

# Charge and spin interference in $\text{Bi}_2\text{Se}_3$ and $\text{Bi}_2\text{Te}_3$ with strong spin-orbit coupling



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# Outline

Part I:

Aharonov-Casher effect in  $\text{Bi}_2\text{Se}_3$   
square-ring interferometers

Part II:

Anomalous Cooper pair interference  
on the surfaces of  $\text{Bi}_2\text{Te}_3$

# Acknowledgements



## Students:

Fanming Qu

Fan Yang

Jun Chen

Jie Shen

Yue Ding

## Structural characterization:

Jiangbo Lu

Yuanjun Song

Huaixin Yang

## Colleagues:

Guangtong Liu

Jie Fan

Yongqing Li

Zhongqing Ji

Changli Yang

## Theory:

Qingfeng Sun

Xincheng Xie



# Motivation

One of the main purposes of **spintronics**

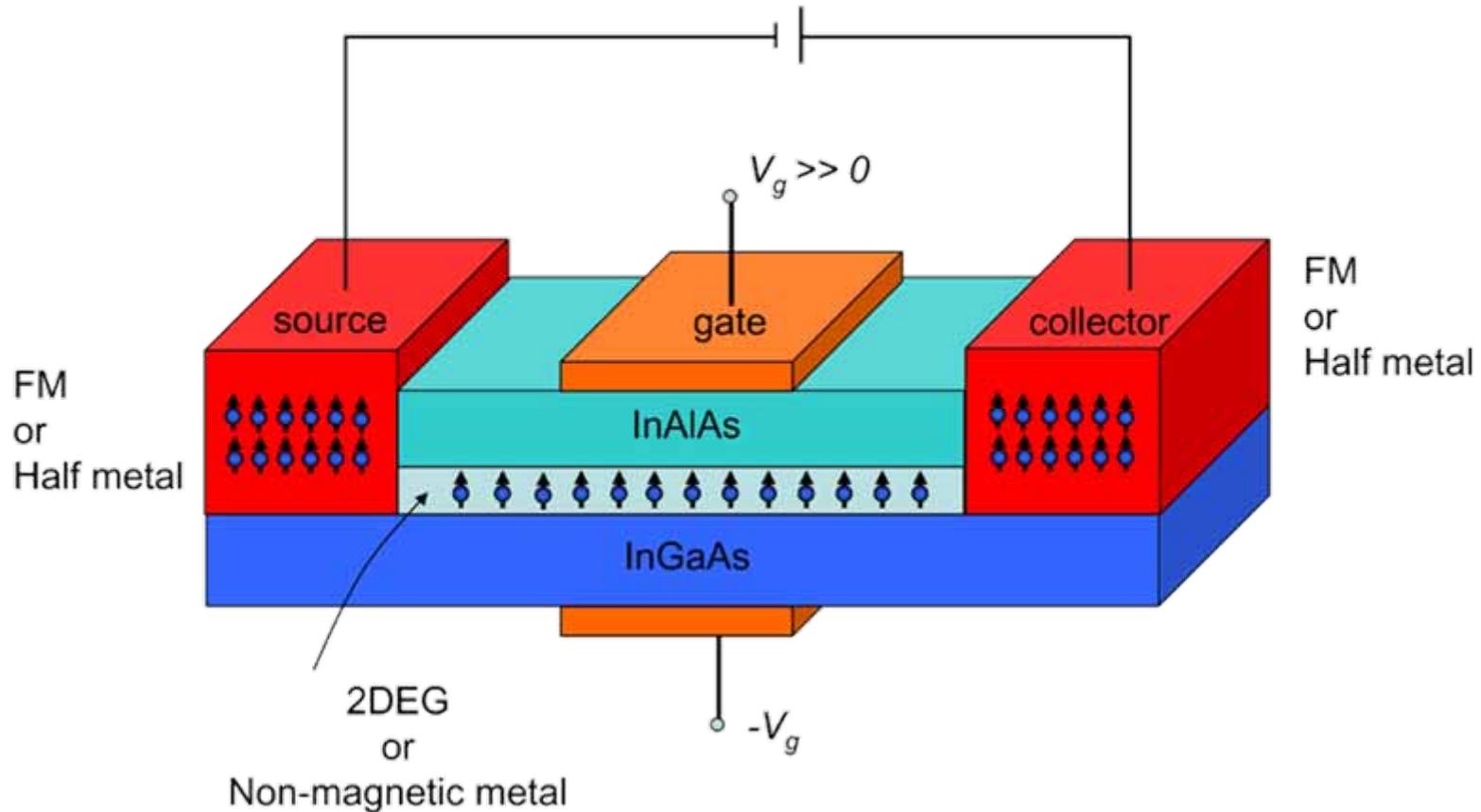
is to explore electrical control of spin dynamics in solid-state devices via spin-orbit coupling (SOC).



Spin field-effect transistor (spin FET)

# Datta-Das Transistor (Spin FET)

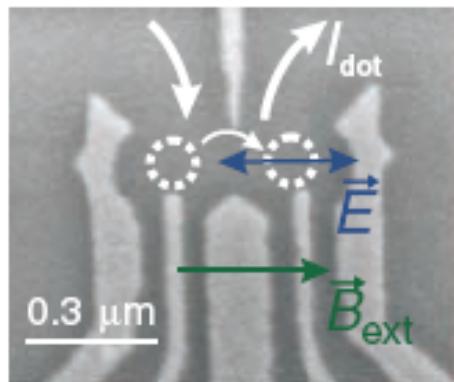
S. Datta, B. Das, et al., Appl. Phys. Lett. 56 665 (1990)



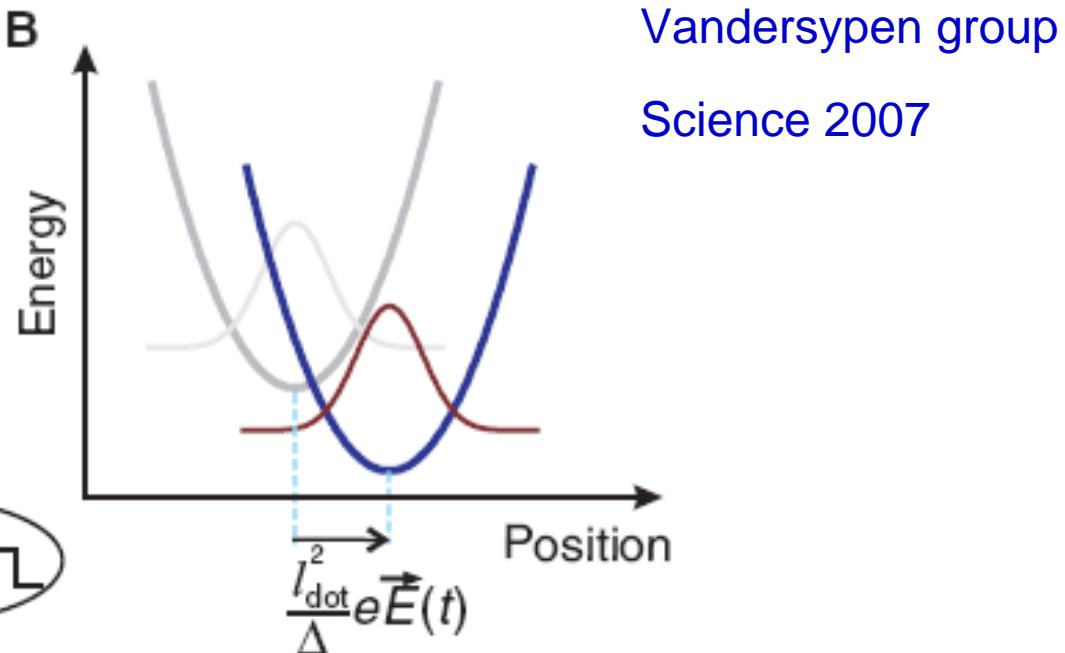
# Ultimate spintronics device: Spin qubits

Taurocha group, Marcus group, Vandersypen group

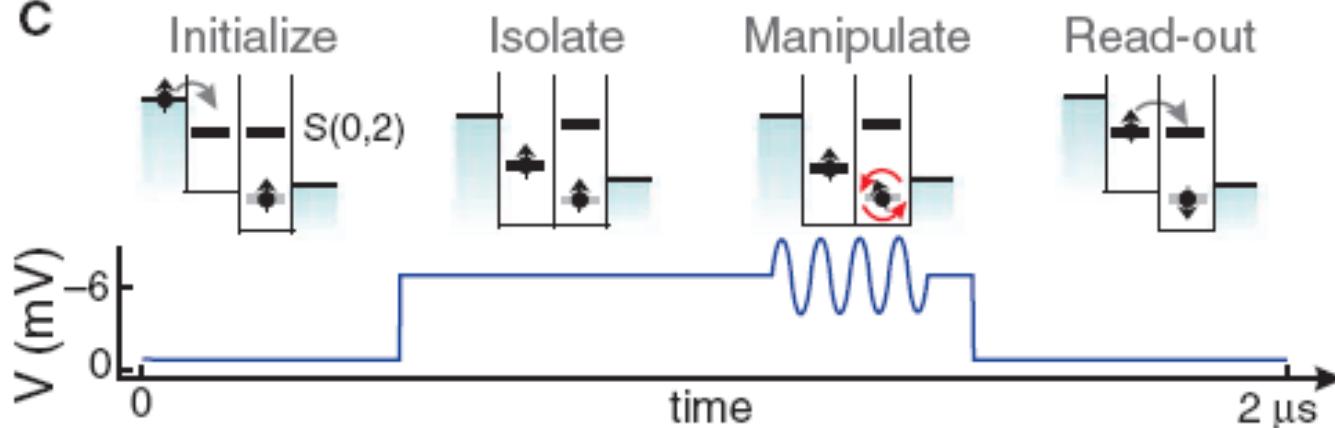
A



B

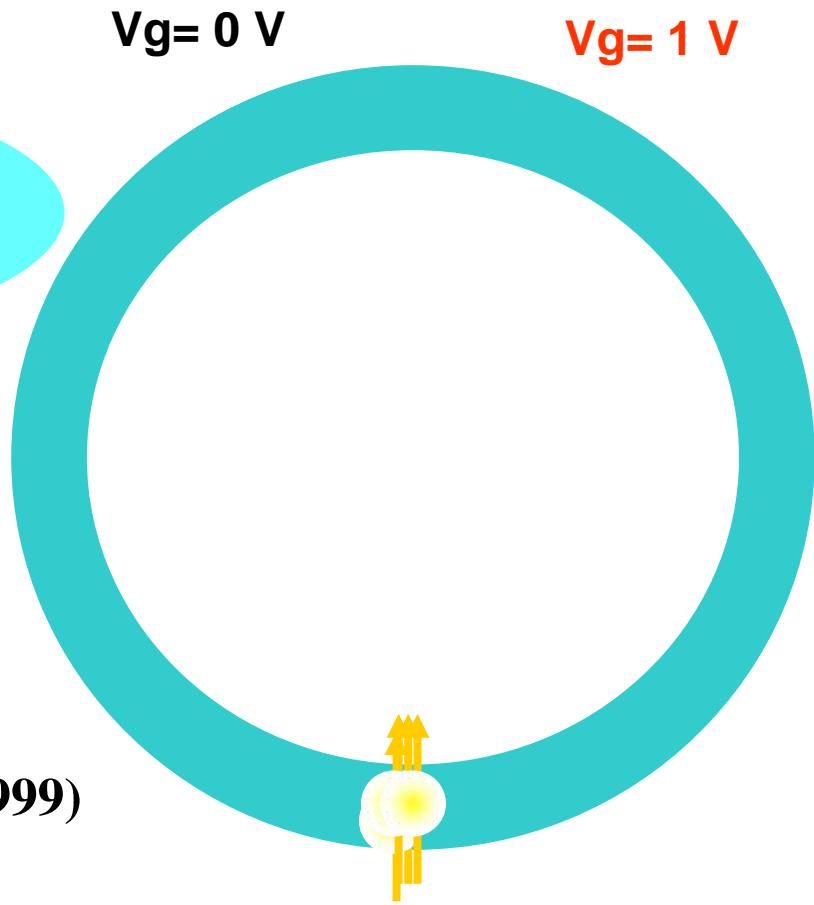
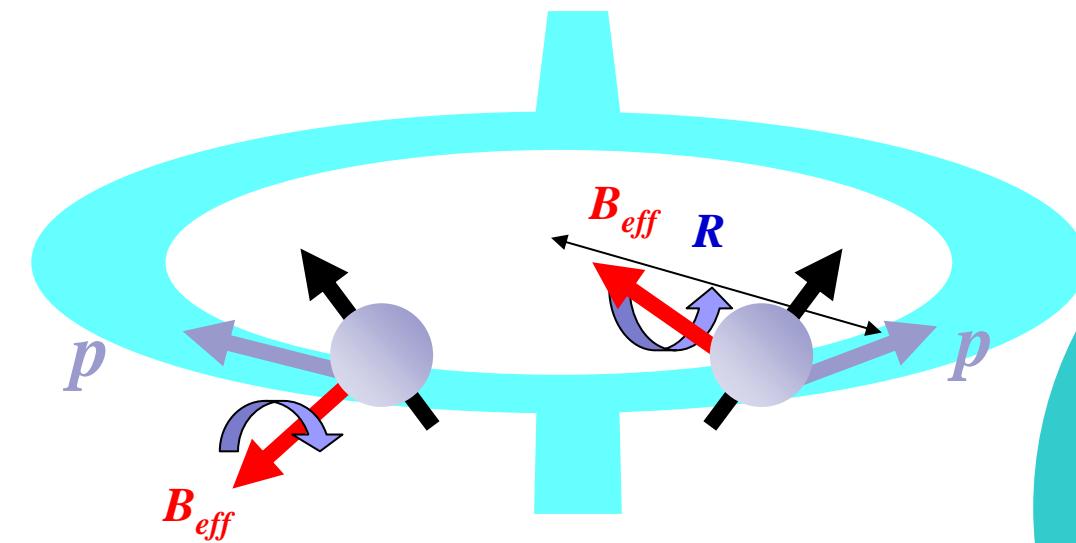


C



# Spin FET via Aharonov-Casher effect

Y. Aharonov and A. Casher, PRL 1984



Spin interference device

Nitta group, Appl. Phys. Lett. 75, 695 (1999)

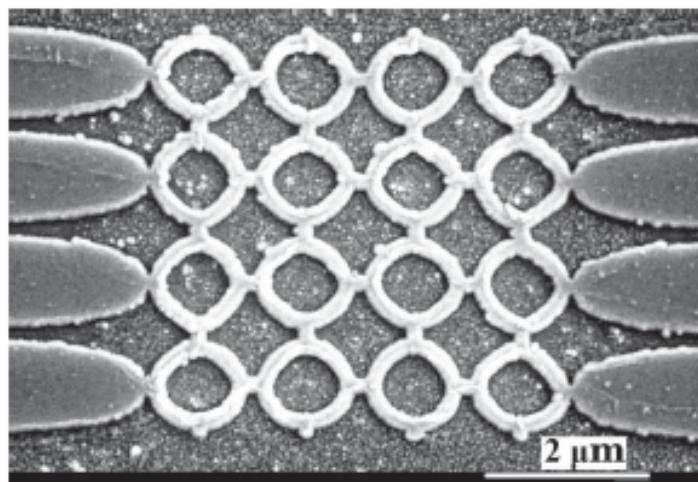
from Nitta's ppt

Ring conductance depends  
on the precession angle

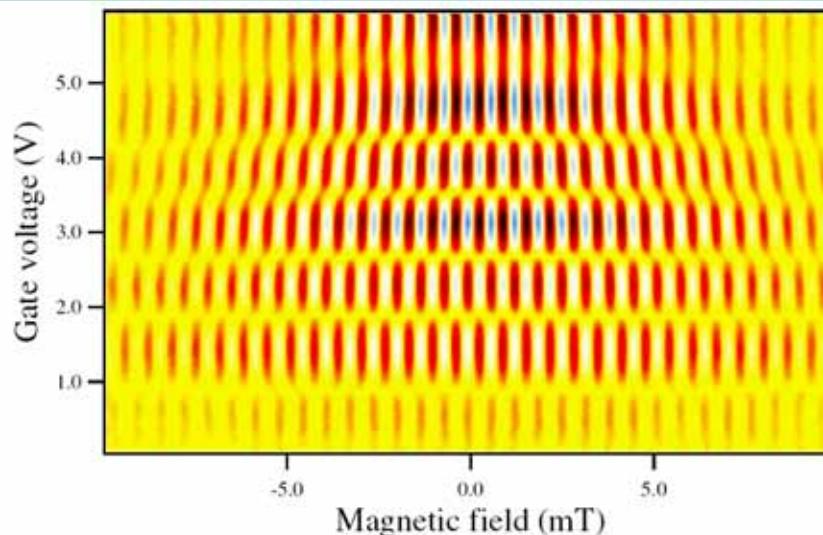
# Previous Experiment on AC effect

- in InAlAs/InGaAs 2DEG (Nitta group)
- in HgTe/HgCdTe 2D TI (Molenkamp group)

