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# Charged hadron multiplicities and quark fragmentation functions from COMPASS

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On behalf of the COMPASS Collaboration

- **Charged hadron multiplicities**
- **Quark fragmentation functions into pions from LO fit**
- **Outlook**



# COMPASS at CERN

Fixed target

160-200 GeV muon beam and 190 hadron beams from CERN SPS

→ Multipurpose setup

Polarized muon beam  
& polarized target: d, p

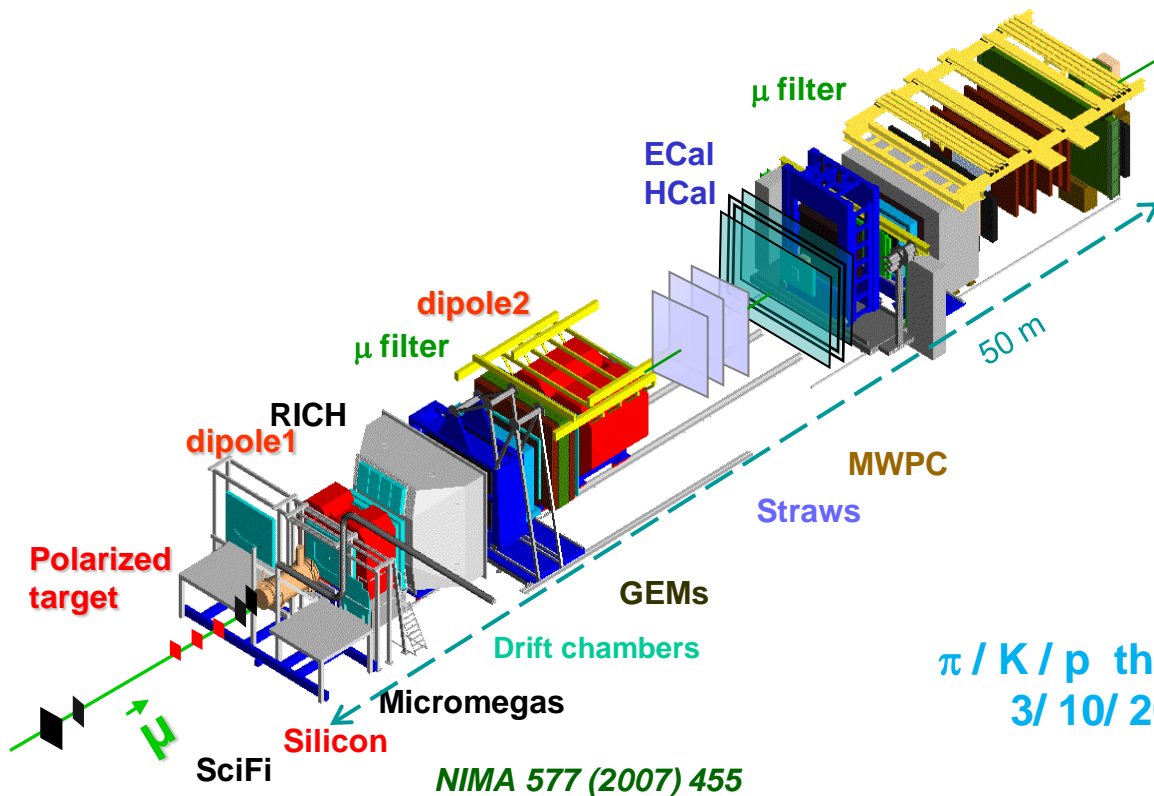
Nucleon spin structure

Hadron beam  $\pi / K / p$   
&  $\text{LH}_2$  or nuclei

Meson spectroscopy  
 $\pi$ , K polarizabilities

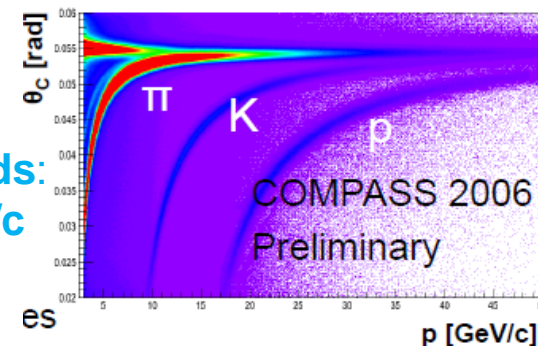
Future:

GPDs from DVCS  
TMDs from Polarized  
Drell-Yan



*NIMA 577 (2007) 455*

RICH  
 $\pi / K / p$  thresholds:  
3/ 10/ 20 GeV/c



# Quark Fragmentation Functions (FF)

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- Non perturbative objects
- Process independent
- Needed to access strange quark polarization  $\Delta s$  from polarized SIDIS.  
strange quark FF = largest uncertainty in this extraction.

