

g_2 Spin Structure Function at Jefferson Lab

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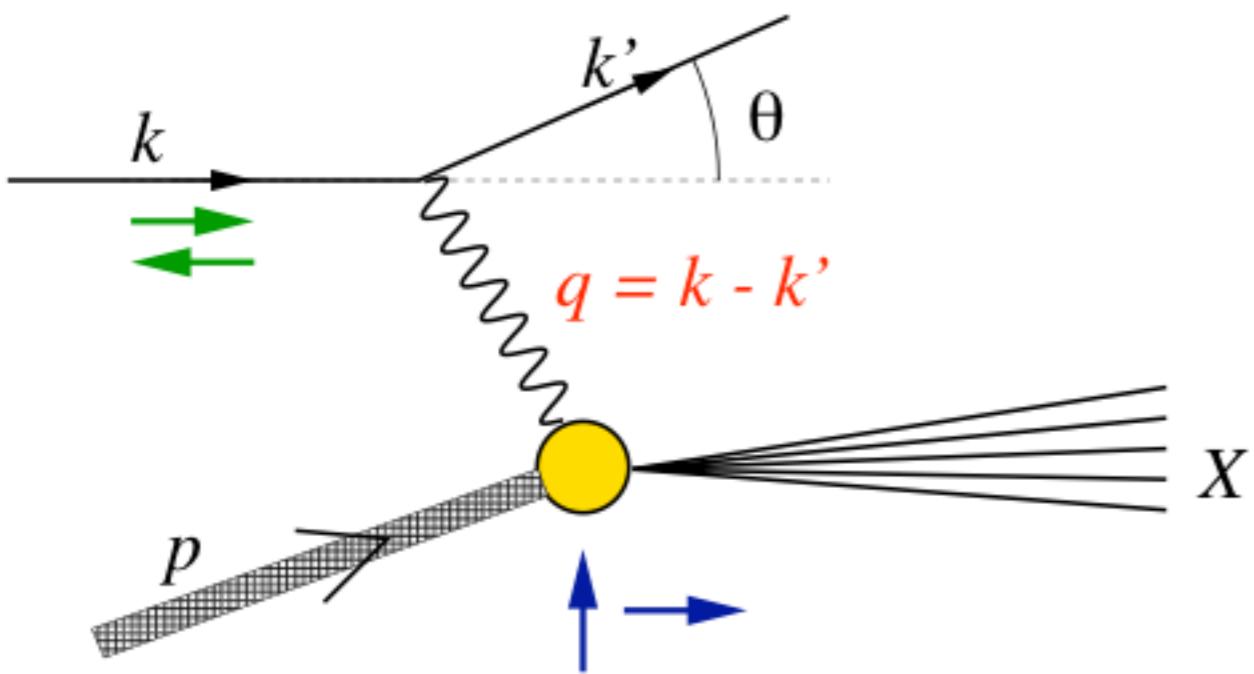
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Peking University, Beijing, China



Outline

- Polarized DIS and spin structure functions
- Experiments at Jefferson Lab for g_2
- Spin Asymmetries of the Nucleon Experiment
- Other experiments for g_2
- Summary

Inclusive e - N Scattering



- Four-momentum transfer
$$Q^2 = -q^2 = 4EE' \sin^2 \frac{\theta}{2}$$
- Energy transfer to the hadron
$$\nu = E - E'$$
- Mass of the hadronic residual (or invariant mass)
$$W = \sqrt{(p + q)^2} = \sqrt{M_N^2 + 2M_N\nu - Q^2}$$
- Bjorken scaling variable

$$x_{\text{Bjorken}} = \frac{Q^2}{2M_N\nu}$$

Polarized DIS

- Deep Inelastic Scattering
 - with polarized electron beams
 - and polarized targets
- Probes spin states of the quarks
- Spin structure functions, g_1 and g_2
 - 2 different target polarization directions

Cross Section & Spin Structure Functions

$$\frac{d^2\sigma}{d\Omega dE'} = \frac{4\alpha^2 E'^2 \cos^2 \frac{\theta}{2}}{Q^4} \left[\frac{F_2}{\nu} + 2 \frac{F_1}{M} \tan^2 \frac{\theta}{2} \right]$$

$$\frac{d^2\sigma}{dE' d\Omega} (\downarrow \uparrow - \uparrow \uparrow) = \frac{4\alpha^2}{MQ^2} \frac{E'}{\nu E} \left[(E + E' \cos \theta) \textcolor{red}{g}_1 - \frac{Q^2}{\nu} \textcolor{red}{g}_2 \right]$$

$$\frac{d^2\sigma}{dE' d\Omega} (\downarrow \Rightarrow - \uparrow \Rightarrow) = \frac{4\alpha^2 \sin \theta}{MQ^2} \frac{{E'}^2}{E} \frac{1}{\nu^2} (\nu \textcolor{red}{g}_1 + 2E \textcolor{red}{g}_2)$$

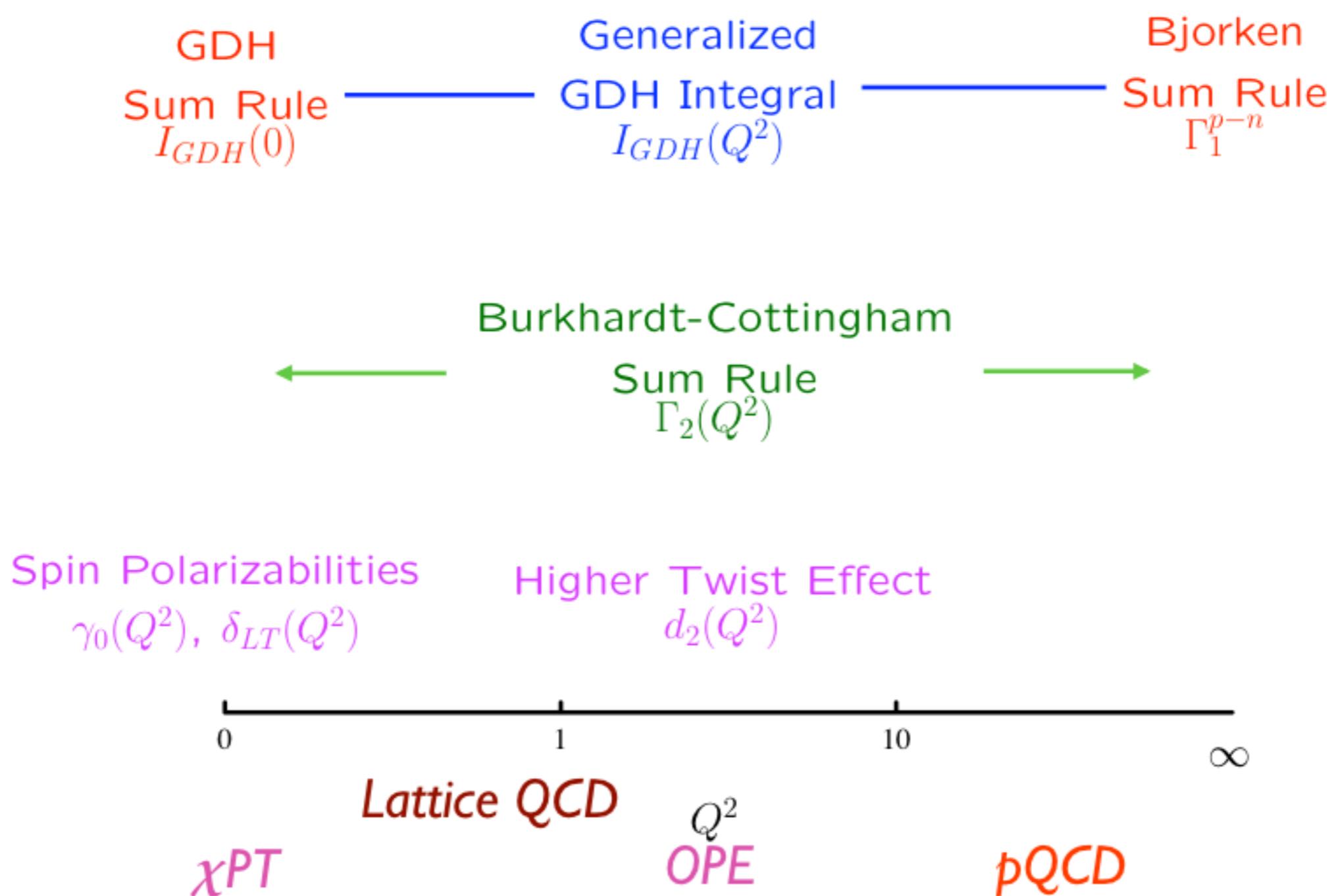
Spin Structure Functions

- g_1 : easy to understand, relatively easy to measure

$$g_1(x, Q^2) = \frac{1}{2} \sum_i e_i^2 [q_i^\uparrow(x, Q^2) - q_i^\downarrow(x, Q^2)]$$

- g_2 : more complex
 - $g_2 = 0$ in naive quark model
 - sensitivity with target polarization perpendicular to beam polarization

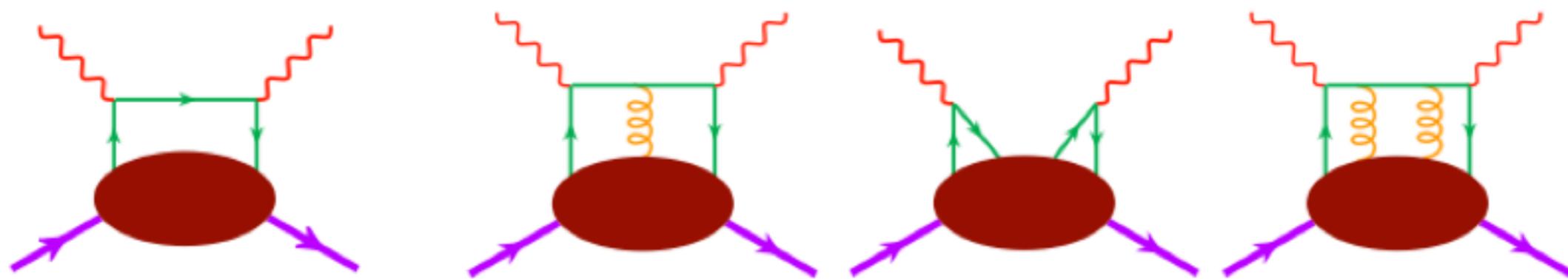
Probe Resolution & Theory Tools



g_2 and Higher Twists

- Decomposition of g_2

$$g_2(x, Q^2) = g_2^{WW}(x, Q^2) + \bar{g}_2(x, Q^2)$$



single quark
scattering

$$\tau = 2$$

qq & qg
correlations

$$\tau > 2$$

g_2 and quark-gluon correlations

g_2 and quark-gluon correlations

- a twist-2 term (Wandzura-Wilcek)

g_2 and quark-gluon correlations

- a twist-2 term (Wandzura-Wilcek)

$$g_2^{WW}(x, Q^2) = -g_1(x, Q^2) + \int_x^1 g_1(x, Q^2) dx$$

g_2 and quark-gluon correlations

- a twist-2 term (Wandzura-Wilcek)

$$g_2^{WW}(x, Q^2) = -g_1(x, Q^2) + \int_x^1 g_1(x, Q^2) dx$$

- a twist-3 term with a suppressed twist-2 piece

g_2 and quark-gluon correlations

- a twist-2 term (Wandzura-Wilcek)

$$g_2^{WW}(x, Q^2) = -g_1(x, Q^2) + \int_x^1 g_1(y, Q^2) dy$$

- a twist-3 term with a suppressed twist-2 piece

$$\bar{g}_2(x, Q^2) = - \int_x^1 \frac{\partial}{\partial y} \left[\frac{m_q}{M} h_T(y, Q^2) + \xi(y, Q^2) \right] \frac{dy}{y}$$

g_2 and quark-gluon correlations

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Transversity

g_2 and quark-gluon correlations

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qg correlations

Interesting Features of g_2

- twist-3 effects: *quark-gluon* correlations
 - d_2 matrix element (3rd moment)
- Test of lattice QCD, QCD sum rules and quark models from moments
- Polarizabilities of color fields

$$\chi_B = \frac{1}{3}(4d_2 + f_2)$$
$$\chi_E = \frac{1}{3}(4d_2 - 2f_2)$$

Interesting Features of g_2

- Color Lorentz force on transverse polarized quark (3rd moment)
 - sign of d_2 related to the sign of the transverse deformation
- Contains chiral odd twist-2 = quark transverse spin (mass term)
 - test of quark masses (covariant parton models)

d_2 Matrix Element

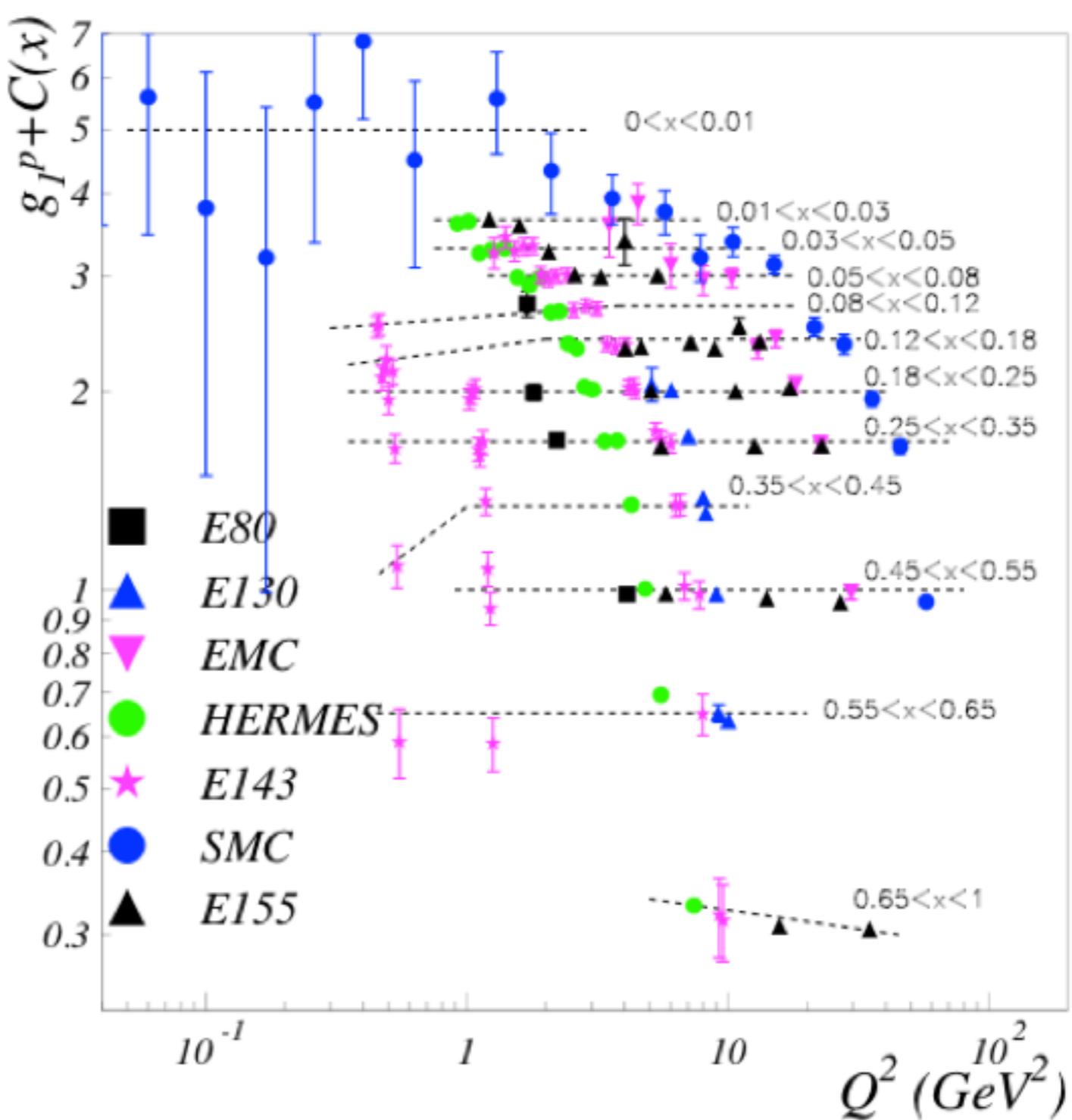
- Dynamical twist-3 matrix element

$$d_2(Q^2) = 3x^2 \int_0^1 \bar{g}_2(x, Q^2) dx$$

$$d_2(Q^2) = \int_0^1 [3g_2(x, Q^2) + 2g_1(x, Q^2)] dx$$

Proton g_1 Structure Function

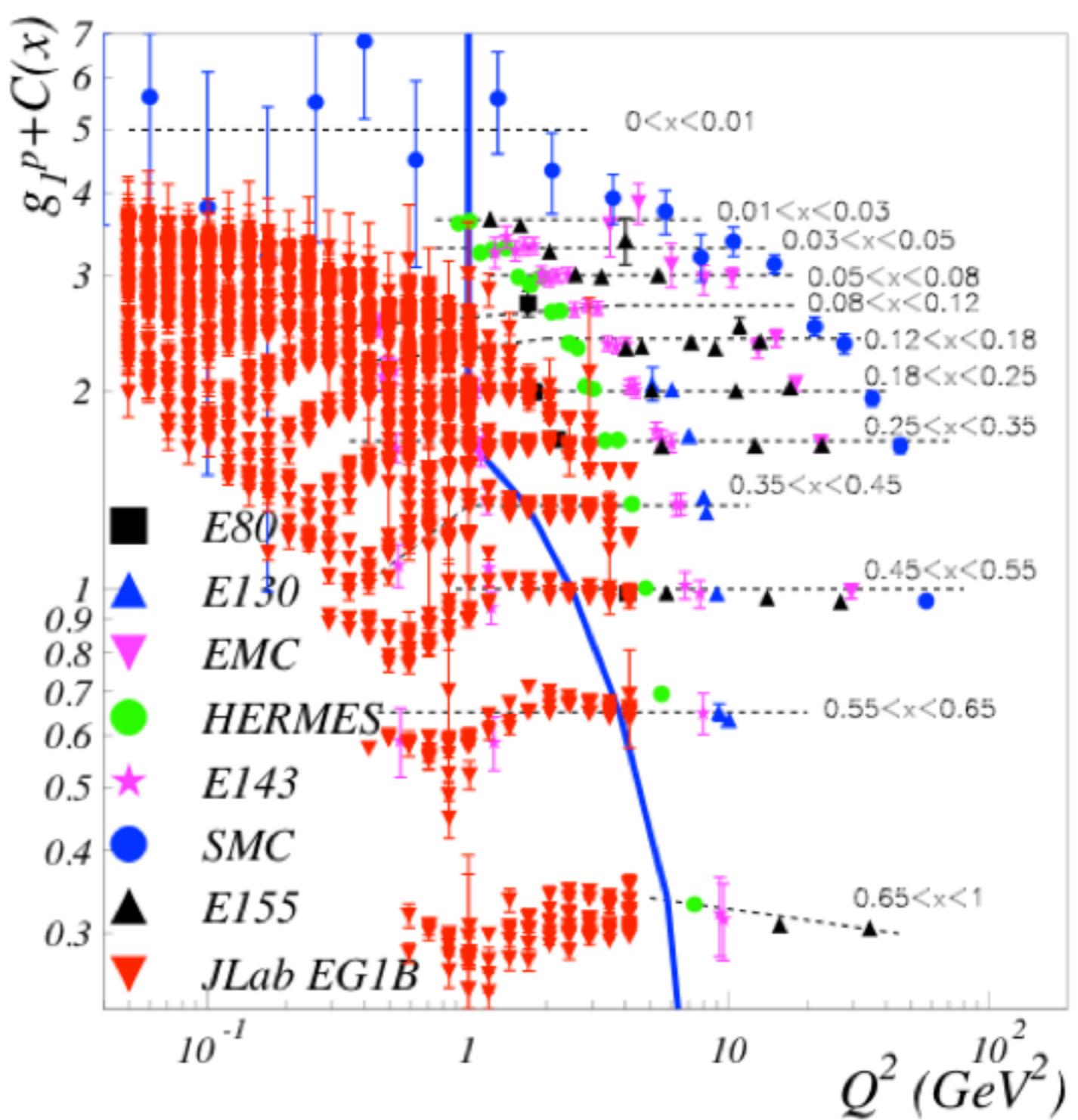
World data on the proton before JLab
(without COMPASS)



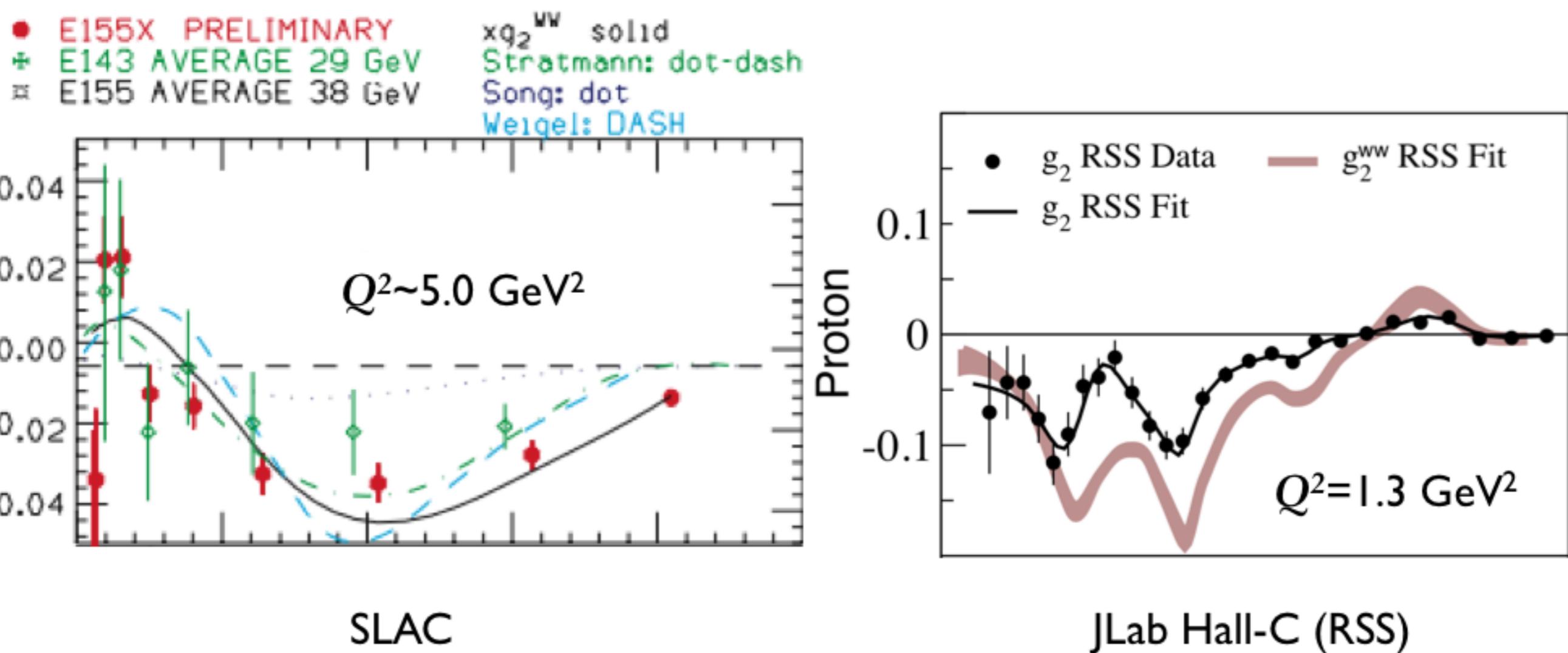
Proton g_1 Structure Function

World data on the proton before JLab
(without COMPASS)

Jefferson Lab Hall-B data



World Data on Proton g_2



World Data on g_1 and g_2

Observable	H target	D target	^3He target
g_1, g_2 at high Q^2	SLAC JLab SANE	SLAC	SLAC JLab E97-117 JLab E01-012 JLab E06-014
g_1, g_2 at low Q^2	JLab RSS	JLab RSS	JLab E94-010 JLab E97-103
g_1, g_2 at $Q^2 \sim 0$	JLab E08-027		JLab E97-110
g_1 at high Q^2	SMC HERMES JLab EGI	SMC HERMES JLab EGI	HERMES
g_1 at low Q^2	SLAC HERMES JLab EGI	SLAC HERMES JLab EGI	HERMES
g_1 at $Q^2 \sim 0$	JLab EG4	JLab EG4	

JLab Data on g_1 and g_2

Observable	H target	D target	^3He target
g_1, g_2 at high Q^2	JLab SANE		JLab E97-117 JLab E01-012 JLab E06-014
g_1, g_2 at low Q^2	JLab RSS	JLab RSS	JLab E94-010 JLab E97-103
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g_1 at high Q^2	JLab EGI	JLab EGI	
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Hall-A

JLab Data on g_1 and g_2

Observable	H target	D target	^3He target
g_1, g_2 at high Q^2	JLab SANE		JLab E97-117 JLab E01-012 JLab E06-014
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g_1 at high Q^2	JLab EGI	JLab EGI	
g_1 at low Q^2	JLab EGI	JLab EGI	Hall-B
g_1 at $Q^2 \sim 0$	JLab EG4	JLab EG4	

JLab Data on g_1 and g_2

Observable	H target	D target	^3He target
g_1, g_2 at high Q^2	JLab SANE		JLab E97-117 JLab E01-012 .. E06-014
g_1, g_2 at low Q^2	JLab RSS	JLab RSS	Hall-C E94-010 JLab E97-103
g_1, g_2 at $Q^2 \sim 0$	JLab E08-027		JLab E97-110
g_1 at high Q^2	JLab EGI	JLab EGI	
g_1 at low Q^2	JLab EGI	JLab EGI	
g_1 at $Q^2 \sim 0$	JLab EG4	JLab EG4	

