

Nuclear Parton Distributions

(concentrating on nCTEQ)

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Outline

Introduction

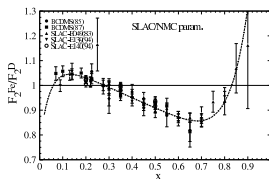
Global Analysis

Summary of available nuclear PDFs

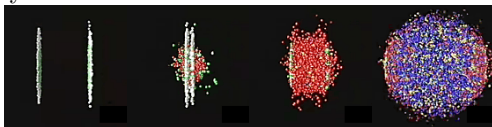
nCTEQ results

Motivations: Why do we need nuclear PDFs?

- ▶ What are PDFs of bound protons/neutrons?



- ▶ Heavy ion collisions in LHC and RHIC



- ▶ Differentiate flavors in free-proton PDFs (e.g. strange)

charged lepton DIS

$$F_2^{l^\pm} \sim \left(\frac{1}{3}\right)^2 [d + s] + \left(\frac{2}{3}\right)^2 [u + c]$$

neutrino DIS

$$F_2^\nu \sim [d + s + \bar{u} + \bar{c}]$$

$$F_2^{\bar{\nu}} \sim [\bar{d} + \bar{s} + u + c]$$

$$F_3^\nu \sim 2[d + s - \bar{u} - \bar{c}]$$

$$F_3^{\bar{\nu}} \sim 2[u + c - \bar{d} - \bar{s}]$$

Motivations: differentiate flavors in proton PDFs

- ▶ To differentiate flavors we need to probe different linear combinations of PDFs

charged lepton DIS

$$F_2^{l\pm} \sim \left(\frac{1}{3}\right)^2 [d + s] + \left(\frac{2}{3}\right)^2 [u + c]$$

neutrino DIS

$$F_2^\nu \sim [d + s + \bar{u} + \bar{c}]$$

$$F_2^{\bar{\nu}} \sim [\bar{d} + \bar{s} + u + c]$$

$$F_3^\nu \sim 2[d + s - \bar{u} - \bar{c}]$$

$$F_3^{\bar{\nu}} \sim 2[u + c - \bar{d} - \bar{s}]$$

- ▶ Neutrino data gives access to different flavor combinations.
- ▶ Can be done only with heavy nuclear targets.
- ▶ Depend on nuclear corrections.

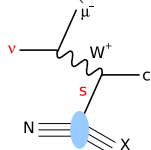
Motivations: proton Strange PDF

Before CTEQ6.6 proton PDFs it was assumed

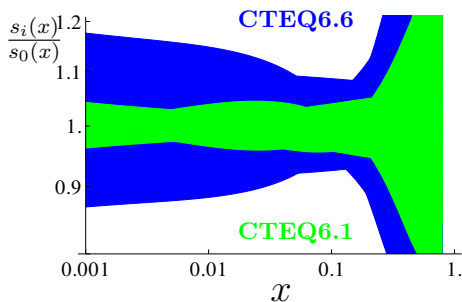
P. Nadolsky et al. PRD 78, 013004 (2008), arXiv:0802.0007

$$s(x) = \bar{s}(x) \sim \kappa \frac{\bar{u}(x) + \bar{d}(x)}{2}, \quad \kappa = \frac{1}{2}$$

- ▶ Underestimating s PDF uncertainty, as \bar{u} , \bar{d} are much better constrained.
- ▶ Neutrino-nucleon dimuon data (CCFR, NuTeV)



allowed to fit s PDF independently of \bar{u} , \bar{d} sea.

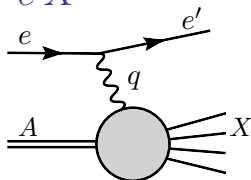


Variables: DIS of nuclear target $eA \rightarrow e'X$

- ▶ DIS variables in case on nucleons

$$\text{in nucleus } \begin{cases} Q^2 \equiv -q^2 \\ x_A \equiv \frac{Q^2}{2p_A \cdot q} \end{cases}$$

- ▶ p^A – nucleus momentum
- ▶ $x_A \in (0, 1)$ – analog of Bjorken variable
(fraction of the nucleus momentum carried by a nucleon)



- ▶ Analogue variables for partons:

- ▶ $p_N = \frac{p_A}{A}$ – average nucleon momentum
- ▶ $x_N \equiv \frac{Q^2}{2p_N \cdot q} = A x_A$ – parton momentum fraction with respect to the average nucleon momentum p_N
- ▶ $x_N \in (0, A)$ – parton can carry more than the average nucleon momentum p_N .

