

# Quark to $\Lambda$ and $\bar{\Lambda}$ longitudinal spin transfers in the current fragmentation region

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- Introduction
- The observable longitudinal spin transfers for  $\Lambda$  and  $\bar{\Lambda}$
- Light-cone SU(6) quark-spectator-diquark model
- Nucleon  $s\bar{s}$  asymmetry to the  $\Lambda / \bar{\Lambda}$  fragmentation

The nonperturbative nature of QCD at low energy scale makes the detailed hadron structure hard to know

- the "spin crisis": quarks and anti-quarks contribute not more than 30% of the total nucleon spin
- the strange and anti-strange quark in the nucleon sea should be or not be symmetry in the nucleon sea.

Semi-inclusive deep inelastic scattering(SIDIS) process is important in dealing with some of these problems in experiment.

# SIDIS process

Use factorization theory, the nonperturbative part can be put into parton distribution functions and fragmentation functions.

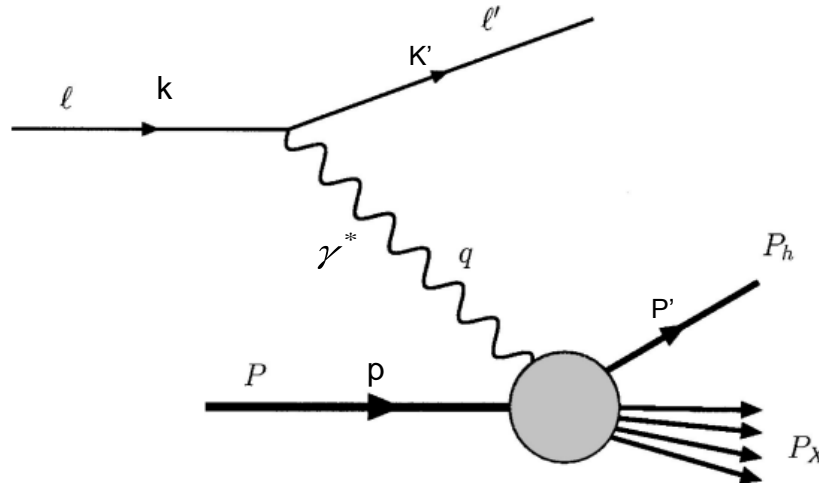


Figure 1: A sketch map for the Semi-inclusive deep-inelastic scattering

The cross section of the final hadron can be expressed as a convolution of the parton distribution functions, the elementary lepton-parton scattering and the fragmentation functions.

The final hyperon plays an important role in the detection of nucleon structures.

# Features of the $\Lambda$ hyperon

- The  $\Lambda$ -hyperon has the “self-analyzing” property in polarization.

Two main decay ways:

$$\Lambda \rightarrow p + \pi^-, (\text{BR} = (63.9 \pm 0.5)\%);$$

$$\Lambda \rightarrow n + \pi^0, (\text{BR} = (35.8 \pm 0.5)\%).$$

In the  $\Lambda$  rest frame, the angle distribution of the produced proton is

$$\frac{dN}{d\Omega_p} \propto 1 + \alpha \vec{P}_\Lambda \cdot \hat{k}_p$$

- The polarization of the produced hadron

$$P_{L'} = P_b \cdot D(y) A_{LL'}^\Lambda, \quad D(y) = \frac{1 - (1 - y)^2}{1 + (1 - y)^2},$$