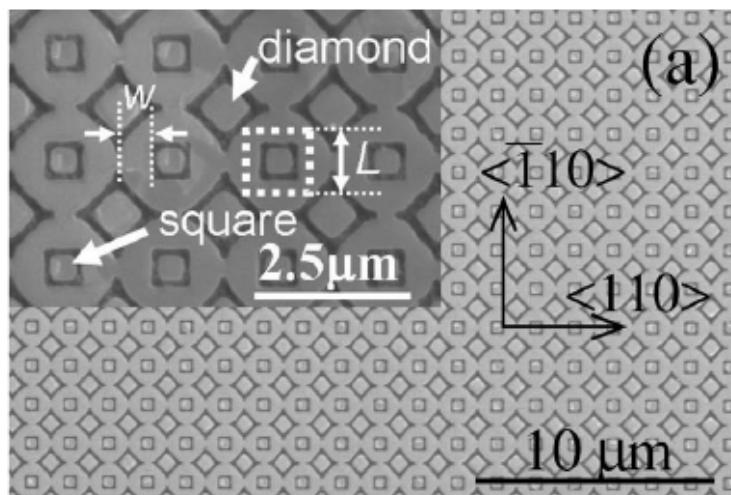
# Aharonov-Casher effect in 2DEG InAlAs/InGaAs



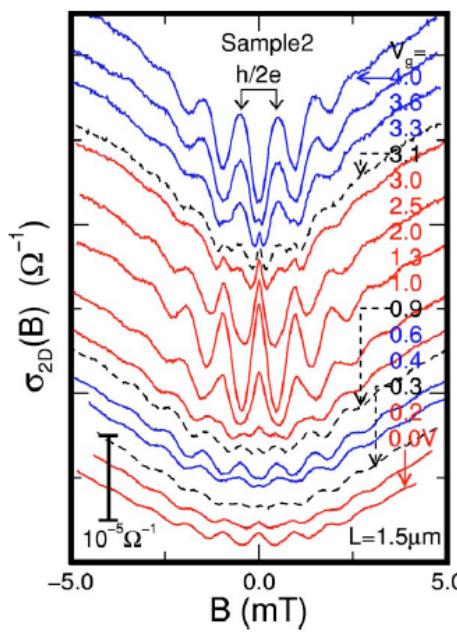
InAlAs/InGaAs



*Nitta group PRL 97,196803(2006)*

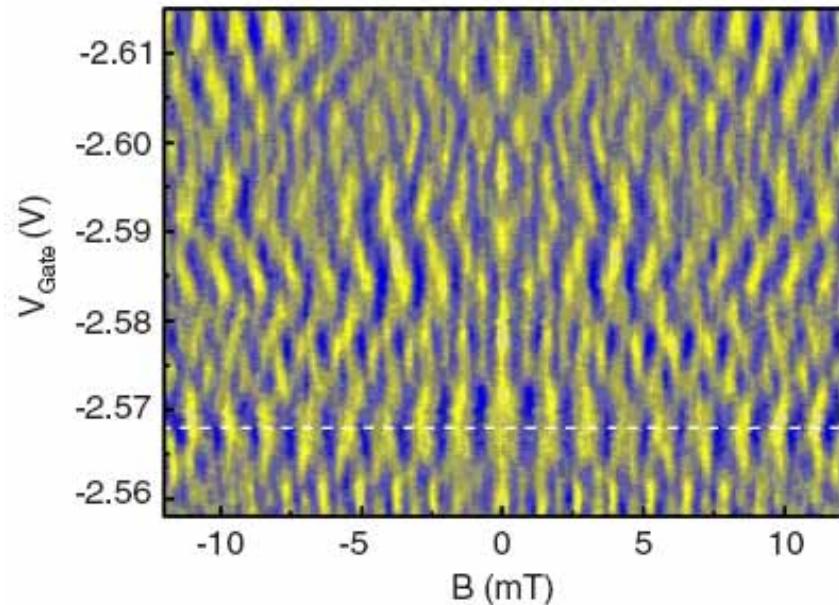
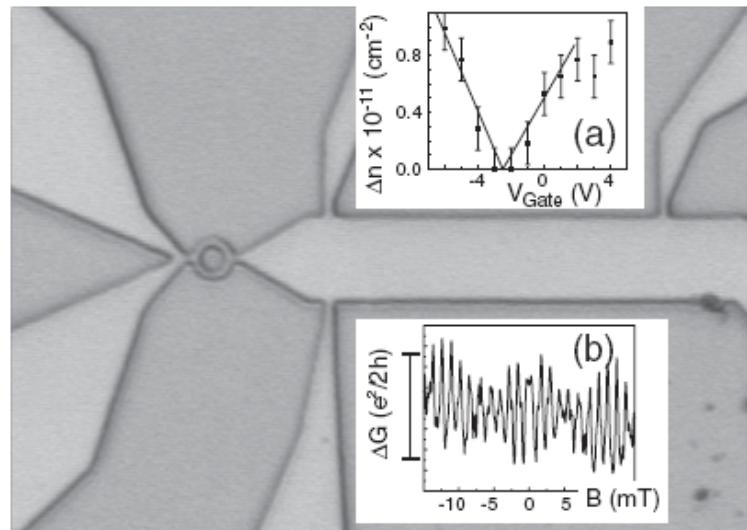


InAlAs/InGaAs



*Nitta group  
PRB 74, 041302(2006)*

# Aharonov-Casher effect in 2D TI HgTe/HgCdTe



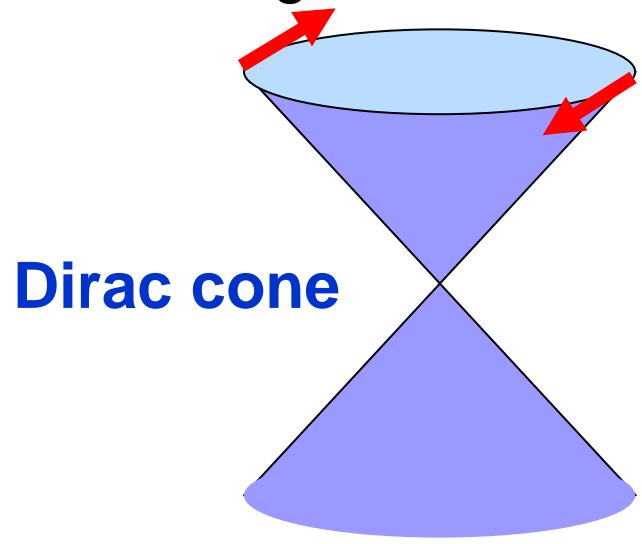
*Molenkamp group PRL 96, 076804(2006)*

# Our Experiment on $\text{Bi}_2\text{Se}_3$ square rings

--- The 1st observation of AC effect on 3D TI

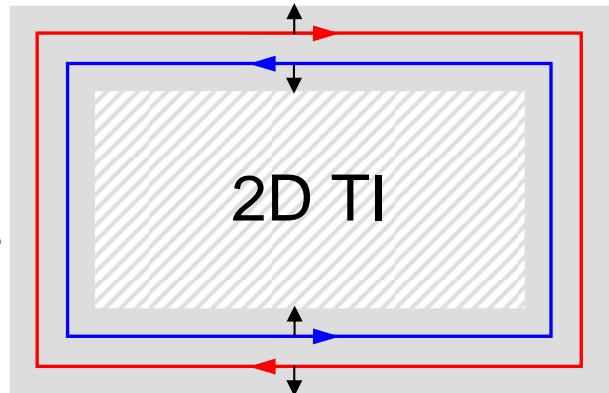
# What is a topological insulator?

insulating bulk + conducting surface/edge



**Dirac cone**

**Helical  
electrons**



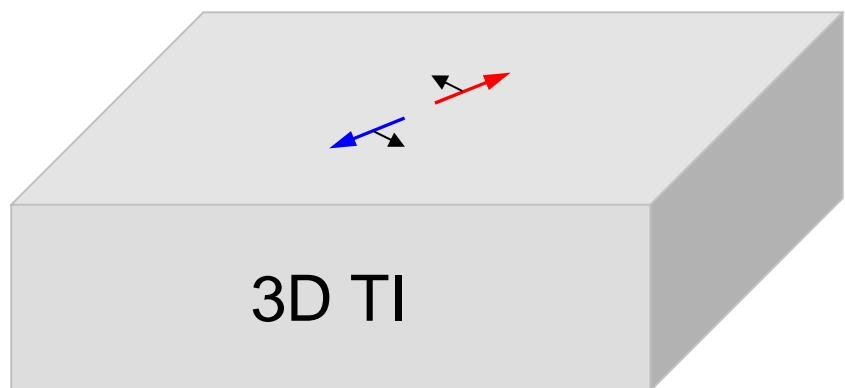
strong SOC



spin-momentum locking

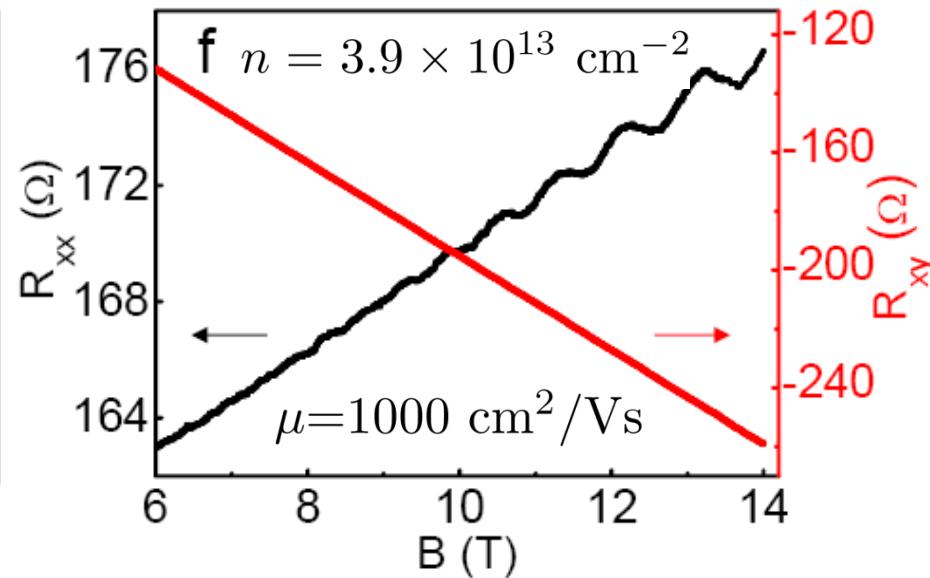
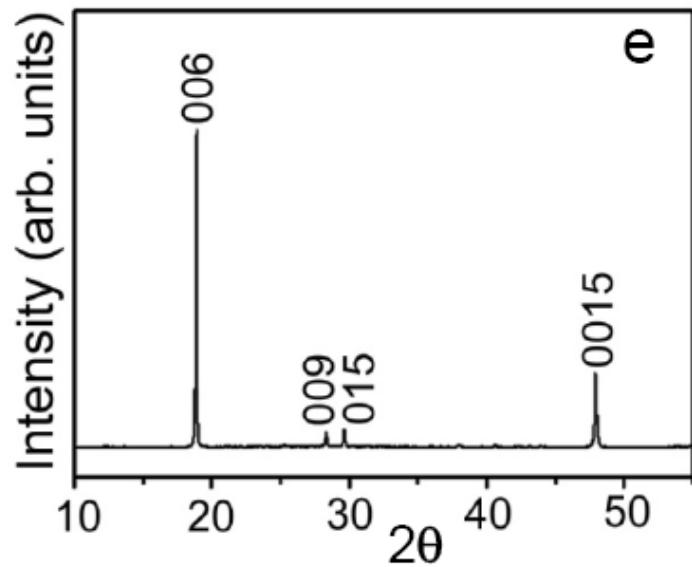
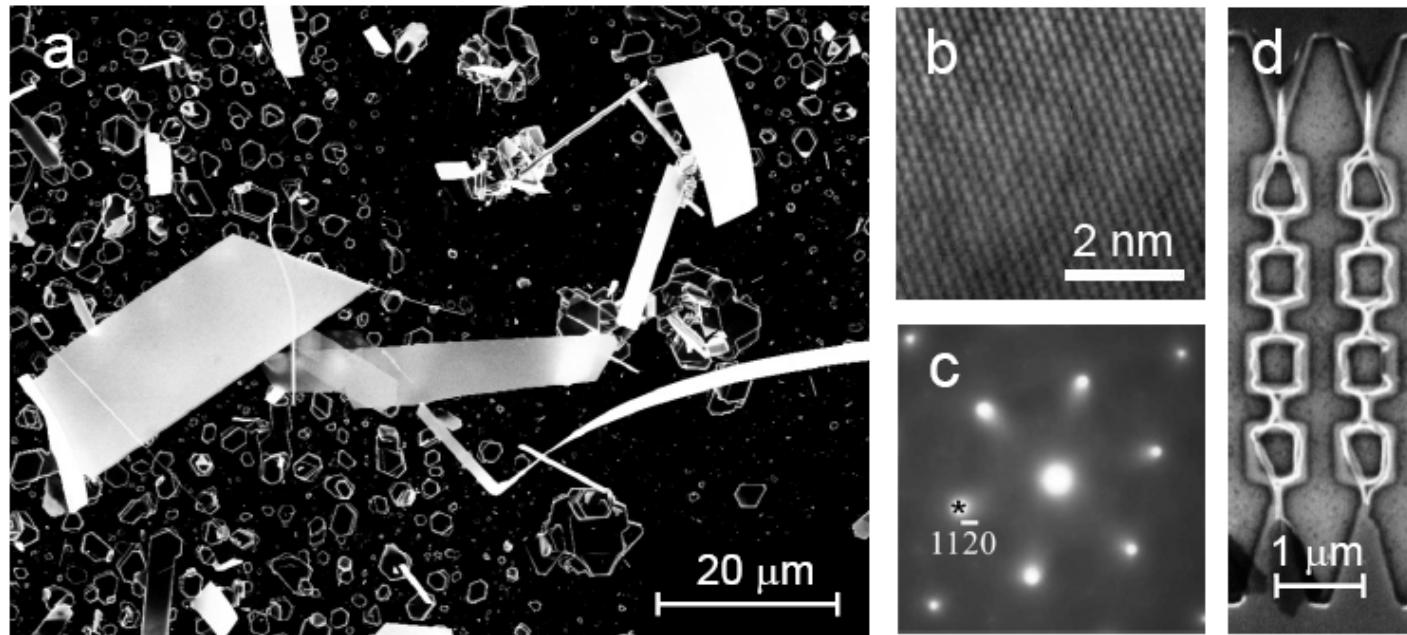


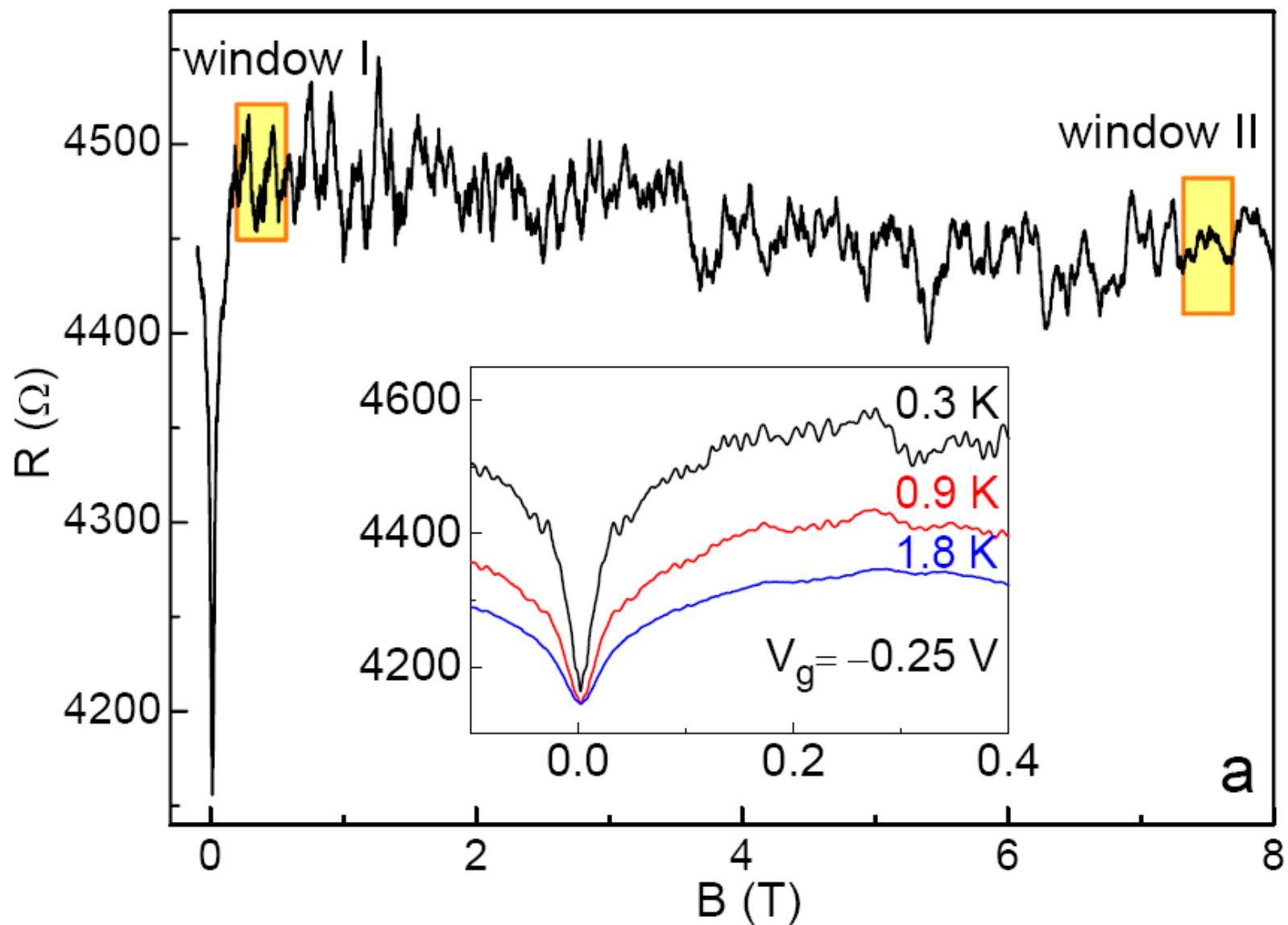
- Band inversion and Dirac cone (momentum space)
- Helical electrons (real space)

