

# Role of Spin in $NN \rightarrow NN\pi$

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Spin 2014, Beijing

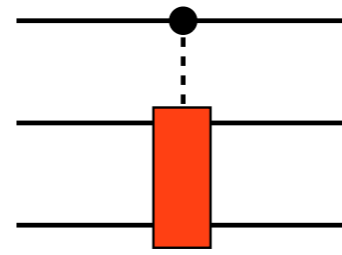
in collaboration with

E. Epelbaum, A. Filin, C. Hanhart, H. Krebs, A. Kudryavtsev, V. Lensky,  
U.-G. Meißner, F. Myhrer

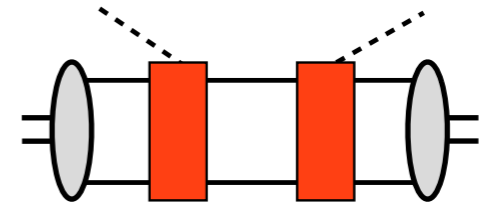
recent review article Int. Jour. Mod. Phys. (2014)

# $NN \rightarrow NN\pi$ . Introduction

- Direct Connection to other low-energy reactions



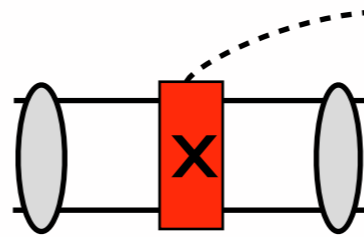
3N Forces



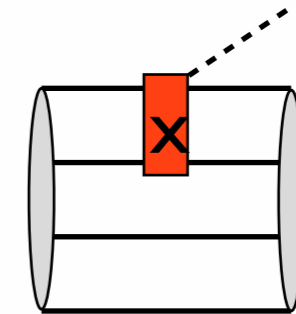
Pionic Deuterium  
 $\pi d \rightarrow NN \rightarrow \pi d$

+ ...

- Study of isospin violation in NN reactions



$pn \rightarrow d\pi^0$



$dd \rightarrow \alpha\pi^0$

Exp. Data:

TRIUMF (2003),  
IUCF (2004),  
COSY (2014)

- **Non-trivial production mechanism:** Channels with drastically different Cross Sections

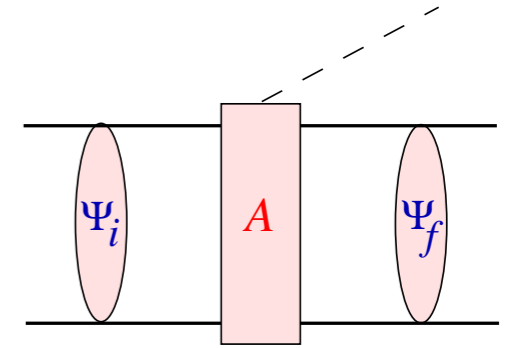
For example:  $pp \rightarrow d\pi^+$  and  $pp \rightarrow pp\pi^0$

- **Appropriate Framework - Chiral EFT:** successfully applied to  $\pi N$  and  $NN$  interactions - main ingredients of  $NN \rightarrow NN\pi$

Weinberg, Gasser, Meißner, Epelbaum, ...

$NN \rightarrow NN\pi$  within hybrid chiral EFT.

Weinberg (1992)



► Chiral expansion of the production operator  $A$  at low energies

– New scale in  $NN \rightarrow NN\pi$ :  $p \simeq \sqrt{m_\pi m_N}$  — initial NN momentum in cms

–  $\chi \sim \frac{p}{\Lambda_\chi} \sim \sqrt{\frac{m_\pi}{m_N}}$  — expansion parameter in  $NN \rightarrow NN\pi$

Cohen et al. (1996); Hanhart et al. (2000)

– Explicit  $\Delta(1232)$ -resonance:  $m_\Delta - m_N \sim p$

– long-range operators (OPE,  $\pi$ -loops)  $\rightarrow$  explicitly

– short-range mechanisms  $\rightarrow$  local contact operators(LECs)

Investigate convergence by explicit treatment of higher-order terms

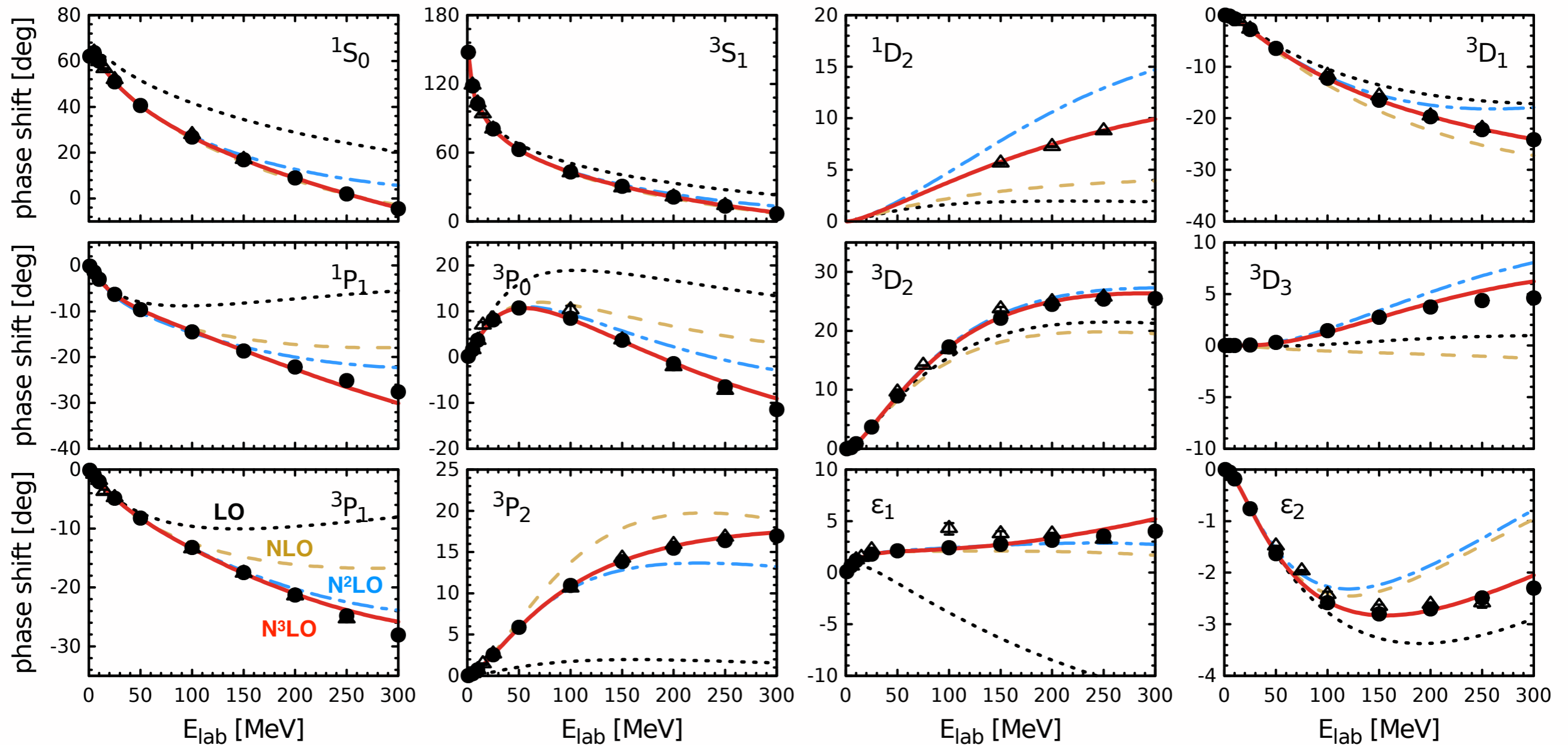
► Convolution with the NN wave functions: CD-Bonn, CCF, AV18, ...

and Chiral EFT

# NN phase shifts in Chiral EFT

Convergence order by order: LO, NLO, N<sup>2</sup>LO, N<sup>3</sup>LO

Epelbaum et al. (2014)