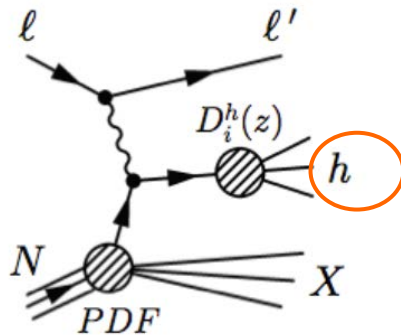
Data sensitive to FFs exist from  $e^+e^-$  and pp reactions,  
but are insufficient for good flavour separation and at too high  $Q^2$

→ extract FFs from unpolarized COMPASS SIDIS data

# Quark FFs from SIDIS

Measurement of multiplicities of  $\pi$ , K, p in **SIDIS**

$\mu^+d \rightarrow \mu^+h^+X$



Hadron multiplicity = mean number of hadrons h per DIS event

$$z = E_h / (E_\mu - E_{\mu'})$$

$$\frac{dM^h(x, Q^2, z)}{dz} \underset{\text{at LO}}{=} \frac{\sum_q e_q^2 \underbrace{f_q(x, Q^2)}_{\text{PDFs}} \underbrace{D_q^h(z, Q^2)}_{\text{FFs}}}{\sum_q e_q^2 f_q(x, Q^2)}$$

PDFs depend on  $x$ , while FFs depend on  $z$

$$\sum_h \int_0^1 z D_q^h(z) dz = 1$$

Data can be obtained in a fine binning in  $x$ ,  $z$ ,  $Q^2$

→ Input to global QCD analyses to extract quark FFs

# Data analysis - hadron multiplicities

- 3 Weeks of 2006 data (1/4 of total stat.)

${}^6\text{LiD}$  target : isoscalar

- **Kinematic cuts :**

- *Inclusive events:*

➤  $Q^2 > 1 \text{ GeV}^2/c^2$

➤  $0.1 < y < 0.7$

➤  $0.004 < x < 0.7$

- *Hadrons :*

➤  $0.2 < z < 0.85$

➤  $10 < p_h < 40 \text{ GeV}/c$

Data cover  $5 < W < 17 \text{ GeV}$

- **Analysis :**

- Calculate **raw** multiplicities of  $h^{+-}$ ,  $\pi^{+-}$  and  $K^{+-}$

- in 3D-binning: ( x, y, z),  $\langle Q^2 \rangle$  evaluated in each bin
- RICH likelihood cuts are used for identification

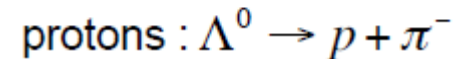
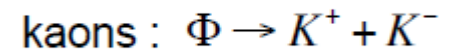
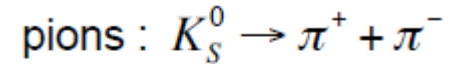
- **Apply corrections:**

- Efficiency/ purity of RICH detector for  $\pi/K$  identification
- Spectrometer acceptance  
including efficiency of detectors and event reconstruction
- Electron contamination of  $\pi$  sample
- Diffractive vector meson production  $\rho^0$  and  $\phi$

# RICH performance matrices

Need to evaluate absolute efficiency / purity of RICH detector

- “pure”  $\pi$ , K and p samples, well identified from parent decays:

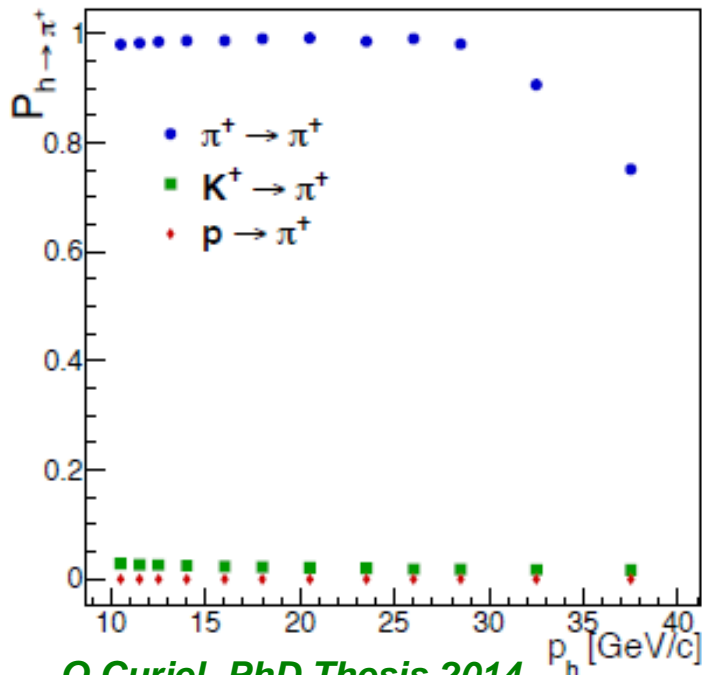


- Look at RICH responses

→ Probabilities  $\mathcal{P}$  of identification and misidentification of  $\pi^{+/-}$ ,  $K^{+/-}$  and p

Example for positive particles

$\mathcal{P}(h^+ \rightarrow \pi^+)$  vs  $p_h$  in one  $\theta$  bin:



