

New Precision Measurement for Proton Zemach Radius with Laser Spectroscopy of Muonic Hydrogen

On behalf of Mup collaboration

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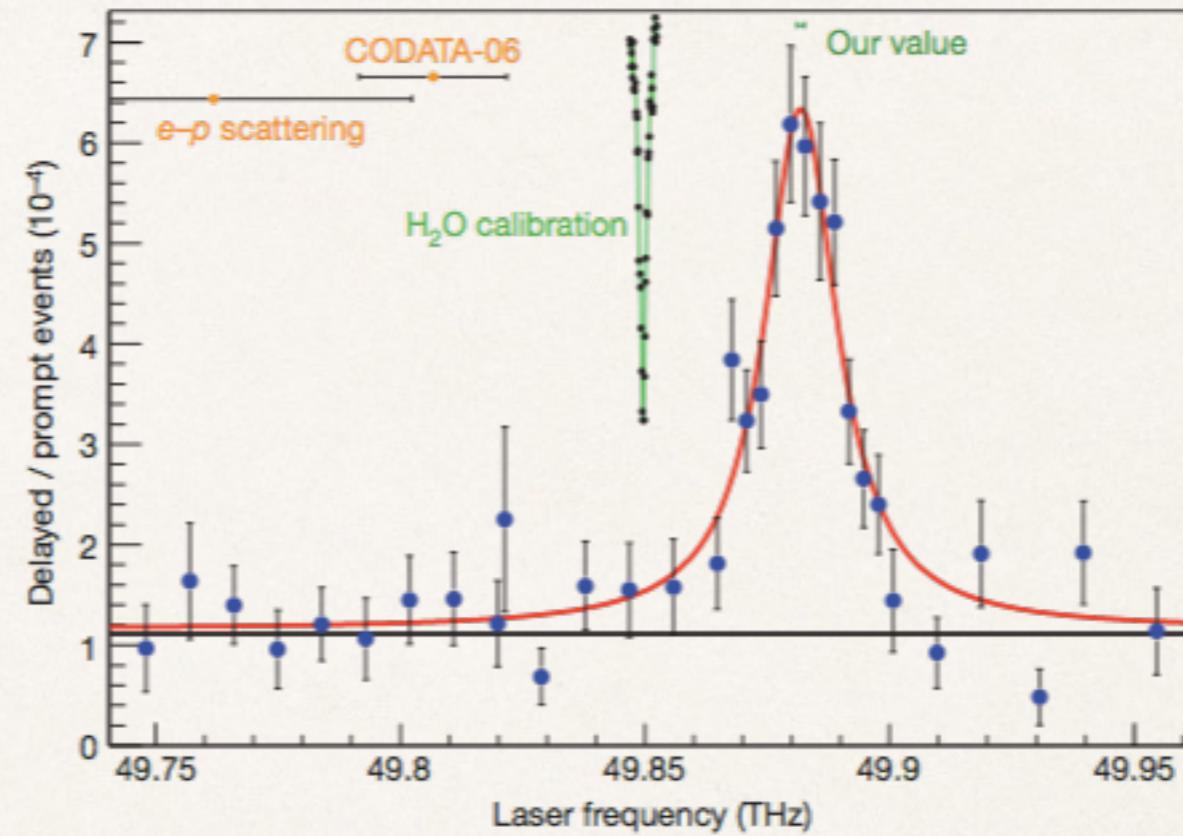
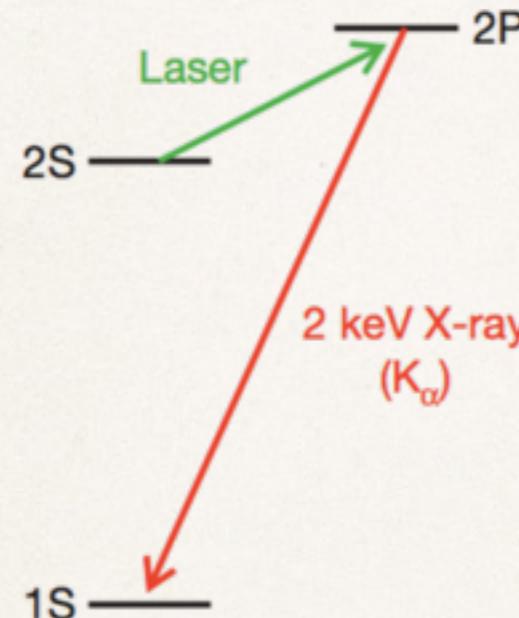
Oct. 21st, 2014

Outline

- ❖ Background & motivation
- ❖ Experimental setup
- ❖ Expected results
- ❖ Summary

Background & motivation

The beginning of proton size puzzle



PSI experiment operation principle:

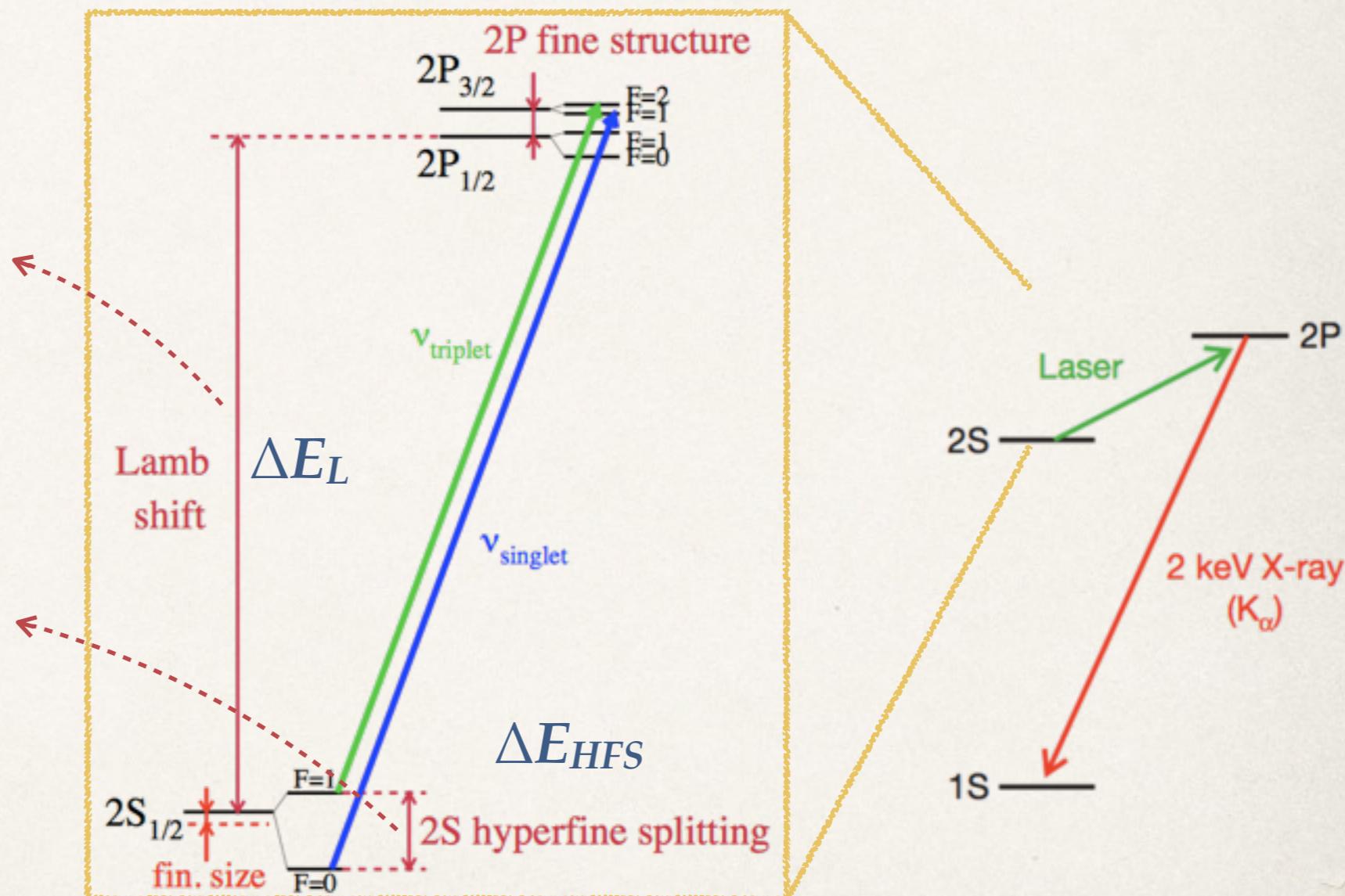
1. Search for 2S-2P level spacing by scanning laser wave length;
2. Coincidence with 2 keV x-ray($K\alpha$) to identify resonance;
3. $r_E = 0.84087(39)\text{fm}$, $7-\sigma$ away from world data



