

Symmetry breaking and determination of parton distribution functions of the nucleon

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1. Symmetries in the PDFs

flavour symmetry, quark-antiquark symmetry

charge symmetry

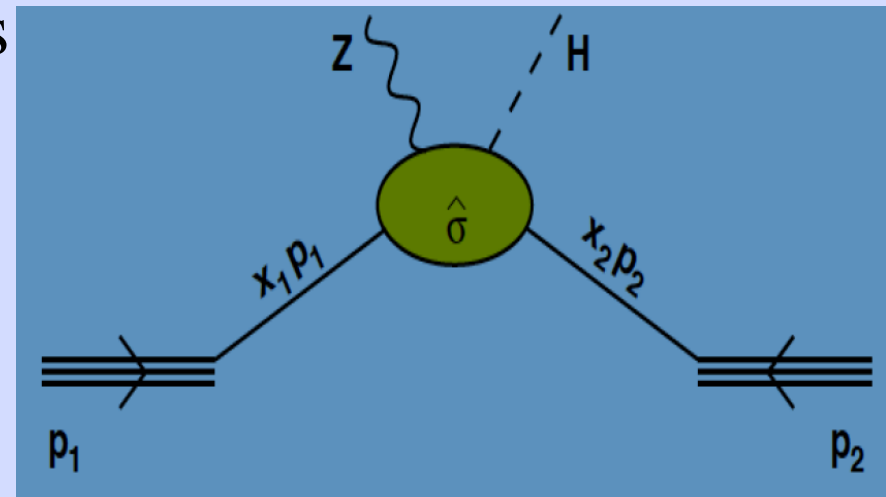
2. Symmetry breaking in the meson cloud model

3. Strange distributions of the nucleon

4. Summary

1. Introduction

- Parton distribution functions are non-perturbative inputs in higher-energy hadron processes.



QCD factorization theorem

$$\sigma = \int dx_1 dx_2 f_{q/p}(x_1, \mu^2) \hat{\sigma}(x_1 p_1, x_2 p_2, \mu^2) f_{q/p}(x_2, \mu^2)$$

Total X-section is factorized into a hard part, $\hat{\sigma}(x_1 p_1, x_2 p_2, \mu^2)$, and soft parts, $f_{q/p}(x_1, \mu^2)$, and $f_{q/p}(x_2, \mu^2)$.

- PDFs are key ingredients for Tevatron and LHC phenomenology, e.g. Higgs electroweak couplings.

- Introduced by Feynman (1969) in the parton model; interpreted as probability distributions
- Universal distributions containing long-distance structure of hadrons; related to parton model distributions at leading order, but with logarithmic scaling violations

$$q(x, Q^2) = q^\uparrow(x, Q^2) + q^\downarrow(x, Q^2) \quad \text{unpolarized PDFs}$$

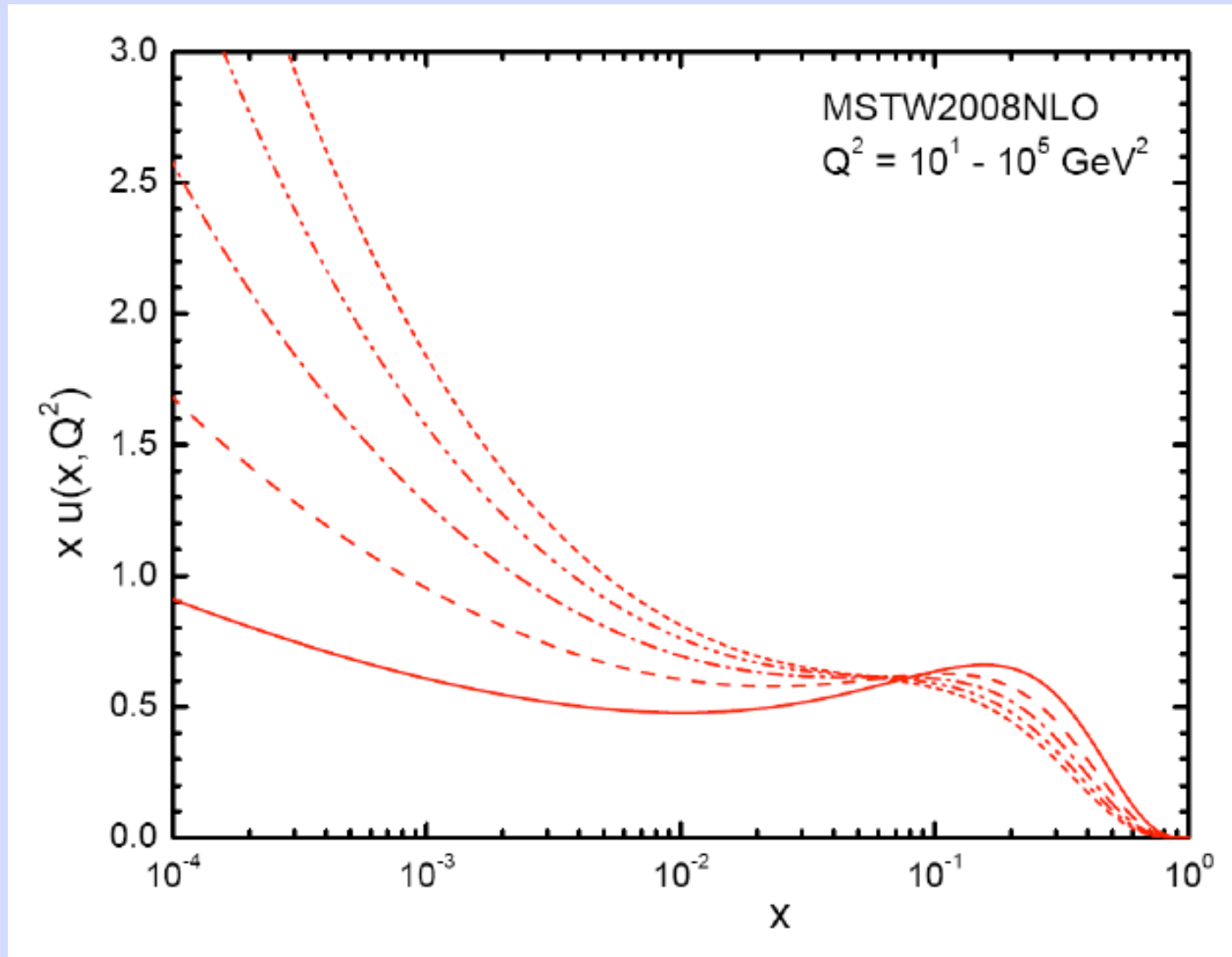
$$\Delta q(x, Q^2) = q^\uparrow(x, Q^2) - q^\downarrow(x, Q^2) \quad \text{longitudinally polarized PDFs} \\ \text{and transversely polarized PDFs}$$

$$q^\uparrow(x, Q^2), q^\downarrow(x, Q^2):$$

number densities of quarks whose spin orientation is parallel and antiparallel to the longitudinal spin direction of the nucleon

x : the fractional parton momentum

- Q^2 -dependence is determined by the DGLAP eq.

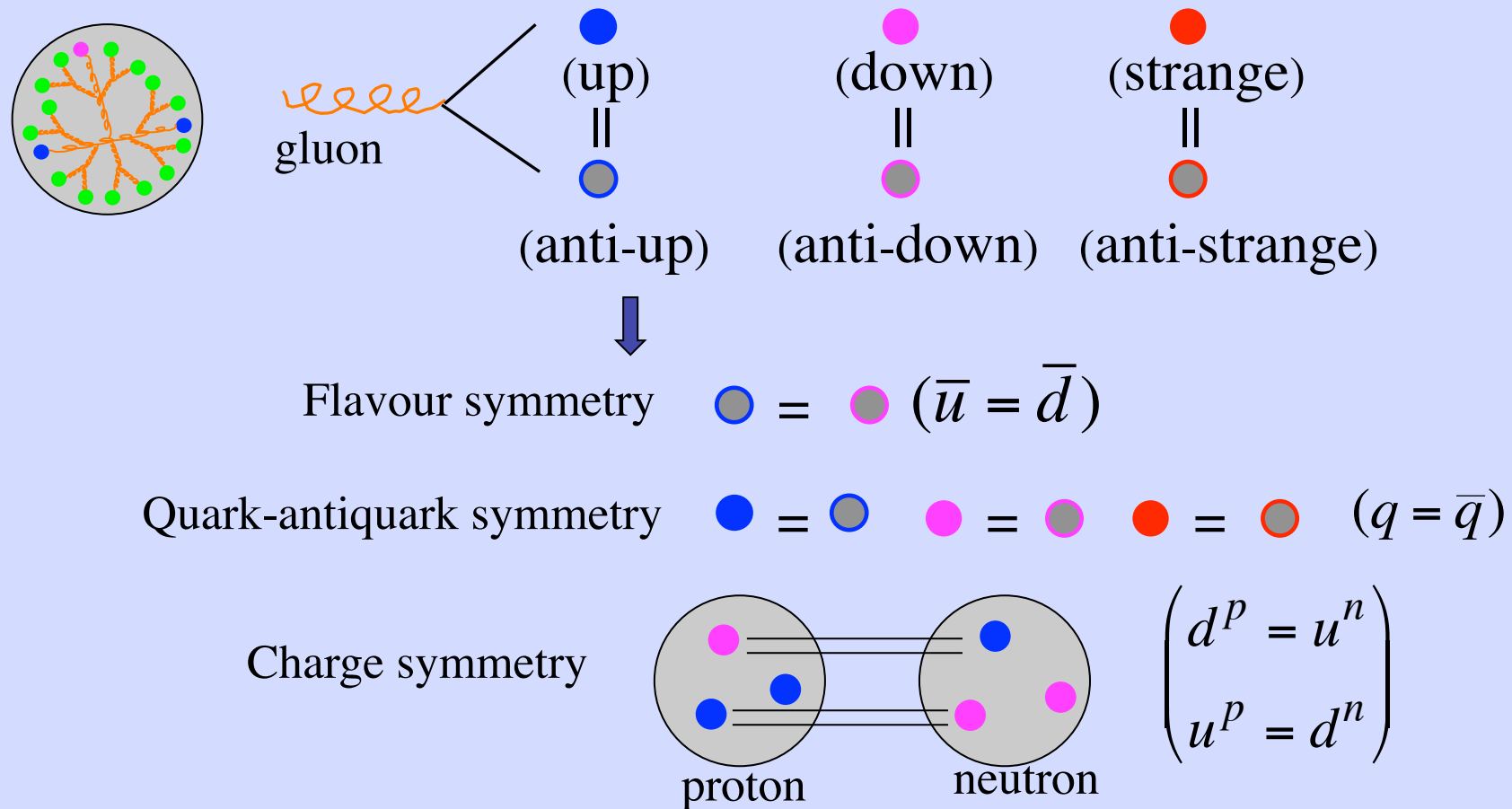


- Determination of the PDFs of the Nucleon
 - Determined via a global fit of experimental data
 - Certain function forms are assumed at an initial scale (but not in neural network methods)
 - QCD evolution equations give PDFs at different scales
 - Comparing theoretical calculations with experimental measurements for various processes
 - Can be calculated using various quark models
- Distributions for the sea quarks are not well determined

Sea quarks: $\bar{u}, \bar{d}, s, \bar{s}, c, \bar{c}, b, \bar{b}$

- Generation of the nucleon sea

Perturbative mechanism for the nucleon sea



Non-perturbative mechanism for the nucleon sea

→ Meson cloud model $|\pi^+ n\rangle > |\pi^- \Delta^{++}\rangle$

→ Pauli blocking

→ Chiral perturbation theory

$$u \rightarrow d \pi^+, \quad d \rightarrow u \pi^-$$

Break
symmetries!