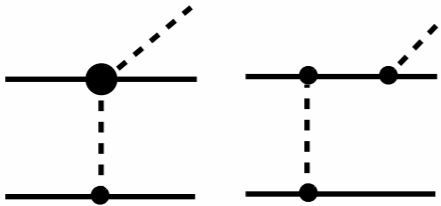
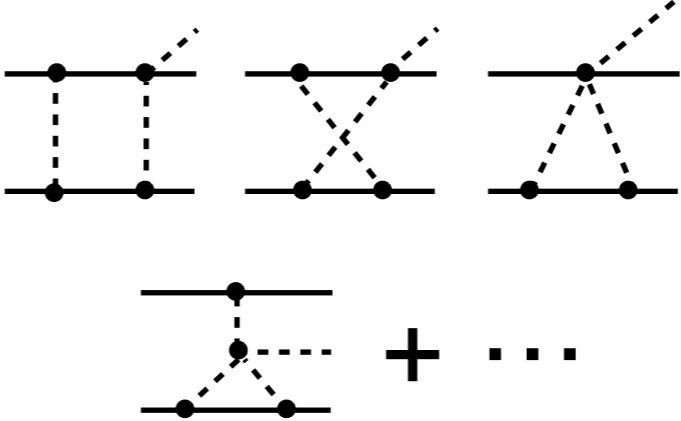
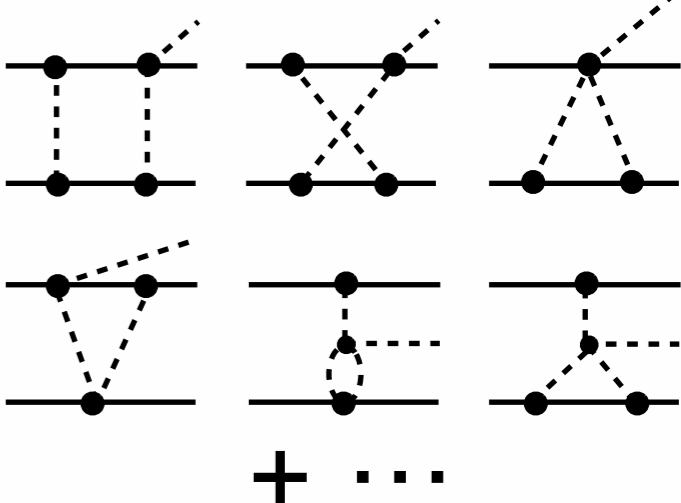


**N<sup>3</sup>LO:** Almost perfect description of Phase Shifts even above pion threshold:  $E_{\text{lab}} \approx 279$  MeV

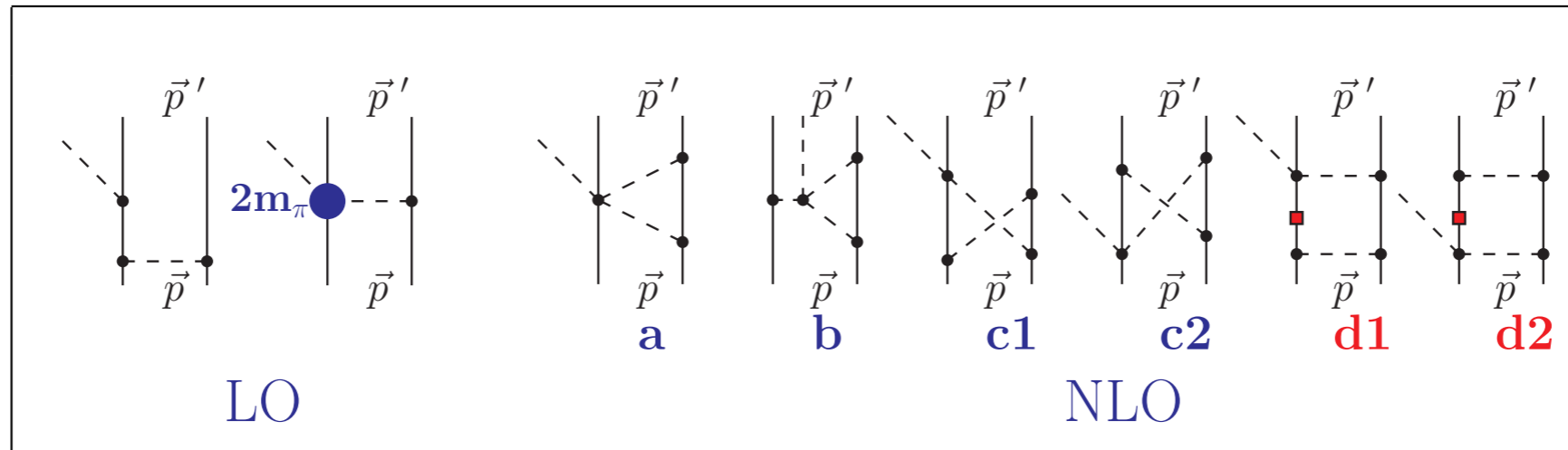
**Calculation of  $NN \rightarrow NN\pi$  with Chiral wave functions becomes possible**

# From S-wave pion production to isospin violation in NN reactions

# s-wave pion production operators

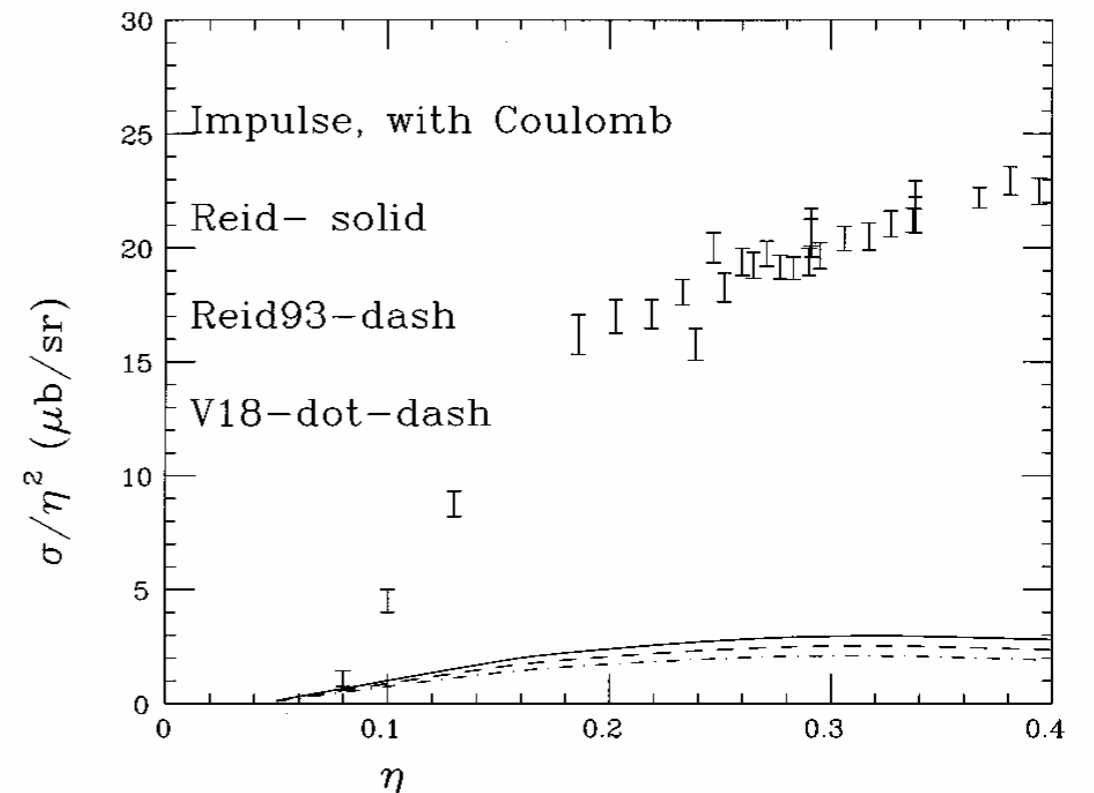
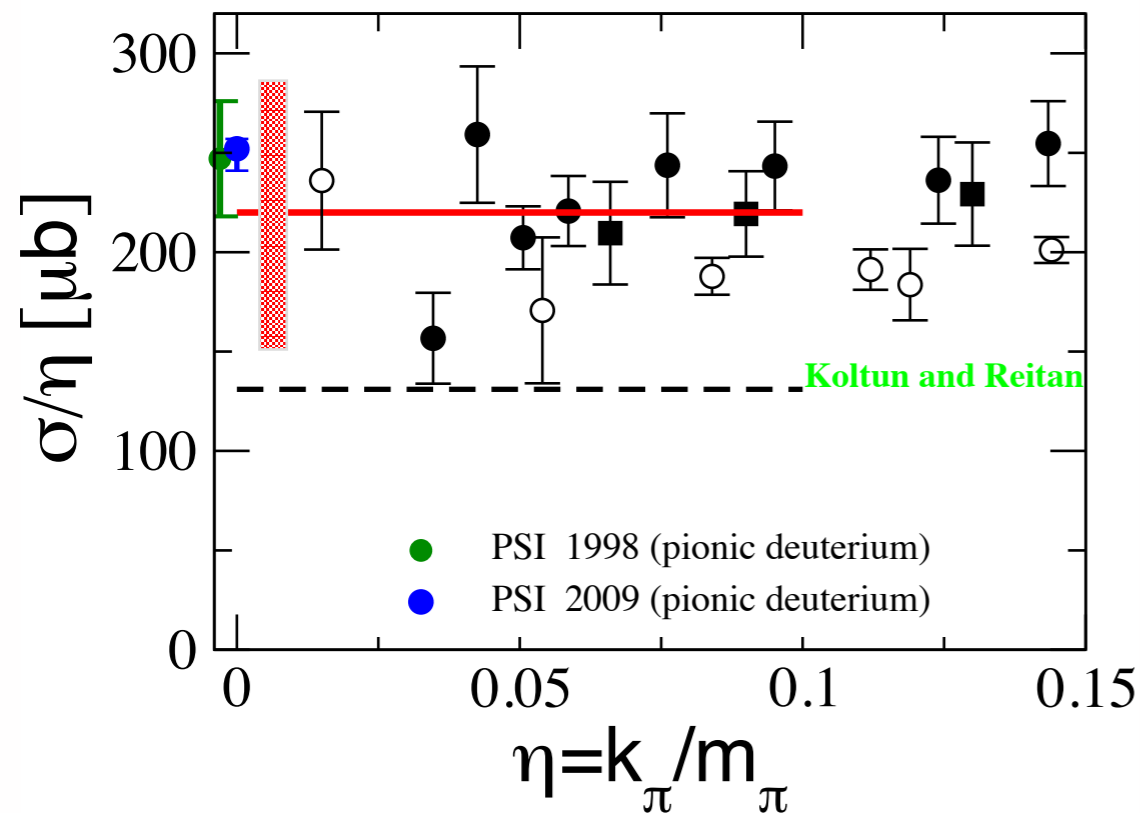
$\chi_{\text{MCS}} \sim \sqrt{\frac{m_\pi}{m_N}}$	LO	NLO	NNLO
			