Q.Curiel, PhD Thesis 2014

$\mathcal{P}$  in  $(p_h, \theta)$  bins

$p_h$  : momentum of hadron

$\theta$  : angle at RICH entrance

Measured

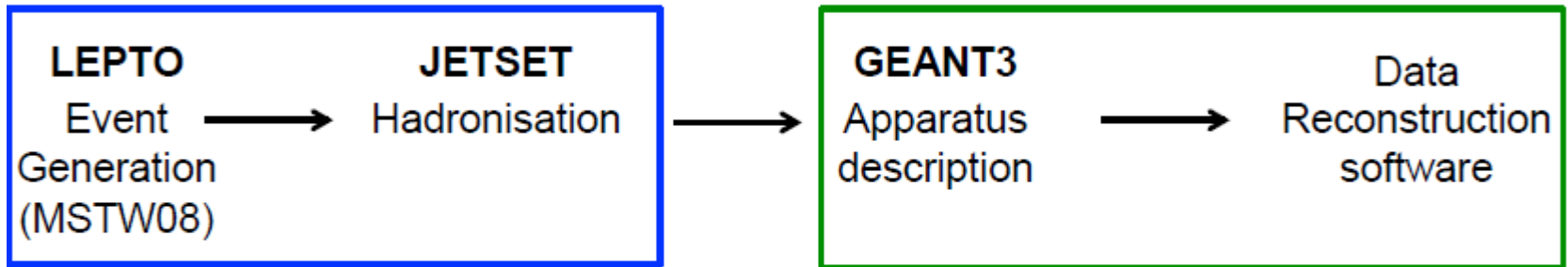
$$\begin{pmatrix} I_\pi \\ I_K \\ I_p \end{pmatrix} = \begin{pmatrix} \epsilon_\pi^\pi & \epsilon_K^\pi & \epsilon_p^\pi \\ \epsilon_\pi^K & \epsilon_K^K & \epsilon_p^K \\ \epsilon_\pi^p & \epsilon_K^p & \epsilon_p^p \end{pmatrix} \begin{pmatrix} T_\pi \\ T_K \\ T_p \end{pmatrix}$$

“True”

# Acceptance calculation

Includes geometric acceptance plus detector and reconstruction efficiency

Monte Carlo Simulation :