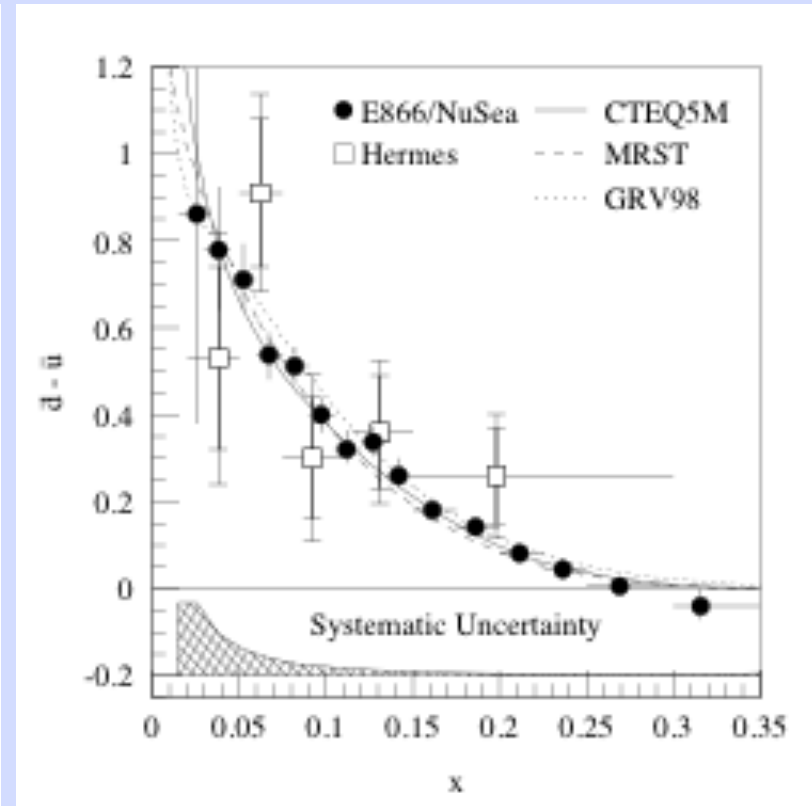
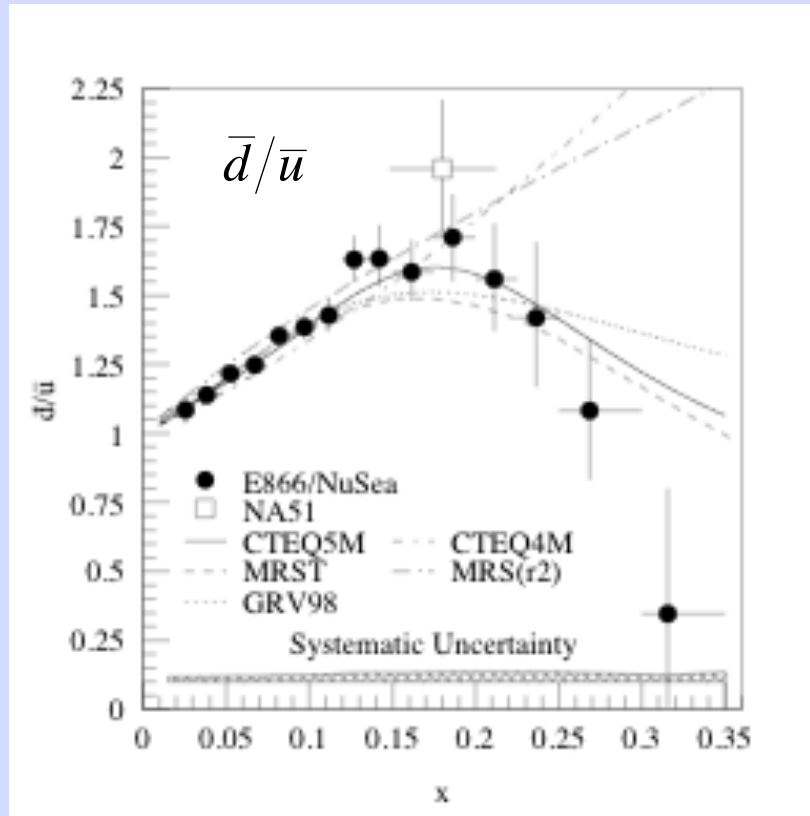
→ Chiral quark-soliton model

$$\bar{d} - \bar{u} = N_c f(x N_c)$$

→ Instanton model

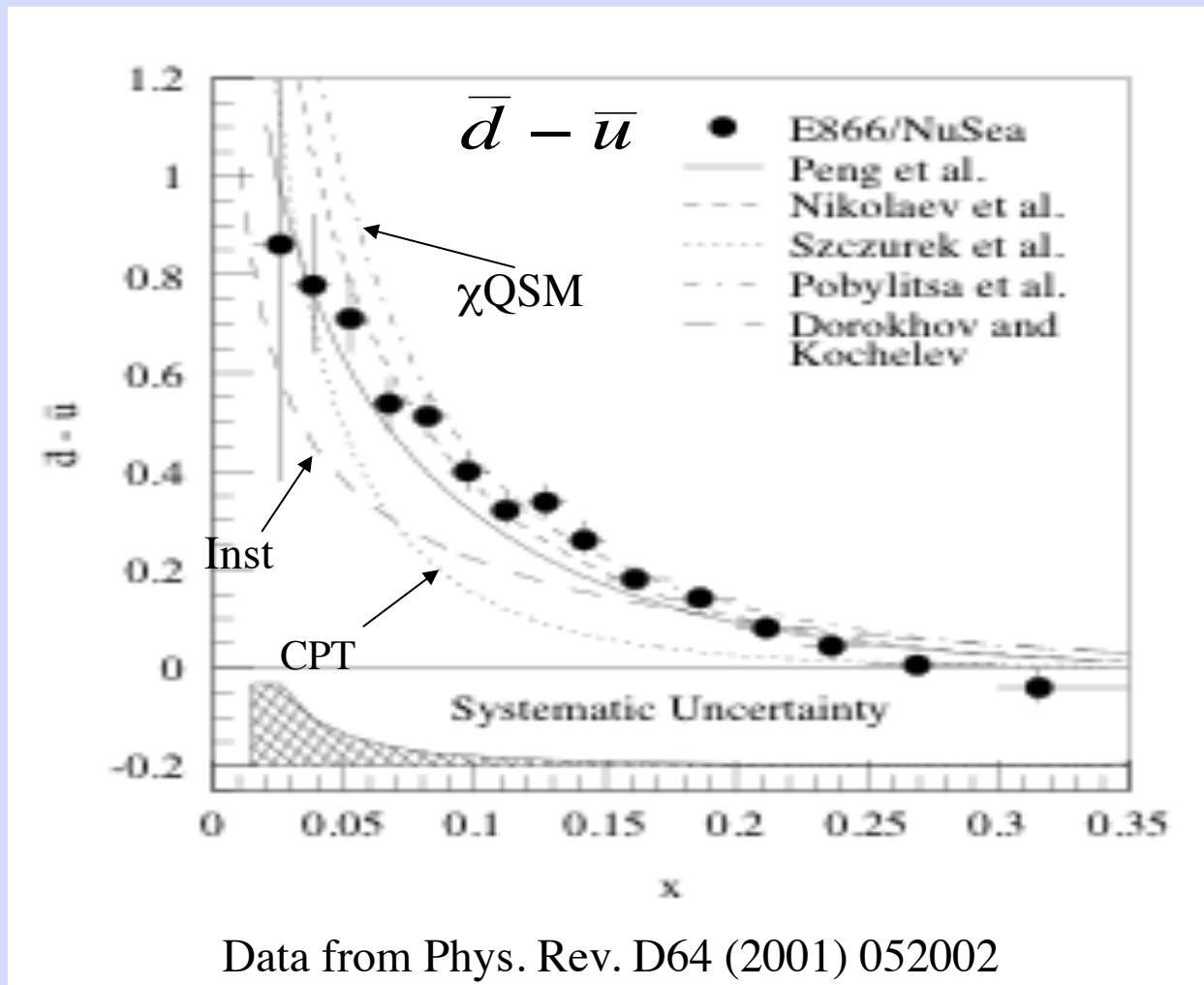
→ Isospin breaking

SU(2) flavour asymmetry in the unpolarized nucleon sea



Garvey&Peng, Prog.Part.Nucl.Phys. 47 (2001) 203-243

SU(2) flavour asymmetry in the unpolarized nucleon sea



- NuTeV anomaly

Neutrino-nucleon deep inelastic processes and
the measurement of $\sin^2 \theta_W$

NuTeV (2002): $0.2277 \pm 0.0013(\text{stat}) \pm 0.0009(\text{syst})$

World Average: 0.2227 ± 0.0004

2% difference $\rightarrow 3\sigma$ discrepancy \rightarrow

The probability that it is
consistent with the
expected result is only
about 1 in 400

- QCD corrections to the Paschos-Wolfenstein ratio

$$R^- = \frac{\sigma_{NC}^{\nu} - \sigma_{NC}^{\bar{\nu}}}{\sigma_{CC}^{\nu} - \sigma_{CC}^{\bar{\nu}}} = \frac{1}{2} - \sin^2 \theta_W + 1.3 \left[\frac{1}{2} (\langle \delta u \rangle - \langle \delta d \rangle) - (\langle s \rangle - \langle \bar{s} \rangle) \right]$$

$\delta u = u^p - d^n$; $\delta d = d^p - u^n$ Charge symmetry breaking

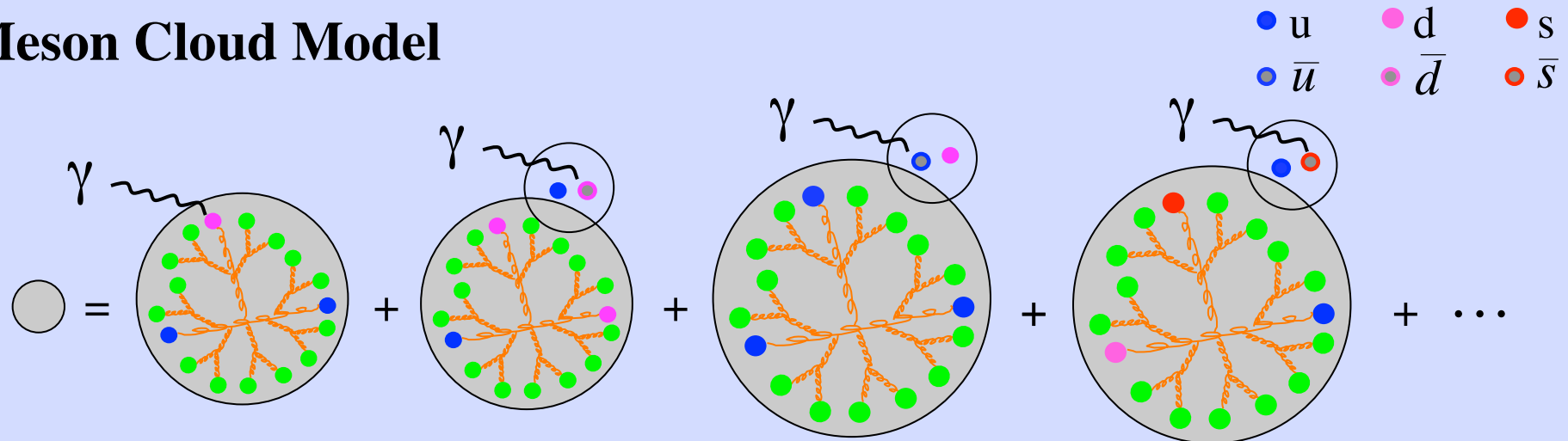
$\langle s \rangle = \int_0^1 dx x s(x)$; $\langle \bar{s} \rangle = \int_0^1 dx x \bar{s}(x)$ s-sbar asymmetry

[...] = -0.0038 is needed to explain the NuTeV anomaly

- No well established experimental evidence for these symmetry breakings
- Models to break these symmetries are known, e.g. the Meson Cloud Model