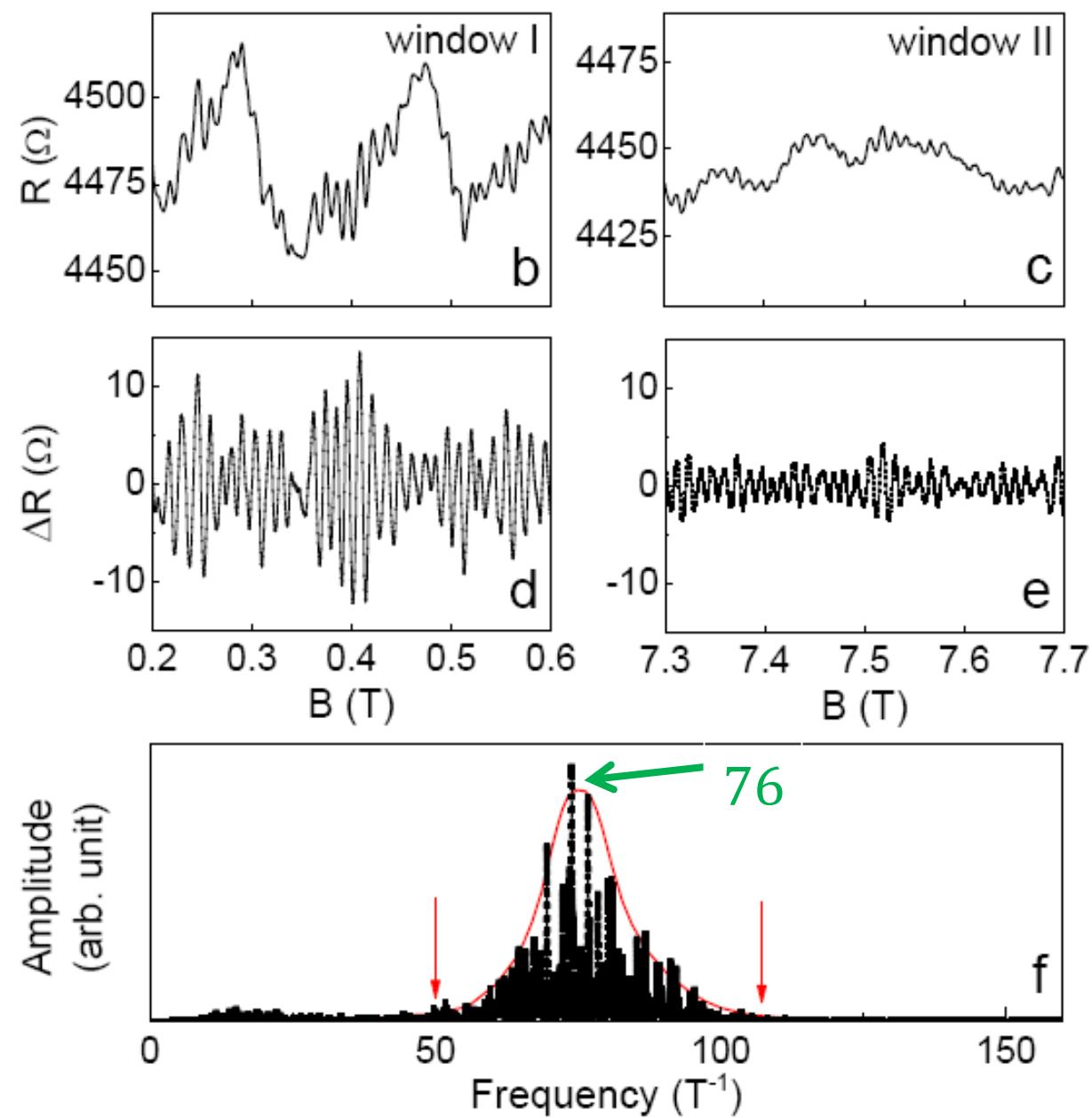


**3D TI**

# Our Experiment on $\text{Bi}_2\text{Se}_3$ square rings



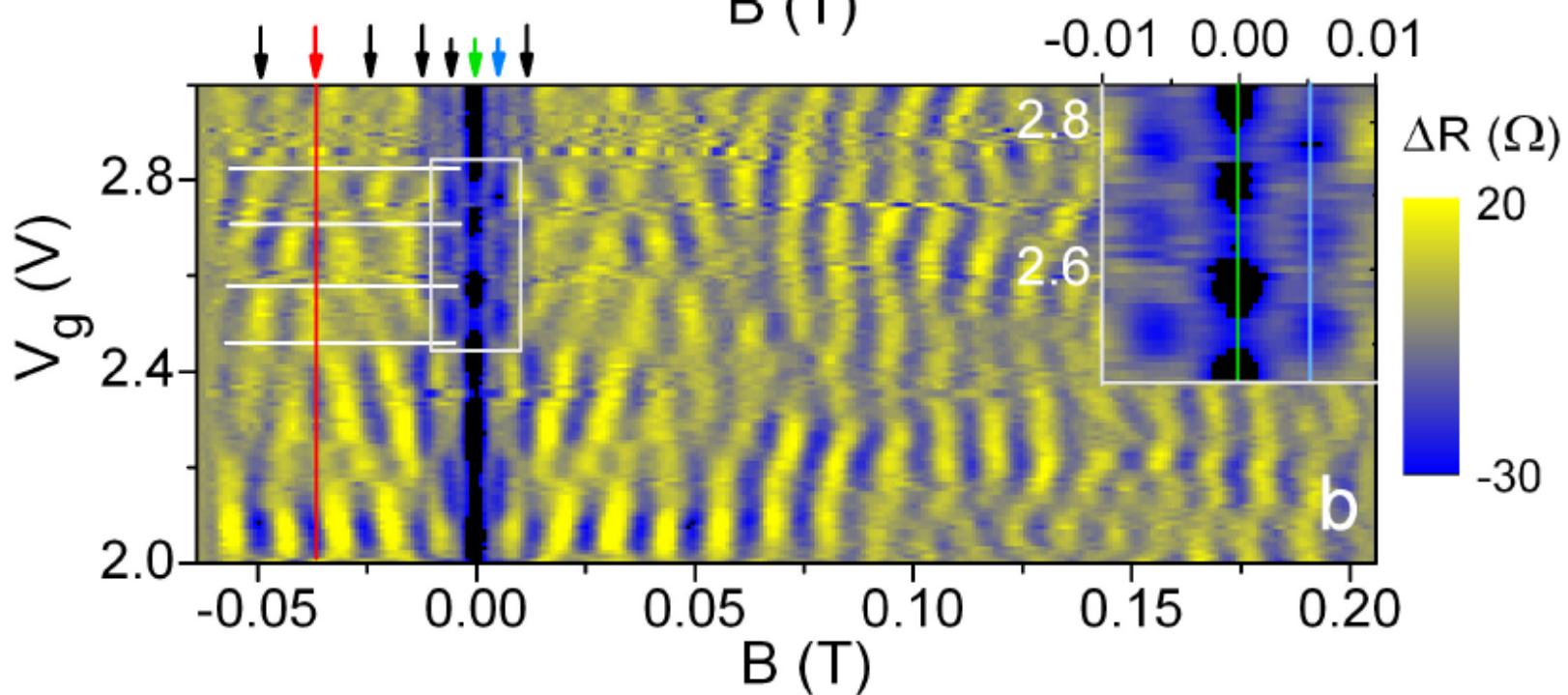
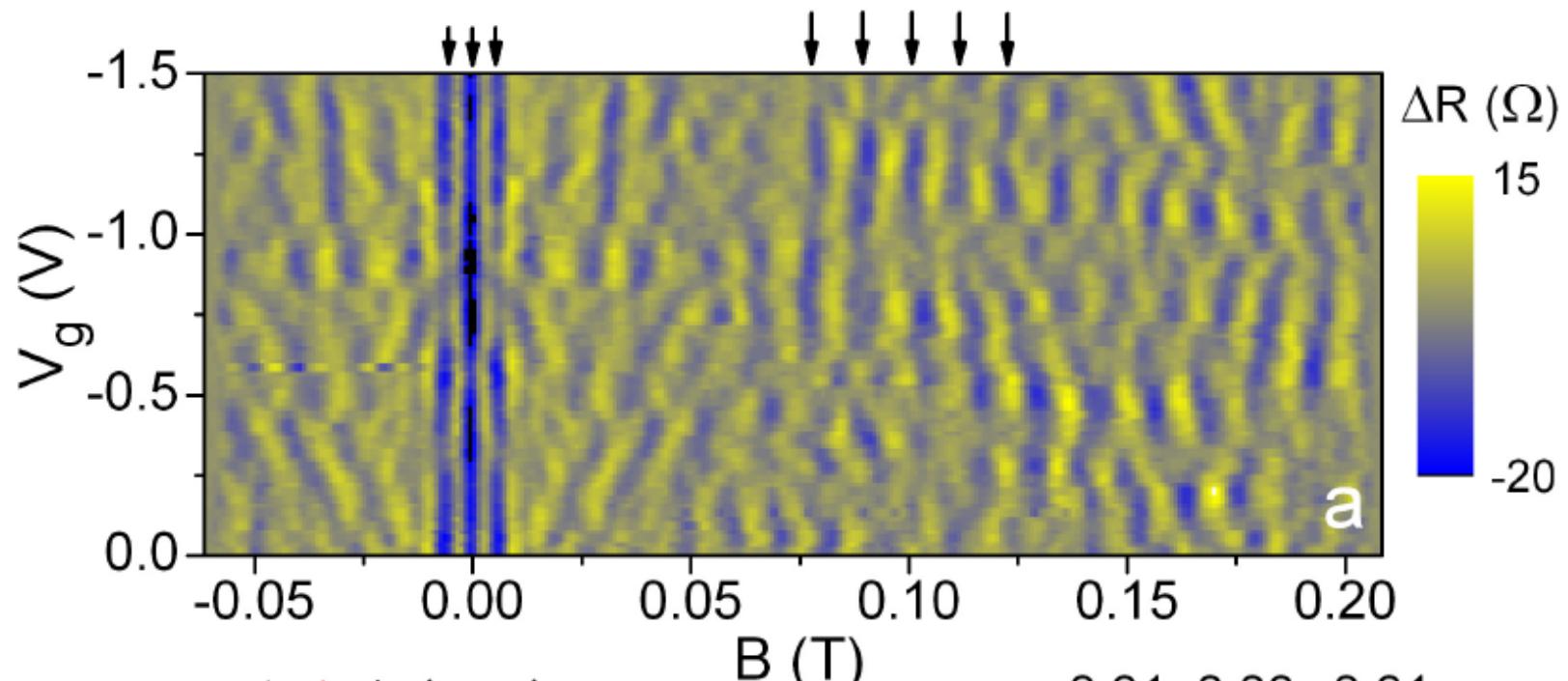


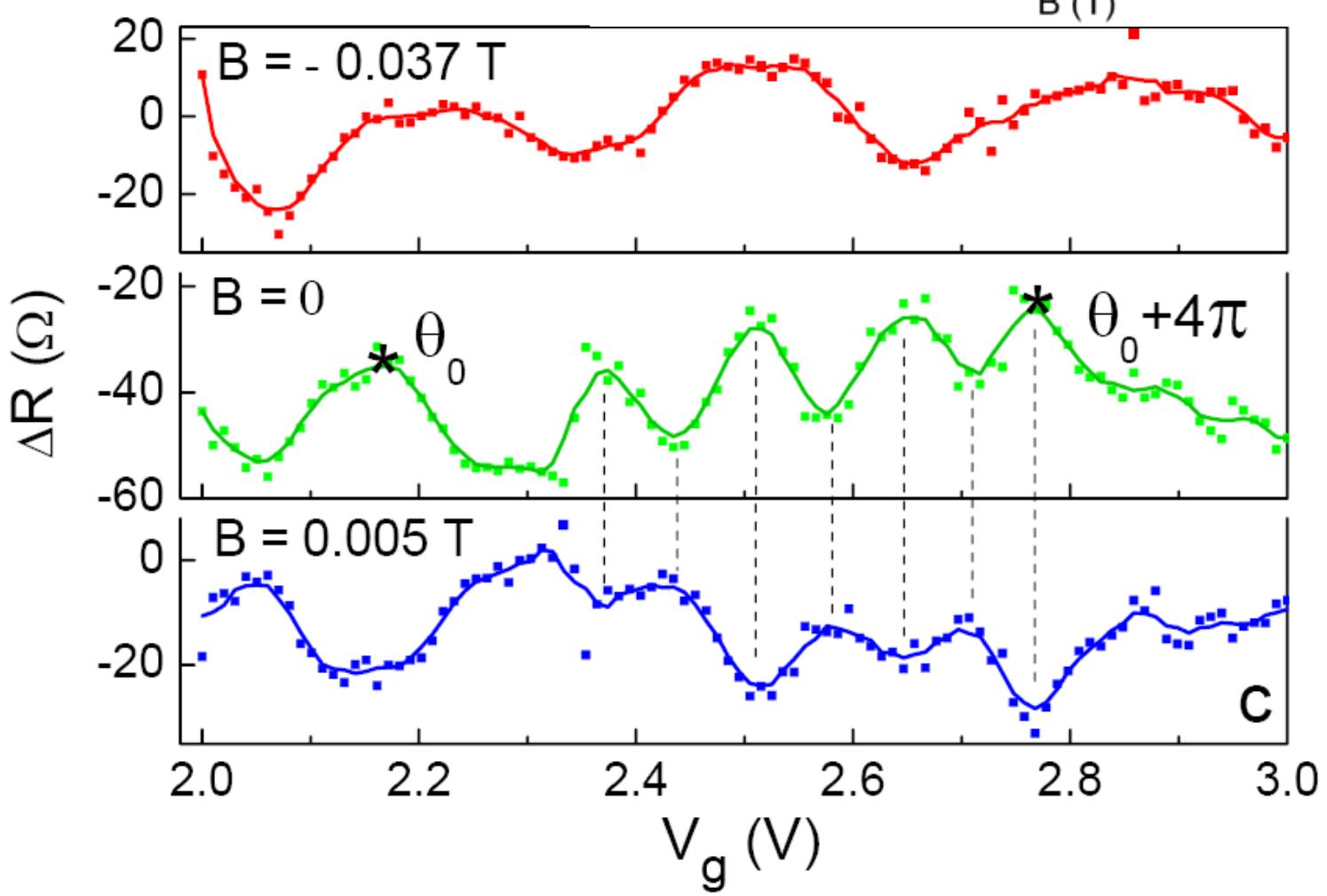
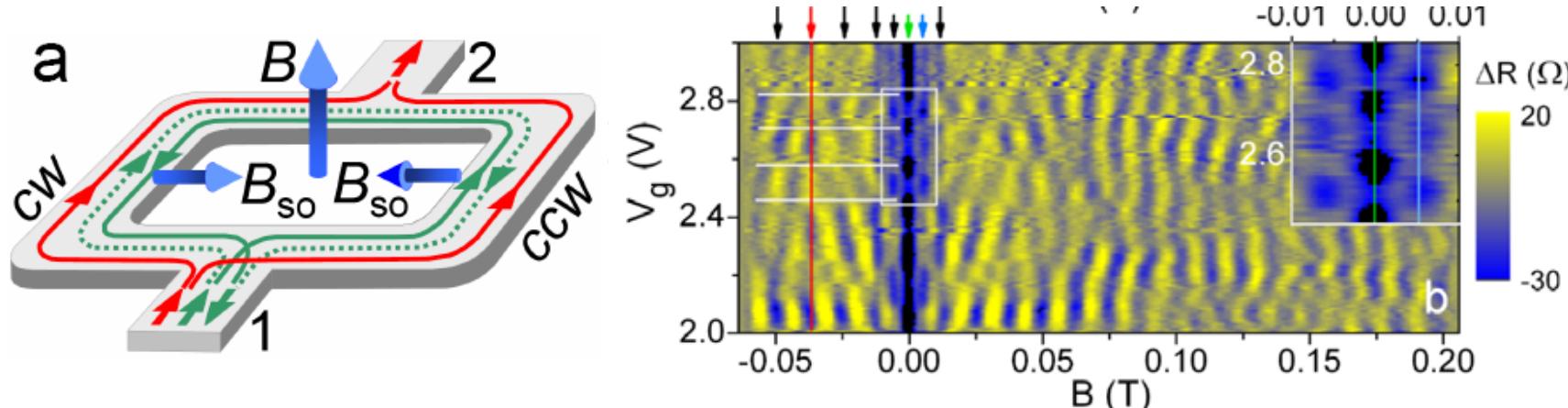