$$A^h(x, y, z) = \frac{M_r^h(x, y, z)}{M_g^h(x, y, z)}$$

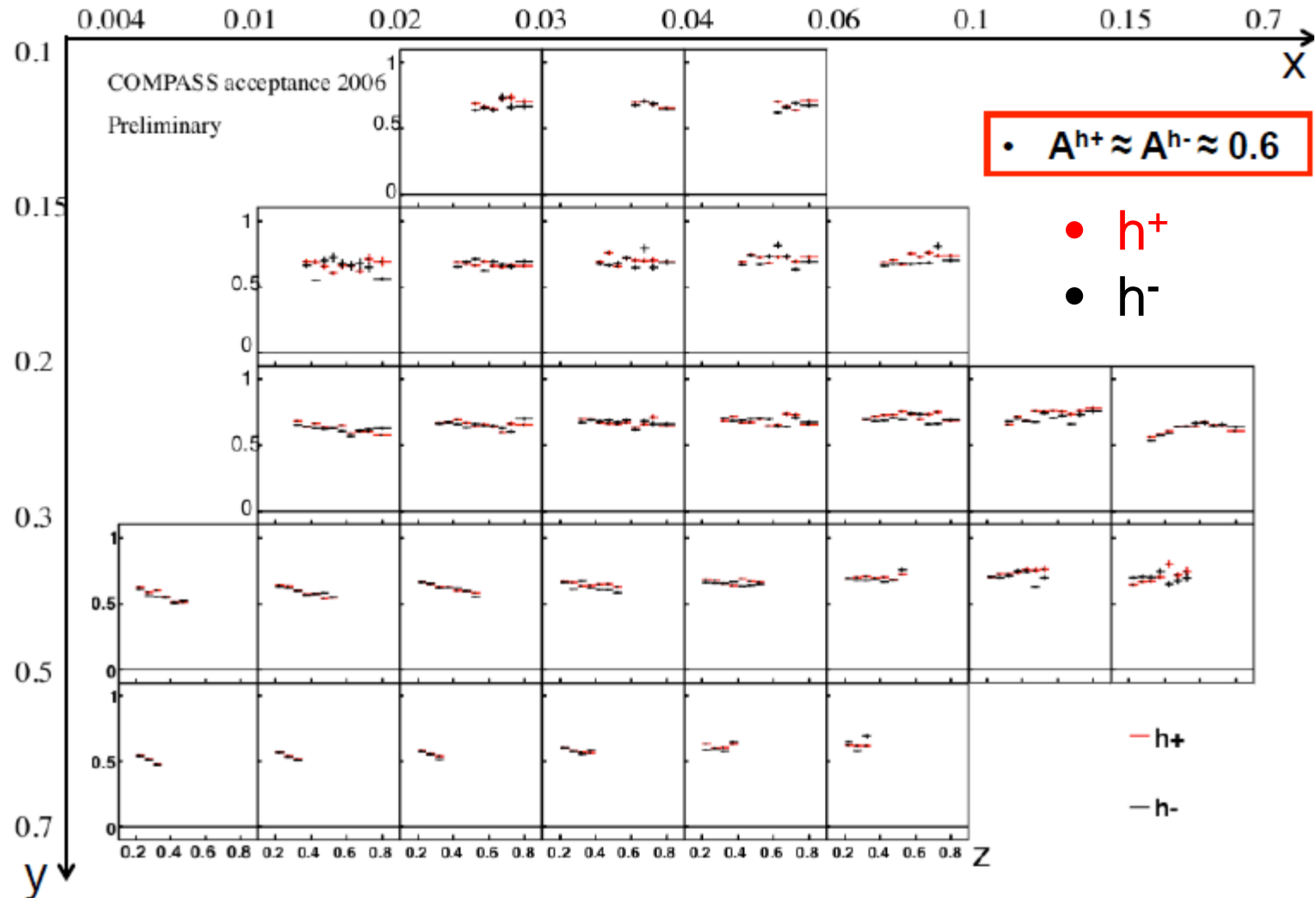
← Reconstructed

← Generated (kinematical cuts only)

$$h = h^+, h^-, \pi^+, \pi^-, K^+, K^-$$

# Spectrometer acceptance for $h^+$ and $h^-$

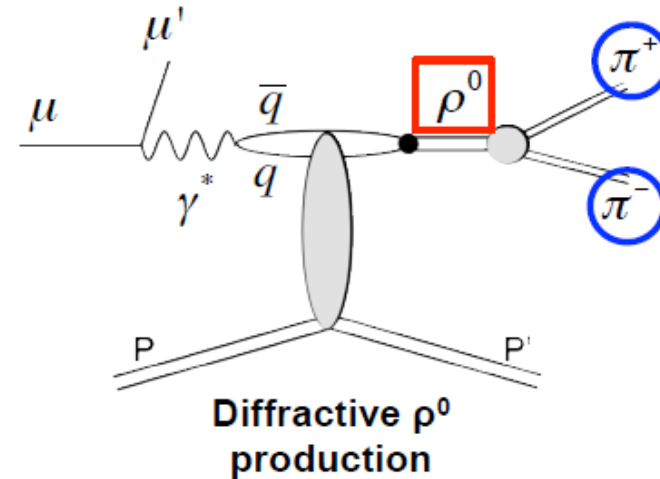
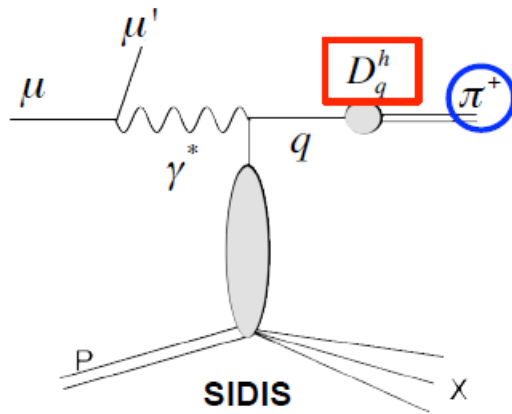
Prelim. results from MC simulation:  $A(z)$  in 29 (x-y) bins





# Contribution from diffractive meson production

The data sample includes SIDIS events but also  $\pi$  and K from diffractive meson production, without quark hadronization.



Main VM:  $\rho^0$  and  $\phi$

$$\gamma^* N \rightarrow \rho^0 N \rightarrow \pi^+ \pi^- N$$

$$\gamma^* N \rightarrow \Phi N \rightarrow K^+ K^- N$$

# Contribution from diffractive meson production

F. Thibaud, QCD Montpellier-2014

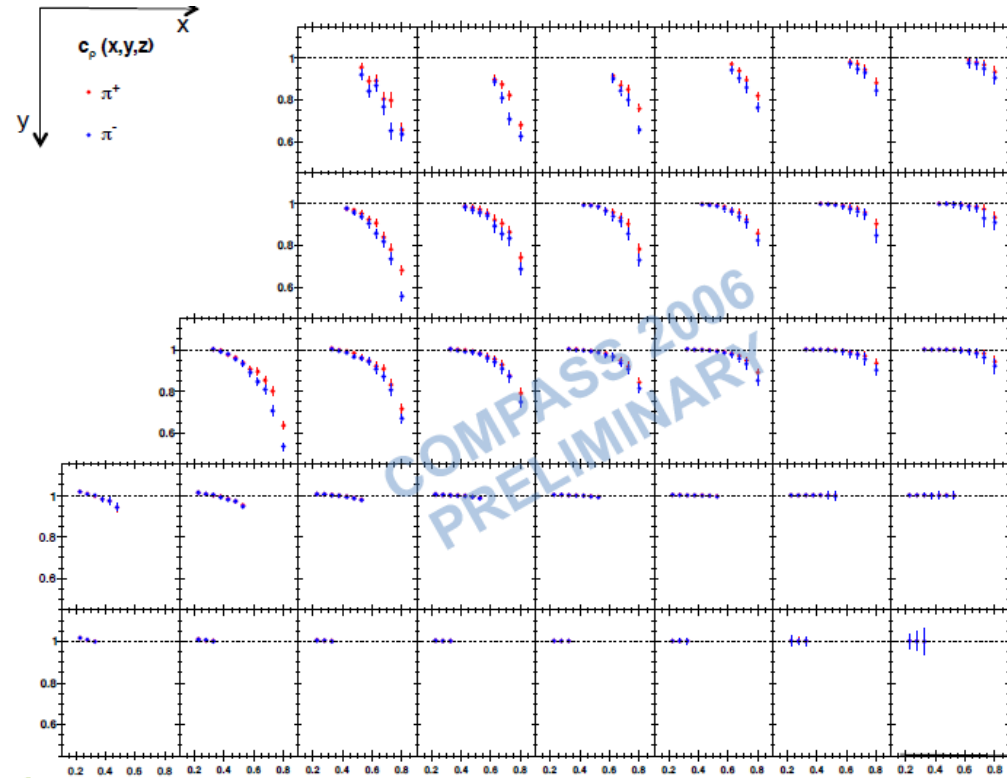
- MC simulation, using LEPTO for SIDIS and HEPGEN for VM production

