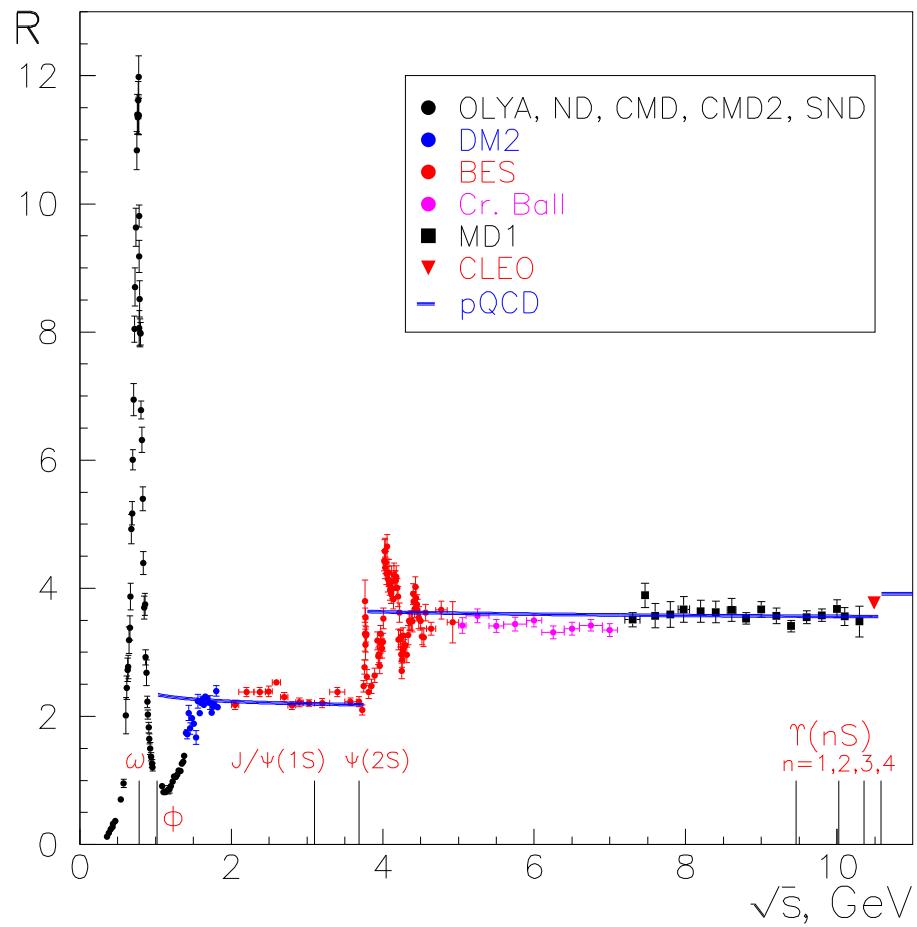
## $R$ Measurement at KEDR from 3.1 to 3.7 GeV



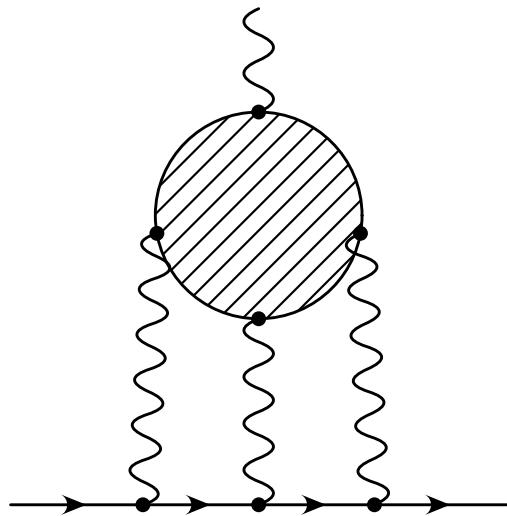
2k events per point, aimed at 4% systematics

With additional  $2 \text{ pb}^{-1}$  in 2014 the total  $\Delta R/R \sim 3\%$  can be achieved

## $R$ Measurements below 10 GeV



## Light-by-Light Scattering – I



Various approaches used:

- Vector Dominance and Chiral models
- Data on  $\gamma\gamma^* \rightarrow \pi^0, \eta, \eta'$  (single-tag)
- Effective field theory
- Dyson-Schwinger equations

M. Knecht and A. Nyffeler, 2002: the correct sign!

## Light-by-Light Scattering – II

Authors	Year	$a_\mu^{\text{lbl}}, 10^{-10}$
J. Bijnens et al.	1996 (2002)	$8.3 \pm 3.2$
M. Hayakawa and T. Kinoshita	1998 (2002)	$9.0 \pm 1.5$
K. Melnikov and A. Vainshtein	2003	$13.6 \pm 2.5$
M. Davier and W. Marciano	2004	$12.0 \pm 3.5$
J. Prades, E. de Rafael, and A. Vainshtein	2009	$10.5 \pm 2.6$
D. Greynat and E. de Rafael	2012	$15.0 \pm 0.3$
T. Goecke, C.S. Fischer and R. Williams	2013	$18.8 \pm 9.0$

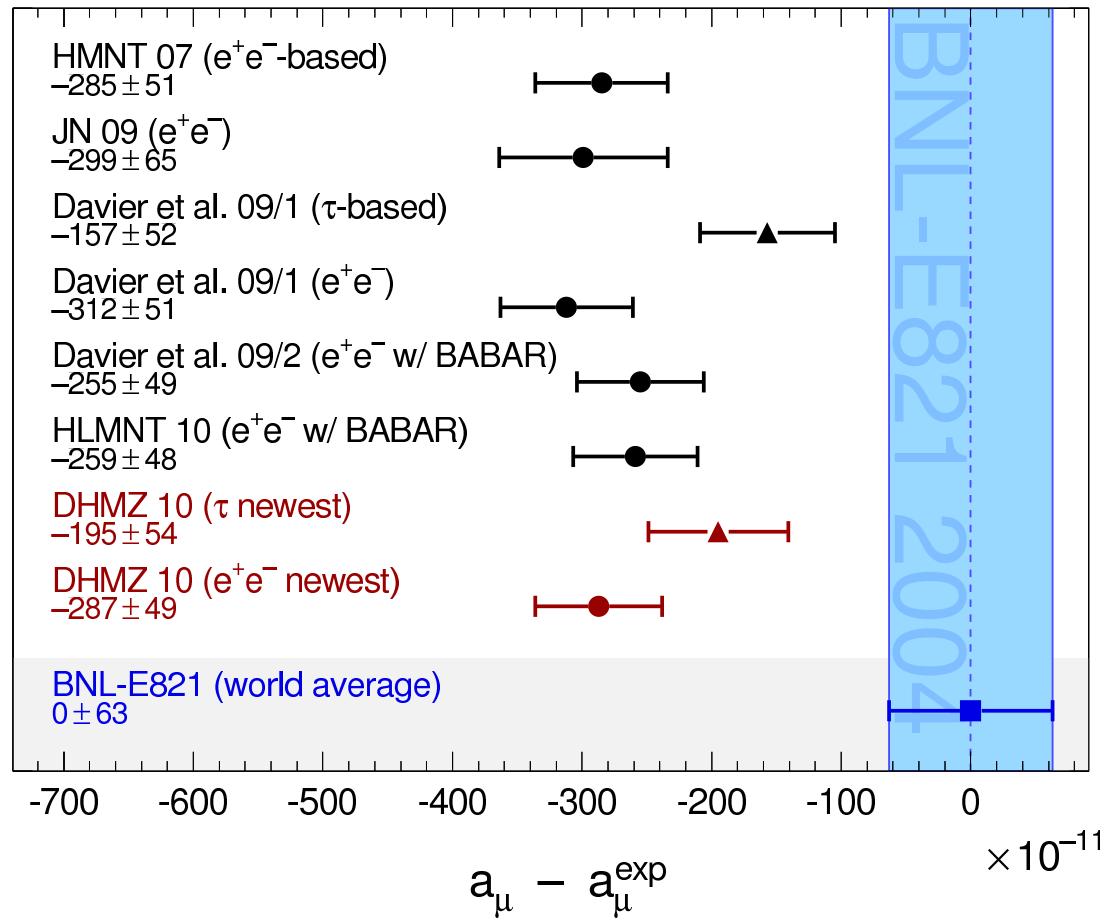
## Experiment vs. Theory – I

$$a_\mu = (g_\mu - 2)/2, \text{ } 10^{-10}$$

Experiment	$11659208.9 \pm 5.4 \pm 3.3$
QED	$11658471.809 \pm 0.015$
EW	$15.4 \pm 0.1 \pm 0.2$
Had LO	$692.3 \pm 4.2$
Had HO	$-9.8 \pm 0.1$
Had LbL	$10.5 \pm 2.6$
Theory	$11659180.2 \pm 4.9$
Exp.-Th.	$28.7 \pm 8.0$