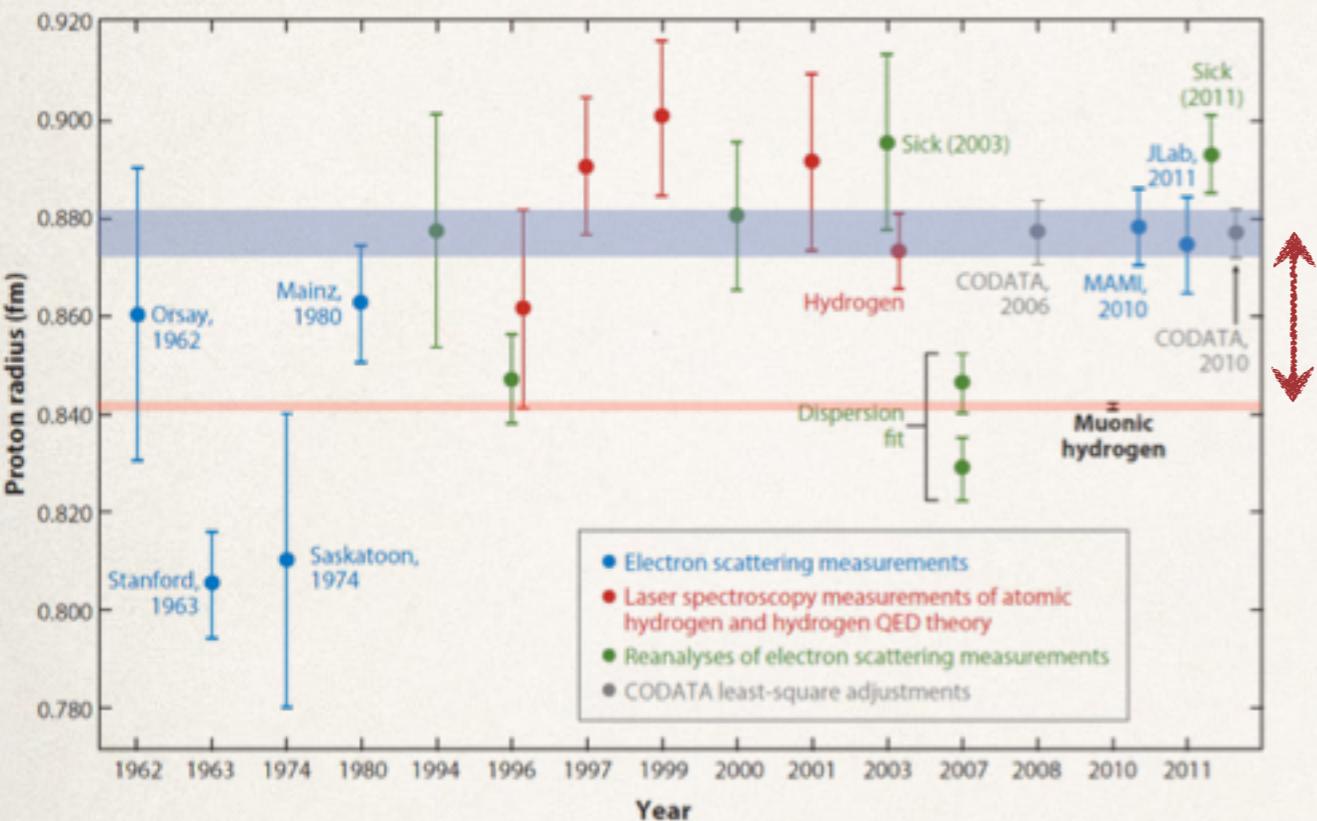
Updated measurements @ PSI

$$\begin{aligned}\Delta E_L &= 0.25h\nu_s + 0.75h\nu_t \\ &\quad - 8.8123(2)\text{meV} \\ \Rightarrow r_E &= 0.84087(26^{\text{exp}})(29^{\text{th}})\text{fm} \\ \delta r_E / r_E &\sim 0.046\%\end{aligned}$$

$$\begin{aligned}\Delta E_{HFS} &= h\nu_s - h\nu_t \\ &\quad + 3.2480(2)\text{meV} \\ \Rightarrow r_Z &= 1.082(31^{\text{exp}})(20^{\text{th}})\text{fm} \\ \delta r_Z / r_Z &\sim 3.4\%\end{aligned}$$