$pp \rightarrow d\pi^+$	<p><b>big</b> contribution Koltun et al. (1966)</p>	<p><b>0</b> Lensky et al. (2006)</p>	<p><b>small,</b> correction to LO</p>
$pp \rightarrow pp\pi^0$	<p>almost <b>negligible</b> Cohen et al. (1996), Park et al. (1996)</p>	<p><b>0</b> Hanhart and Kaiser (2005)</p>	<p><b>small,</b> but main contribution <b>(!)</b></p>

# S-wave pion production: Theory vs. Experiment



Theory band  from Lensky et al. (2006)

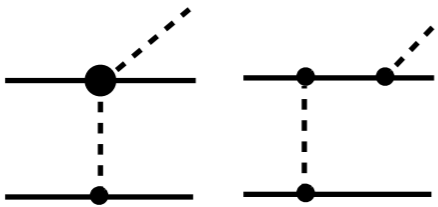
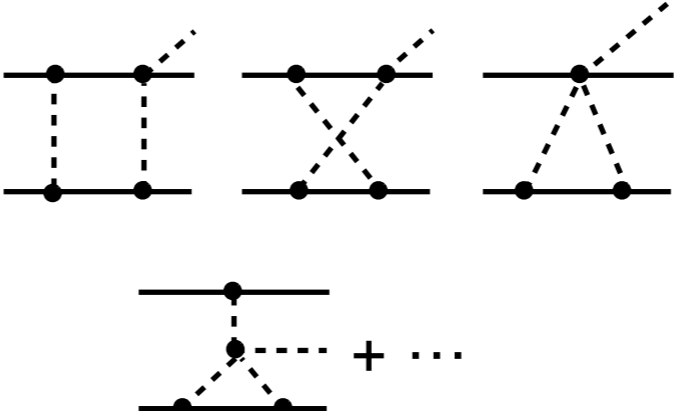
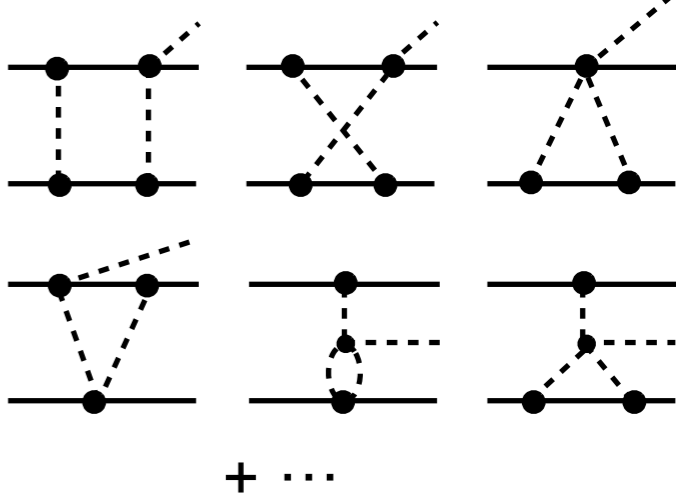
Picture and Theory curves: from Cohen et al. (1996)  
 Similar conclusions: Park et al. (1996)



Quantitative description

Underestimation of data by an order of magnitude

# s-wave pion production operators

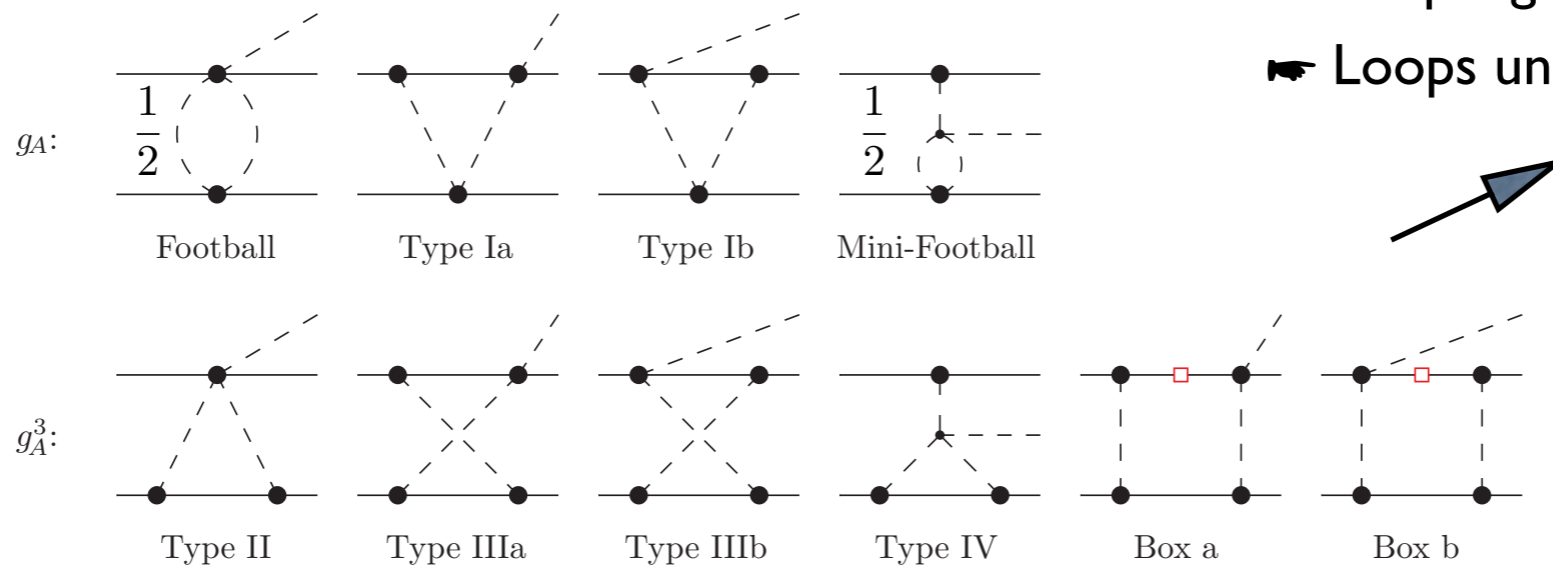
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For  $pp \rightarrow pp\pi^0$  LO rescattering contribution is **forbidden**, NLO is **zero**  
 $\Rightarrow$  effects of **NNLO** loops are very **important**



