

# Experimental Overview on DVCS Measurements (Past, Present and Future)

SPIN 2014

Beijing, October 2014

Horst Fischer

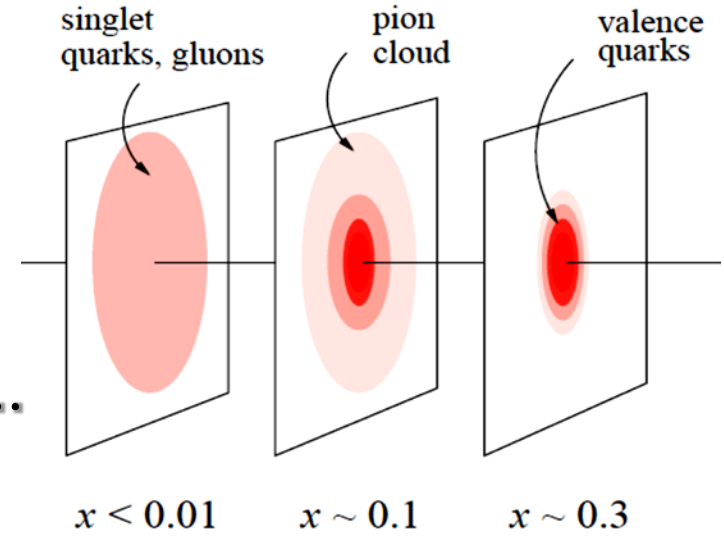
ALU Freiburg

Outline of this talk:

- Introduction
- Experiments
- Selected results:
  - ➔ Cross section
  - ➔ Beam charge & spin difference
  - ➔ Interference Term
  - ➔ Measurements for GPD E

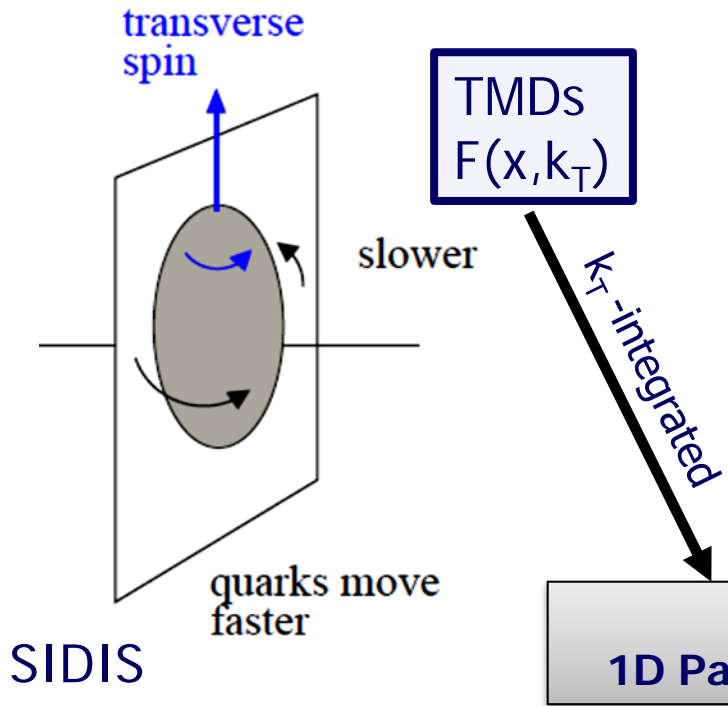
# Nucleon Tomography

**Holy grail:**  
**Wigner Distributions**  
**5 D picture of nucleon phase space**  
 $\rho(x, k_T, b_T)$



Experimentally from 3-D Pictures ...

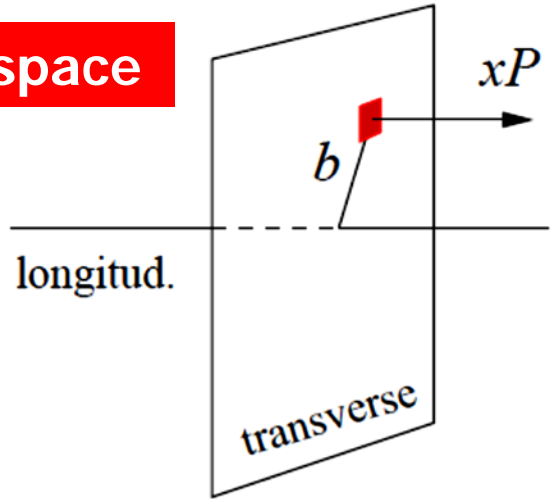
... in momentum space ...



... in configuration space

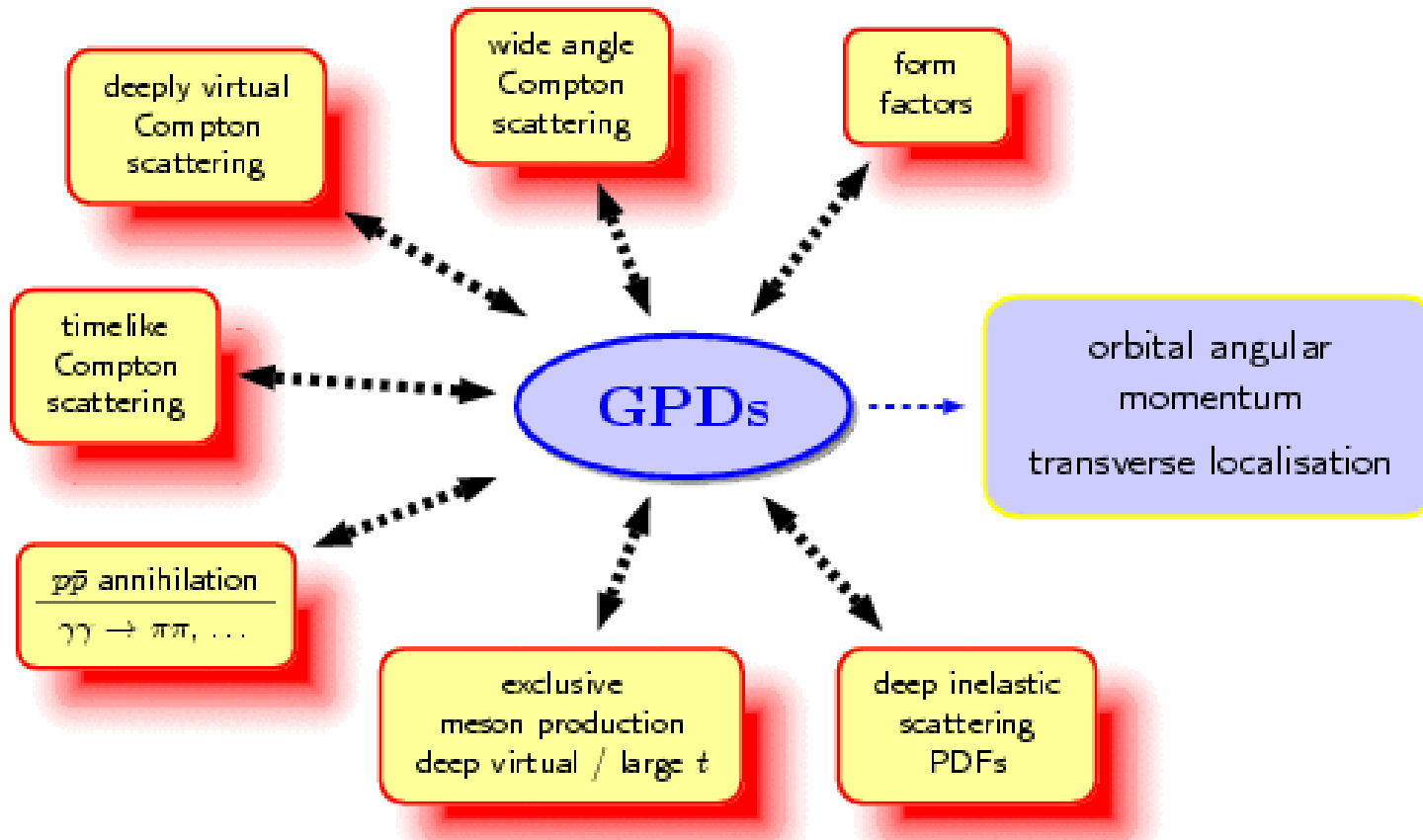
GPDs  
 $H(x, b_\perp) \leftrightarrow H(x, \xi, t)$

$\xi=0, t=0$



Exclusive reactions

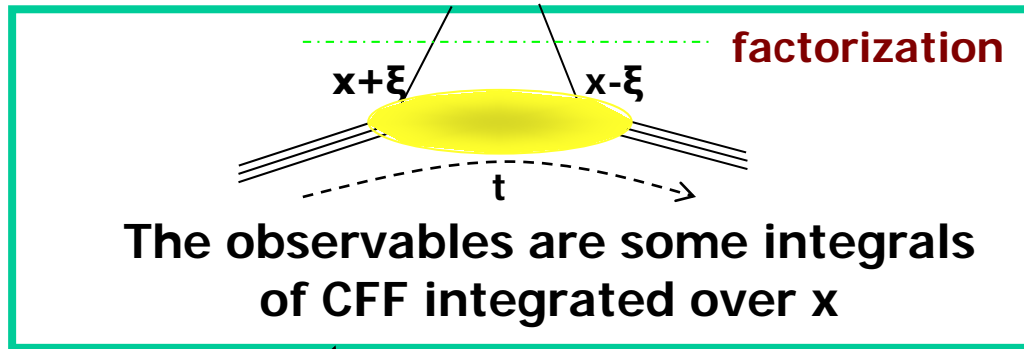
# Accessing GPDs



GPD filter by quantum numbers of final state:

- DVCS ( $\gamma$ ): H, E,  $\tilde{H}$ ,  $\tilde{E}$
- VM ( $\rho, \omega, \phi$ ): H, E
- different quark flavours ( $p, e$ ):  $\tilde{H}$ ,  $\tilde{E}$

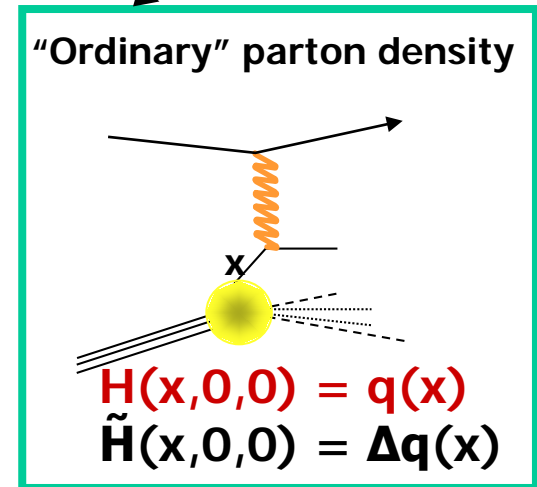
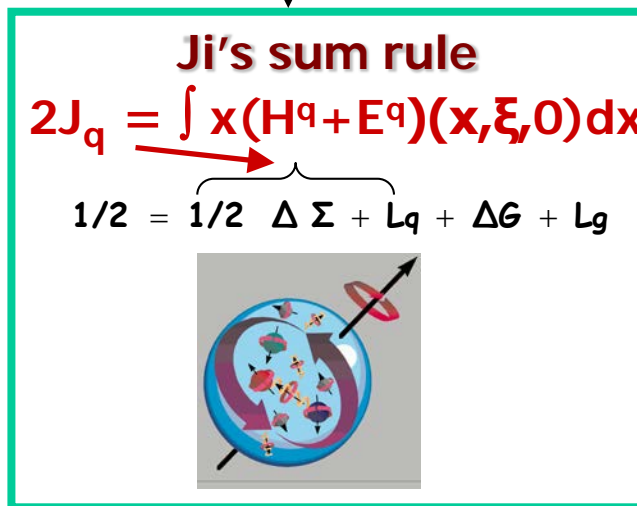
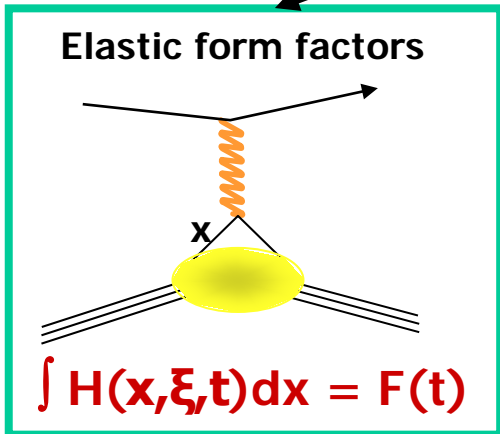
# GPDs and their Relation to Observables



Dynamics of partons in nucleon models:  
**Parameterization**

**Fit parameters to the data**

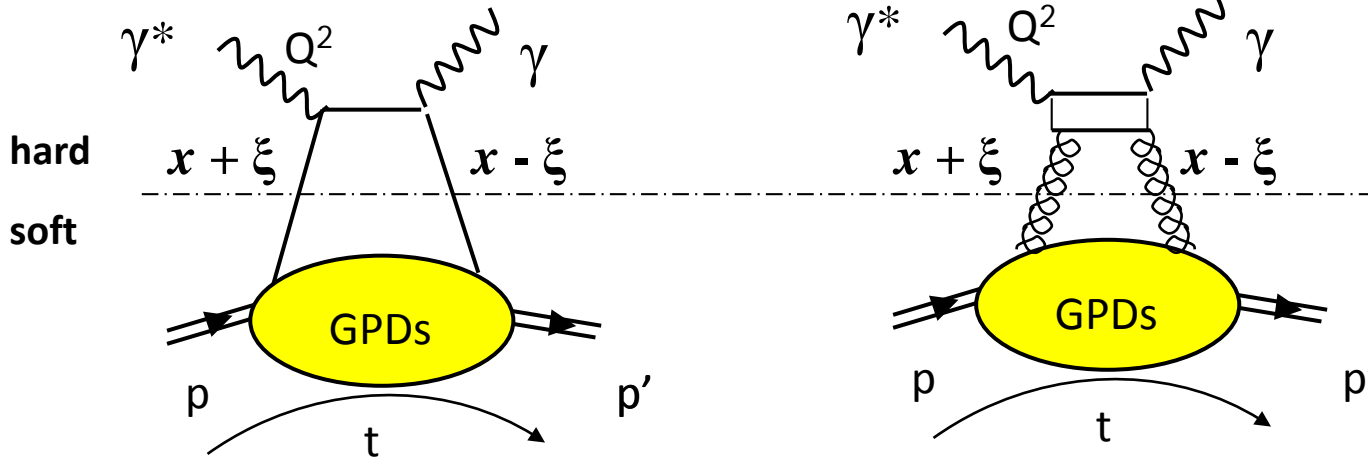
$H, \tilde{H}, E, \tilde{E}(x, \xi, t)$



# Exclusive reactions: DVCS and HEMP

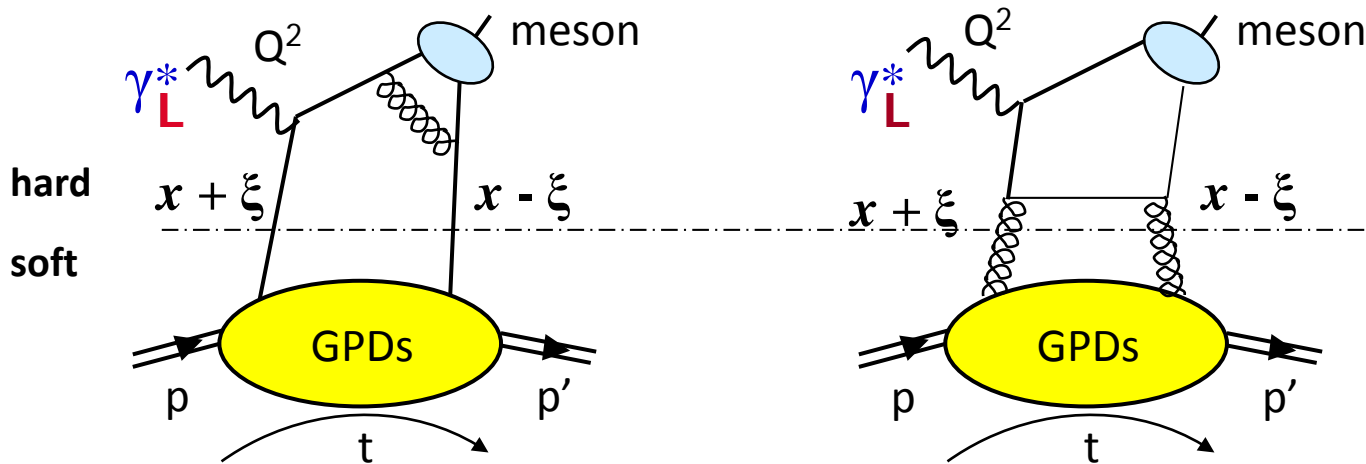
## Deeply Virtual Compton Scattering (DVCS):

Factorisation:  
Collins *et al.*



$Q^2$  large  
 $t \ll Q^2$

## Hard Exclusive Meson Production (HEMP):



+  $\gamma_L^*$

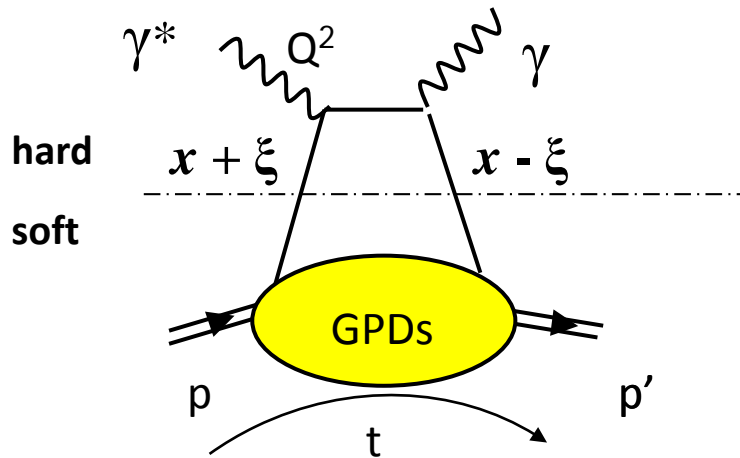
Meson w.f.  
Large power & NLO  
Very slow scaling

Quark contribution

Gluon contribution

# Exclusive reactions: DVCS and HEMP

## Deeply Virtual Compton Scattering (DVCS):



**Golden channel**

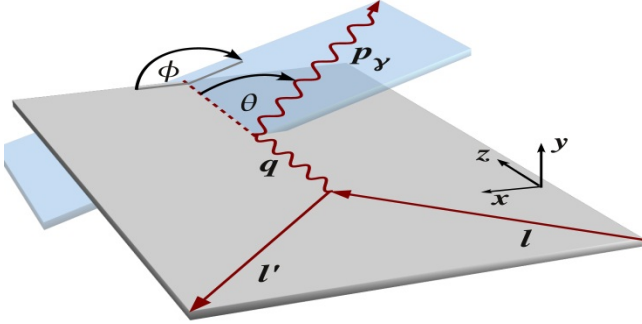
Definition of variables:

$x$ : average long. momentum - NOT ACCESSIBLE

$\xi$ : long. mom. difference  $\simeq x_B / (2 - x_B)$

$t$ : four-momentum transfer  
related to  $b_{\perp}$  via Fourier transform

# Cross Section & Angular Dependence



$$d\sigma_{(\mu p \rightarrow \mu p \gamma)} = d\sigma^{BH} + d\sigma_{unpol}^{DVCS} + P_\mu d\sigma_{pol}^{DVCS} + e_\mu a^{BH} \text{Re} T^{DVCS} + e_\mu P_\mu a^{BH} \text{Im} T^{DVCS}$$

$$d\sigma^{BH} = \frac{\Gamma(x_B, Q^2, t)}{P_1(\phi)P_2(\phi)} (c_0^{BH} + c_1^{BH} \cos \phi + c_2^{BH} \cos 2\phi)$$