2. Symmetry breaking in the meson cloud model

Meson Cloud Model



$$|p\rangle_{phys} = |p\rangle_{bare} + |n\pi^+\rangle + |\Delta^{++}\pi^-\rangle + |\Lambda K^+\rangle + \dots$$

-- Fock state expansion of proton's wave function

- The photons may 'see' the anti-quarks in the mesons.
- Observed PDFs:

$$q_{phys} = q_{bare} + \delta q \quad \text{with} \quad \delta q = \int_x^1 \frac{dy}{y} f_{BM}(y) q^{B(M)}\left(\frac{x}{y}\right)$$

- Each NBM vertex is described by an effective Lagrangian

$$e.g. \quad L = i g_{NN\pi} \bar{N} \gamma_5 \pi N \quad \text{for the } NN\pi \text{ vertex}$$

- f is calculated using time-order perturbative theory (TOPT) in the infinite momentum frame

$$f_{BM}(y) = \sum_{\lambda\lambda'} \int_0^\infty dk_\perp^2 \left| \phi_{BM}^{\lambda\lambda'}(y, k_\perp^2) \right|^2, \quad \phi_{BM}^{\lambda\lambda'}(y, k_\perp^2) \propto V_{IMF}(y, k_\perp^2) G(y, k_\perp^2)$$

↑
Phenomenological form factor

- Prescriptions for $q^{B(M)}$

→ Bag model calculations

→ Ansatz based on lattice calculations $\int_0^1 \Delta V_\rho(x) dx = 0.6 \int_0^1 V_\rho(x) dx$
 $\rightarrow \Delta V_\rho = 0.6 V_\rho = 0.6 V_\pi$

→ SU(3) symmetry $S^\Lambda = S^\Sigma = \frac{1}{2} \mathbf{u}^N$

Mechanism for symmetry breaking:

Probabilities are different;

PDFs of meson and baryon are different.

$$q_{phys} = q_{bare} + \delta q \quad \text{with} \quad \delta q = \int_x^1 \frac{dy}{y} f_{BM}(y) q^{B(M)}\left(\frac{x}{y}\right)$$

Possible symmetry breakings:

1. Flavor symmetry breaking
2. Quark-antiquark symmetry breaking
3. Charge symmetry breaking

Flavor symmetry breaking

- SU(2) flavour asymmetry in the unpolarized nucleon sea is well established.

$$\text{Prob}(p \rightarrow n \pi^+ (u \bar{d})) > \text{Prob}(p \rightarrow \Delta \pi^0 (\bar{u} d)) \Rightarrow \bar{d} > \bar{u}$$

Flavor symmetry breaking

- Possible SU(2) flavour asymmetry in the polarized nucleon sea?
- The extent of SU(3) flavour symmetry breaking

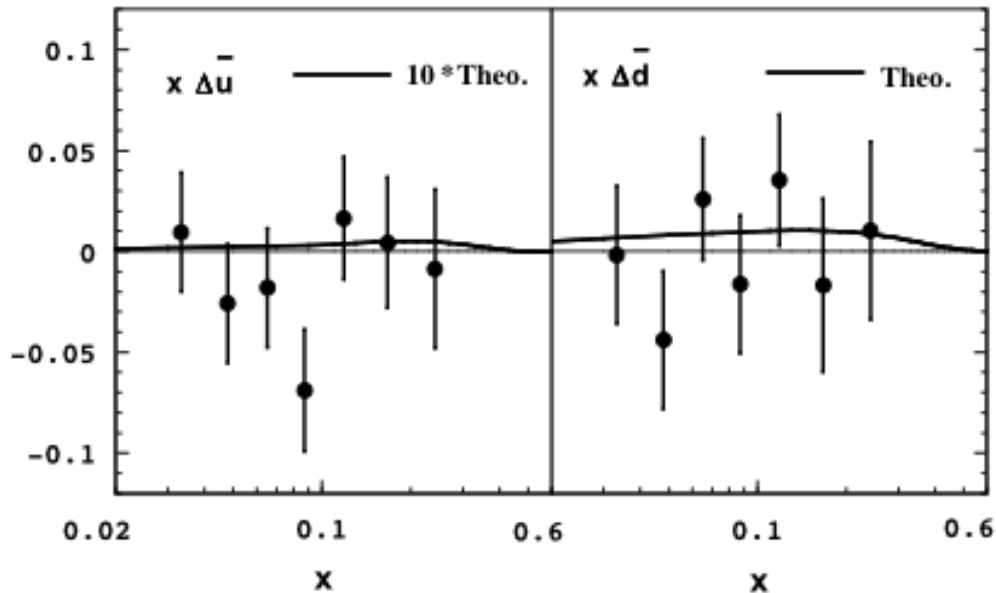
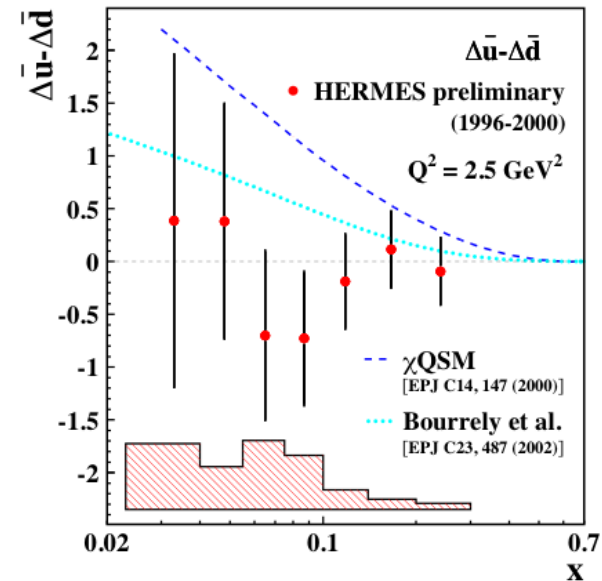
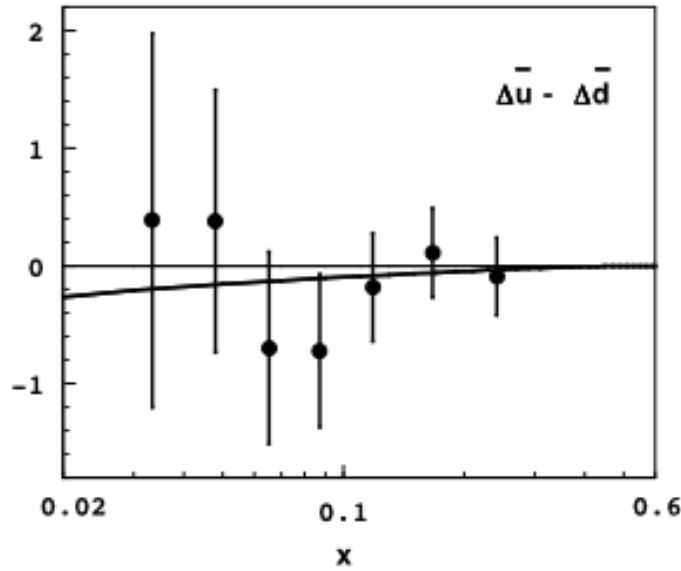
Common practice in most global QCD analyses of PDFs is

$$s(x) + \bar{s}(x) = r[\bar{u}(x) + \bar{d}(x)] \text{ with } r = 0.50 \text{ (CTEQ6.5M)}$$

while $r = 1.0$ under SU(3) symmetry and $q - \bar{q}$ symmetry.

Direct experimental evidence for the value of r is very weak.

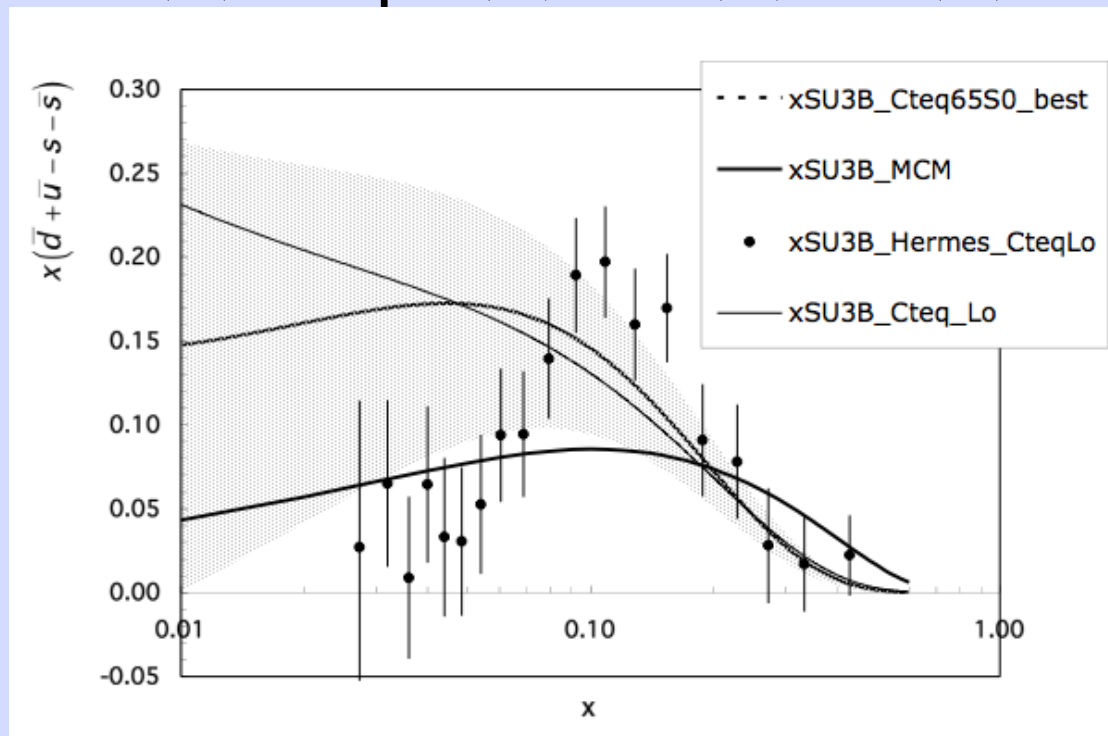
SU(2) flavour asymmetry in the polarized nucleon sea



FGC, A.I. Signal,
EPJC21(2001)105;
PRD68(2003)074002

SU(3) flavour asymmetry in the unpolarized nucleon sea

$$x\Delta(x) = x[\bar{d}(x) + \bar{u}(x) - s(x) - \bar{s}(x)]$$



H. Chen, FGC,
A.I. Signal,
JPG37(2010)1
05006

Early refs. e.g.,
S. Kumano,
PRD43(1991)59

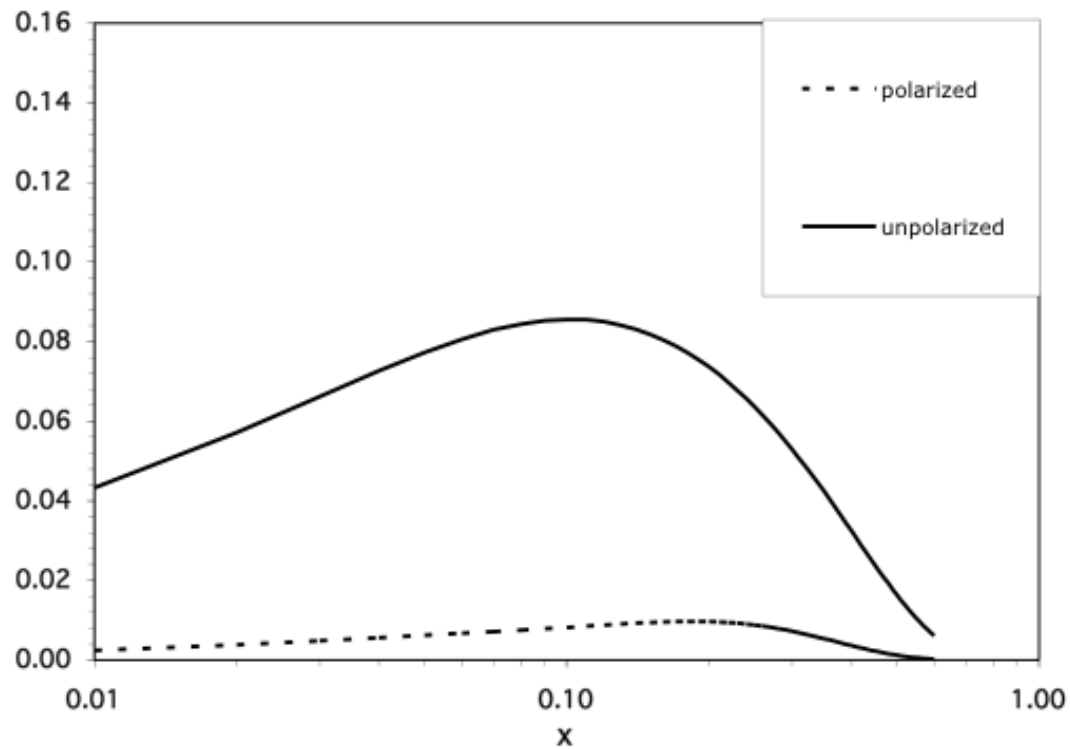
CTEQ65S [JHEP 0704 : 089,2007]:

$s(x) + \bar{s}(x)$ has different shape from $\bar{d}(x) + \bar{u}(x)$

HERMES[PLB666(2008)446 also arXiv:0803.2993]:

a measurement of $s(x) + \bar{s}(x)$ and $\Delta s(x) + \Delta \bar{s}(x)$

SU(3) flavour asymmetry in the polarized nucleon sea



Strange-antistrange asymmetry: unpolarized nucleon sea

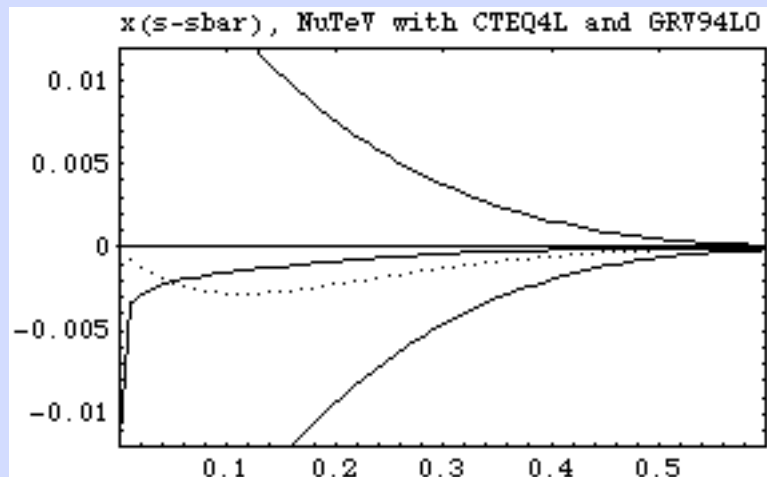
- No net strangeness: $\int_0^1 dx s(x) = \int_0^1 dx \bar{s}(x)$

- CCFR (Z. Phys. C65 (1995) 189)

$$x s = K \frac{\bar{u} + \bar{d}}{2} (1-x)^\alpha, \quad x \bar{s} = \bar{K} \frac{\bar{u} + \bar{d}}{2} (1-x)^{\bar{\alpha}}$$

\Rightarrow No evidence for $s(x) \neq \bar{s}(x)$

- NuTeV (PRD 64 (2001) 112006)

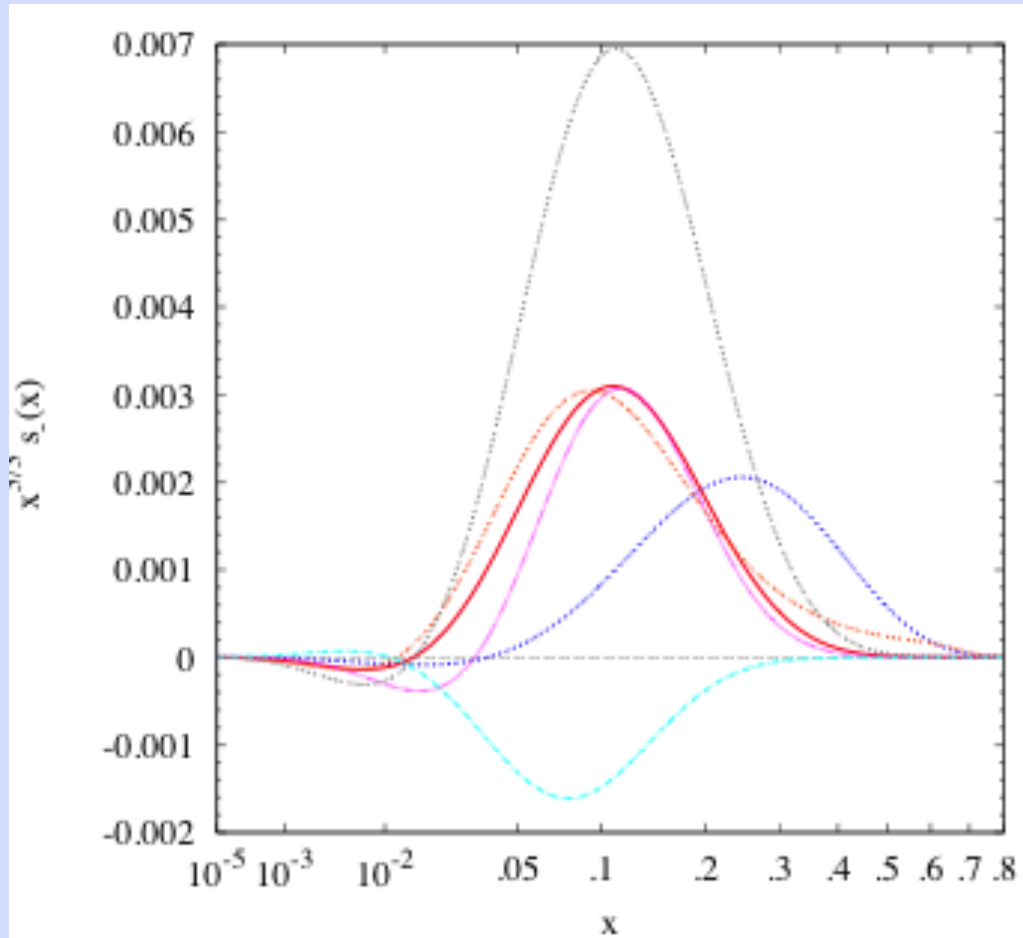


- CTEQ4L: $\langle s \rangle - \langle \bar{s} \rangle = -0.0004$

- GRV94LO: $\langle s \rangle - \langle \bar{s} \rangle = -0.0008$

- H. L. Lai et. al (CTEQ6.5S), JHEP 0704:089 (2007)

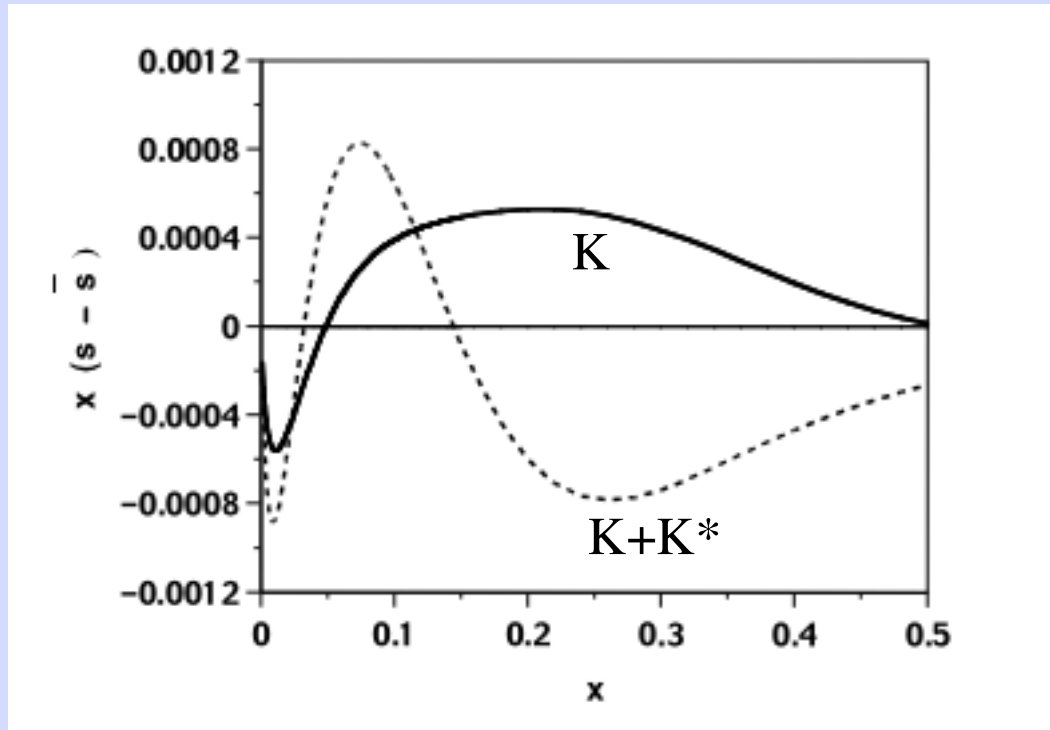
$$s_-(x, Q_0) = s_+(x, Q_0) \frac{2}{\pi} \tan^{-1} \left[cx^a \left(1 - \frac{x}{b}\right) e^{dx+ex^2} \right]$$



$$-0.001 < \langle x \rangle_{s_-} < 0.005$$

Large experimental
uncertainties

Strange-antistrange asymmetry: unpolarized nucleon sea



$$p \rightarrow \Lambda K; \Sigma K; \Lambda K^*; \Sigma K^*$$

$$p \rightarrow \Lambda K^*; \Sigma K^*$$

is expected to be suppressed.