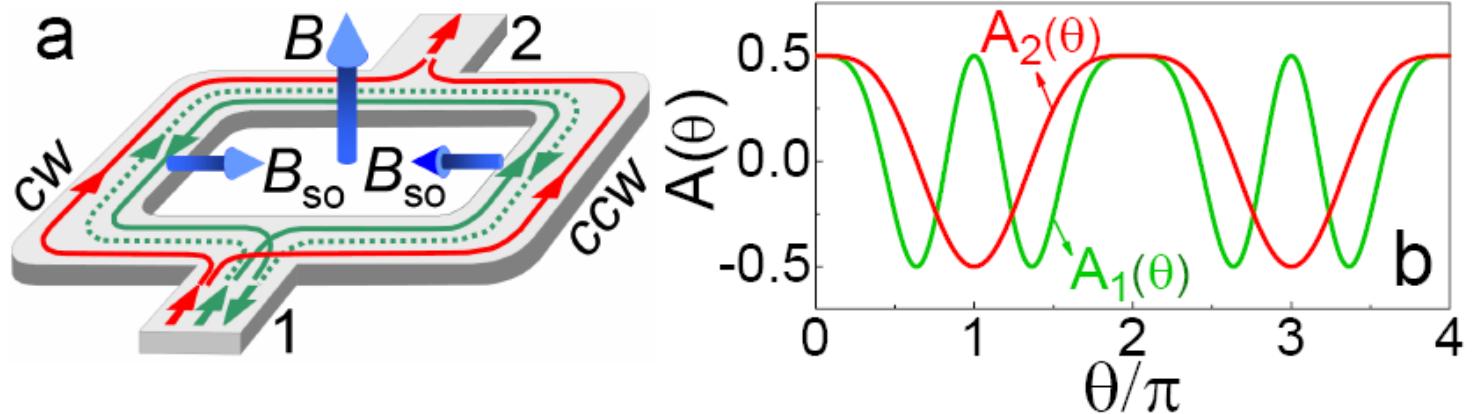
$S = 560 \text{ nm} \times 560 \text{ nm}$

$(\Delta B)^{-1} = S/\phi_0 = 75 \text{ T}^{-1}$

Width of the ring: 120 nm







AAS type

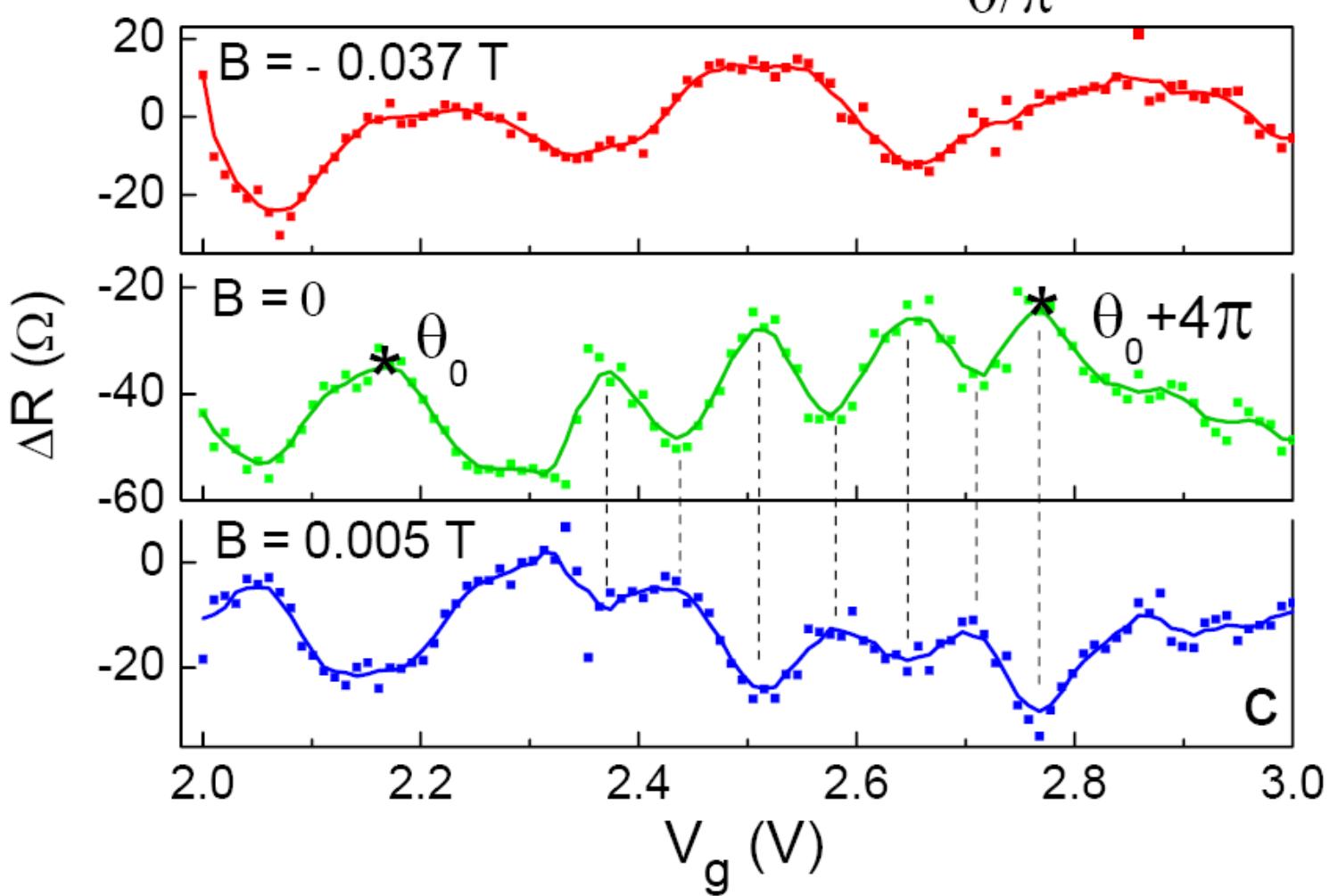
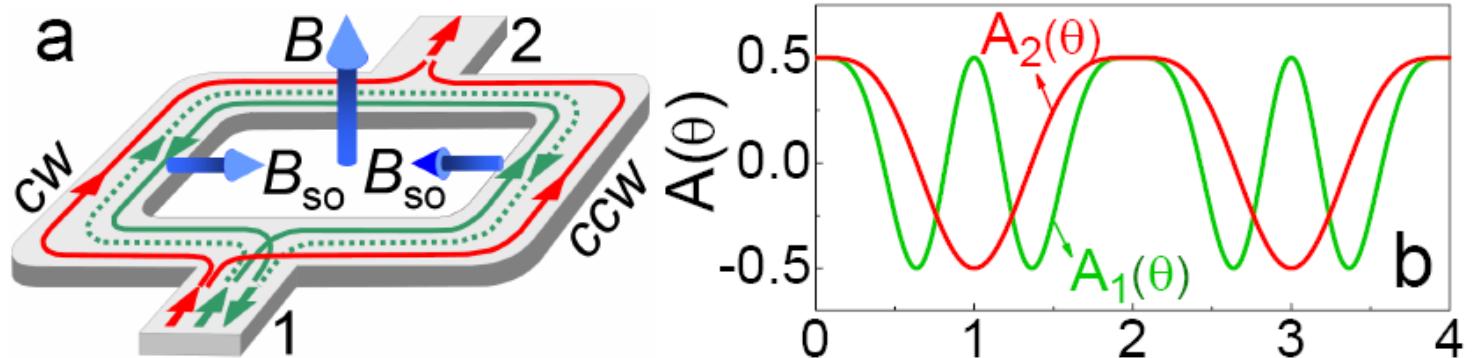
$$\begin{aligned} \overline{\langle \Psi | \Psi \rangle} &= \frac{1}{2} + \frac{1}{4} (\cos^4 \theta + 4 \cos \theta \sin^2 \theta + \cos 2\theta) \cos \phi_1 \\ &\equiv \frac{1}{2} + A_1(\theta) \cos \phi_1 \quad \phi_1 = 2eBL^2 / \hbar \end{aligned}$$

*Nitta group, PRB 70, 161302(2004)*

AB type

$$\begin{aligned} \overline{\langle \Psi | \Psi \rangle} &= \frac{1}{2} + \frac{1}{4} (\sin^2 \theta + 2 \cos \theta) \cos \phi_2 \\ &\equiv \frac{1}{2} + A_2(\theta) \cos \phi_2 \quad \phi_2 = eBL^2 / \hbar \end{aligned}$$

*X. C. Xie group, PRB 74, 085327(2006)*



# The tunability of the Spin-FET

$$\Delta\theta/\Delta V_g = 6.6\pi/V$$

$$\theta = 2\alpha m^* L/\hbar^2$$

$$\Delta\alpha/\Delta V_g = (\hbar^2/2m^*)\Delta\theta/L\Delta V_g = 11(\text{peVm})/V$$

The tunability in our device is the highest:

- an order of magnitude larger than that of InAlAs/InGaAs devices;
- more than two times larger than that of HgTe/HgCdTe devices.

# Conclusion of Part I

- $\text{Bi}_2\text{Se}_3$  - A good candidate with large SOC for constructing spintronics devices.
- AC effect - A powerful tool to control spin interference.

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square-ring interferometers

Part II:

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on the surfaces of  $\text{Bi}_2\text{Te}_3$

## Students:



Jie Shen

Yue Ding

Yuan Pang

Fanming Qu Fan Yang Jun Chen

J.Y. Feng, J.H. Wang, ....

## Colleagues:

- Changli Yang
- Zhongqing Ji
- Xiunian Jing
- Yongqing Li
- Jie Fan
- Guangtong Liu

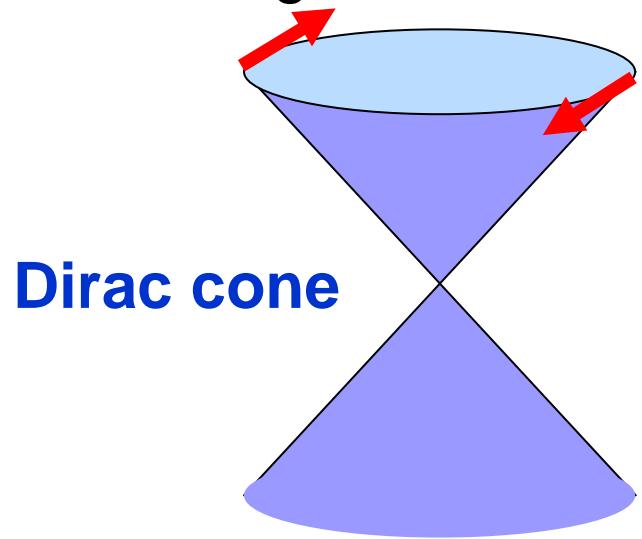
## Thanks:

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- Z. Fang
- R. Du
- X. Dai
- S.Y. Han
- G. M. Zhang
- S. P. Zhao
- X. C. Xie
- L. Yu



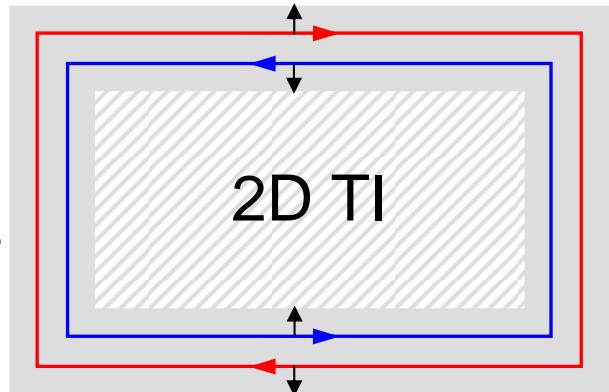
# What is a topological insulator?

insulating bulk + conducting surface/edge



**Dirac cone**

**Helical  
electrons**



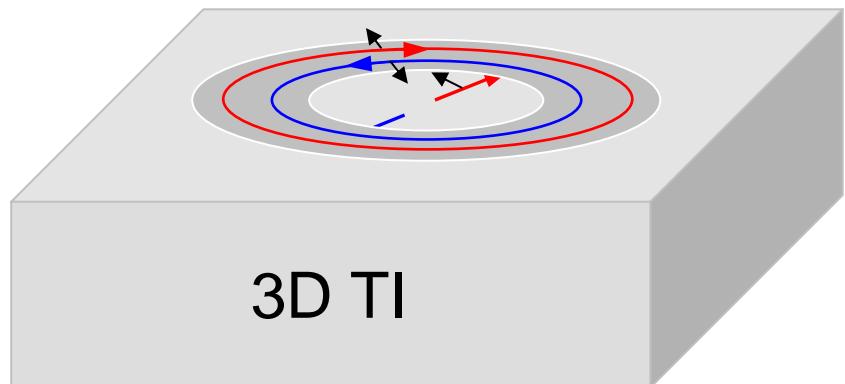
strong SOC



spin-momentum locking

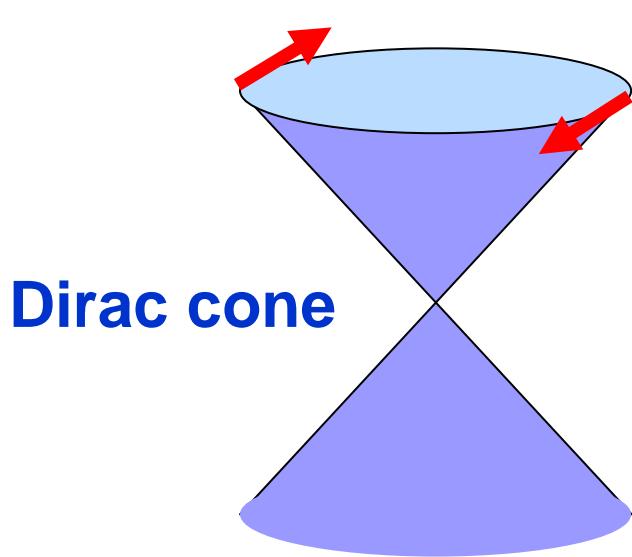


- Band inversion and Dirac cone (momentum space)
- Helical electrons (real space)

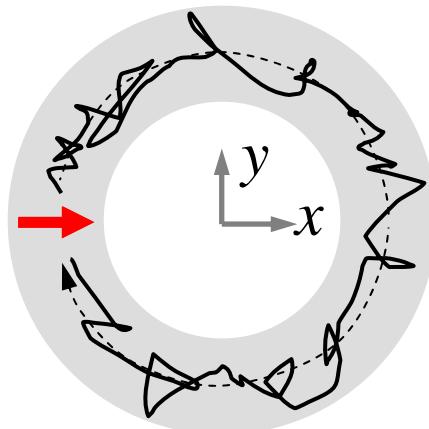


**3D TI**

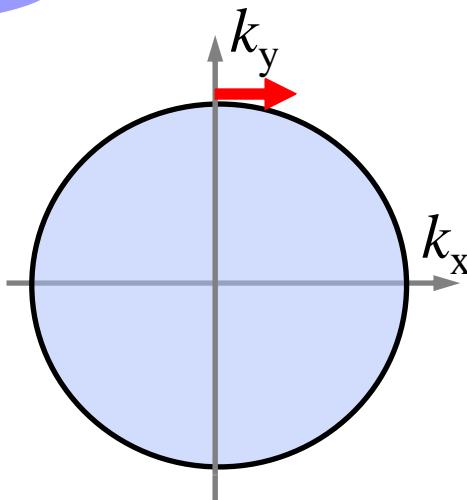
# $\pi$ Berry phase



Dirac cone



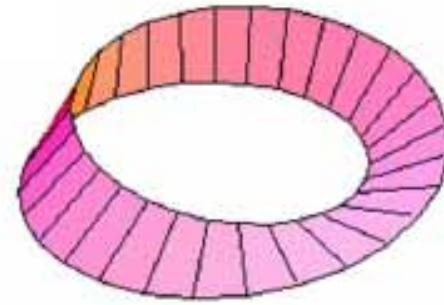
real space



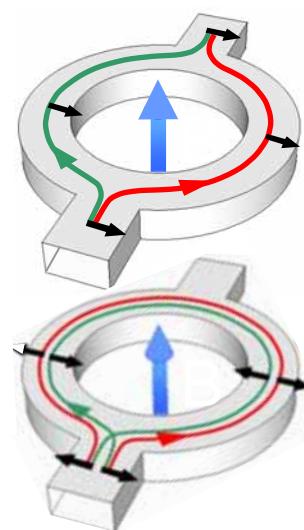
momentum space

## Consequences:

- ✓ Suppression of back-scattering
- ✓ Weak anti-localization
- ✓ ....