Known to 1%

$$d\sigma_{unpol}^{DVCS} = \frac{e^6}{y^2 Q^2} (c_0^{DVCS} + c_1^{DVCS} \cos \phi + c_2^{DVCS} \cos 2\phi)$$

Bilinear combination of GPDs

$$d\sigma_{pol}^{DVCS} = \frac{e^6}{y^2 Q^2} (s_1^{DVCS} \sin \phi)$$

$$a^{BH} \text{Re} T^{DVCS} = \frac{e^6}{xy^3 t P_1(\phi)P_2(\phi)} (c_0^{Int} + c_1^{Int} \cos \phi + c_2^{Int} \cos 2\phi + c_3^{Int} \cos 3\phi)$$

linear combination of GPDs

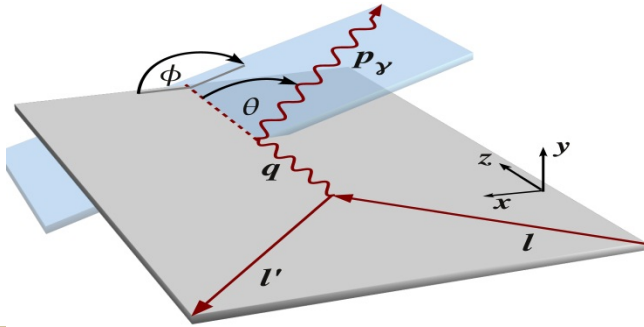
$$a^{BH} \text{Im} T^{DVCS} = \frac{e^6}{xy^3 t P_1(\phi)P_2(\phi)} (s_1^{Int} \sin \phi + s_2^{Int} \sin 2\phi)$$

Twist 2

Twist 3

Twist 2 gluon

# Example: Observables with unpolarized targets



$$d\sigma_{(\mu p \rightarrow \mu p \gamma)} = d\sigma^{BH} + d\sigma_{unpol}^{DVCS} + P_\mu d\sigma_{pol}^{DVCS} + e_\mu a^{BH} \text{Re} T^{DVCS} + e_\mu P_\mu a^{BH} \text{Im} T^{DVCS}$$

● Beam Charge & Spin Sum:

$$S_{CS,U} = d\sigma^{+\leftarrow} + d\sigma^{-\rightarrow} = 2 \left( d\sigma^{BH} + d\sigma_{unpol}^{DVCS} + e_\mu P_\mu a^{BH} \text{Im} T^{DVCS} \right)$$

$$c_0^{DVCS+BH} + c_1^{DVCS+BH} \cos \phi + c_2^{DVCS+BH} \cos 2\phi$$

$$\frac{d\sigma}{d|t|}$$

$$s_1^{Int} \sin \phi + s_2^{Int} \sin 2\phi$$

$$\text{Im}(F_1 \mathcal{H})$$

● Beam Charge & Spin Difference:

$$\mathcal{D}_{CS,U} = d\sigma^{+\leftarrow} - d\sigma^{-\rightarrow} = 2 \left( P_\mu d\sigma_{pol}^{DVCS} + e_\mu a^{BH} \text{Re} T^{DVCS} \right)$$

$$s_1^{DVCS} \sin \phi$$

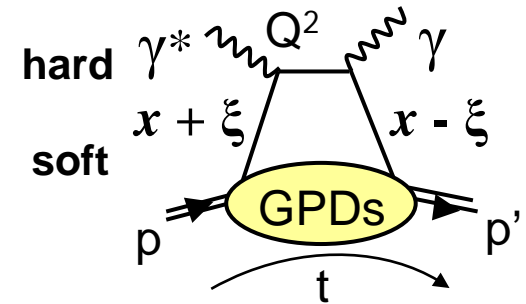
$$c_0^{Int} + c_1^{Int} \cos \phi + c_2^{Int} \cos 2\phi + c_3^{Int} \cos 3\phi$$

$$\text{Re}(F_1 \mathcal{H})$$



# Compton Form Factors are measured in DVCS

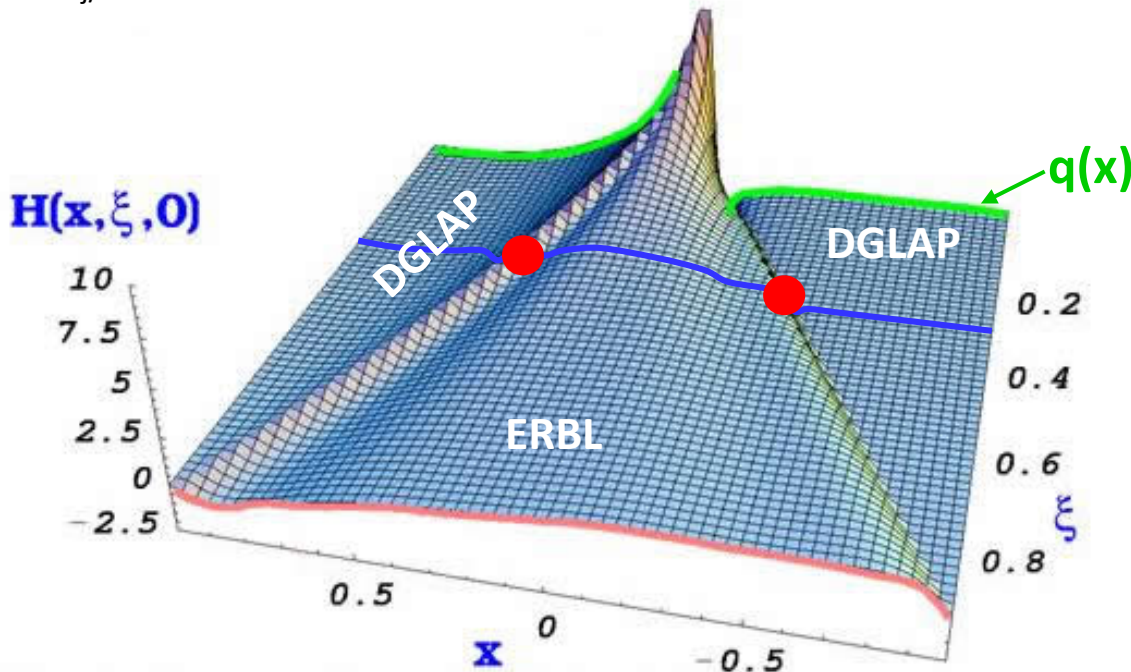
The amplitude DVCS at LT & LO in  $\alpha_S$ :



$$\mathcal{H} = \int_{-1}^{+1} dx \frac{H(x, \xi, t)}{x - \xi + i\epsilon} = \mathcal{P} \int_{-1}^{+1} dx \frac{H(x, \xi, t)}{x - \xi} - i \pi H(x = \xi, \xi, t)$$

Real part
Imaginary part

$t, \xi \sim x_{Bj/2}$  fixed

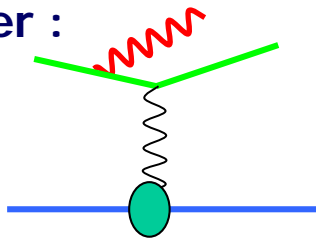


Im part measured in  
**Beam Spin**  
 or **Target Spin** asymmetries

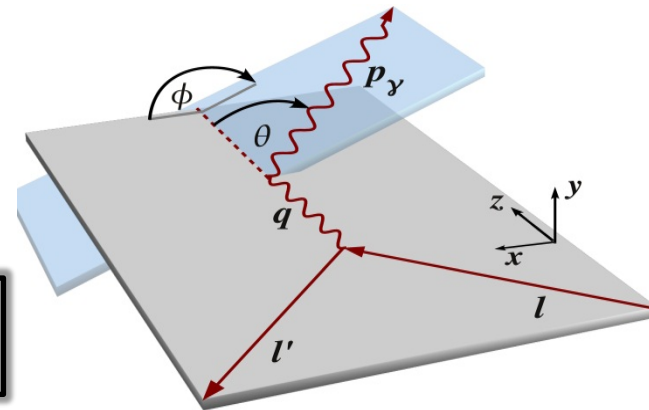
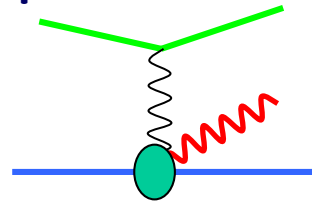
Real part measured in  
**Beam Charge** asymmetry  
 or **cross section**

# Bethe-Heitler & DVCS Cross Sections

Bethe-Heitler :



DVCS :

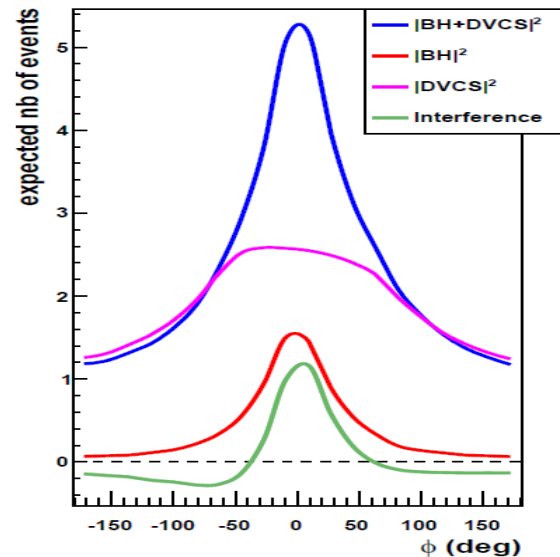
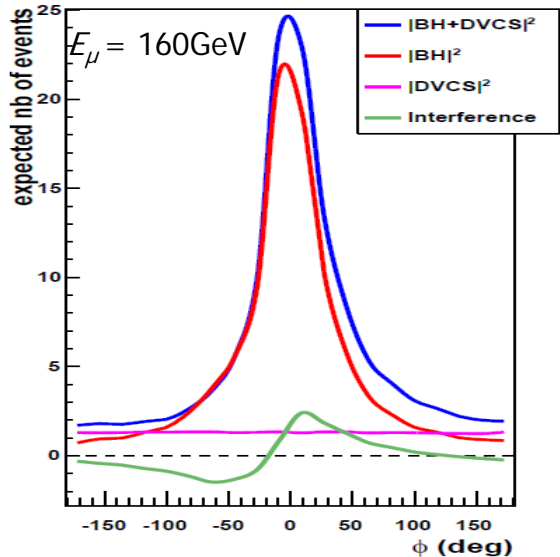
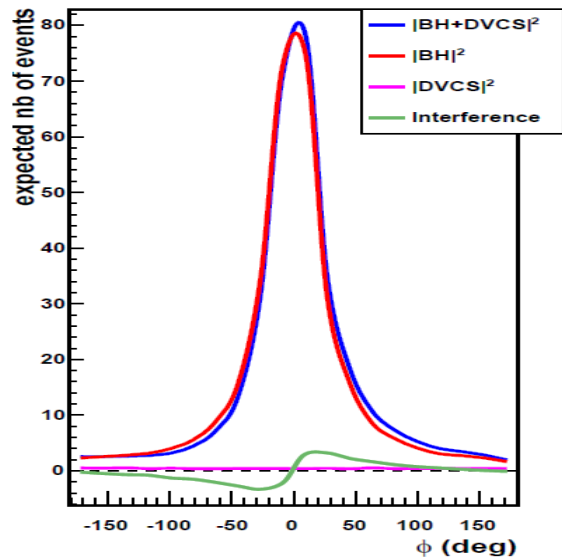


$$d\sigma \propto |T_{BH}|^2 + \text{Interference Term} + |T_{DVCS}|^2$$

Low  $x_B$ : BH dominates  
 $0.005 < x_{Bj} < 0.01$

Large  $x_B$ : Int dominates  
 $0.01 < x_{Bj} < 0.03$

Large  $x_B$ : DVCS dominates  
 $x_{Bj} > 0.03$



● Reference yield from almost pure BH

● Study DVCS through interference term

● Study  $d\sigma^{DVCS}/dt$   
➔ Transverse Imaging

➔  $Re T^{DVCS}$  &  $Im T^{DVCS}$

# Focus on DVCS2<sup>2</sup> or Interference?

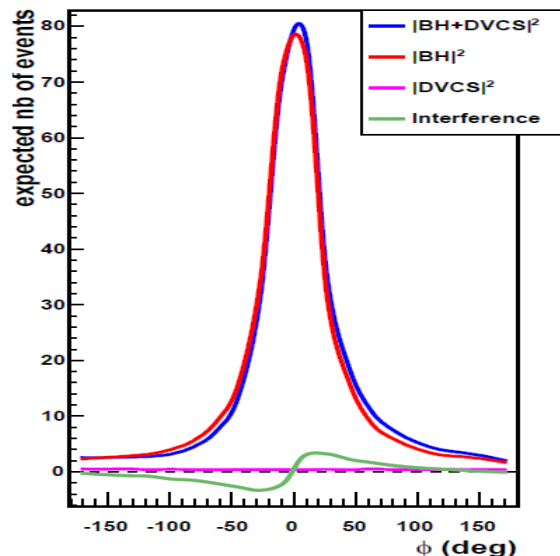
- Strong  $x_{Bj}$  -  $E_{\text{beam}}$  correlation in fixed target experiments

HERMES, JLAB,  
COMPASS

Only  
H1, ZEUS,  
COMPASS

Low  $x_B$ : BH dominates

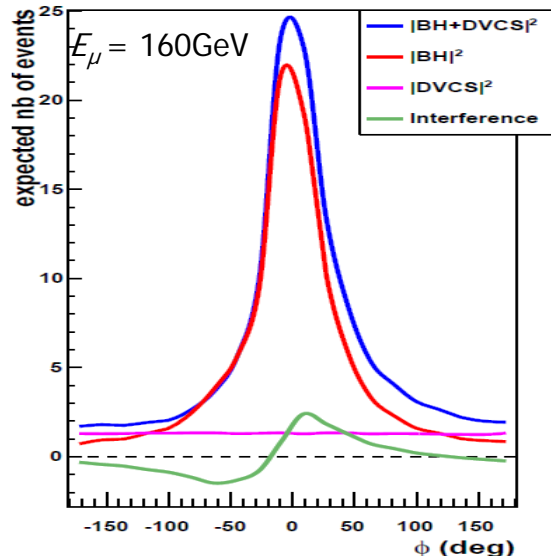
$$0.005 < x_{Bj} < 0.01$$



- Reference yield from almost pure BH

Large  $x_B$ : Int dominates

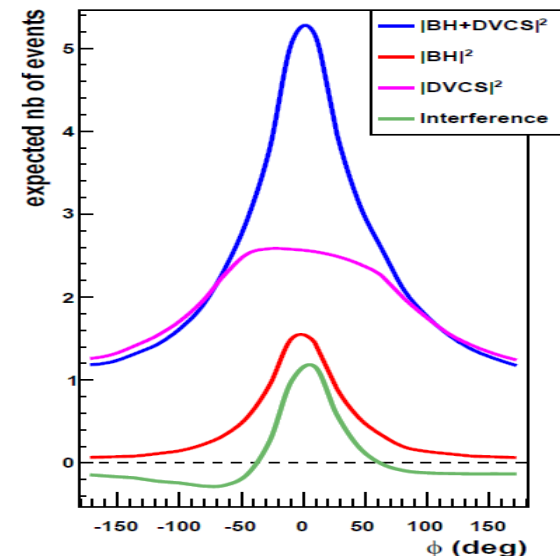
$$0.01 < x_{Bj} < 0.03$$



- Study DVCS through interference term
- $\text{Re } T^{\text{DVCS}}$  &  $\text{Im } T^{\text{DVCS}}$

Large  $x_B$ : DVCS dominates

$$x_{Bj} > 0.03$$



- Study  $d\sigma^{\text{DVCS}}/dt$
- Transverse Imaging

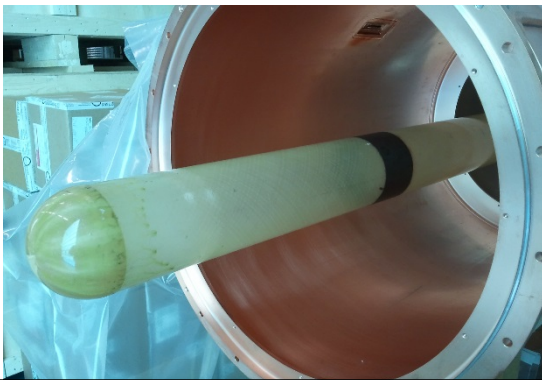
# The ideal experiment

## Beam:

- high beam energy to ensure hard regime
- longitudinally polarized beam
- positive and negative lepton beam
- variable energy for  $\varepsilon$  separation for DVCS<sup>2</sup> and interference term



High luminosity to allow fully differential analysis in  $x_{Bj}$   $Q^2$   $t$   $\phi$

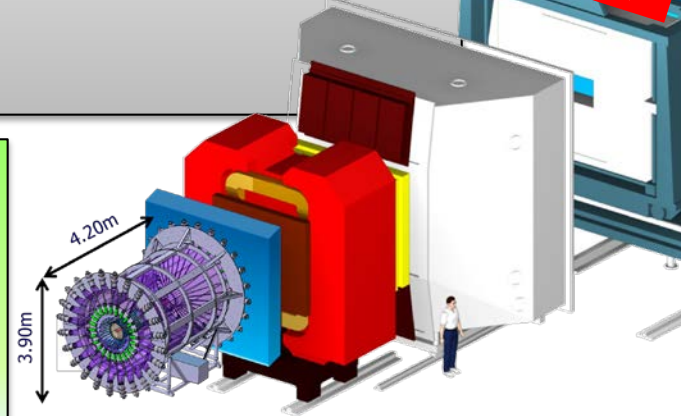


## Target:

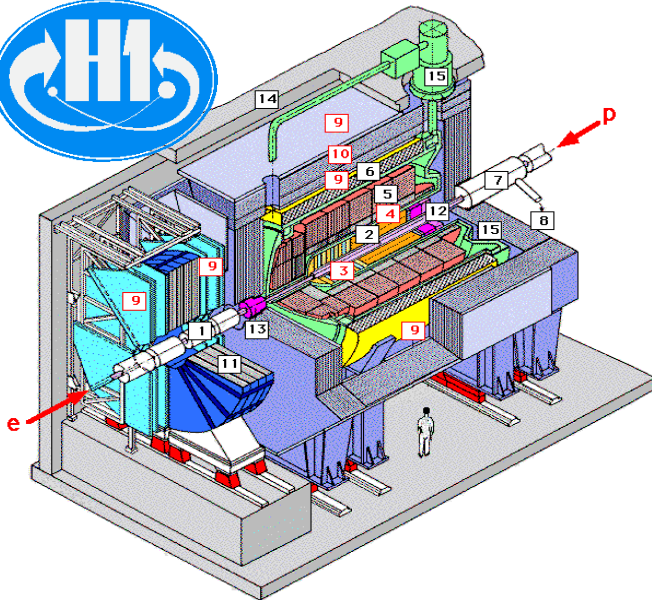
- H<sub>2</sub> and D<sub>2</sub>
- unpolarized, longitudinal or transverse polarized target

## Detector:

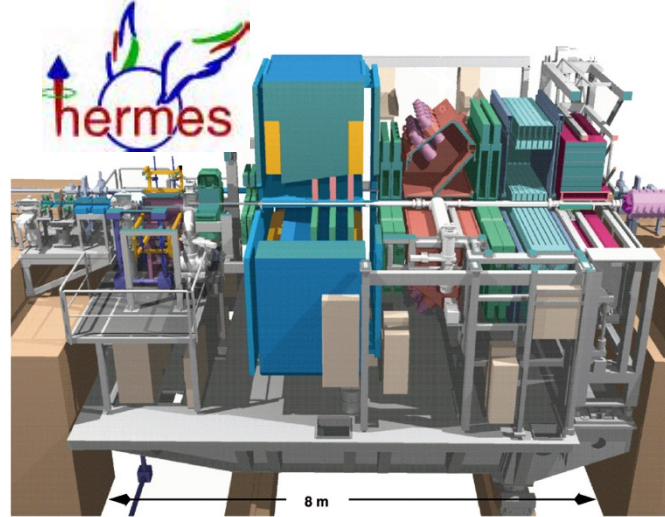
- hermetic to ensure exclusivity
- efficient calorimetry with good energy resolution