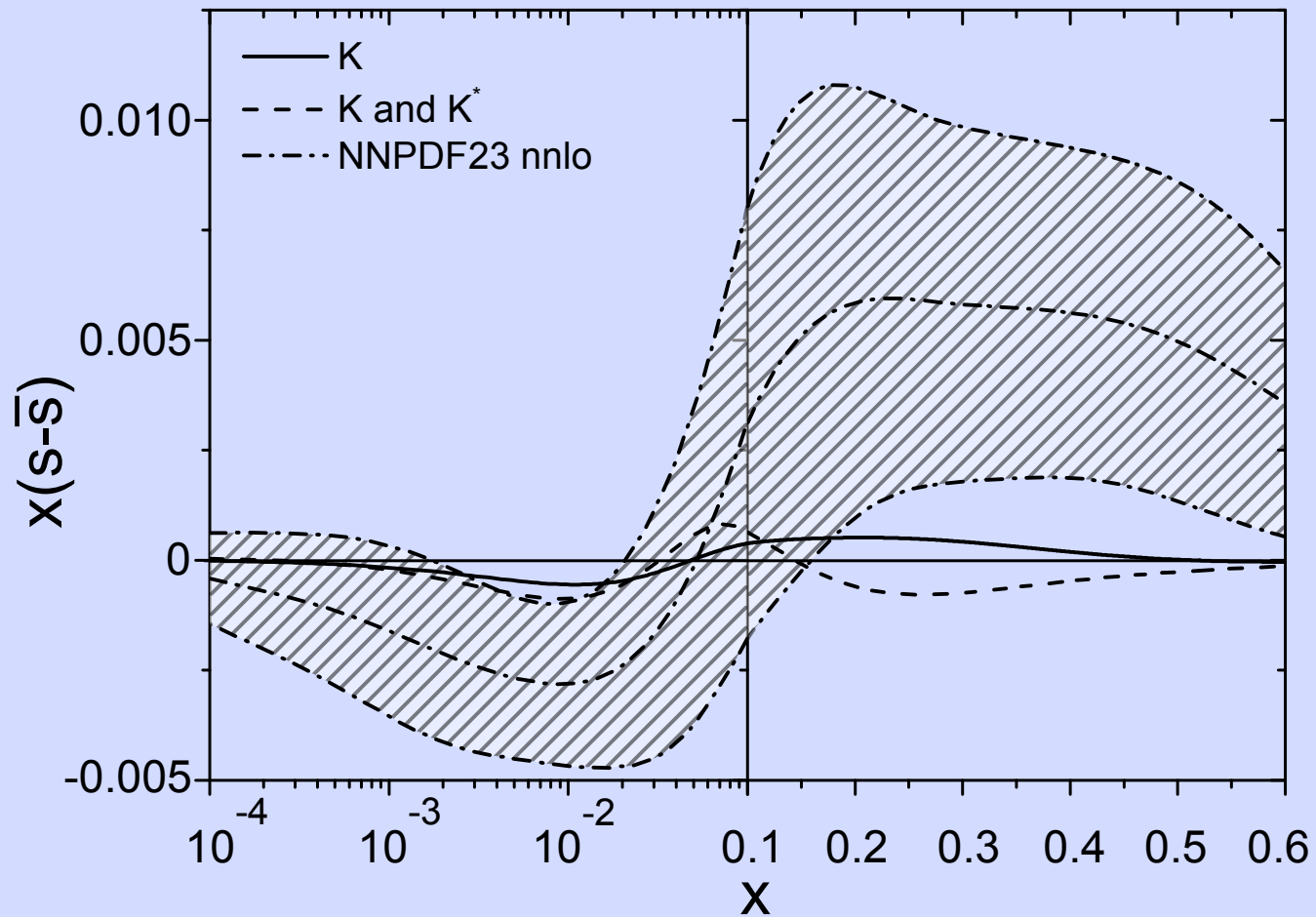
$$\langle s \rangle - \langle \bar{s} \rangle = 0.00014 \quad \text{including only K}$$

$$\langle s \rangle - \langle \bar{s} \rangle = -0.00014 \quad \text{including K+K}^*$$

FGC, A.I. Signal,
PLB559(2003)229

- Contributions from fluctuations involving K^* are important.

Comparison with global fit results



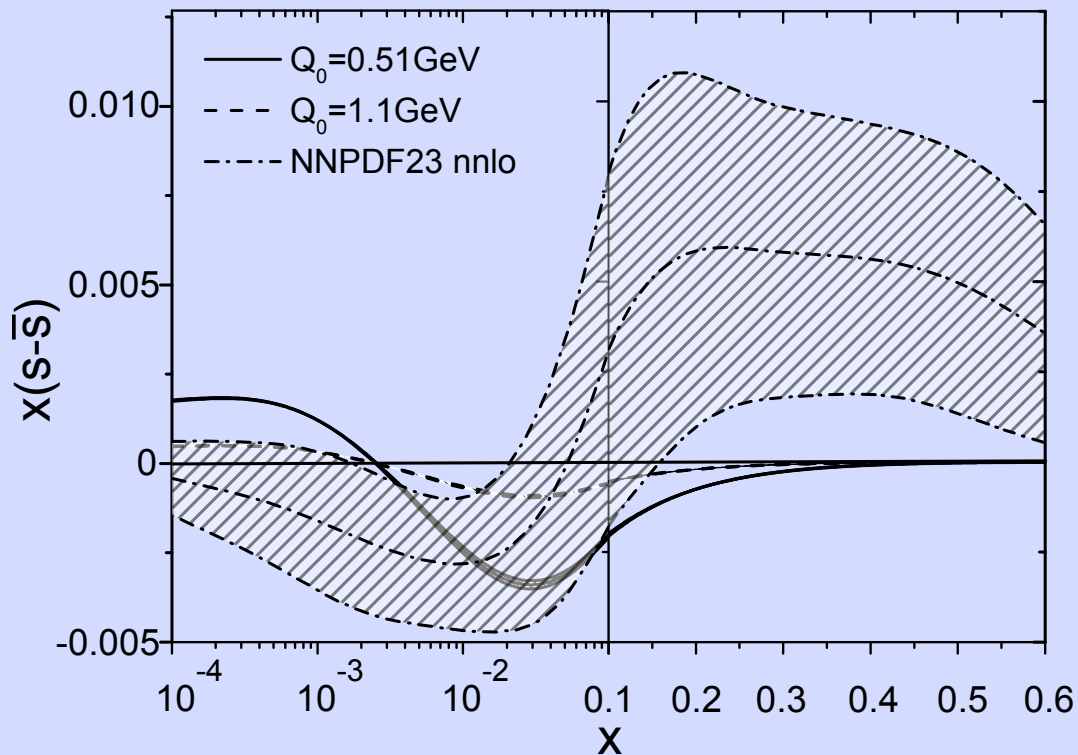
Non-pert.
contribution

G.Q. Feng, FGC,
A.I. Signal,
EPJC72(2012)2250

Perturbative vs. non-perturbative contributions

- NNLO effects [S. Catani et. al PRL93 (2004) 152003]
- Splitting functions for q and qbar are different at NNLO

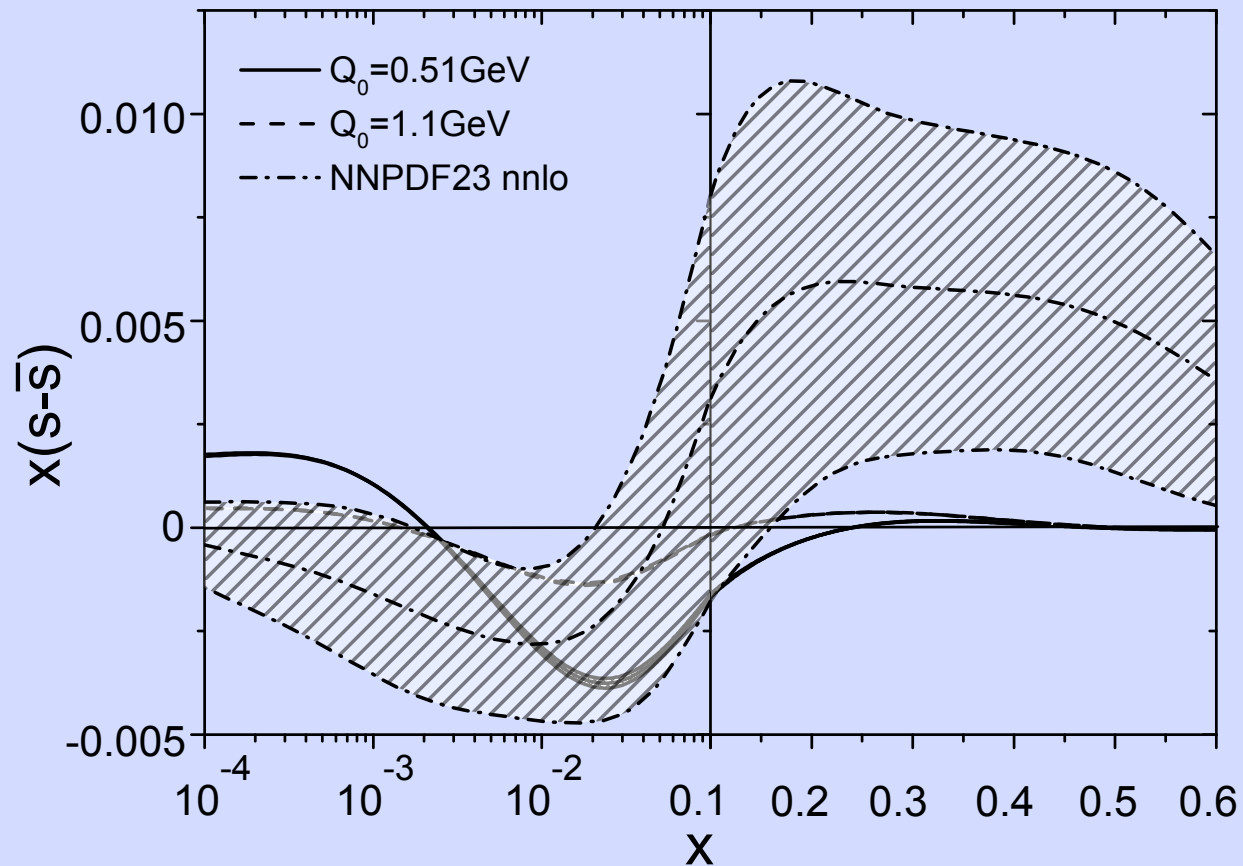
$$(s - \bar{s})(x, Q^2) \propto \int_x^1 \frac{dz}{z} P_{ns}^{(2)}\left(\frac{x}{z}\right) (u^v + d^v)(x, Q^2)$$



Perturbative
contribution

G.Q. Feng, FGC,
A.I. Signal,
EPJC72(2012)2250

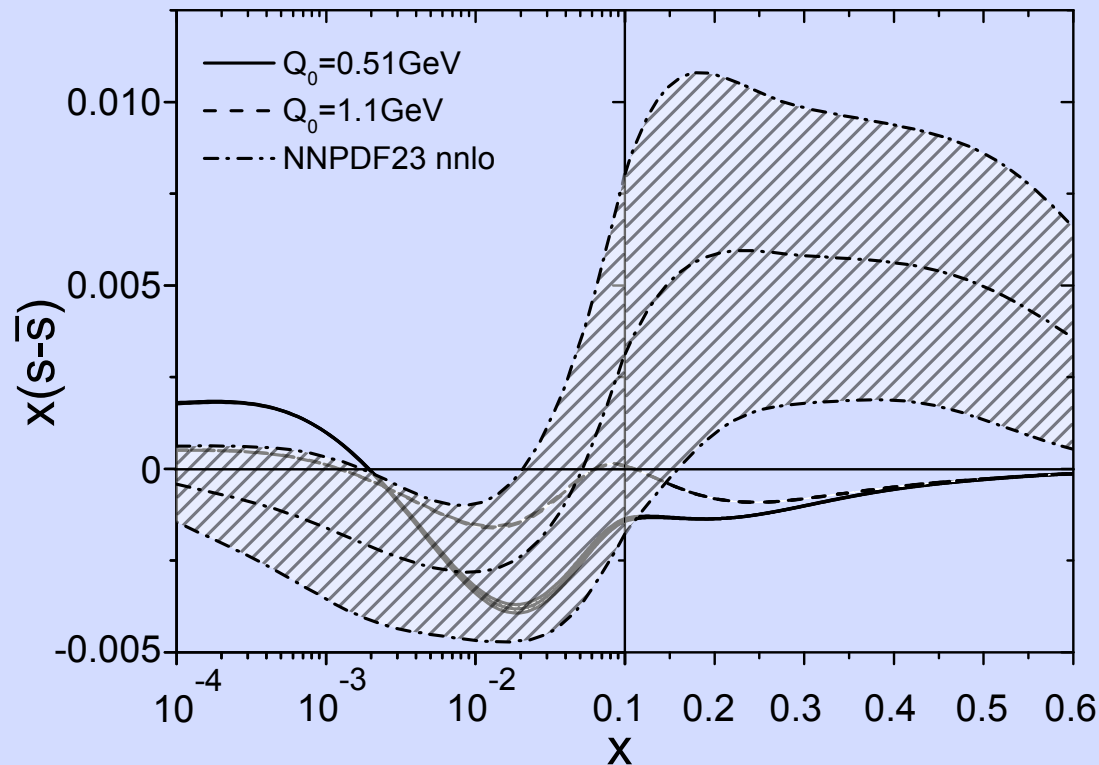
Perturbative vs. non-perturbative contributions