Proton radius data summary

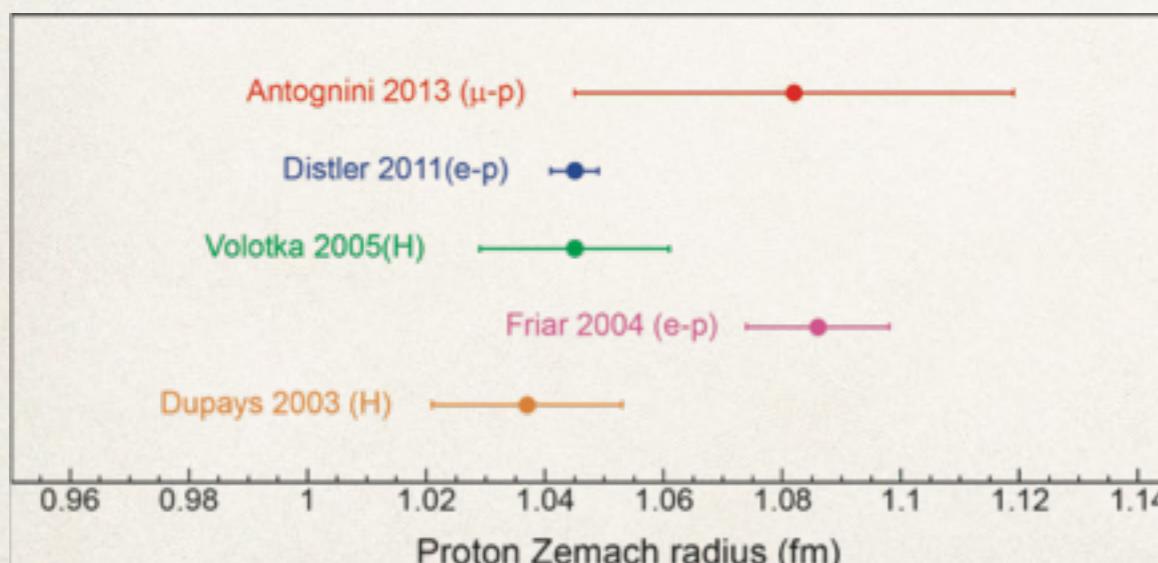


$$r_E^2 = \int d^3r r r^2 \rho_E(r)$$

7- σ deviation, $\delta r_E / r_E \sim 0.046\%$

Precision is the key:

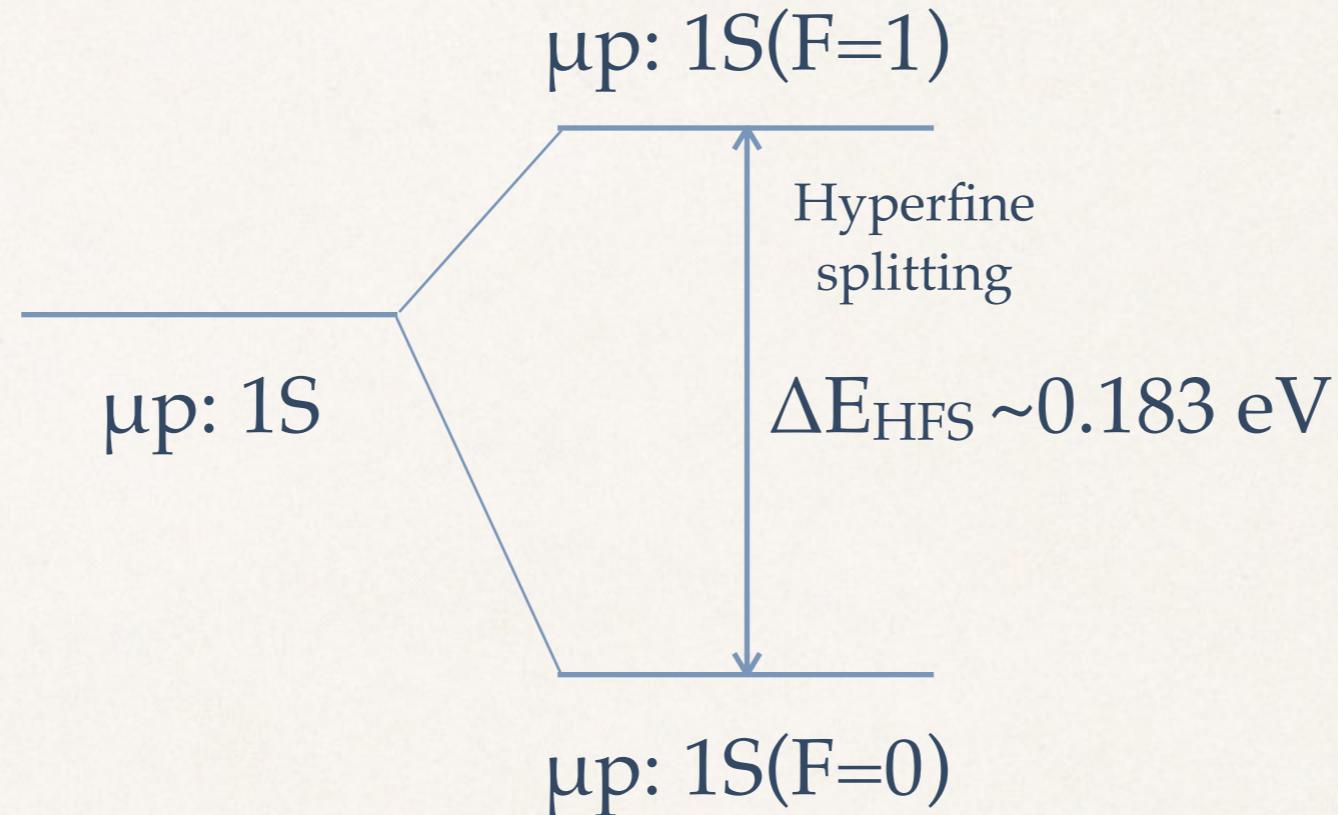
1. with 1% accuracy, r_E will be “consistent”;
2. what about r_Z with better accuracy?