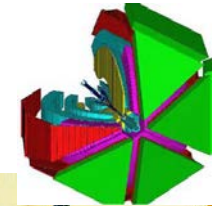
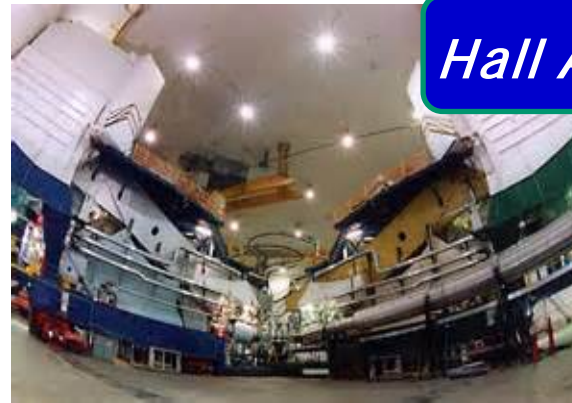
# Experiments in the past



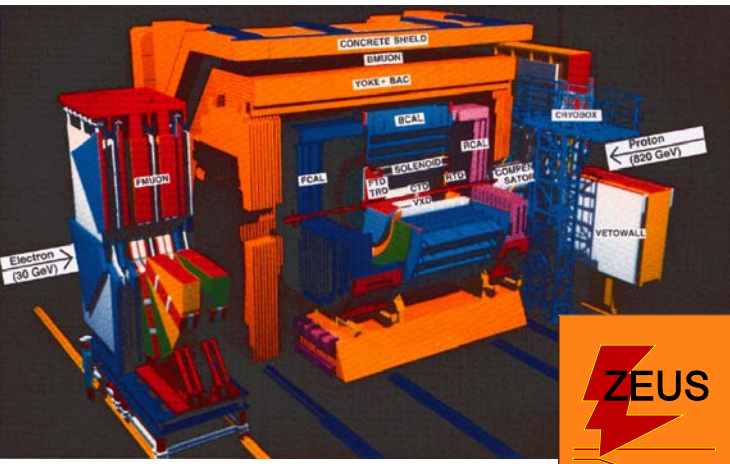
Polarised 27 GeV  $e^-/e^+$   
 Unpolarised 920 GeV p  
 ~ Full event reconstruction



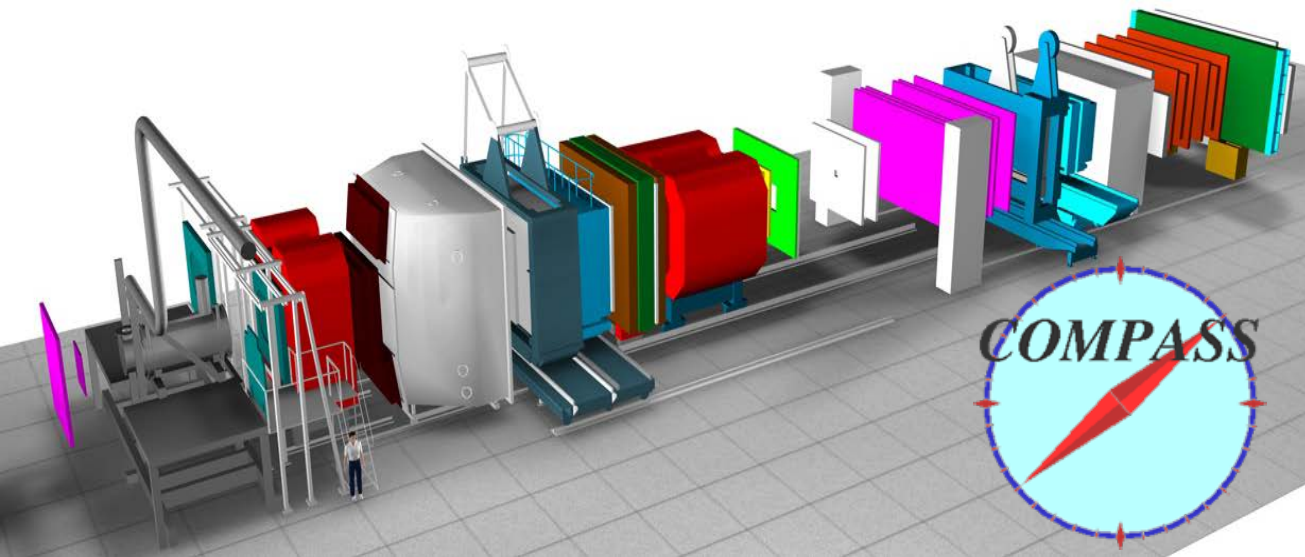
Polarised 27 GeV  $e^-/e^+$   
 Long, trans polarized p, d  
 Missing mass technique,  
 2006-07 recoil detector



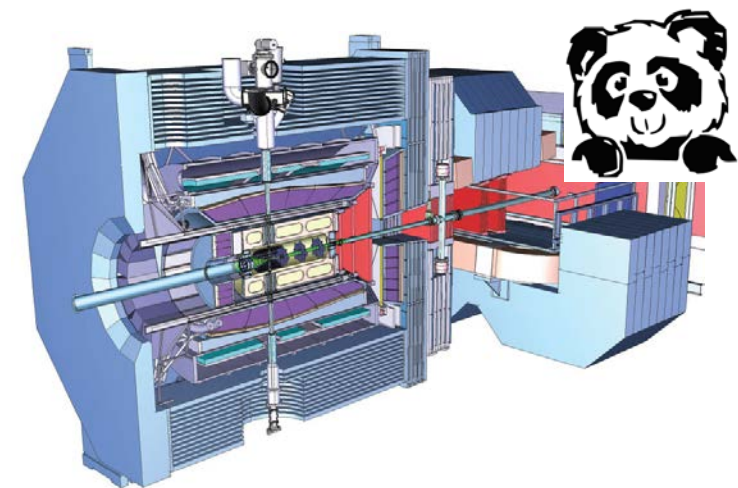
Highly polarization 6 GeV  $e^-$   
 Highest luminosity  
 Long, trans. polarized p, d  
 Missing mass technique



# Present & Future Experiments (limited to this decade ... maybe ...)



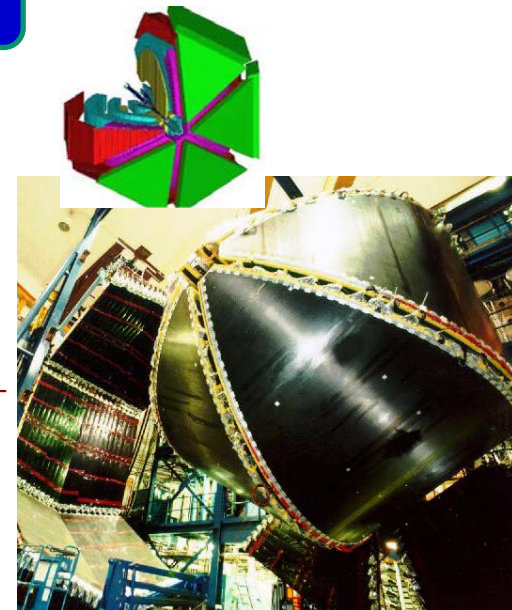
Highly polarised  $160 \text{ GeV } \mu^+/\mu^-$   
Unpolarized p  
(Long, trans. polarized p, d)  
Recoil detection



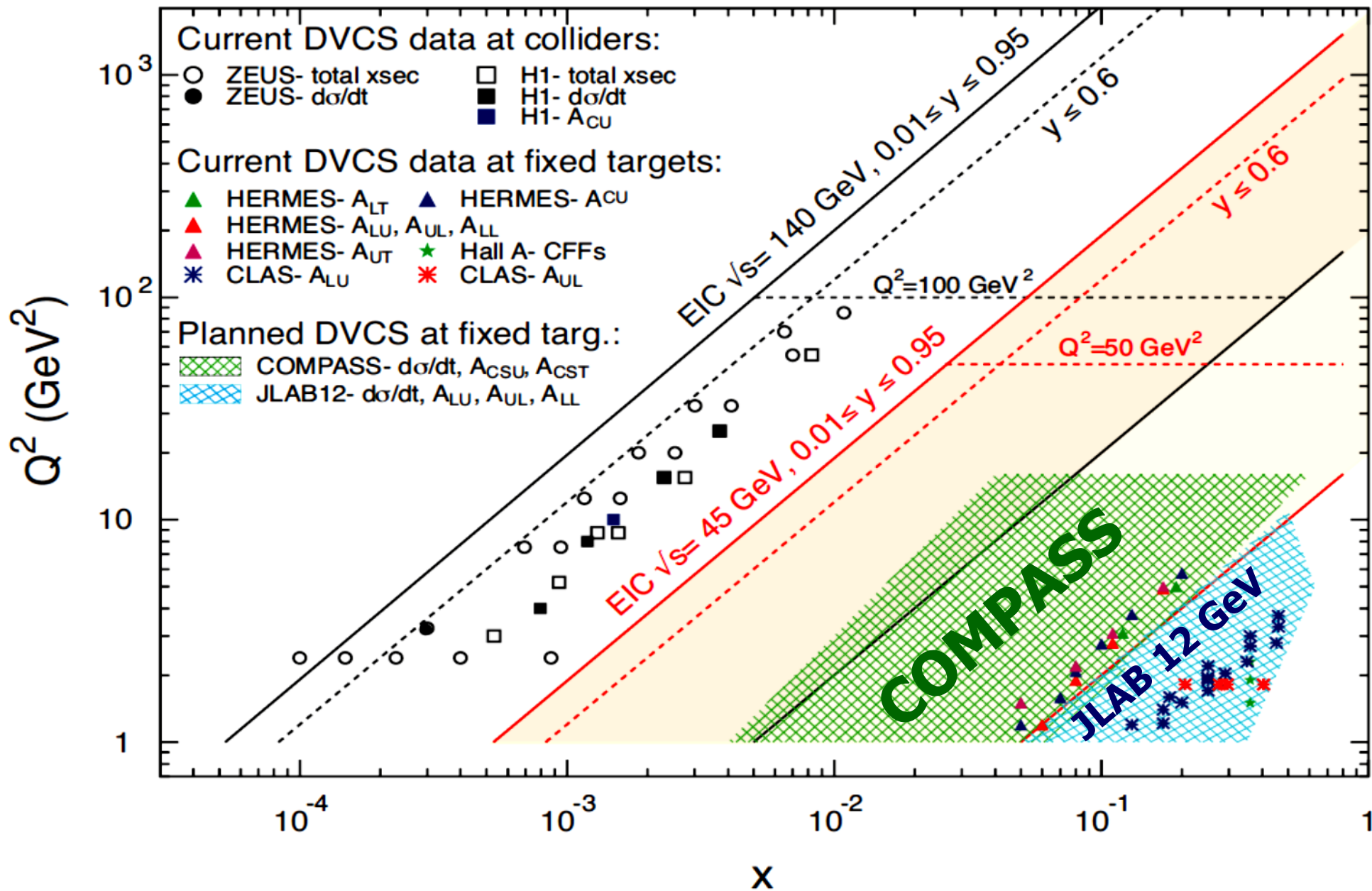
Antiproton beam, fixed target p  
time-like form factors



Highly polarization  $12 \text{ GeV } e^-$   
Highest luminosity  
Long, trans. polarized p, d  
Missing mass technique

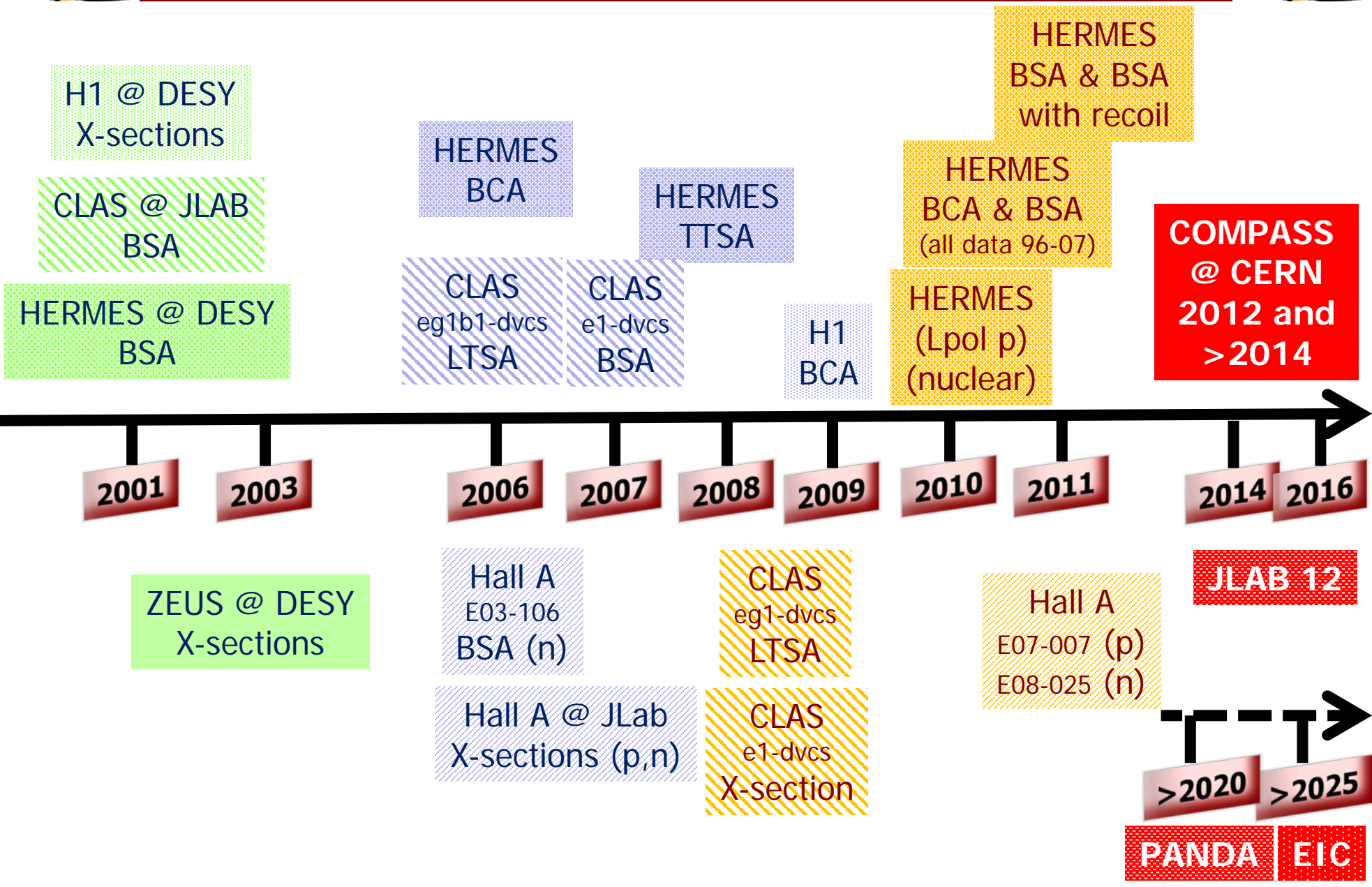


# Kinematic Coverage





# Some DVCS related measurements





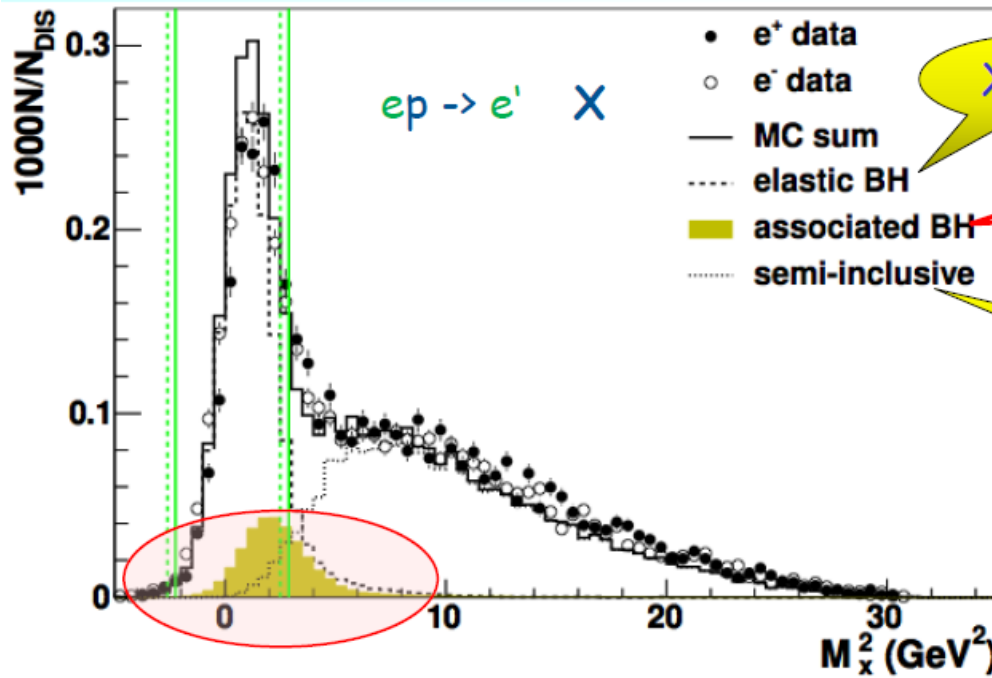
# Exclusivity: $ep \rightarrow e + \gamma + p$

Fixed target mode slow recoil proton

$$M_X^2 = (P_e + P_p - P_{e'} - P_\gamma)^2$$



without recoil detector



$ep \rightarrow e'$  X

- $e^+$  data
- $e^-$  data
- MC sum
- ⋯ elastic BH
- associated BH
- ⋯ semi-inclusive

$X = p$

$\ell p \rightarrow \ell' + \gamma (+p')$

$X = \Delta^+$

$\ell p \rightarrow \ell' + \gamma (+\Delta^+)$

$X = \pi^0 + \dots$

$\ell p \rightarrow \ell' + \gamma (+\gamma + p' + \dots)$   
from  $\pi^0$  decay...