Pert + Non-
pert. K-mesons

G.Q. Feng, FGC,
A.I. Signal,
EPJC72(2012)2250

Perturbative vs. non-perturbative contributions

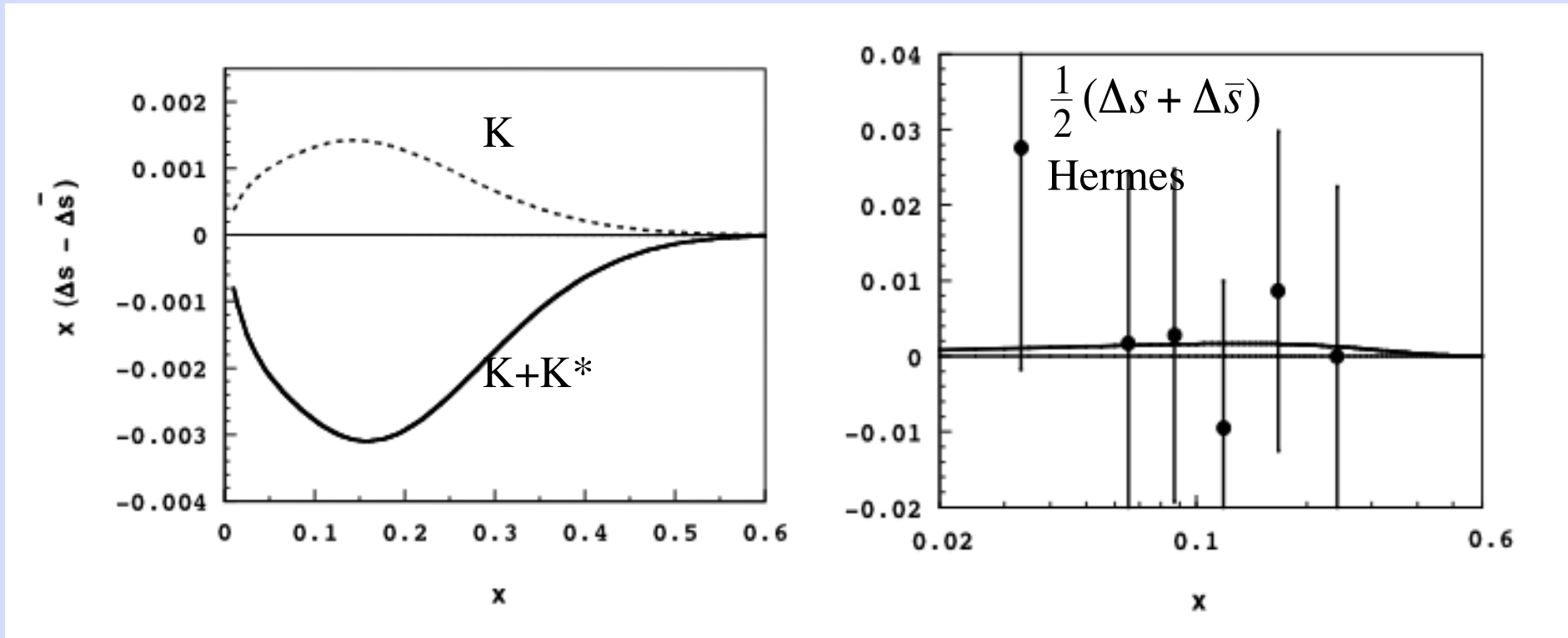


Pert + Non-
pert. $K + K^*$
mesons

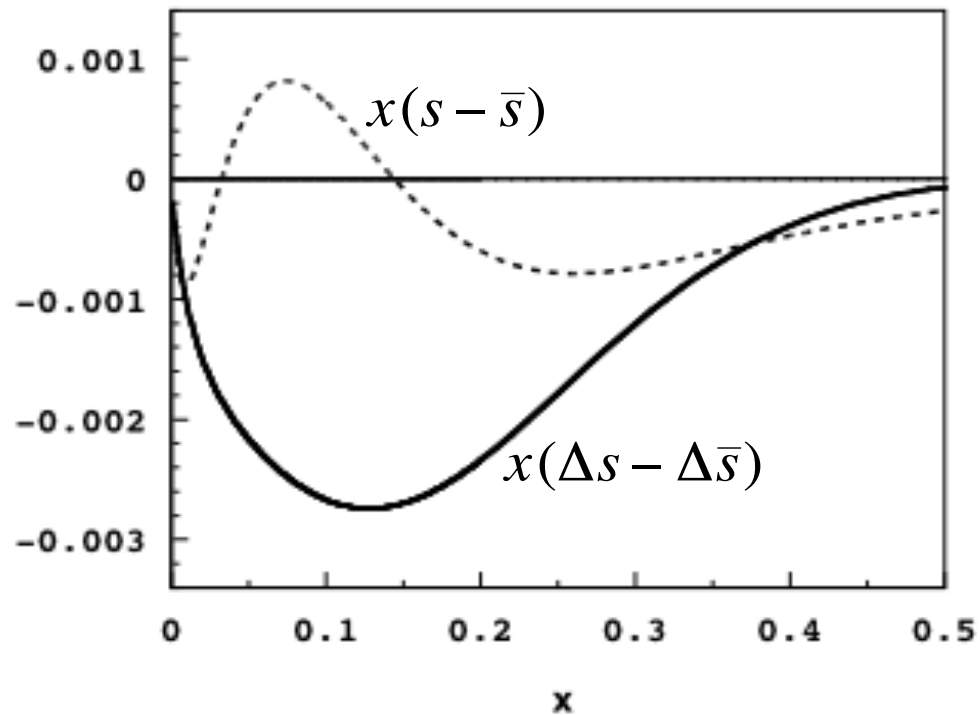
G.Q. Feng, FGC,
A.I. Signal,
EPJC72(2012)2250

- Best region to detect the asymmetry $0.02 < x < 0.03$.
- Multiple nodes having implications for parameterizations of the asymmetry in global analysis.

Strange-antistrange asymmetry: polarized nucleon sea



- Strange-antistrange symmetry is broken in the polarized nucleon sea.



FGC, A.I. Signal,
PLB559(2003)229

- Strange-antistrange asymmetry is more significant in the polarized nucleon sea than that in the unpolarized nucleon sea.

Charge symmetry breaking in the PDFs

- Definitions

$$\delta u_V = u_V^p - d_V^n; \quad \delta d_V = d_V^p - u_V^n;$$

$$\delta \bar{u} = \bar{u}_V - \bar{d}_V; \quad \delta \bar{d} = \bar{d}_V - \bar{u}_V; \quad \delta s = s^p - s^n; \quad \delta \bar{s} = \bar{s}^p - \bar{s}^n$$

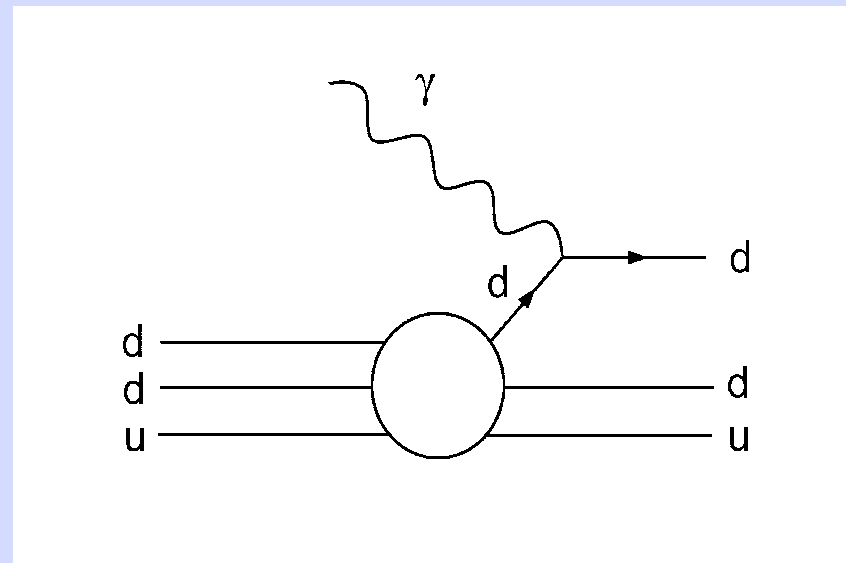
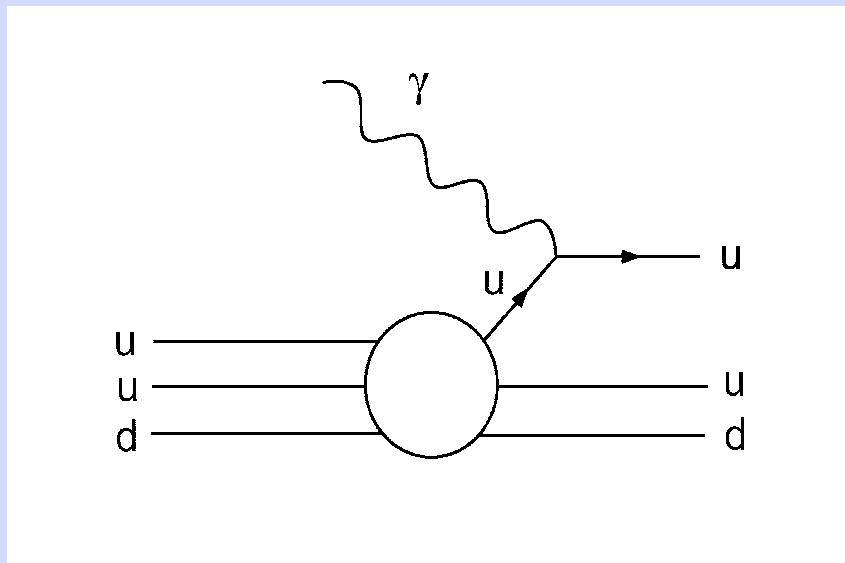
- CS is universally assumed in the quark phenomenology

- Nuclear physics: 1%

- EW interaction: $\frac{m_d - m_u}{M} = \frac{3 \sim 5 \text{ MeV}}{0.5 \sim 1 \text{ GeV}} < 1\%$

- Quark model calculations:

EW interaction; mass differences of the struck quark; mass differences of the di-quark; quark wavefunction



(Ref: Prog. Par. Nucl 41 (1998) 41; Londegran and Thomas)

- MCM calculation for the charge symmetry breaking

$$d^P = d_{bare}^P + d_{per.}^P + d_{non}^P; \quad u^n = u_{bare}^n + u_{per.}^n + u_{non}^n;$$

$$\bar{d}^P = \bar{d}_{per.}^P + \bar{d}_{non}^P; \quad \bar{u}^{-n} = \bar{u}_{per.}^{-n} + \bar{u}_{non}^{-n};$$

$$\Downarrow d_{per.}^P = \bar{d}_{per.}^P;$$

$$d_V^P = d_{bare}^P + d_{non}^P - \bar{d}_{non}^P; \quad u_V^n = u_{bare}^n + u_{non}^n - \bar{u}_{non}^{-n};$$

$$\delta d_V = \left[d_{bare}^P - u_{bare}^n \right] + \left[\left(d_{non}^P - \bar{d}_{non}^P \right) - \left(u_{non}^n - \bar{u}_{non}^{-n} \right) \right];$$