# Experiment measurement of $\Lambda$ and $\bar{\Lambda}$ spin transfers

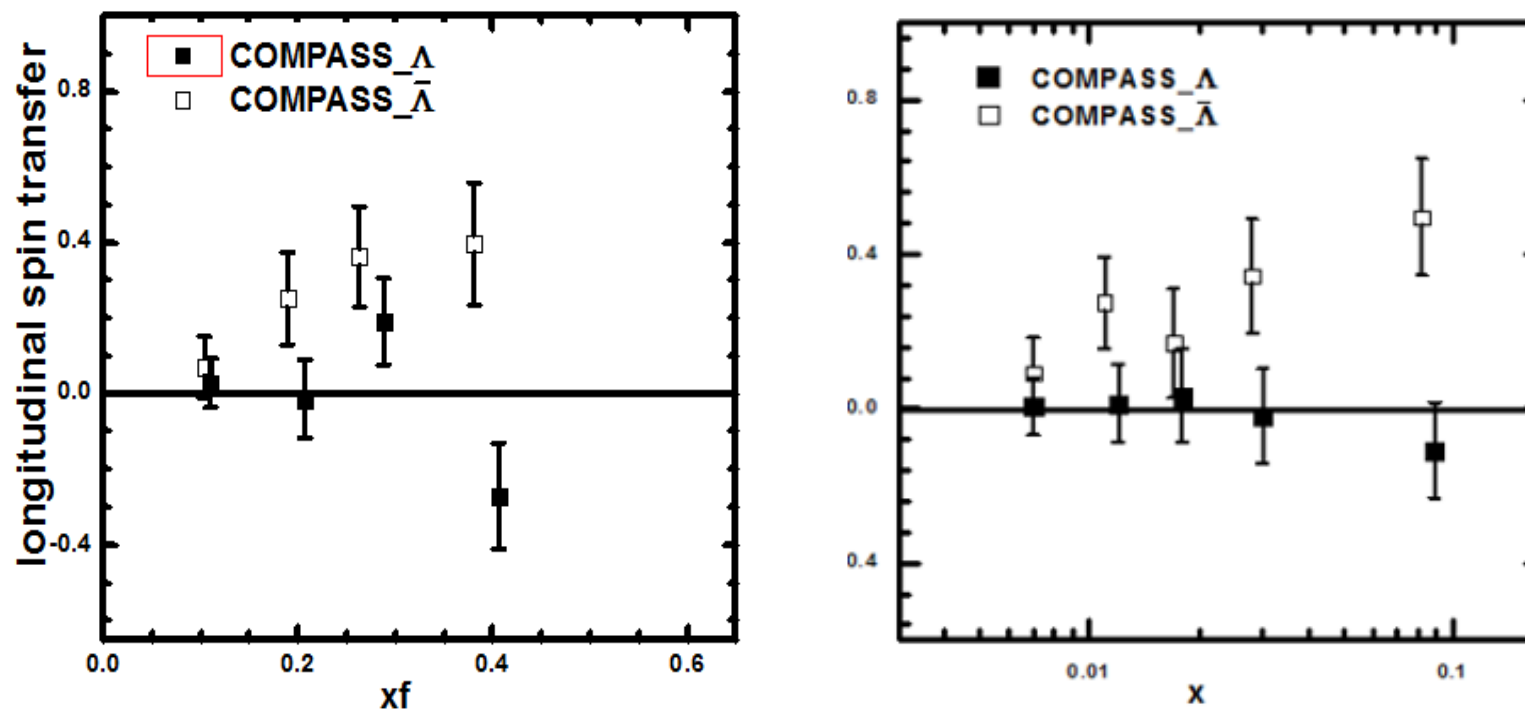


Figure 2: Longitudinal spin transfer of  $\Lambda$  and  $\bar{\Lambda}$  hyperon versus  $x_F$  and  $x$  variables at COMPASS experiment

 M. Alekseev *et al.* (COMPASS Collaboration), Eur. Phys. J. C 64, 171 (2009).

# The observable longitudinal spin transfers for $\Lambda$ and $\bar{\Lambda}$

For a general SIDIS process  $\ell p \rightarrow \ell P_h X$  the differential cross section is

$$\frac{d\sigma}{dx dy dz d^2 \vec{P}_{h\perp}} = \frac{\pi \alpha_{\text{em}}^2 y}{2Q^4} L_{\mu\nu} W^{\mu\nu}.$$