Experiment is higher than theory by 3.6 standard deviations

## Experiment vs. Theory – II



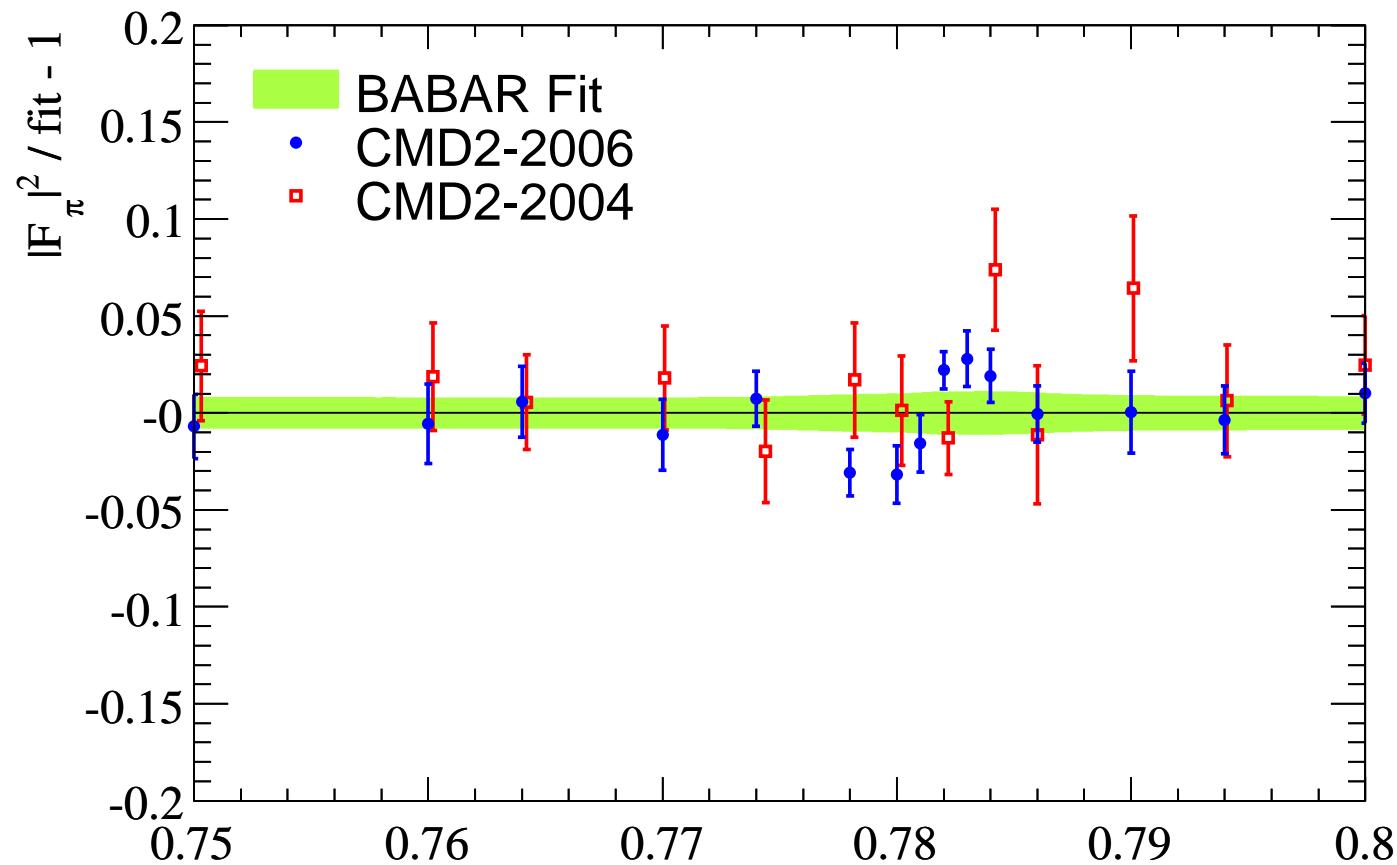
## How Real is $a_\mu^{\text{had}}$ Accuracy?

- Radiative corrections: ISR and HVP probably OK,  
FSR demands testing (charge asymmetry,  $\pi^+\pi^-\gamma$ )
- Scan vs. ISR method
- Missing states: neutrals,  $\pi^+\pi^-n\pi^0$ ,  $K\bar{K}n\pi$  - isospin
- Correlations
- Averaging
- Light-by-light term
- Double counting (LO and HO)

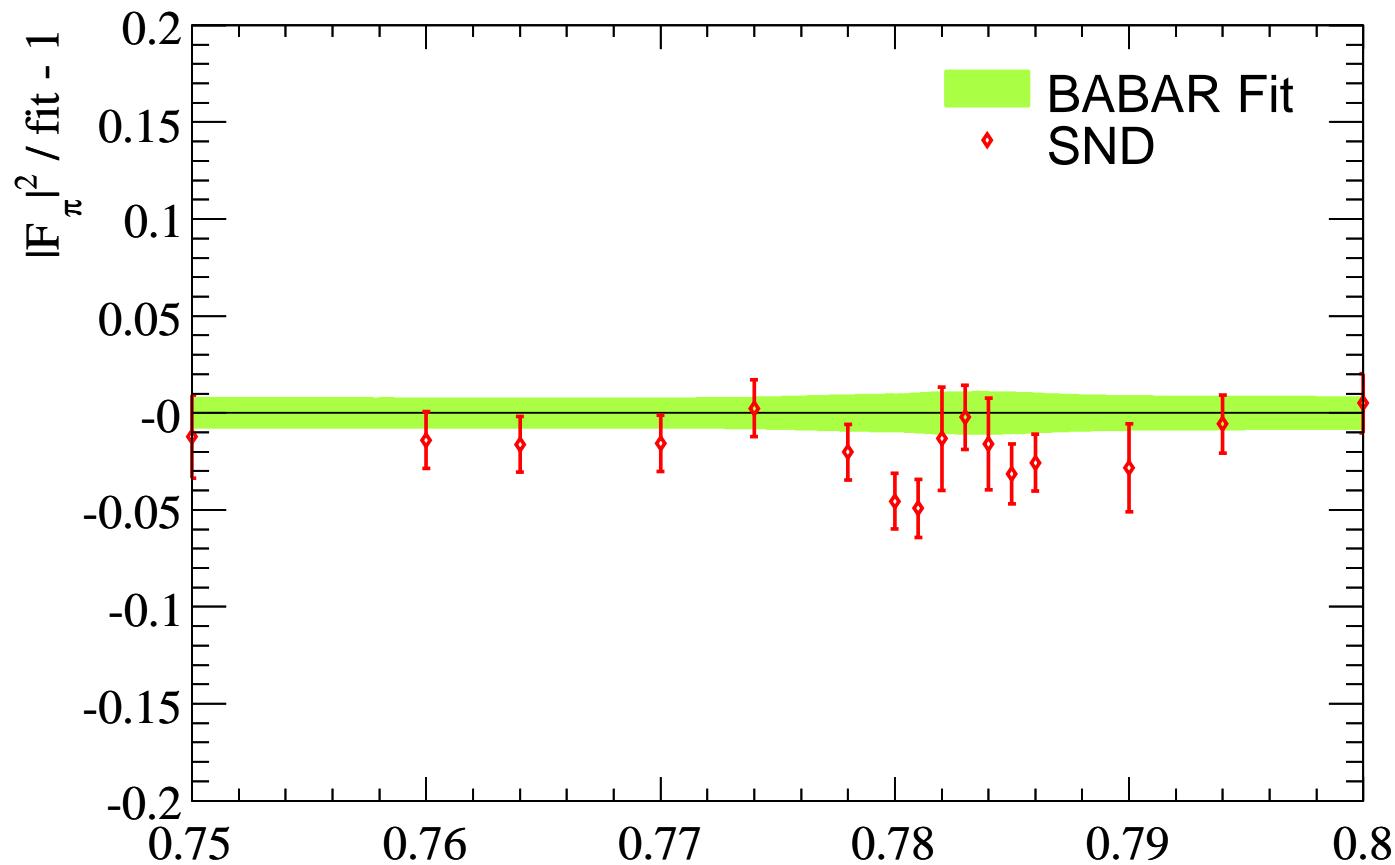
## Contribution of Various Energy Ranges

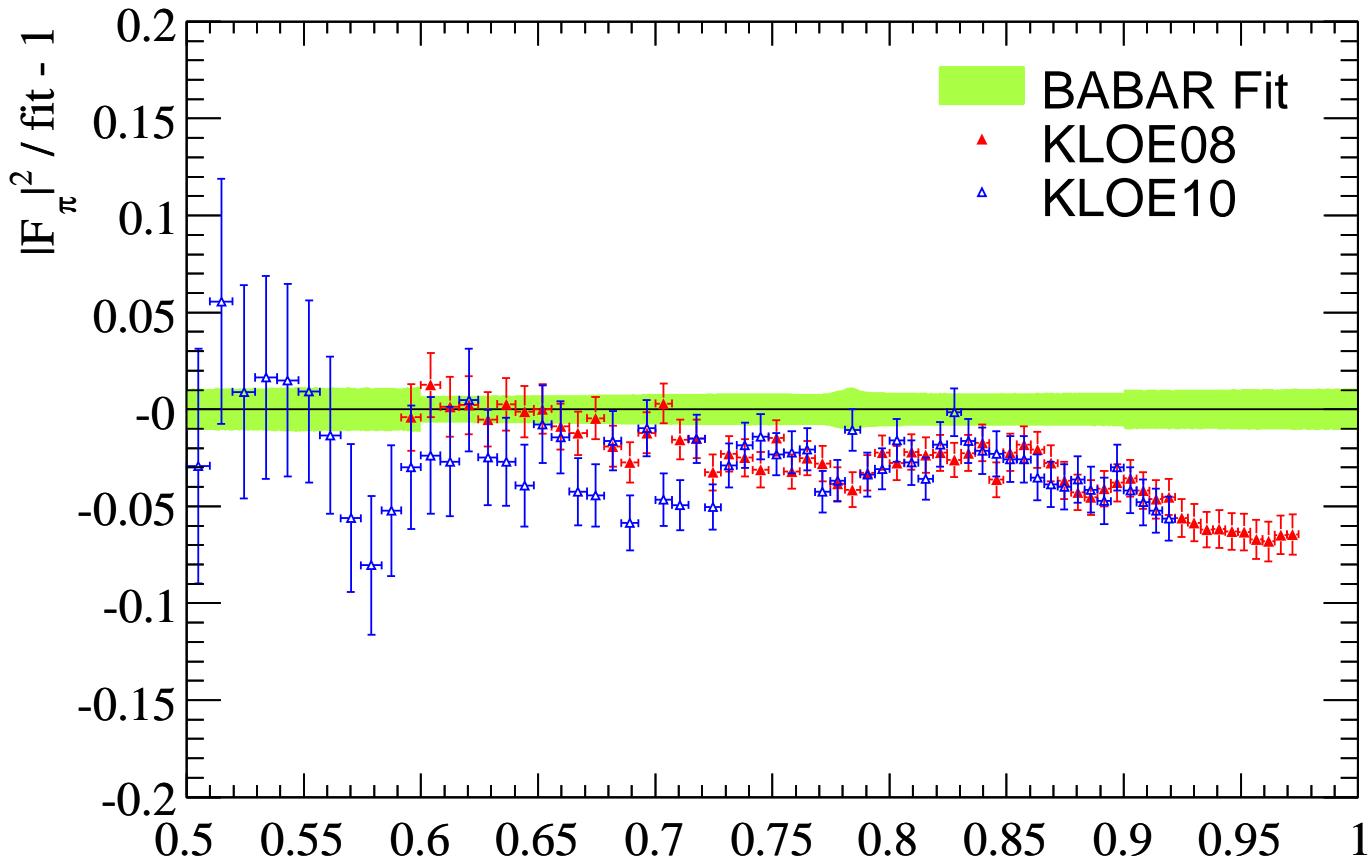
$\sqrt{s}$ , GeV	$\Delta a_\mu^{\text{had,LO}}$
$\pi^+ \pi^-$	$507.80 \pm 2.84$
$\pi^+ \pi^- \pi^0$	$46.00 \pm 1.73$
$K^+ K^-$	$21.63 \pm 0.73$
$K_S^0 K_L^0$	$12.96 \pm 0.39$
$m/h < 1.8$	$45.50 \pm 3.44$
1.8-3.7	$33.45 \pm 0.28(2.00)$
$> 3.7$	$17.16 \pm 0.31$
Total	$692.3 \pm 4.2$