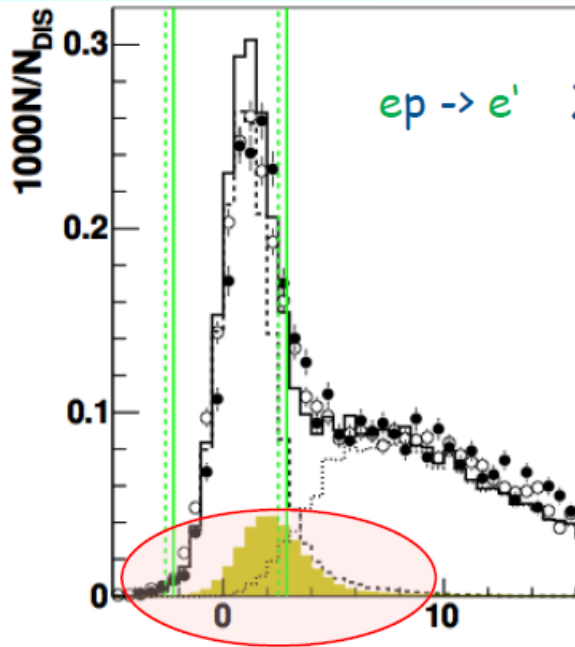
# Exclusivity: $ep \rightarrow e + \gamma + p$

Fixed target mode slow recoil proton

$$M_X^2 = (P_e + P_p - P_{e'} - P_\gamma)^2$$



without recoil detector



- $e^+$  data
- $e^-$  data
- MC sum
- ⋯ elastic BH
- associated BH
- ⋯ semi-inclusive

$X = p$

$\ell p \rightarrow \ell' + \gamma (+p')$

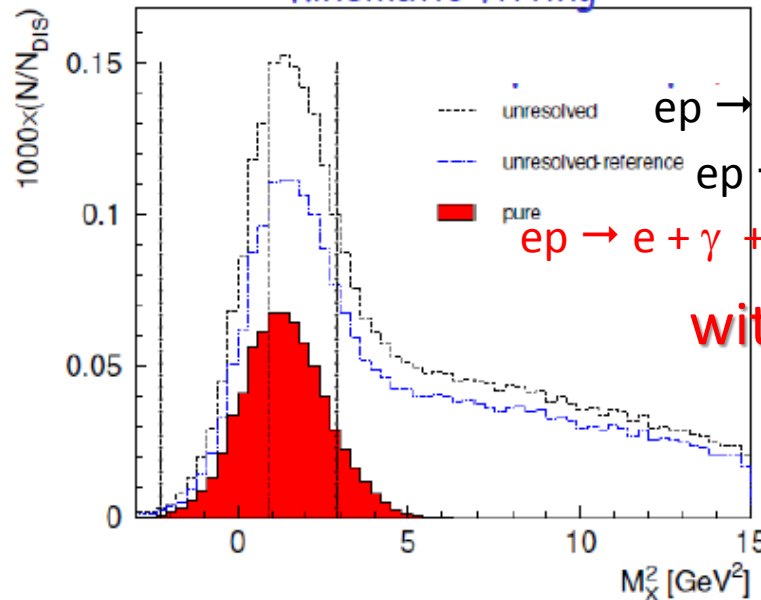
$X = \Delta^+$

$\ell p \rightarrow \ell' + \gamma (+\Delta^+)$

$X = \pi^0 + \dots$

$\ell p \rightarrow \ell' + \gamma (+\gamma + p' + \dots)$   
from  $\pi^0$  decay...

kinematic fitting



unresolved

$ep \rightarrow e + \gamma (+p + \dots)$

unresolved-reference

$ep \rightarrow e + \gamma (+p \text{ in acceptance} + \dots)$

pure

$ep \rightarrow e + \gamma + p$

with recoil detector



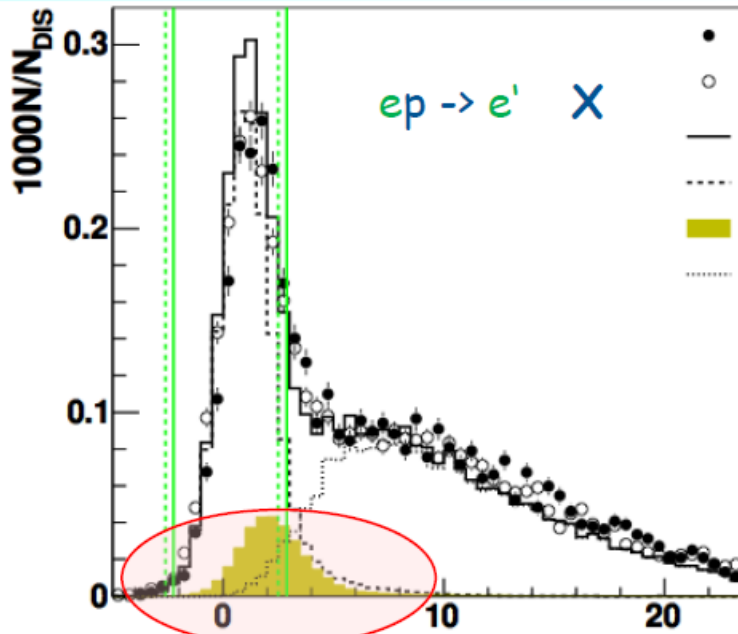
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Fixed target mode slow recoil proton

$$M_X^2 = (P_e + P_p - P_{e'} - P_\gamma)^2$$



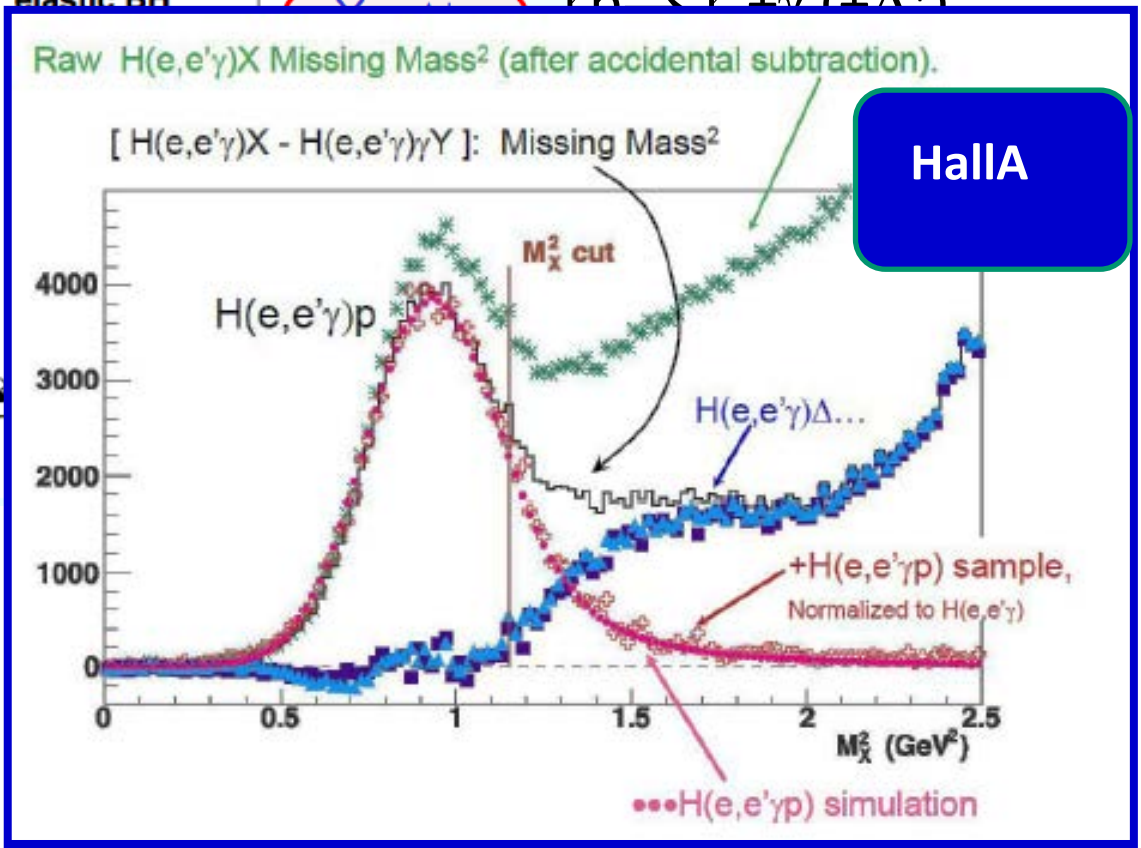
without recoil detector



$X = p$

$\ell p \rightarrow \ell' + \gamma (+p')$

$\ell p \rightarrow \ell' + \gamma (+\Delta^+)$



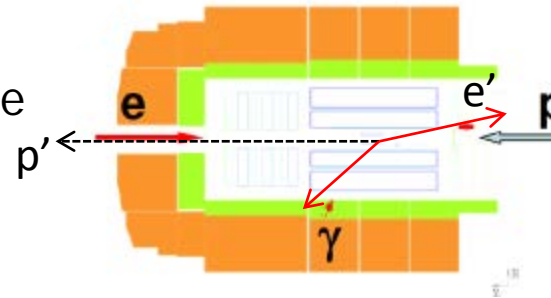
HallA

Background suppression  
~ syst. error

# Exclusivity: $ep \rightarrow e + \gamma + p$

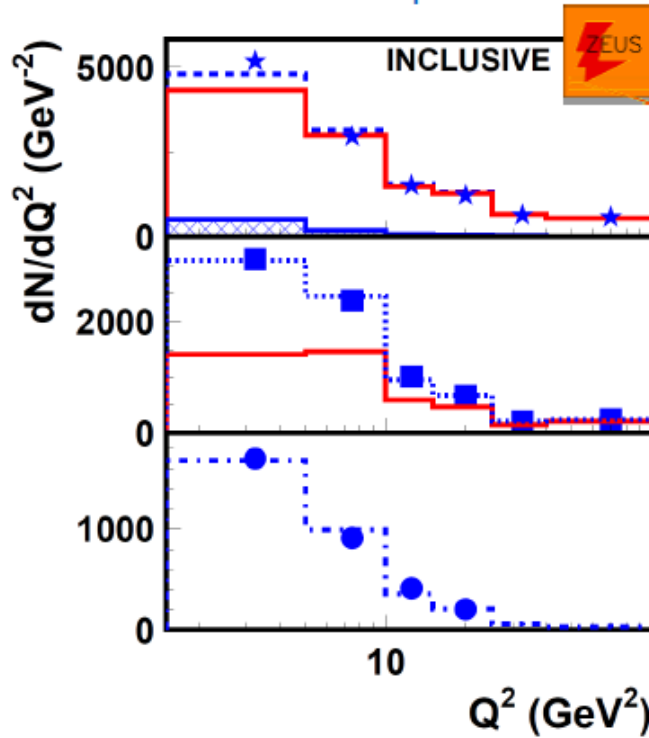
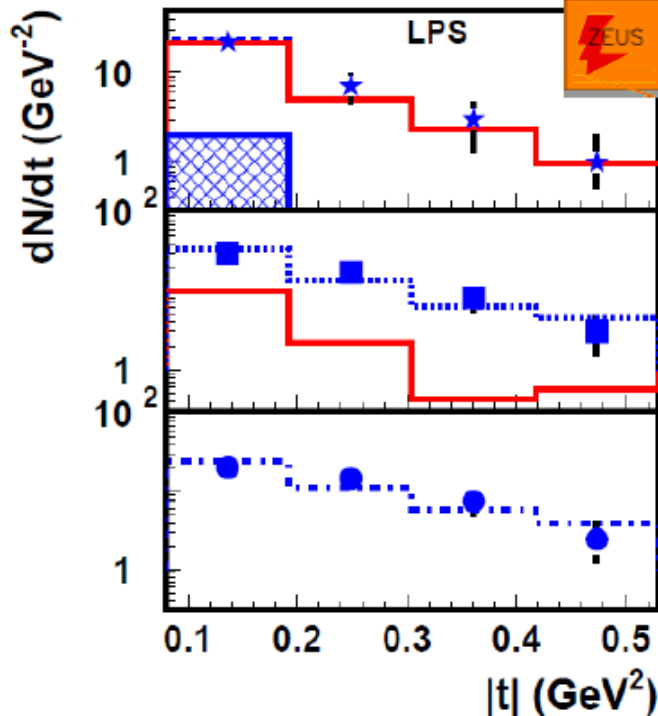
Collider mode e-p forward fast proton

Outgoing proton escapes through the beam pipe  
Tagged in forward proton spectrometer



LPS:  $p$  tagged data sample

full data sample



- ★ e-sample: BH control sample
- ▨ e+e-, J/ψ bg-sample
- ⋯ BH+e<sup>+</sup>e<sup>-</sup>+J/ψ
- BH
- γ-sample: BH+DVCS
- BH
- ⋯ BH+FFS (DVCS)
- (BH+DVCS) - BH
- ⋯ FFS (DVCS)

● Interference term integrated over  $\phi \rightarrow$  pure DVCS cross section

# Selected results and perspectives

**Cross sections measurements:** DVCS and mesons

**Study of the GPD H with DVCS on proton:**

Beam Spin Asymmetry:	HallA – CLAS - HERMES
Beam Charge Asymmetry:	HERMES – H1 – COMPASS
Cross section difference and sum:	HallA – CLAS – COMPASS

**Hunting GPD E:**

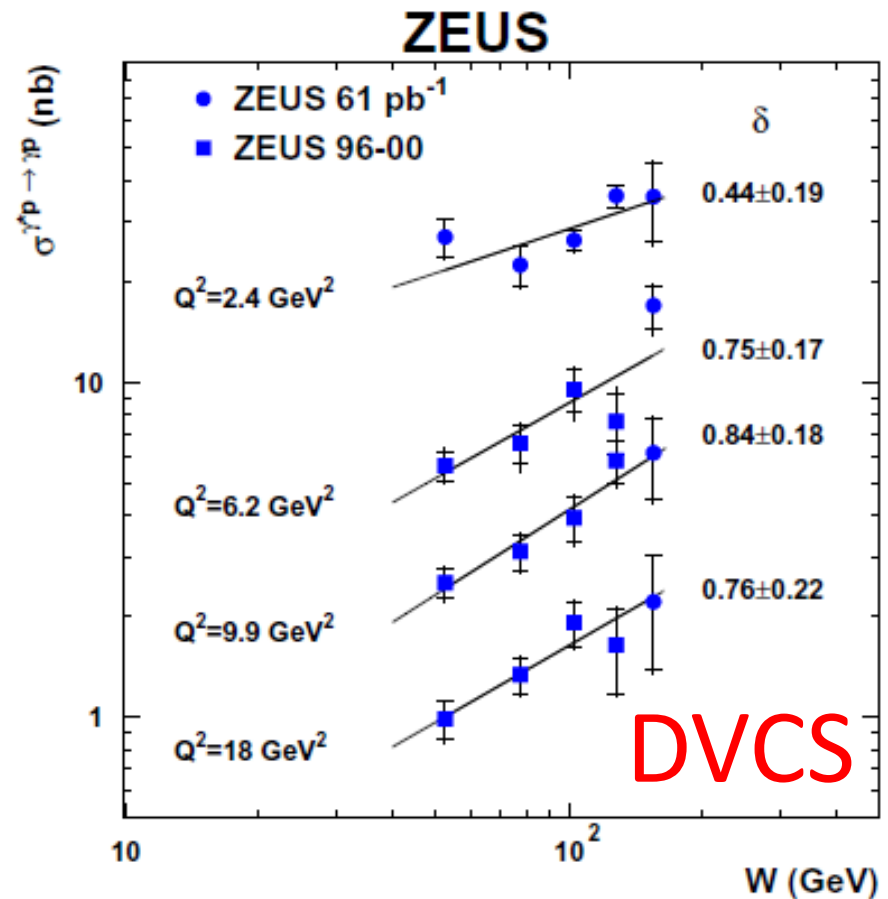
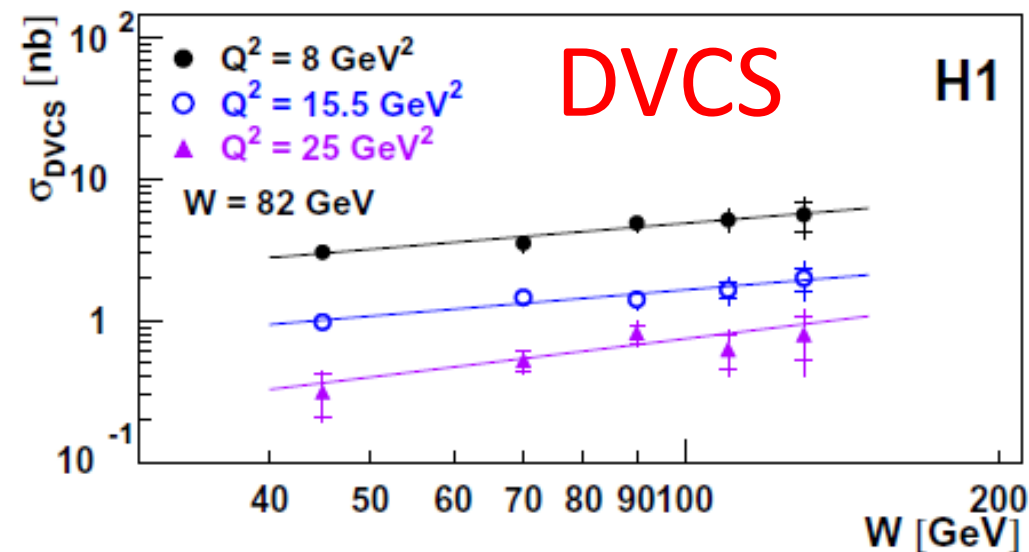
Beam Spin cross section on the neutron:	HallA
Transverse pol. Target Asymmetry on proton:	HERMES

→ 'Holy grail' for OAM

# Cross sections and W dependence

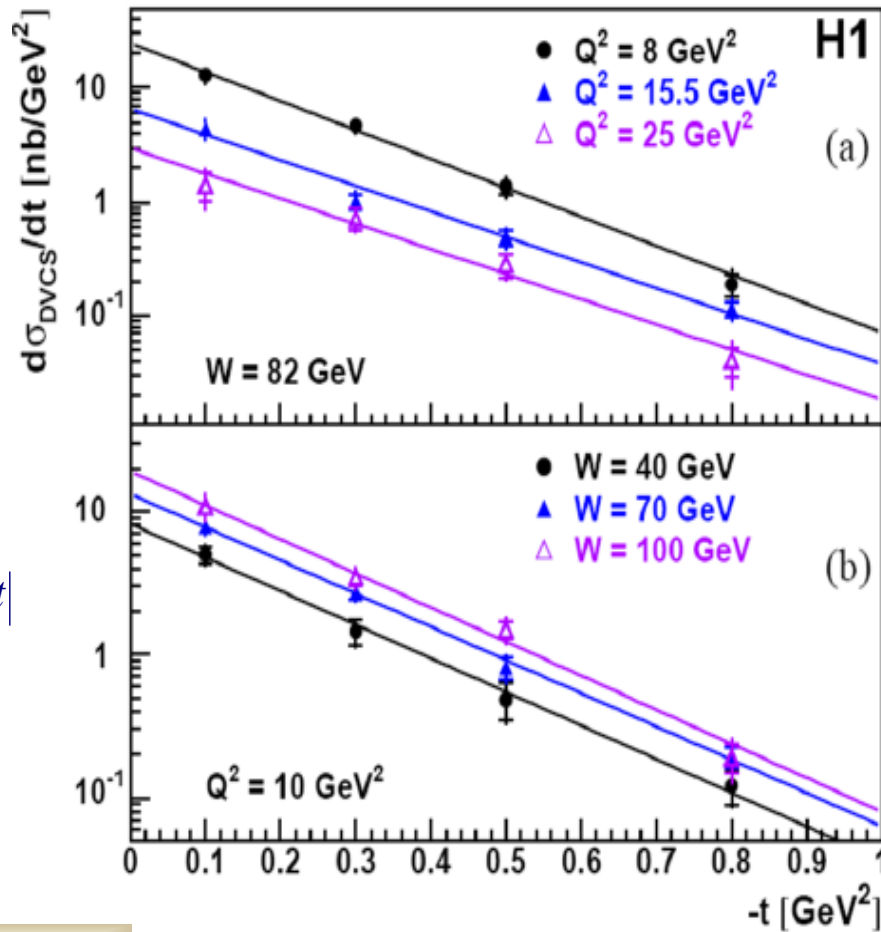
Are we in the hard regime ?