Three Lorentz invariants

$$x = \frac{Q^2}{2P \cdot q}, \quad y = \frac{P \cdot q}{P \cdot \ell}, \quad z = \frac{P \cdot P_h}{P \cdot q}$$

The differential cross section for the production of the unpolarized hadron h

$$\frac{d\sigma}{dx dy dz} = \frac{4\pi \alpha_{\text{em}}^2 S}{Q^4} \sum_q e_q^2 x \frac{1 + (1-y)^2}{2} f_q(x, Q^2) D_q(z, Q^2),$$

# The observable longitudinal spin transfers for $\Lambda$ and $\bar{\Lambda}$

For polarized electron beam hit on an unpolarized proton target process, the helicity asymmetry cross section is

$$\begin{aligned} A(x, y, z) &= \frac{d\sigma_{\uparrow} - d\sigma_{\downarrow}}{d\sigma_{\uparrow} + d\sigma_{\downarrow}} \\ &= \frac{\frac{4\pi\alpha_{\text{em}}^2 S}{Q^4} \sum_a e_a^2 xy(1 - y/2) f_a(x, Q^2) \Delta D_a(z, Q^2)}{\frac{4\pi\alpha_{\text{em}}^2 S}{Q^4} \sum_a e_a^2 x \frac{1+(1-y)^2}{2} f_a(x, Q^2) D_a(z, Q^2)}, \end{aligned}$$

Removing the depolarization factor  $D(y)$  from the asymmetry cross section

$$A(x, y, z) = \frac{\frac{Sx}{Q^4} \sum_q e_q^2 f_q^p(x, Q^2) \Delta D_q^h(z, Q^2)}{\frac{Sx}{Q^4} \sum_q e_q^2 f_q^p(x, Q^2) D_q^h(z, Q^2)}.$$

Consider intermediate hyperon decay process

$$\begin{aligned} D_{\Lambda}^{q(\bar{q})}(z, Q^2) &= a_1 D_{q(\bar{q})\Lambda}(z, Q^2) + a_2 D_{\Sigma^0}^{q(\bar{q})}(z', Q^2) \\ &+ a_3 D_{\Sigma^*}^{q(\bar{q})}(z', Q^2) + a_4 D_{\Xi}^{q(\bar{q})}(z', Q^2), \end{aligned}$$



# Modeling quark fragmentation functions

$$\begin{aligned}\Delta D_{\Lambda}^q(z, Q^2) &= a_1 \Delta D_{q\Lambda}(z, Q^2) + a_2 \Delta D_{\Sigma^0}^q(z', Q^2) \alpha_{\Sigma^0\Lambda} \\ &+ a_3 \Delta D_{\Sigma^*}^q(z', Q^2) \alpha_{\Sigma^*\Lambda} \\ &+ a_4 \Delta D_{\Xi}^q(z', Q^2) \alpha_{\Xi\Lambda},\end{aligned}$$

The production weight coefficients and the polarization parameters

$$\begin{aligned}a_1 &= 0.4, & a_2 &= 0.2, & a_3 &= 0.3, & a_4 &= 0.1, \\ \alpha_{\Sigma^0\Lambda} &= -0.333, & \alpha_{\Sigma^*(\frac{3}{2}, \frac{3}{2})\Lambda} &= 1.0, \\ \alpha_{\Sigma^*(\frac{3}{2}, \frac{1}{2})\Lambda} &= 0.333, & \alpha_{\Xi^0\Lambda} &= -0.406, \\ \alpha_{\Xi^-\Lambda} &= -0.458.\end{aligned}$$



R. Gatto, Phys. Rev. 109, 610 (1958).

Beringer et al. [Particle Data Group], Phys. Rev. D 86, 010001 (2012).