- In total, contribution from VM small : few %

However in some bins, it reaches:

- 40% for  $\pi$  (high  $z$ , low  $Q^2$ )
- there,  $\pi$  multiplicities are very small
- 20% for K ( $z \sim 0.6$ , low  $Q^2$ )

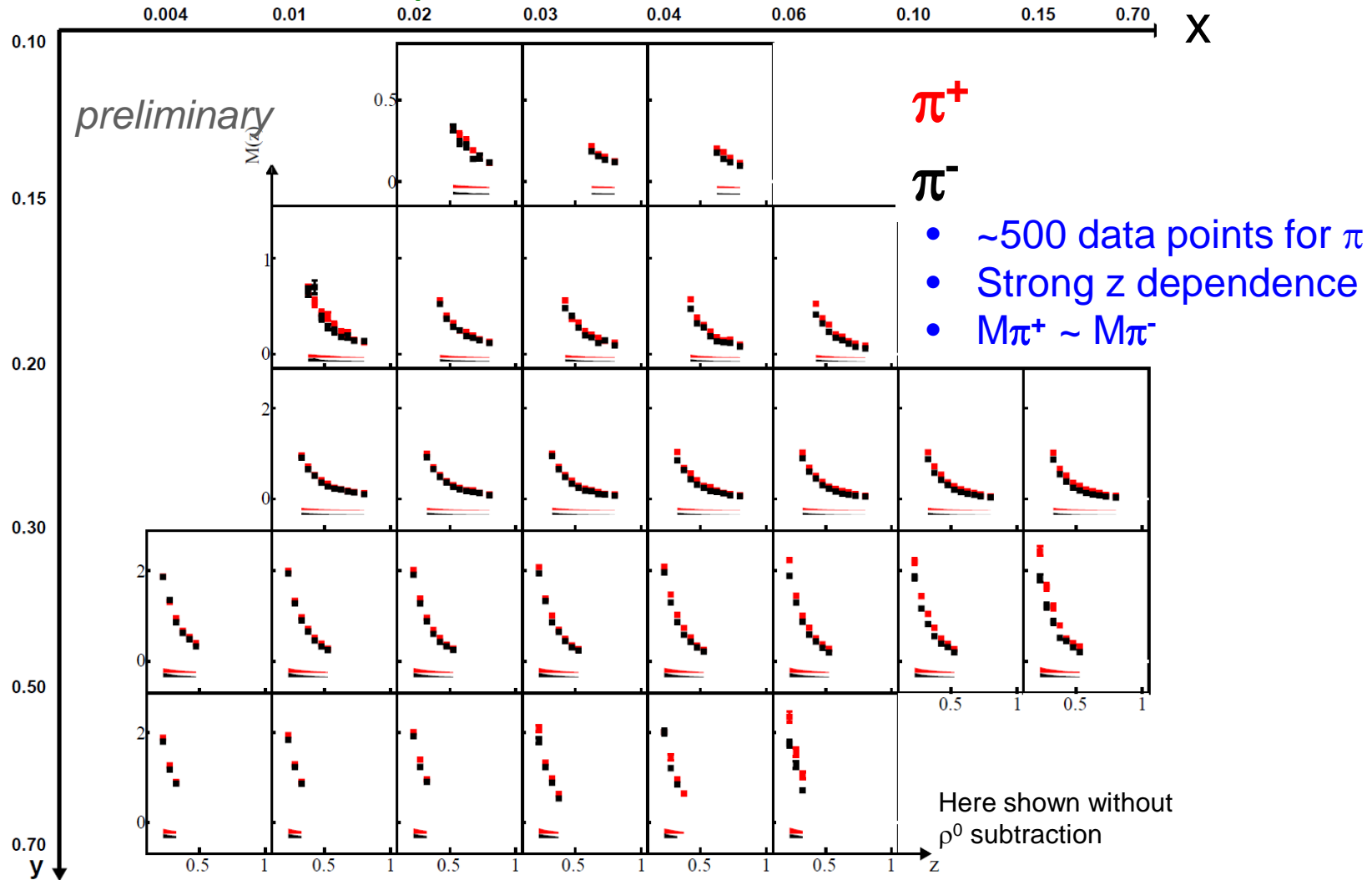
- Multiplicity data will be published with and without correction



Ex: Correction for contribution of  $\pi$  from  $\rho^0$  in the data sample, vs  $z$ , in 35  $(x,y)$  bins