# NNLO loop-diagrams

- Topologies of NNLO diagrams:



- ➡ Keep higher-order vertices from  $\mathcal{L}_{\pi N}^{(2)}$
- ➡ Loops undergo significant cancellations

- Compact analytic result:

Filin, V.B., Epelbaum, Hanhart, Krebs, Kudryavtsev, Myhrer (2012)

$$\begin{aligned}
 iM_{nucl}^{Sym.} = & \frac{g_A^3}{f_\pi^5} v \cdot q \tau_+^a (i\varepsilon^{\alpha\mu\nu\beta} v_\alpha k_{1\mu} S_{1\nu} S_{2\beta}) (-2I_{\pi\pi}) \quad \longrightarrow \quad pp \rightarrow pp\pi^0 \\
 & + \frac{g_A^3}{f_\pi^5} v \cdot q \tau_\times^a (S_1 + S_2) \cdot k_1 \left( -\frac{19}{24} I_{\pi\pi} + \frac{5}{9} \frac{1}{(4\pi)^2} \right) \quad \longrightarrow \quad pp \rightarrow d\pi^+ \\
 & + \frac{g_A}{f_\pi^5} v \cdot q \tau_\times^a (S_1 + S_2) \cdot k_1 \left( \frac{1}{6} I_{\pi\pi} - \frac{1}{18} \frac{1}{(4\pi)^2} \right)
 \end{aligned}$$

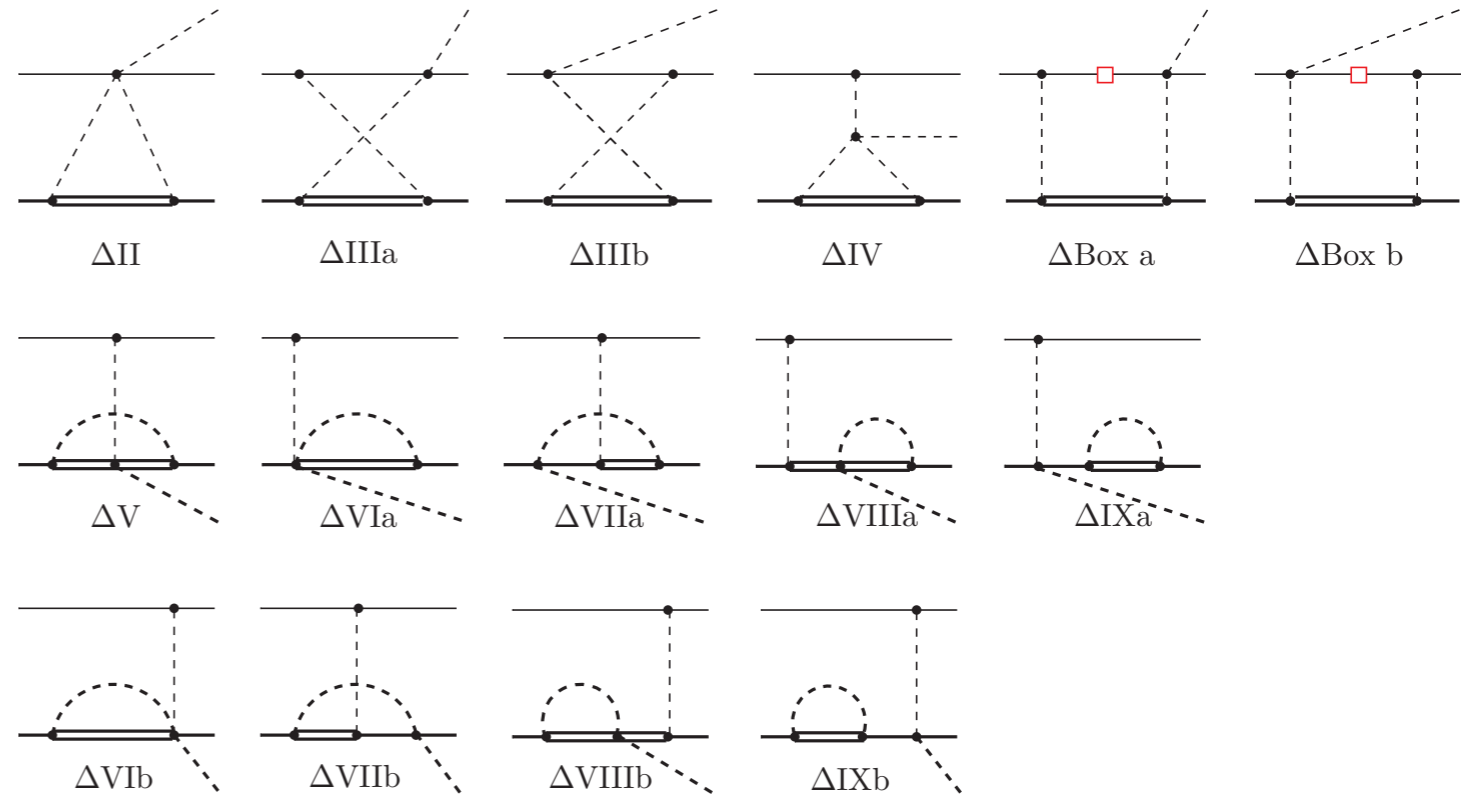
with only one basic integral: 
$$I_{\pi\pi} = \frac{\mu^\epsilon}{i} \int \frac{d^{4-\epsilon} l}{(2\pi)^{4-\epsilon} (l^2 - m_\pi^2 + i0)((l+k_1)^2 - m_\pi^2 + i0)}$$

# Explicit Delta: More NNLO Loops

- Delta-nucleon mass difference

$m_\Delta - m_N \approx 280 \text{ MeV} \rightarrow$  same order as  $p$

$\Rightarrow$  dynamical degree of freedom



Filin, V.B., Epelbaum, Hanhart, Krebs, Kudryavtsev, Myhrer (2013)