$e^+e^- \rightarrow \pi^+\pi^-$ , BaBar vs. CMD-2



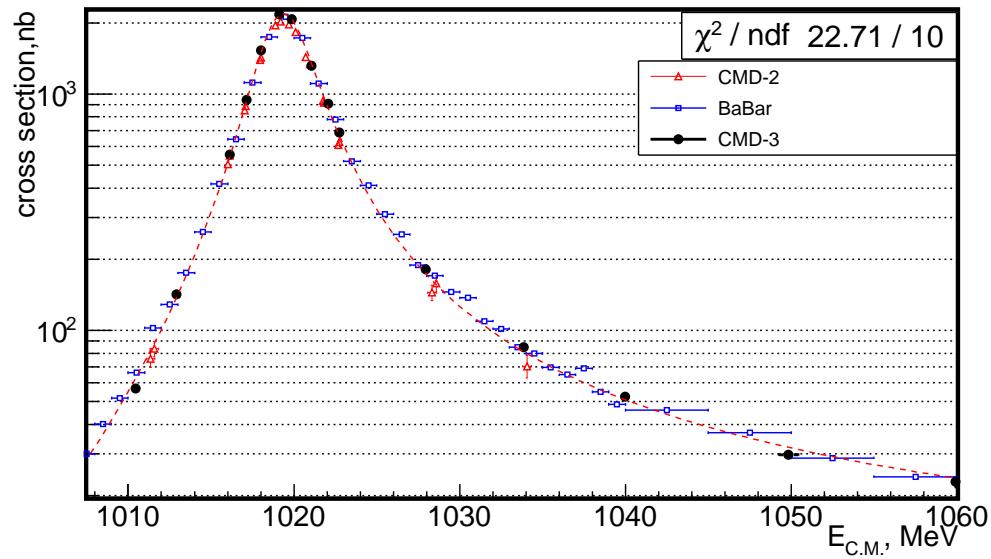
$e^+e^- \rightarrow \pi^+\pi^-$ , BaBar vs. SND



$e^+e^- \rightarrow \pi^+\pi^-$ , BaBar vs. KLOE

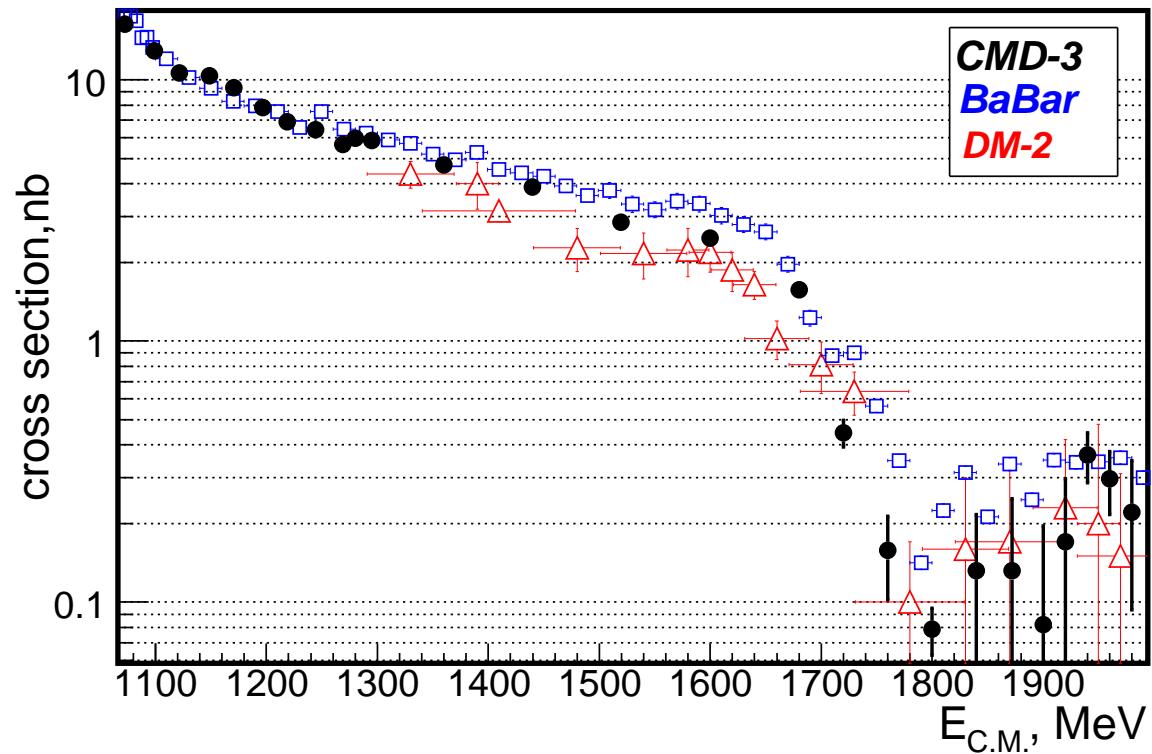
Do we have completely correct ISR theory?

$e^+e^- \rightarrow K^+K^-$  at CMD-3 – I



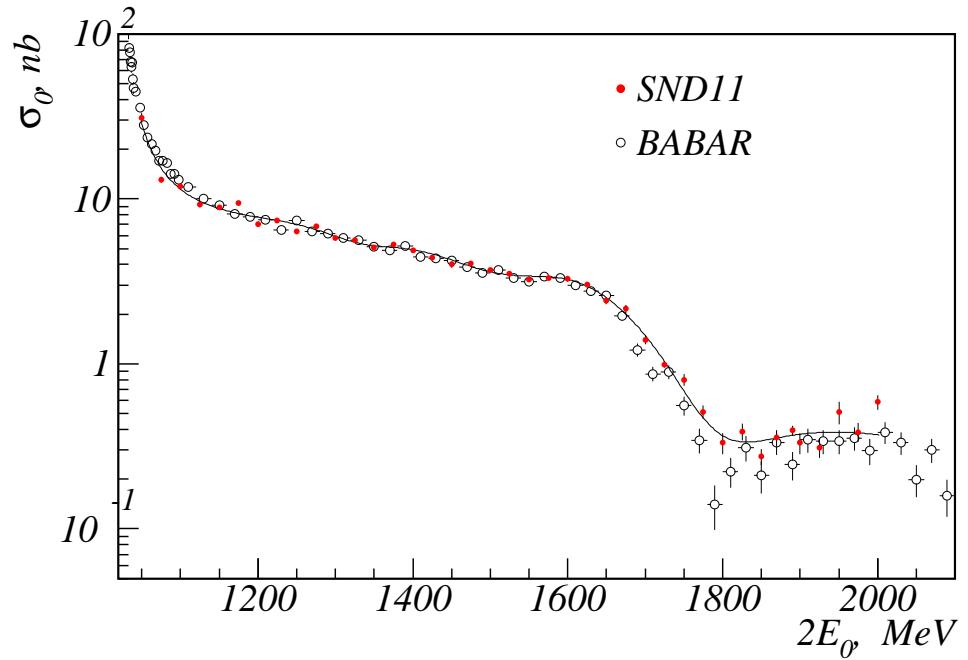
BaBar data higher than CMD-3, CMD-2 and CMD-3 agree