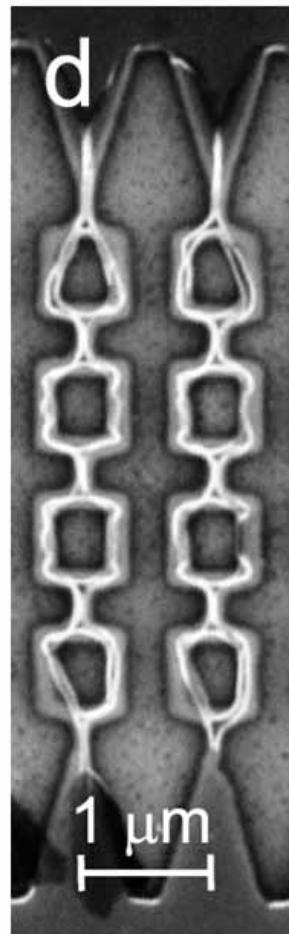


# Altshuler-Aronov-Spivak, Aharonov-Bohm, and Aharonov-Casher effects

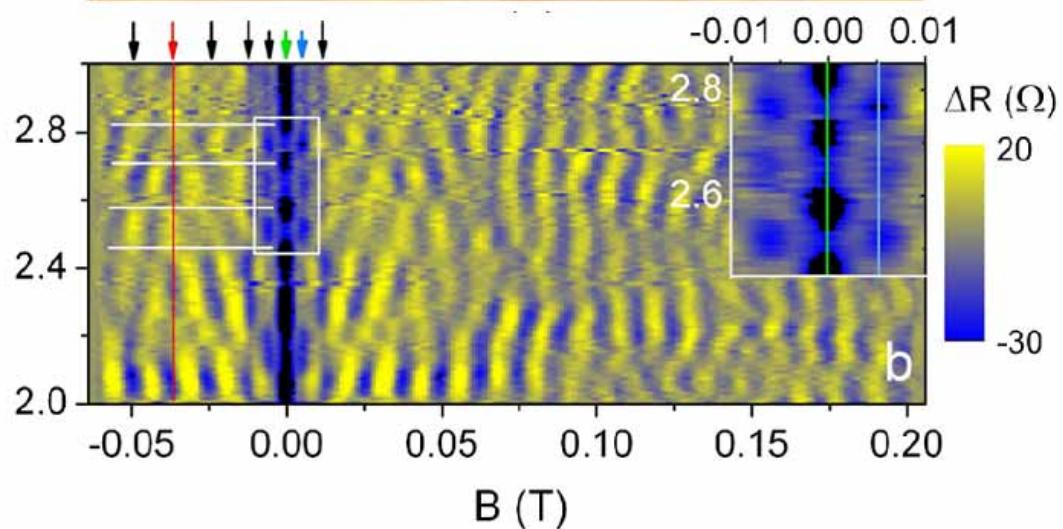


AB

AAS

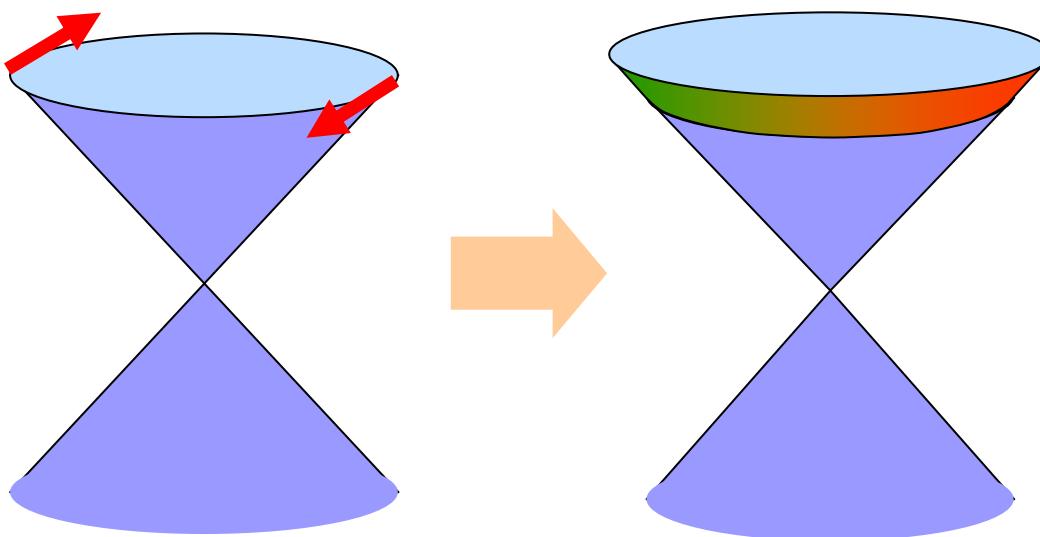


$\Sigma_g >$



F. M. Qu, et al., PRL'2011

# When helical electrons pair up ...

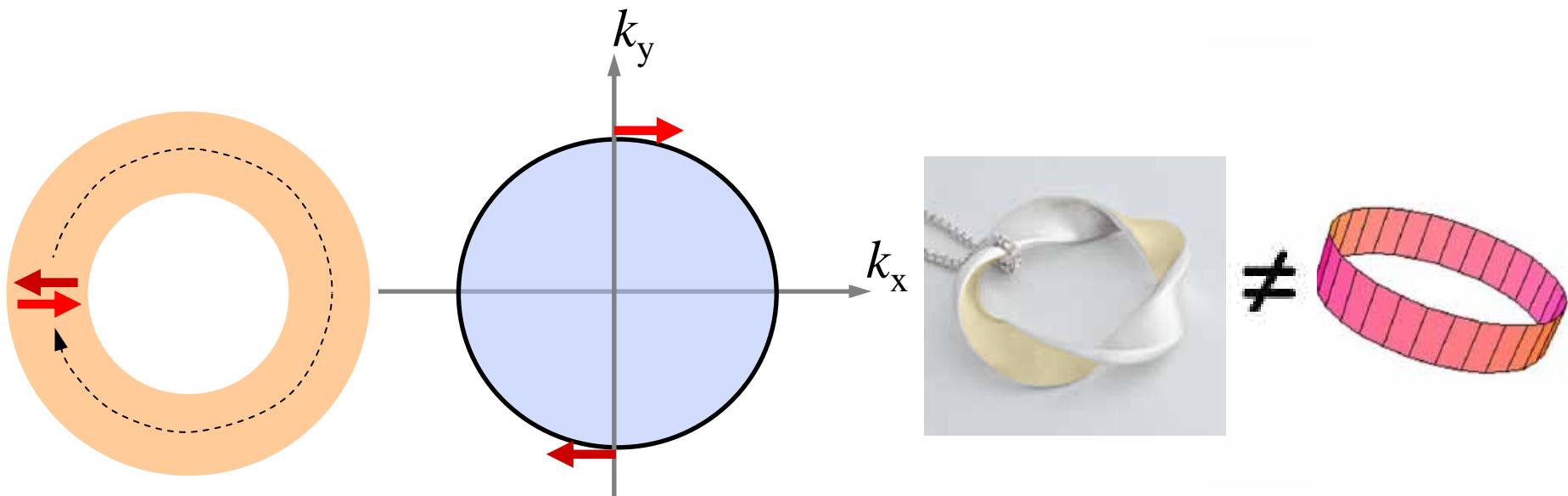
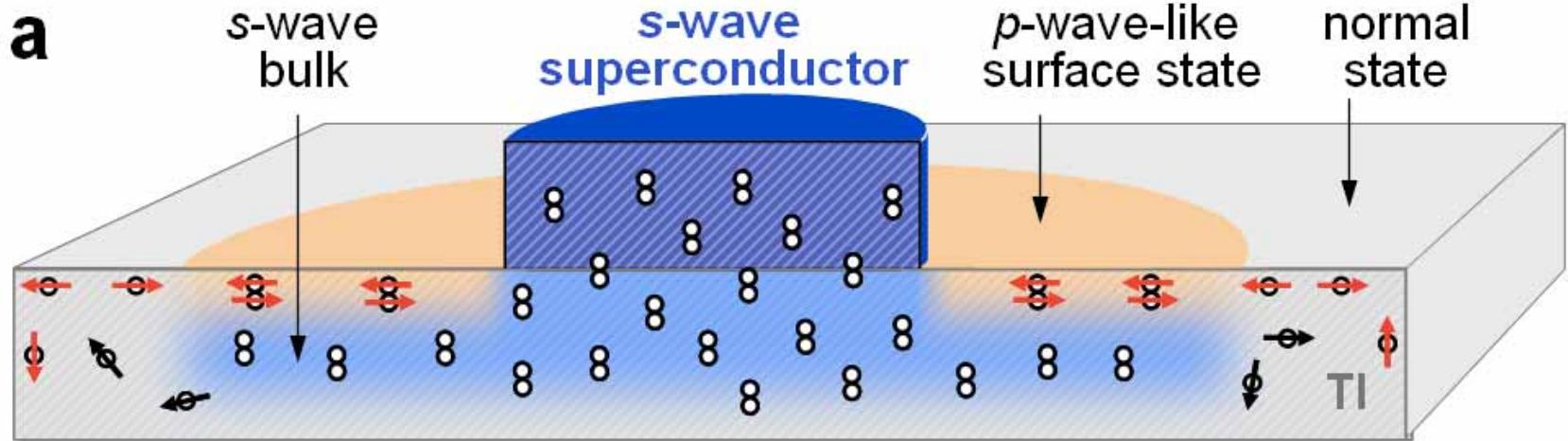


Fu & Kane (PRL 2008):

resembling a spinless  $p_x+ip_y$ -wave superconductor

$$\Delta(r, \theta) = \Delta_0(r)e^{\pm i\theta}$$

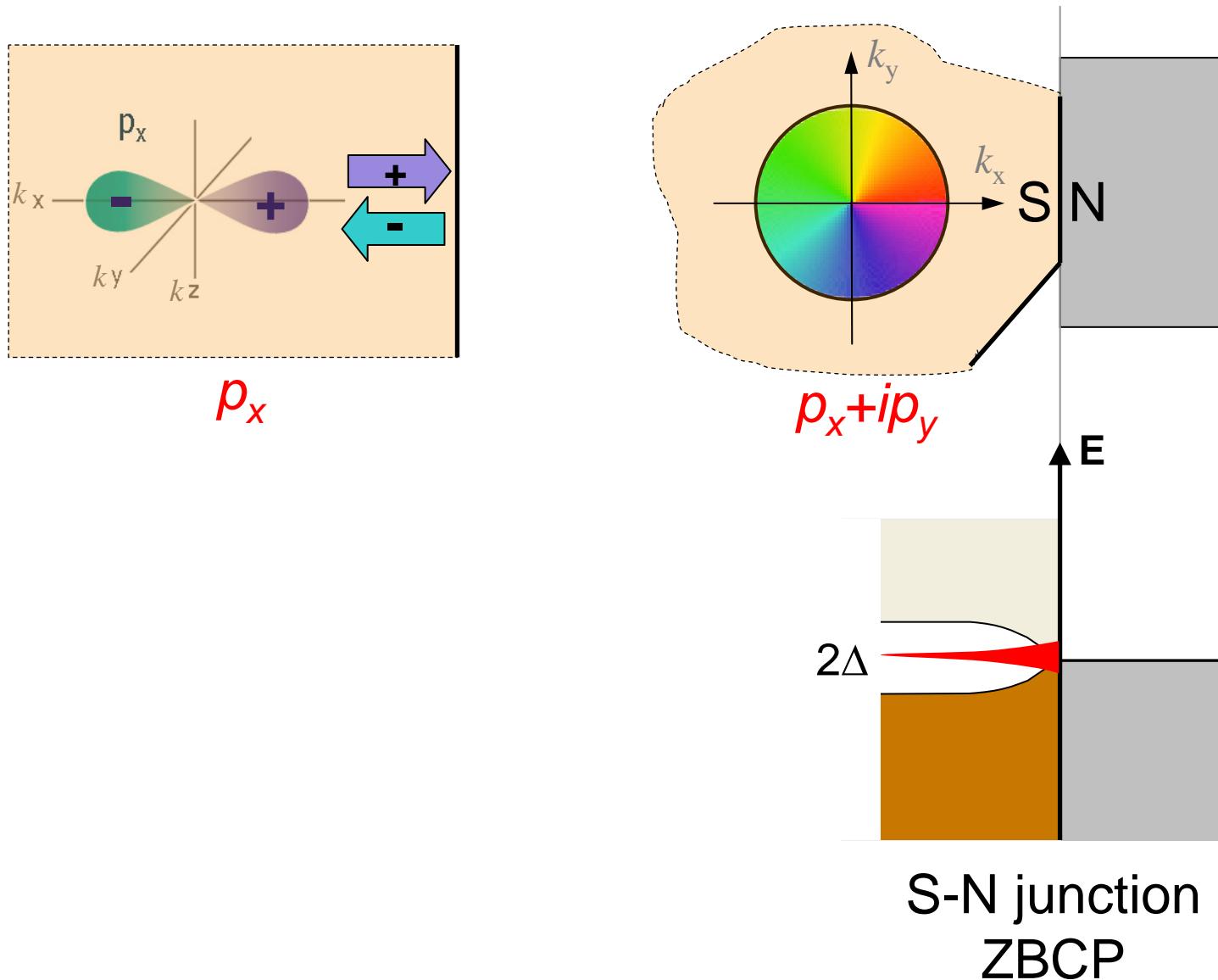
# $2\pi$ Berry phase



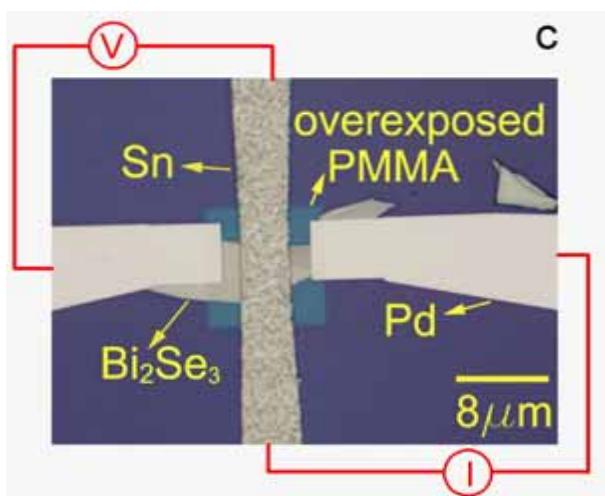
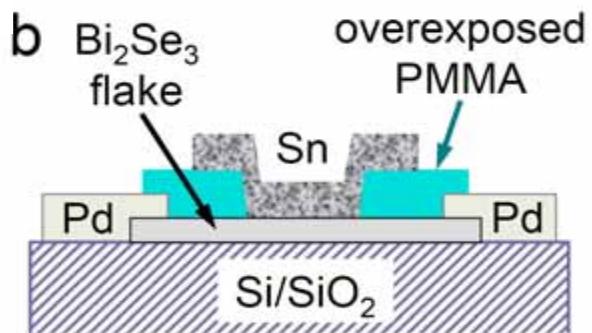
$$\Psi = \Psi_{\text{mass center}} \cdot \Psi_{\text{relative}}$$