Assumptions entering the nuclear PDF analysis

1. **Factorization** & DGLAP evolution
 - ▶ allow for definition of **universal PDFs**
 - ▶ make the formalism **predictive**
 - ▶ needed even if it is broken
2. Isospin symmetry $\begin{cases} u^{n/A}(x) = d^{p/A}(x) \\ d^{n/A}(x) = u^{p/A}(x) \end{cases}$
3. The *bound proton* PDFs have the *same evolution equations* and sum rules as the free proton PDFs *provided we neglect any contributions from the region $x > 1$* (which is expected to have negligible contribution [[PRC 73, 045206 \(2006\)](#), [arXiv:hep-ph/0509241](#)])

Then observables \mathcal{O}^A can be calculated as:

$$\mathcal{O}^A = Z \mathcal{O}^{p/A} + (A - Z) \mathcal{O}^{n/A}$$

With the above assumptions we can use the free proton framework to analyze nuclear data

Schematics of Global Analysis

1. Parametrize PDFs at low initial scale $\mu = Q_0 = 1.3\text{GeV}$:

$$f(x, Q_0) = f(x; a_0, a_1, \dots) = a_0 x^{a_1} (1-x)^{a_2} P(x; a_3, \dots)$$

2. Use DGLAP equation to evolve $f(x, \mu)$ from $\mu = Q_0$ to $\mu = Q_{\text{max}}$.
3. Define and minimize appropriate χ^2 function (with respect to parameters a_0, a_1, \dots)

$$\chi^2(\{a_i\}) = \sum_{\text{experiments}} w_n \chi_n^2(\{a_i\})$$

$$\chi_n^2(\{a_i\}) = \sum_{\text{data points}} \left(\frac{\text{data} - \text{theory}(\{a_i\})}{\text{uncertainty}} \right)^2$$

(by default $w_n = 1$)

Uncertainties in global analysis

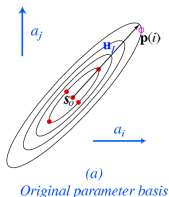
- ▶ **Experimental errors** (included in PDFs error analysis)
- ▶ **Theoretical uncertainties** (not included)
- ▶ **“Details”** of Global Fits
(e.g. parametrization, HF schemes; hard to estimate not included)

Propagating experimental errors to PDFs:

- ▶ Hessian Method
 - ▶ Eigenvector PDFs
 - ▶ Quadratic approximation
 - ▶ Simple computation of correlations
- ▶ Lagrange Multipliers
- ▶ Monte Carlo Methods

- **Expand** χ^2 function around minimum, $\{a_i^0\}$,

$$\chi^2 = \chi_0^2 + \sum_{ij} \frac{1}{2} (a_i - a_i^0)(a_j - a_j^0) \left(\frac{\partial^2 \chi^2}{\partial y_i \partial y_j} \right)_0$$

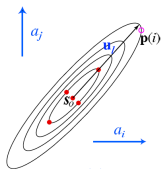


Hessian method

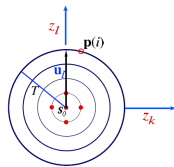
[JHEP 07 (2002) 012, arXiv:hep-ph/0201195]

- **Expand** χ^2 function around minimum, $\{a_i^0\}$, and **diagonalize**

$$\chi^2 = \chi_0^2 + \sum_{ij} \frac{1}{2} (a_i - a_i^0)(a_j - a_j^0) \left(\frac{\partial^2 \chi^2}{\partial y_i \partial y_j} \right)_0 = \chi_0^2 + \sum_i z_i^2$$