$$\sigma(W) \propto W^\delta$$

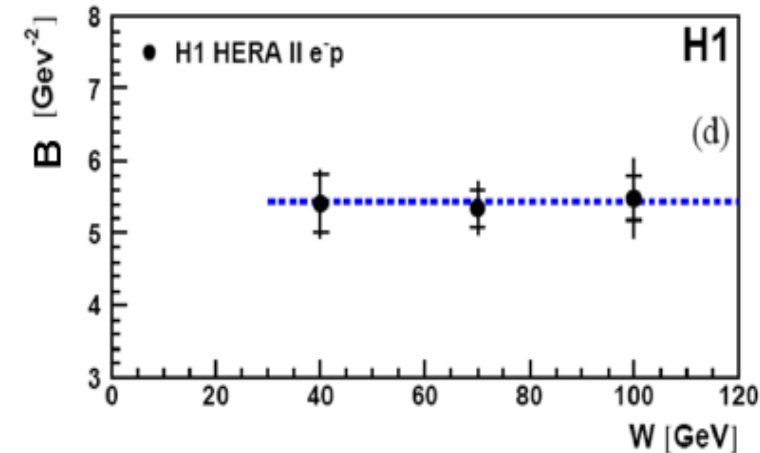
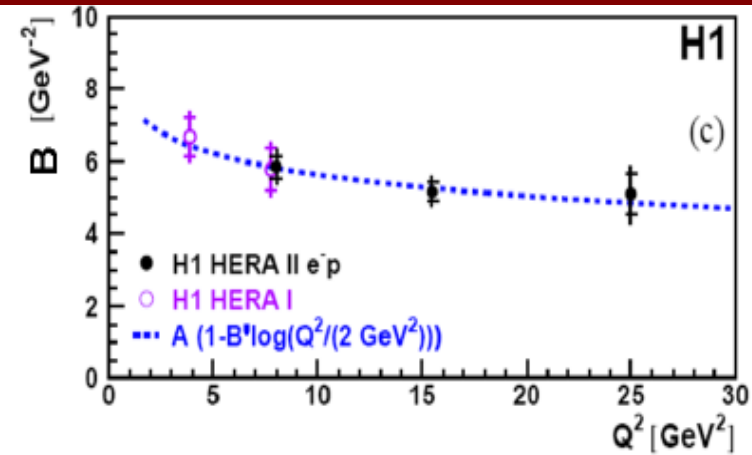


$\delta$  increases from soft ( $\sim 0.2$ ) to hard ( $\sim 0.8$ )

# Cross sections and t dependence



$$\frac{d\sigma}{d|t|} \propto e^{-B|t|}$$



$$\langle r_{\perp}^2(x_B) \rangle \sim 2B(x_B)$$

Almost no evolution as a function of W

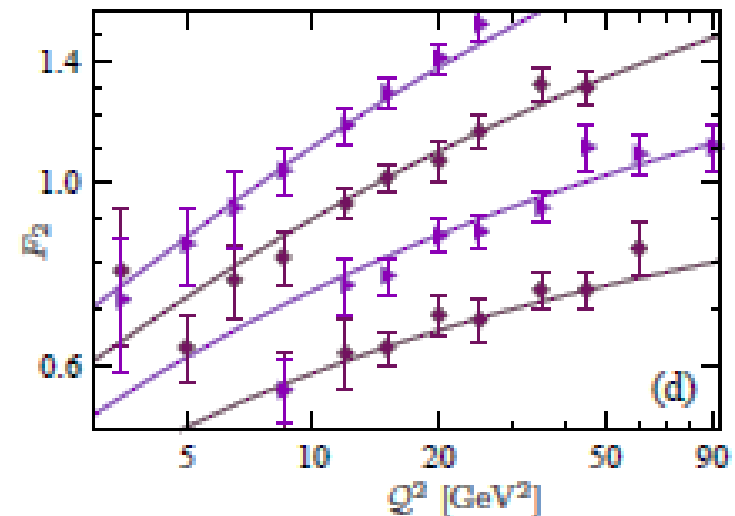
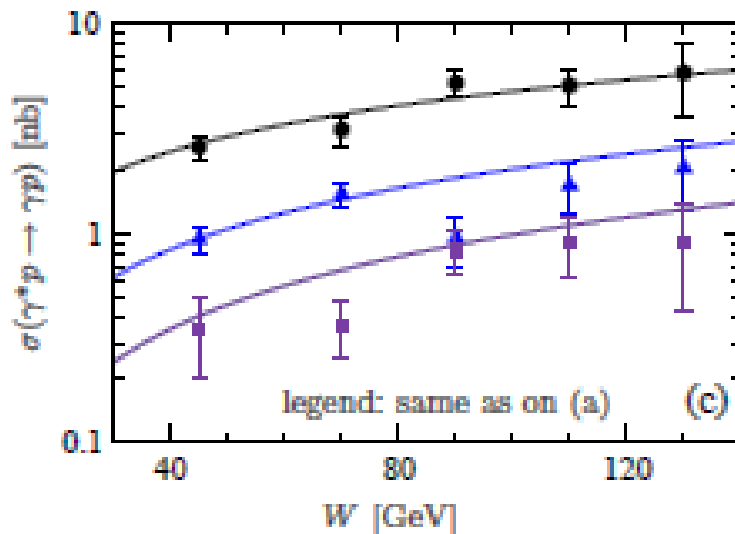
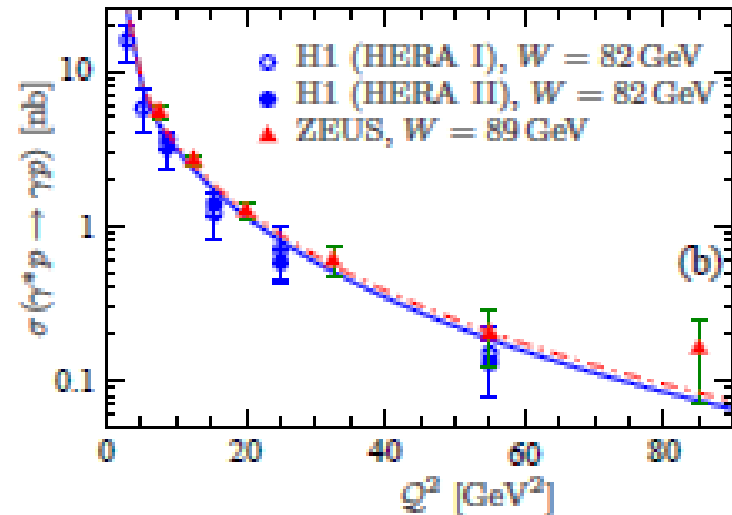
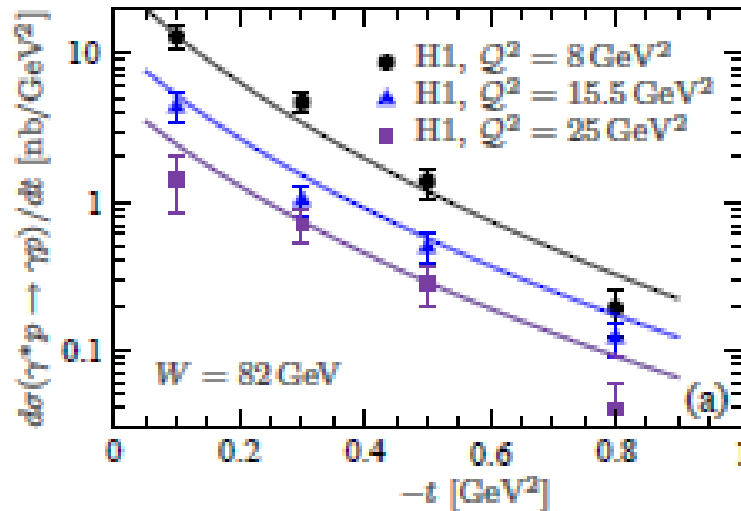
$$B = 5.45 \pm 0.19 \pm 0.34 \text{ GeV}^{-2}$$

at  $\langle Q^2 \rangle = 8 \text{ GeV}^2$  and  $\langle x \rangle = 1.2 \cdot 10^{-3}$

$$\sqrt{\langle r_{\perp}^2 \rangle} = 0.65 \pm 0.02 \text{ fm}$$

**b decreases from soft ( $\sim 10 \text{ GeV}^{-2}$ ) to hard ( $\sim 5 \text{ GeV}^{-2}$ )**

# Predictions for DVCS from KM model



**KM10:** Kumericki and Mueller NPB (2010) 841; arXiv:0904.0458  
 one of the most general parameterization of GPDs based on their mathematic  
 Properties fit to the DVCS data and DIS



# COMPASS: Beam Charge & Spin Difference $S_{CS,U}$ - Transverse imaging

$$S_{CS,U} = d\sigma^{+\leftarrow} + d\sigma^{-\rightarrow} = 2 \left( d\sigma^{BH} + d\sigma_{unpol}^{DVCS} + e_{\mu} P_{\mu} a^{BH} \text{Im} T^{DVCS} \right)$$

- Using  $S_{CS,U}$
- Integrating over  $\phi$
- Subtracting BH

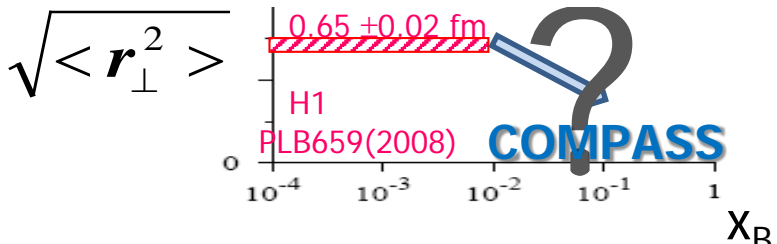
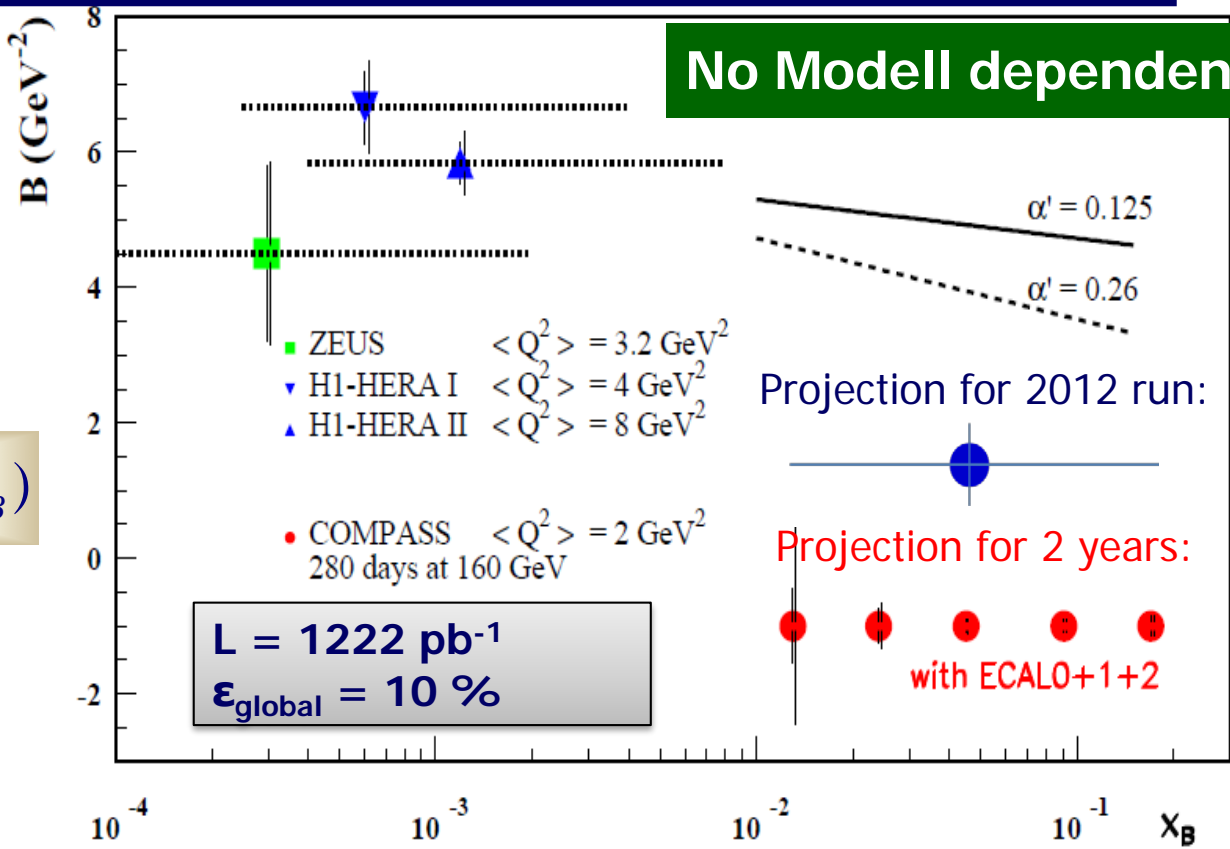
$$\frac{d\sigma}{d|t|} \propto e^{-B|t|}$$

$$\langle r_{\perp}^2(x_B) \rangle \sim 2B(x_B)$$

- Ansatz at small  $x_B$ :  
( $x \sim x_B$ )

$$B(x_B) = b_0 + 2\alpha' \ln \frac{x_0}{x_B}$$

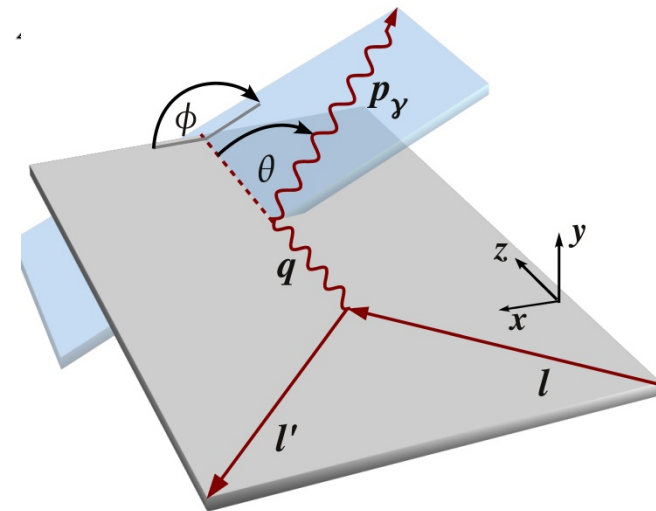
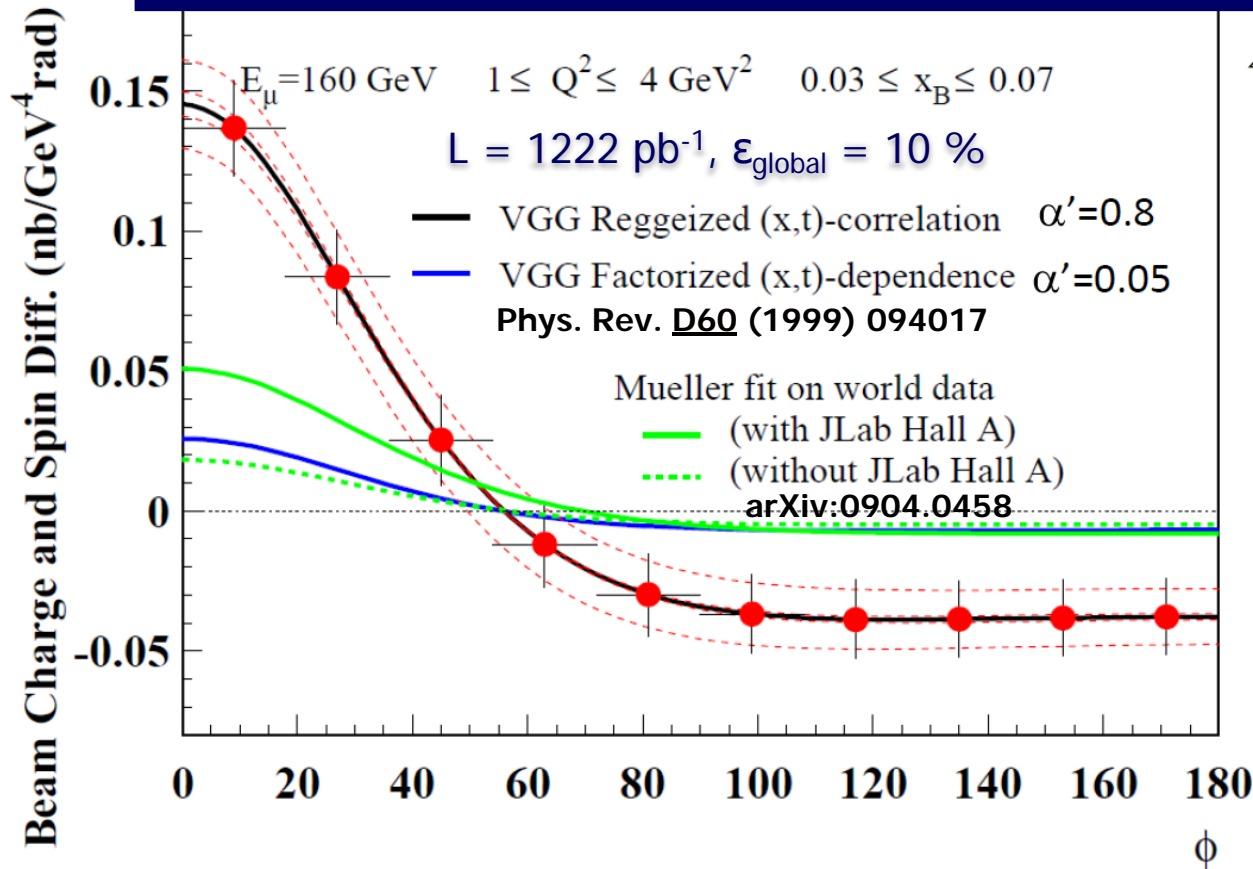
measure  $\alpha'$  with accuracy  $> 2.5\sigma$   
for any  $\alpha' > 0.125$



$x_B$

# Beam Charge & Spin Difference $\mathcal{D}_{CS,U}$

$$\mathcal{D}_{CS,U} = d\sigma^{+\leftarrow} - d\sigma^{-\rightarrow} = 2 \left( P_{\mu} d\sigma_{pol}^{DVCS} + e_{\mu} a^{BH} \text{Re} T^{DVCS} \right)$$