↑

Calculated with
quark models

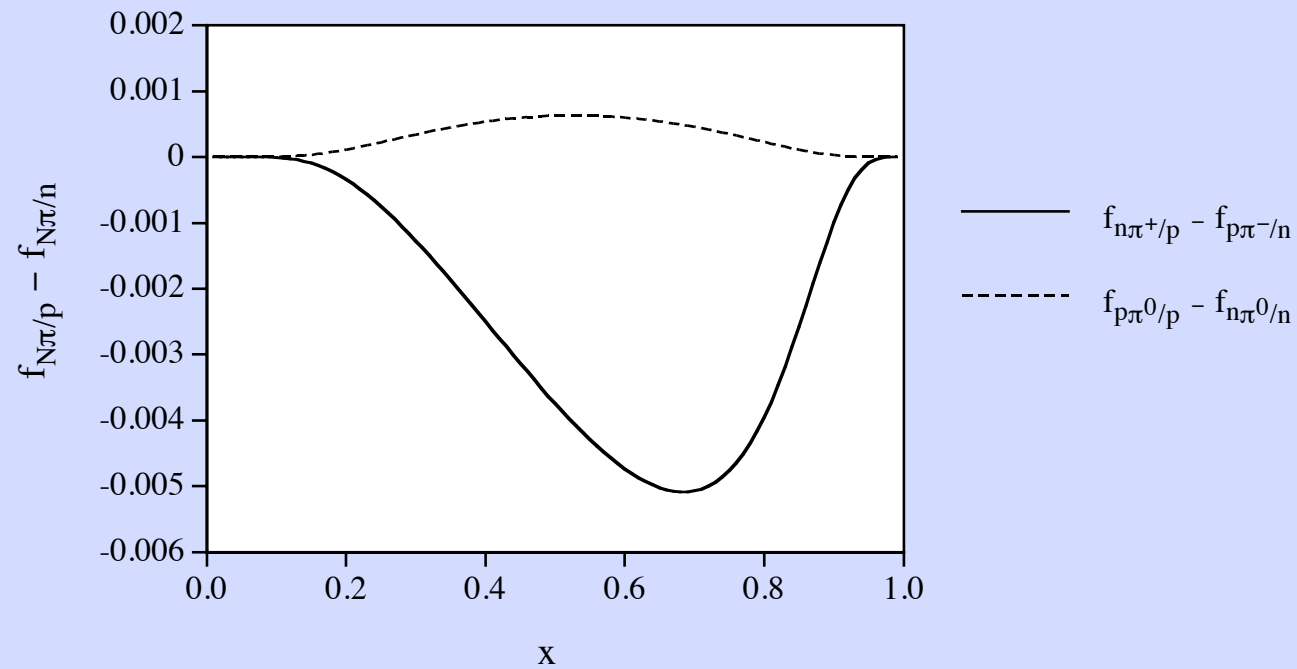
↑

Calculated with the
Meson cloud model

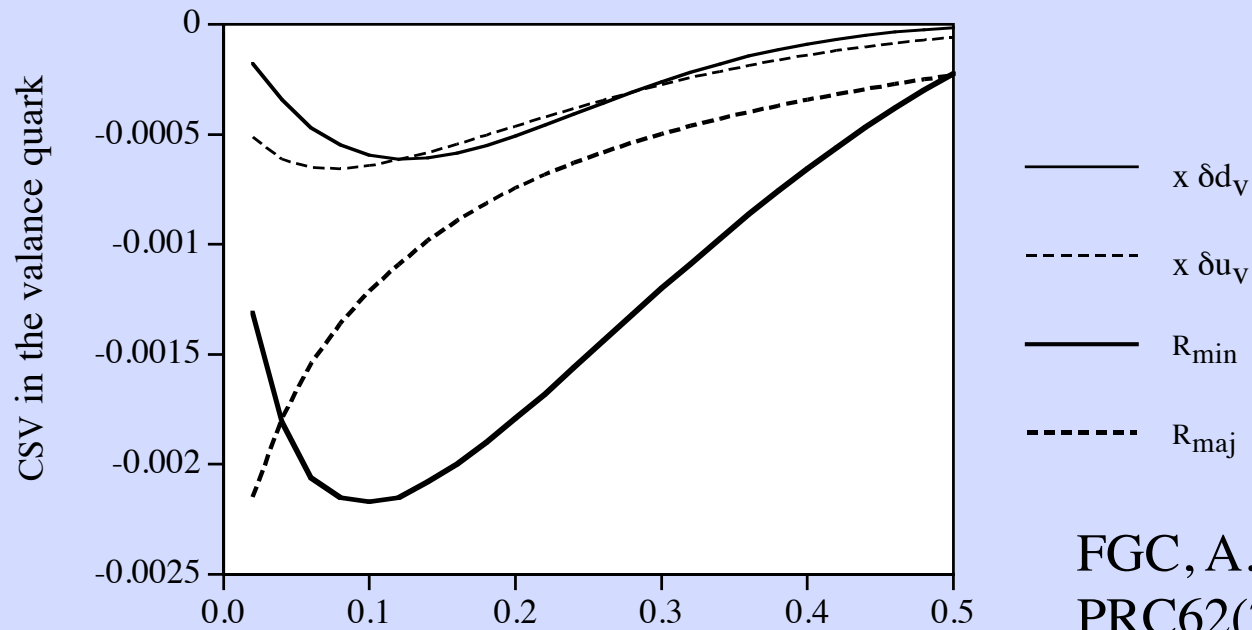
- MCM calculation for the charge symmetry breaking

Fluctuations considered include:

$$\begin{aligned}
 p &\rightarrow n \pi^+; & n &\rightarrow p \pi^-; & m_p - m_n &= -1.3 \text{ MeV}, \\
 p &\rightarrow \Delta^0 \pi^+; & n &\rightarrow \Delta^+ \pi^-; & m_{\pi^\pm} - m_{\pi^0} &= 4.6 \text{ MeV, etc} \\
 p &\rightarrow \Lambda K^+; & n &\rightarrow \Lambda K^0
 \end{aligned}$$



Charge symmetry breaking in the valence quarks

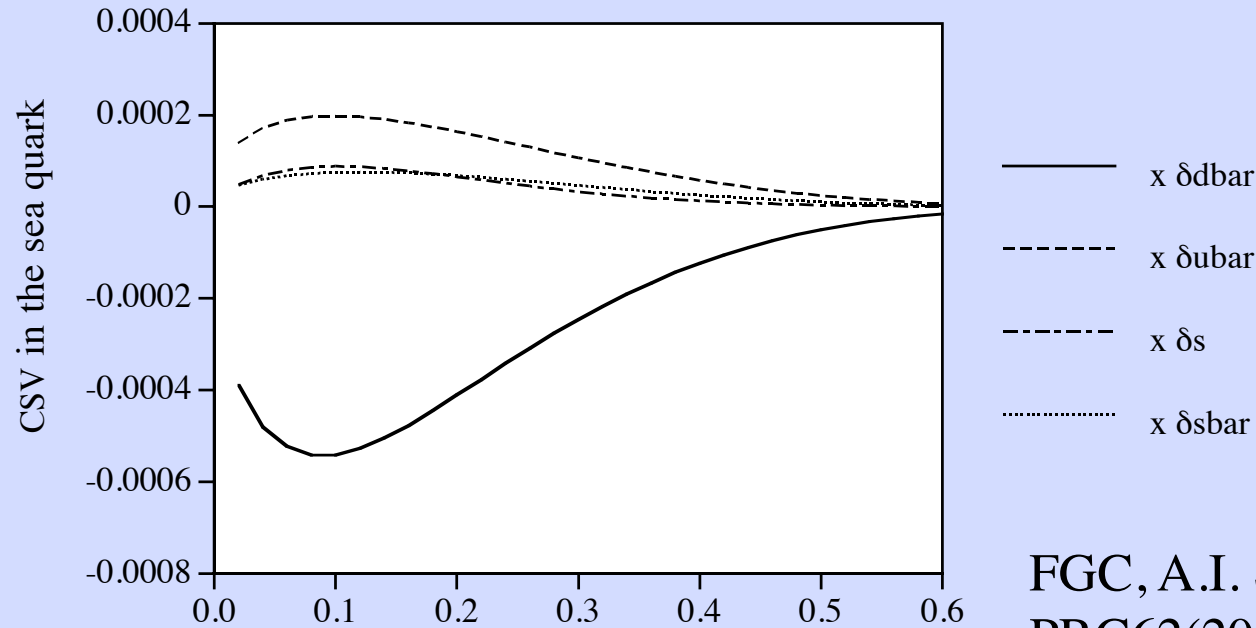


FGC, A.I. Signal,
PRC62(2000)015203

$$\delta u_V = u_V^p - d_V^n, \quad \delta d_V = d_V^p - u_V^n;$$

$$R_{\min} = \frac{\delta d_V}{d_V}, \quad R_{\max} = \frac{\delta u_V}{u_V}$$

Charge symmetry breaking in the sea quarks



FGC, A.I. Signal,
PRC62(2000)015203

$$\delta \bar{u} = \bar{u}_V - \bar{d}_V; \quad \delta \bar{d} = \bar{d}_V - \bar{u}_V; \quad \delta s = s^p - s^n; \quad \delta \bar{s} = \bar{s}^p - \bar{s}^n$$

Meson cloud contributions to the CSV are slightly smaller than that calculated with quark models.

3. Strange sea distributions

Strange sea distributions are not well determined compared with the valence distributions and light quark sea.

CTEQ6.5S [H. L. Lai et. al, JHEP 0704:089 (2007)]

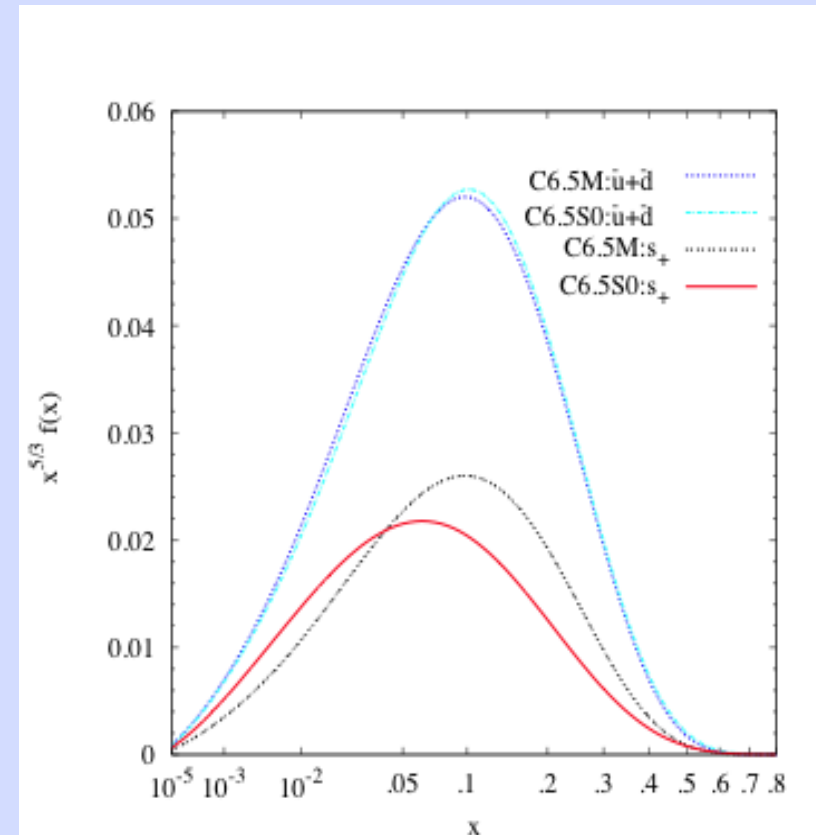
$$s_{\pm}(x, Q_0) = s(x, Q_0) \pm \bar{s}(x, Q_0)$$