$2\pi$  Berry phase, p-like

# Zero-bias conductance peak (ZBCP) at S-N interface

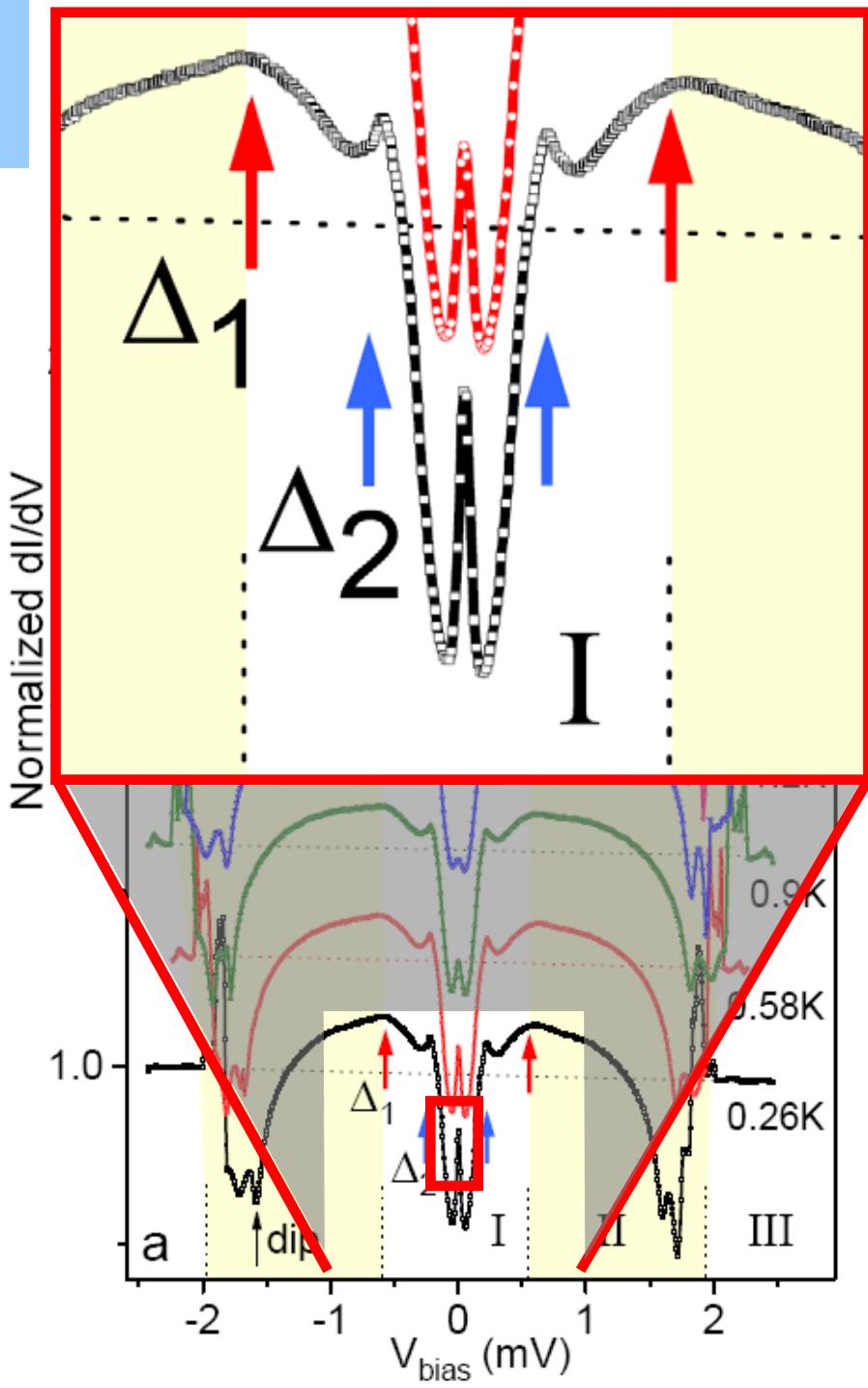


# Observation of Zero-bias conductance peak



More than a dozen of devices were studied

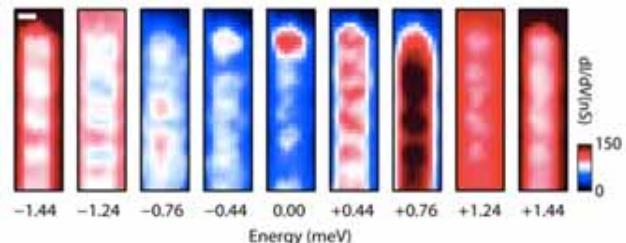
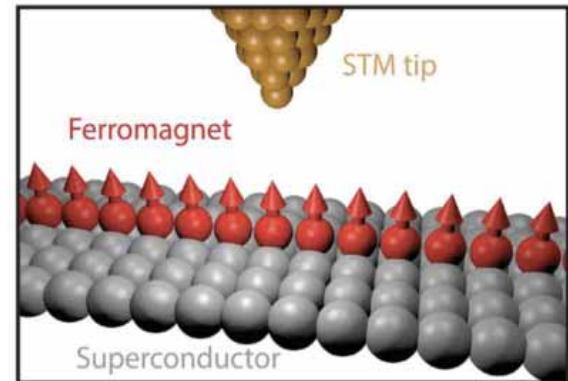
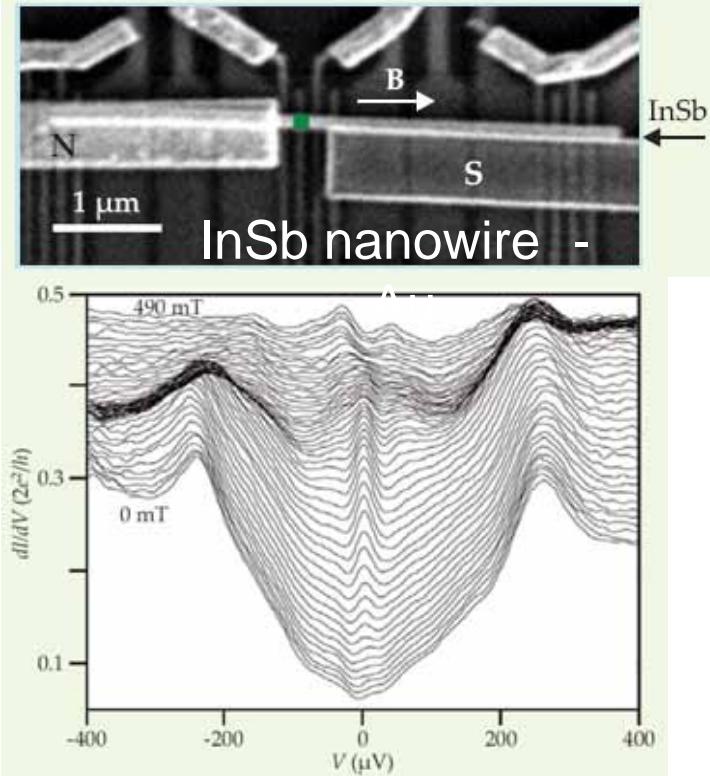
F. Yang, et al.,  
arXiv:1105.0229v1, PRB' 2012



# More ZBCPs

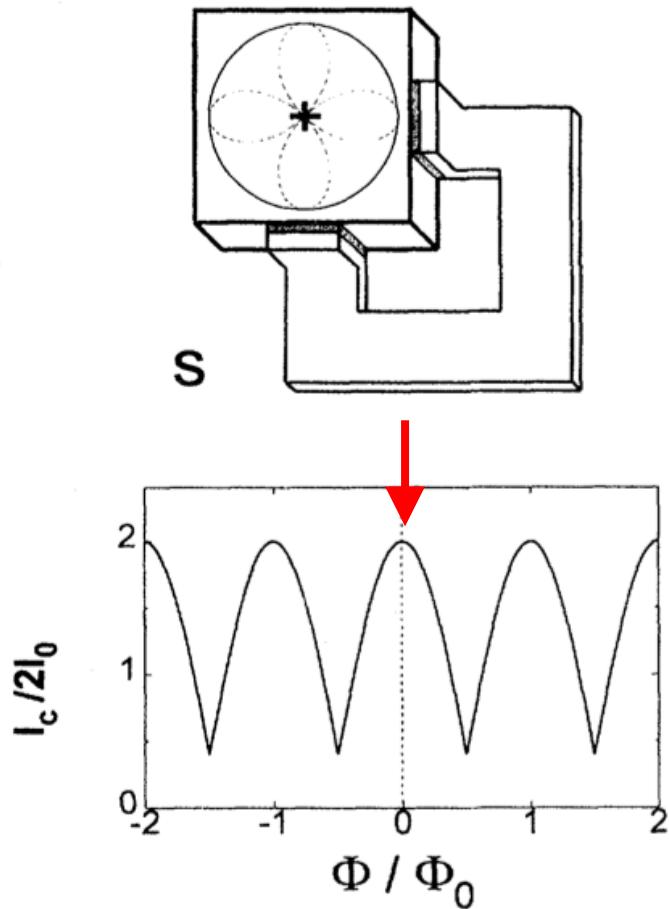
- Ando group  
 $\text{Cu}_x\text{Bi}_2\text{Se}_3$ , PRL 2011
- Jia/Xue groups  
vortex core, Science 2012
- Kouwenhoven group  
1D wire, Science 2012
- Xu group  
1D wire, Nano Lett. 2012
- Yazdani Group  
1D Fe chain on Pb, Science 2014

Having a ZBCP is  
necessary but not sufficient  
for *p*-wave-like SC / MBS

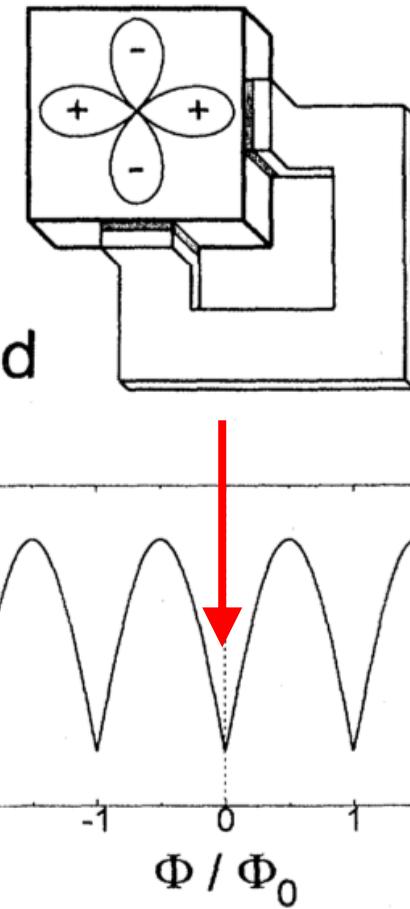


# Phase-sensitive experiment (van Harlingen)

0-loop

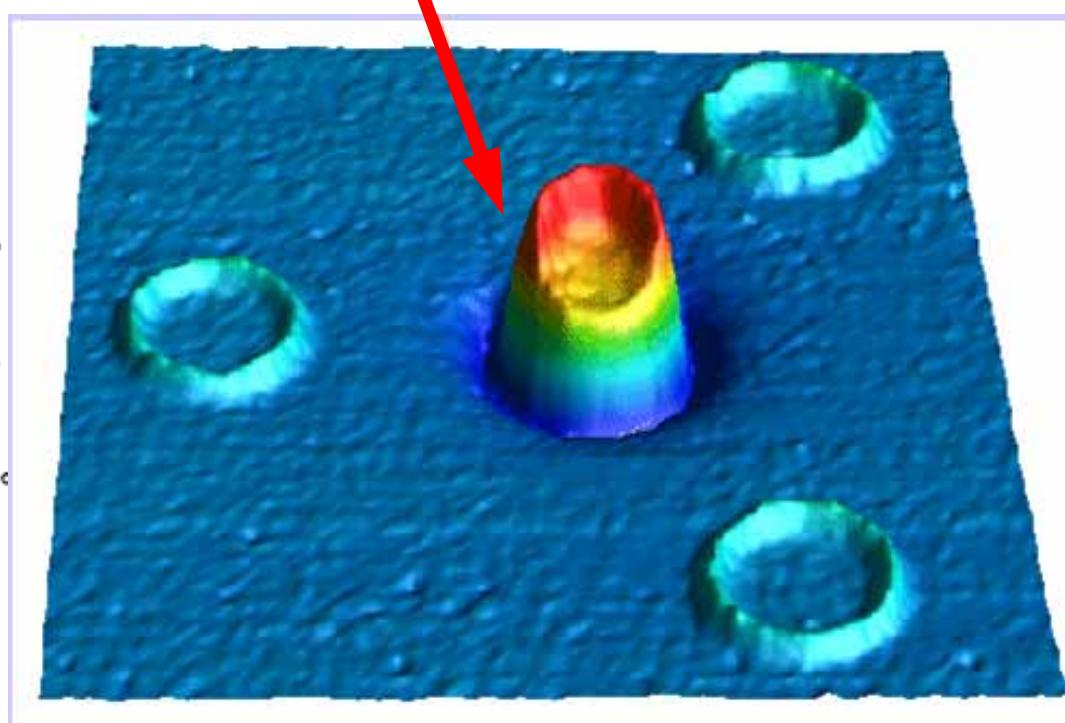
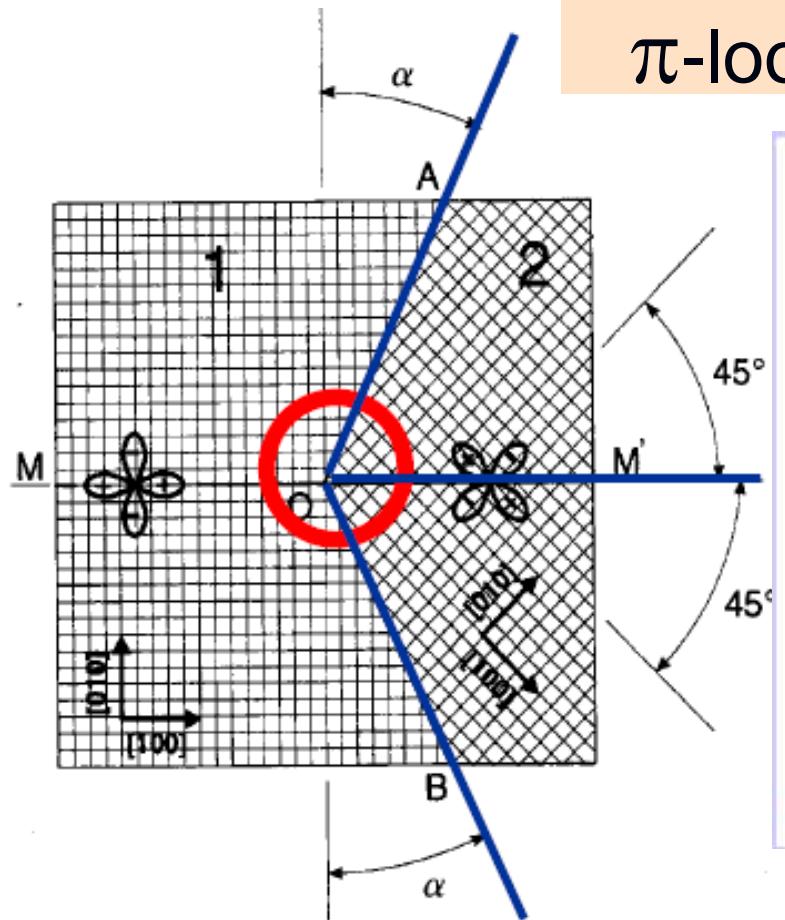