JLab Experiments focusing on g_2

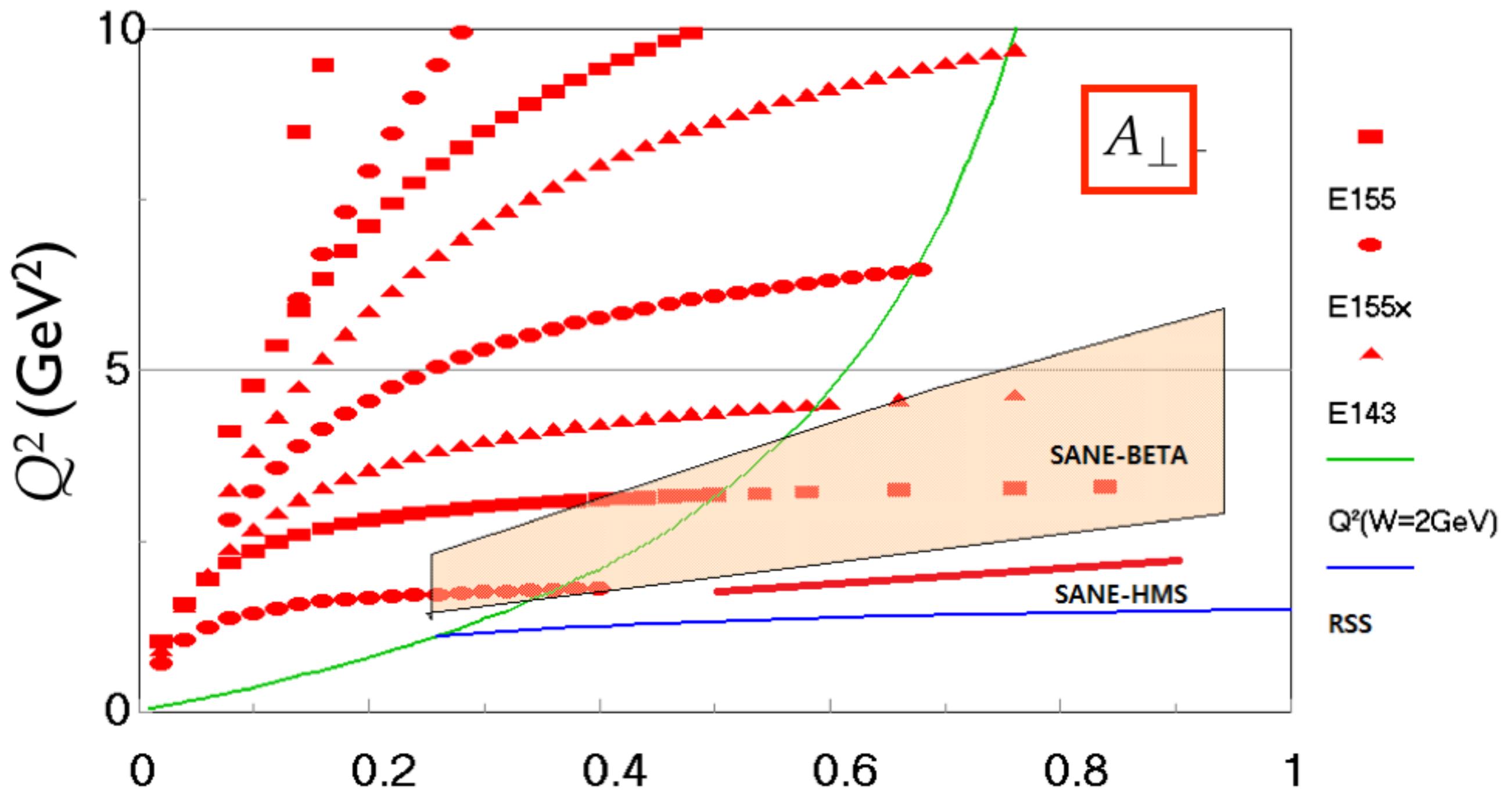
- SANE
 - proton, relatively high Q^2
- d_2^n
 - neutron, relatively high Q^2
- g_2^p
 - proton, very small Q^2
- d_2^n at 12 GeV

Spin Asymmetries of the Nucleon Experiment

Experiment Summary

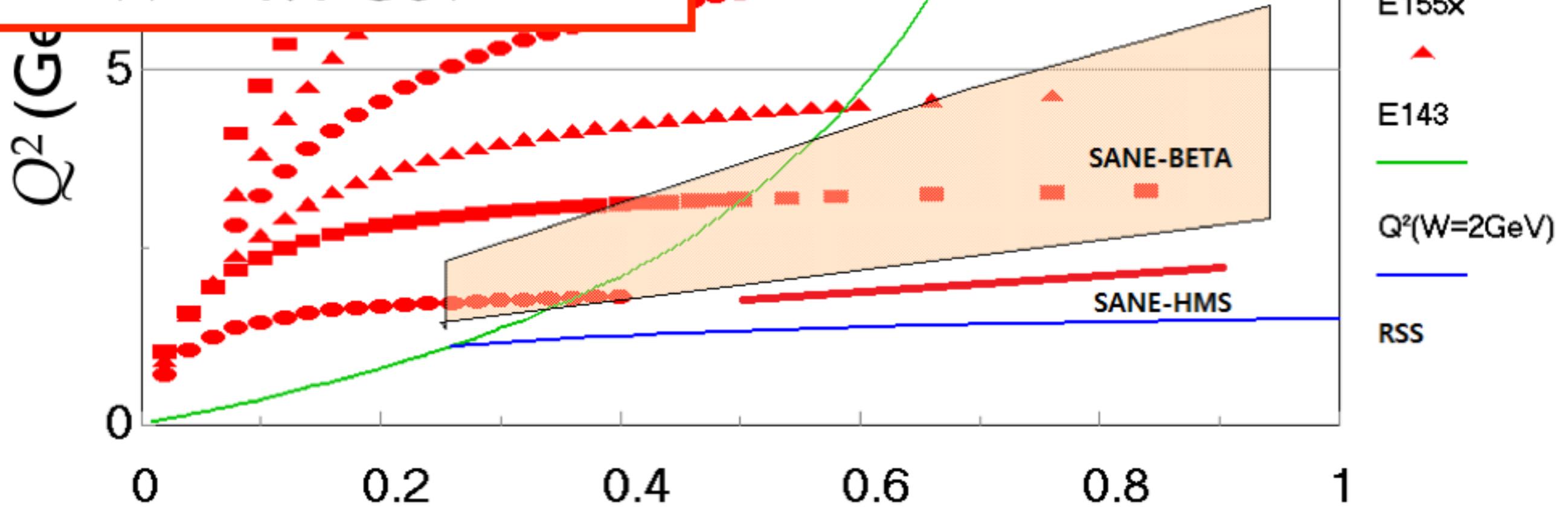
- **Beam**: polarized electron beam (Jefferson Lab) at **4.7** and **5.9** GeV
- **Target**: Polarized **Proton** (NH_3) target
 - Polarization: $\sim 71\%$
 - Orientation: **parallel** (180°) or “**perpendicular**” (80°)
- **Detectors**: **BETA** and **HMS** of Hall-C
- Scattering angle: 40° for **BETA**, 15.5° or 20° for **HMS**

Kinematic Coverage

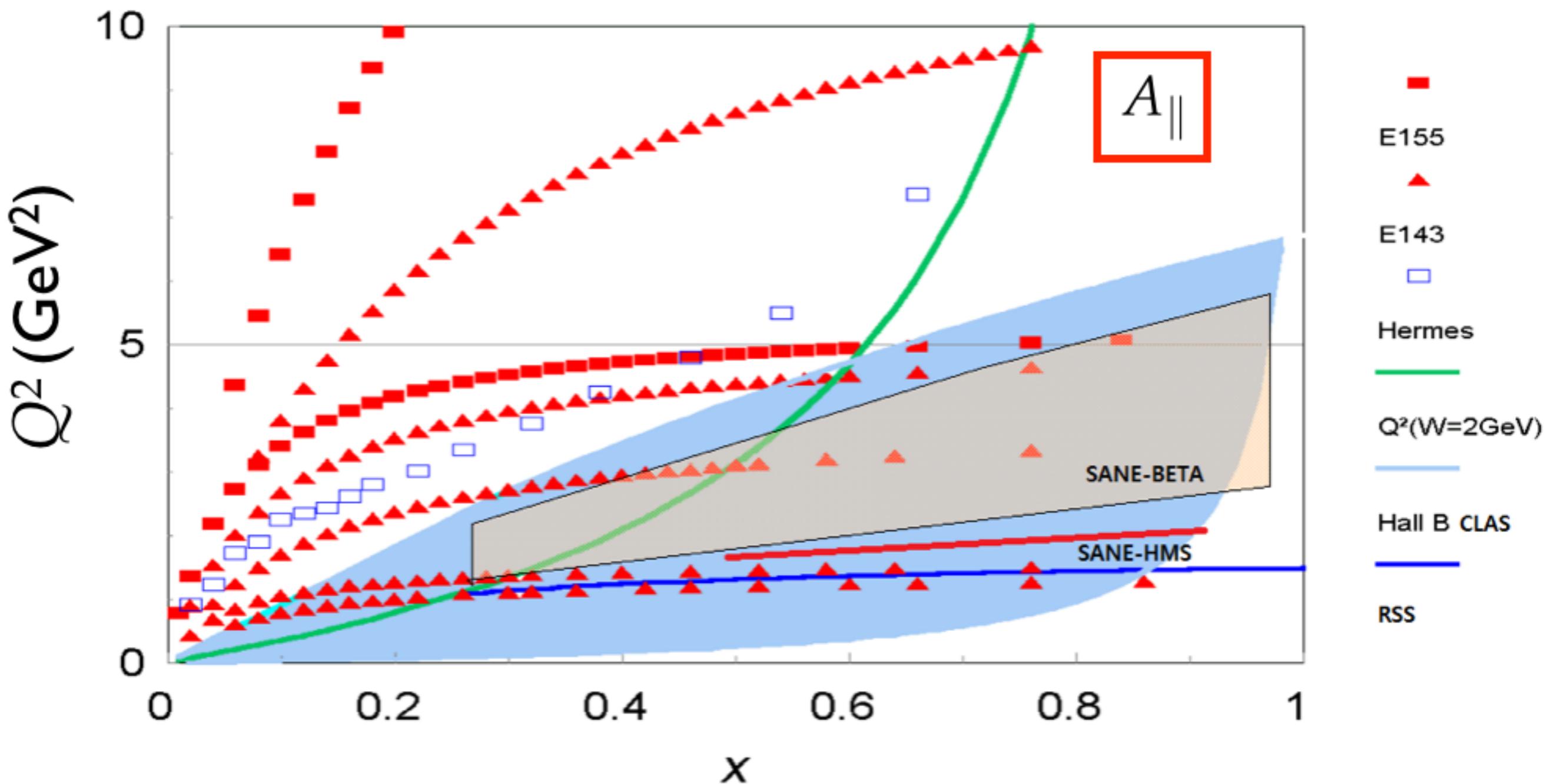


Kinematic Coverage

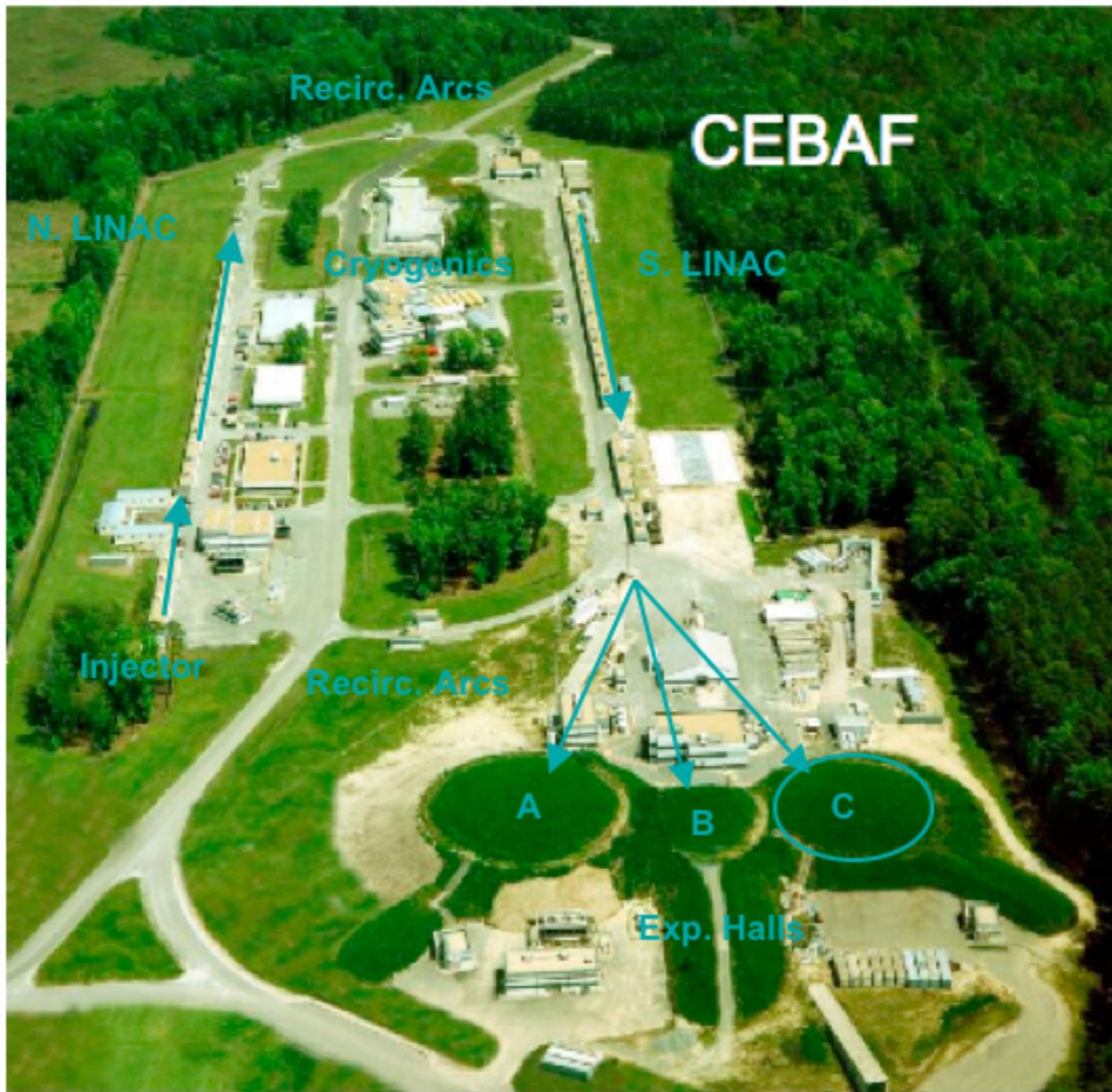
- $2.5 < Q^2 < 6.5 \text{ GeV}^2$
- $0.3 < x < 0.8$
- $W > 1.4 \text{ GeV}$



Kinematic Coverage

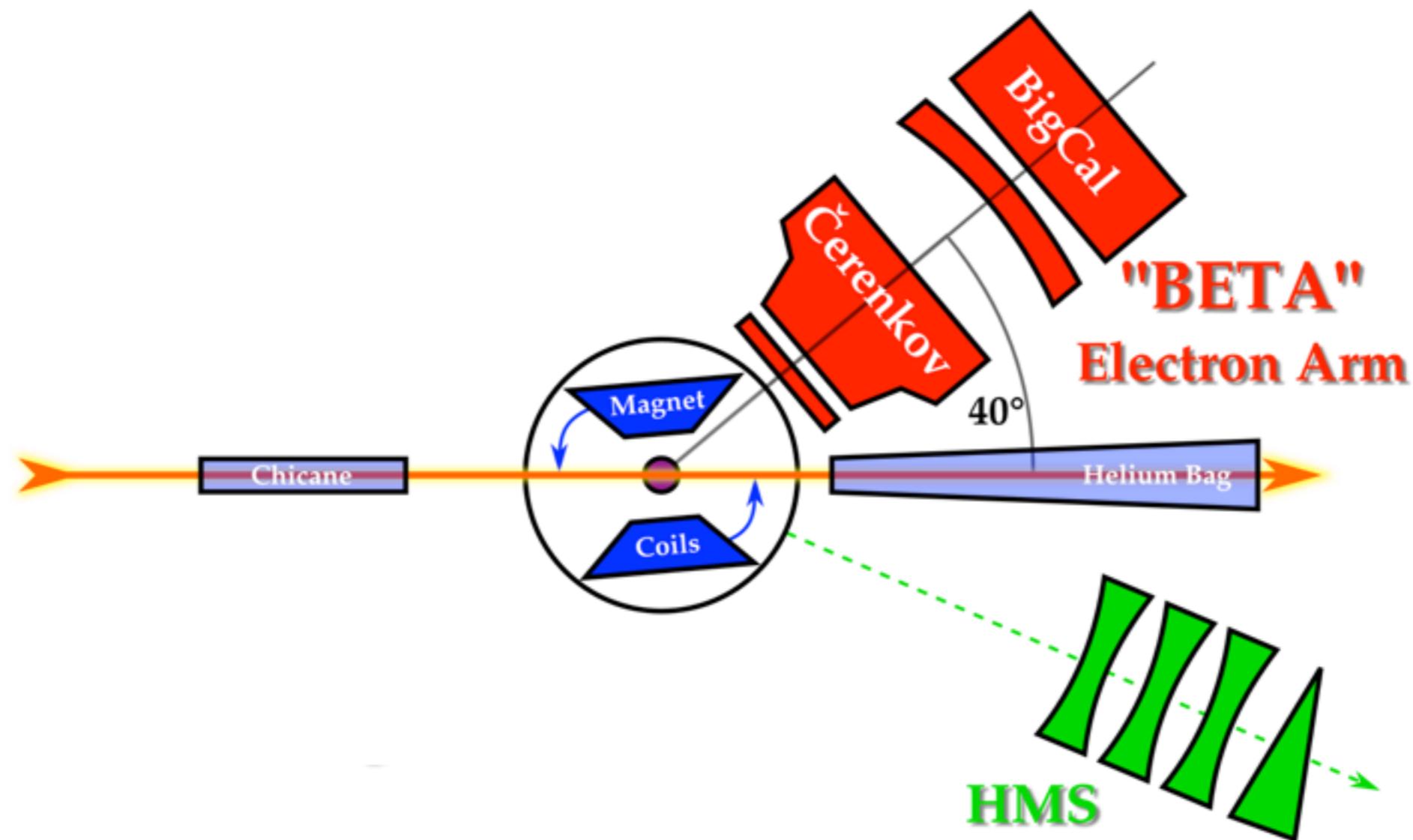


Jefferson Lab

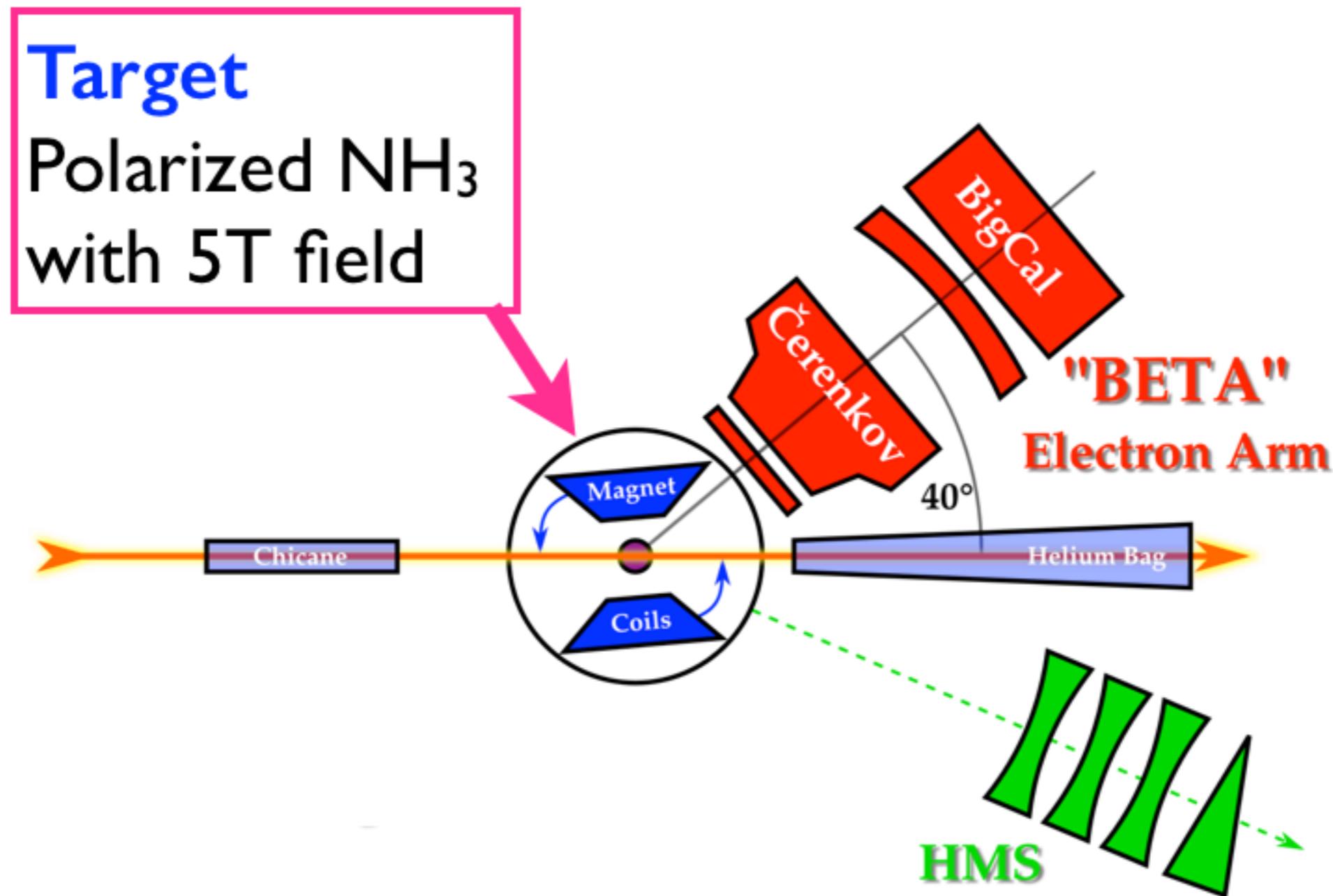


- 2 Linacs with recirculation
- Electron beam of energies up to 6 GeV
- 3 Experimental Halls in simultaneous operation