# $\pi^+$ and $\pi^-$ multiplicities vs $z$ in $(x,y)$ bins

COMPASS *prelim.* (DIS-2013, N.Makke)

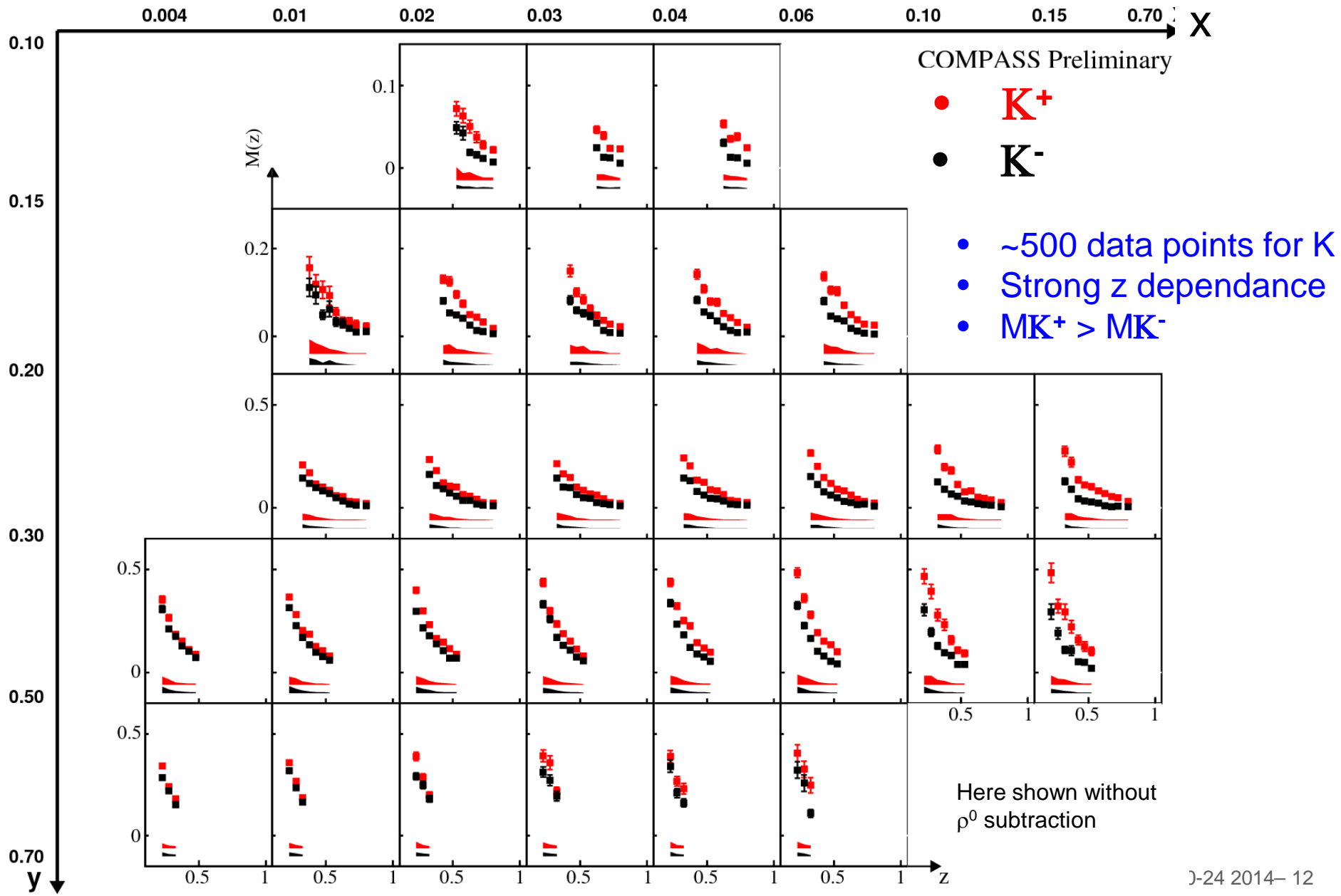


Systematics dominated by uncertainty on acceptance (5%) and RICH.

NB- Also measured:  $p_T$  dependence (*see talk of N.Makke*) and 2h multiplicities

# $K^+$ and $K^-$ multiplicities vs $z$ in $(x,y)$ bins

COMPASS prelim. (DIS-2013, N.Makke)