$$s_+(x, Q_0) = A_0 x^{A_1} (1-x)^{A_2}$$

$$A_1^{s_+} = A_1^{(\bar{u}+\bar{d})_+} \text{ is assumed}$$

A_0 is related to suppression factor

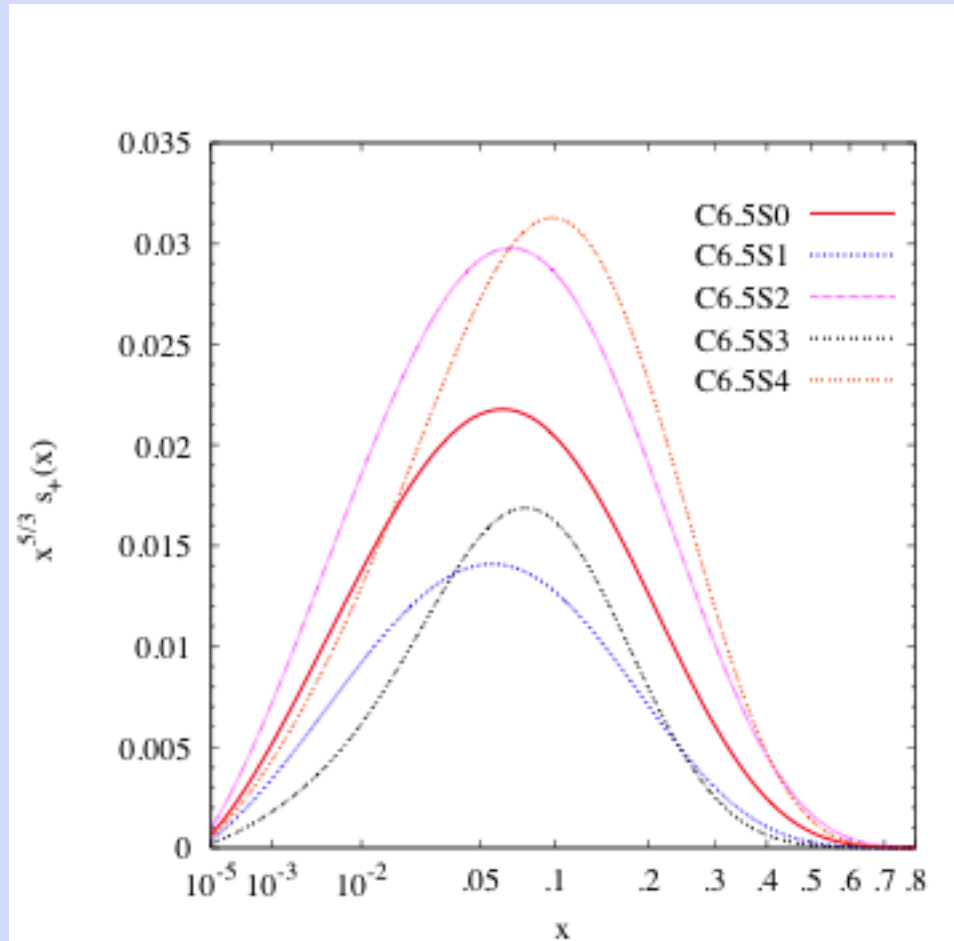
$$r = \frac{\langle x \rangle_{s_+}}{\langle x \rangle_{\bar{u}(x)+\bar{d}(x)}}$$



Light sea is almost unchanged while $s_+(x)$ becomes smaller and softer compared to CTEQ6.5M.

$r = 0.44$ (CTEQ6.5S₀) vs. 0.50 (CTEQ6.5M)

- Allowed range for $s_+(x)$

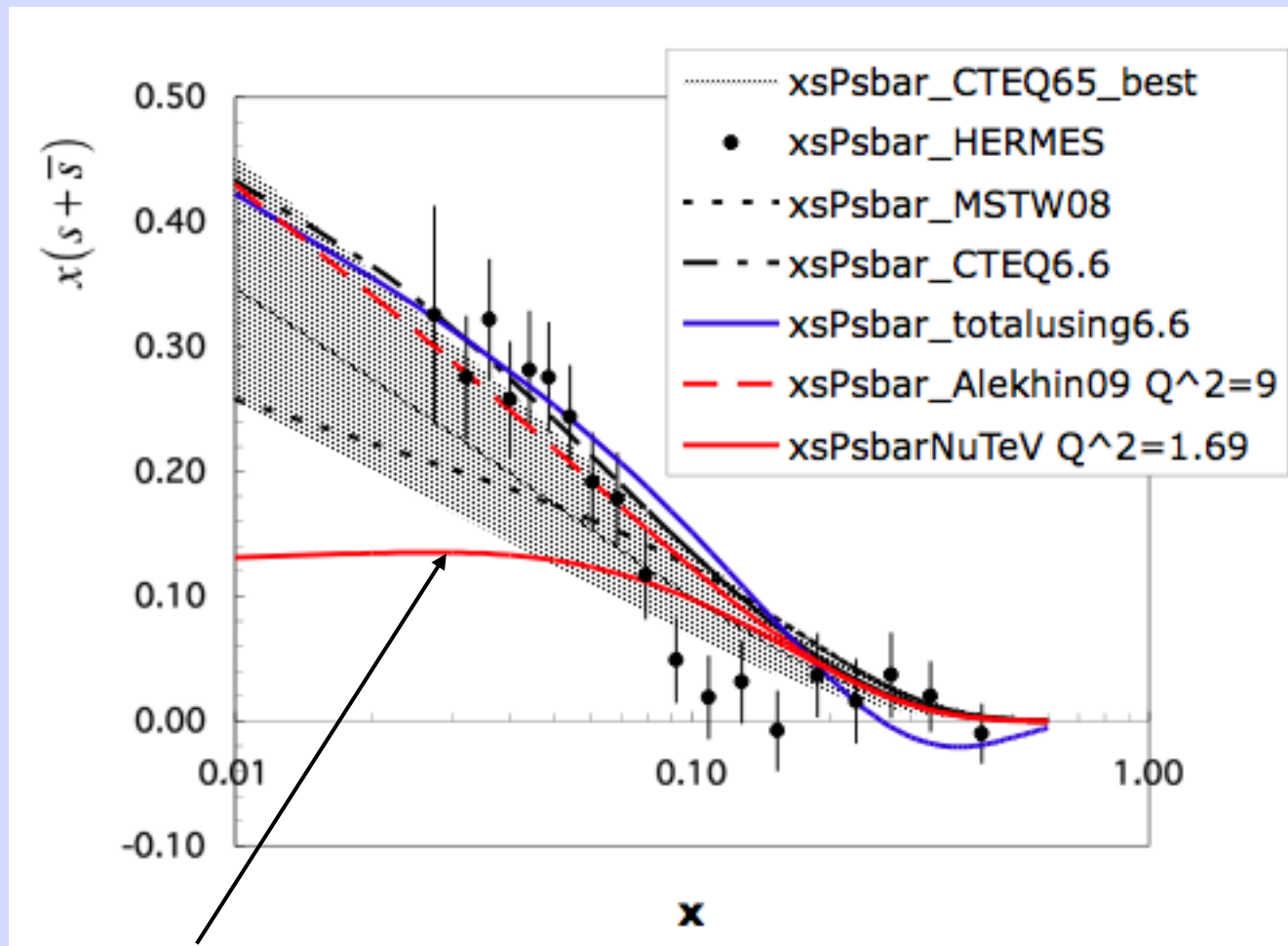


Momentum fraction

$$0.018 < \langle x \rangle < 0.040;$$

Different parameterizations

$$xS_+(x) = \left[\bar{d}(x) + \bar{u}(x) \right]_{\text{Fit}} - x\Delta(x)_{\text{MCM}}$$



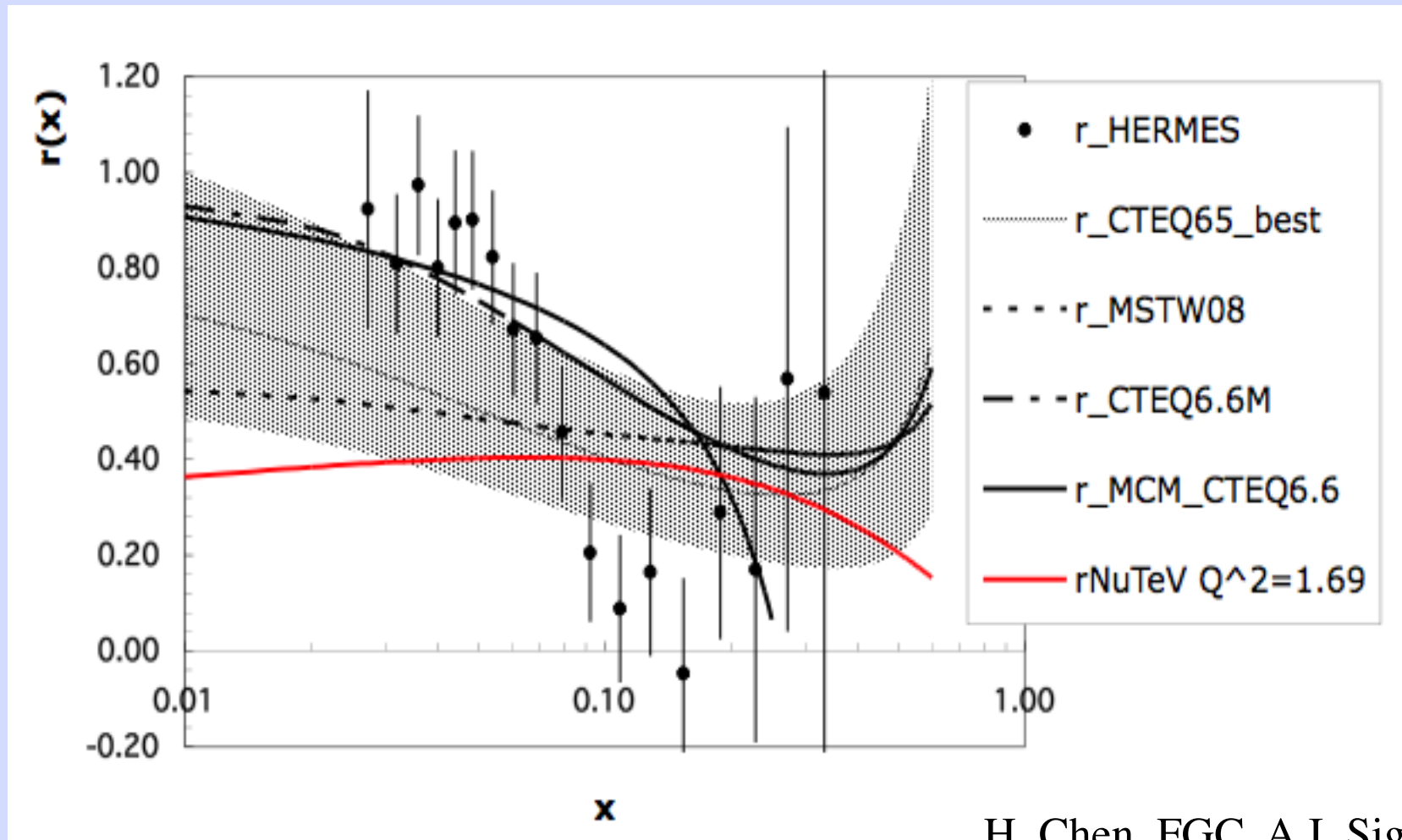
NLO analysis of NuTeV data PRL99(2007)192001

H. Chen, FGC, A.I. Signal,

JPG37(2000)105006

SPIN 2014, Oct 2014, Beijing

The suppression factor $r(x) = \frac{s(x) + \bar{s}(x)}{\bar{d}(x) + \bar{u}(x)}$



H. Chen, FGC, A.I. Signal,
JPG37(2000)105006

4. Summary

- Non-pert. QCD models for the nucleon structure can make reliable predictions for the symmetry breaking effects.
- Possible strange-antistrange asymmetry is of great interest. The asymmetry may have multiple nodes.
- Strange sea distributions are not well constrained. Combining the MCM calculations for the $SU(3)_f$ breaking effect with global analysis results for the light quark sea, we estimated the total strange sea distributions.