$$r_Z = \int d^3r \int d^3r' r' \rho_E(r) \rho_M(r - r')$$

compatible, $\delta r_Z / r_Z \sim 3.4\%$

Our proposed measurement

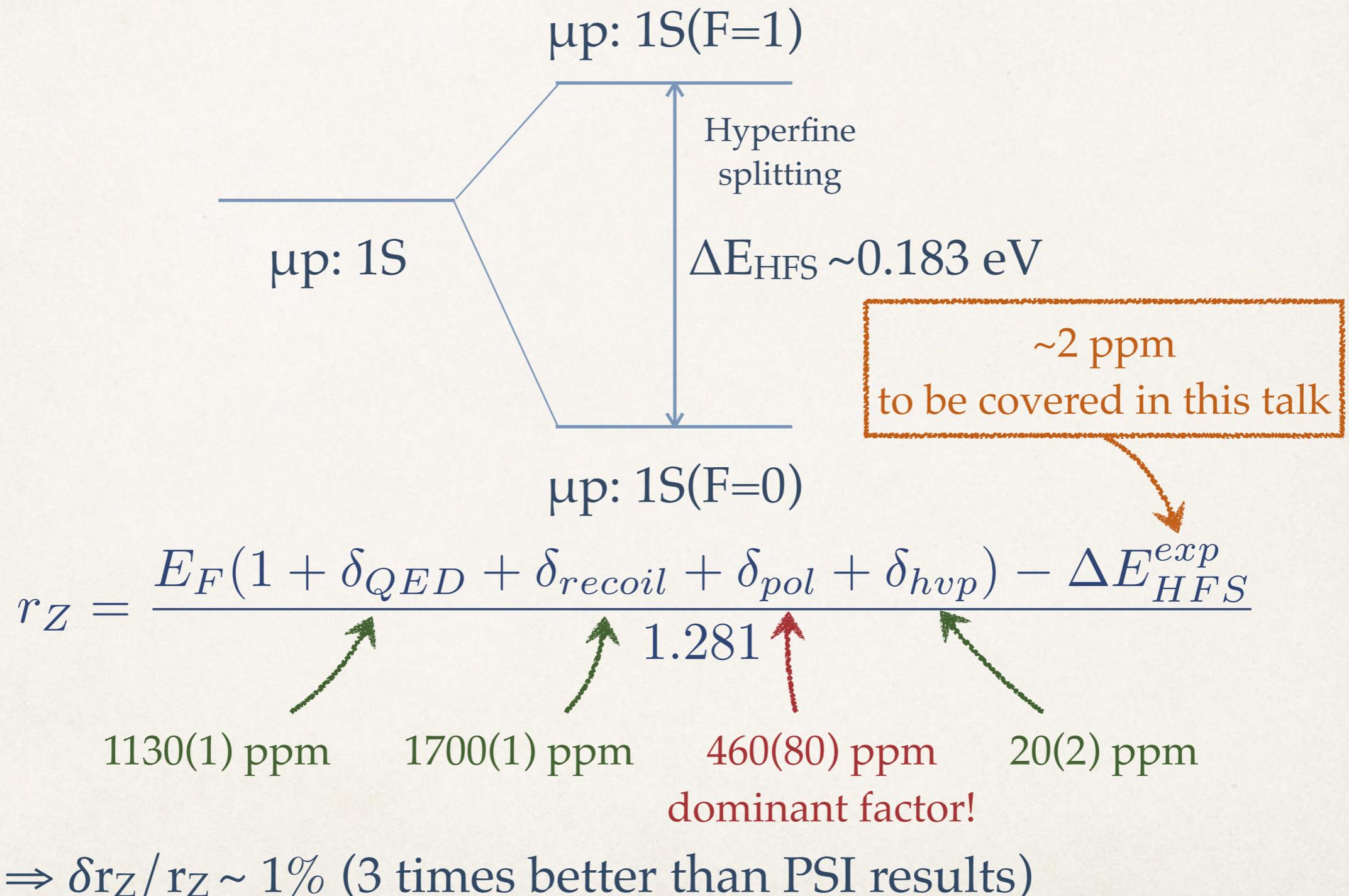


$$\begin{aligned}\Delta E_{HFS}^{th} &= E_F(1 + \delta_{QED} + \delta_{str}) \\ &= E_F(1 + \delta_{QED} + \delta_{Zemach} + \delta_{recoil} + \delta_{pol} + \delta_{hvp})\end{aligned}$$

$$E_F = \frac{8}{3} \alpha^4 \frac{m_\mu^2 m_p^2}{m_\mu + m_p} \mu_p$$

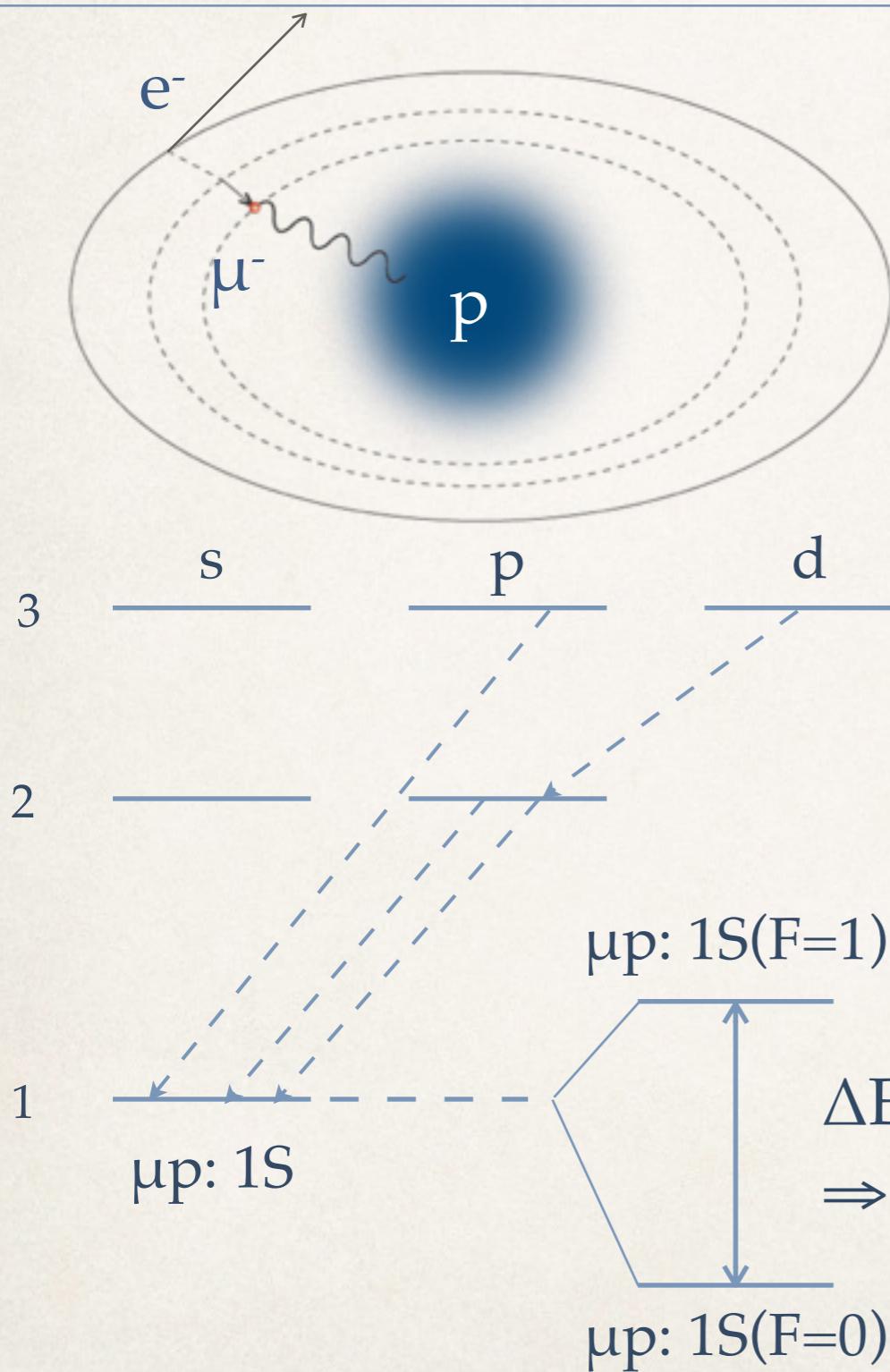
$$\delta_{Zemach} = -\alpha m_{\mu p} r_Z + O(\alpha^2)$$