$\pi$ -loop

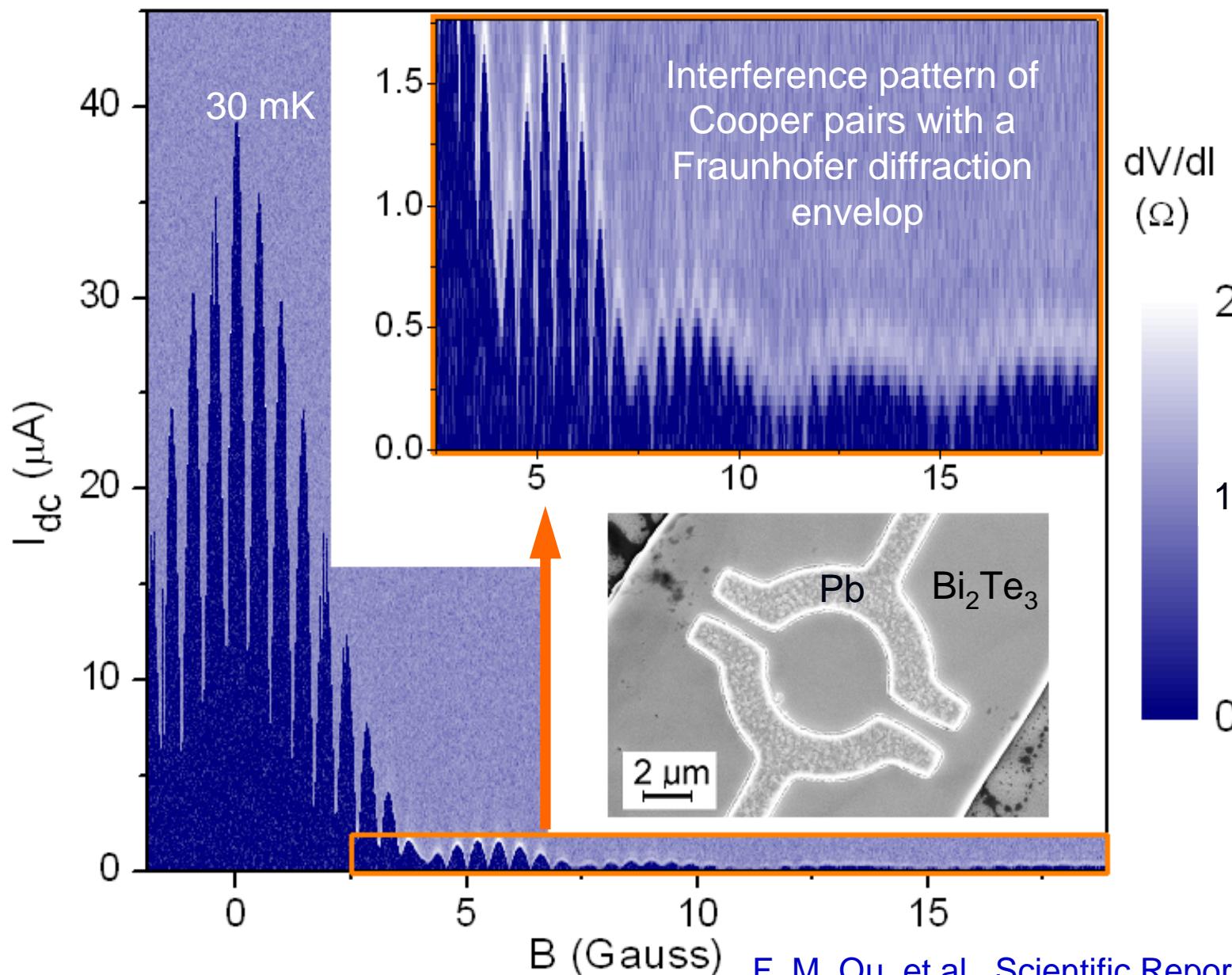


# Phase-sensitive experiment (C.C. Tsuei)

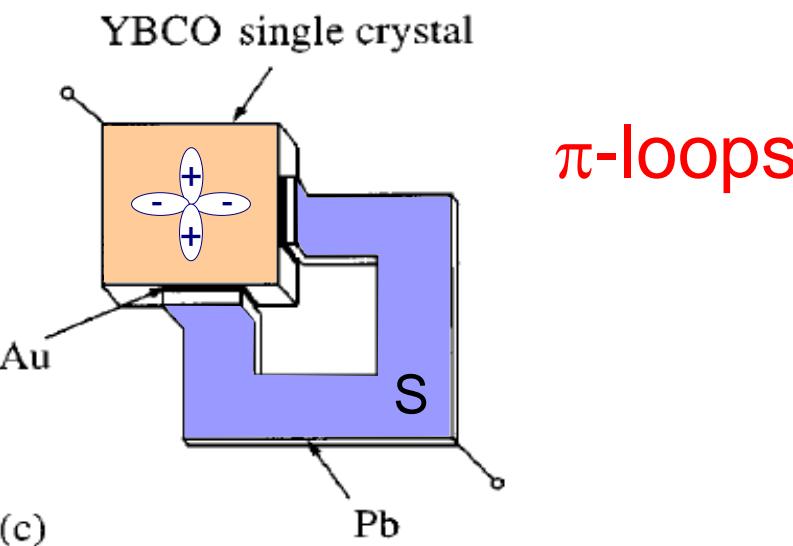
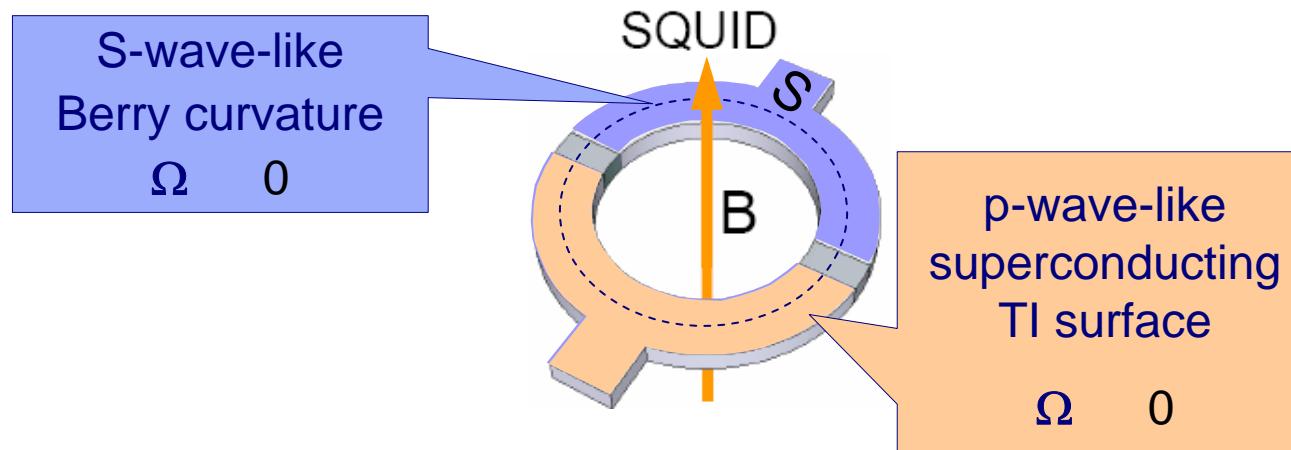
YBCO tri-crystal SQUID  
 $\pi$ -loop & half flux quanta



# Superconducting quantum interference device (SQUID)

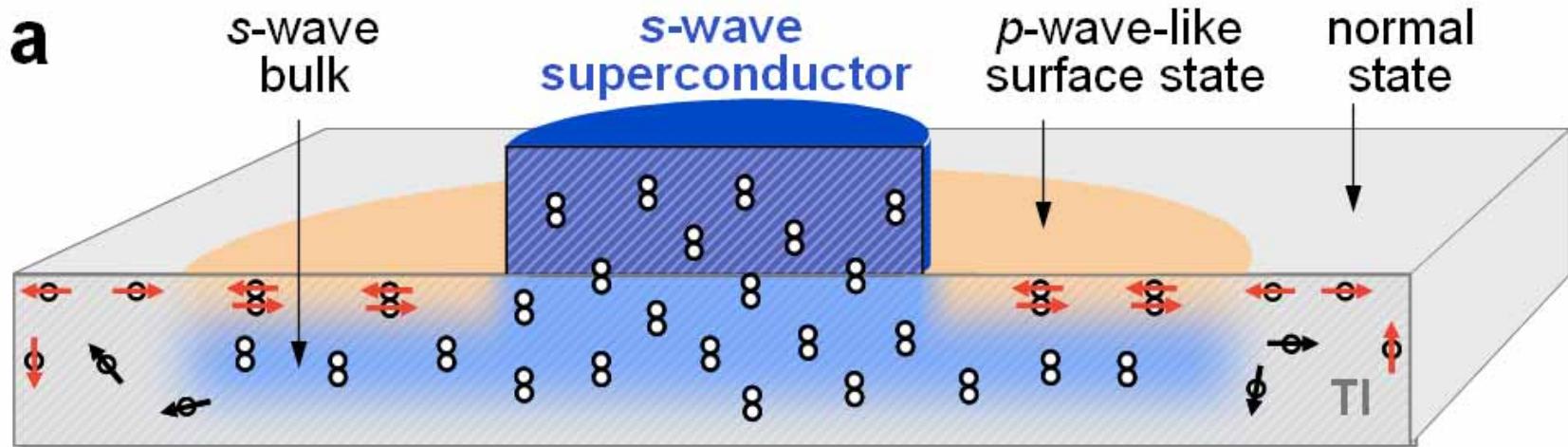


# Why $I_c$ maximizes at $B=0$ in previous exp.?

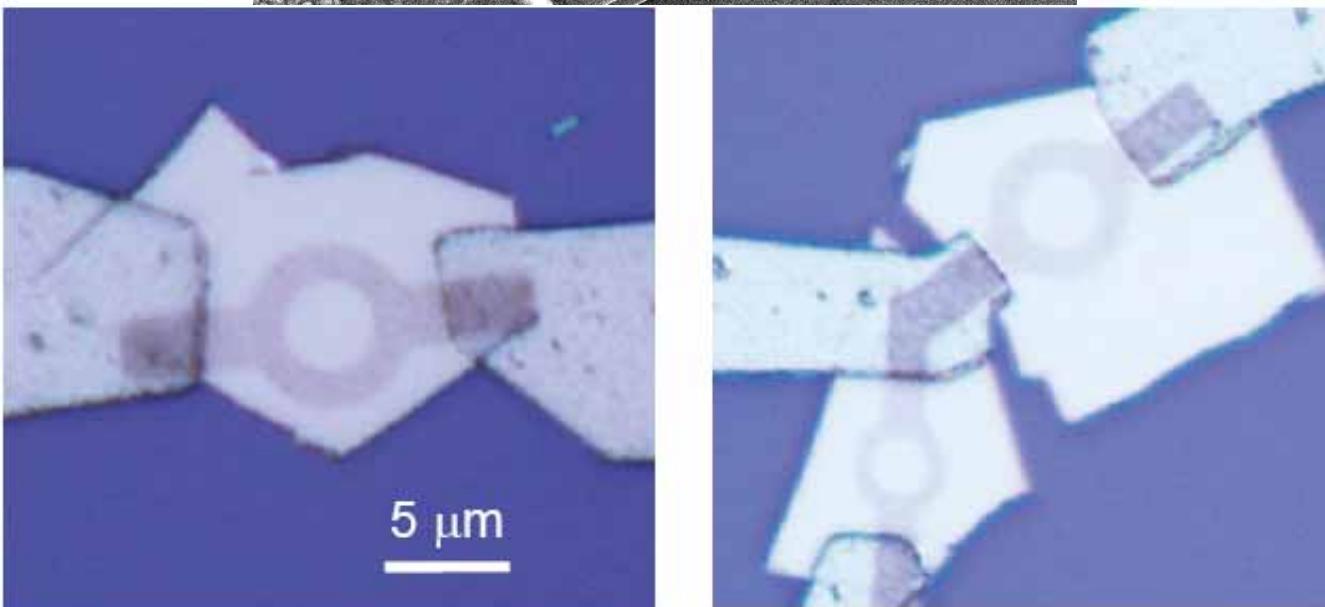
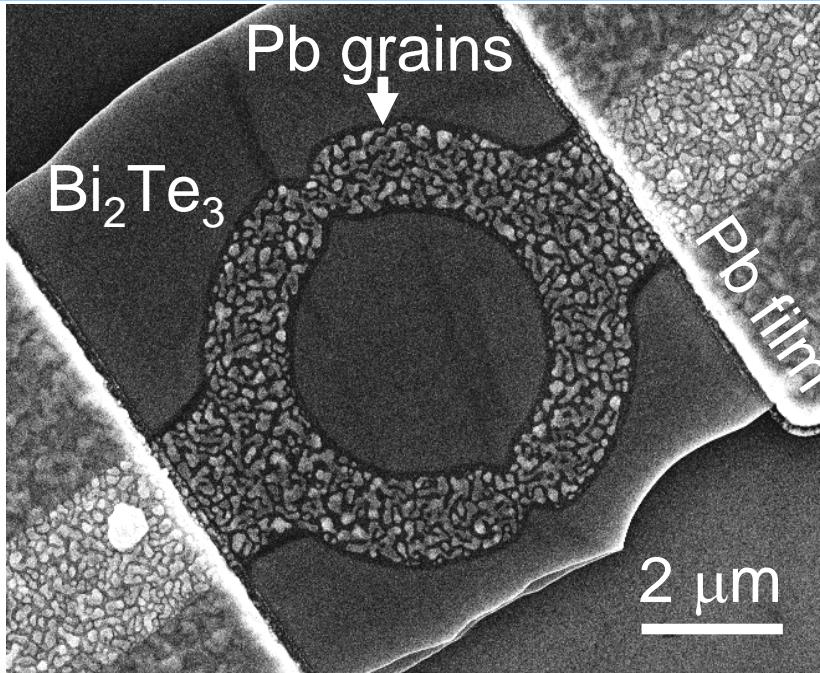


To examine the p-wave-like feature, one needs to form a loop which picks up the Berry phase of the p-like state