**Result:**

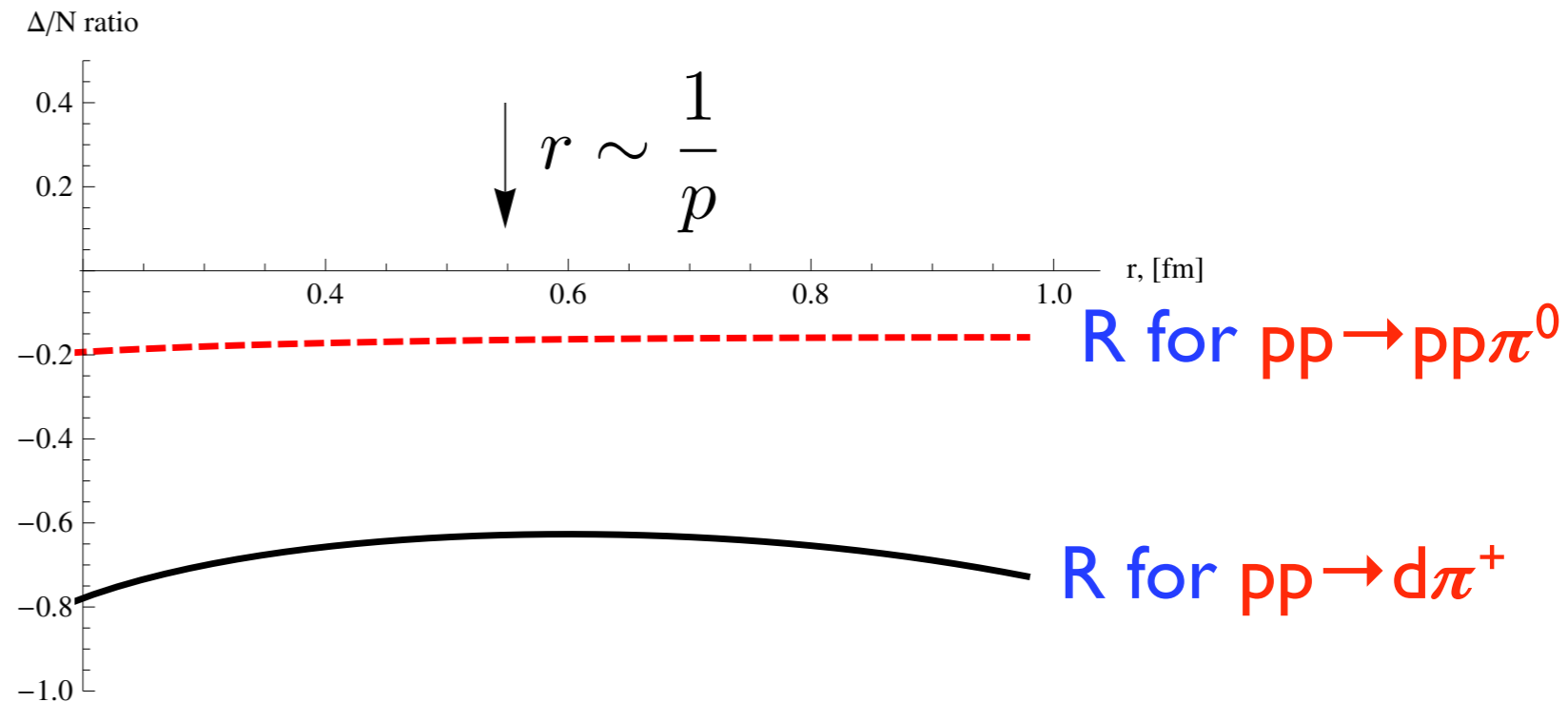
$$\begin{aligned}
 iM_{\Delta\text{-loops}}^{\text{NNLO}} = & \frac{g_A g_{\pi N \Delta}^2}{f_\pi^5} v \cdot q \tau_+^a (i\varepsilon^{\alpha\mu\nu\beta} v_\alpha k_{1\mu} S_{1\nu} S_{2\beta}) \\
 & \times \left\{ \frac{2}{9} \left( I_{\pi\pi} + \frac{1}{2} \frac{J_{\pi\Delta}}{\Delta} + \Delta J_{\pi\pi\Delta} + \frac{2}{(4\pi)^2} \right) + \frac{1}{18} k_1^2 J_{\pi\pi N\Delta} \right\} \longrightarrow \text{pp} \rightarrow \text{pp}\pi^0 \\
 & + \frac{g_A g_{\pi N \Delta}^2}{f_\pi^5} v \cdot q \tau_\times (S_1 + S_2) \cdot k_1 \\
 & \times \left\{ \frac{5}{9} \left( I_{\pi\pi} + \frac{1}{2} \frac{J_{\pi\Delta}}{\Delta} + \Delta J_{\pi\pi\Delta} + \frac{2}{(4\pi)^2} \right) + \frac{1}{18} k_1^2 J_{\pi\pi N\Delta} \right. \\
 & \left. + \frac{8}{9} \frac{\delta^2}{k_1^2} \left( I_{\pi\pi} + \frac{1}{2} \frac{J_{\pi\Delta}}{\Delta} + \Delta J_{\pi\pi\Delta} + \frac{2}{(4\pi)^2} \right) - \frac{2}{27} \left( I_{\pi\pi} + \frac{1}{2} \frac{J_{\pi\Delta}}{\Delta} + \frac{1}{3} \frac{2}{(4\pi)^2} \right) \right\} \longrightarrow \text{pp} \rightarrow \text{d}\pi^+
 \end{aligned}$$

Correct analytic behavior: If  $m_\Delta \rightarrow \infty$  the contribution of Delta vanishes (decoupling)

# The Role of Long-range parts of Loops

Ratio of model-independent long-range loop contributions:

$R = \text{Delta Loops} / \text{Nucleon Loops}$



- Nucleon and Delta loops are of similar size: Proves power counting
- Net effect of long-range loops looks consistent with what is needed from Data

$pp \rightarrow d\pi^+$ :  
 ➡ net result is small due to cancellations  
 ➡ good description of data already at NLO

$pp \rightarrow pp\pi^0$ :  
 ➡ net result is of sizable  
 ➡ we probe NNLO contributions directly ( LO + NLO  $\approx 0$  )

# Charge symmetry breaking

Charge symmetry – invariance under interchange of u- and d-quarks

- Approximate symmetry of QCD
- Explicitly broken due to **quark-mass difference** and **electromagnetic effects**
- On the level of hadrons → invariance under interchange of **p** and **n**

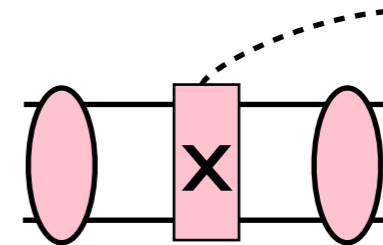
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Charge symmetry breaking in  $pn \rightarrow d\pi^0$  :

Opper et al. (2003), v.Kolck et al (2000), Bolton and Miller (2009), Filin et al.(2009)



- Interchange of **p** and **n** changes differential cross section

- Forward-Backward Assymetry  $A_{fb} \propto \frac{\frac{d\sigma}{d\Omega}(\theta) - \frac{d\sigma}{d\Omega}(\pi - \theta)}{\frac{d\sigma}{d\Omega}(\theta) + \frac{d\sigma}{d\Omega}(\pi - \theta)}$  TRIUMF (2003)

- Theory:  $A_{fb} \propto \frac{\text{Re}(M_{s\text{-wave}}^{\text{CSB}} M_{p\text{-wave}}^{\text{CS}*})}{|M_{s\text{-wave}}^{\text{CS}}|^2} \propto (m_p - m_n)^{\text{str}}$  due to  $m_u - m_d$

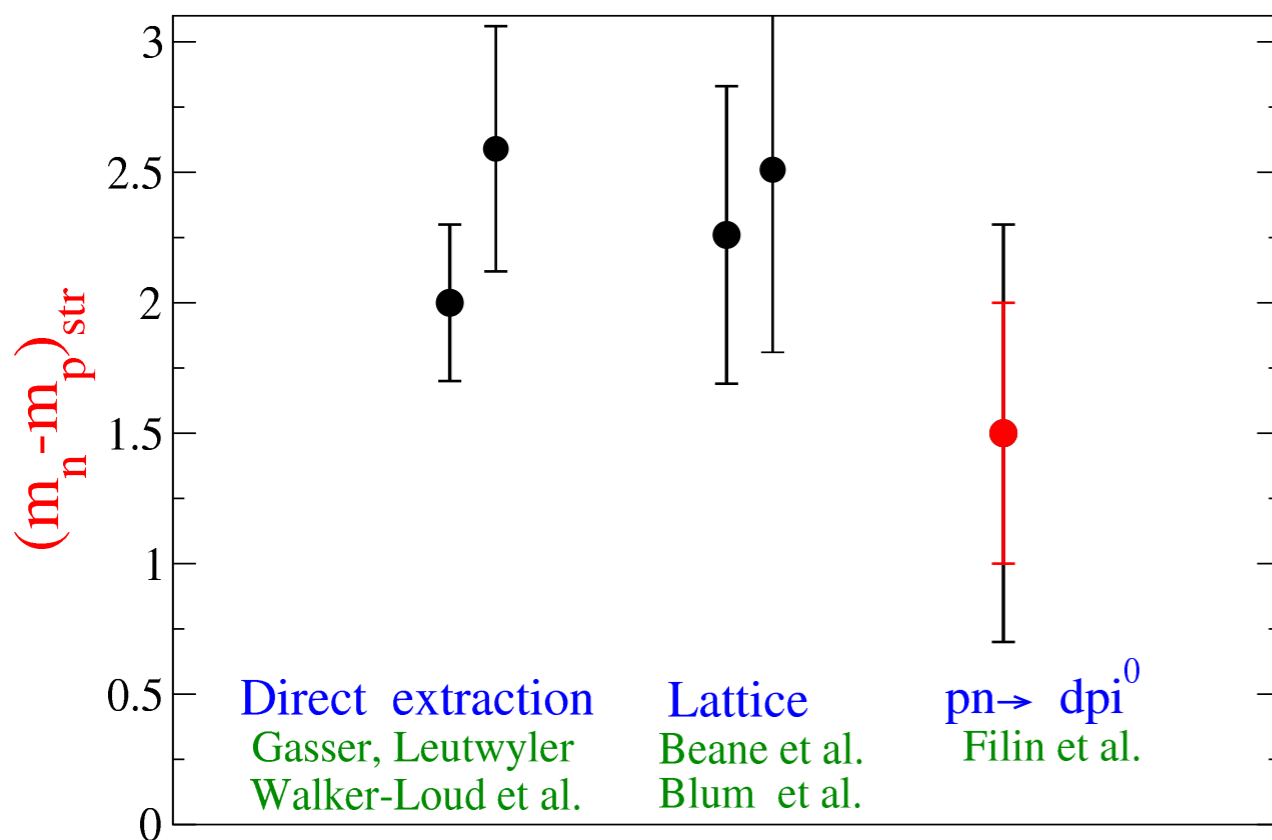
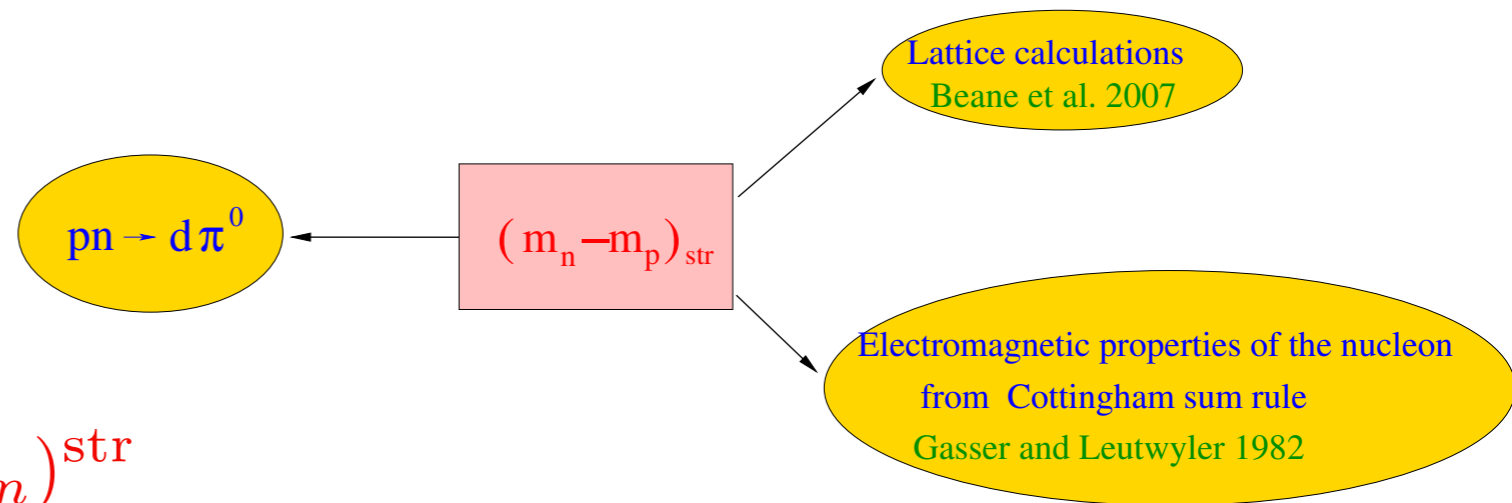
# Charge symmetry breaking in $pn \rightarrow d\pi^0$