$e^+e^- \rightarrow K^+K^-$  at CMD-3 – II



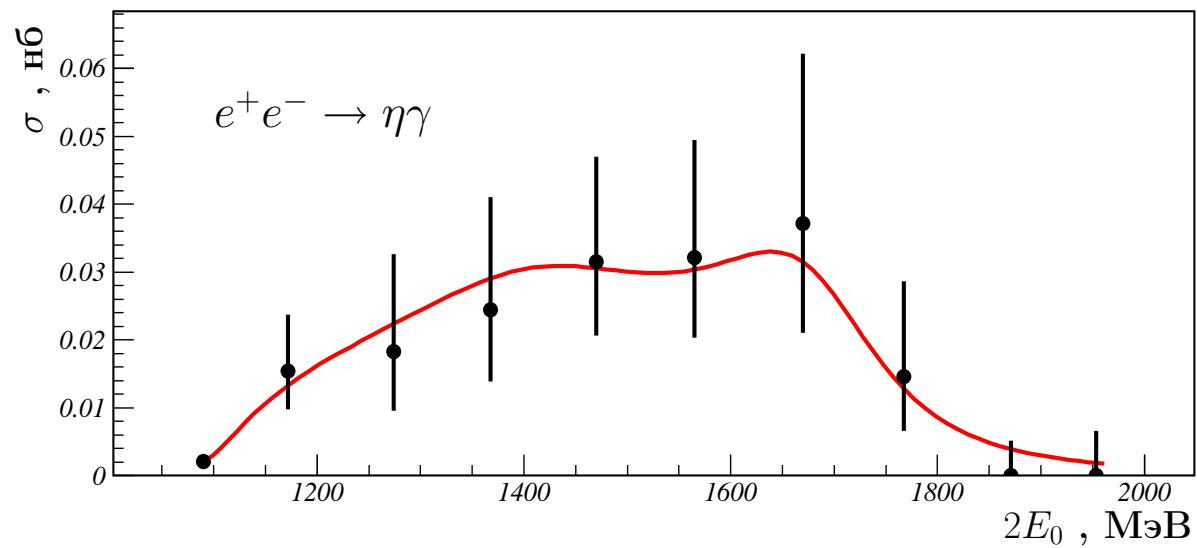
BaBar data higher than CMD-3

$e^+e^- \rightarrow K^+K^-$  at SND



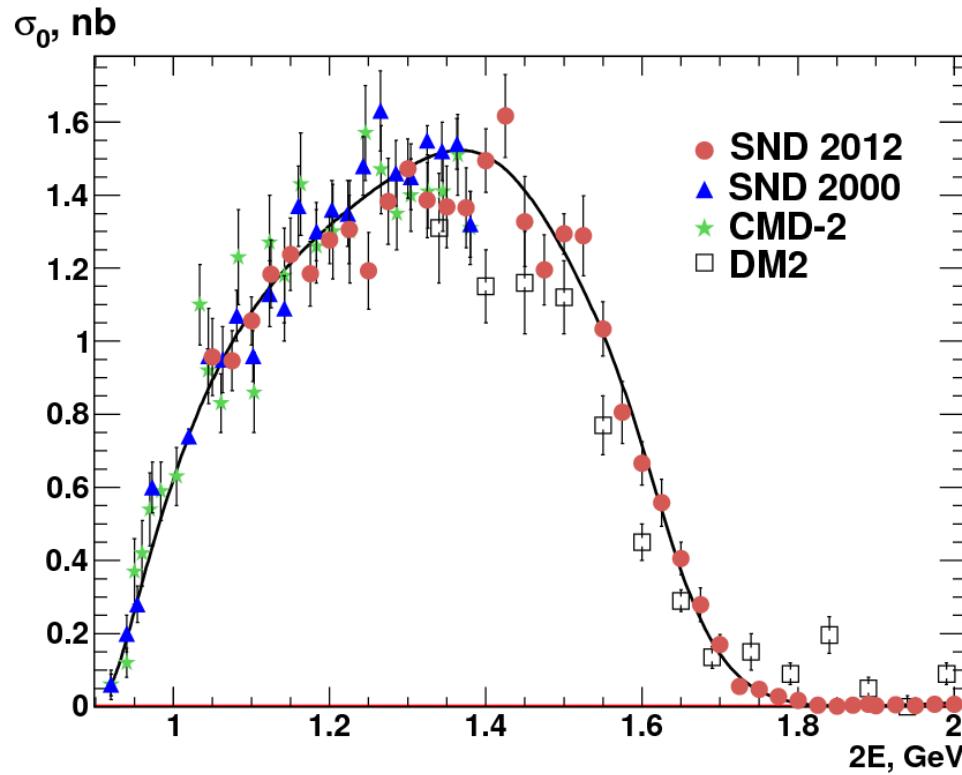
Very preliminary SND data agree with BaBar

$e^+e^- \rightarrow \eta\gamma$  at SND



The first measurement of radiative decays above 1.4 GeV,  $\rho(1450)$  and  $\phi(1680)$ ,  
the  $\pi^0\gamma$  also looked for,  $3\gamma$  suffers from QED background

$$e^+e^- \rightarrow \omega\pi^0 \rightarrow \pi^0\pi^0\gamma \text{ at SND}$$



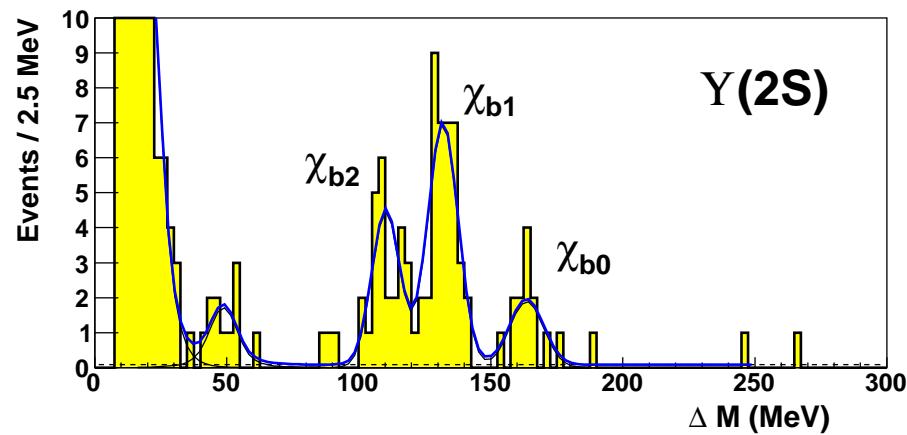
Phys. Rev. D 88 (2013) 054013

First observation above 1.4 GeV,  $\pi^0\eta\gamma$ ,  $\eta\eta\gamma$  needed

### Missing States – Isospin Relations

- Correctly separate  $I = 0$  and  $I = 1$ , e.g.,  $e^+e^- \rightarrow \pi^+\pi^- 4\pi^0$  has  $\omega(\phi)\eta$  with  $I = 0$
- $K\bar{K}\pi - K^+K^-\pi^0$ ,  $K_S^0 K^\pm \pi^\mp$  seen,  $K^0\bar{K}^0\pi^0$  – not yet
- Even more combinations with  $K\bar{K}\pi\pi$ , recent progress at BaBar

## Importance of FSR Corrections – I



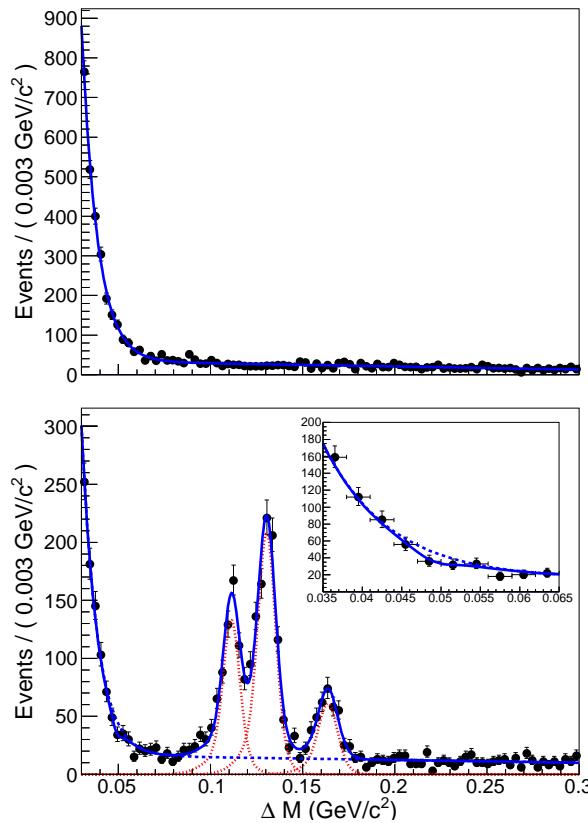
S. Dobbs et al., Phys. Rev. Lett. 109, 082001 (2012) used  $9.3 \cdot 10^6$   $\Upsilon(2S)$  of CLEO data to study  $\Upsilon(2S) \rightarrow \eta_b(2S)\gamma$

## Importance of FSR Corrections – II

Group	Signal	$\Delta M_{\text{HF}}$ , MeV	$M$ , MeV	Sign., $\sigma$
”CLEO”	$11.4^{+4.3}_{-3.5}$	$48.7 \pm 2.3 \pm 2.1$	$9974.6 \pm 2.3 \pm 2.1$	4.9
Belle	$(25.8 \pm 4.9) \cdot 10^3$	$24.3^{+4.0}_{-4.5}$	$9999.0 \pm 3.5^{+2.8}_{-1.9}$	4.2

R. Mizuk et al., Phys. Rev. Lett. 109, 232002 (2012) (Belle) at the  $\Upsilon(5S)$

## Importance of FSR Corrections – III



17 times larger statistics – no signal, UL for  $\mathcal{B}$  8 times smaller!

## Conclusions on HVP

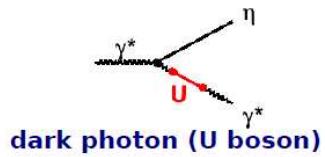
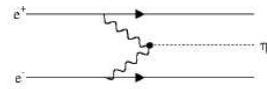
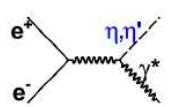
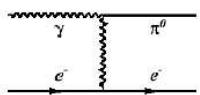
- VEPP-2000 is running smoothly with CMD-3 and SND
- New channels with many neutrals observed
- CMD-3 and SND at VEPP-2000 will provide high accuracy, comparable or better than ISR measurements, the tentative goals are 0.35%(0.5%) for  $\pi^+\pi^-$  and 3% for multibody modes
- Below 2 GeV progress (a factor of 2-3) expected in exclusive  $\sigma$ 's due to scans in Novosibirsk and ISR from KLOE, BaBar, Belle, BES3 and Belle2
- Above 2 GeV  $R$  measurements with 3-4% accuracy at BES3 and KEDR
- More precise measurements of  $\Gamma_{ee}$  for the narrow  $\psi$  and  $\Upsilon$  at KEDR and Belle
- Various high-statistics experiments will substantially improve the accuracy of vacuum polarization calculations for  $(g_\mu - 2)/2$

## Transition Form Factors - I (General)

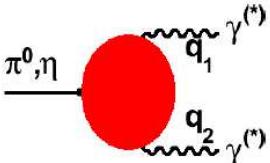
**Low energy QCD**

**I<sup>+</sup>I<sup>-</sup> spectra for HI**

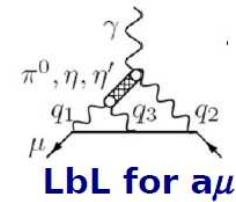
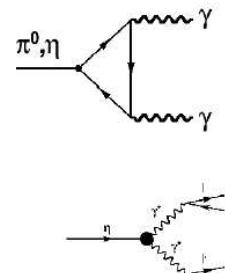
$\pi^0, \eta, \eta', \eta_c \dots \rightarrow \gamma^* \gamma^*$