Gives access to:  
 $\text{Re } F_1 \mathcal{H}$

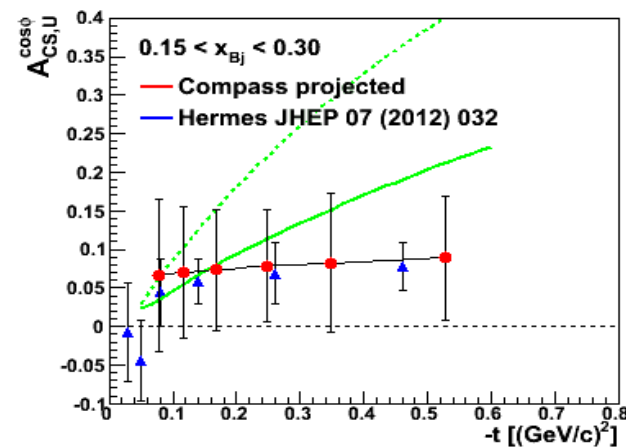
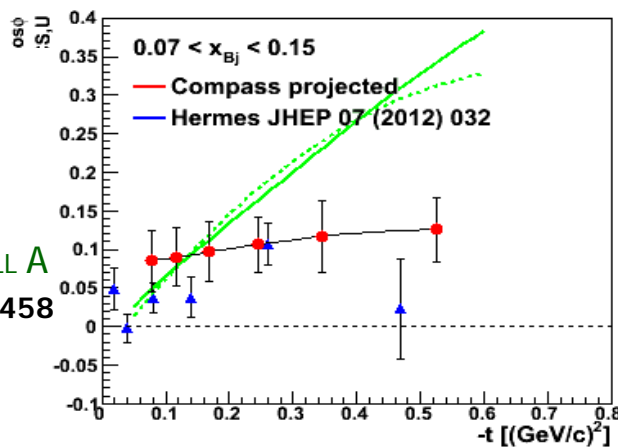
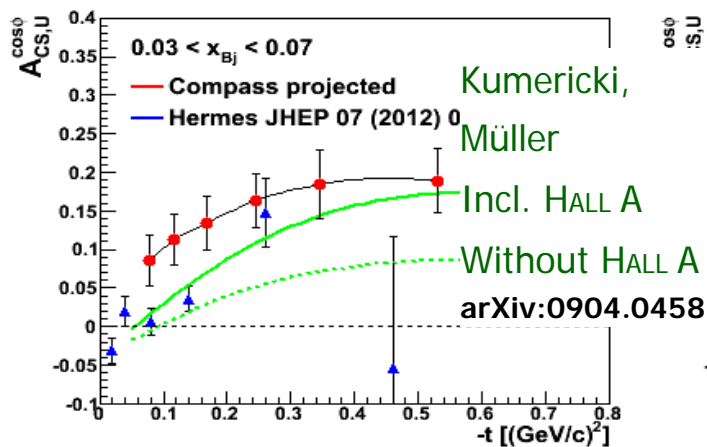
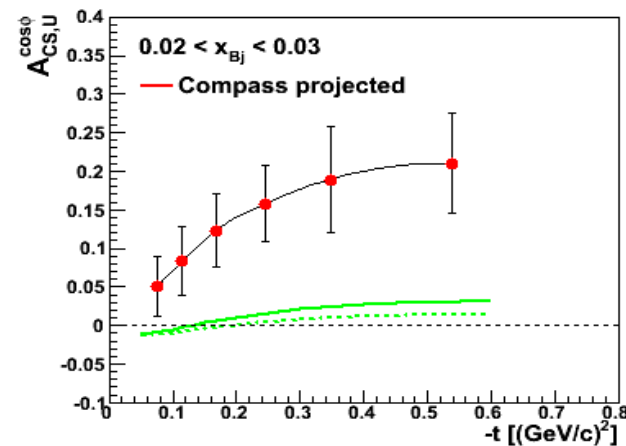
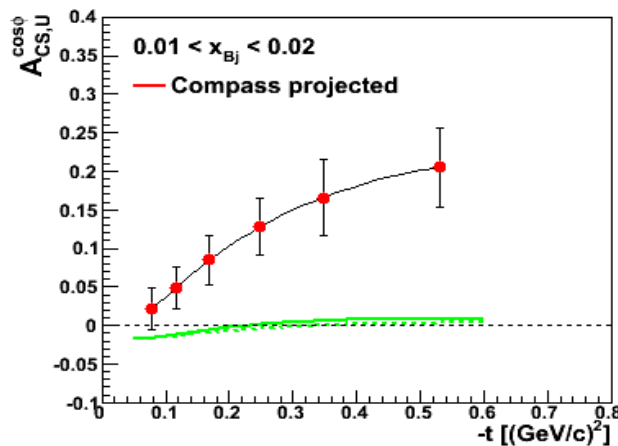
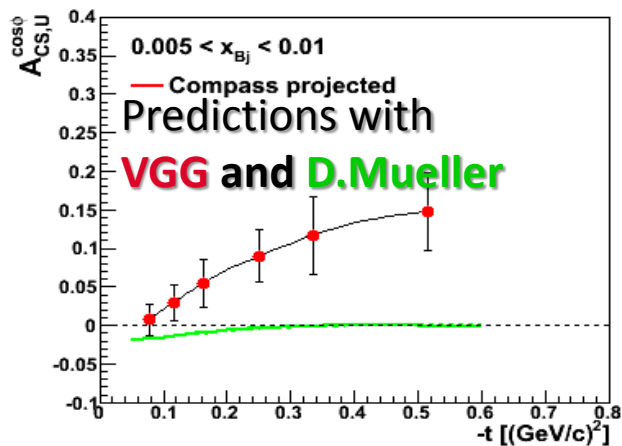
- Need to control detector acceptance and beam flux with high precision
- Error band includes a 3% systematic uncertainty between  $\mu^+$  and  $\mu^-$
- Use inclusive events and BH for check

# Beam Charge & Spin Asymmetry $\mathcal{D}_{CS,U} / S_{CS,U}$

$$\begin{aligned} \text{BCSA} &= \mathcal{D}_{CS,U} / S_{CS,U} \\ &= A_0 + A_{CS,U} \cos \phi + A_2 \cos 2\phi \end{aligned}$$

→ Measurement of  $\text{Re}(F_1 H)$

$\text{Re}(F_1 H) > 0$  @ H1  
 $< 0$  @ HERMES  
 Node? Where in  $x_{Bj}$ ? → COMPASS



# DVCS interference on the proton

- $Im$  DVCS with BSA or Beam Spin difference
- $Re$  DVCS with BCA or Beam Charge difference
  
- mainly constrains on the GPD H

# Beam Spin Sum and Difference - HallA

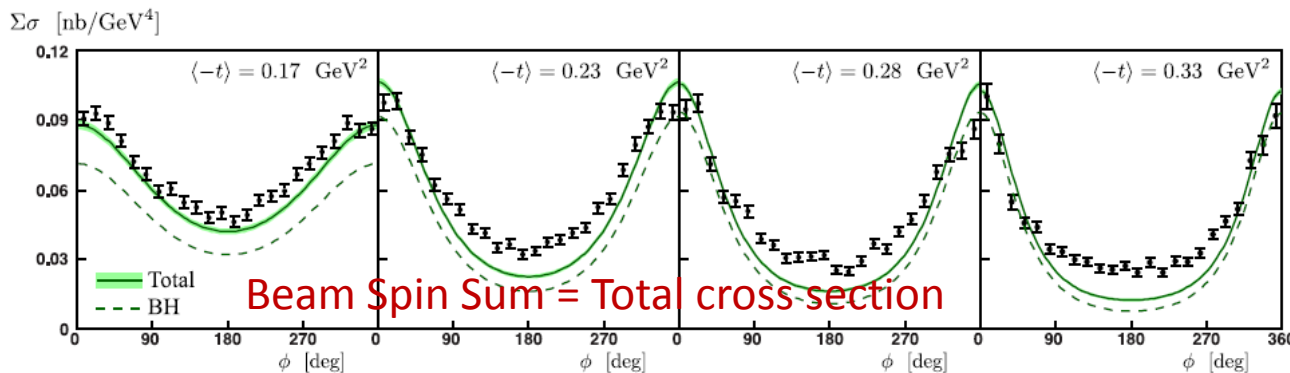
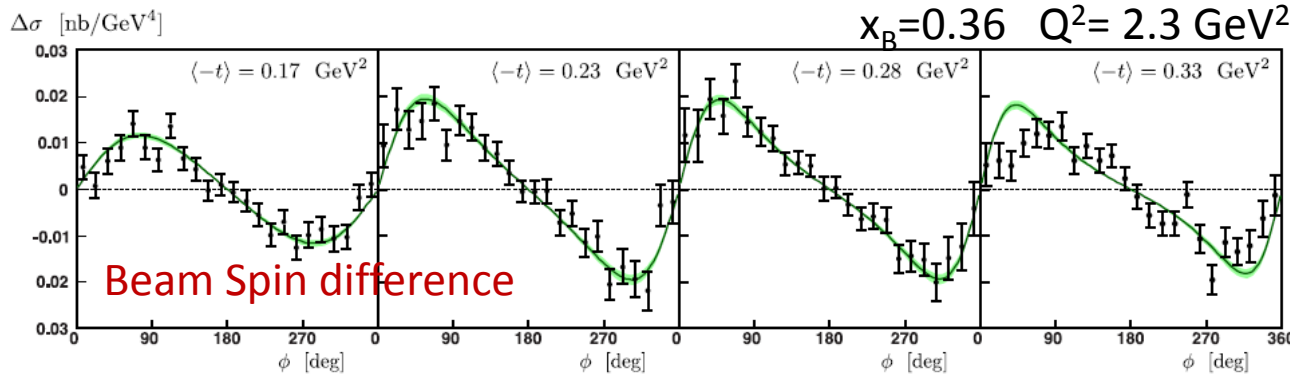
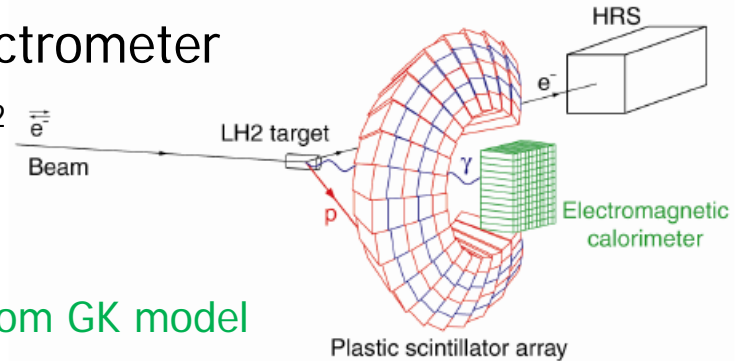
E00-110 pioneer experiment with magnetic spectrometer

3 measurements:  $x_B=0.36$   $Q^2= 1.5, 1.9, 2.3 \text{ GeV}^2$

$$\vec{e} p \rightarrow e \gamma p$$

Data: Munoz et al. PRL97, 262002 (2006)

Model: Kroll, Moutarde, Sabatié, EPJC73 (2013) with GPDs from GK model



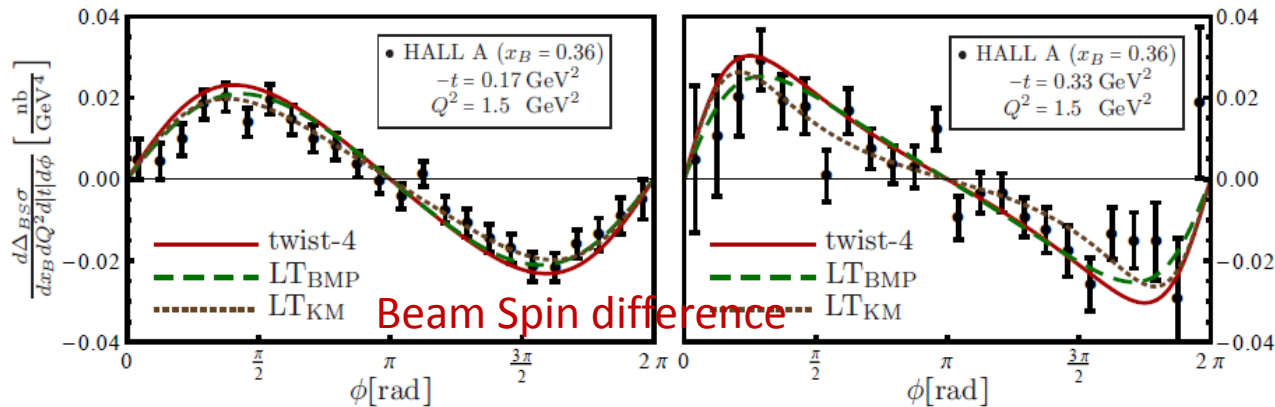
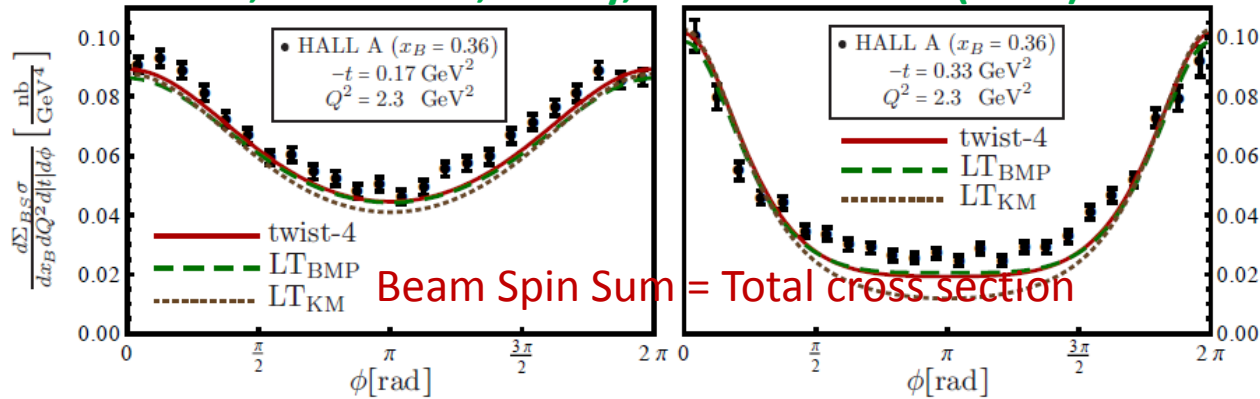
News:

- Re-analysis of the data (MC, RC, normalisation/DIS)
- 2010: run E07-007 Rosenbluth-like DVCS<sup>2</sup>/Interpolation
- 2014: HallA with 11 GeV
- 2018: HallC with 11 GeV

# Beam Spin Sum and Difference - HallA

Data: Munoz et al. PRL97, 262002 (2006)

Model: Braun, Manashov, Pirnay, Mueller PRD79 (2014)



GK12 model evaluated  
with KM and BMP  
prescription

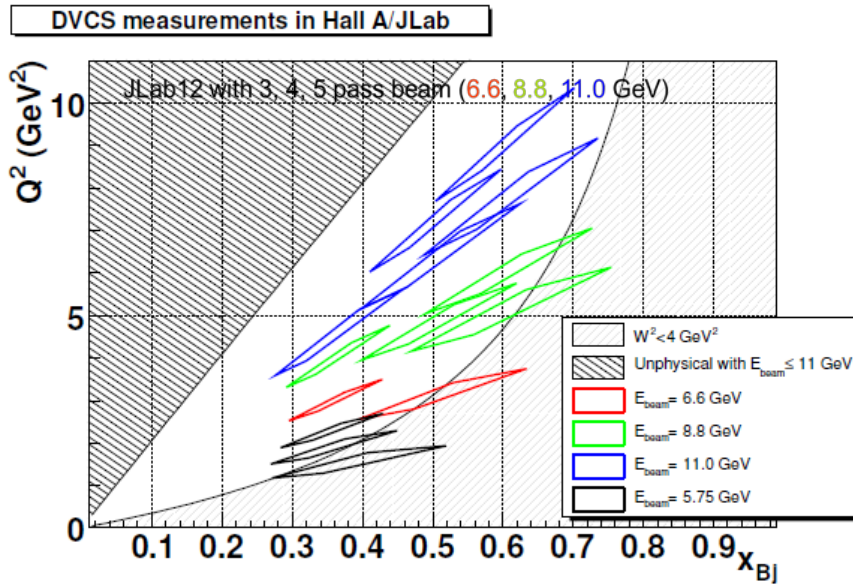
including  
kinematic corrections  
(finite-t, target mass corr.)

Do we understand Hall A data?

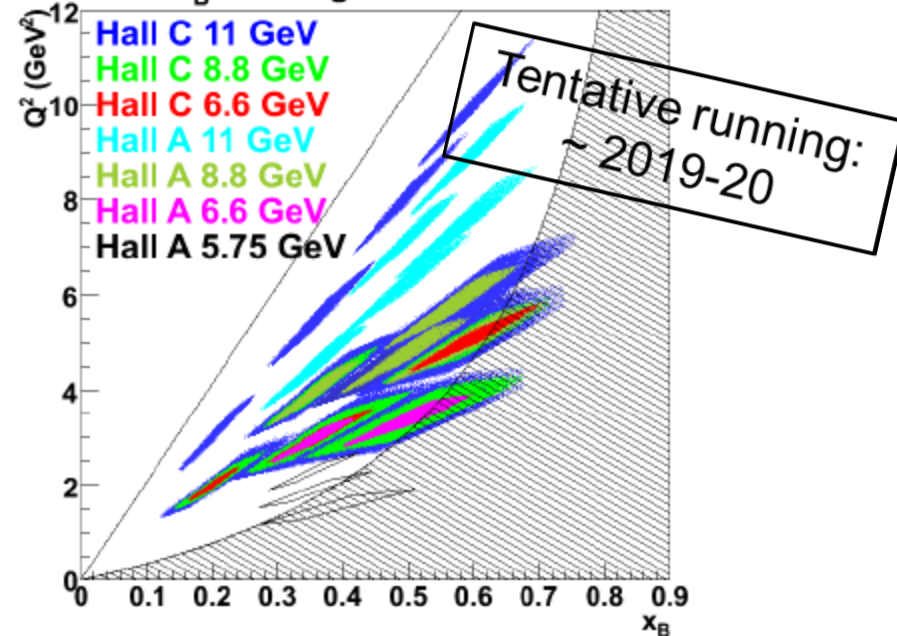
# JLAB Hall A & Hall C - future

with magnetic spectrometer + Calorimeter

## E12-06-114: DVCS at 11 GeV in Hall A



## $Q^2$ vs $x_B$ coverage in Halls A and C



## E12-13-010: DVCS at 11 GeV in Hall C

- Energy separation of the DVCS cross section
- Higher  $Q^2$ : measurement of higher twist contributions
- Low- $x_B$  extension (thanks to sweeping magnet)

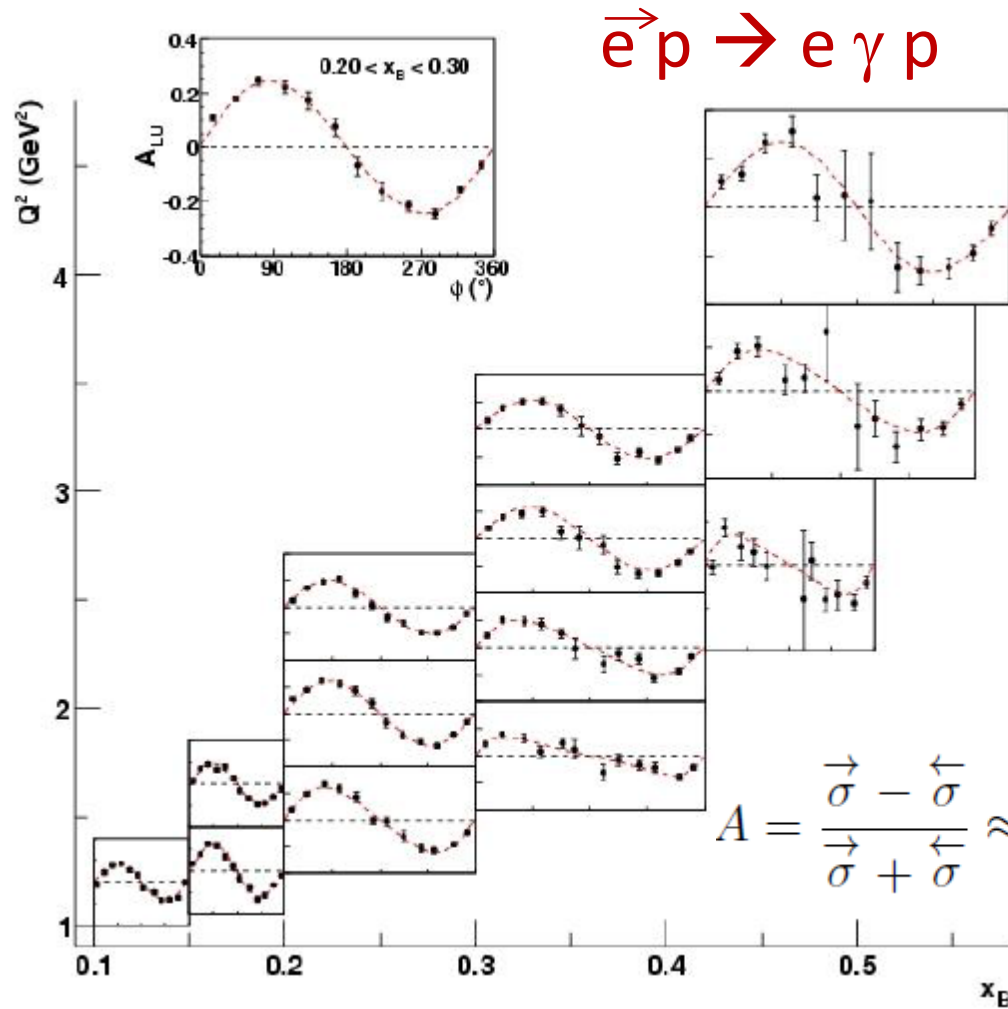
**Need a new challenging Calorimeter**

- Absolute cross-section measurements
- Test of scaling:  $Q^2$  dependence of  $d\sigma$  at fixed  $x_{Bj}$
- Increased kinematical coverage