Gribov - Lipatov phenomenological relation:

$$D_q^h(z) \sim z f_h^q(z).$$



Y. Chi and B.-Q. Ma, Phys. Lett. B **726**, 737 (2013).

V.N. Gribov and L.N. Lipatov, Phys. Lett. B **37**, 78 (1971).

If any one of the quark is probed, the remaining two quarks in the nucleon can be treated as a quasi-particle spectator which can be described by two quark wave functions with spin 0 or 1 (scalar or vector diquark).

Commonly, the unpolarized and polarized quark distribution functions can be expressed as

$$q(x) = c_q^S a_S(x) + c_q^V a_V(x), \quad \Delta q(x) = \tilde{c}_q^S \tilde{a}_S(x) + \tilde{c}_q^V \tilde{a}_V(x).$$

where

$$a_D(x) \propto \int [d^2\mathbf{k}_\perp] |\varphi(x, \mathbf{k}_\perp)|^2$$

$$\tilde{a}_D(x) = \int [d^2\mathbf{k}_\perp] W_D(x, \mathbf{k}_\perp) |\varphi_D(x, \mathbf{k}_\perp)|^2, \quad (D = S \text{ or } V),$$

$$W_D(x, \mathbf{k}_\perp) = \frac{(k^+ + m_q)^2 - \mathbf{k}_\perp^2}{(k^+ + m_q)^2 + \mathbf{k}_\perp^2}, \quad \text{with } k^+ = x\mathcal{M} \text{ and } \mathcal{M}^2 = \frac{m_q^2 + \mathbf{k}_\perp^2}{x} + \frac{m_D^2 + \mathbf{k}_\perp^2}{1-x}.$$



B.-Q. Ma, I. Schmidt, J. Soffer, and J.-J. Yang, Phys. Rev. D **65**, 034004 (2002).

# Table 1: Quark distribution function of octet baryons

Baryon	$q$		$\Delta q$		$m_q$ (MeV)	$m_V$ (MeV)	$m_S$ (MeV)
p	$u$	$\frac{1}{6}a_V + \frac{1}{2}a_S$	$\Delta u$	$-\frac{1}{18}\tilde{a}_V + \frac{1}{2}\tilde{a}_S$	330	800	600
(uud)	$d$	$\frac{1}{3}a_V$	$\Delta d$	$-\frac{1}{9}\tilde{a}_V$	330	800	600
n	$u$	$\frac{1}{3}a_V$	$\Delta u$	$-\frac{1}{9}\tilde{a}_V$	330	800	600
(udd)	$d$	$\frac{1}{6}a_V + \frac{1}{2}a_S$	$\Delta d$	$-\frac{1}{18}\tilde{a}_V + \frac{1}{2}\tilde{a}_S$	330	800	600
$\Sigma^+$	$u$	$\frac{1}{6}a_V + \frac{1}{2}a_S$	$\Delta u$	$-\frac{1}{18}\tilde{a}_V + \frac{1}{2}\tilde{a}_S$	330	950	750
(uus)	$s$	$\frac{1}{3}a_V$	$\Delta s$	$-\frac{1}{9}\tilde{a}_V$	480	800	600
$\Sigma^0$	$u$	$\frac{1}{12}a_V + \frac{1}{4}a_S$	$\Delta u$	$-\frac{1}{36}\tilde{a}_V + \frac{1}{4}\tilde{a}_S$	330	950	750
(uds)	$d$	$\frac{1}{12}a_V + \frac{1}{4}a_S$	$\Delta d$	$-\frac{1}{36}\tilde{a}_V + \frac{1}{4}\tilde{a}_S$	330	950	750
	$s$	$\frac{1}{3}a_V$	$\Delta s$	$-\frac{1}{9}\tilde{a}_V$	480	800	600
$\Sigma^-$	$d$	$\frac{1}{6}a_V + \frac{1}{2}a_S$	$\Delta d$	$-\frac{1}{18}\tilde{a}_V + \frac{1}{2}\tilde{a}_S$	330	950	750
(dds)	$s$	$\frac{1}{3}a_V$	$\Delta s$	$-\frac{1}{9}\tilde{a}_V$	480	800	600
$\Lambda^0$	$u$	$\frac{1}{4}a_V + \frac{1}{12}a_S$	$\Delta u$	$-\frac{1}{12}\tilde{a}_V + \frac{1}{12}\tilde{a}_S$	330	950	750
(uds)	$d$	$\frac{1}{4}a_V + \frac{1}{12}a_S$	$\Delta d$	$-\frac{1}{12}\tilde{a}_V + \frac{1}{12}\tilde{a}_S$	330	950	750
	$s$	$\frac{1}{3}a_S$	$\Delta s$	$\frac{1}{3}\tilde{a}_S$	480	800	600
$\Xi^-$	$d$	$\frac{1}{3}a_V$	$\Delta d$	$-\frac{1}{9}\tilde{a}_V$	330	1100	900
(dss)	$s$	$\frac{1}{6}a_V + \frac{1}{2}a_S$	$\Delta s$	$-\frac{1}{18}\tilde{a}_V + \frac{1}{2}\tilde{a}_S$	480	950	750
$\Xi^0$	$u$	$\frac{1}{3}a_V$	$\Delta u$	$-\frac{1}{9}\tilde{a}_V$	330	1100	900
(uss)	$s$	$\frac{1}{6}a_V + \frac{1}{2}a_S$	$\Delta s$	$-\frac{1}{18}\tilde{a}_V + \frac{1}{2}\tilde{a}_S$	480	950	750