# Quark FFs into $\pi$ , from COMPASS LO fits

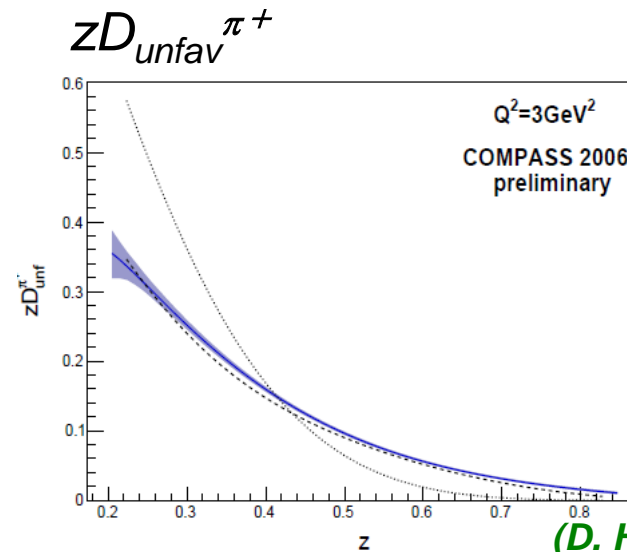
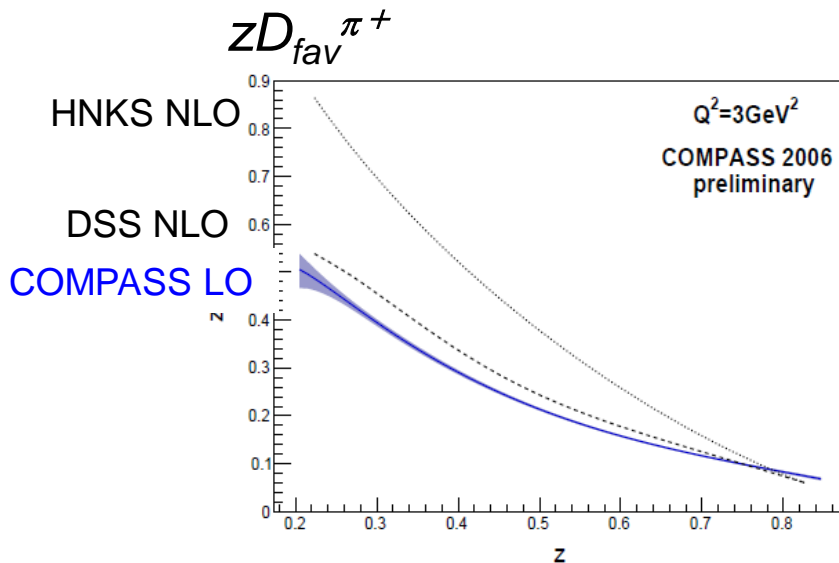
Assume isospin and charge symmetry:

$$D_{\text{fav}}^{\pi^+} = D_U^{\pi^+} = D_d^{\pi^+} = D_d^{\pi^-} = D_U^{\pi^-}$$

$$D_{\text{unf}}^{\pi^+} = D_d^{\pi^+} = D_U^{\pi^+} = D_U^{\pi^-} = D_d^{\pi^-} \quad \text{Assume also} \quad D_S^{\pi^+} = D_S^{\pi^-} = D_{\text{unf}}^{\pi^+}$$

Choose functional forms for FFs ( $z$ ); use DGLAP.

Fit  $\pi^+$  and  $\pi^-$  multiplicities and extract the 2 independent FFs:



— COMPASS LO  
 ..... DSS NLO  
 - - - - HNKS NLO

(D. Hahne DPG-2014 and  
 N. du Fresne von  
 Hohenesche. DIS-2014)

Next step: Fragmentation functions into kaons  $D_S^{K^+}$  and  $D_S^{K^-}$   
 starting from kaon multiplicities

# Summary

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## Multiplicities for $h^+, h^-, \pi^+, \pi^-, K^+, K^-$

in a fine binning of  $x, y, z$ ;  $5 < W < 17$  GeV

Important input to global QCD fit of FFs at NLO

## Quark FF into pions from LO fit of $\pi^+, \pi^-$ multiplicities

$D_{\text{fav}}^{\pi}$  &  $D_{\text{unfav}}^{\pi}(z, Q^2)$  : Promising results already at LO

## In progress

Finalize pion and kaon multiplicities with improved MC and RICH treatment

Extract quark FF into kaons

Analyze data on  $H_2$  target (2012)  $\rightarrow$  more input for flavor separation

## Future

2016-2017 : large set of proton data

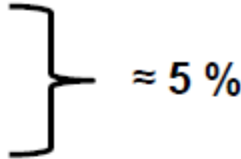
(in parallel to GPD program:  $\mu$  beam,  $H_2$  target & upgraded RICH detector).

# Spares

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# Systematic uncertainties

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- Acceptance :
  - different sets of PDF in Lepto
  - different JETSET tunings  $\approx 5 \%$
- RICH PID efficiency
  - pions : **1 % - 3 %**
  - kaons : **5 % - 10 %**
- Diff.  $\rho^0$  and  $\phi$  correction
  - 30 % theoretical uncertainty on HEPGEN cross-section
    - **12 %** max uncertainty on correction
- Electron correction
  - 25 % MC/data difference -> **50 %** conservative syst. error



# Quark FFs into $\pi$ , from COMPASS fits

*N. Dufresnes at DIS-2014* Starting from  $\pi$  multiplicities, extract 2 FFs.