Experiment

$$A_{fb} = (17.2 \pm 8 \pm 5.5) \cdot 10^{-4}$$

Our LO result:

$$A_{fb} = (11.5 \pm 3.5) \cdot 10^{-4} (m_p - m_n)^{str}$$



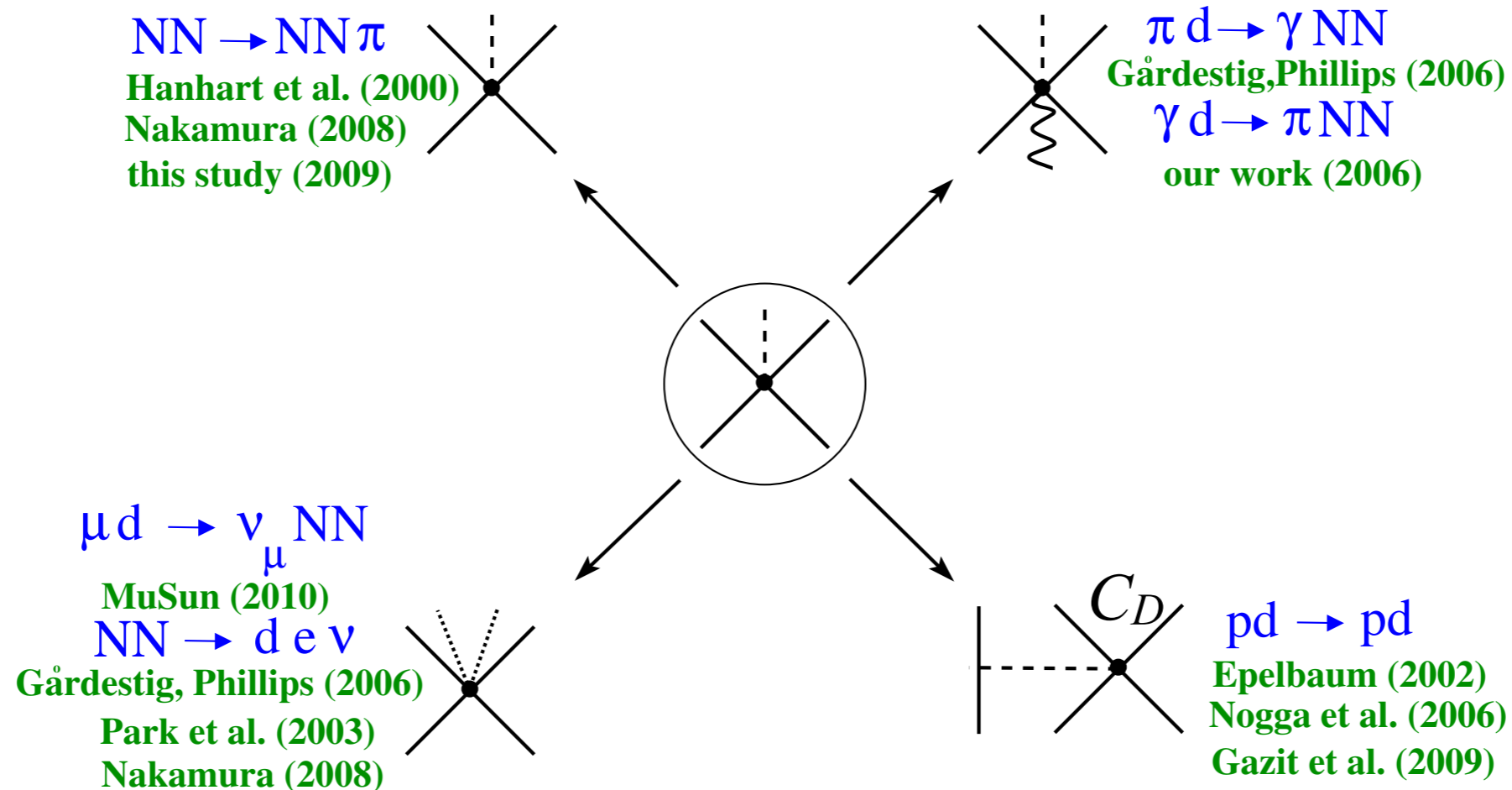
Further Improvements require:

- ➡ CSB Chiral Loops at NNLO
- ➡ Combined analysis together with  $dd \rightarrow \alpha\pi^0$

First studies: Nogga et al. (2004,2006)

From  $NN \rightarrow NN\pi$  to weak few-nucleon reactions,  $3N$ -force, ...

# p-wave pion production and $(N^\dagger N)^2 \pi$ LEC



$$\mathcal{L} = -2d (N^\dagger S \cdot u N) N^\dagger N$$

$$f_\pi u_\mu = -\tau \partial_\mu \pi - \varepsilon_{3ab} V_\mu \pi_a \tau_b + f_\pi A_\mu + \dots$$

$NN \rightarrow NN\pi$ : Best channel to extract LEC  $d$  is  $pn \rightarrow pp\pi^-$  V.B. et al (2009)