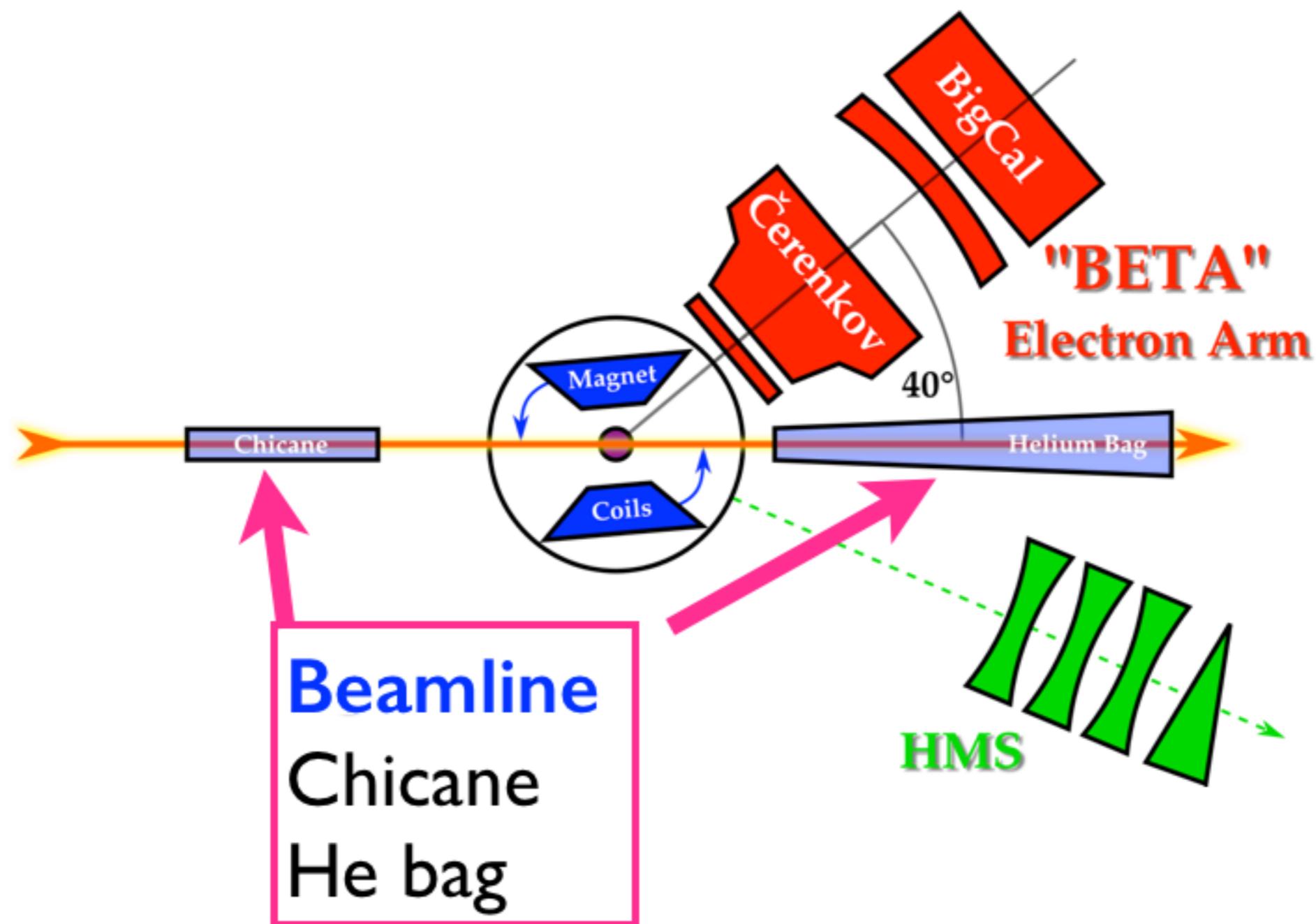
Setup



Setup

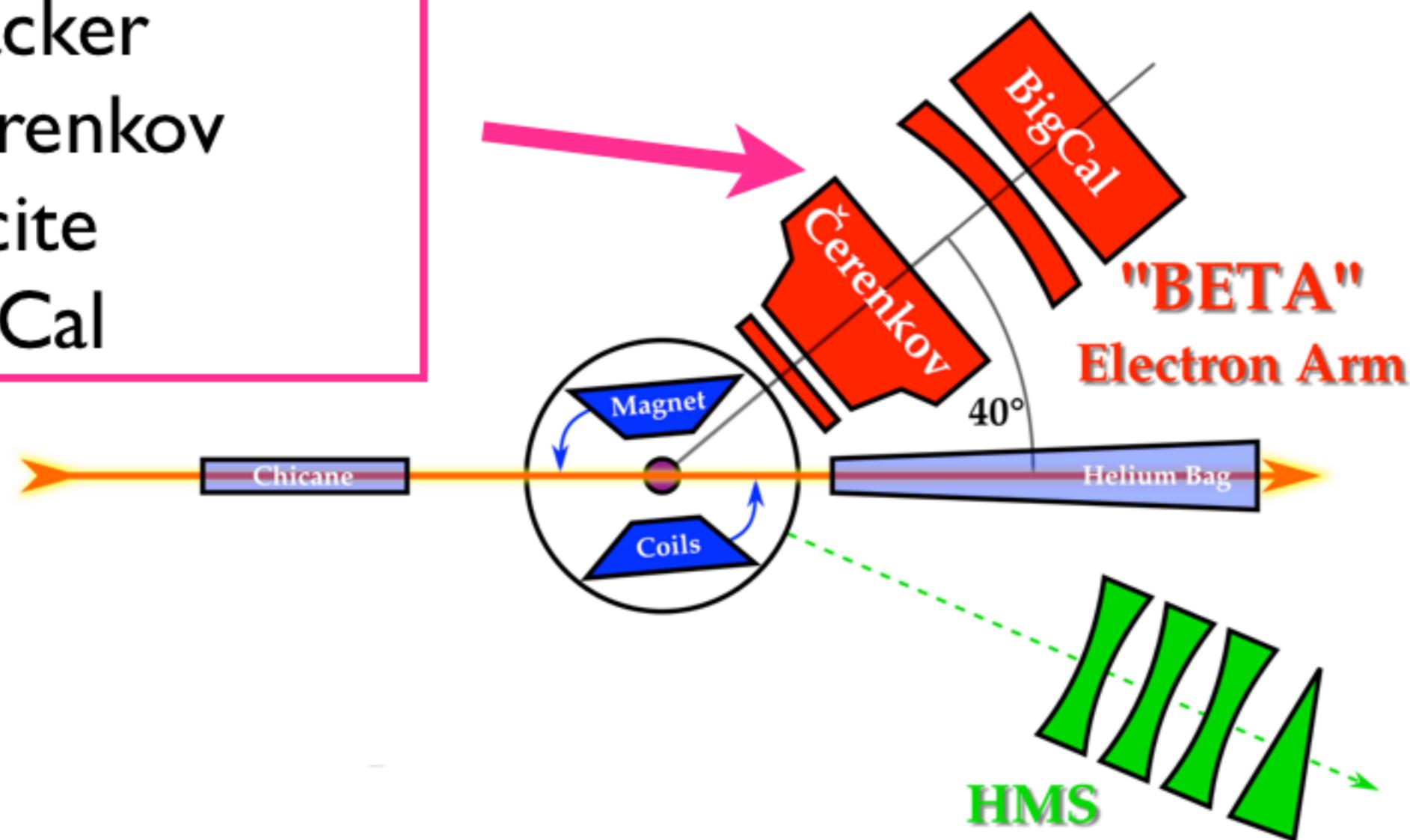


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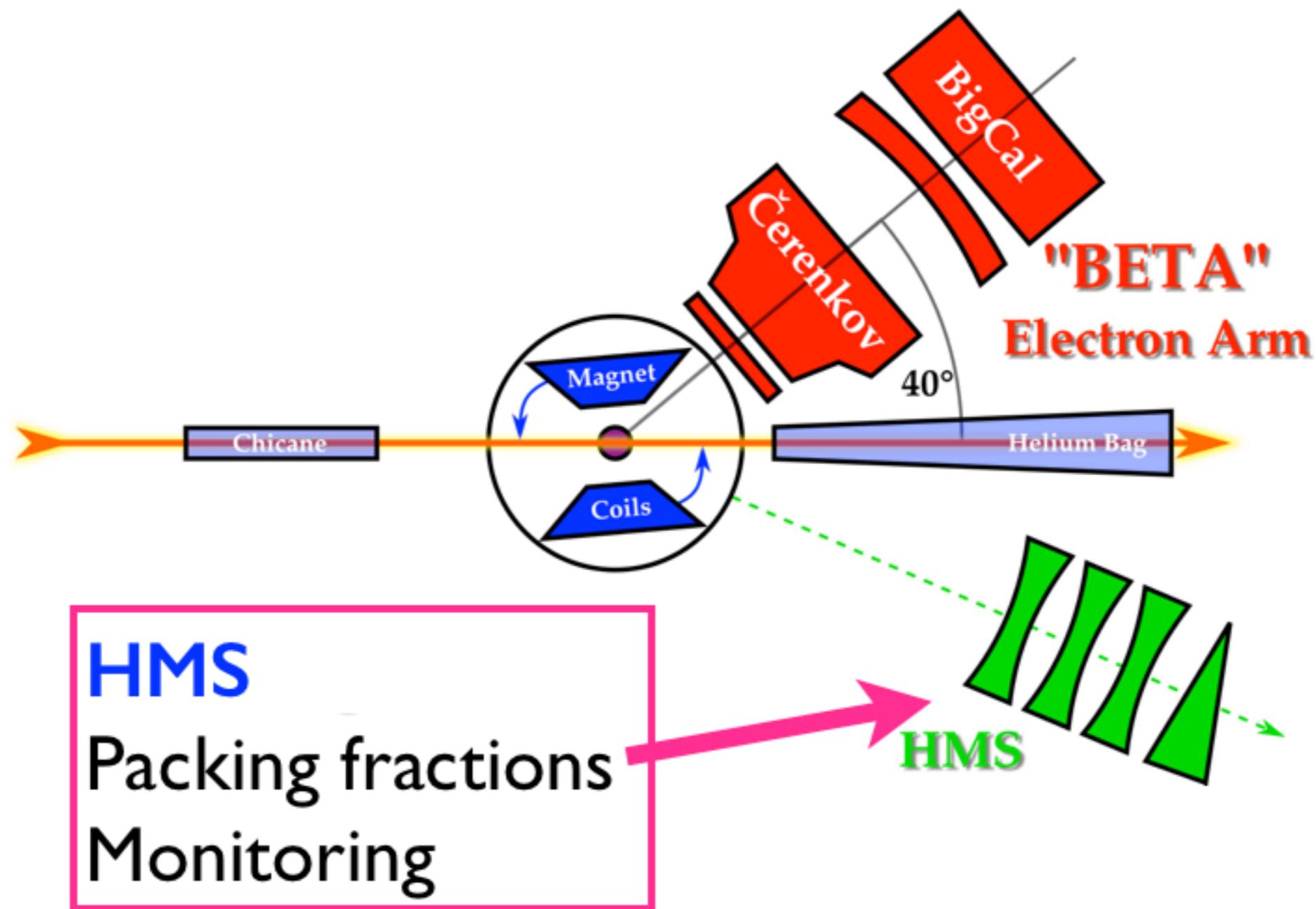


Setup

Electron Arm
Tracker
Cerenkov
Lucite
BigCal



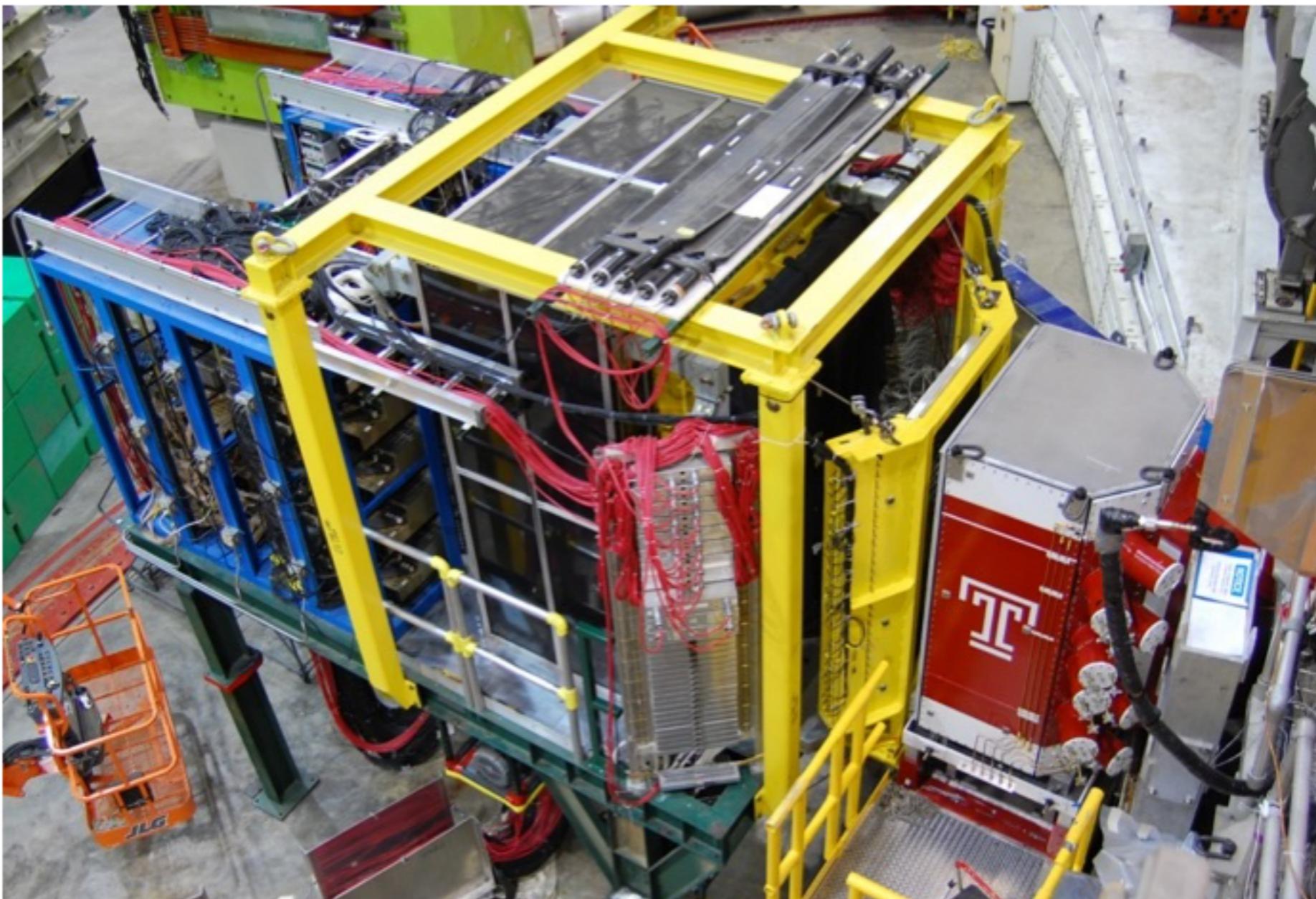
Setup



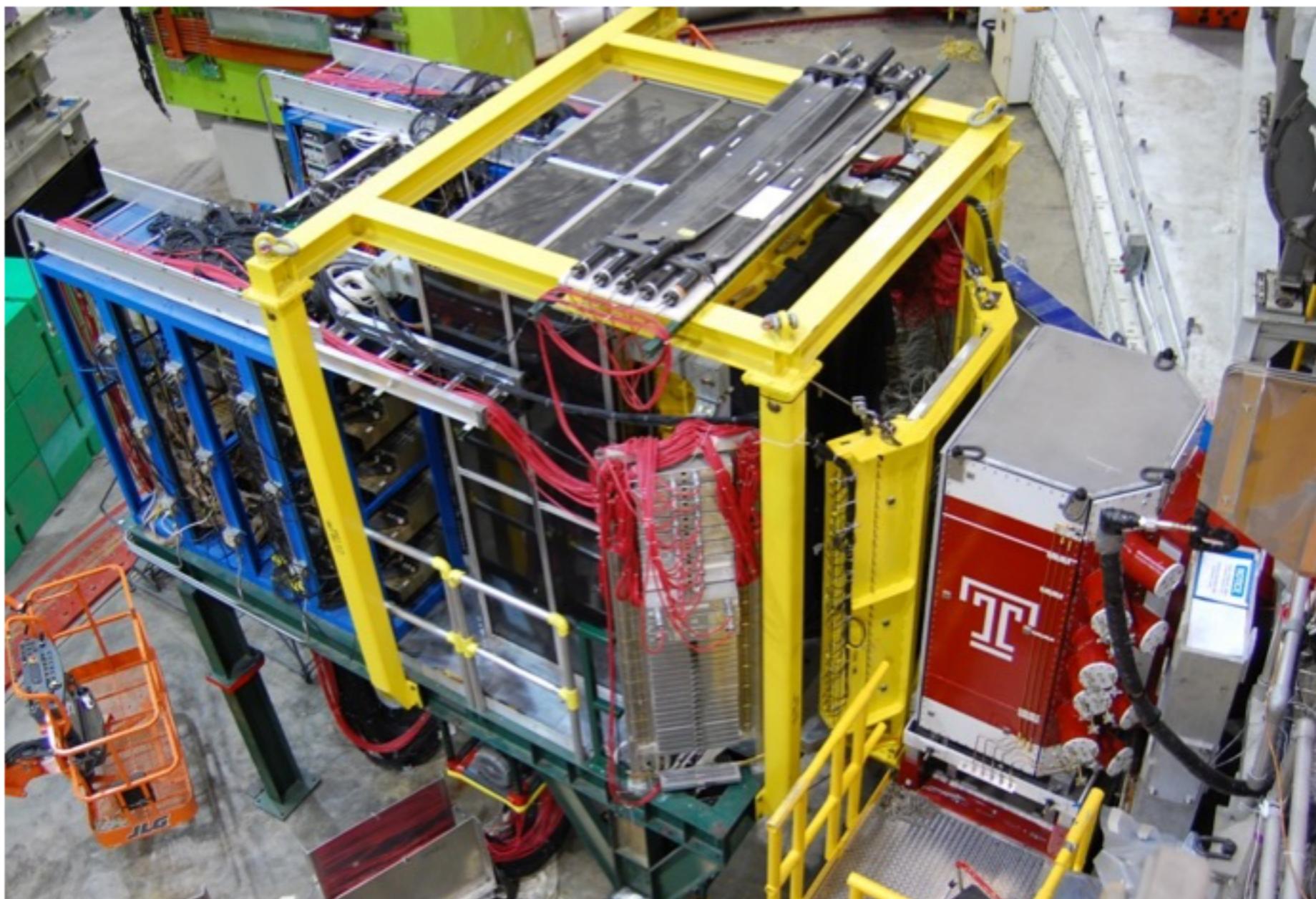
Big Electron Telescope Array

- Electron detector without magnet
- Should provide
 - **Tracking** information
 - Forward tracker, Lucite hodoscope, BigCal
 - **Particle identification**
 - Cerenkov detector
 - **Energy** measurement
 - BigCal (Lead glass calorimeter)