$\Gamma(P \rightarrow \gamma\gamma)$



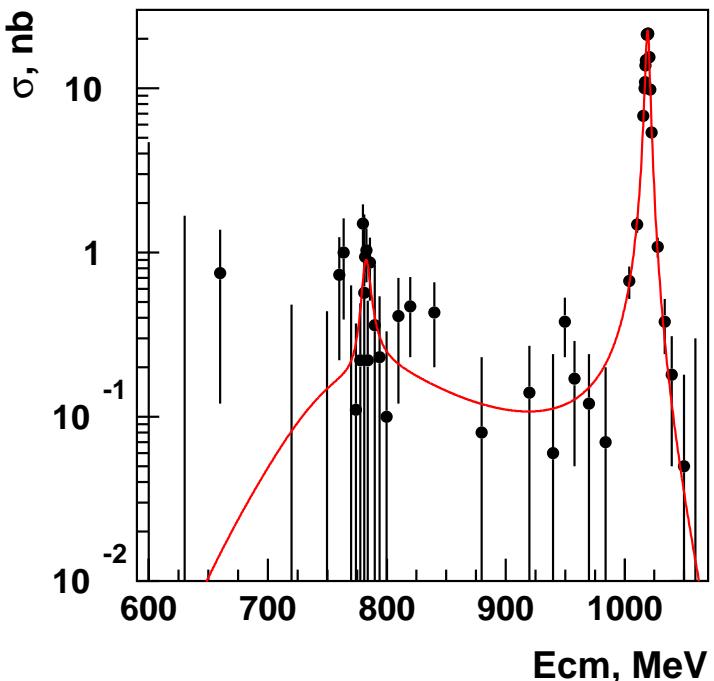
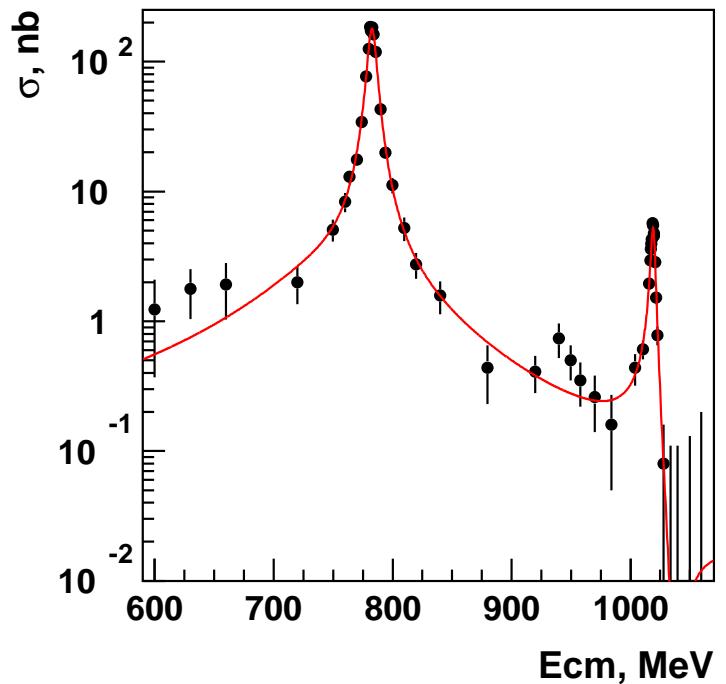
$F_P(q_1^2, q_2^2)$



## Transition Form Factors - II (General)

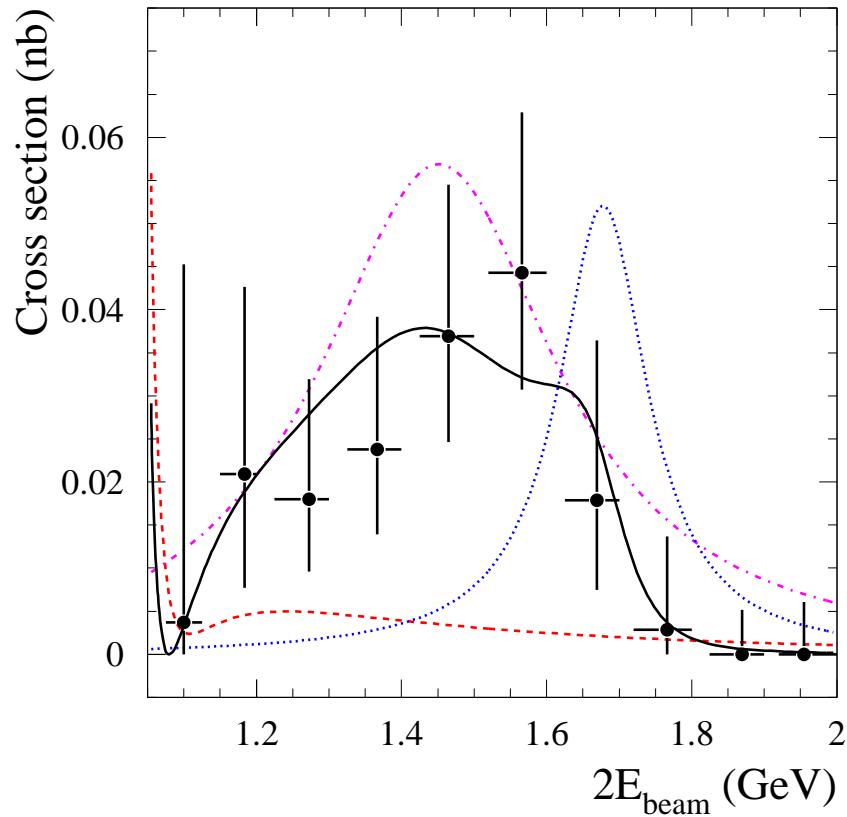
- We are interested in studying the  $P\gamma\gamma$  vertex and the related TFF  $\mathcal{F}_P(q_1^2, q_2^2)$ , at any  $q_{1(2)}^2$  and  $P = \pi^0, \eta, \eta'$ , the processes studied are  $P \rightarrow \gamma^{(*)}\gamma^{(*)}$ ,  $\gamma^* \rightarrow P\gamma^{(*)}$  and  $\gamma^*\gamma^* \rightarrow P$
- In  $e^+e^-$  annihilation we study:  $e^+e^- \rightarrow \gamma^* \rightarrow P\gamma$ ,  $q_1^2 = s > 0$  and  $q_2^2 = 0$ ;  $e^+e^- \rightarrow \gamma^* \rightarrow P\gamma^* \rightarrow Pl^+l^-$ ,  $l = e, \mu$ ,  $q_1^2 = s > 0$ ,  $4m_l^2 < q_2^2 < (\sqrt{s} - m_P)^2$ ;  $e^+e^- \rightarrow e^+e^- \gamma^*\gamma^* \rightarrow e^+e^- P$  with  $q_{1(2)}^2 < 0$
- In VDM (vector dominance model) hadrons are produced via vector mesons, so any production of vectors  $\gamma^* \rightarrow V \rightarrow P\gamma^{(*)}$  is relevant, e.g.,  $e^+e^- \rightarrow V \rightarrow P\gamma$  with  $q_1^2 \sim m_V^2$  and  $q_2^2 = 0$  or  $e^+e^- \rightarrow V \rightarrow Pl^+l^-$  with  $q_1^2 \sim m_V^2$  and  $4m_l^2 < q_2^2 < (m_V - m_P)^2$
- At the  $V$  factory radiative decays like  $V \rightarrow P\gamma$  are a copious source of  $P$  decays, e.g.,  $P \rightarrow l^+l^-\gamma$  and  $P \rightarrow l^+l^-l^+l^-$  can be studied

$e^+e^- \rightarrow \pi^0\gamma/\eta\gamma$  with CMD-2



R.R. Akhmetshin et al., Phys. Lett. B 605 (2005) 26

10 times larger statistics expected at VEPP-2000

$e^+e^- \rightarrow \eta\gamma$  with SND at VEPP-2000

The first measurement of radiative decays above 1.4 GeV,  $\rho(1450)$ ,  $\phi(1680)$   
M.N. Achasov et al., arXiv:1312.7078

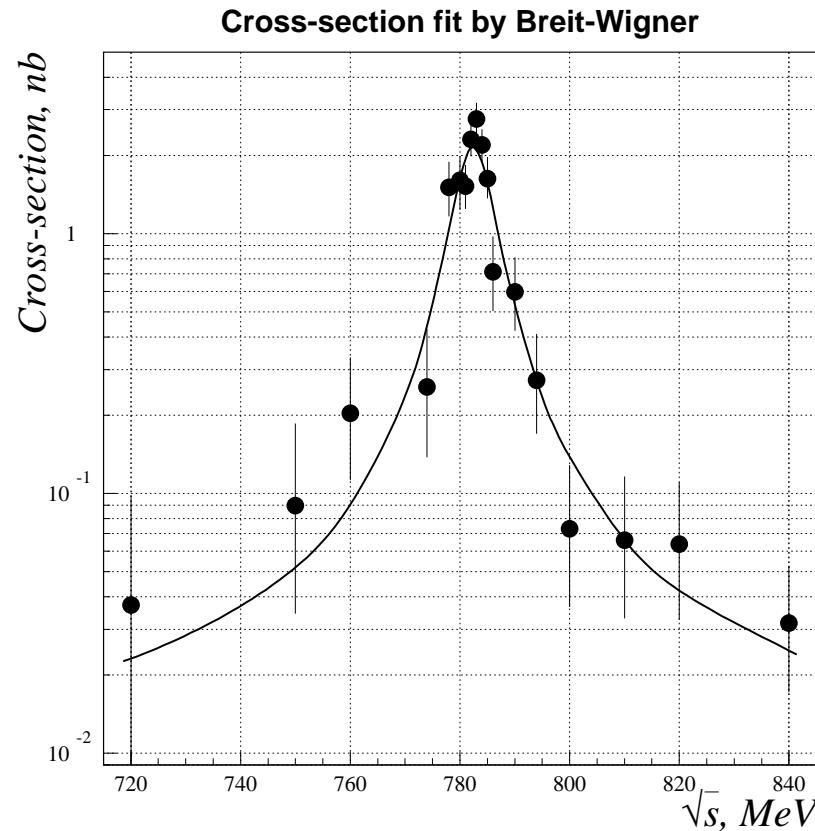
$$e^+ e^- \rightarrow \eta' \gamma$$

Seen in  $\phi$  decays only! A study of  $\sigma(s)$  not simple. BaBar measured at  $\Upsilon(4S)$   
 First observed by CMD-2 from 5.5M  $\phi$ 's with 6 events only  
 R.R. Akhmetshin et al., Phys. Lett. B 415 (1997) 445