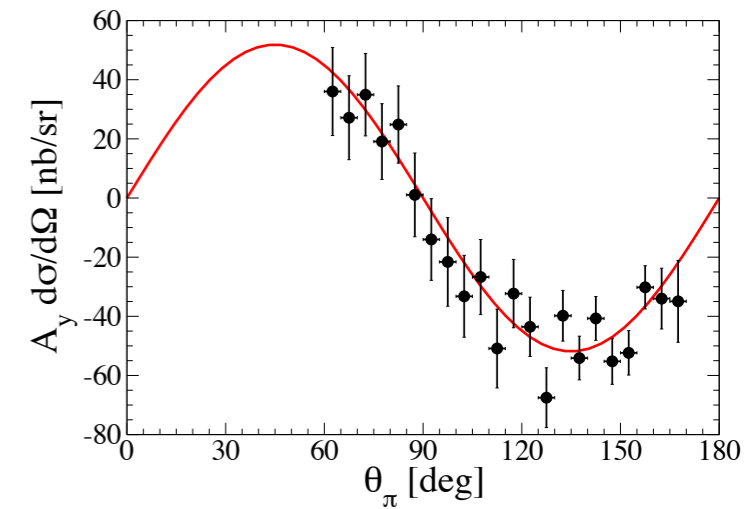
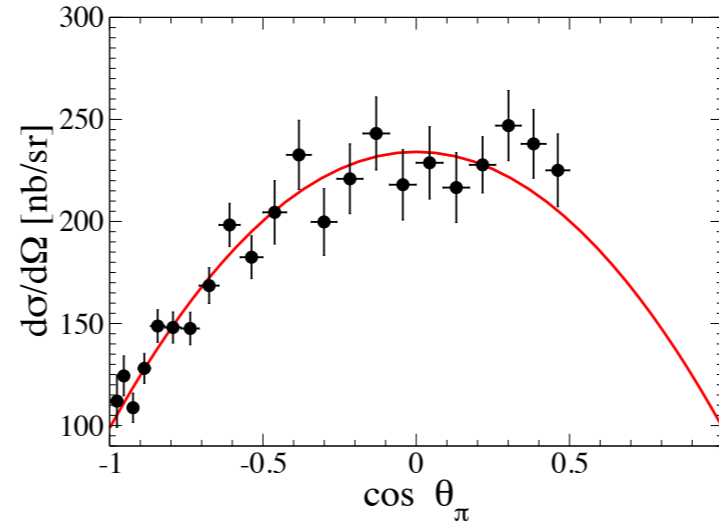
Relevant Transition:  ${}^3S_1 \rightarrow {}^1S_0 p \Rightarrow$  proposal to measure at COSY



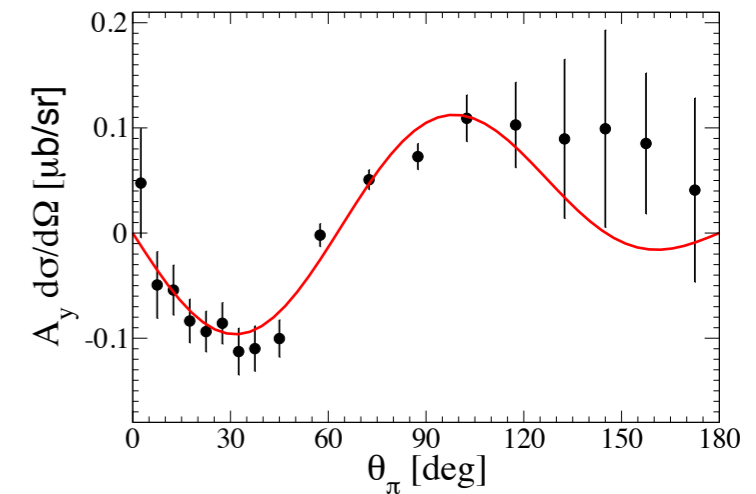
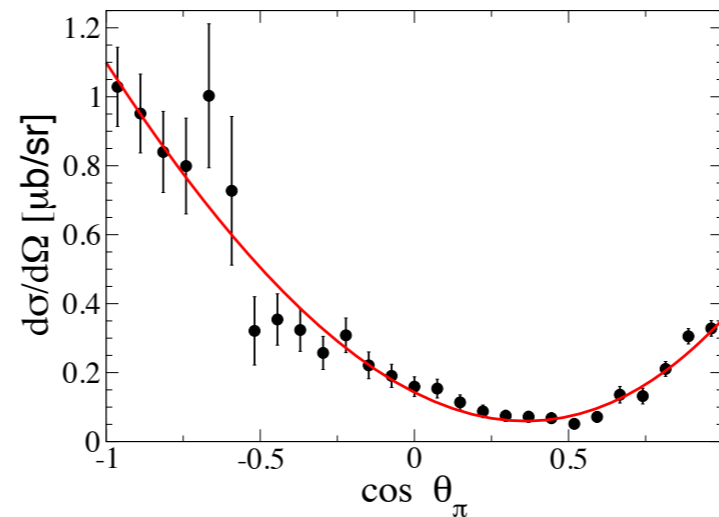
# $pp \rightarrow (pp)_S \pi^0$ and $pn \rightarrow (pp)_S \pi^-$ at COSY and amplitude analysis (ANKE 2012)

$T_{lab} = 353 \text{ MeV}$ ,  $E_{pp} < 3 \text{ MeV} \implies$  S-wave  $pp$  state:  $(pp)_S$

$pp \rightarrow (pp)_S \pi^0$



$pn \rightarrow (pp)_S \pi^-$



- ▶ confirmed older TRIUMF data and extended them to the whole angular domain
- ▶ no signal of  $\cos^4 \theta_\pi$  (and higher power) terms  $\implies$  partial waves higher than (pion)  $d$ -waves are irrelevant
- ▶ 5 partial waves:  $M_{s\text{-wave}}^{3P_0}$ ,  $M_{p\text{-wave}}^{3S_1}$ ,  $M_{p\text{-wave}}^{3D_1}$ ,  $M_{d\text{-wave}}^{3P_2}$  and  $M_{d\text{-wave}}^{3F_2}$  to be fitted to data
- ▶ impose the phase information from NN interaction  $M = |M| e^{i\delta_{ISI}} e^{i\delta_{FSI}}$  – Watson theorem for uncoupled or weakly coupled partial waves

# Results of PWA

- ▶ Direct fit to data on  $pp \rightarrow (pp)_S \pi^0$  yields for **s-** and **d-wave** amplitudes

$$M_{s\text{-wave}}^{3P_0} = (55.3 \pm 0.4) - (14.7 \pm 0.1)i \sqrt{\text{nb/sr}}$$

$$M_{d\text{-wave}}^{3P_2} = -(26.6 \pm 1.1) - (8.6 \pm 0.4)i \sqrt{\text{nb/sr}}$$

$$M_{d\text{-wave}}^{3F_2} = (5.3 \pm 2.3) \sqrt{\text{nb/sr}}$$

- ▶ robust results confirmed by global fit to  $pp \rightarrow (pp)_S \pi^0$  and  $pn \rightarrow (pp)_S \pi^-$
- ▶ pion **d-waves** are quite large even near threshold
- ▶ comparison of  $\chi\text{EFT}^*$  with data on the amplitude level is possible