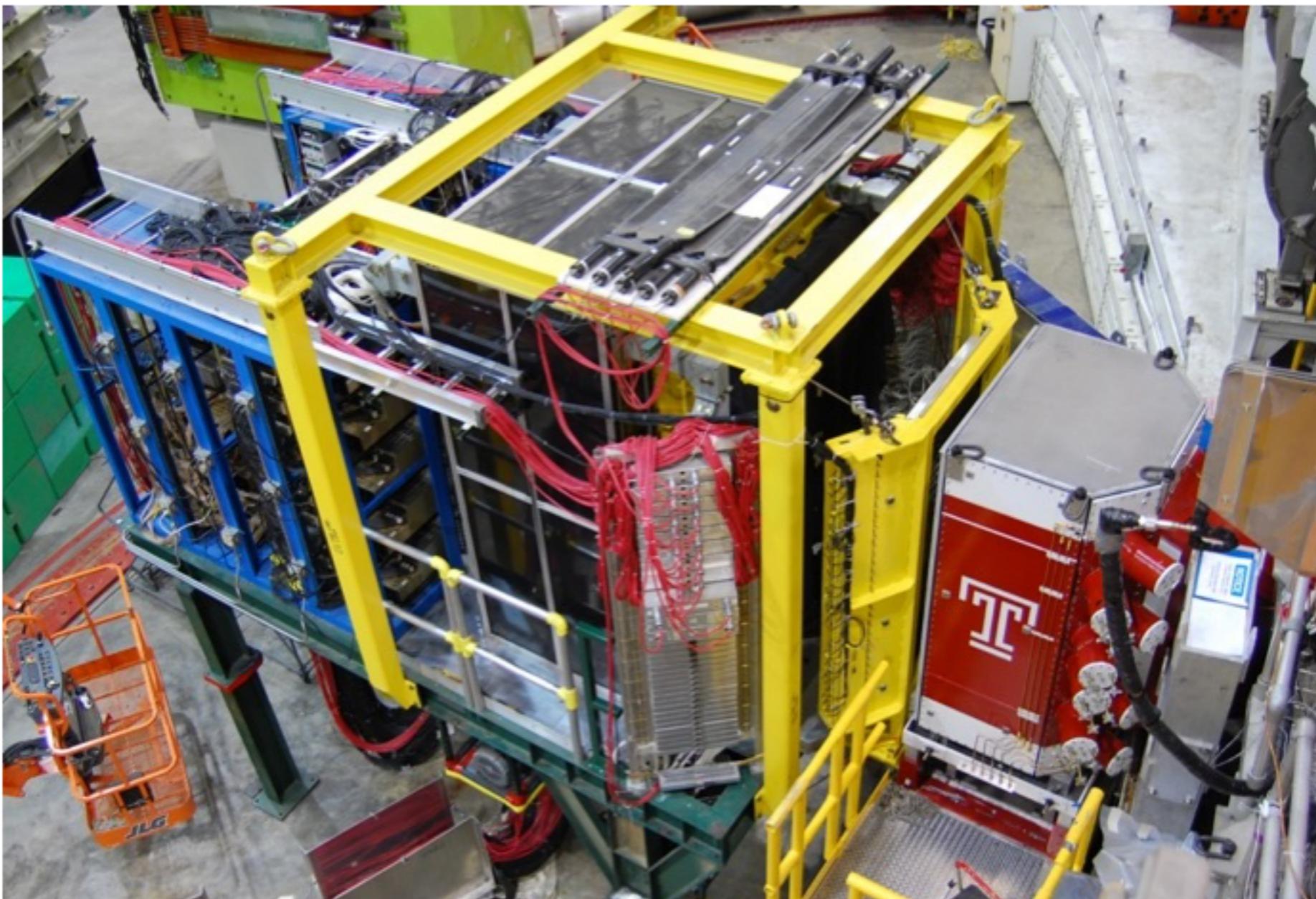
BETA



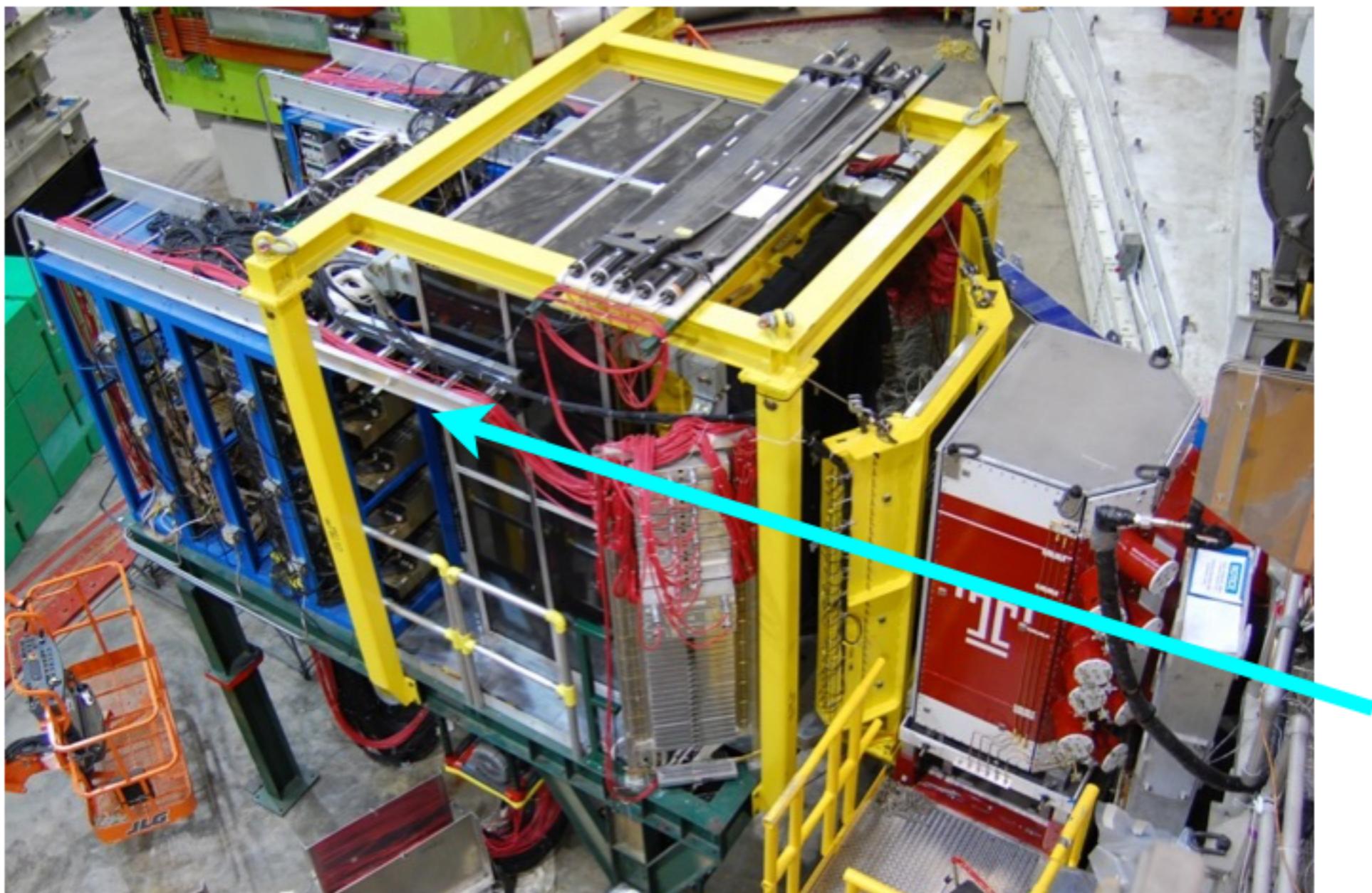
BETA



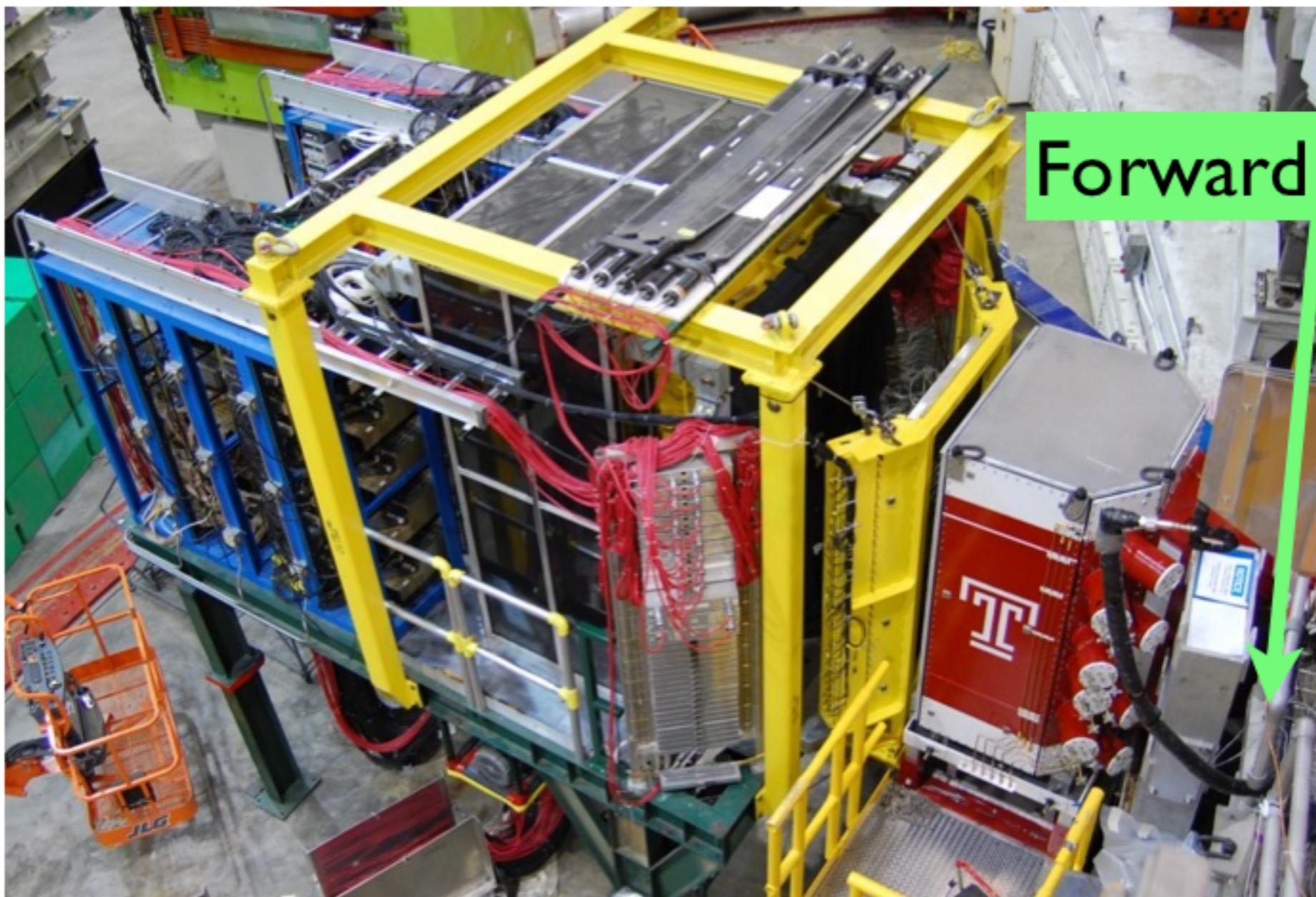
BETA



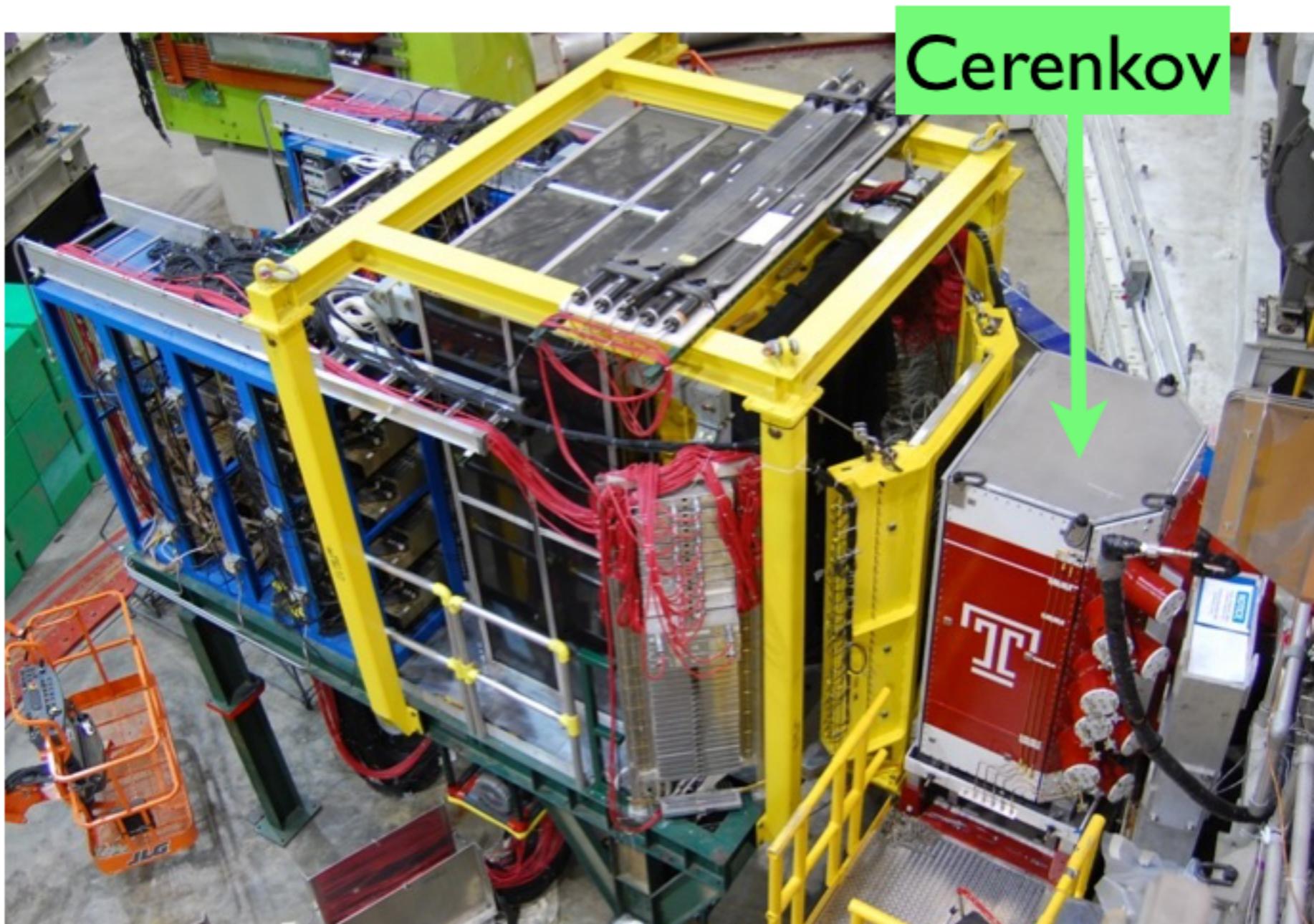
BETA



BETA

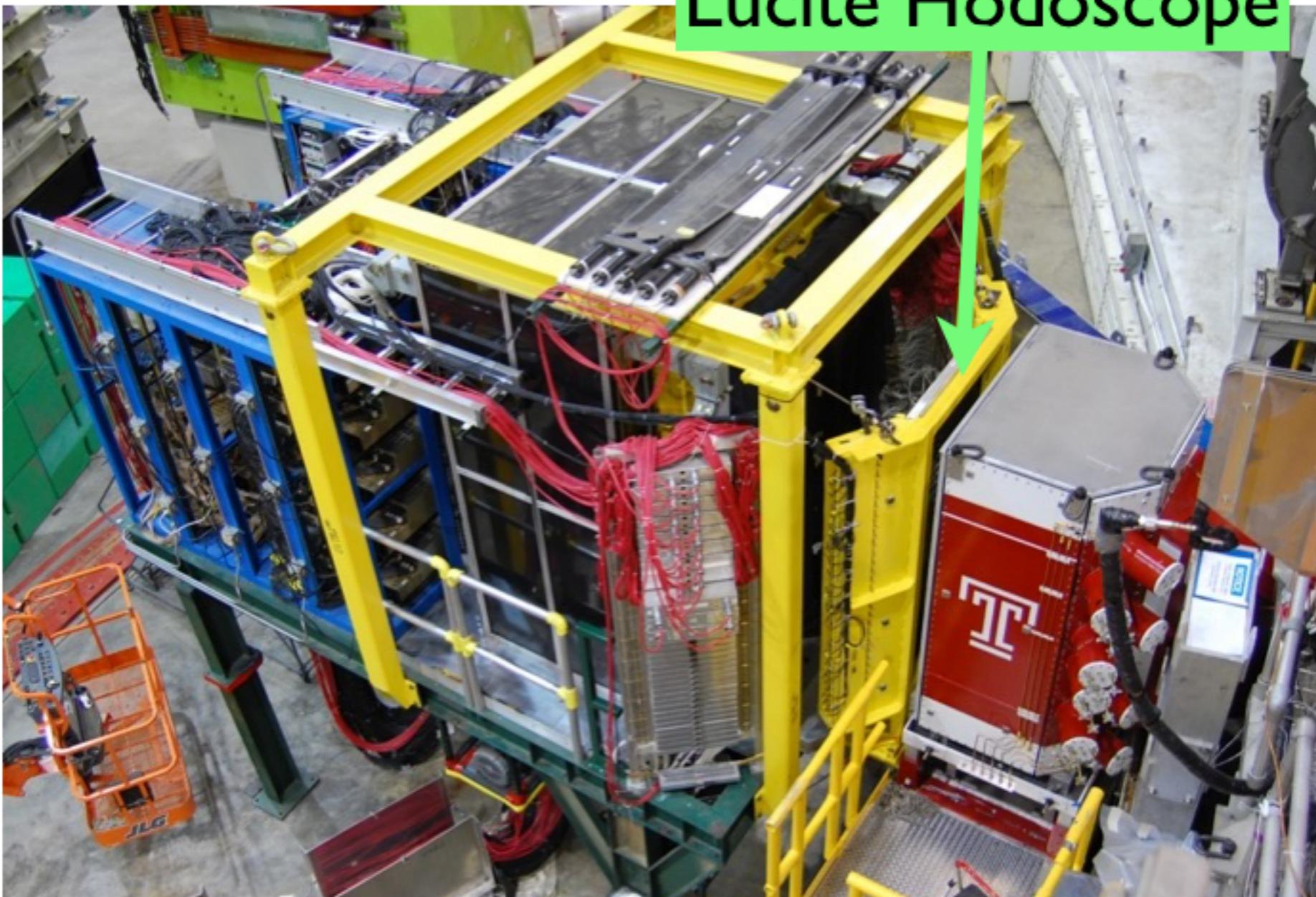


BETA

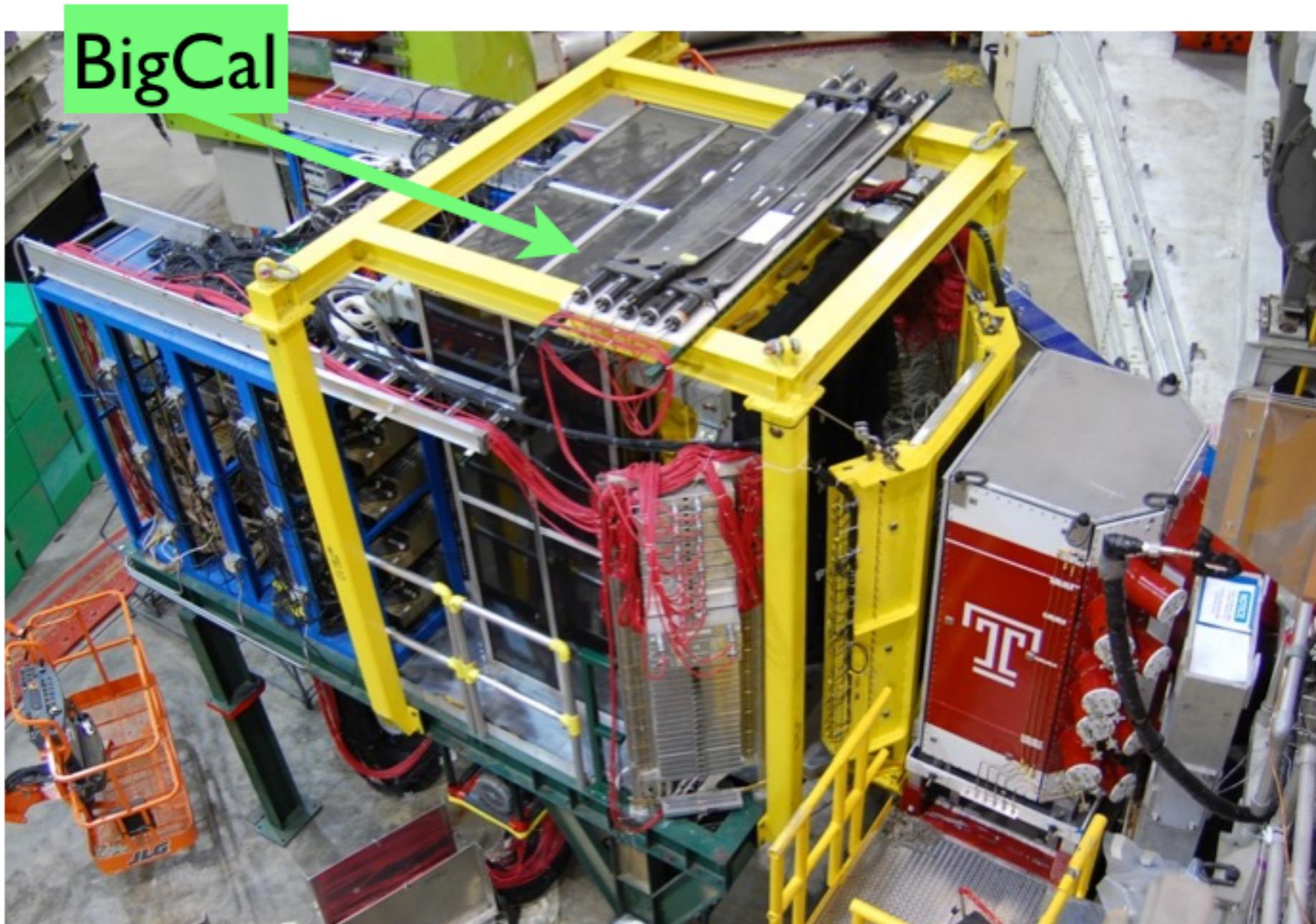


BETA

Lucite Hodoscope

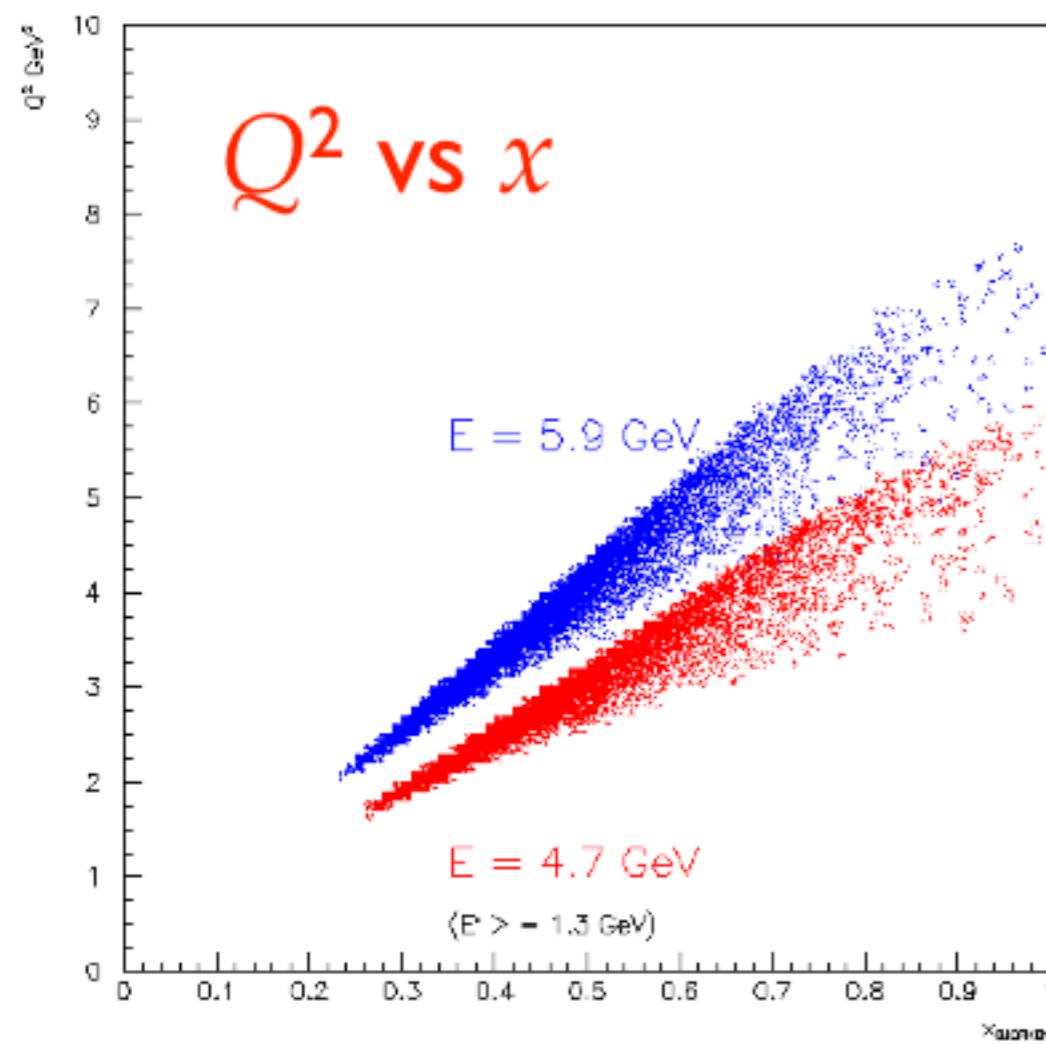


BETA

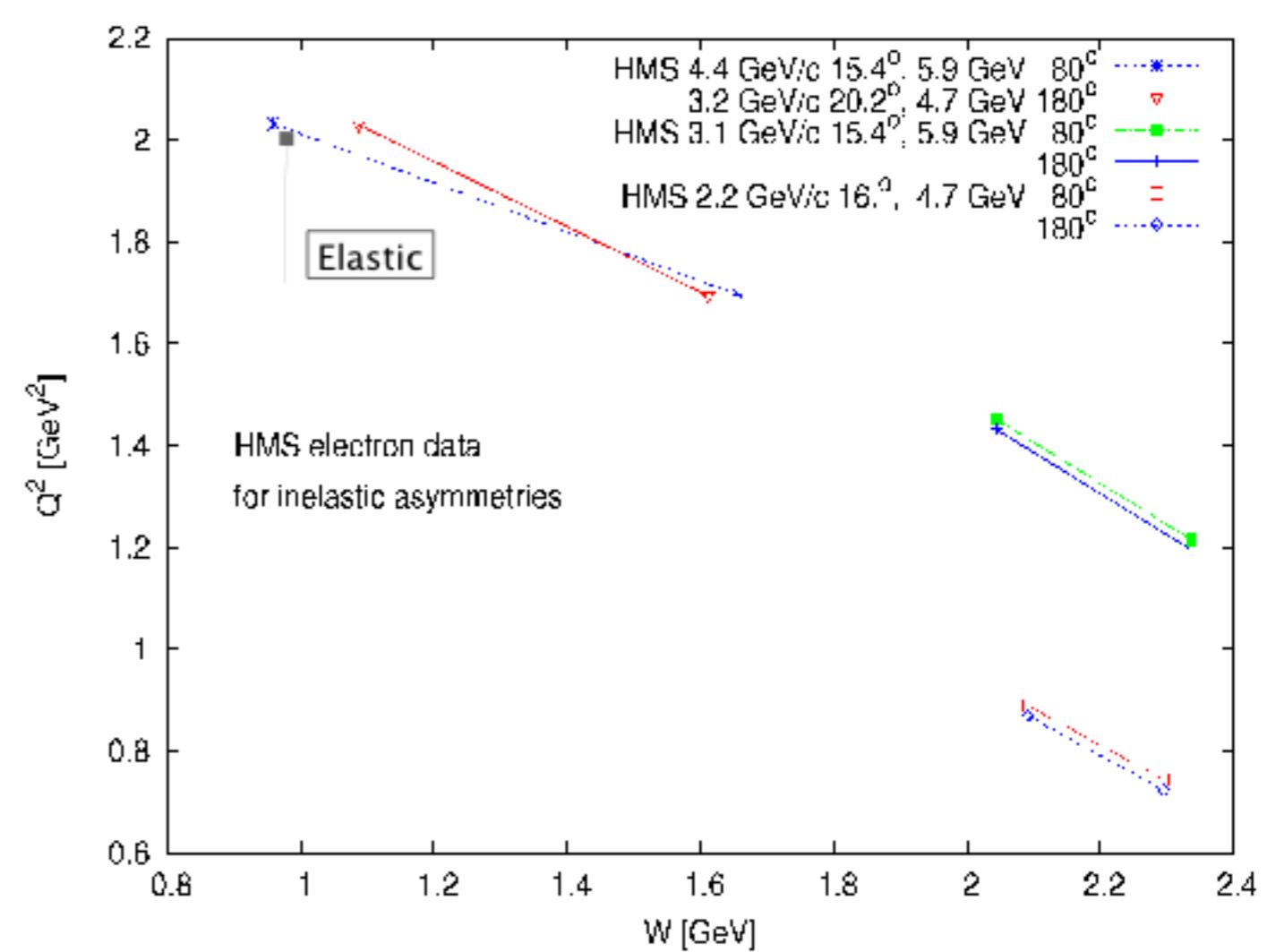


Kinematic Coverage

BETA

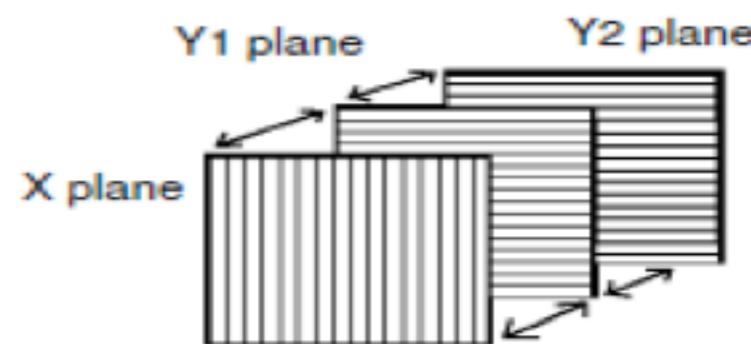


HMS



BETA

- Forward Tracker
 - 3 planes of Bicron Scintillators
 - Early particle tracking
- Cerenkov
 - N₂ gas
 - 8 sets of mirror + PMT
 - Particle ID



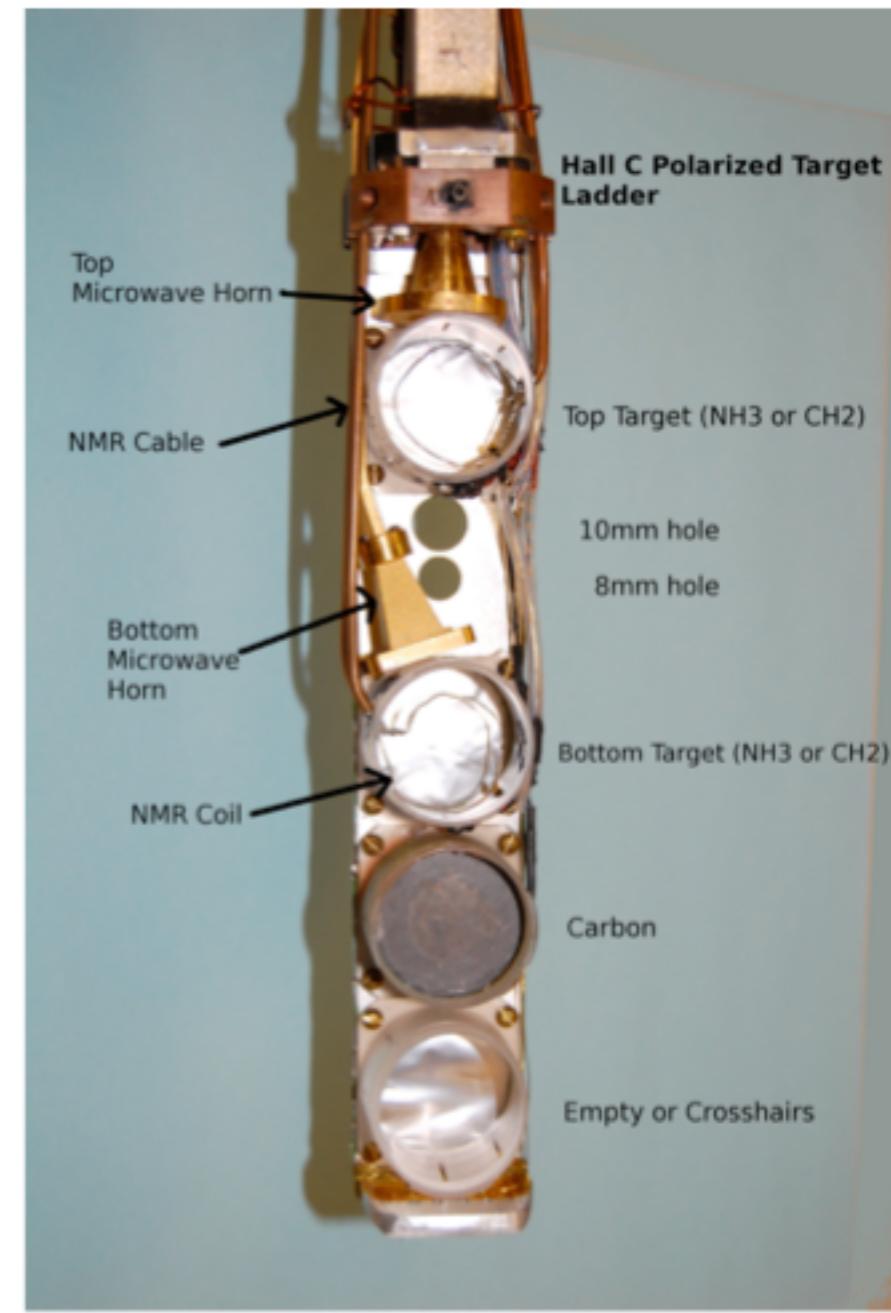
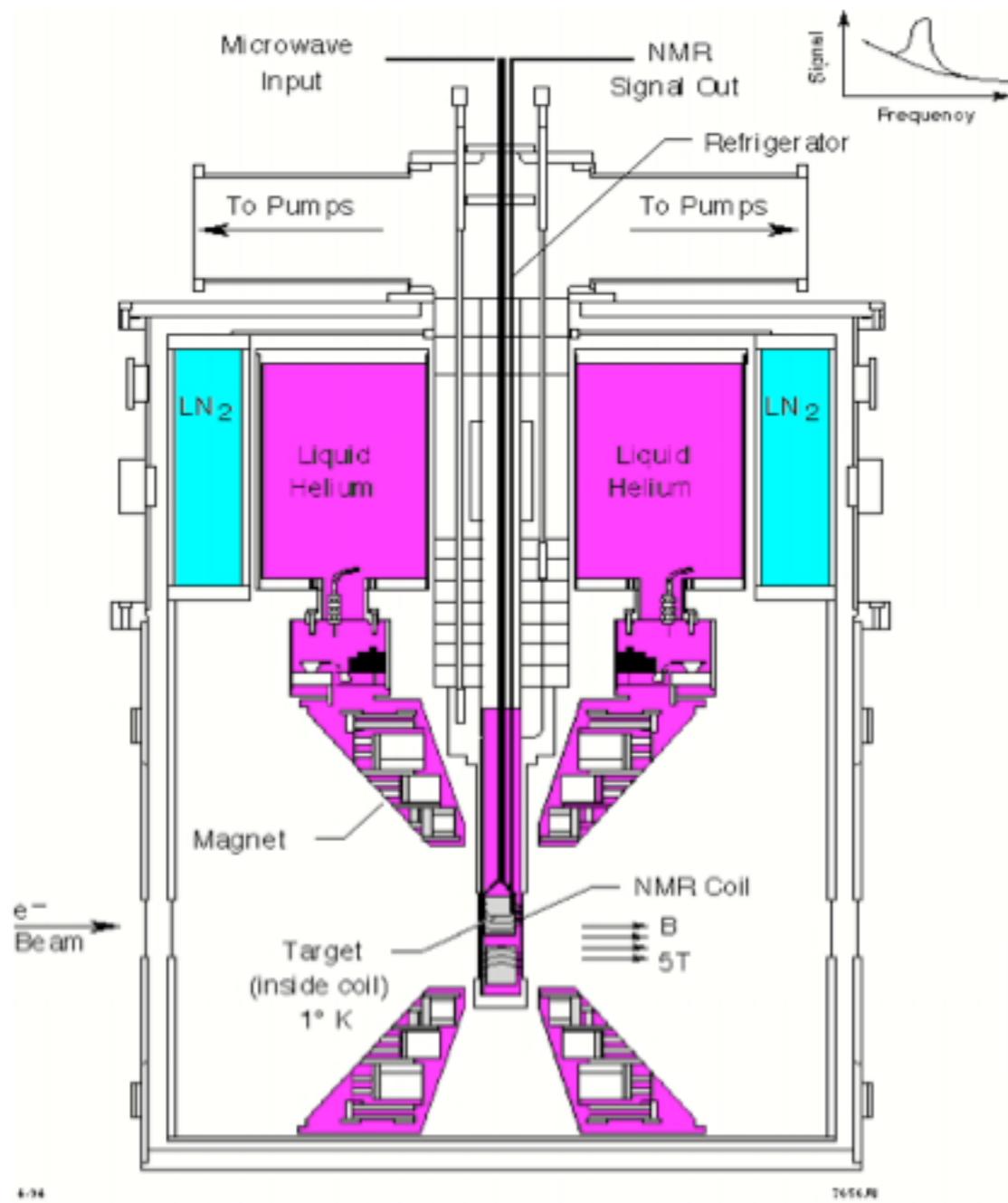
BETA

- **Lucite Hodoscope**
 - 28 bars of 6cm wide lucite
 - Vertically stacked bars for Y information
 - PMT's on both sides for X information
- **BigCal**
 - Lead glass calorimeter
 - 1744 blocks (about 4cm x 4cm each)
 - Position and energy measurement