Our proposed measurement



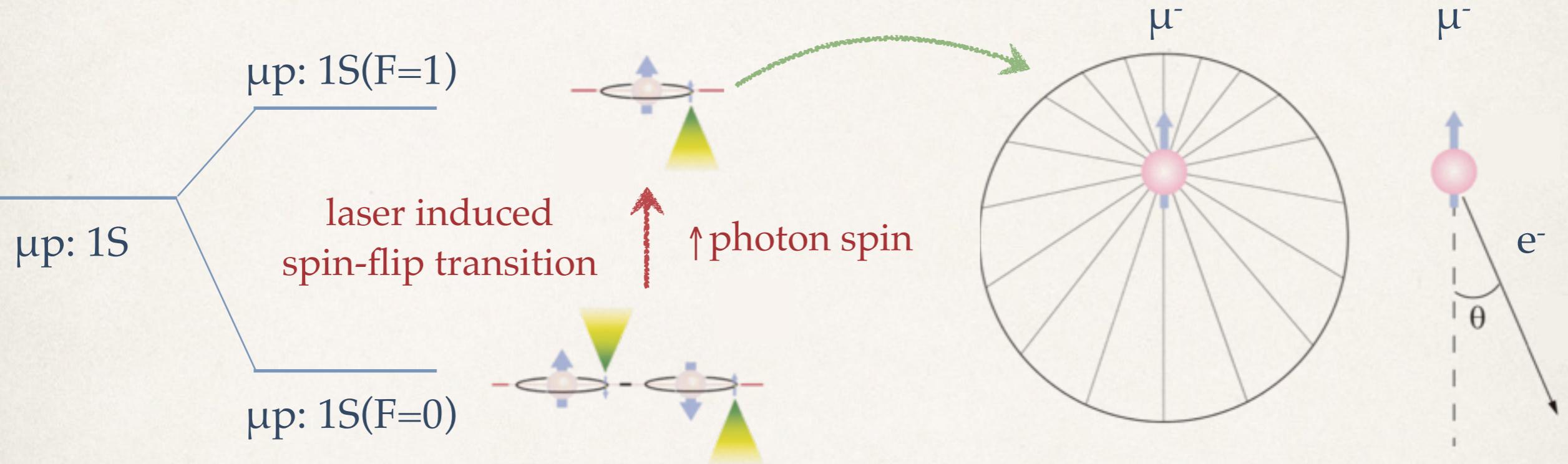
Experimental setup: how to measure ΔE_{HFS} with 2ppm accuracy?

Measurement principle

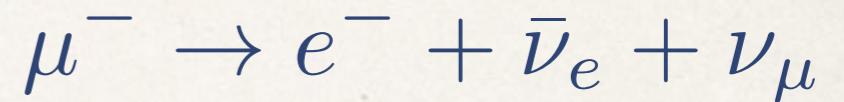


1. μ^- captured by Hydrogen gas (RAL or J-PARC);
2. formation of 1S ground state;
3. $1S(F=0) \rightarrow 1S(F=1)$ transition(M1) by laser;
4. measure decay asymmetry of polarised μ^- decay to identify resonance

Measurement principle



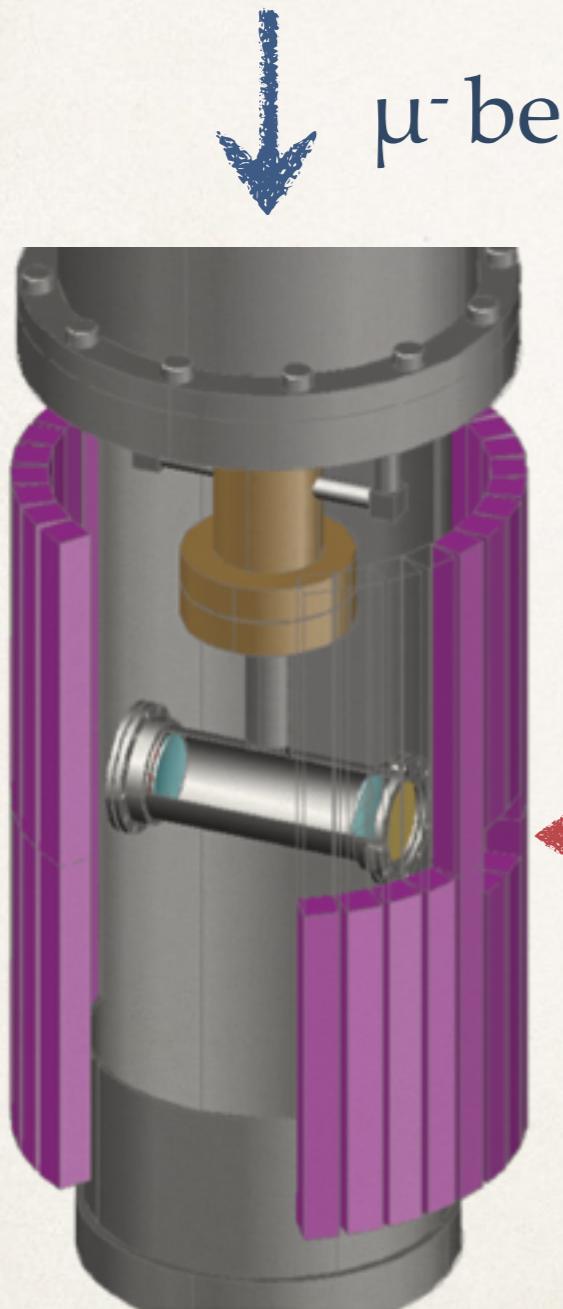
1. shoot μ^- beam on Hydrogen target & formation of muonic hydrogen(μp);
2. shed laser on muonic hydrogen & scanning over laser wave length to search for $\mu p: 1S(F=0) \rightarrow 1S(F=1)$ resonance frequency;
3. identify resonance frequency by detecting maximum $\mu^- \rightarrow e^- + \bar{\nu}_e + \nu_\mu$ decay asymmetry