$$D_{fav}^{\pi^+} = D_u^{\pi^+} = D_d^{\pi^+} = D_d^{\pi^-} = D_u^{\pi^-}$$

$$D_{unf}^{\pi^+} = D_d^{\pi^+} = D_u^{\pi^+} = D_u^{\pi^-} = D_d^{\pi^-}$$

And assuming  $D_{unf}^{\pi^+} = D_s^{\pi^+} = D_s^{\pi^-}$

$$M^{\pi^+}(x, Q^2, z) = \frac{(4(u+d) + \bar{u} + \bar{d})D_{fav} + (u+d + 4(\bar{u} + \bar{d}) + 2(s + \bar{s}))D_{unf}}{5(u+d + \bar{u} + \bar{d}) + 2(s + \bar{s})}$$

$$M^{\pi^-}(x, Q^2, z) = \frac{(u+d + 4(\bar{u} + \bar{d}))D_{fav} + (4(u+d) + \bar{u} + \bar{d} + 2(s + \bar{s}))D_{unf}}{5(u+d + \bar{u} + \bar{d}) + 2(s + \bar{s})}$$

$u, d, \bar{u}, \bar{d}, s, \bar{s}(x, Q^2) =$  parton distribution functions (MSTW08)

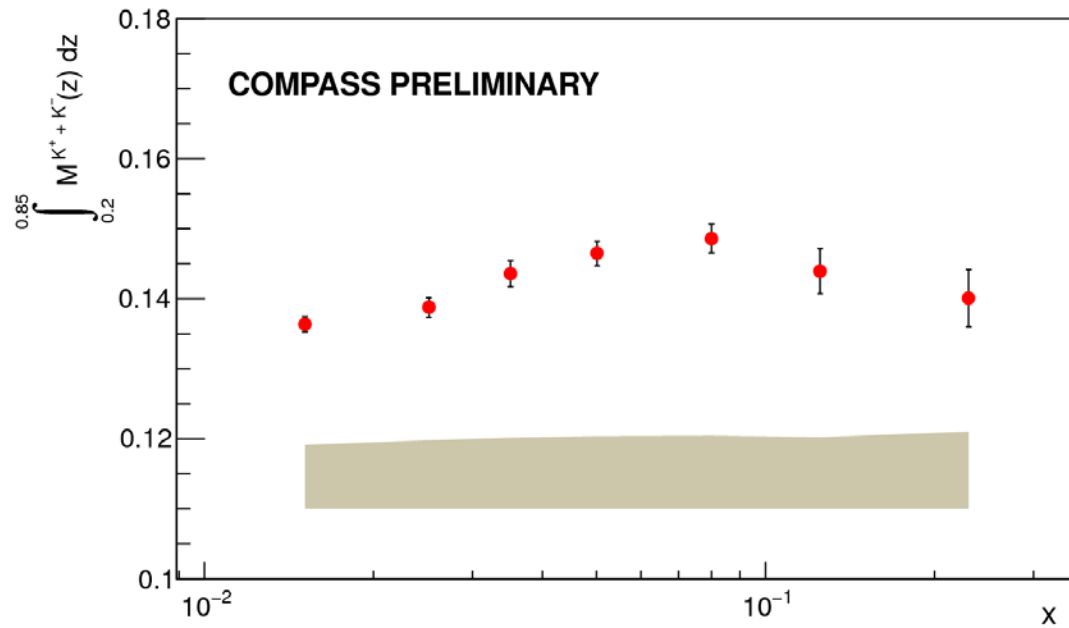
LO fit of experimental multiplicities :

➤ Functional form :  $zD_{fav} = zD_{unf} = Nz^\alpha(1-z)^\beta [1 + \gamma(1-z)^\delta]$  at a given  $Q_0^2$

➤ Evolution from  $Q_0^2$  to  $Q^2$  of data points with DGLAP

# Sum $M(K^+) + M(K^-)$

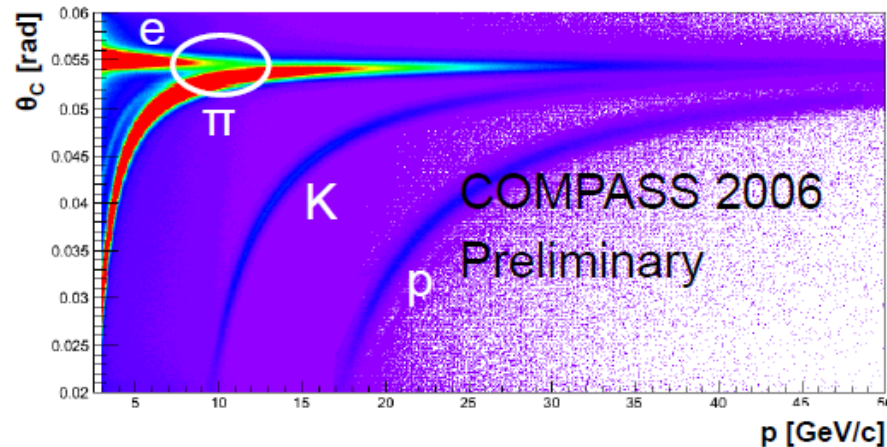
*N.Makke, DIS 2013*



# Electron contamination of pion sample

Electrons can be misidentified as pions

- 3 - 8 GeV/c :
  - e/ $\pi$  separation possible
  - difference MC/data 25 %
- 10 - 40 GeV/c (analysis range) :
  - Contamination evaluated by MC
  - 50 % systematic uncertainty



Correction of pions yields : <1% (high z) to 5% (low z)