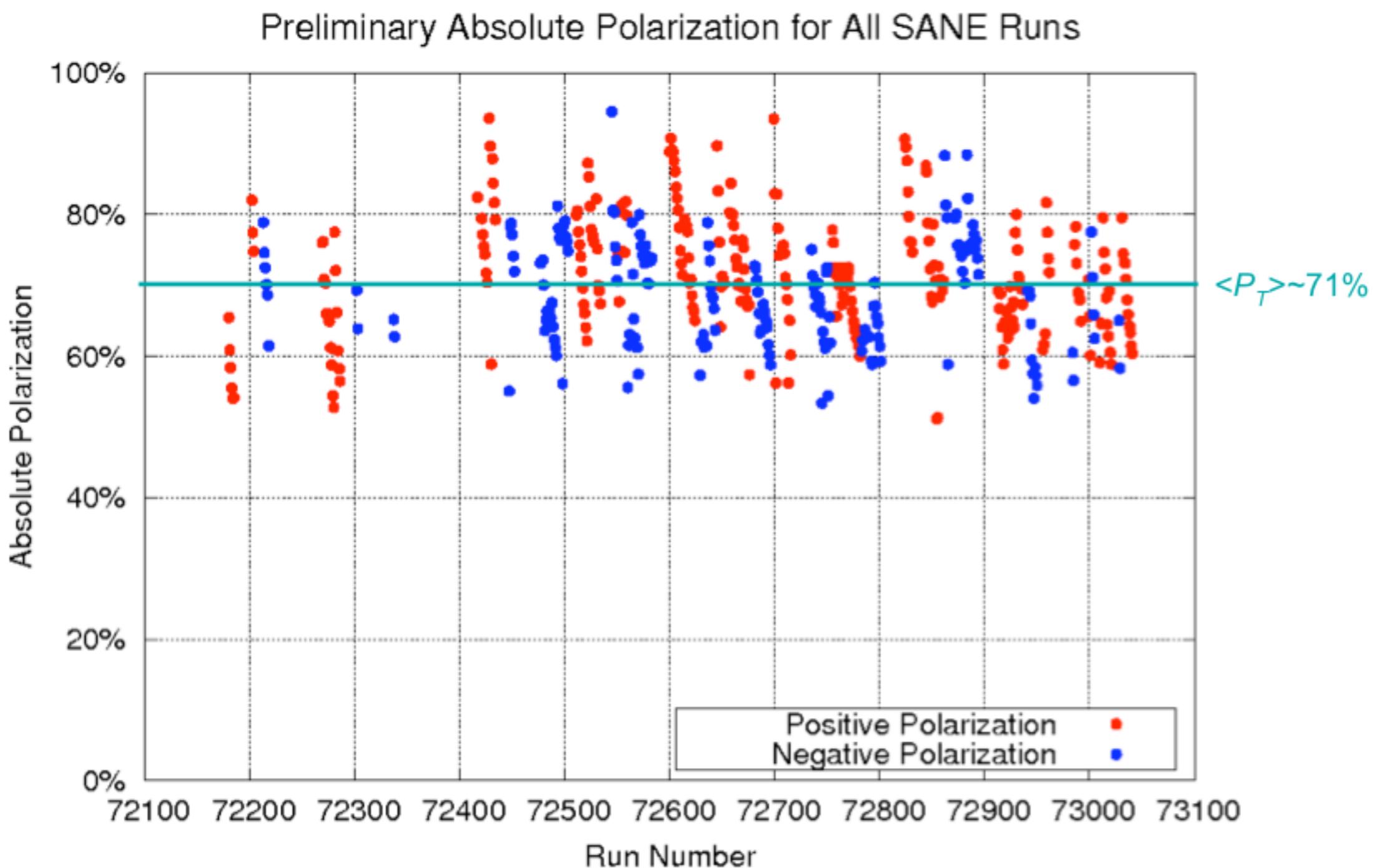
BETA - Characteristics

- Effective solid angle: 0.9 sr
- Energy resolution: $5\%/\sqrt{E(\text{GeV})}$
- Angular resolution $\sim 1\text{mr}$
- Pion rejection of 1000:1
- Vertex resolution: $\sim 5\text{mm}$

Polarized NH₃ Target



Target Performance



Data Taking

Data Taking

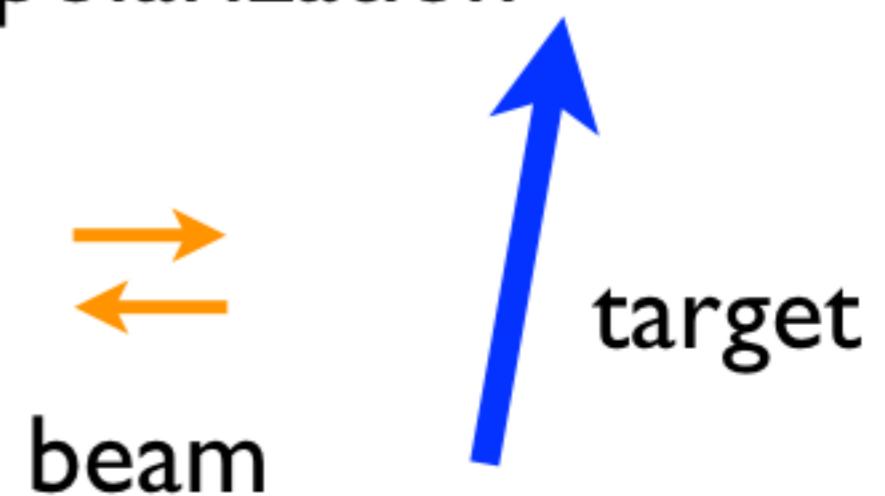
- For 2 beam energies: **4.7** and **5.9**

Data Taking

- For 2 beam energies: **4.7** and **5.9**
- 2 different orientations of polarizations

Data Taking

- For 2 beam energies: **4.7** and **5.9**
- 2 different orientations of polarizations
 - **perpendicular**: target polarization at 80° with respect to the beam polarization



Data Taking

- For 2 beam energies: **4.7** and **5.9**
- 2 different orientations of polarizations
 - **perpendicular**: target polarization at 80° with respect to the beam polarization
 - **parallel**: 180°



Data Analysis

- Beam spin asymmetries

$$A_{\parallel} A_{\perp} = \frac{1}{f P_B P_T} \frac{N^{\uparrow} - N^{\downarrow}}{N^{\uparrow} + N^{\downarrow}}$$

- Physics asymmetries

$$A_1 = \frac{E - E' \cos \theta}{E - E'} A_{\parallel} - \frac{E' \sin \theta}{E - E'} A_{\perp}$$

Data Analysis

- Structure Functions

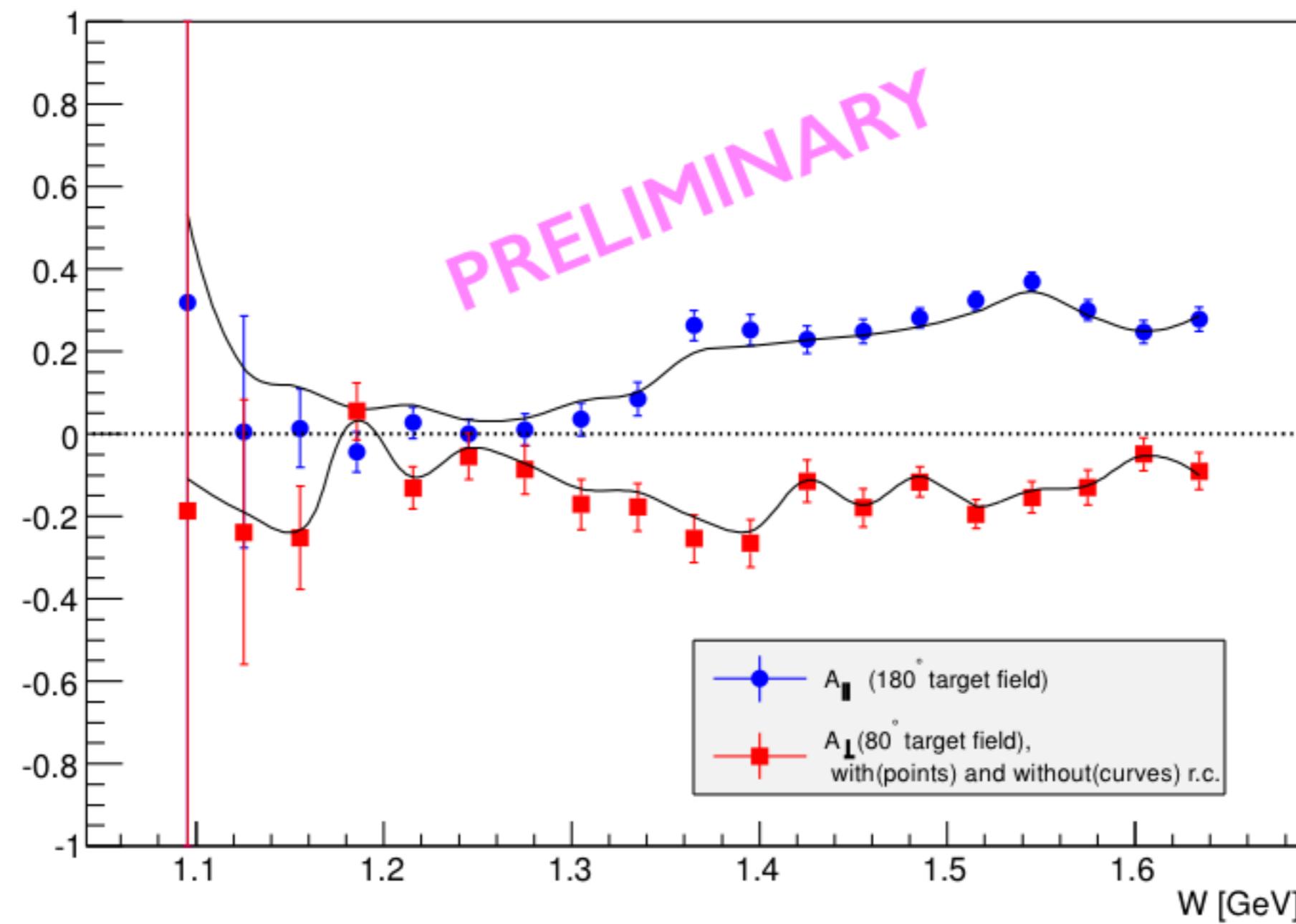
$$g_1 = \frac{F_1}{1 + \gamma^2} (A_1 + \gamma A_2)$$

$$g_2 = \frac{F_1}{\gamma(1 + \gamma^2)} (A_2 - \gamma A_1)$$

- d_2 matrix element

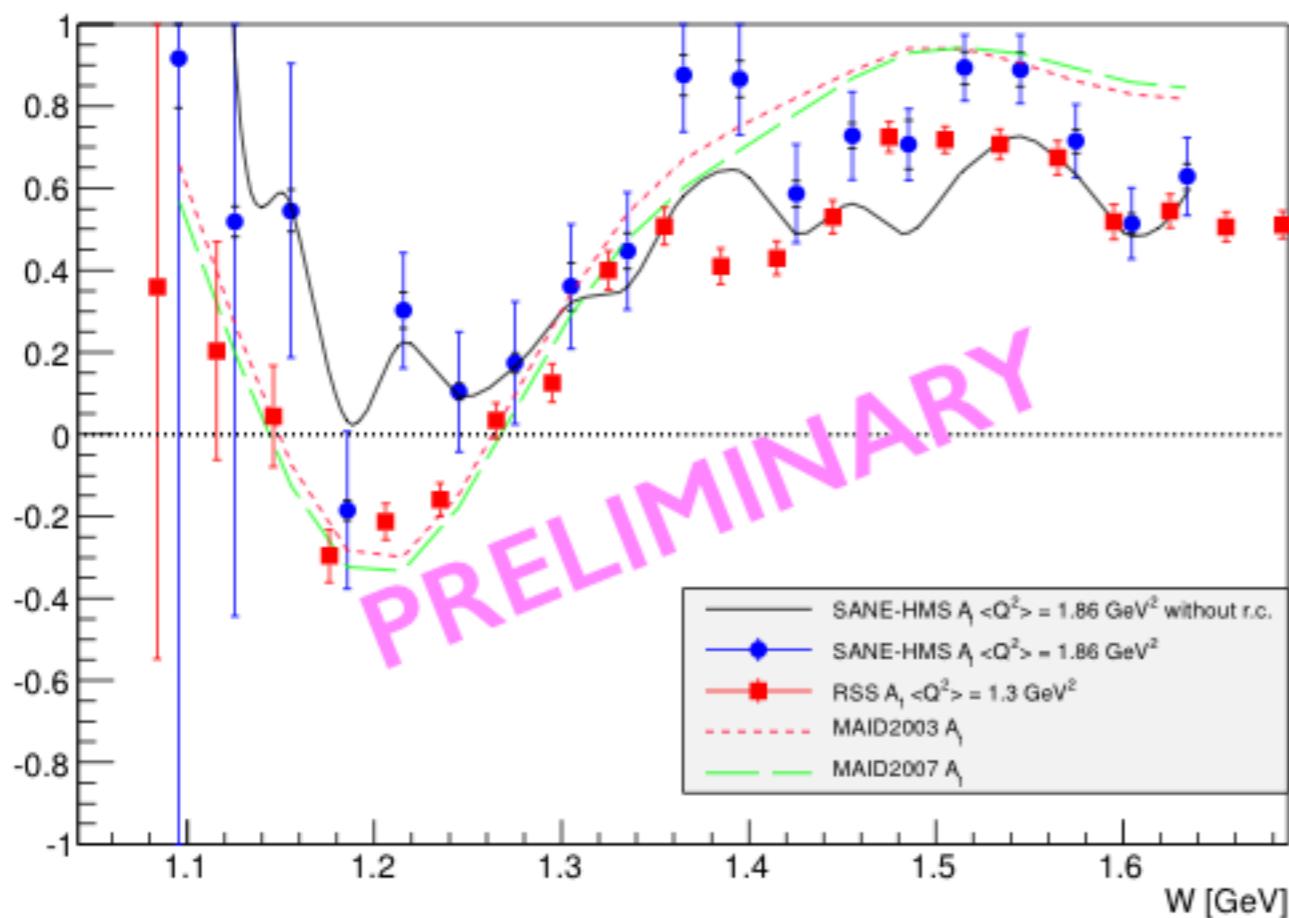
$$d_2(Q^2) = \int_0^1 [3g_2(x, Q^2) + 2g_1(x, Q^2)] dx$$

Parallel & Perpendicular Asymmetries

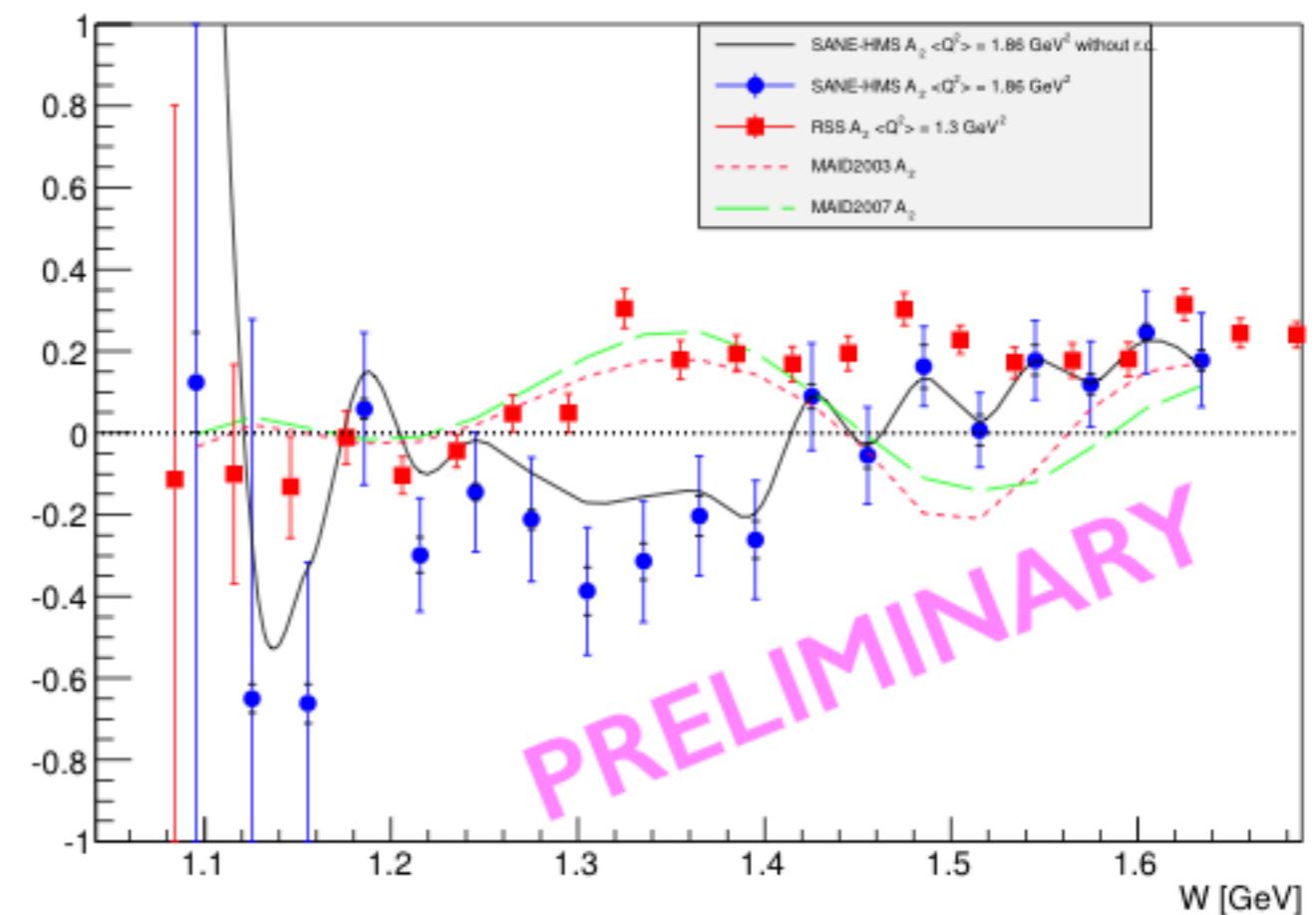


A_1 and A_2

A_1



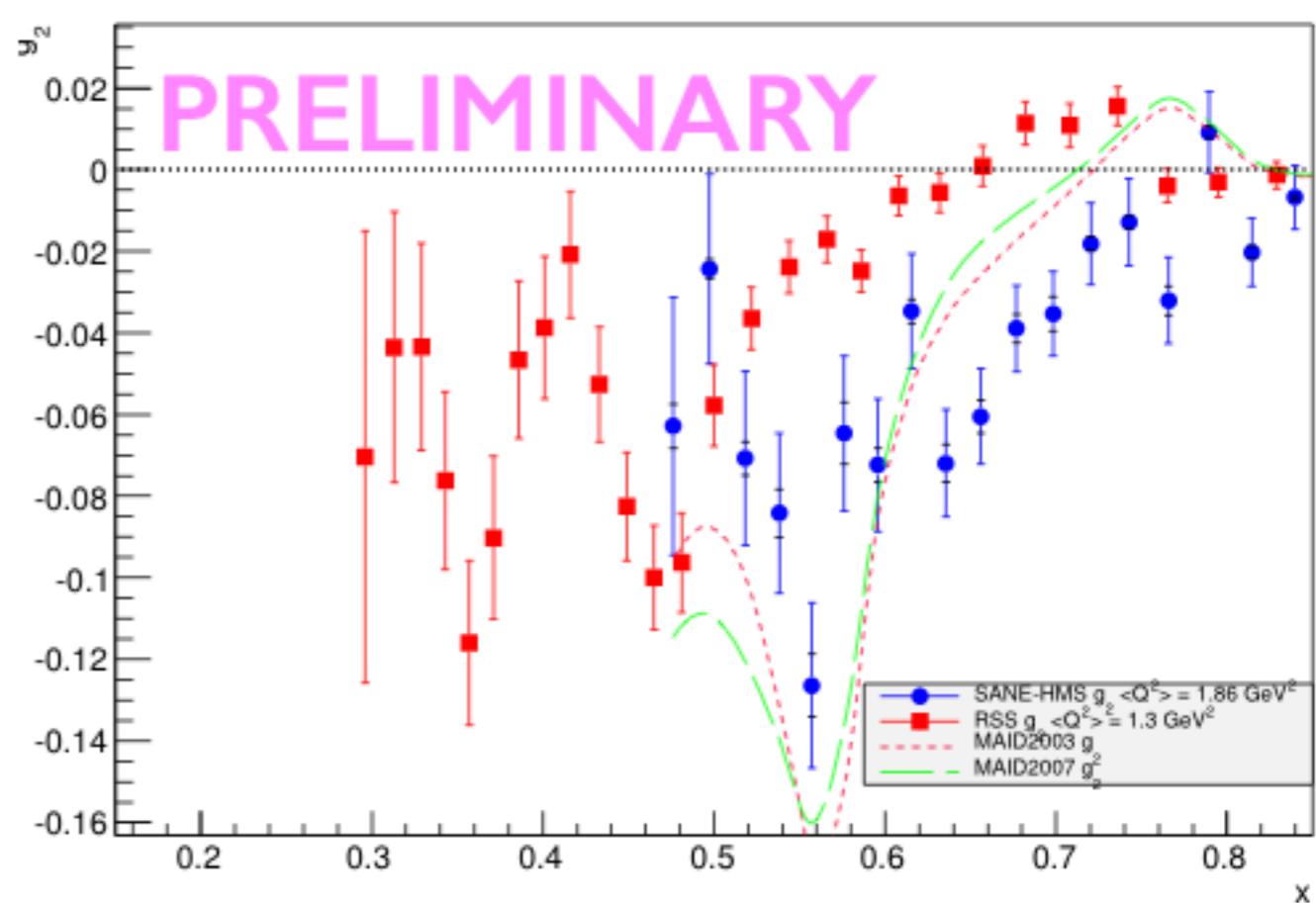
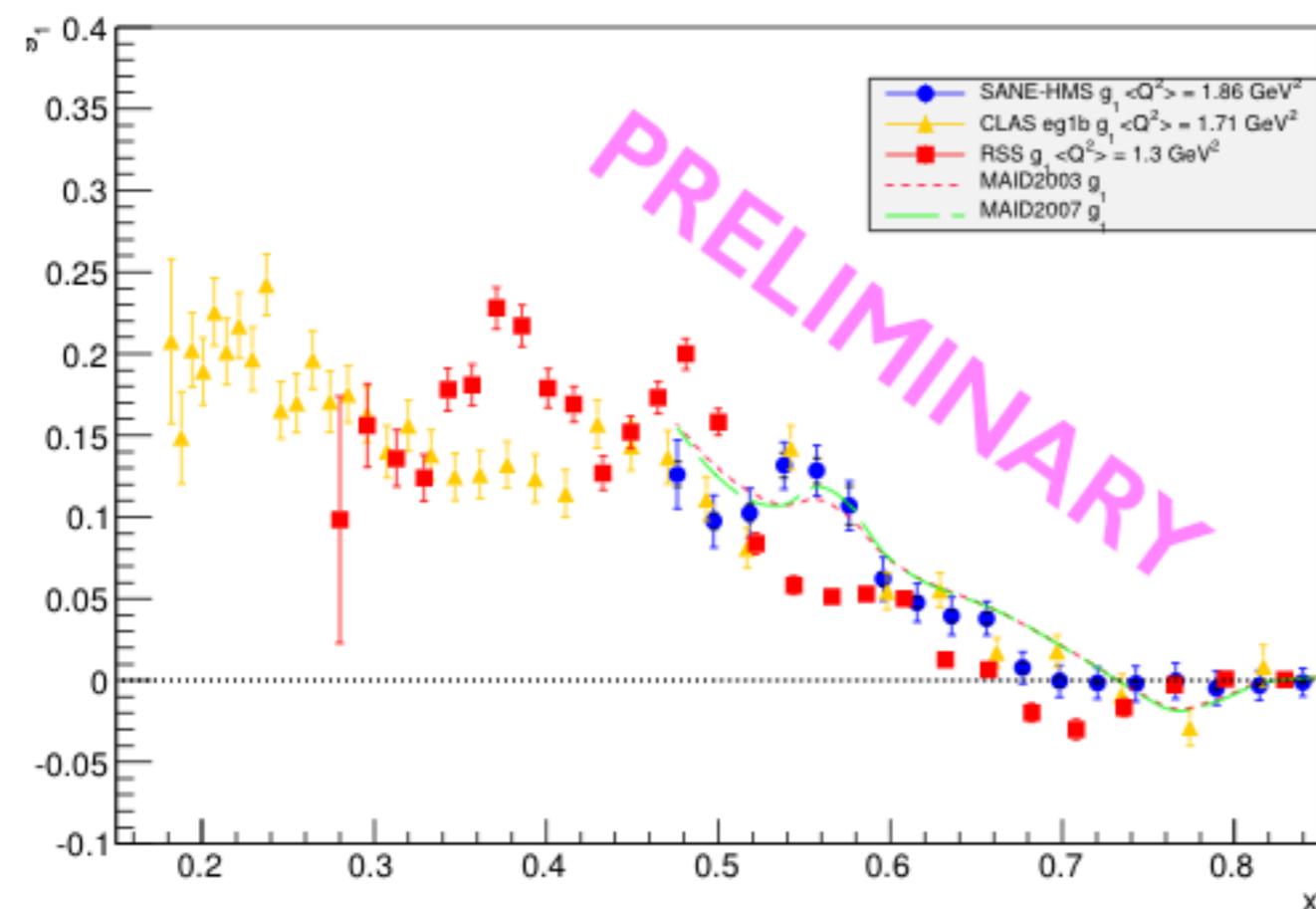
A_2