$$d\sigma_{e^-}(\theta)d\Omega \propto \left(1 - \frac{1}{3}P\cos\theta\right)$$

$$\text{Asymmetry} = \frac{N_F - N_B}{N_F + N_B}$$

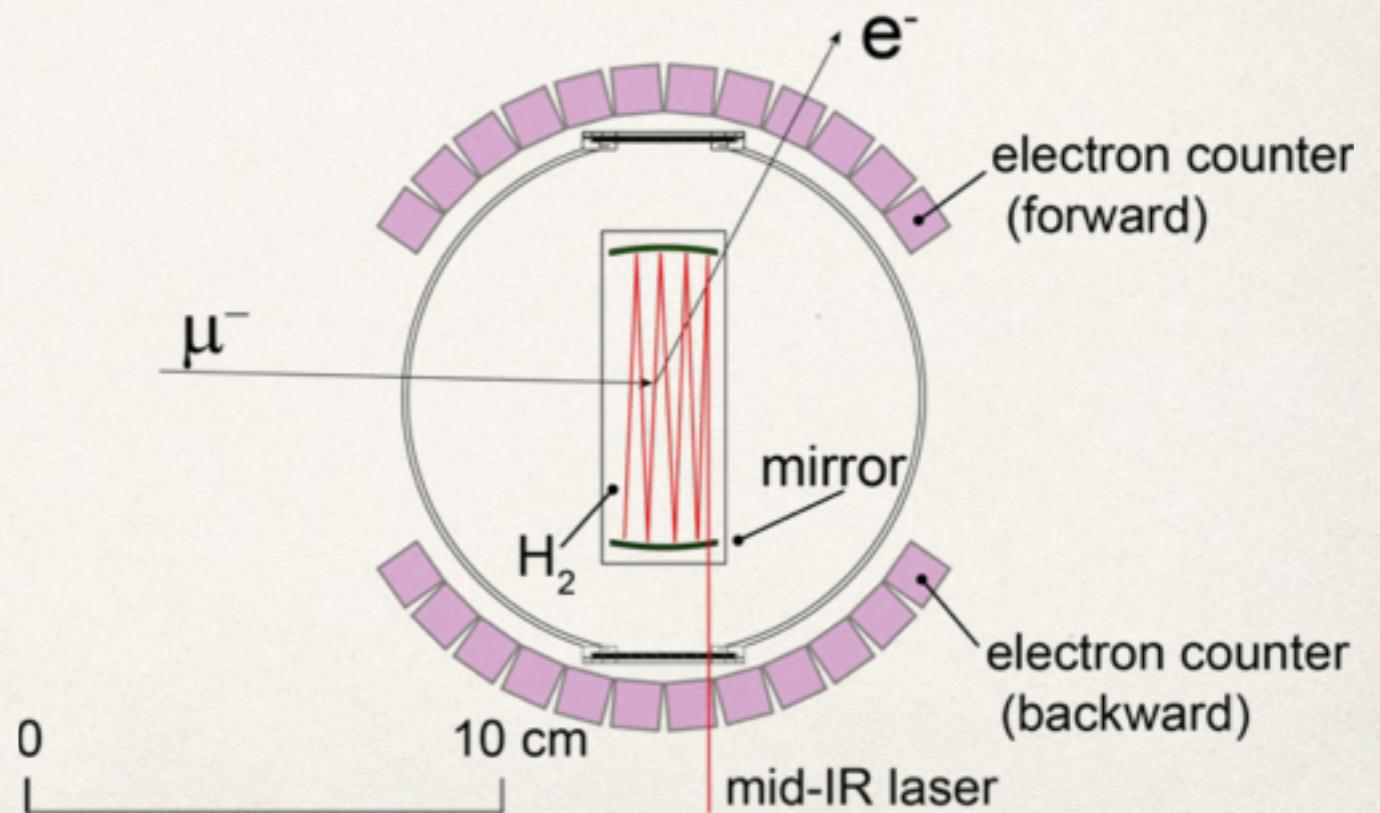
Experiment concept: target & counter



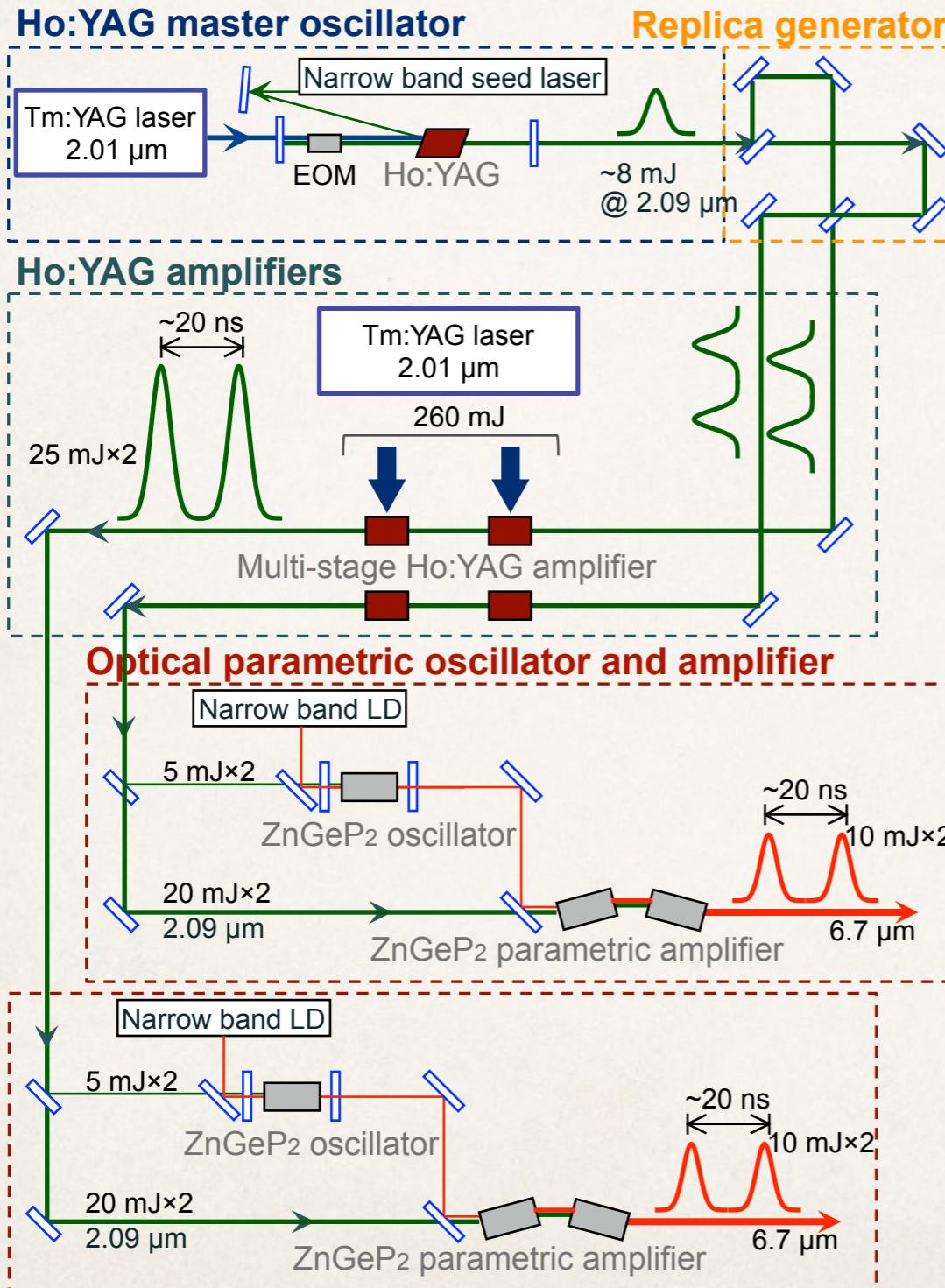
$$\mu^- \rightarrow e^- + \bar{\nu}_e + \nu_\mu$$