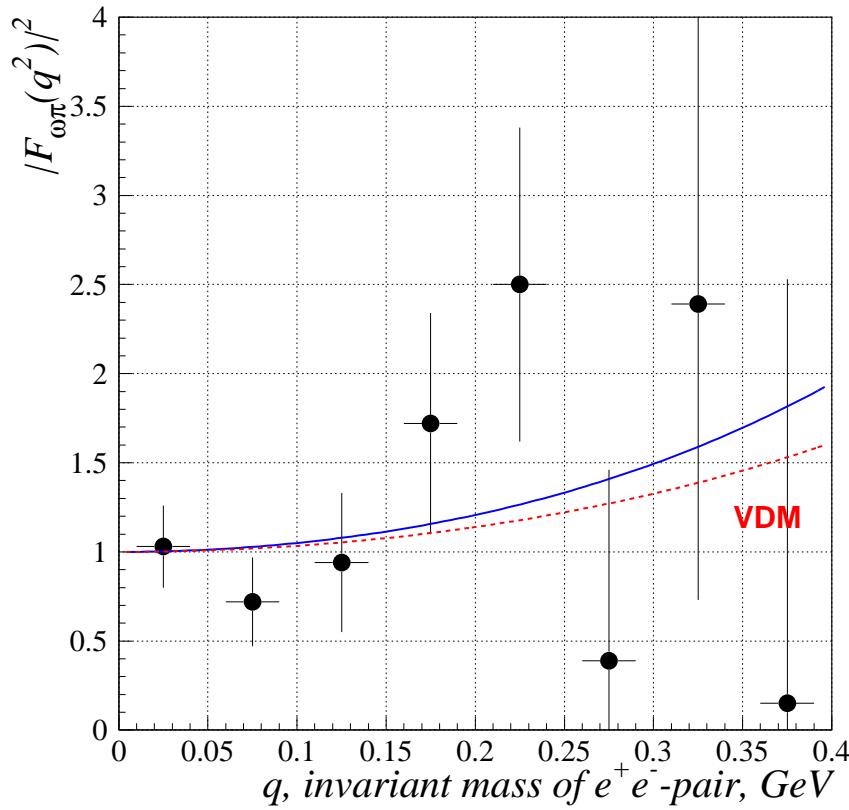
Group	Date	$N_{\text{ev}}$	$\mathcal{B}, 10^{-5}$
CMD-2	2000	30	$6.4 \pm 1.4$
KLOE	2002	120	$6.10 \pm 0.61 \pm 0.43$
SND	2003	12	$6.7^{+2.8}_{-2.4} \pm 0.8$
KLOE	2007	3407	$6.25 \pm 0.28 \pm 0.11$
PDG	2012	–	$6.25 \pm 0.21$

## Conversion Decays of $\omega(\rho)$ Mesons – I

$e^+e^- \rightarrow \pi^0 e^+e^-$  in the  $\omega(\rho)$  energy range



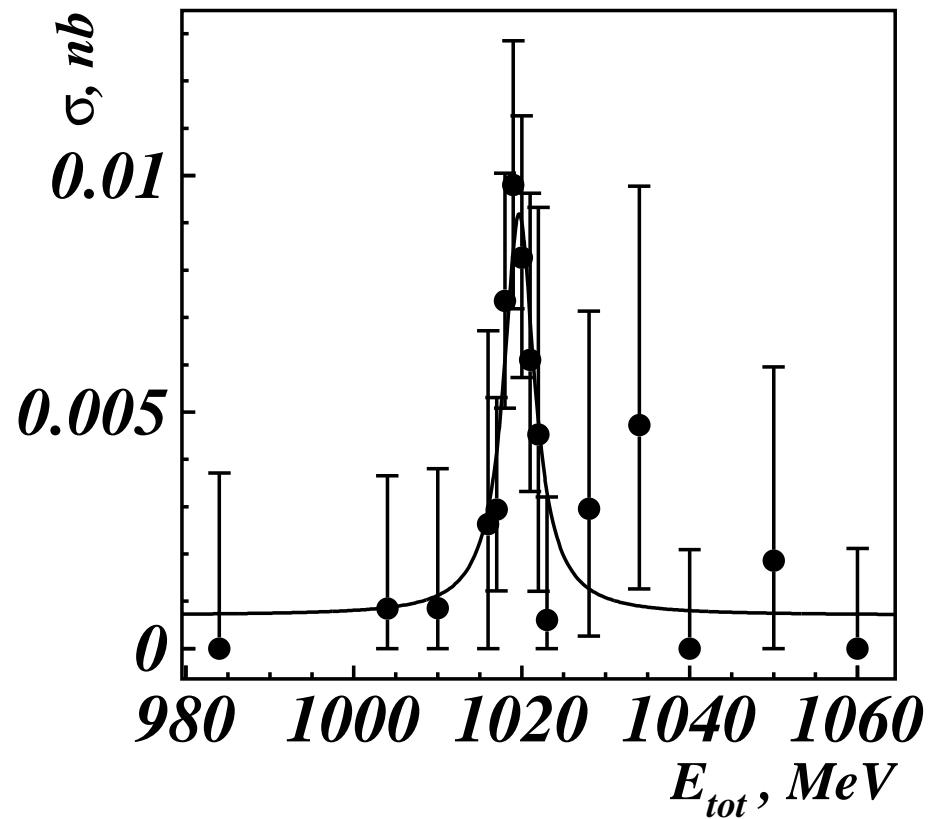
R.R. Akhmetshin et al., Phys. Lett. B 613 (2005) 29

Conversion Decays of  $\omega(\rho)$  Mesons – III

A fit gives a slope of  $2.5 \pm 3.1 \text{ GeV}^{-2}$  compatible with  $1/m_\rho^2 \sim 1.7 \text{ GeV}^{-2}$

## Conversion Decays of $\phi$ Mesons – I

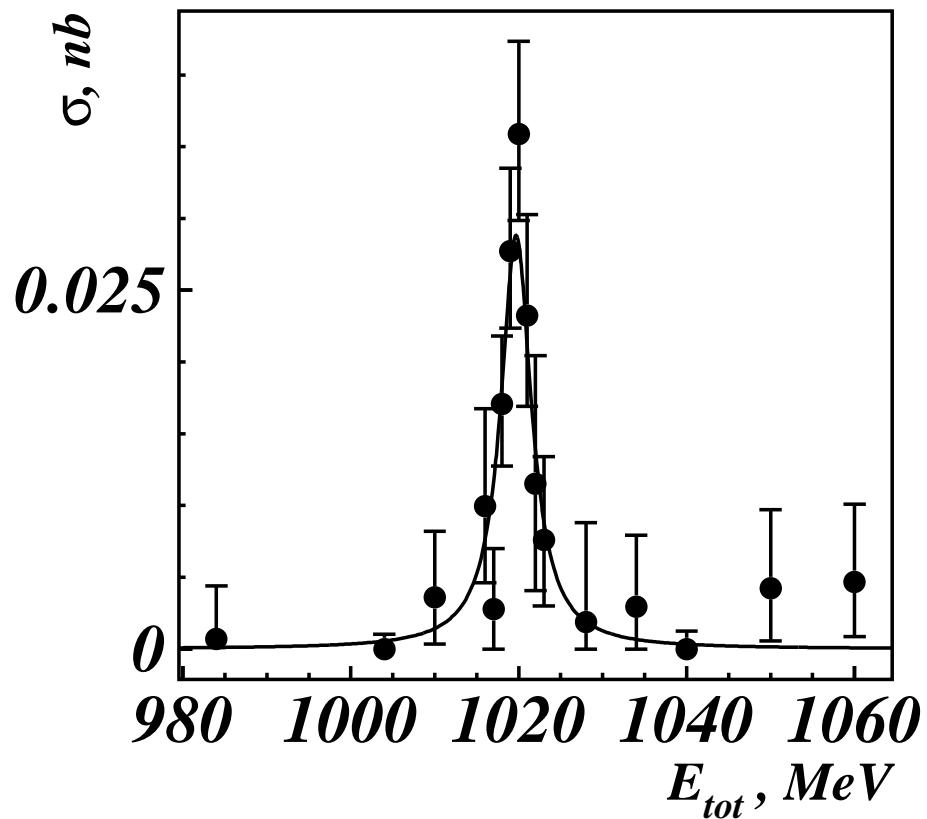
$e^+e^- \rightarrow \pi^0 e^+e^-$  in the  $\phi$  energy range



R.R. Akhmetshin et al., Phys. Lett. B 503 (2001) 237

## Conversion Decays of $\phi$ Mesons – II

$e^+e^- \rightarrow \eta e^+e^-$  in the  $\phi$  energy range



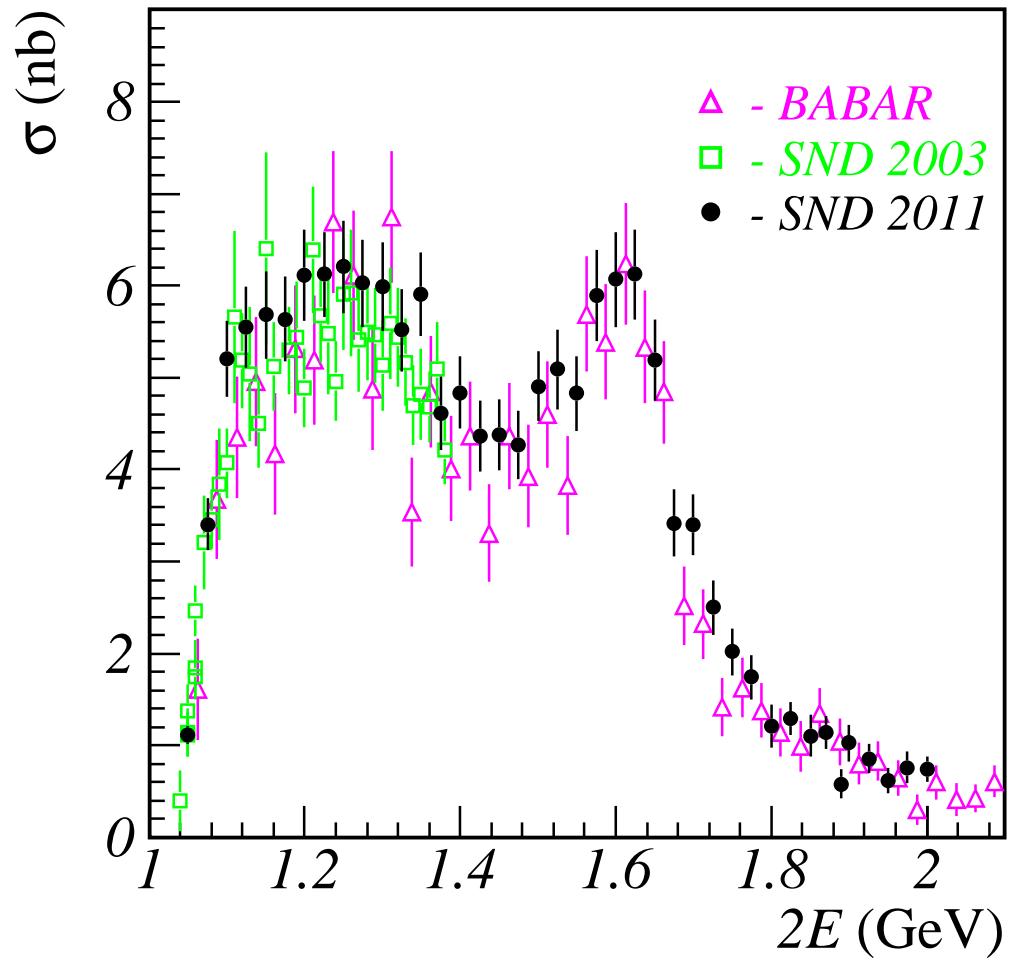
R.R. Akhmetshin et al., Phys. Lett. B 501 (2001) 191