Proton g_1 and g_2

g_1

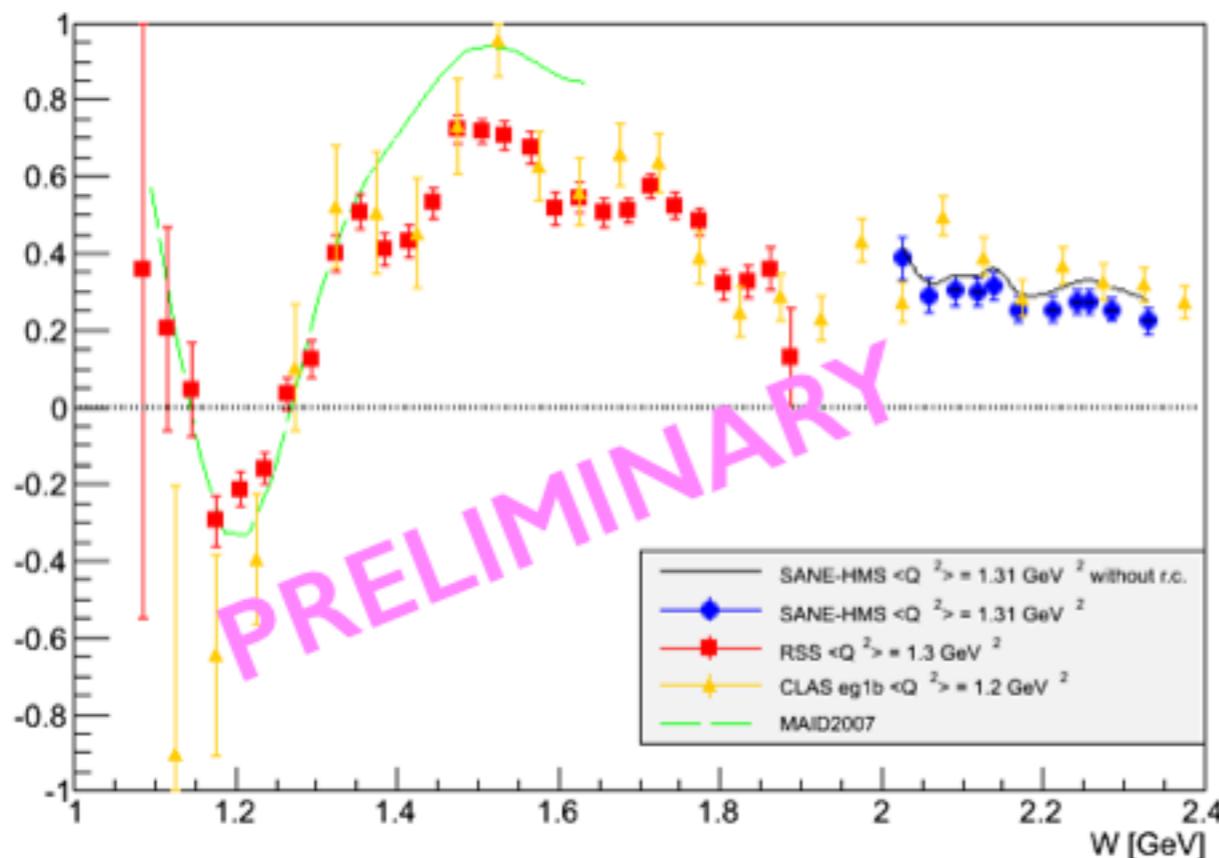
g_2



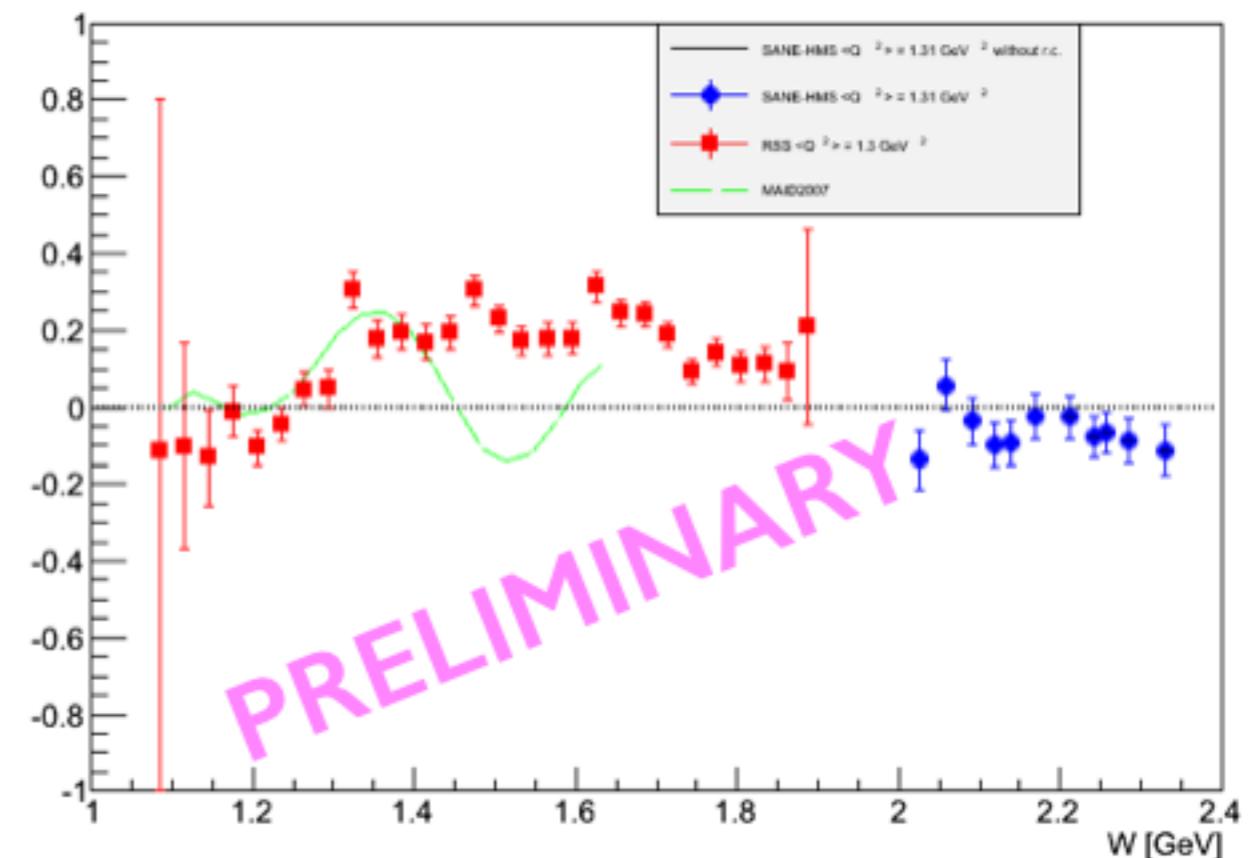
A_1 and A_2

(As an extension of RSS)

A_1

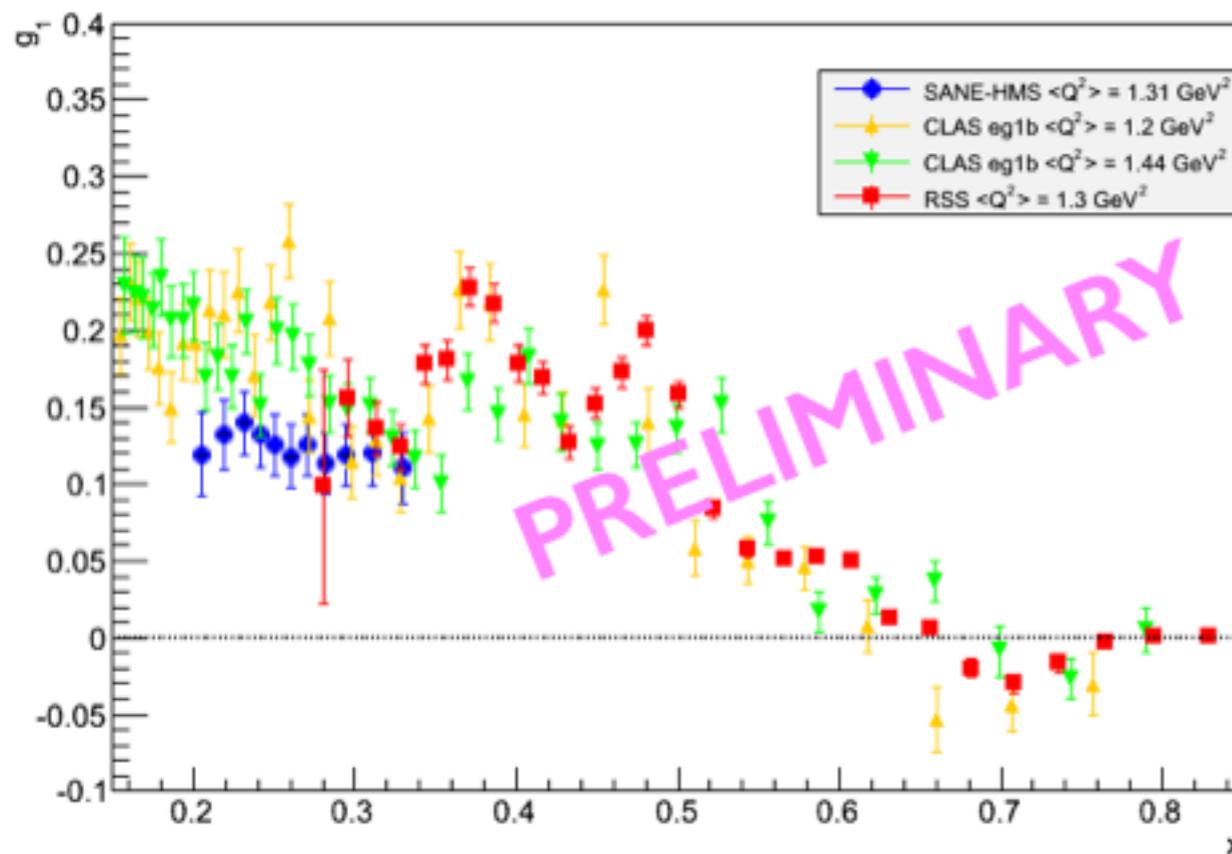


A_2

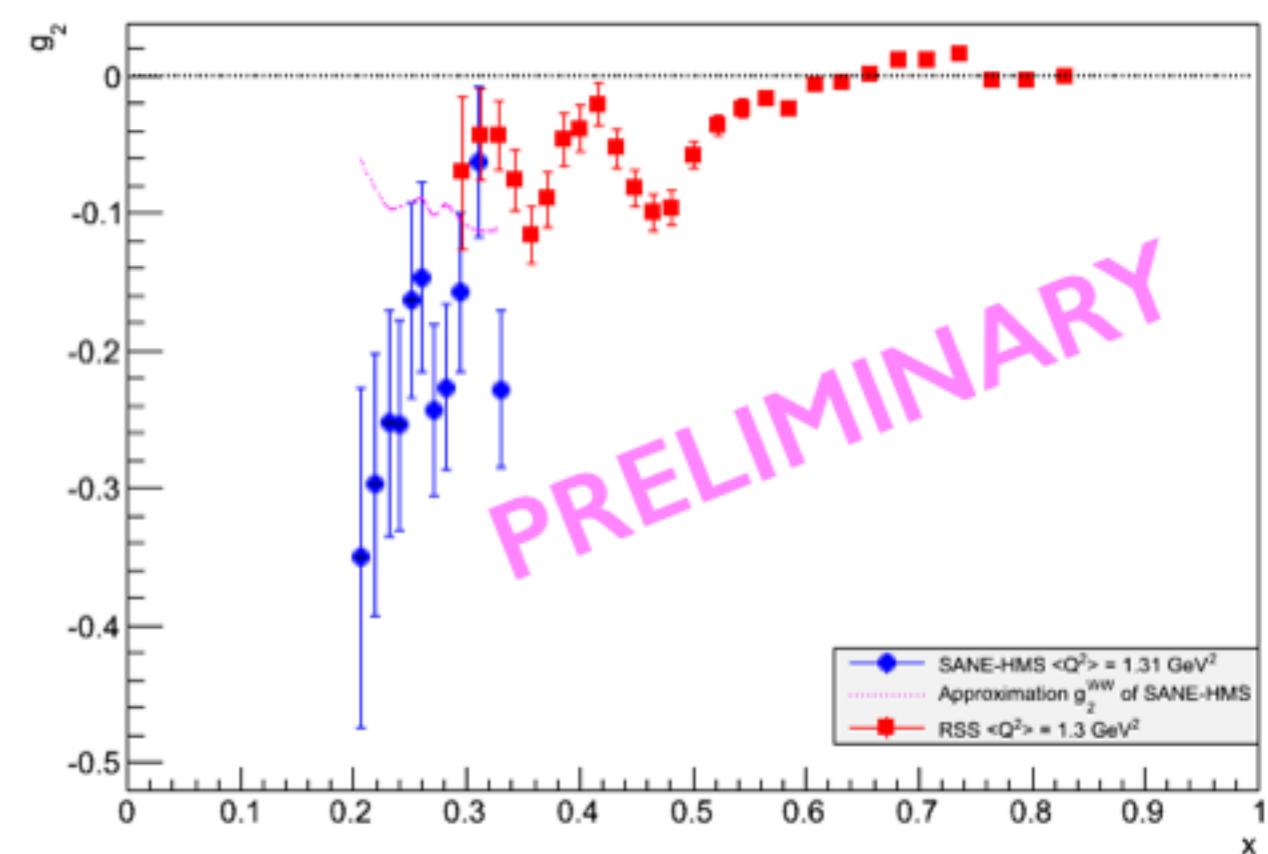


Proton g_1 and g_2 (As an extension of RSS)

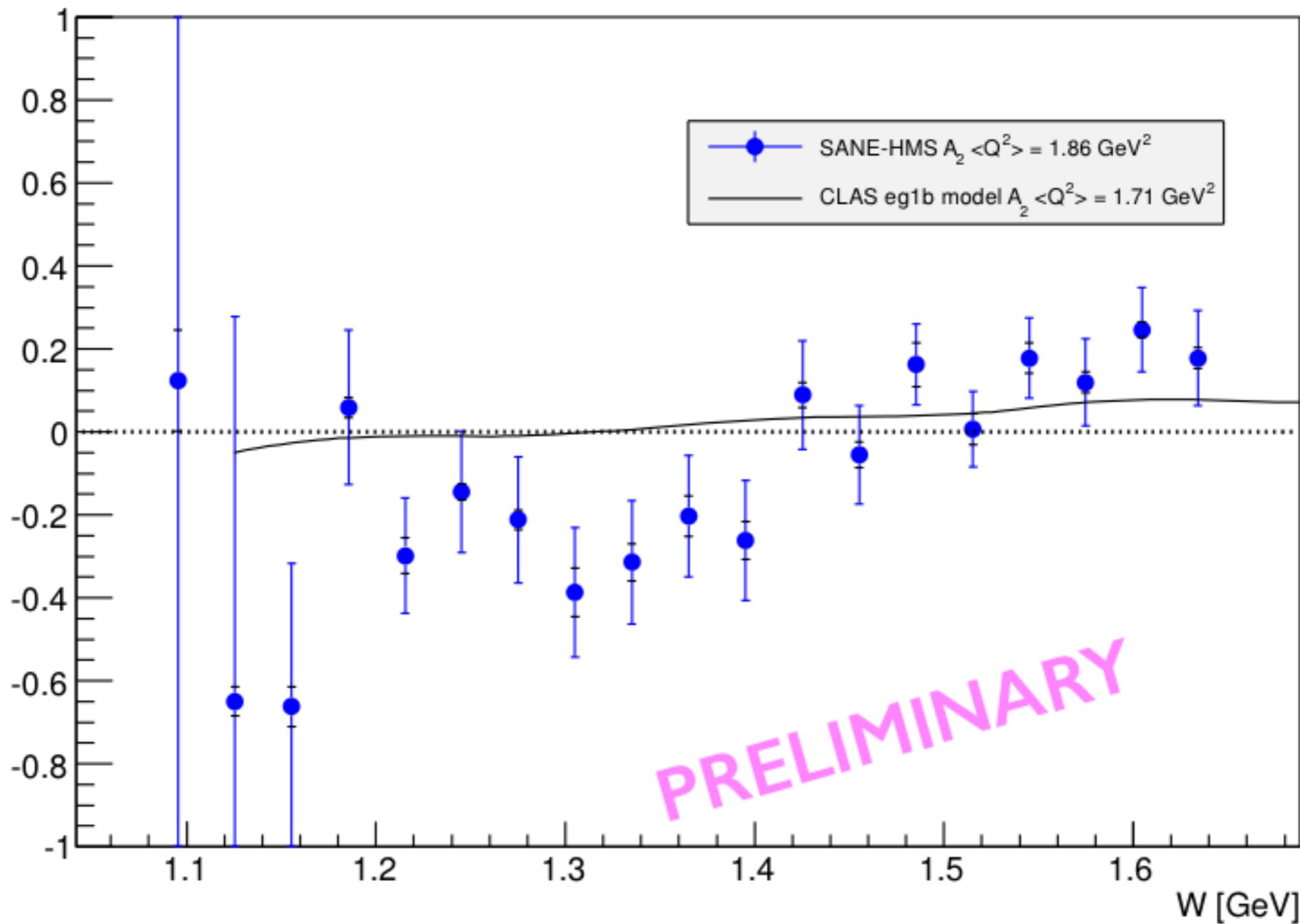
g_1



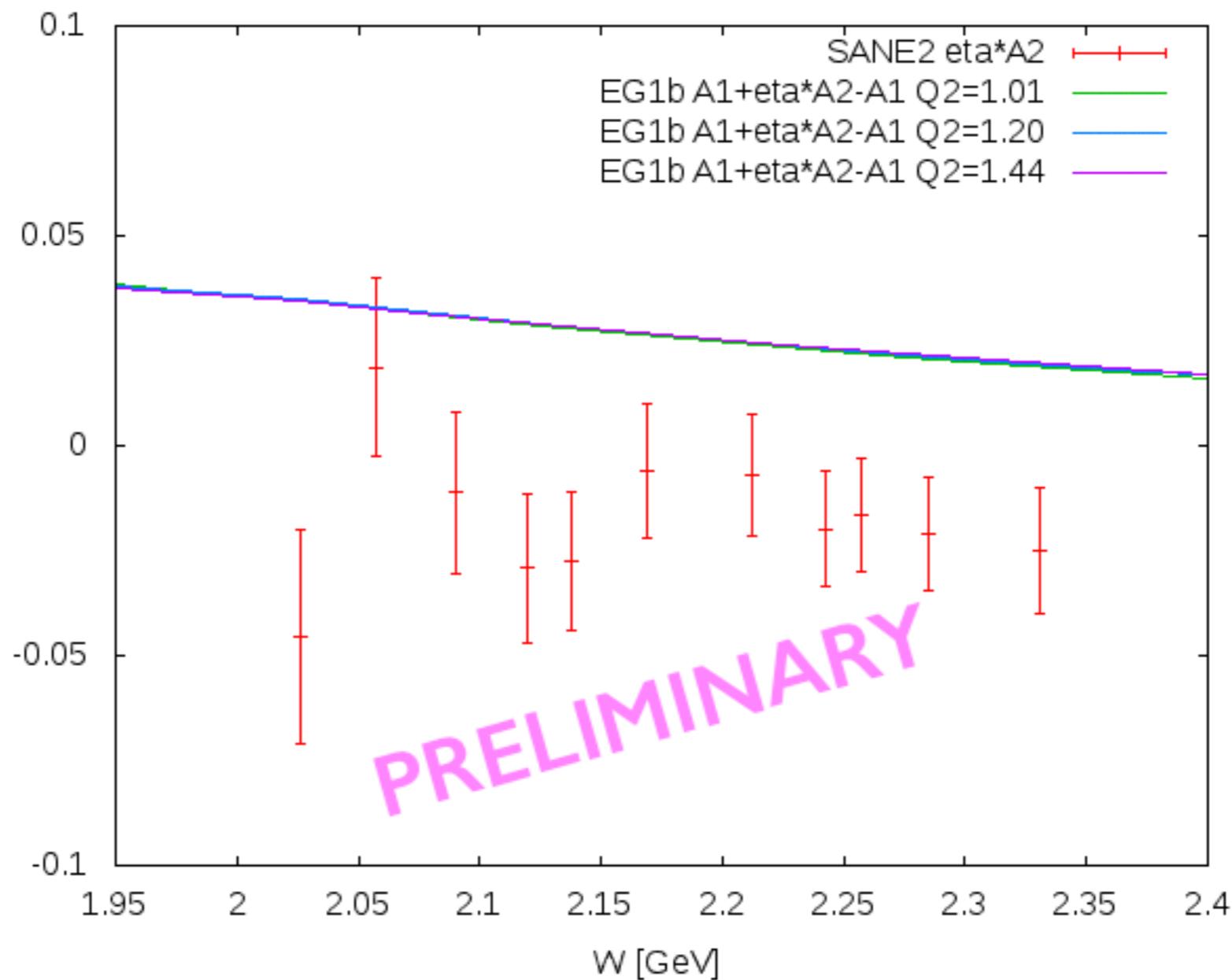
g_2



Proton A_2 and Model

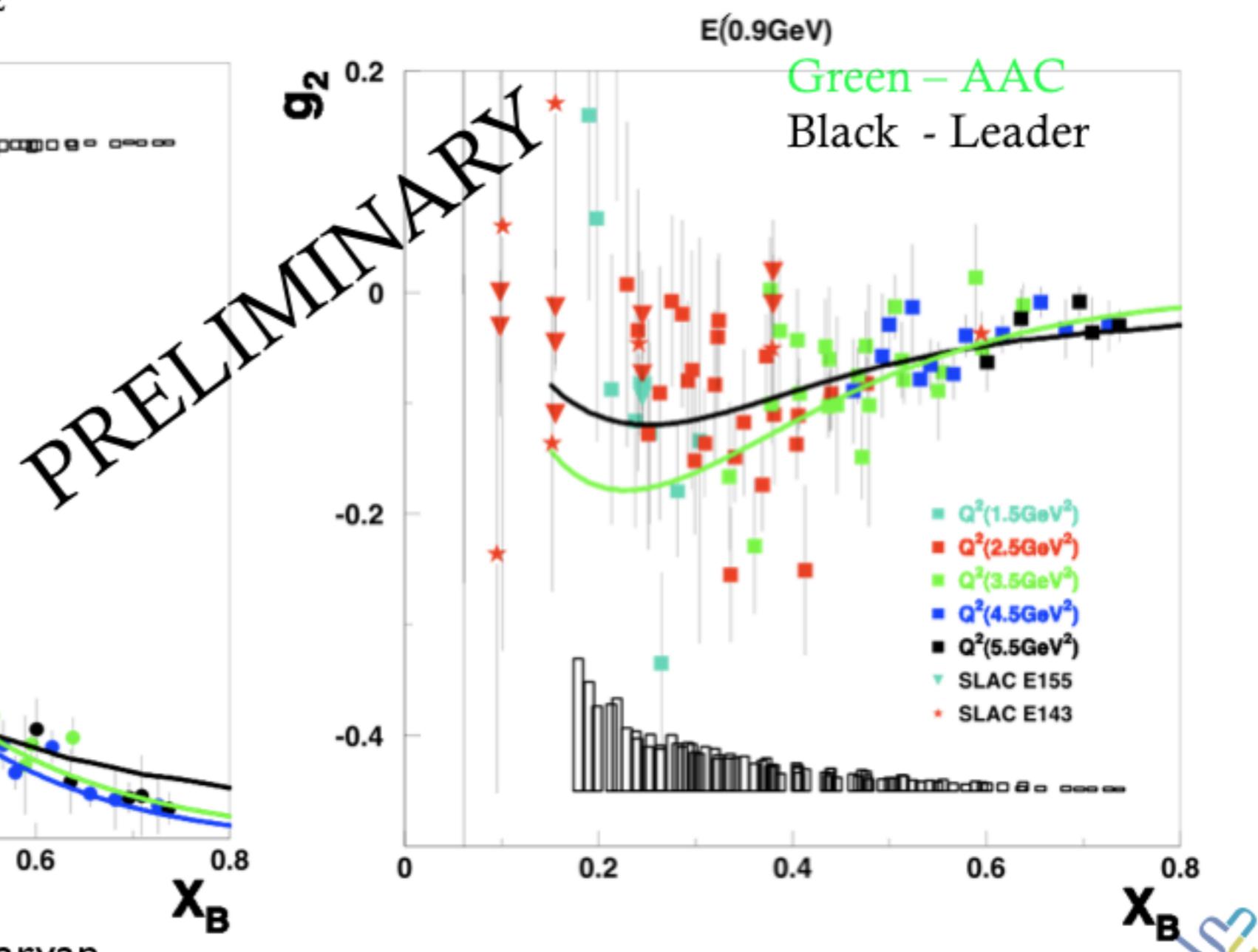
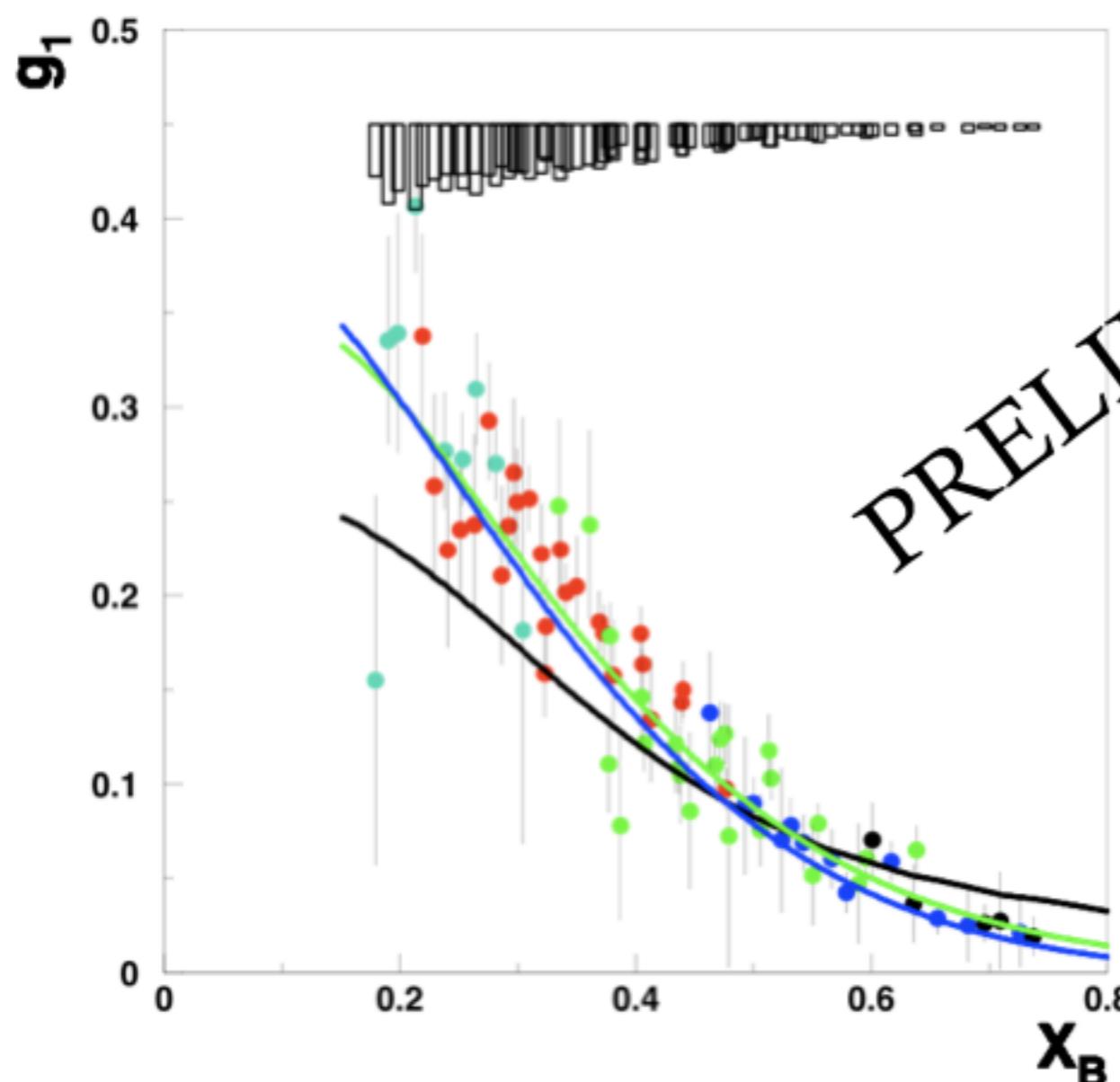