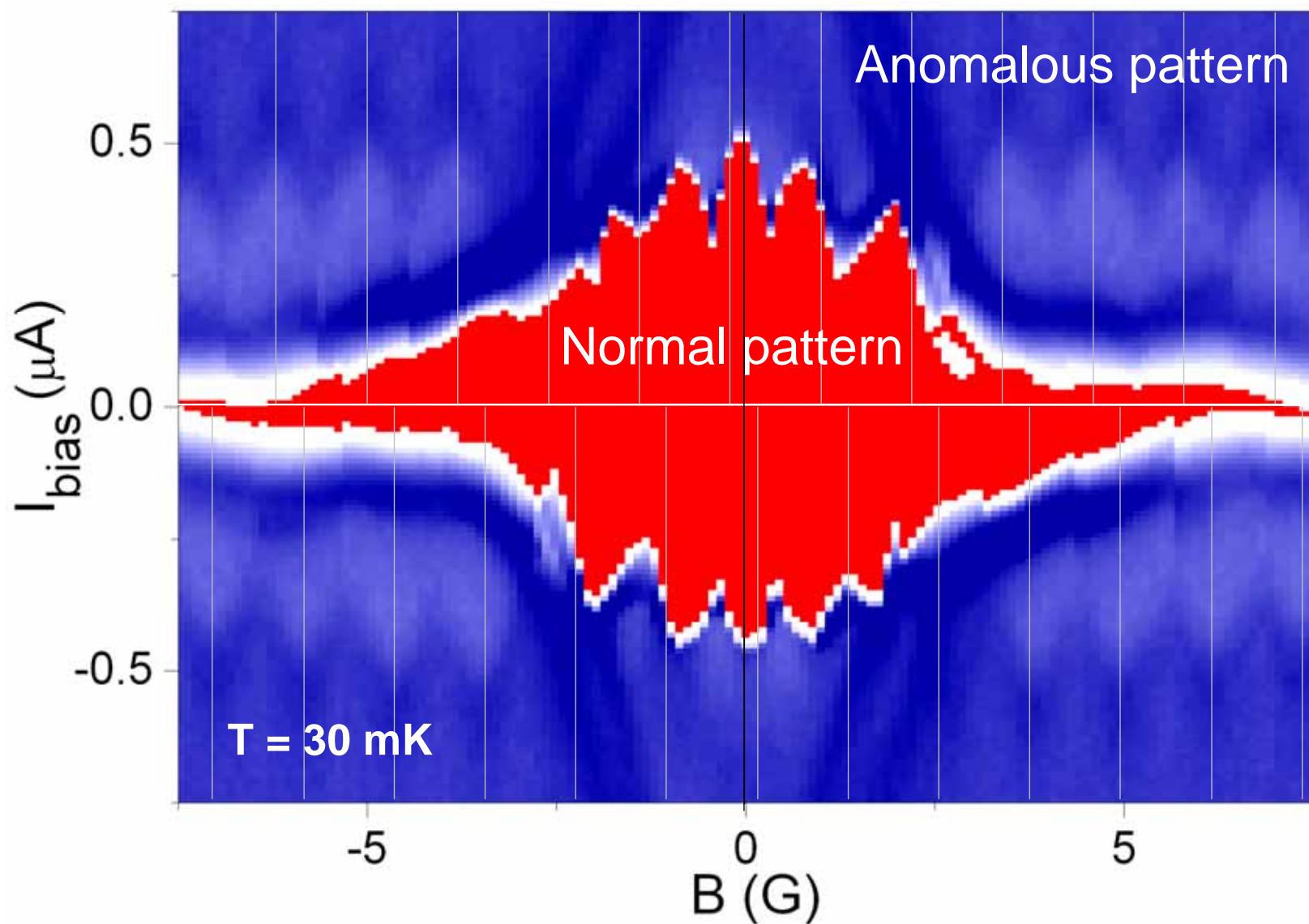
# Proximity Effect at SC-TI Interface



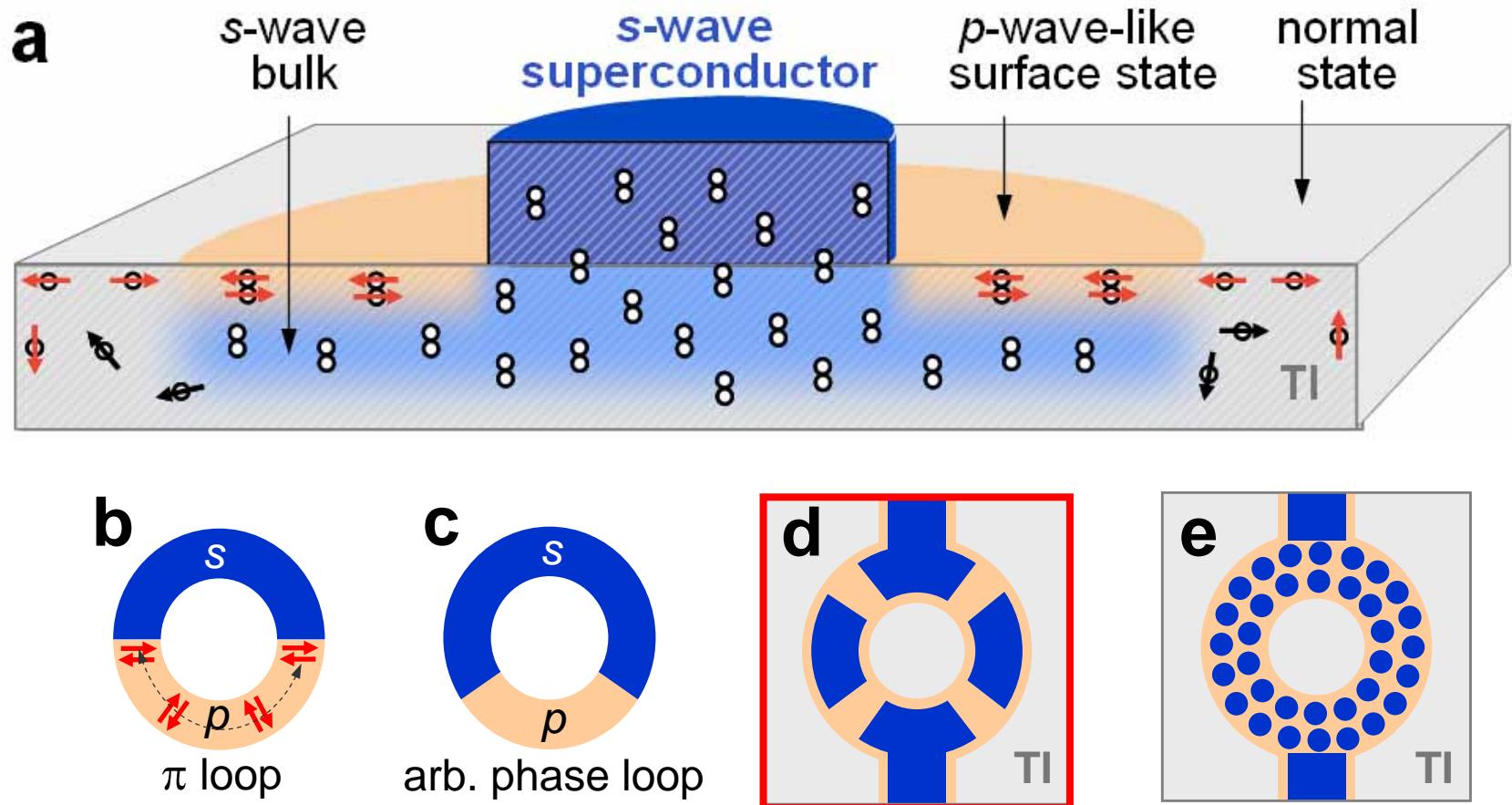
# Pb-grain SQUIDs on $\text{Bi}_2\text{Te}_3$



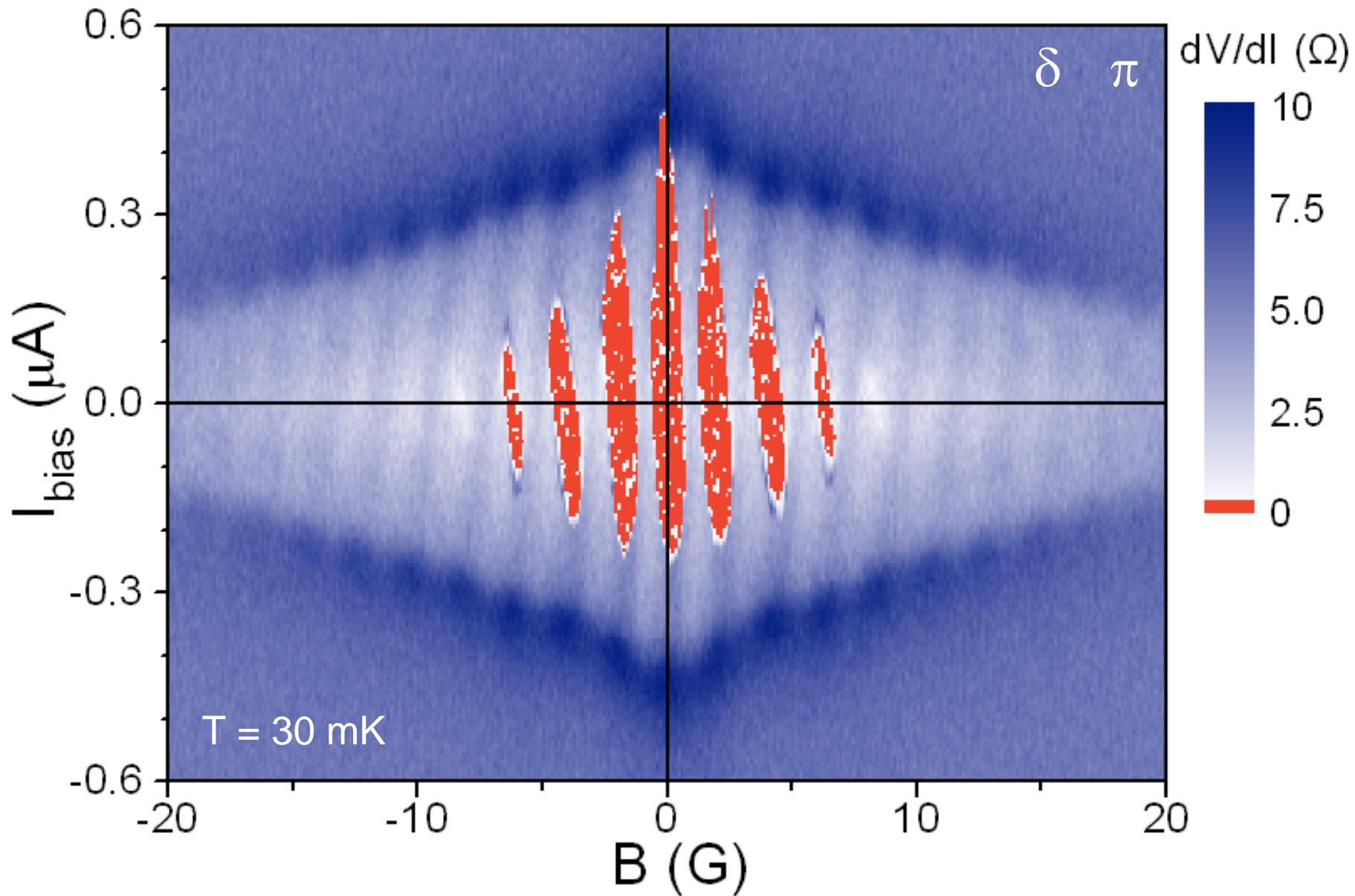
# Interference Patterns



# Proximity Effect at SC-TI Interface



# Four Pb segments SQUIDs on $\text{Bi}_2\text{Te}_3$



# Our picture for the anomalous pattern

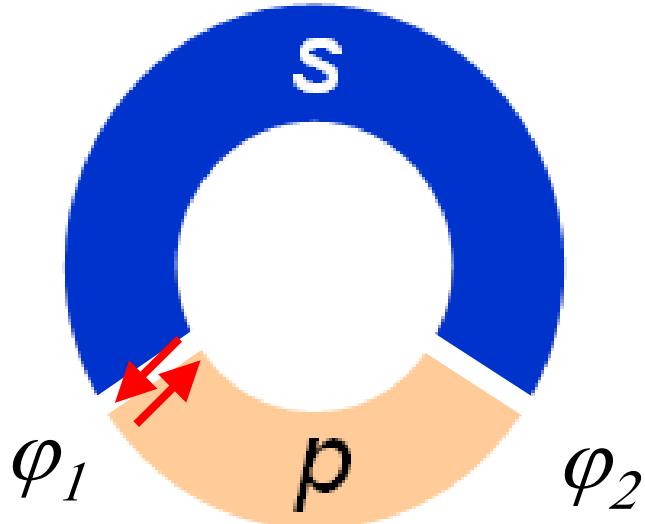
Fluxoid quantization along the loop:

$$\varphi_1 + \varphi_2 + 2\pi \Phi_{\text{ex}}/\phi_0 \pm \delta = 2\pi N$$

Berry phase  $\sim B_{\text{eff}}$

Free energy:

$$U = (\Phi_{\text{ex}} - N\phi_0)^2/2L - E_{J1}\cos\varphi_1 - E_{J2}\cos\varphi_2$$



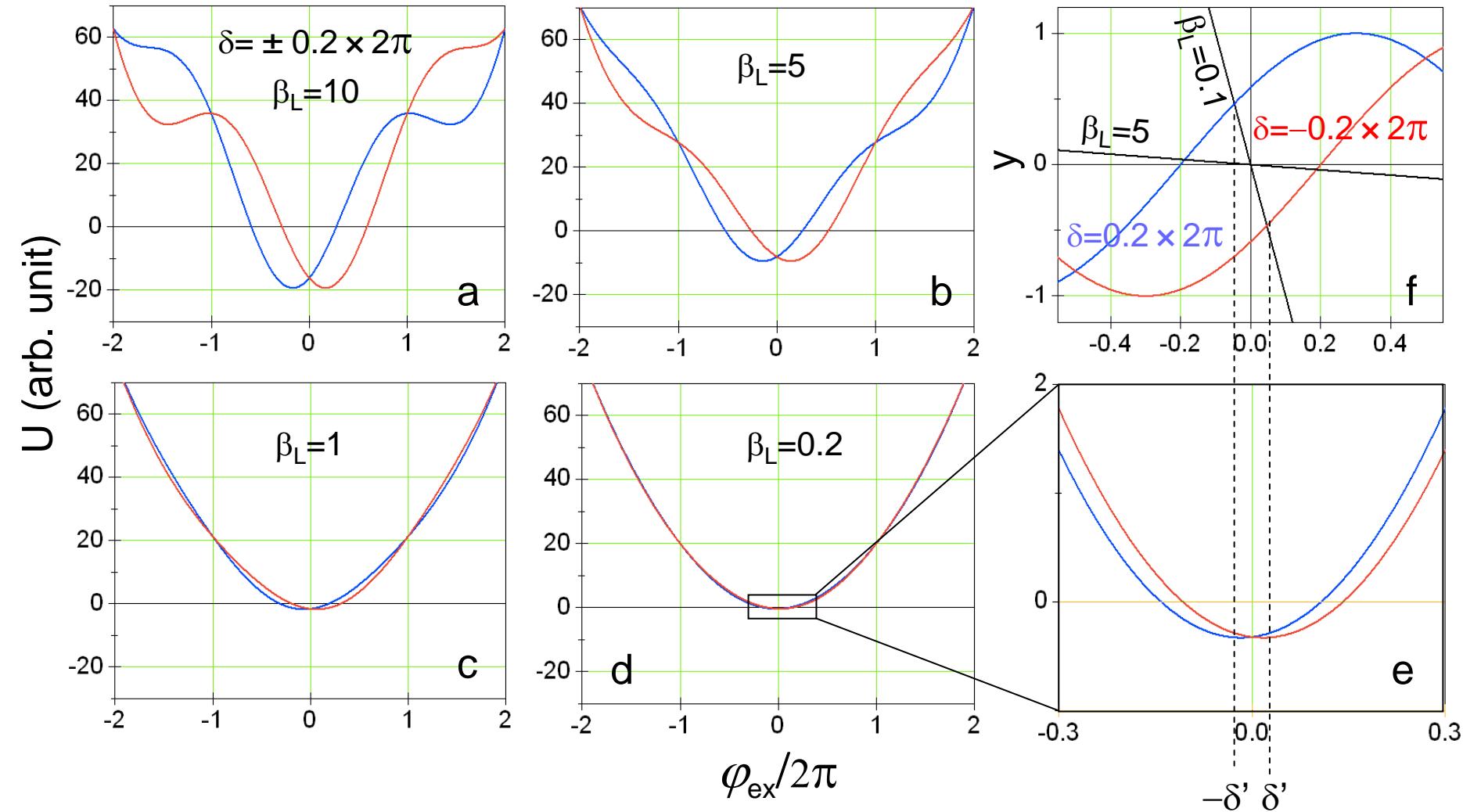
When  $E_{J1} = E_{J2}$ :

$$U = \varphi_{\text{ex}}^2/2 - 2\beta_L \cos(\varphi_{\text{ex}}/2 \pm \delta/2)$$

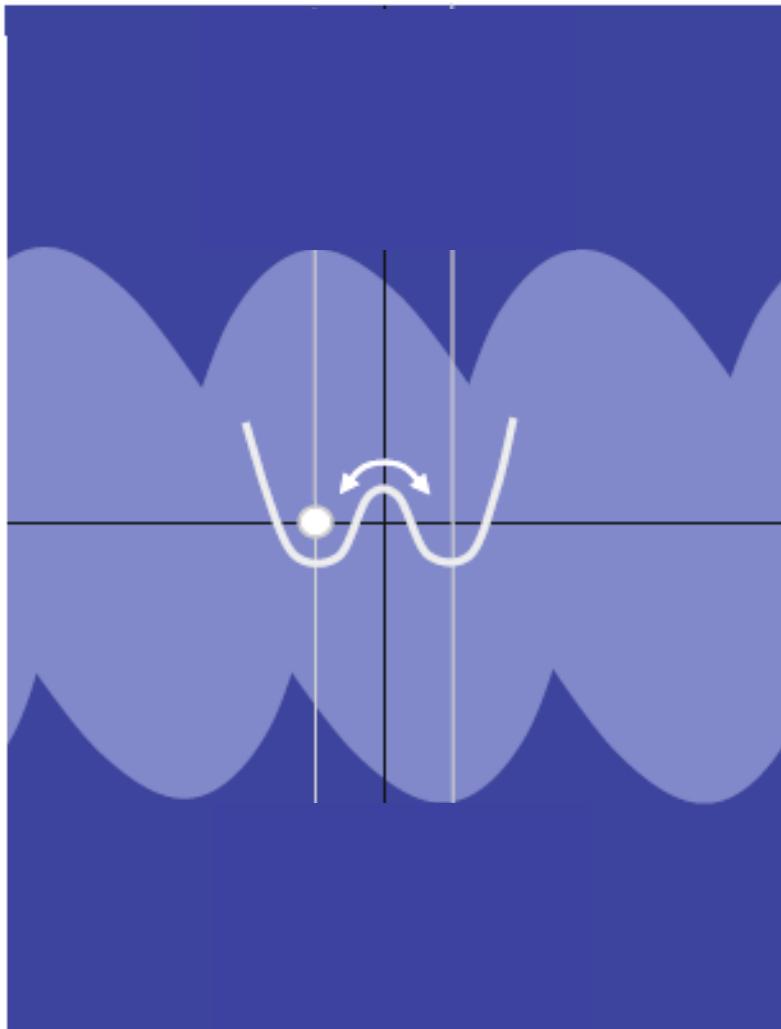
$$\beta_L = 2\pi L I_c / \phi_0$$

# Formation of a double-well potential

$$U = \varphi_{\text{ex}}^2/2 - 2\beta_L \cos(\varphi_{\text{ex}}/2 \pm \delta/2)$$



# Break the time reversal symmetry?



- cw and ccw **double wells**
- with inter-well tunneling, it forms a **two-level system**:
$$|\Psi_0\rangle = |cw\rangle + |ccw\rangle$$
$$|\Psi_1\rangle = |cw\rangle - |ccw\rangle$$
- The wavefunctions are **time reversal invariant** within the decoherence time.
- In real measurement, the system will project to  $|cw\rangle$  or  $|ccw\rangle$  states spontaneously.
- The projection is selected by the bias current.

# Summary

- Used  $2\pi$  Berry phase to describe the p-wave-like superconductivity of Cooper pairs made of helical electrons.
- Constructed two types of Cooper pair interference loops to detect the Berry phase on the surface of 3D TI.
- Observed in addition to a normal interference pattern an anomalous one, which survives in parallel magnetic field, presumably arising from the Berry phase of the Cooper pairs.

arXiv:1303.5598v3

Thank You