## Summary of $\rho, \omega, \phi$ Conversion Decays

Decay	$l = e$		$l = \mu$	
	$\mathcal{B}_{\text{exp}}$	$\mathcal{B}_{\text{th}}$	$\mathcal{B}_{\text{exp}}$	$\mathcal{B}_{\text{th}}$
$\rho \rightarrow \pi^0 l^+ l^-$	$< 1.2 \cdot 10^{-5}$	$4.1 \cdot 10^{-6}$	—	$4.6 \cdot 10^{-7}$
$\rho \rightarrow \eta l^+ l^-$	$< 0.7 \cdot 10^{-5}$	$2.7 \cdot 10^{-6}$	—	$7.0 \cdot 10^{-11}$
$\omega \rightarrow \pi^0 l^+ l^-$	$(7.7 \pm 0.6) \cdot 10^{-4}$	$7.9 \cdot 10^{-4}$	$(1.3 \pm 0.4) \cdot 10^{-4}$	$9.2 \cdot 10^{-5}$
$\omega \rightarrow \eta l^+ l^-$	—	$6.0 \cdot 10^{-6}$	—	$1.8 \cdot 10^{-9}$
$\phi \rightarrow \pi^0 l^+ l^-$	$(1.12 \pm 0.28) \cdot 10^{-5}$	$1.6 \cdot 10^{-5}$	—	$4.8 \cdot 10^{-6}$
$\phi \rightarrow \eta l^+ l^-$	$(1.15 \pm 0.10) \cdot 10^{-4}$	$1.1 \cdot 10^{-4}$	$< 9.4 \cdot 10^{-6}$	$6.8 \cdot 10^{-6}$

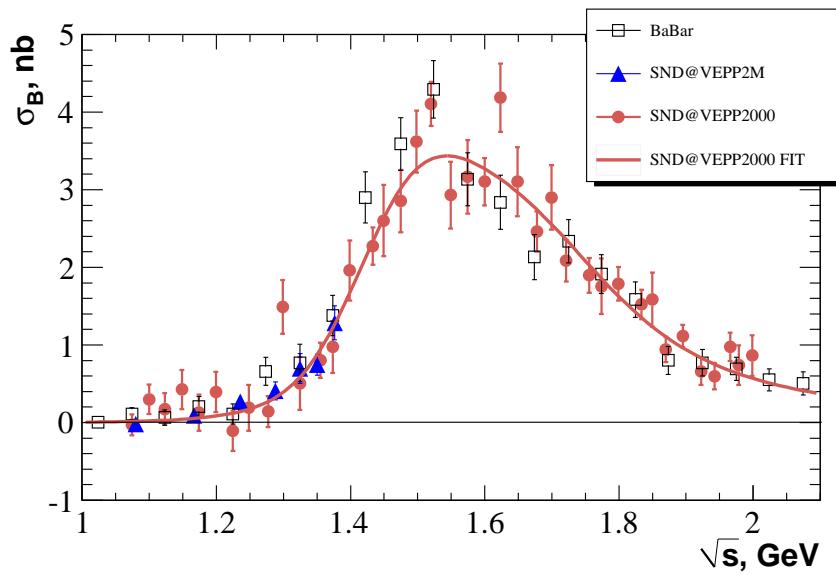
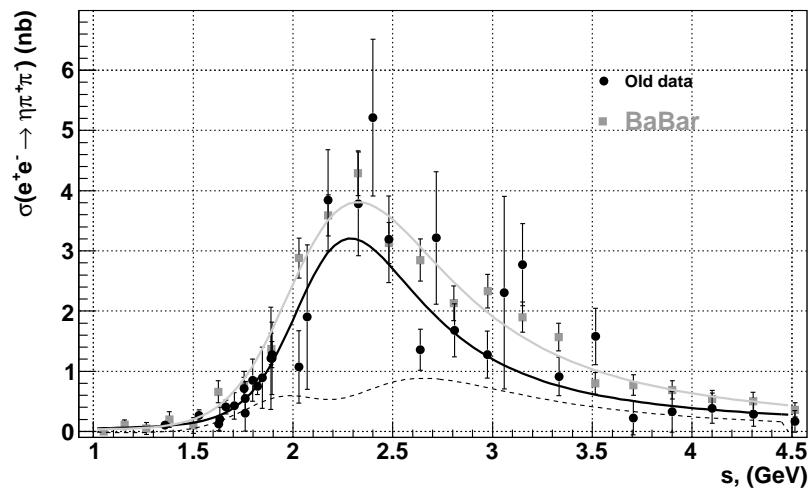
Decays with muons are much worse studied

$e^+e^- \rightarrow \pi^+\pi^-\pi^0$  at SND



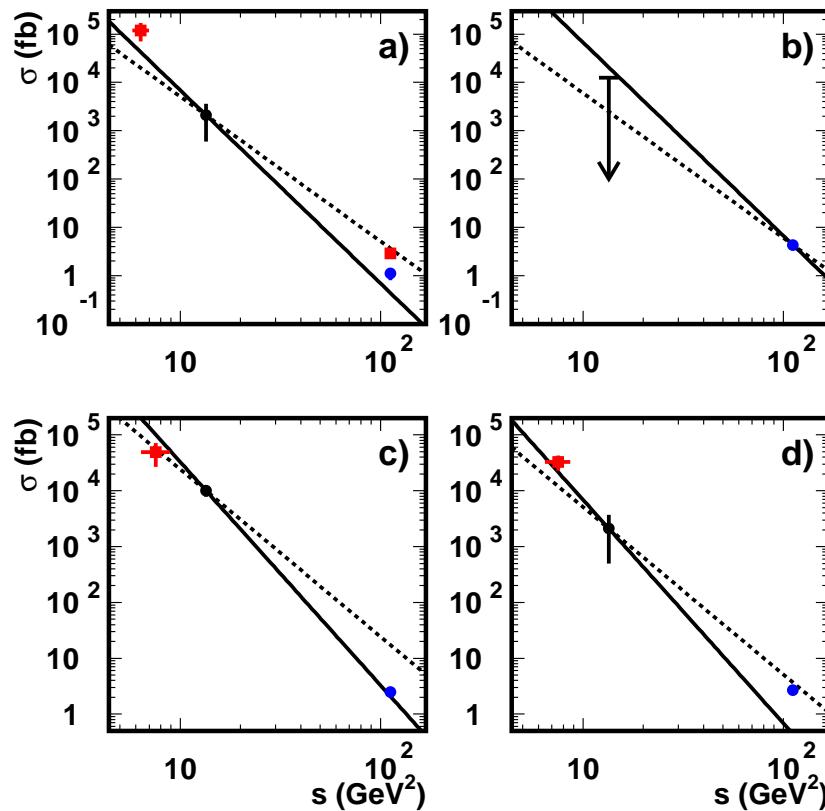
It's interesting to disentangle the  $\rho\pi$  and direct  $3\pi$  modes

$e^+e^- \rightarrow \eta\pi^+\pi^-$  at SND



BaBar data higher than old data by  $\sim 15\%$ , not confirmed by new SND data?

Dominated by  $e^+e^- \rightarrow \eta\rho$

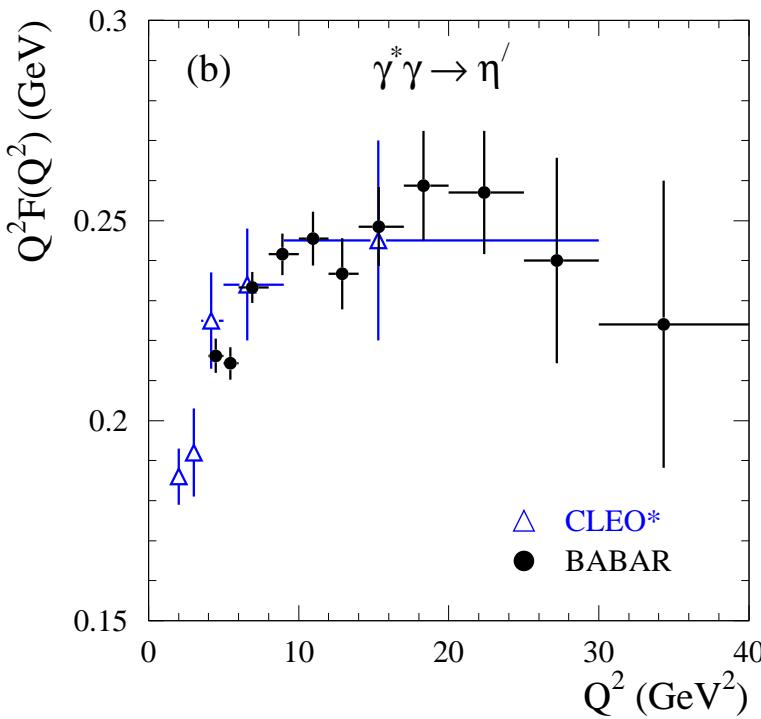
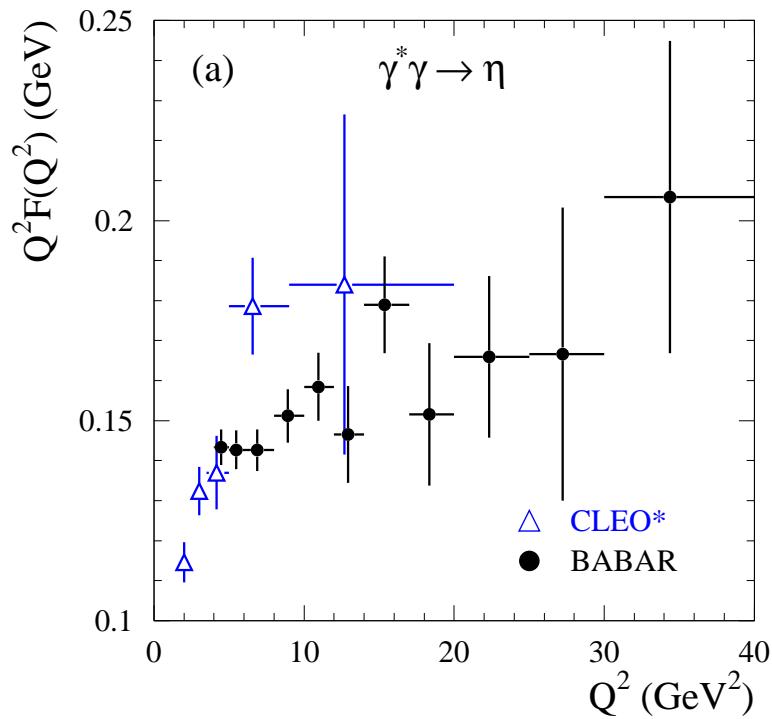
$\gamma^* \rightarrow VP$ 