B.-Q. Ma, I. Schmidt, J.-J. Yang, Nucl. Phys. B **574**, 331 (2000).

# Table 2: Quark distribution function of $\Sigma(1385)$

Baryon	$q$		$\Delta q$	(3/2,3/2)	(3/2,1/2)	$m_q$ (MeV)	$m_V$ (MeV)
$\Sigma^+(1385)$	$u$	$\frac{2}{3}a_V$	$\Delta u$	$\frac{2}{3}\tilde{a}_V$	$\frac{2}{9}\tilde{a}_V$	330	950
	(uus)	$s$	$\frac{1}{3}a_V$	$\Delta s$	$\frac{1}{3}\tilde{a}_V$	480	800
$\Sigma^0(1385)$	$u$	$\frac{1}{3}a_V$	$\Delta u$	$\frac{1}{3}\tilde{a}_V$	$\frac{1}{9}\tilde{a}_V$	330	950
	(uds)	$d$	$\frac{1}{3}a_V$	$\Delta d$	$\frac{1}{3}\tilde{a}_V$	330	950
		$s$	$\frac{1}{3}a_V$	$\Delta s$	$\frac{1}{3}\tilde{a}_V$	480	800
$\Sigma^-(1385)$	$d$	$\frac{2}{3}a_V$	$\Delta d$	$\frac{2}{3}\tilde{a}_V$	$\frac{1}{9}\tilde{a}_V$	330	950
	(dds)	$s$	$\frac{1}{3}a_V$	$\Delta s$	$\frac{1}{3}\tilde{a}_V$	480	800



Y. Chi, X. Du and B.-Q. Ma, Phys. Rev. D **90**, 074003 (2014).

# Inputs of the quark fragmentation functions

- Use CTEQ parameterization as an input

$$\begin{aligned}u_v^p(x) &= u_v^{\text{ctq}}(x), & \Delta d_v^\Lambda(x) &= \Delta u_v^\Lambda(x) = \frac{\Delta u_v^{\Lambda, \text{th}}(x)}{u_v^{p, \text{th}}(x)} * u_v^{\text{ctq}}(x), \\d_v^\Lambda(x) &= u_v^\Lambda(x) = \frac{u_v^{\Lambda, \text{th}}(x)}{u_v^{p, \text{th}}(x)} * u_v^{\text{ctq}}(x), & \Delta s_v^\Lambda(x) &= \frac{\Delta s_v^{\Lambda, \text{th}}(x)}{u_v^{p, \text{th}}(x)} * u_v^{\text{ctq}}(x), \\s_v^\Lambda(x) &= \frac{s_v^{\Lambda, \text{th}}(x)}{u_v^{p, \text{th}}(x)} * u_v^{\text{ctq}}(x),\end{aligned}$$