Proton A_2 and Model



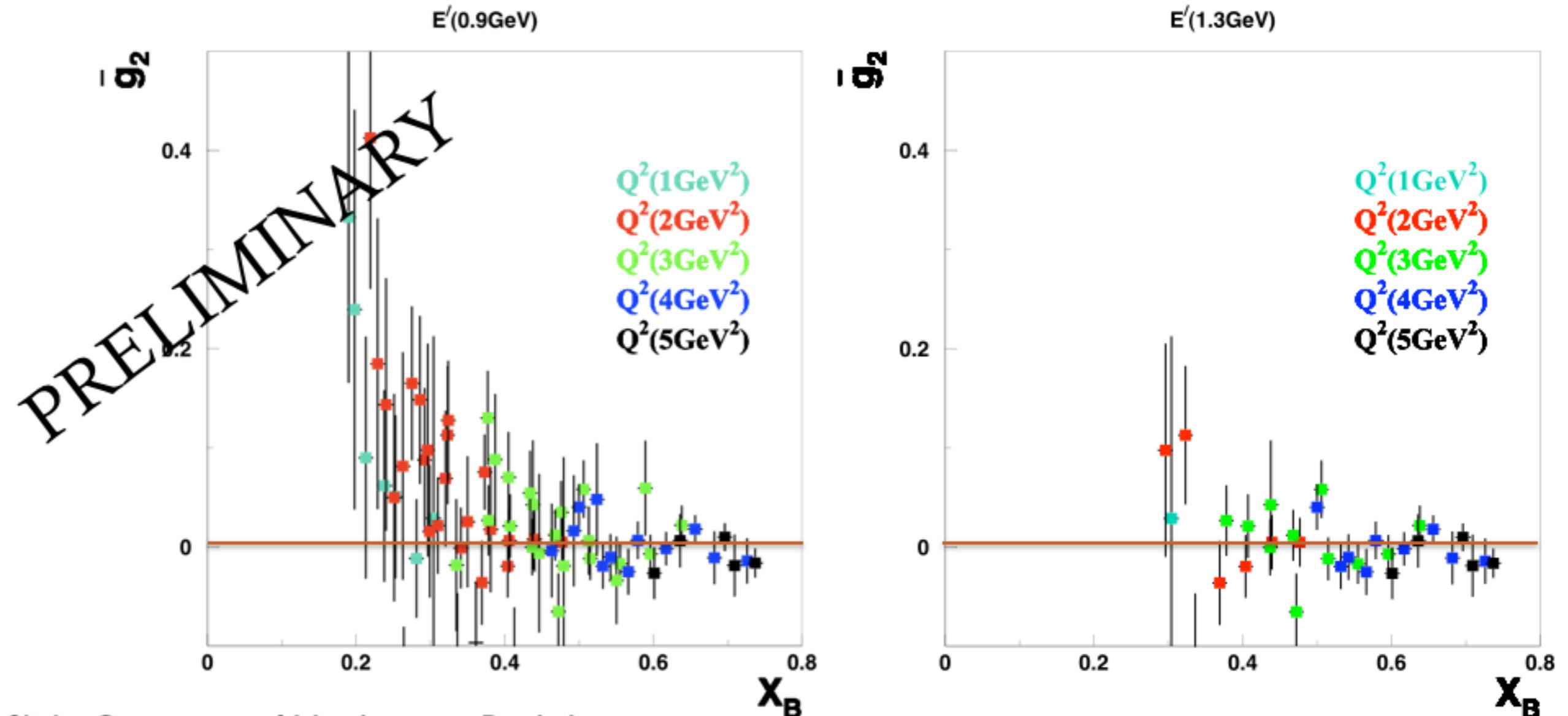
Sneak Preview of Asymmetries from BETA

- g_1 agrees with AAC
- g_2 is much larger than g_2^{WW}



Spin Structure Functions \bar{g}_2 from BETA

- \bar{g}_2 rises at low x_B
- Contribution to d_2 can be sizable



SANE Collaboration

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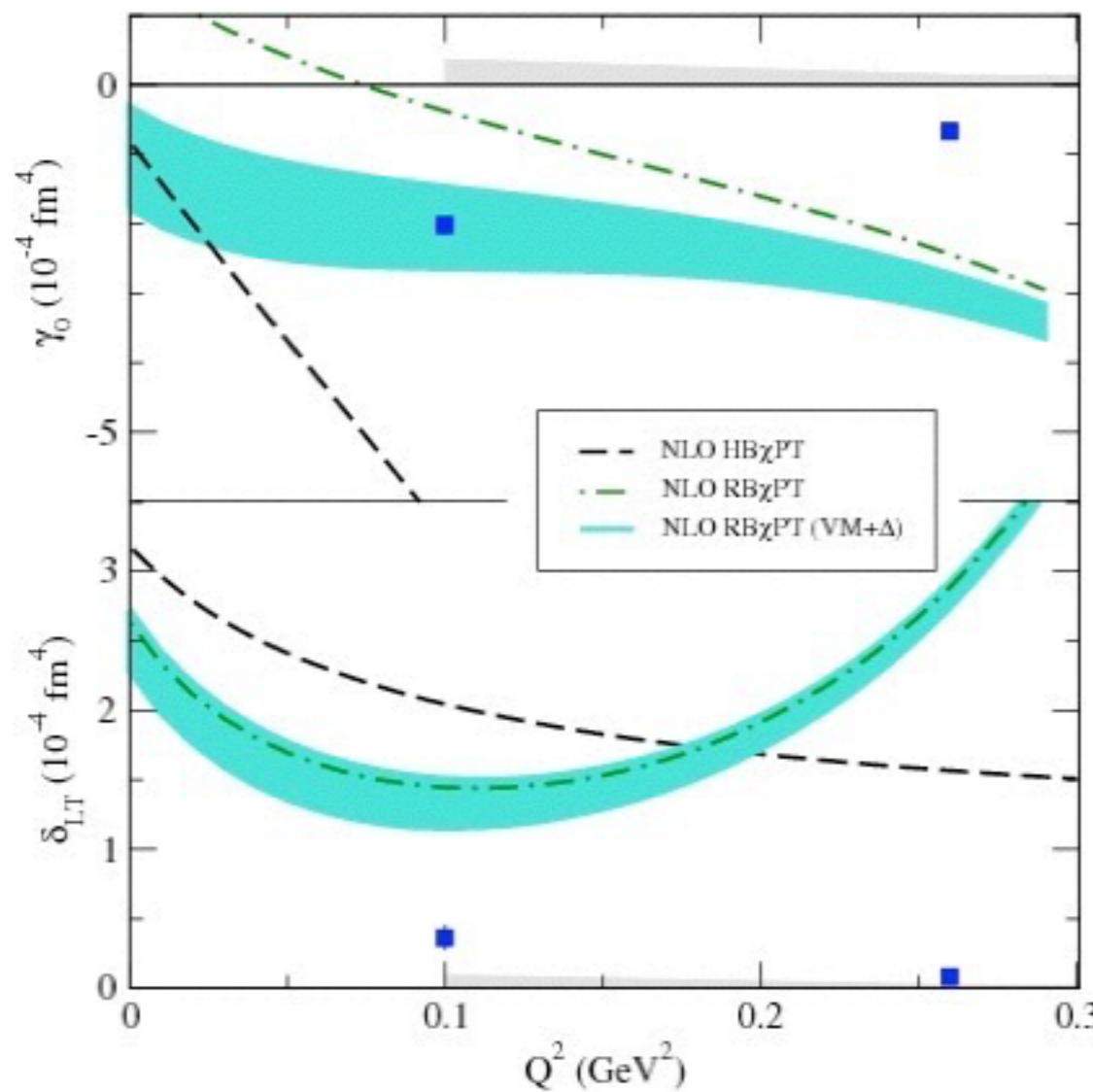
Ph.D. student, M.S. Student, Student



Spin Polarizabilities at Small Q^2

Neutron Spin Polarizabilities at Low Q^2

Neutron (E94010)



$$\gamma_0 = \frac{16\alpha M^2}{Q^6} \int_x^{x_0} x^2 \left[g_1 - \frac{4M^2}{Q^2} x^2 g_2 \right]$$

$$\delta_{LT} = \frac{16\alpha M^2}{Q^6} \int_x^{x_0} x^2 [g_1 + g_2]$$

Possible clue from **isospin combination** with similar data on the **proton**

E08-027 : Proton g_2 Structure Function

Fundamental spin observable has never been measured at low or moderate Q^2

A⁻ rating by PAC33

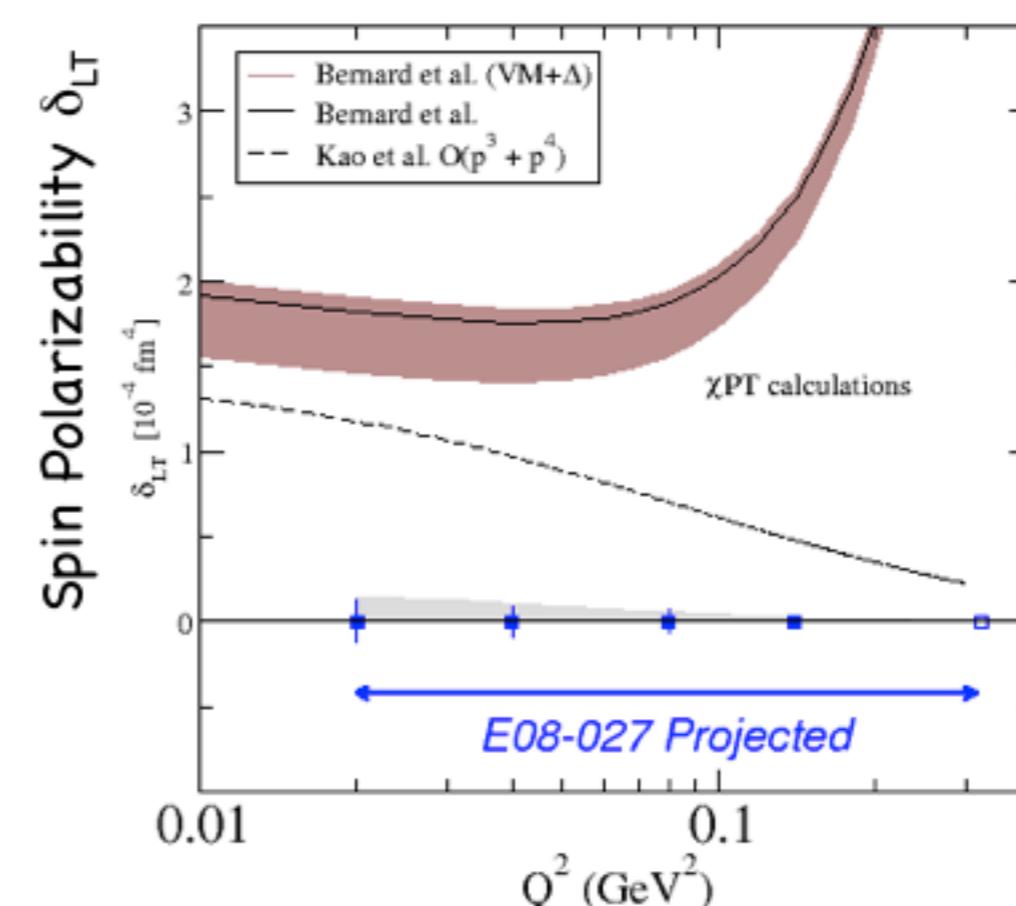
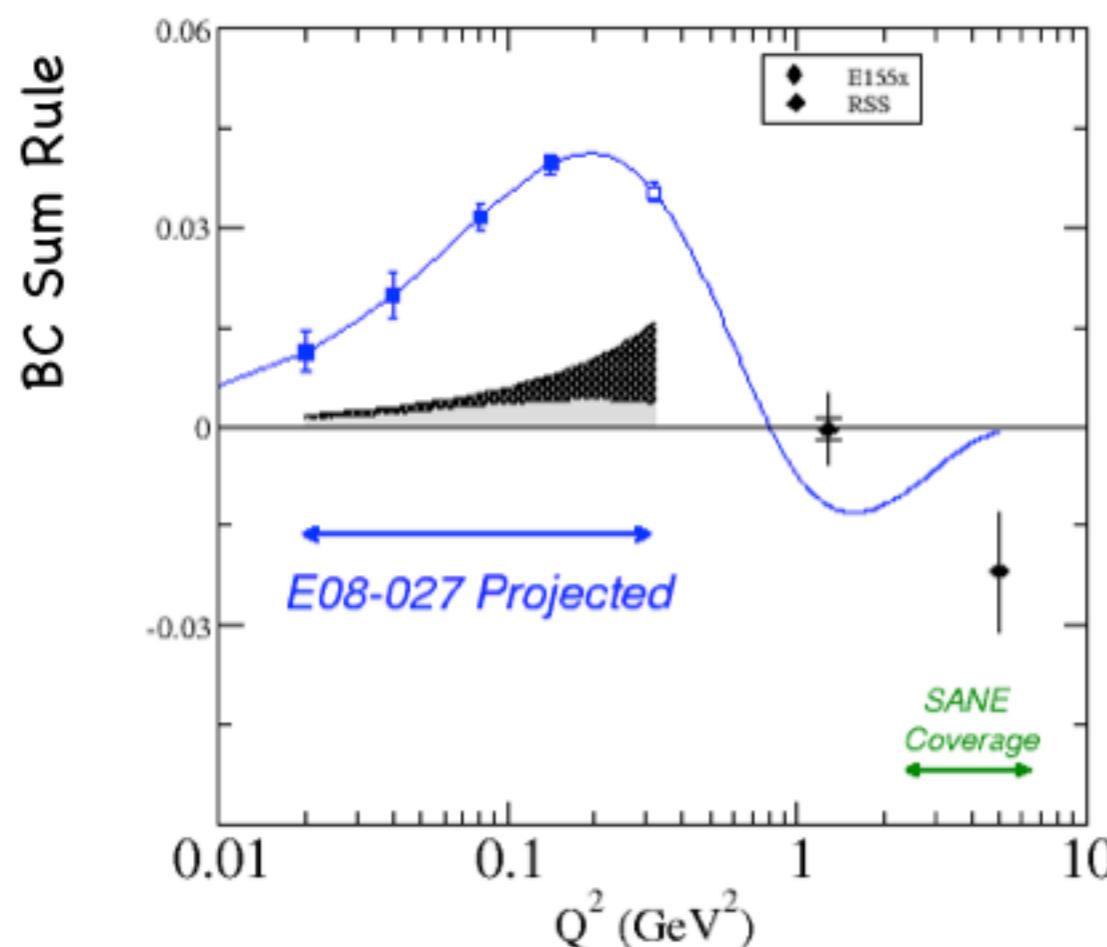
Spokesmen: Camsonne, Crabb, Chen, Slifer

BC Sum Rule : violation suggested for proton at large Q^2 , but found satisfied for the neutron & ${}^3\text{He}$.

Spin Polarizability : Major failure ($>8\sigma$) of χPT for neutron δ_{LT} . Need g_2 isospin separation to solve.

Hydrogen HyperFine Splitting : Lack of knowledge of g_2 at low Q^2 is one of the leading uncertainties.

Proton Charge Radius : one of the leading uncertainties in extraction of $\langle R_p \rangle$ from μ -H Lamb shift.



Experiment Overview

Polarized proton target

upstream chicane

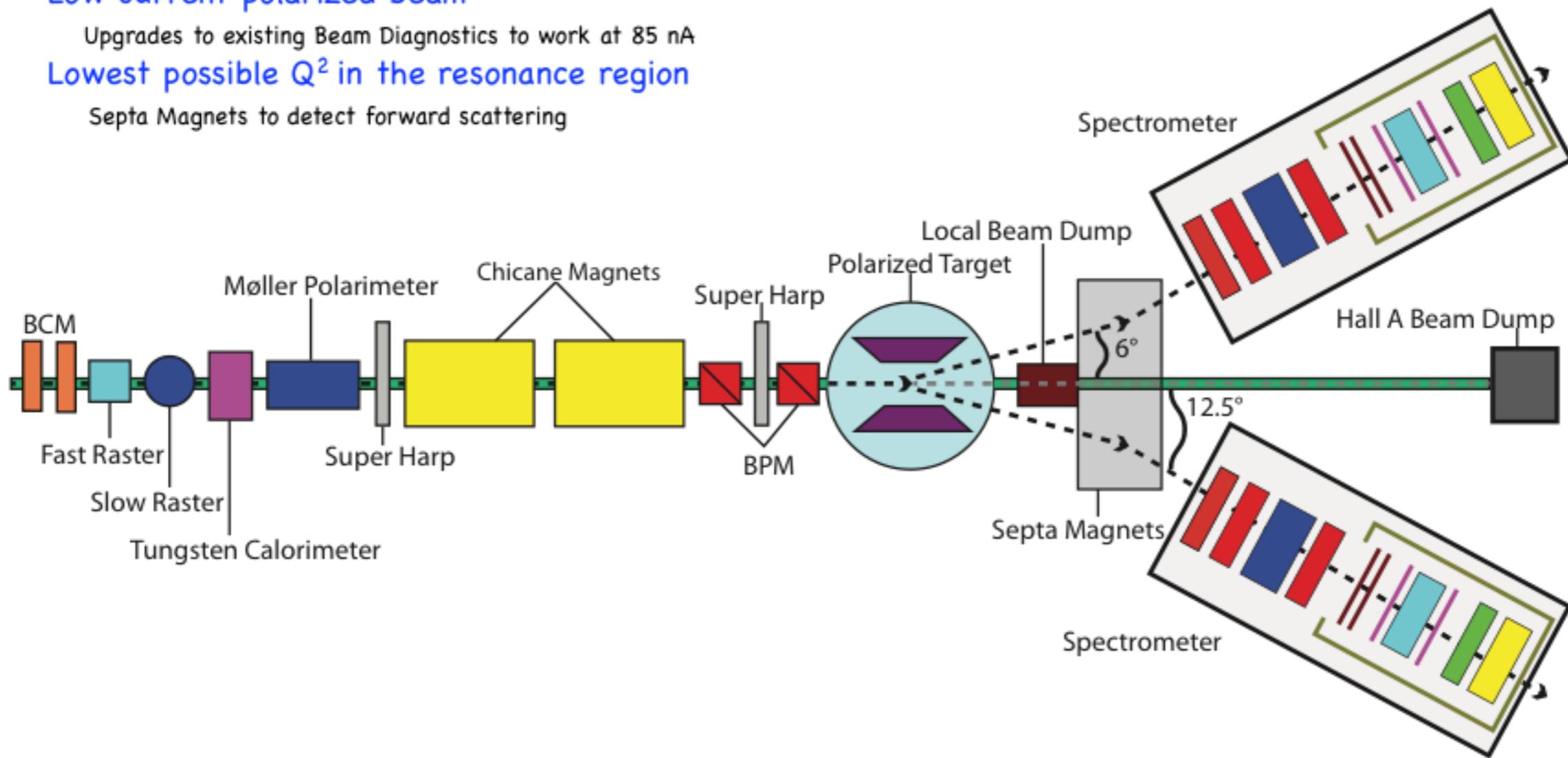
downstream local dump

Low current polarized beam

Upgrades to existing Beam Diagnostics to work at 85 nA

Lowest possible Q^2 in the resonance region

Septa Magnets to detect forward scattering



Installation

Polarized proton target

upstream chicane

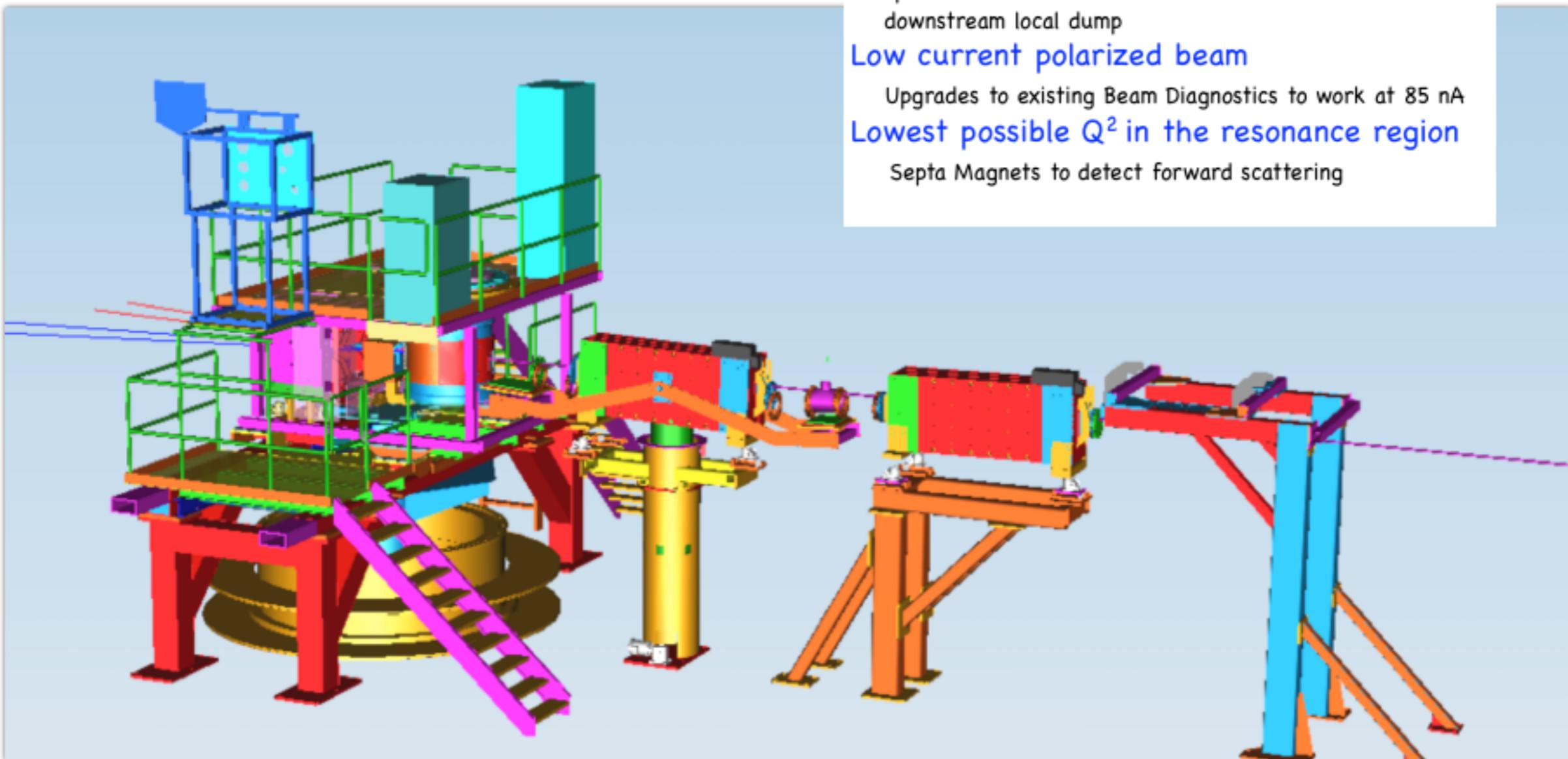
downstream local dump

Low current polarized beam

Upgrades to existing Beam Diagnostics to work at 85 nA

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Highlights and Preliminary Results

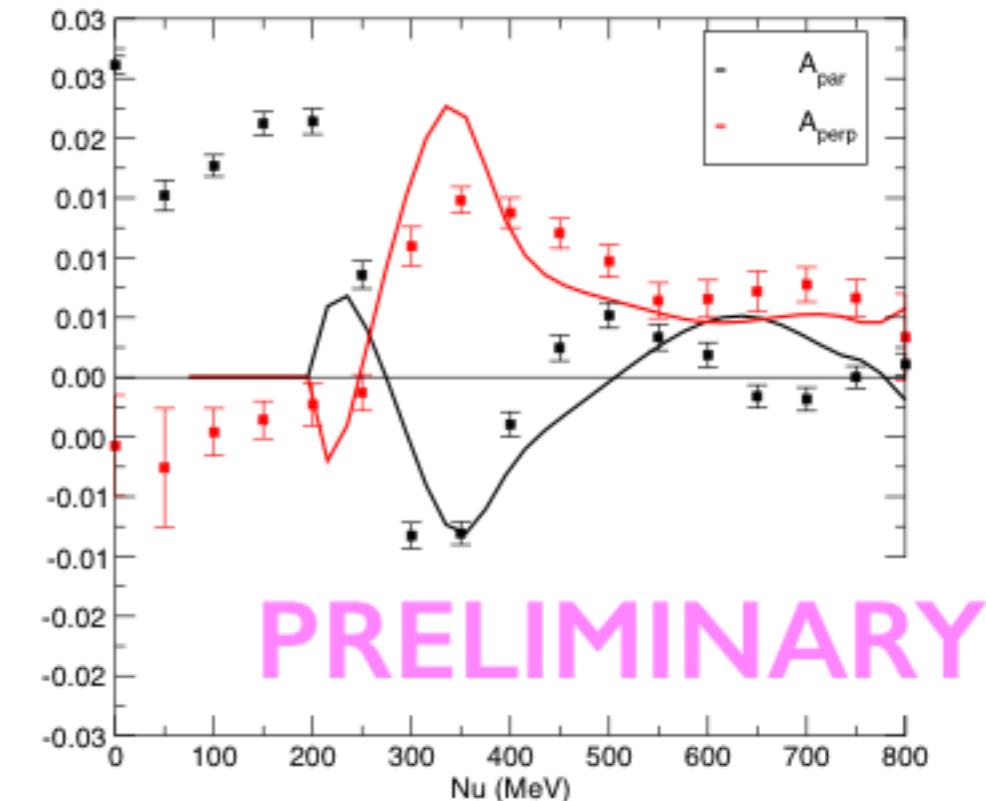
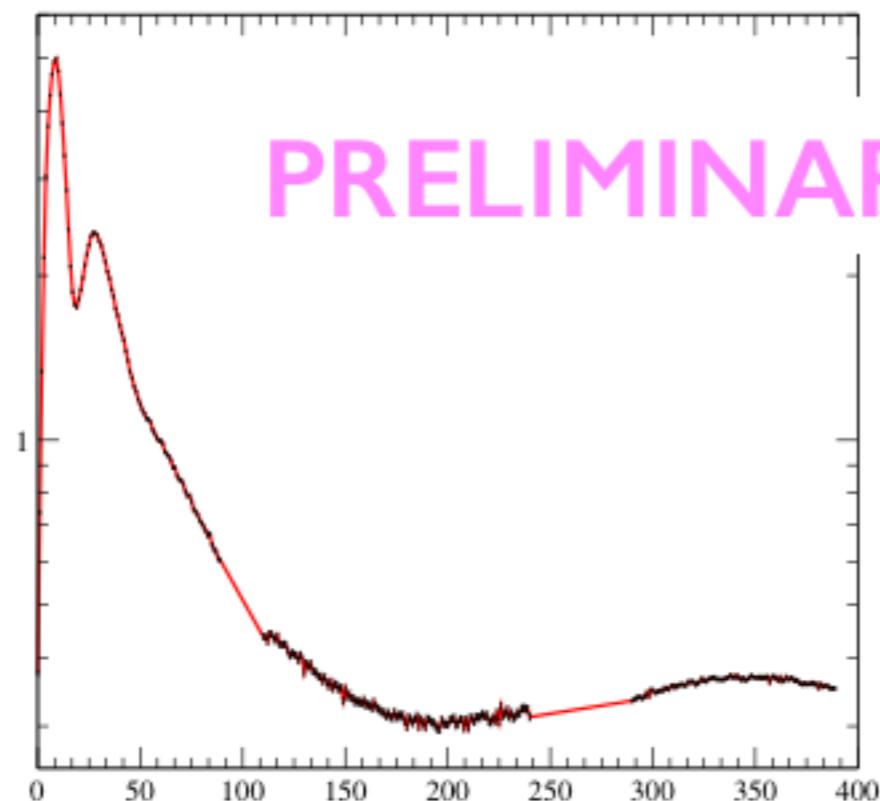
Will be the definitive measurement of g_{2p} for $0.02 < Q^2 < 0.2 \text{ GeV}^2$