$$d\sigma_{e^-}(\theta)d\Omega \propto \left(1 - \frac{1}{3}P\cos\theta\right)$$

$$Asymmetry = \frac{N_F - N_B}{N_F + N_B}$$



Experiment concept: laser system



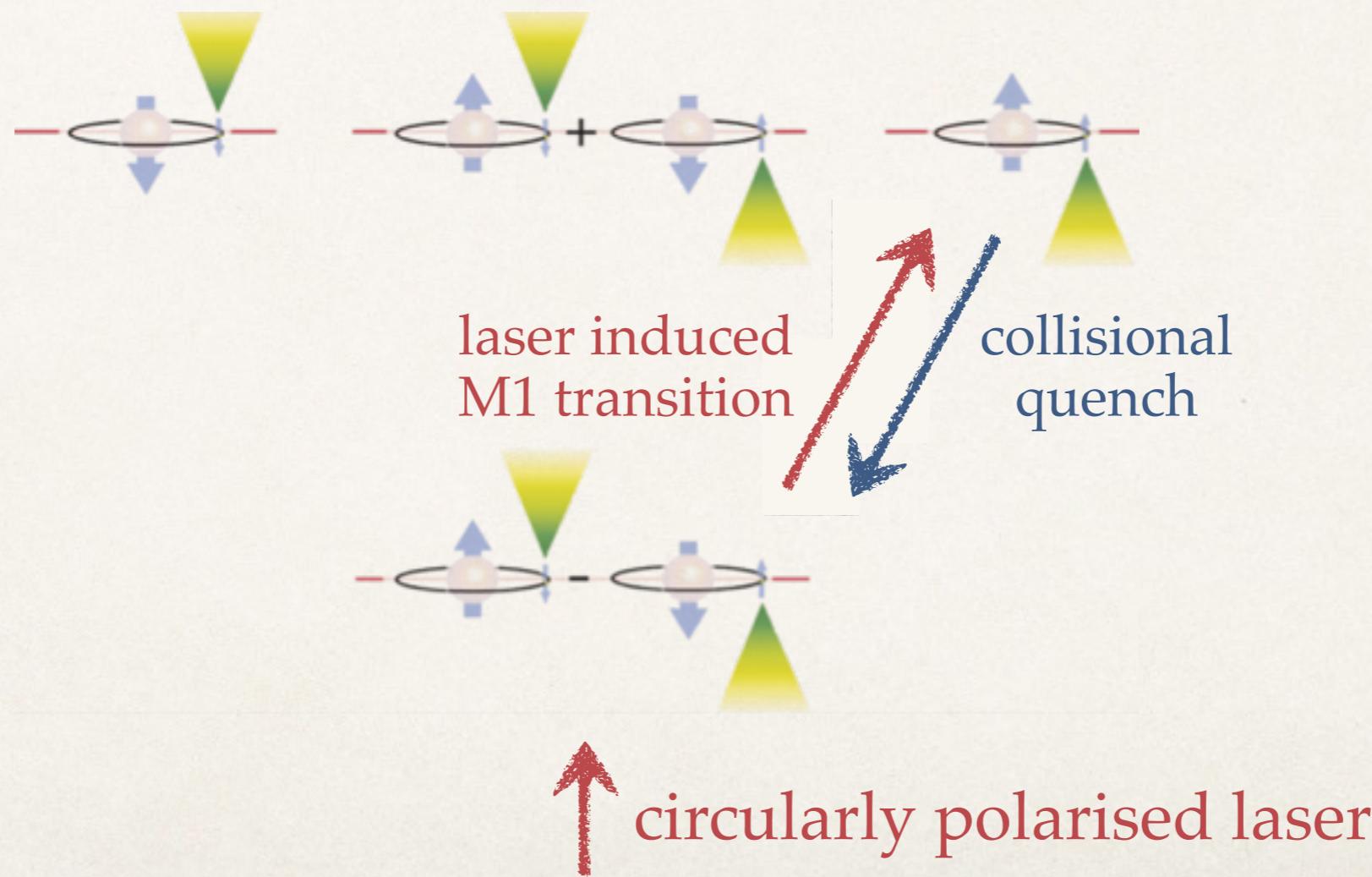
Laser system parameters:

1. Tunable mid-infrared laser (R&D by Wada group@RIKEN);
2. 6.8 μm (> 6 GHz tunability);
3. repetition ~ 50 Hz;
4. band width ~ 50 MHz;
5. double pulse 10 mJ×2 sets = 40 mJ;
6. OPO controlled seed;

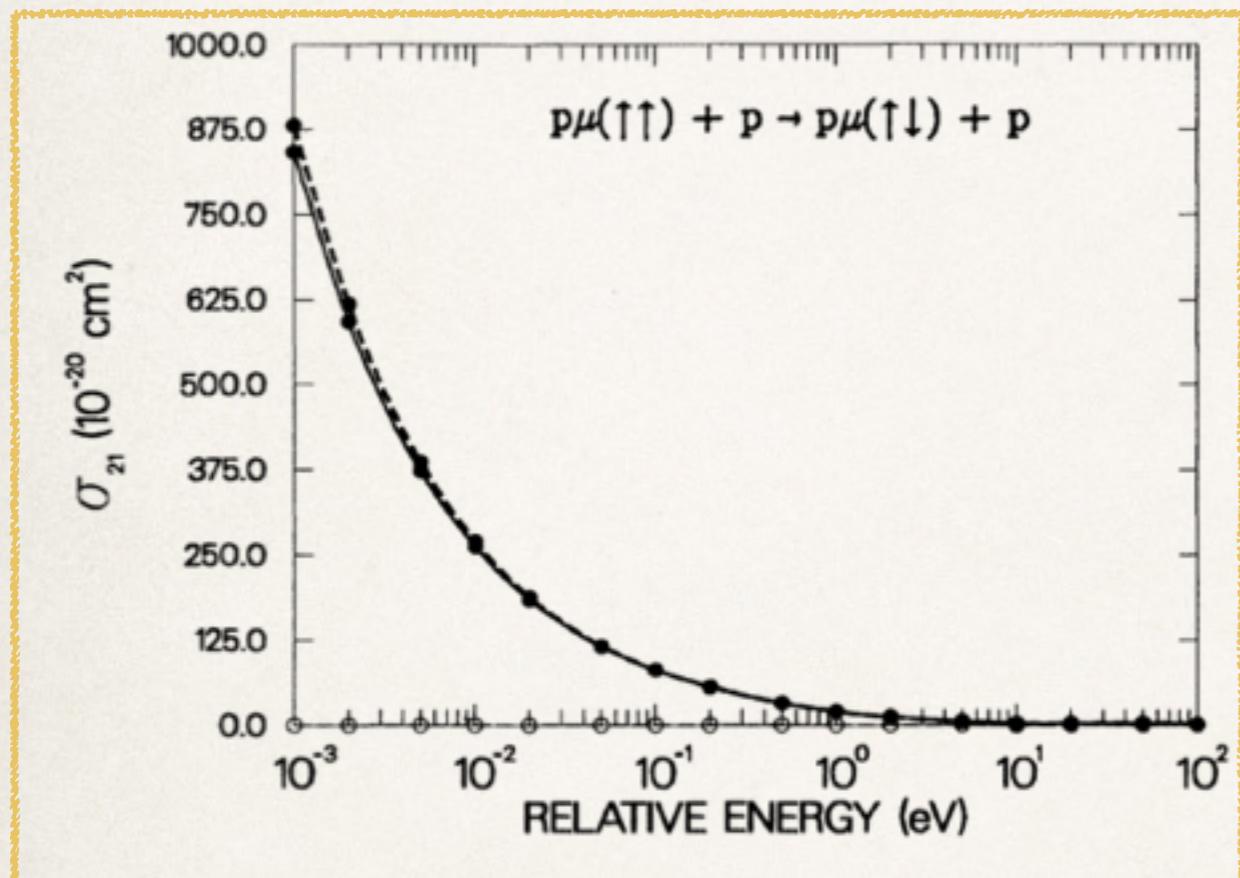
Expected results

Yield estimation

Competition between laser induced transition
and collisional quench.