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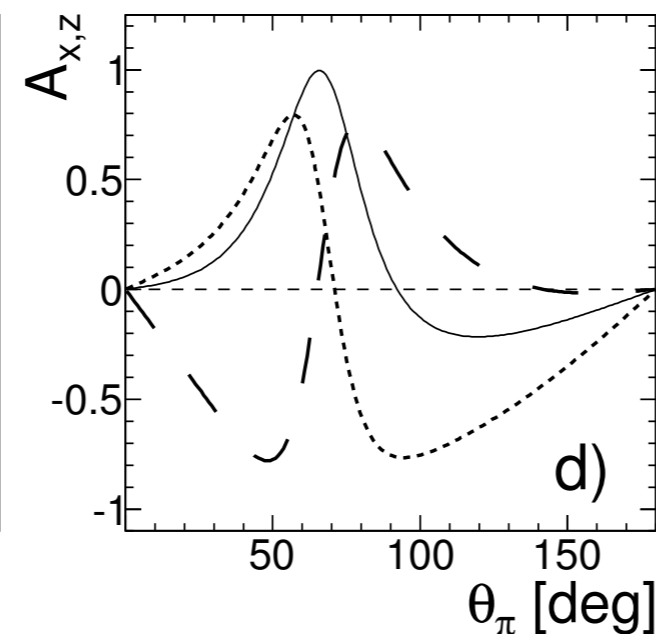
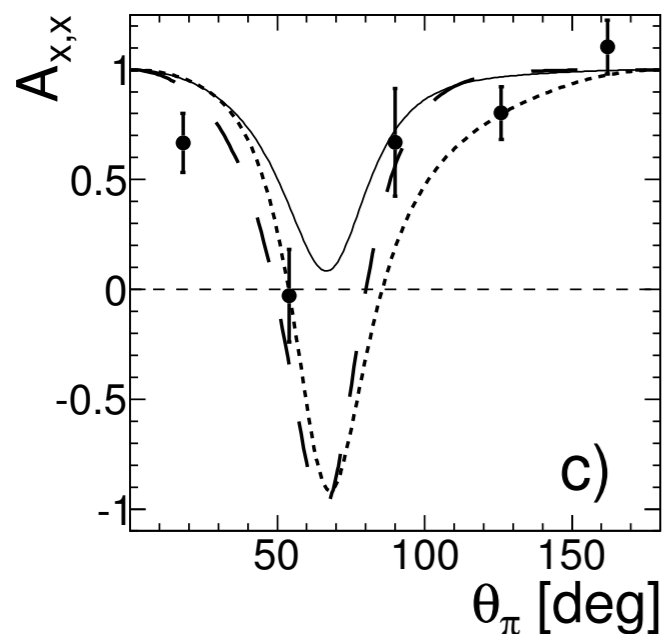
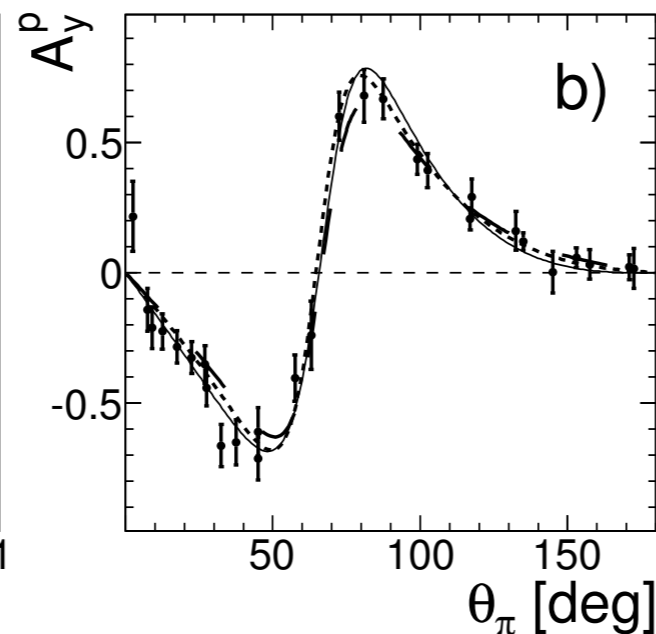
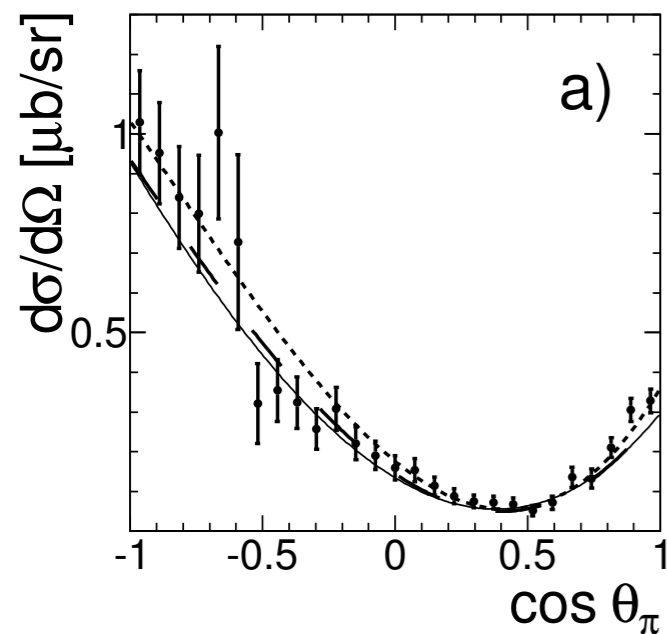
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- ▶ pion **d-waves** are quite large even near threshold
- ▶ comparison of  $\chi^{\text{EFT}^*}$  with data on the amplitude level is possible
- ▶ But there is NO definite conclusion for **p-wave** amplitudes

PWA has 3 minima with almost the same  $\chi^2$  but with different p-wave amplitudes!

# Results of PWA

Amplitude	Real	Imaginary	Im/Re
Solution 1: $\chi^2 / ndf = 101 / 82$ solid line			
${}^3S_1 \rightarrow {}^1S_0 p$	$-37.5 \pm 1.7$	$16.5 \pm 1.9$	$-0.44 \pm 0.06$
${}^3D_1 \rightarrow {}^1S_0 p$	$-93.1 \pm 6.5$	$122.7 \pm 4.4$	$-1.32 \pm 0.11$
Solution 2: $\chi^2 / ndf = 103 / 82$ dashed line			
${}^3S_1 \rightarrow {}^1S_0 p$	$-63.7 \pm 2.5$	$-1.3 \pm 1.6$	$0.02 \pm 0.03$
${}^3D_1 \rightarrow {}^1S_0 p$	$-109.9 \pm 4.2$	$52.9 \pm 3.2$	$-0.48 \pm 0.03$
Solution 3: $\chi^2 / ndf = 106 / 82$ dotted line			
${}^3S_1 \rightarrow {}^1S_0 p$	$-25.4 \pm 1.9$	$-7.3 \pm 1.5$	$0.20 \pm 0.07$
${}^3D_1 \rightarrow {}^1S_0 p$	$-172.2 \pm 5.6$	$92.0 \pm 6.2$	$-0.53 \pm 0.04$



- All solutions describe  $d\sigma/d\Omega$  and  $A_y$
- $A_{x,x}$  could be useful but high precision needed
- $A_{x,x}$  at COSY (2013): not enough statistics
- $A_{x,z}$  is most promising

# Results of PWA. Theory Insights

Amplitude	Real	Imaginary	$\tan(\delta) = \text{Im}/\text{Re}$
<b>Solution 1: <math>\chi^2 / \text{ndf} = 101 / 82</math></b>			
${}^3S_1 \rightarrow {}^1S_0 p$	$-37.5 \pm 1.7$	$16.5 \pm 1.9$	$-0.44 \pm 0.06$
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- ▶ Phases should not be far from those predicted by the Watson theorem:  $\tan \delta_{3S_1} = 0.03$  and  $\tan \delta_{3D_1} = -0.46$  (SAID, Arndt et al.(2000))
- ▶ Preference against solution 1 and possibly in favour of solution 2.
- ▶ For the relevant  ${}^3S_1 \rightarrow {}^1S_0 p$  amplitude our  $\text{N}^2\text{LO } \chi\text{EFT}^*$  calculation (2009) gave  $-53.7 - 2.6 i \implies$  indication in favour of solution 2

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${}^3D_1 \rightarrow {}^1S_0 p$	$-109.9 \pm 4.2$	$52.9 \pm 3.2$	$-0.48 \pm 0.03$
<b>Solution 3: <math>\chi^2 / \text{ndf} = 106 / 82</math></b>			
${}^3S_1 \rightarrow {}^1S_0 p$	$-25.4 \pm 1.9$	$-7.3 \pm 1.5$	$0.20 \pm 0.07$
${}^3D_1 \rightarrow {}^1S_0 p$	$-172.2 \pm 5.6$	$92.0 \pm 6.2$	$-0.53 \pm 0.04$

- ▶ Phases should not be far from those predicted by the Watson theorem:  $\tan \delta_{3S_1} = 0.03$  and  $\tan \delta_{3D_1} = -0.46$  (SAID, Arndt et al.(2000))
- ▶ Preference against solution 1 and possibly in favour of solution 2.
- ▶ For the relevant  ${}^3S_1 \rightarrow {}^1S_0 p$  amplitude our  $N^2\text{LO } \chi\text{EFT}^*$  calculation (2009) gave  $-53.7 - 2.6 i \implies$  indication in favour of solution 2  
( $\tan \delta = 0.05$ )

# Summary

We investigate chiral dynamics in the reaction  $NN\text{-}NN\pi$  at low energies

## Non-trivial production mechanism

- $pp\text{-}d\pi^+$  is dominated by the **Weinberg-Tomosawa** mechanism while  $pp\text{-}pp\pi^0$  probes higher-order (**NNLO**) contributions
- **Chiral Loops at NNLO** are derived: **big potential** to understand data in both channels

## Charge symmetry breaking in $NN\text{-}NN\pi$

- Access to the quark-mass induced contribution to the proton-neutron mass difference
- NLO calculation of  $pn\text{-}d\pi^0$  in agreement with lattice and dispersive results

## Connection to other low-energy reactions: LEC $d$

- Can be extracted from  $NN\text{-}NN\pi$ :  $pn\text{-}pp\pi^-$  measured at COSY
- PWA of data: **no unique solution** for the relevant  ${}^3S_1\text{-}{}^1S_0$  p amplitude
- PWA + theory constraints: probably **the unique solution**