(a)  $\phi\eta$ , (b)  $\phi\eta'$ , (c)  $\rho\eta$ , (d)  $\rho\eta'$   
Solid –  $1/s^4$ , dashed –  $1/s^3$

## QCD Studies in $\gamma\gamma \rightarrow M_1 M_2$ at Belle

Final state	$\int L dt, \text{ fb}^{-1}$	$W, \text{ GeV}$	$ \cos \theta^* $	Reference
$\pi^+ \pi^-$ , $K^+ K^-$	87.7	2.4-4.1	< 0.6	H. Nakazawa et al., PLB 615, 39 (2005)
$p\bar{p}$	89	2.025-4	< 0.6	C.C.Kuo et al., PLB 621, 41 (2005)
$\pi^0 \pi^0$	223	0.6-4.1	< 0.8	S.Uehara et al., PRD 79, 052009 (2009)
$\eta \pi^0$	223	0.84-4.0	< 0.8	S.Uehara et al., PRD 80, 032001 (2009)
$\eta \eta$	393	1.096-3.8	< 0.9 < 1.0	S.Uehara et al., PRD 82, 114031 (2010)
$K_S^0 K_S^0$	972	1.05-4.0	< 0.8	S.Uehara et al., PTEP2013(2013)123C01

## Transition Form Factors in $\gamma^*\gamma \rightarrow \eta, \eta'$

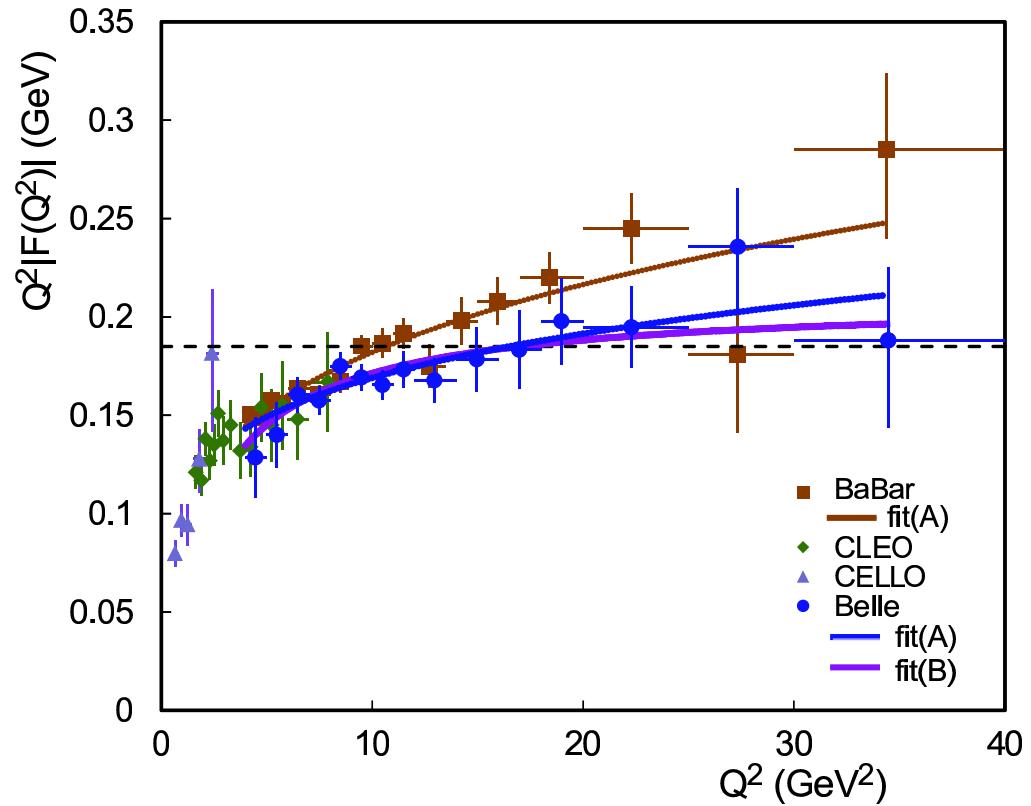


Single-tag measurements probe  $\gamma\gamma^*$

P. del Amo Sanchez et al. (BaBar), Phys. Rev. D 84, 052011 (2011)

J. Gronberg et al. (CLEO), Phys. Rev. D 57, 33 (1998)

## Transition Form Factors in $\gamma^*\gamma \rightarrow \pi^0$

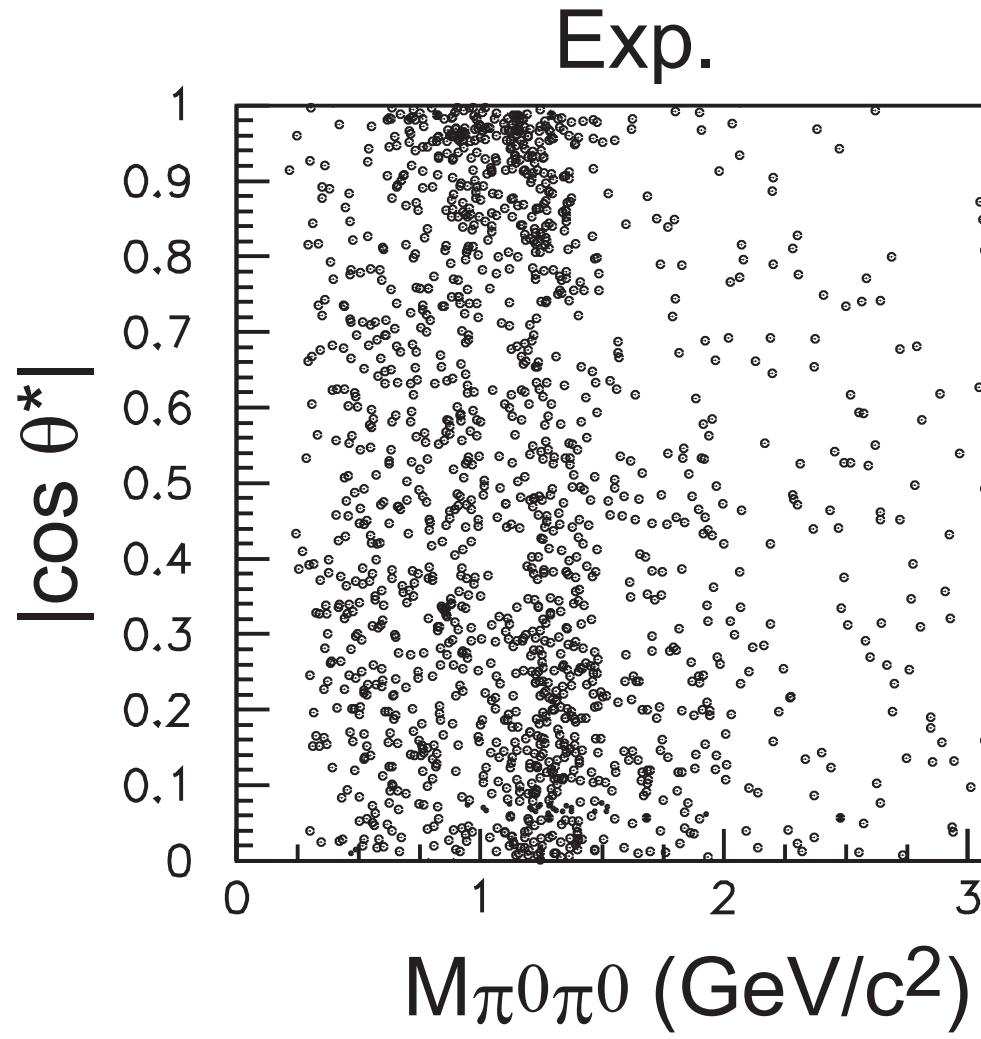


Belle data do not confirm fast rise observed at BaBar

S. Uehara et al., Phys. Rev. D 86 (2012) 092007

### Single-tag $\gamma\gamma \rightarrow \pi^0\pi^0$ at Belle – I

- Background for single-tag  $\gamma\gamma \rightarrow \pi^0$  ( $759 \text{ fb}^{-1}$ )
- A clear signal of  $f_2(1270)$ , possibly  $f_0(980)$ ?
- A few thousand events,  $3 < Q^2 < 30 \text{ GeV}^2$  and  $0.5 < W < 2.5 \text{ GeV}$
- Information on transition f/f for tensors, scalars;  
with other final states to axial vectors

Single-tag  $\gamma\gamma \rightarrow \pi^0\pi^0$  at Belle – II

## Conclusions

- $e^+e^-$  colliders (DAFNE, VEPP-2000, BEPC-II and SuperKEKB) have a very high potential for studying  $\gamma^{(*)}\gamma^{(*)}$  physics
- A lot of different possibilities:  $e^+e^- \rightarrow P\gamma$ ,  $P l^+l^-$ ,  $P\pi^+\pi^-$ ,  $e^+e^- \rightarrow e^+e^- P$
- KLOE-2 with taggers –  $\Gamma_{\gamma\gamma}$  for  $\pi^0$ ,  $\eta$ ,  $\gamma\gamma \rightarrow \pi^0\pi^0$
- Taggers would be extremely helpful, but they are not absolutely necessary
- $\mathcal{F}_P(q_1^2, q_2^2)$  can be studied in various regions of  $q_i^2$ , hopefully leading to better modeling of HLbL for  $a_\mu$