- For sea quark distribution functions, use SU(3) symmetry

$$\begin{aligned}d_s^\Lambda(x) &= u_s^\Lambda(x) = \bar{u}^\Lambda(x) = \frac{1}{2}(\bar{u}^{\text{ctq}}(x) + \bar{d}^{\text{ctq}}(x)) \\s_s^\Lambda(x) &= \bar{s}^\Lambda(x) = \bar{d}^{\text{ctq}}(x),\end{aligned}$$

Gribov - Lipatov phenomenological relation:  $D_q^h(z) \sim z f_h^q(z)$ .



Y. Chi and B.-Q. Ma, Phys. Lett. B **726**, 737 (2013).

V.N. Gribov and L.N. Lipatov, Phys. Lett. B **37**, 78 (1971).

# Inputs of quark distribution functions

- Nonstrange distribution functions in the proton are from the CTEQ parameterization.
- For the strange and antistrange sea quark distribution in the proton

In the baryon-meson fluctuation model

$$s(x) = \int_x^1 \frac{dy}{y} f_{\Lambda/K+\Lambda}(y) q_{s/\Lambda} \left( \frac{x}{y} \right),$$
$$\bar{s}(x) = \int_x^1 \frac{dy}{y} f_{K^+/K+\Lambda}(y) q_{\bar{s}/K^+} \left( \frac{x}{y} \right).$$

Use the model as an effective modification to the whole strange sea, the strange sea PDFs read

$$s^P(x) = \frac{2s^{\text{th}}}{s^{\text{th}} + \bar{s}^{\text{th}}} s^{\text{ctq}},$$
$$\bar{s}^P(x) = \frac{2\bar{s}^{\text{th}}}{s^{\text{th}} + \bar{s}^{\text{th}}} s^{\text{ctq}}.$$



S. J. Brodsky and B.-Q. Ma, Phys. Lett. B **381**, 317 (1996)

Exact relation between  $x_F$ ,  $x$ ,  $y$ ,  $z$  variables

$$x_F = \frac{Syz}{M [M^2 + Sy(1-x)]} \left[ \left( M + \frac{Sy}{2M} \right) \times \sqrt{\frac{1 - [4M^2(M_h^2 + P_{h\perp}^2)]}{(Syz)^2}} - \sqrt{\frac{S^2y^2}{4M^2} + Sxy} \right]$$