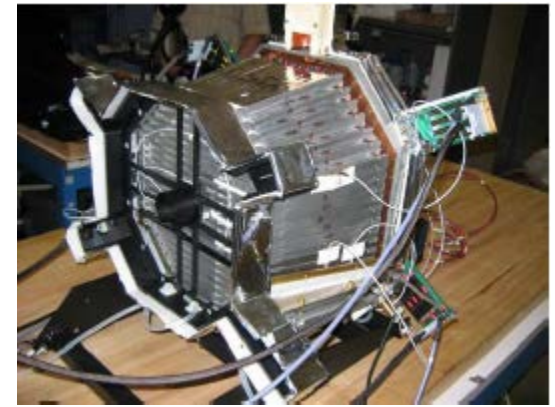
Start on Feb 2014,  
for 1 year of data taking

# CLAS: BSA in a large kinematic domain

Part 1 of the E01-113 or e1-DVCS exp



CLAS + Inner Calorimeter  
Solenoid magnet



No simple  
interpretation of  $\alpha$

Data: Girod et al. PRL100, 162002 (2008)

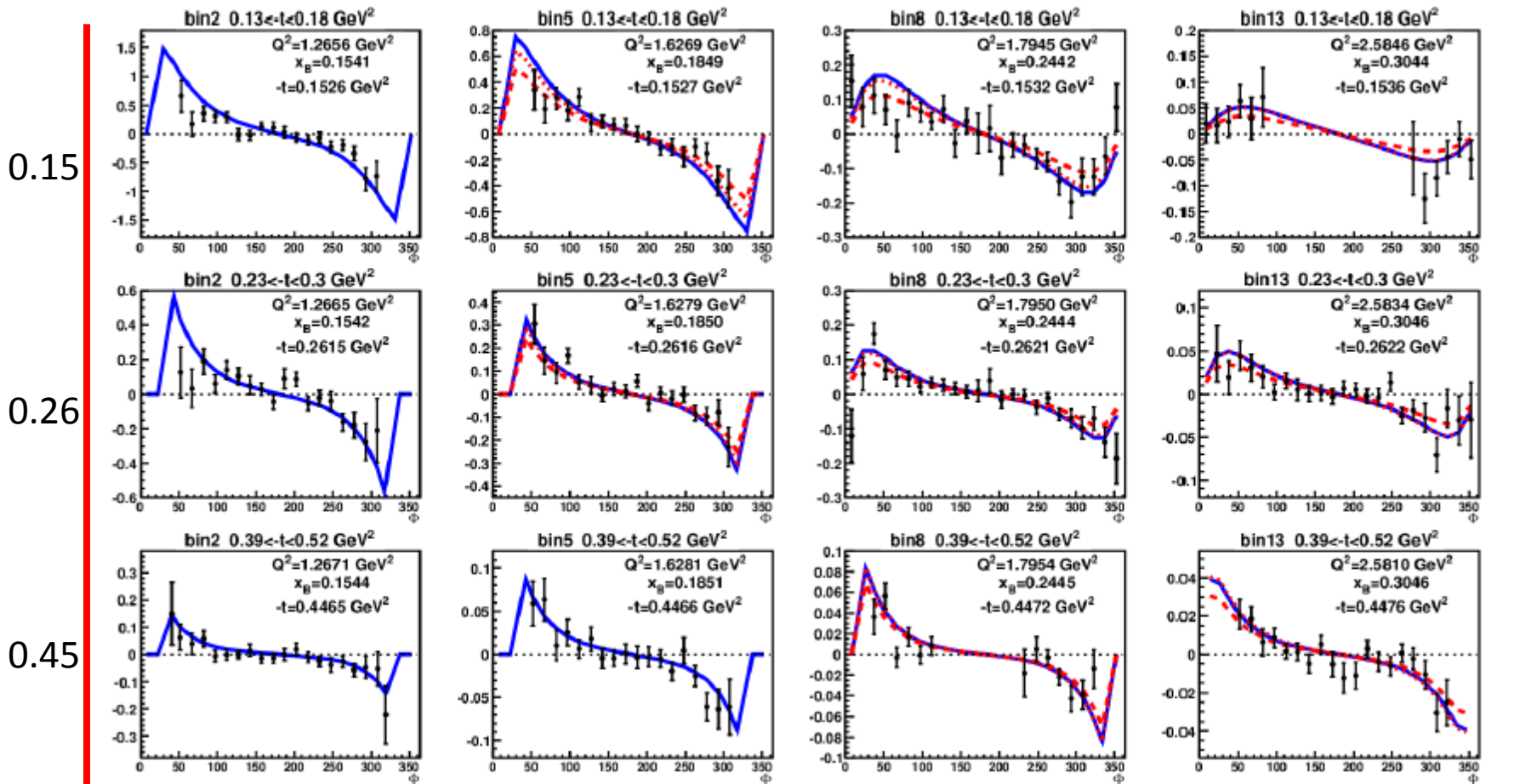


# Beam Spin Difference - CLAS

Data from: H.S. Jo

— VGG  
 — KM10a (without Hall A)  
 ···· KM10b

PRELIMINARY



KM10ab (fit) : Kumericki, Müller, Nucl.Phys. B841 1 (2010)

VGG (only H) : Goeke, Polyakov, Vanderhaeghen, Prog.Part.Nucl.Phys. 47 401 (2001)

$|t|$   
(GeV<sup>2</sup>)

1.27  
0.15

1.63  
0.18

1.80  
0.24

2.58  
0.30

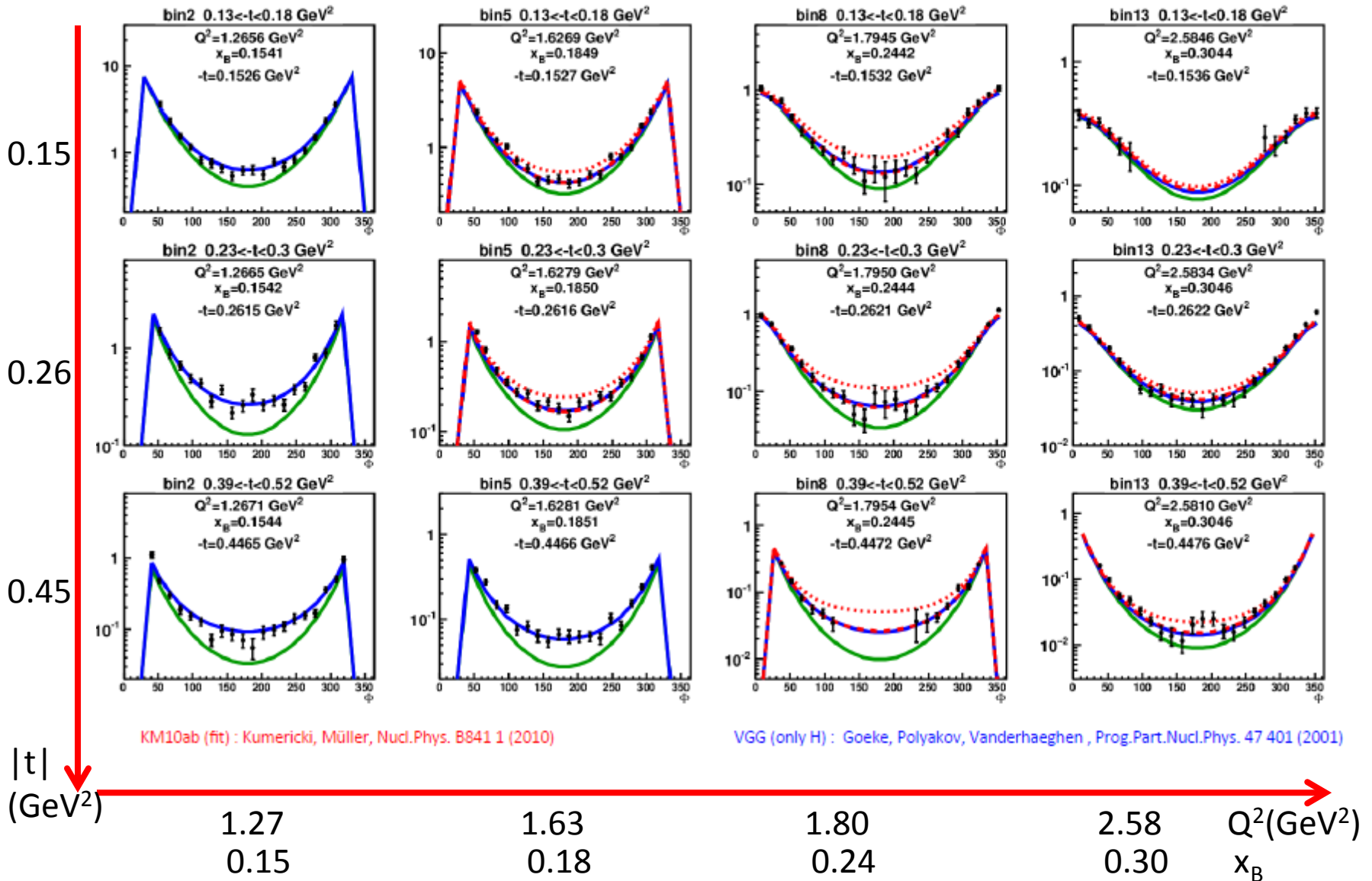
$Q^2$ (GeV<sup>2</sup>)  
 $x_B$

# Beam Spin Sum - CLAS

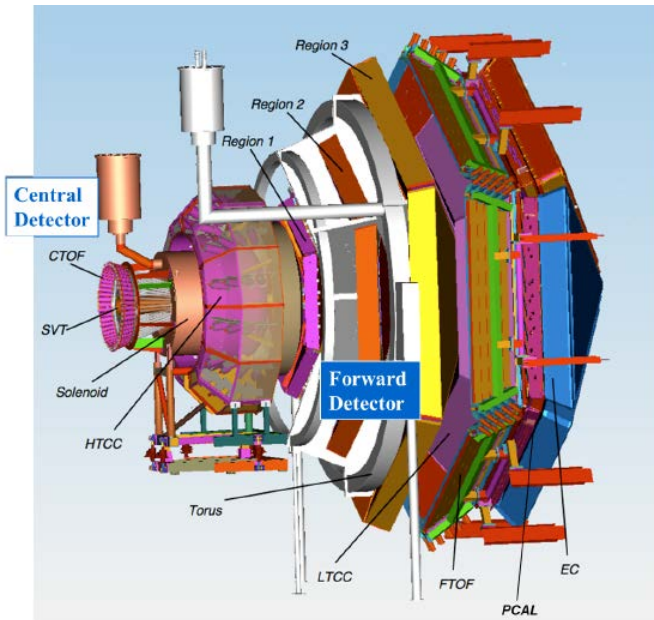
Data from: H.S. Jo

- VGG
- KM10a (without Hall A)
- BH
- ⋯ KM10b

PRELIMINARY



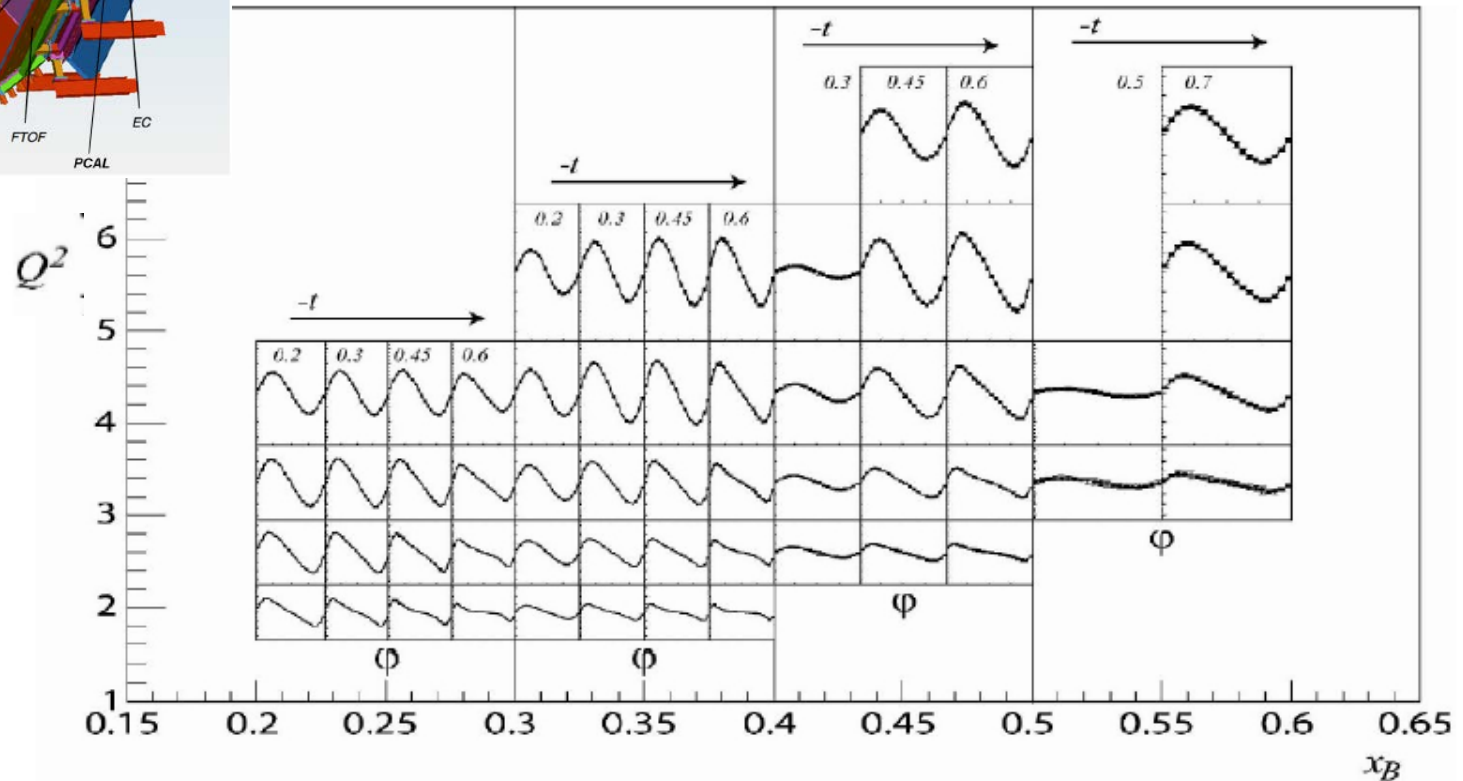
# Future - CLAS12



E12-06-119

Strong effort in Detector upgrades

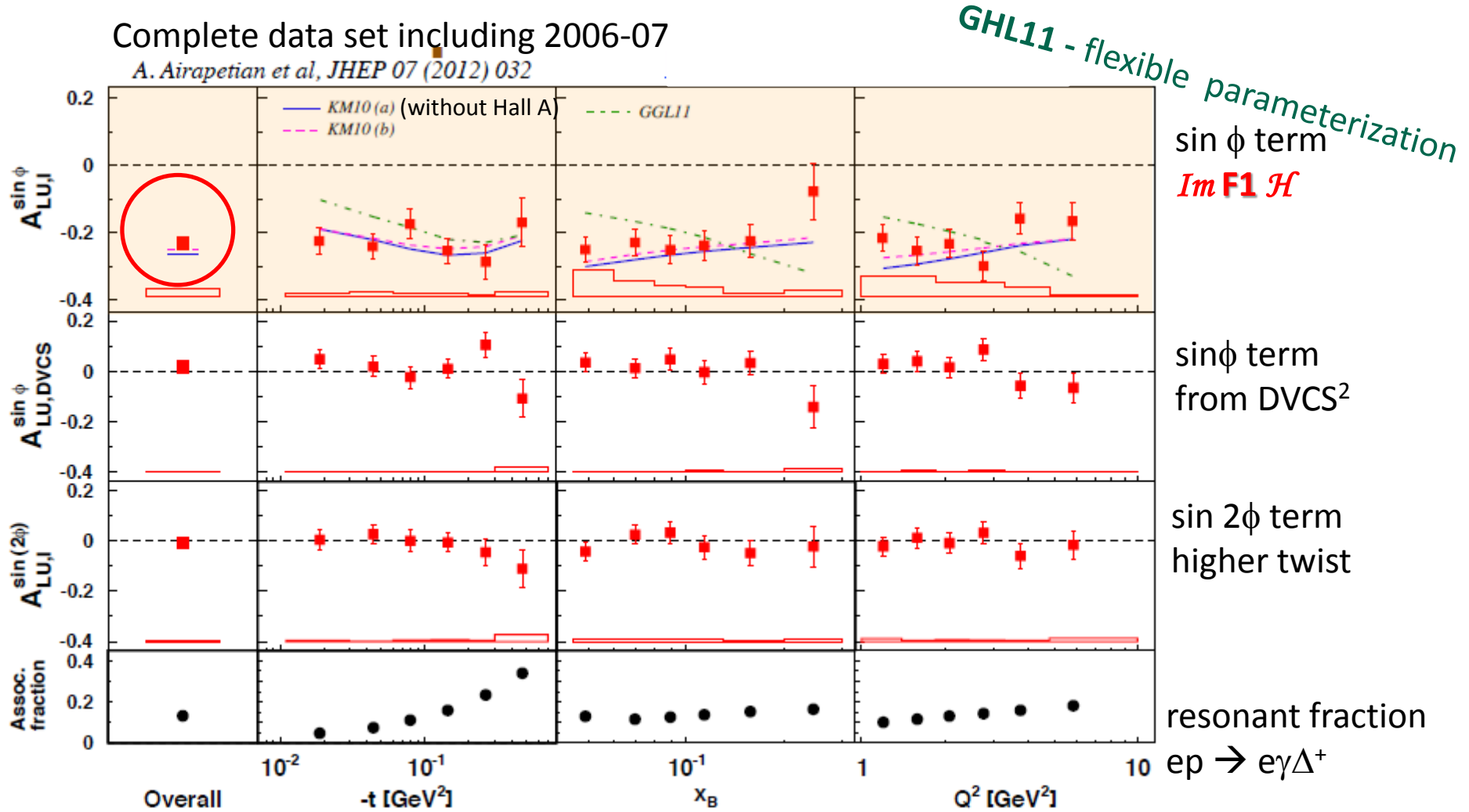
LH<sub>2</sub> Target and Long. Pol. Target  
in 2016