Largest Installation in Hall A History

Entire new suite of beamline diagnostics for operation at 50nA

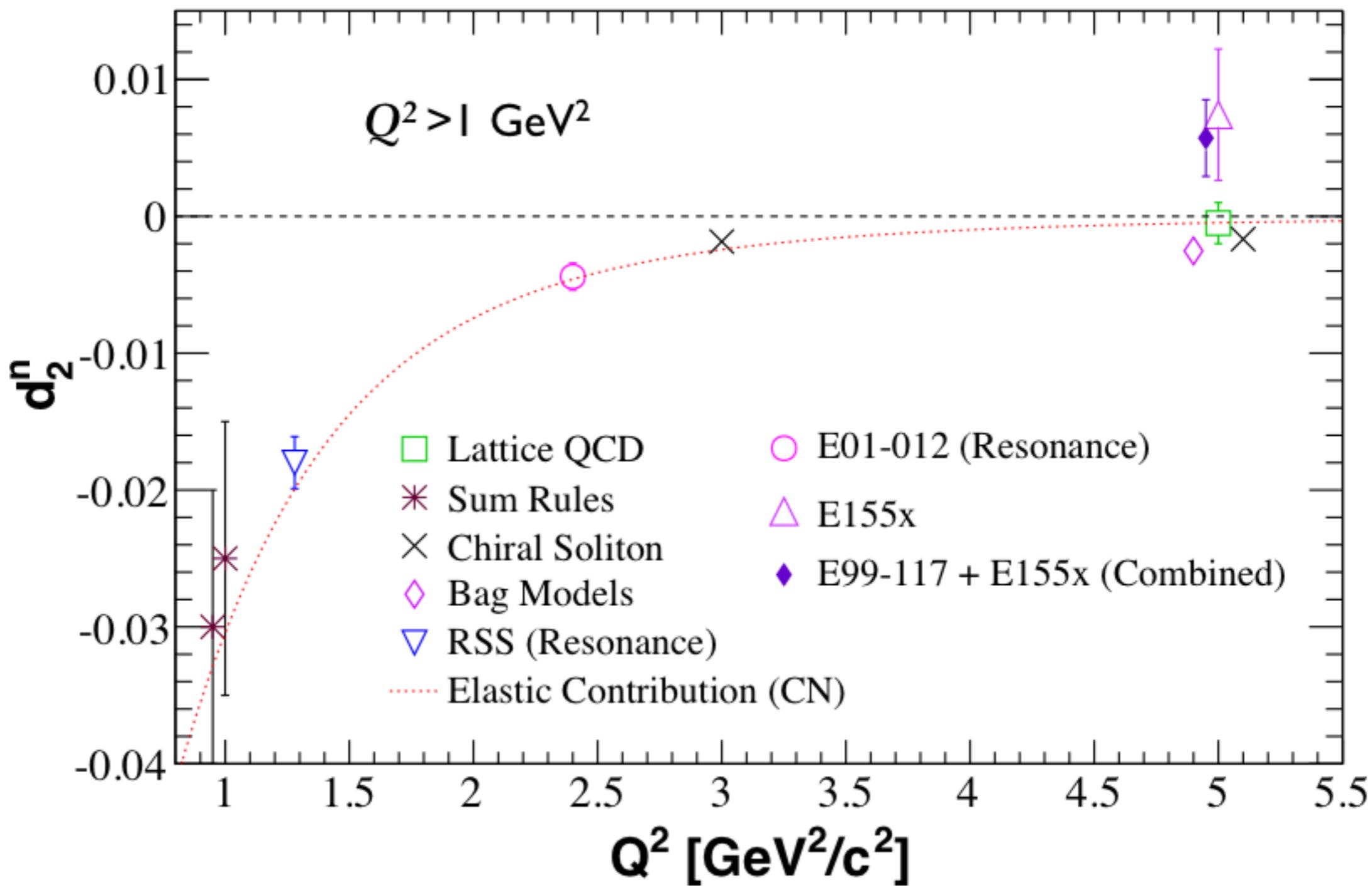
DAQ rate was Hall A record : 6.5 kHz/HRS with <25% deadtime

Polarized target performed very reliably



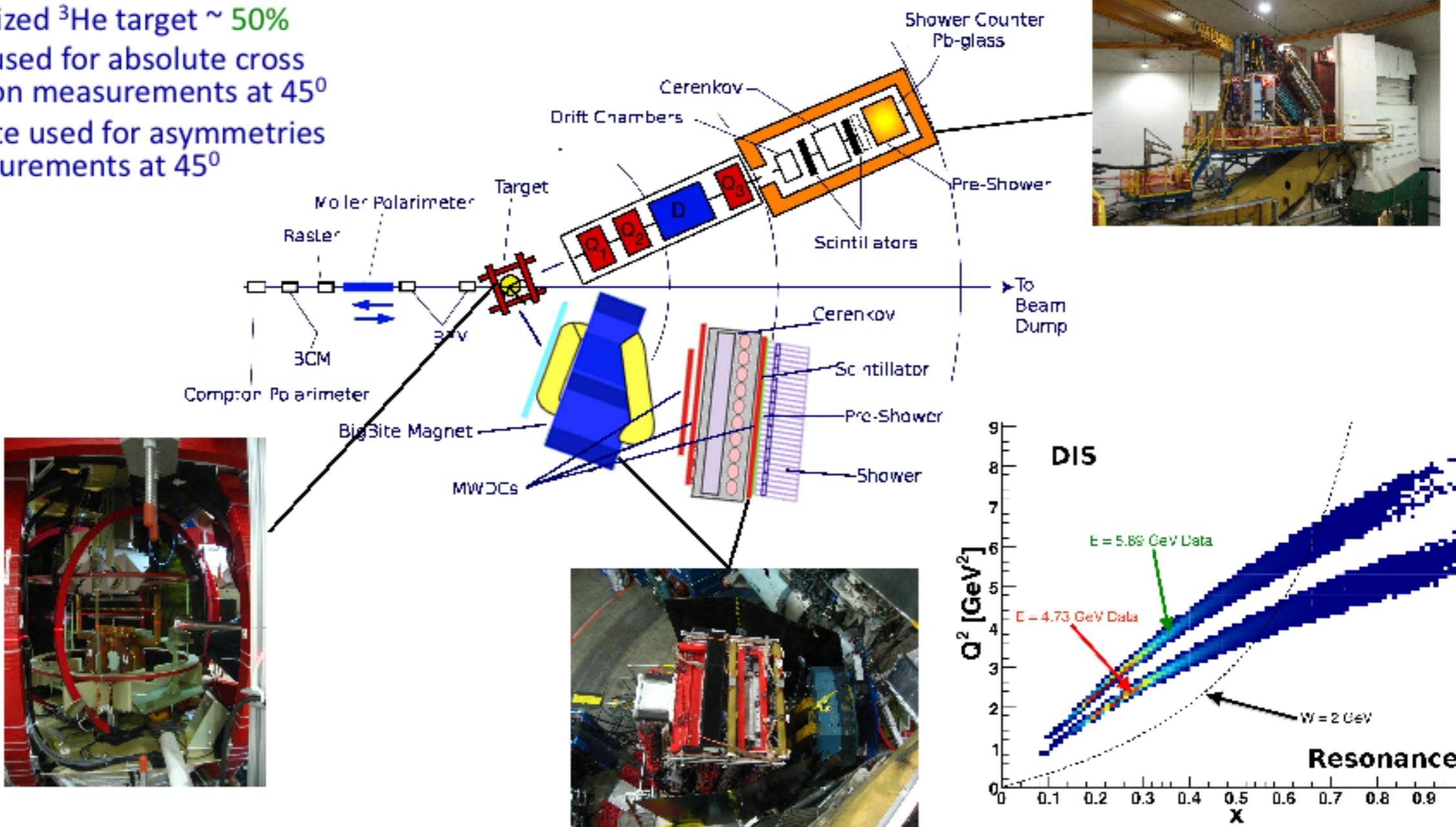
Precision Measurement of d_2^n

d_2^n World Summary

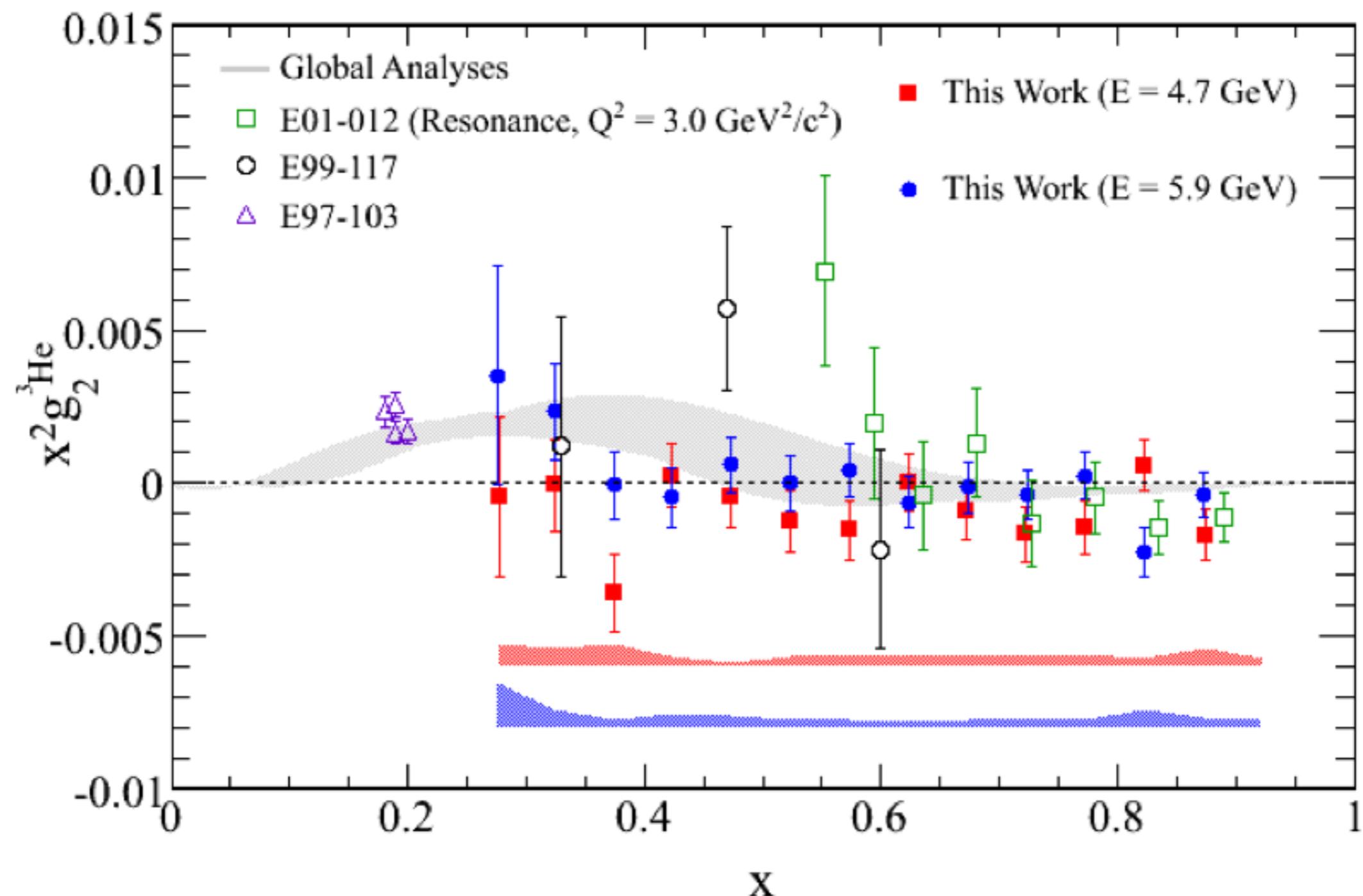


New Experiment at JLab

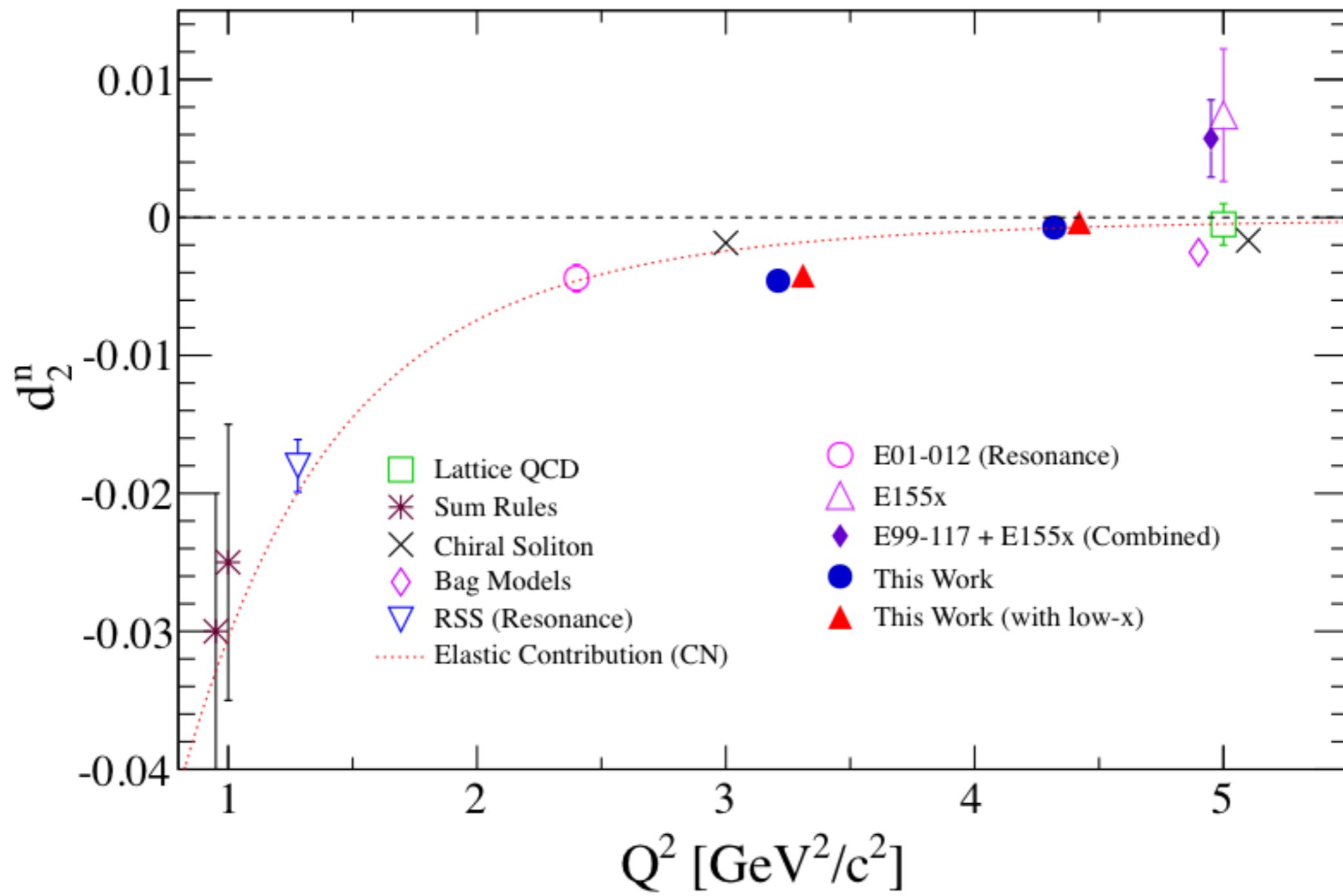
- Polarized electron beam: $E=4.74$, 5.89 GeV, polarization $\sim 71\%$
- Polarized ^3He target $\sim 50\%$
- HRS used for absolute cross section measurements at 45°
- Bigbite used for asymmetries measurements at 45°



$g_2(^3\text{He})$ Structure Function

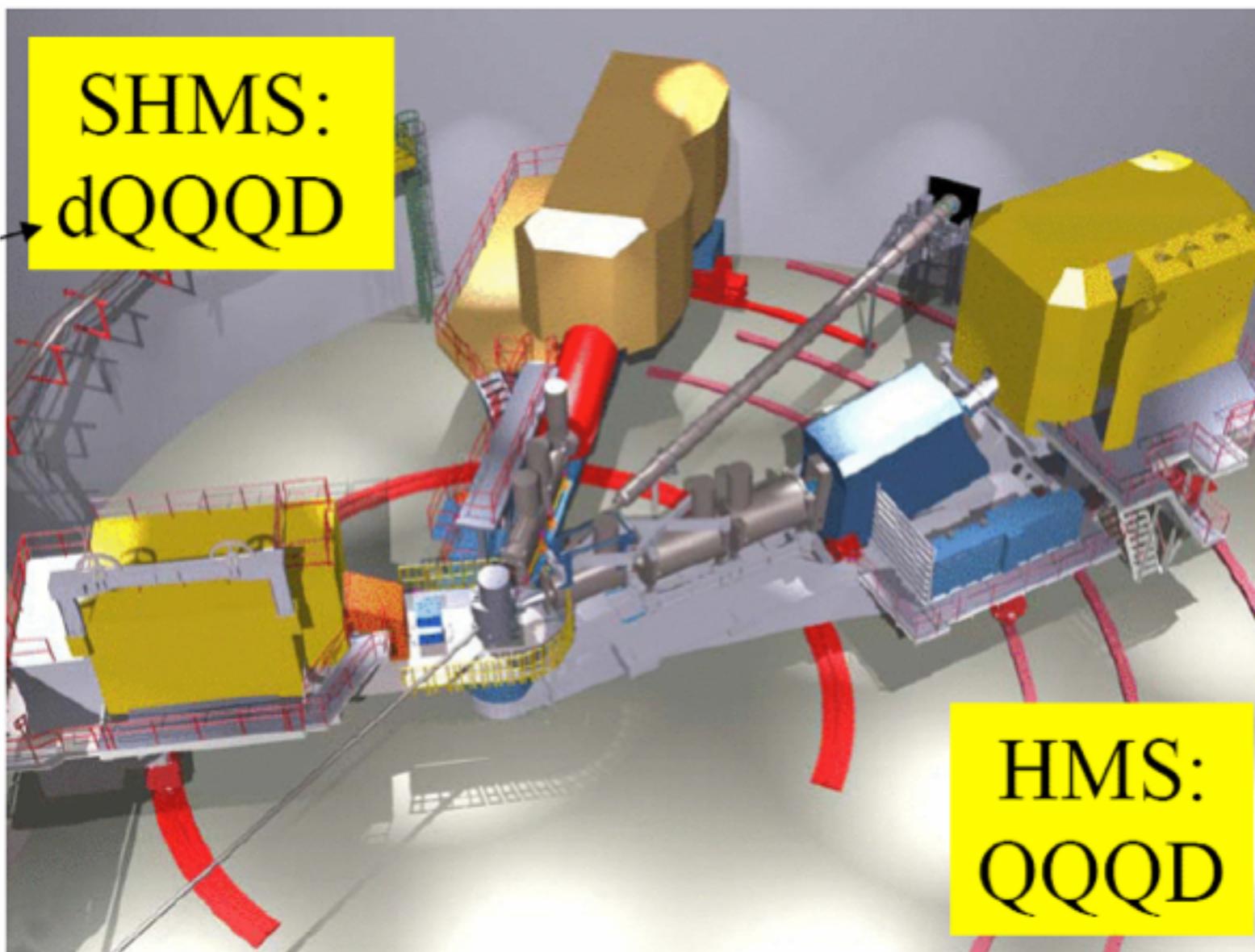


d_2^n Results



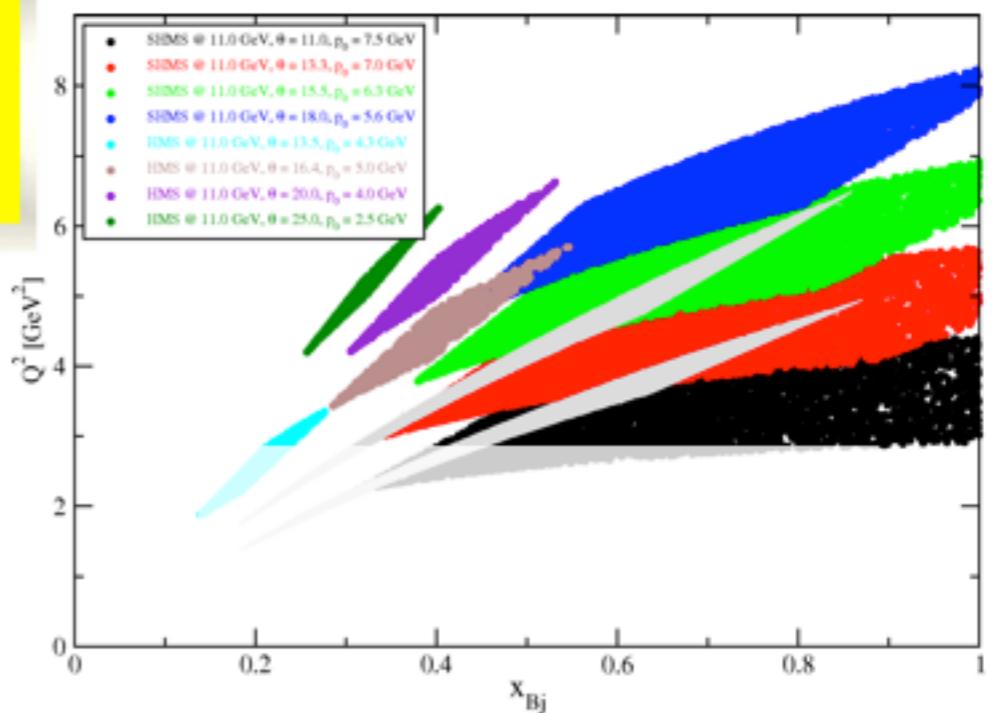
Spin Structure Functions at 12 GeV

E12-06-121: d_2^n, g_2^n

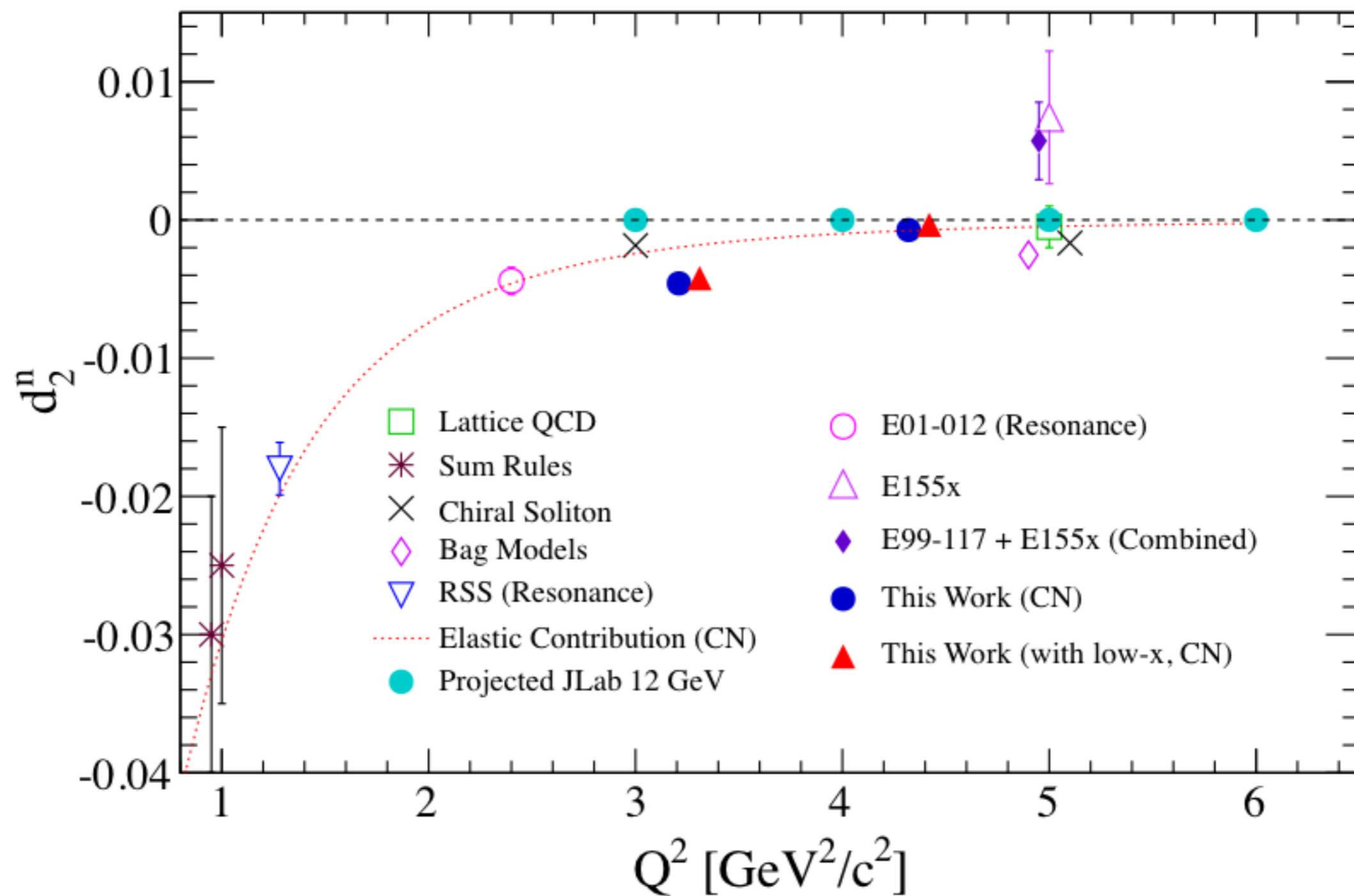


- SHMS collects data at $\Theta = 11^\circ, 13.3^\circ, 15.5^\circ$ and 18.0° for 125 hrs each
 - data from each setting divided into 4 bins
- HMS collects data at $\Theta = 13.5^\circ, 16.4^\circ, 20.0^\circ$ and 25.0° for 125 hrs each

- Hall C: SHMS + HMS
- One beam energy
 - 11 GeV
- Each arm measures a total cross section independent of the other arm.
- Experiment split into four pairs of 125 hour runs with spectrometer motion in between.



JLab 12 Projection of d_2^n



Summary (SANE)

- SANE measures double-spin asymmetries, A_{\parallel} and A_{\perp} of ep DIS
- Kinematic coverage of $2.5 < Q^2 < 6.5$, $0.3 < x < 0.8$,
- New non-magnetic detector **BETA** used for electron detection
- Expected to produce high precision data on d_2 and A_1
- Analysis finished for HMS data, publication is in preparation.

Summary

- Polarized DIS at various laboratories in the world
- Extensive measurements for g_1 over large Q^2 region
 - Both for the proton and the neutron
- Limited data for g_2 , especially for the proton
 - Precision measurements of g_2/d_2 : higher twists
 - Generalized spin polarizabilities
 - Test of xPT calculations: δ_{LT} puzzle
 - New data will be available for the proton