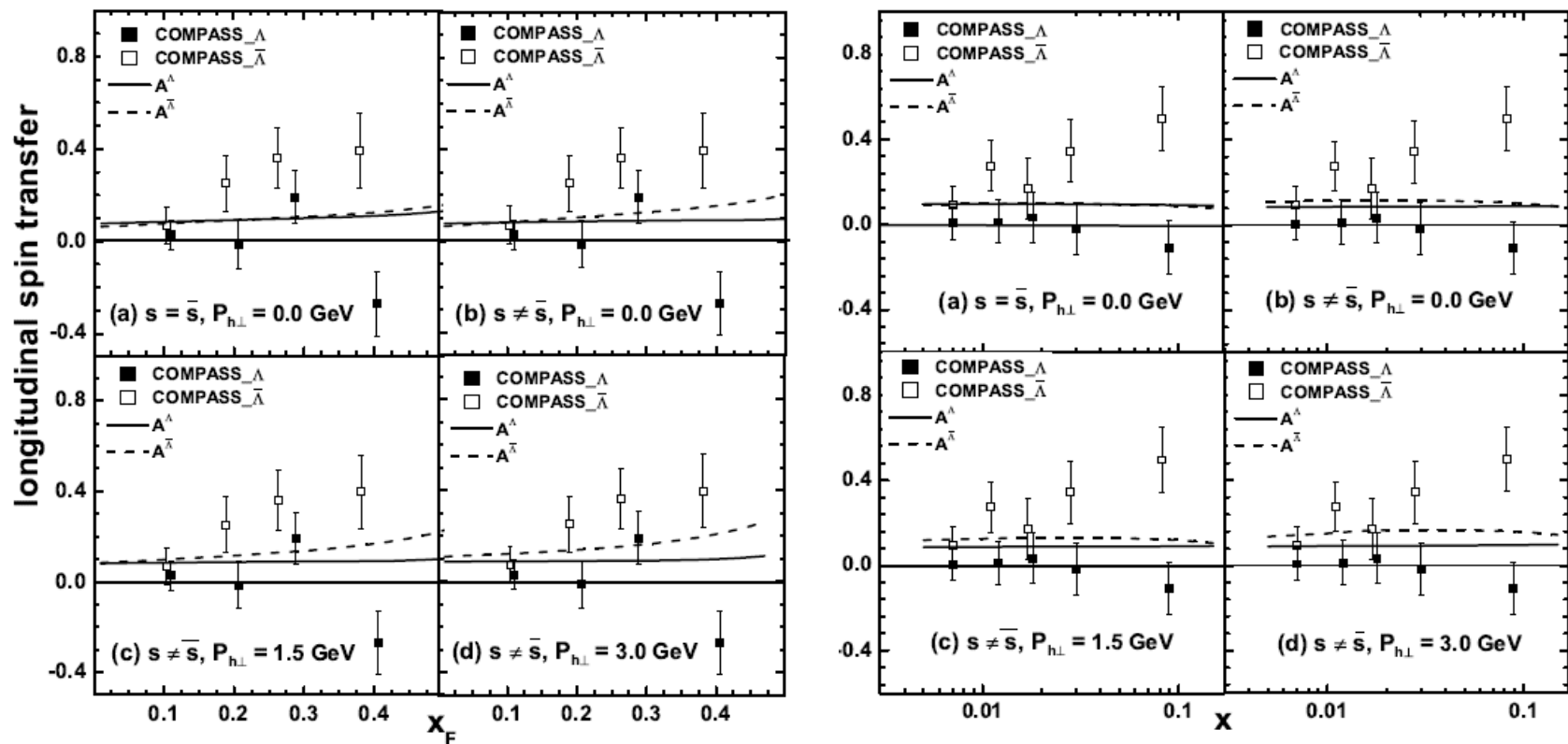
The COMPASS experimental cuts for 2004 run

$$1 \text{ GeV}^2 < Q^2 < 50 \text{ GeV}^2, 0.005 < x < 0.65, \\ 0.2 < y < 0.9, 0.05 < x_F < 0.5$$



Y. Chi, X. Du and B.-Q. Ma, Phys. Rev. D **90**, 074003 (2014).

# Nucleon strange $s\bar{s}$ asymmetry to the $\Lambda / \bar{\Lambda}$ fragmentation



**Figure 3:**  $x_F$  and  $x$ -dependent longitudinal spin transfer in polarized SIDIS process. Inputs of the proton strange sea asymmetry and the  $P_{h\perp}$  nonzero values are considered step by step.



- ◆ The  $S\bar{S}$  asymmetry gives more proper trend to the difference between the  $\Lambda$  and  $\bar{\Lambda}$  longitudinal spin transfer.
- ◆ The large  $z$  region is more sensitive to the asymmetric nucleon strange sea input, and this sensitivity can give better explanations to the experimental data.
- ◆ We suggest new and precise experimental measurement of the  $\Lambda$  and  $\bar{\Lambda}$  production in the large  $z$  region.