# BSA - HERMES

Complete data set including 2006-07

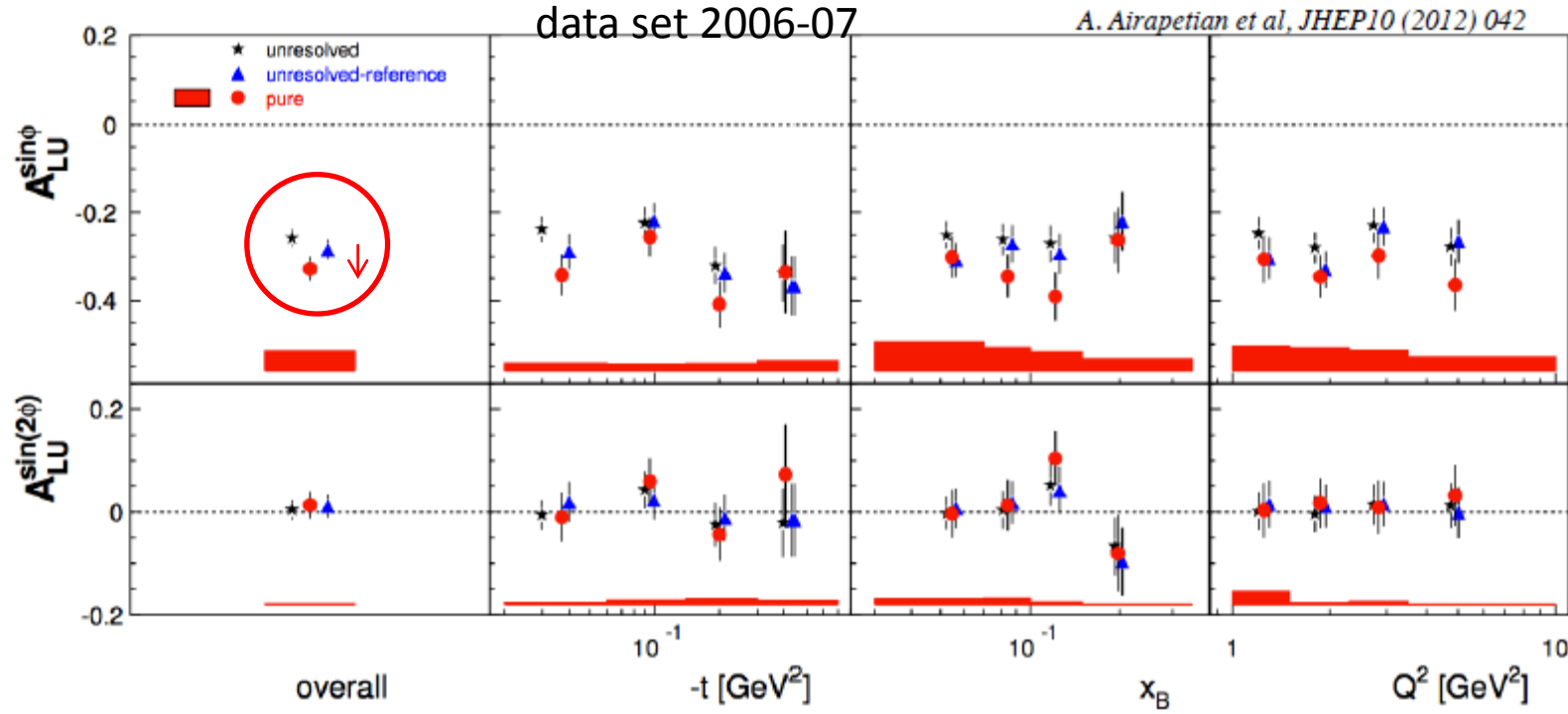
A. Airapetian et al, JHEP 07 (2012) 032



Kumericki, Müller Nucl. Phys. B841 (2010)

Goldstein, Hernandez, Liuti Phys. Rev. D84 (20101)

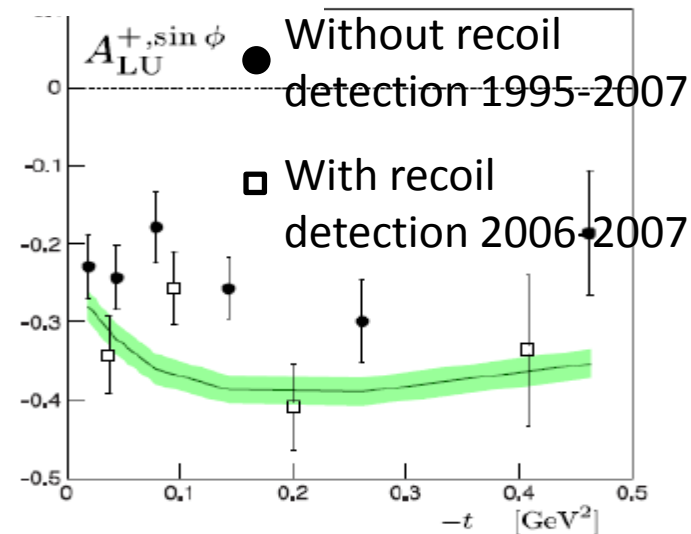
# BSA with recoil detector - HERMES



High-purity event selection shows that there is only a small influence on the extracted BSA amplitude from events involving a  $\Delta$  particle (associated DVCS)

The leading asymmetry has increased by  $0.054 \pm 0.016$   
 Mainly dilution due to associated DVCS

Model: Kroll, Moutarde, Sabatié, EPJC73 (2013) with GPDs from GK model

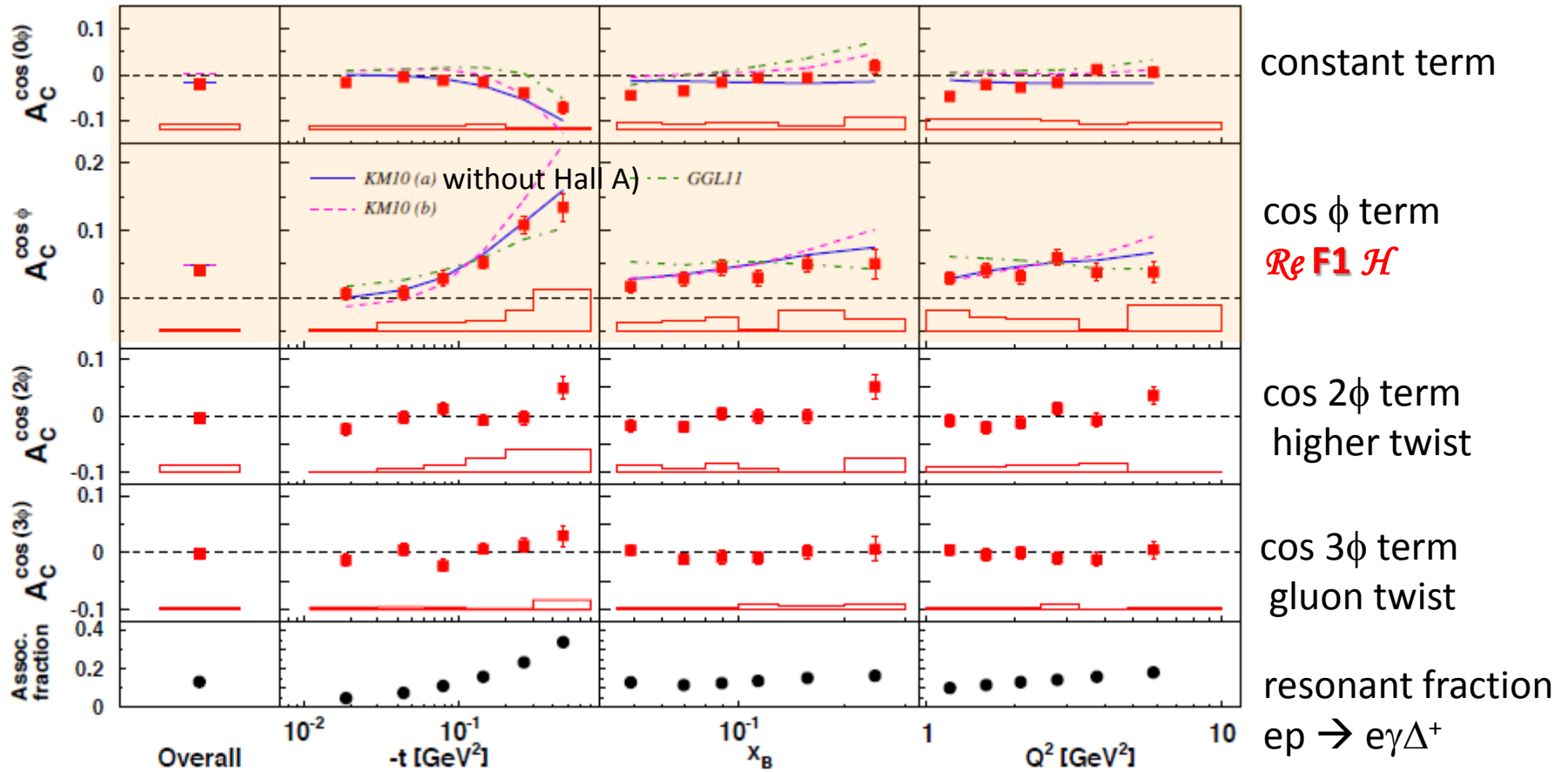


# BCA - HERMES

Complete data set including 2006-07 without recoil detection

A. Airapetian et al, JHEP 07 (2012) 032

<http://arxiv.org/abs/1203.6287>

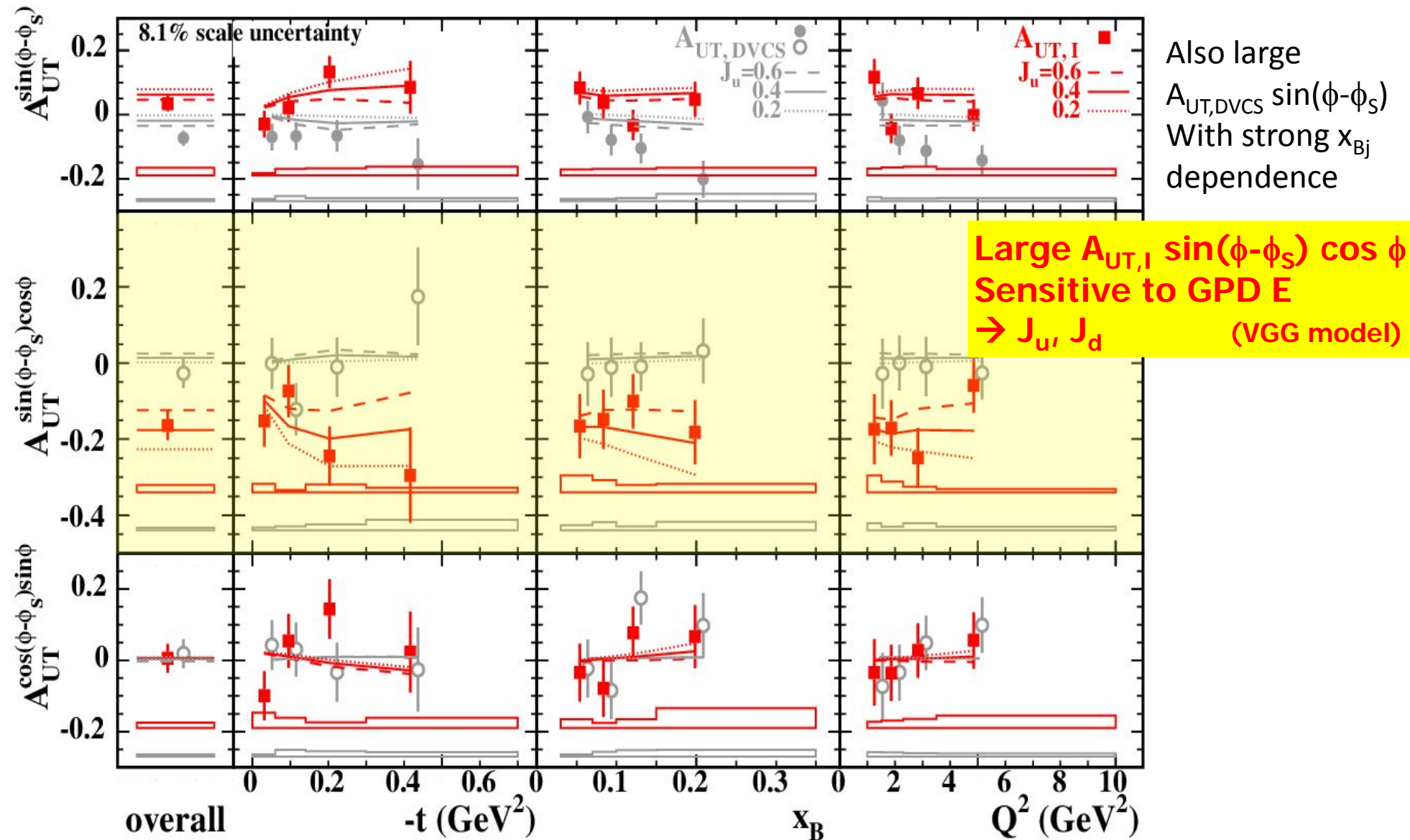


Kumericki, Müller Nucl. Phys. B841 (2010)

Goldstein, Hernandez, Liuti Phys. Rev. D84 (2011)

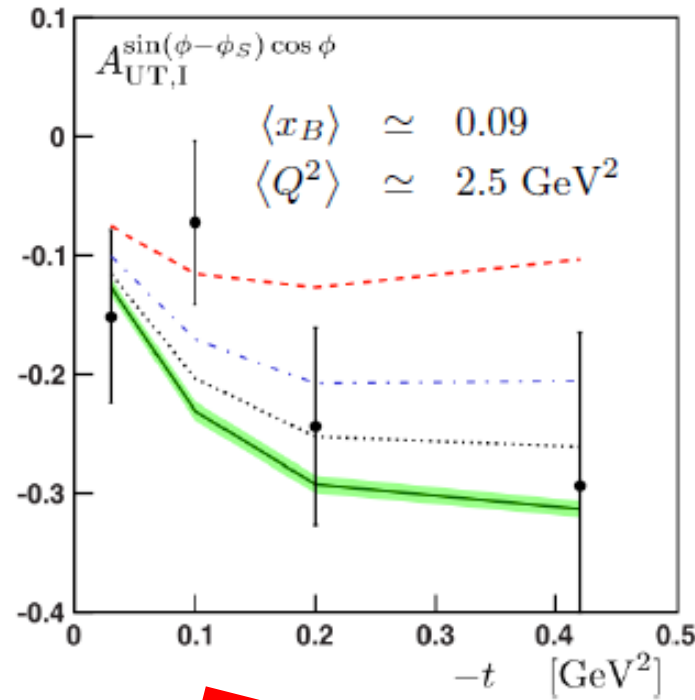
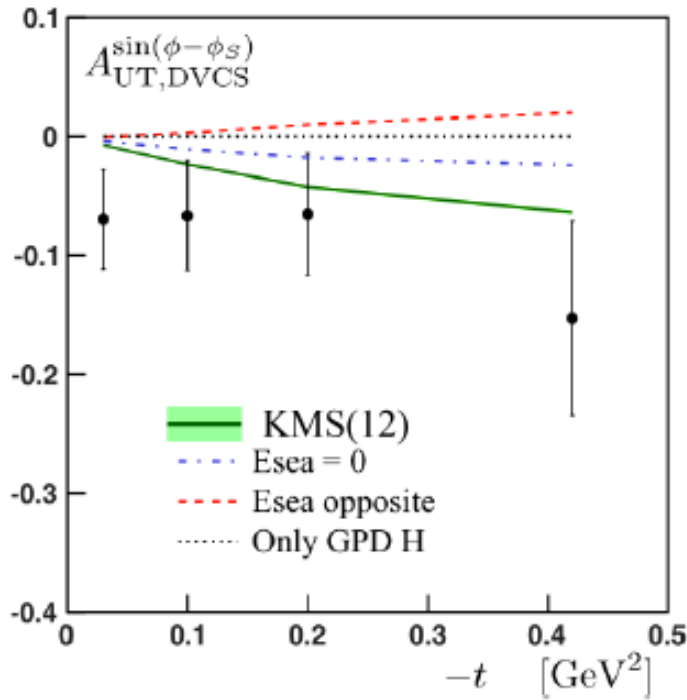
# GPD E Trans. Target Spin Asymmetry (Proton)

## HERMES



# Trans. Target Spin Asymmetry (Proton) - HERMES

Model: Kroll, Moutarde, Sabatié, EPJC73 (2013) with GPDs from GK model



$$A_{UT,DVCS}^{\sin(\phi-\phi_S)} \sim \text{Im}[\mathcal{E}^* \mathcal{H}]$$

$$A_{UT,DVCS}^{\sin(\phi-\phi_S)} \neq 0 \implies \mathcal{E} \neq 0$$

cancellation between  $\mathcal{E}^s$  and  $\mathcal{E}^g$  does not occur as for  $\rho^0$  asymmetry,  
DVCS observables are very sensitive to  $E_{\text{sea}}$

**$E_{\text{sea}} < 0$  is favored by HERMES data**



# Hunting the GPD E with CLAS12 at Jlab

$$\vec{e} d \rightarrow e n \gamma (p) \quad \text{E12-11-003}$$

$$\Delta\sigma_{LU} \sim \text{Im} (F_{1n} \mathcal{H} - F_{2n} \mathcal{E})$$

With **LD2 target** + CLAS12  
 + Forward Calorimeter  
 + Neutron Detector ToF

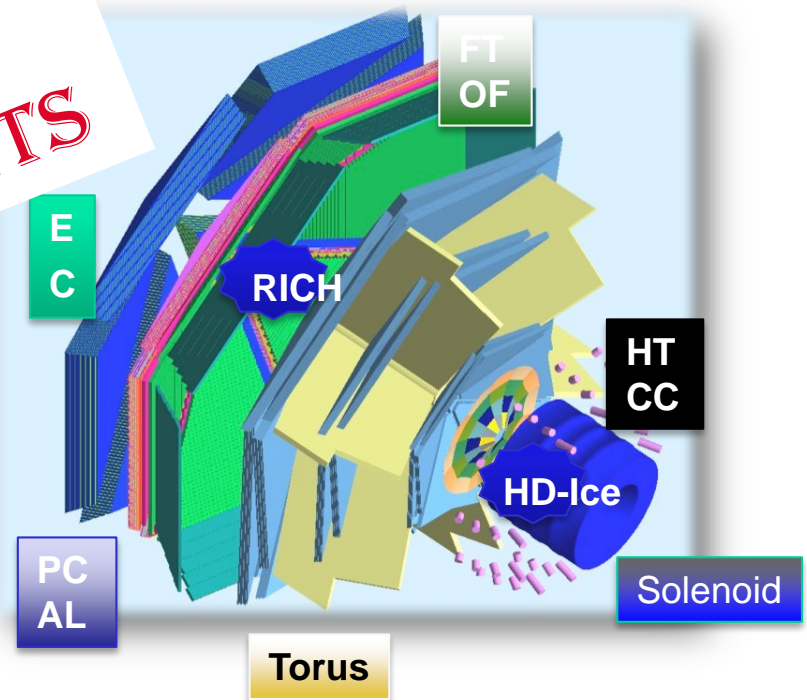
$$\vec{e} p^{\uparrow} \rightarrow e p \gamma \quad \text{E12-12-010}$$

$$\Delta\sigma_{UT} \sin(\phi - \phi_s) \cos \phi = \text{Im} (F_2 \mathcal{H} - F_1 \mathcal{E})$$

$$\Delta\sigma_{LT} \sin(\phi - \phi_s) \cos \phi = \text{Re} (F_2 \mathcal{H} - F_1 \mathcal{E})$$

With the **HD ice target**  
 (transv pol = 60% H )  
 + CLAS12

SELECTED IN THE  
 «HIGH IMPACT» EXPERIMENTS





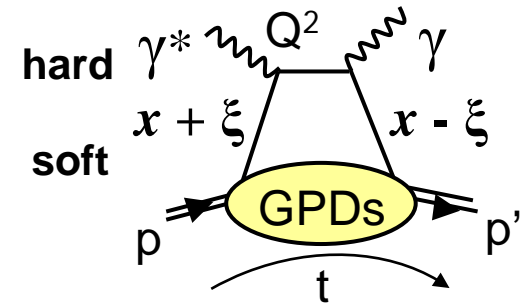
The End

Thank you for your attention

Dragon: among many others it is a symbol for fortune and glory ... like the measurements of GDPs

# Compton Form Factors are measured in DVCS

The amplitude DVCS at LT & LO in  $\alpha_S$ :



$$\mathcal{H} = \int_{-1}^{+1} dx \frac{H(x, \xi, t)}{x - \xi + i\epsilon} = \mathcal{P} \int_{-1}^{+1} dx \frac{H(x, \xi, t)}{x - \xi} - i \pi H(x = \xi, \xi, t)$$

Real part                      Imaginary part

$t, \xi \sim x_{Bj/2}$  fixed

$$\text{Re } \mathcal{H}(\xi, t) = \mathcal{P} \int dx \frac{\text{Im } \mathcal{H}(x, t)}{x - \xi} + \mathcal{D}(t)$$

**$\mathcal{D}$  term** related to the Energy-Momentum Tensor :  
Polyakov, PLB 555 (2003) 57-62

Im part measured in  
**Beam Spin**  
or **Target Spin** asymmetries

Real part measured in  
**Beam Charge** asymmetry  
or **cross section**