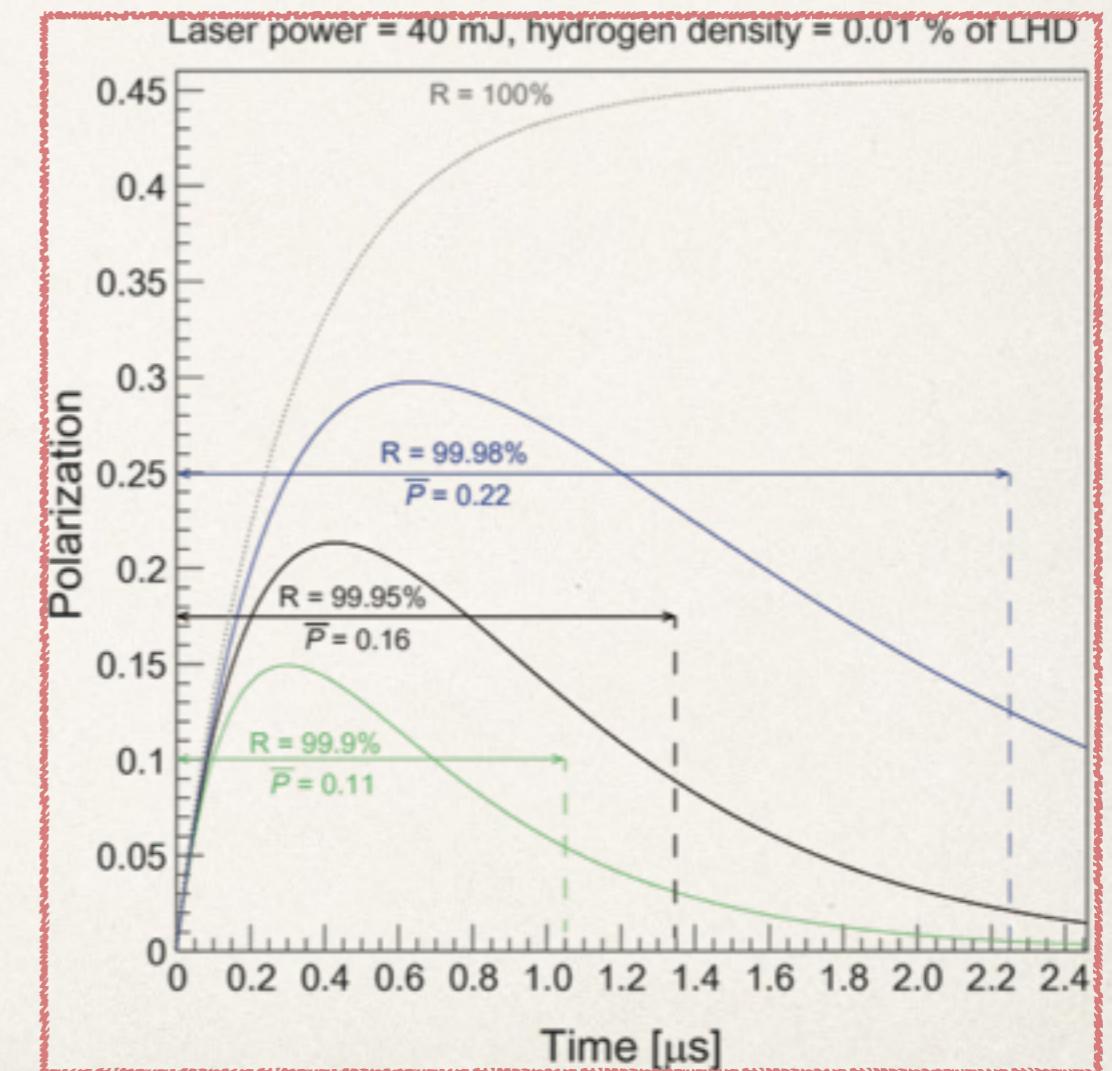
Yield estimation



Collisional quench rate proportional
to target density:

$$\tau = 500 \text{ ns with } \rho = 0.01\% \text{ LHD}$$

$$\bar{P} = 2 \times 10^{-5} \frac{E}{S\sqrt{T}}$$



Beam time estimation

$$\text{Significance}(\sigma) = \frac{\text{signal}}{\text{fluctuation}} = \frac{N_F - N_B}{\sqrt{N_F + N_B}}$$

RAL pulsed muon source:

- intensity: 2.4×10^4 (50 Hz);
- momentum: 40 MeV / c ($\pm 4\%$);

Laser system:

- power: 40 mJ;
- band width: 50 MHz;
- mirror: 99.95%;

H₂ target:

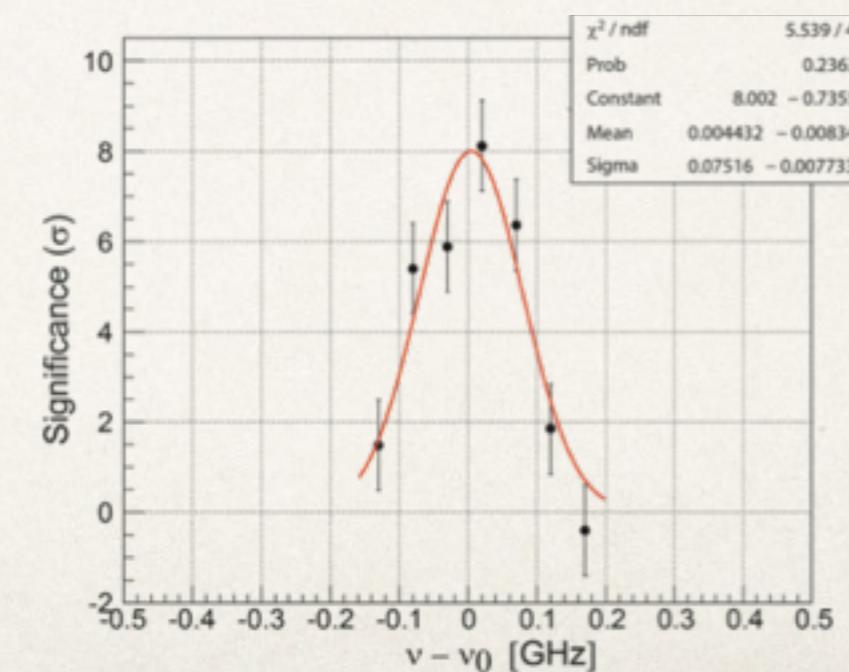
- 0.0001 LHD

scan interval: 100 MHz (2ppm accuracy);
scan region: ± 5.7 GHz ($\delta_{\text{Zemach}} + \delta_{\text{pol}}$);

Three scanning-stage approach:

- 3σ (wide range): 25 days;
- 5σ (interested region): 11 days;
- 7σ (precise): 8 days;

44 days beam time!



Summary

- ✿ New proposal for precision Zemach radius measurement with laser spectroscopy
- ✿ Detector & laser system R&D are ready
- ✿ Beam time request has been proposed to RAL & J-PARC facility