(a)
Original parameter basis

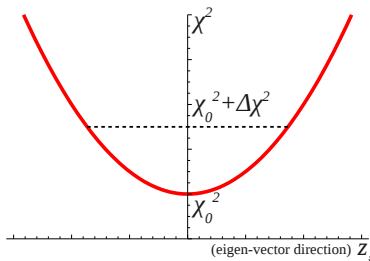


(b)
Orthonormal eigenvector basis

- ▶ **Expand** χ^2 function around minimum, $\{a_i^0\}$, and **diagonalize**

$$\chi^2 = \chi_0^2 + \sum_{ij} \frac{1}{2} (a_i - a_i^0)(a_j - a_j^0) \left(\frac{\partial^2 \chi^2}{\partial y_i \partial y_j} \right)_0 = \chi_0^2 + \sum_i z_i^2$$

- ▶ Choose tolerance criteria $\Delta\chi^2 = \chi^2 - \chi_0^2$ value (defining $1-\sigma$ uncertainty),
 - ▶ ideal case $\Delta\chi^2 = 1$
 - ▶ realistic global analysis $\Delta\chi^2 \sim 1 - 100$



- ▶ **Expand** χ^2 function around minimum, $\{a_i^0\}$, and **diagonalize**

$$\chi^2 = \chi_0^2 + \sum_{ij} \frac{1}{2} (a_i - a_i^0)(a_j - a_j^0) \left(\frac{\partial^2 \chi^2}{\partial y_i \partial y_j} \right)_0 = \chi_0^2 + \sum_i z_i^2$$

- ▶ Choose tolerance criteria $\Delta\chi^2 = \chi^2 - \chi_0^2$ value (defining 1- σ uncertainty),
 - ▶ ideal case $\Delta\chi^2 = 1$
 - ▶ realistic global analysis $\Delta\chi^2 \sim 1 - 100$
- ▶ Construct error PDFs corresponding to each eigenvector direction:

$$f_i^\pm = f(\{z_i\}) = f(0, \dots, z_i = \pm\sqrt{\Delta\chi^2}, \dots, 0)$$

$$z_i = \pm\sqrt{\Delta\chi^2}$$

- ▶ Calculate errors of observable X :

$$\Delta X = \frac{1}{2} \sqrt{\sum_i [X(f_i^+) - X(f_i^-)]^2}$$

Differences with the free-proton PDFs

- ▶ Different data sets – much less data:
 - ▶ Less data \rightarrow less constraining power \rightarrow more assumptions (fixing) about a_i parameters
 - ▶ **Assumptions replace uncertainties!**
- ▶ Parametrization

Outline

Introduction

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Summary of available nuclear PDFs

nCTEQ results

Available nuclear PDFs

▶ Multiplicative nuclear correction factors

$$f_i^{p/A}(x_N, \mu_0) = R_i(x_N, \mu_0, A) f_i^{\text{free proton}}(x_N, \mu_0)$$

- ▶ Hirai, Kumano, Nagai [PRC 76, 065207 (2007), arXiv:0709.3038]
- ▶ Eskola, Paukkunen, Salgado [JHEP 04 (2009) 065, arXiv:0902.4154]
- ▶ de Florian, Sassot, Stratmann, Zurita
[PRD 85, 074028 (2012), arXiv:1112.6324]

▶ Native nuclear PDFs

- ▶ nCTEQ [PRD 80, 094004 (2009), arXiv:0907.2357]

$$f_i^{p/A}(x_N, \mu_0) = f_i(x_N, A, \mu_0)$$
$$f_i(x_N, A = 1, \mu_0) \equiv f_i^{\text{free proton}}(x_N, \mu_0)$$

HKN framework [PRC 76, 065207 (2007), arXiv:0709.3038]

- ▶ LO & NLO PDFs with errors
- ▶ Error PDFs produced with *Hessian method*
- ▶ Parametrization ($Q_0=1\text{GeV}$)

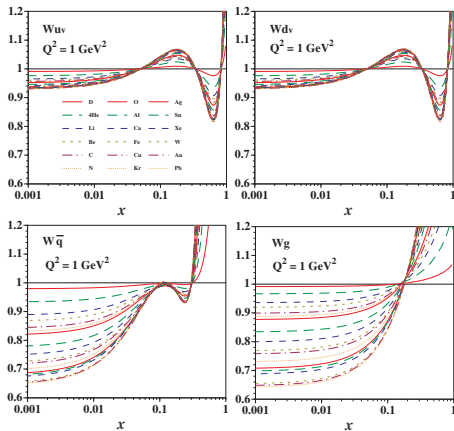
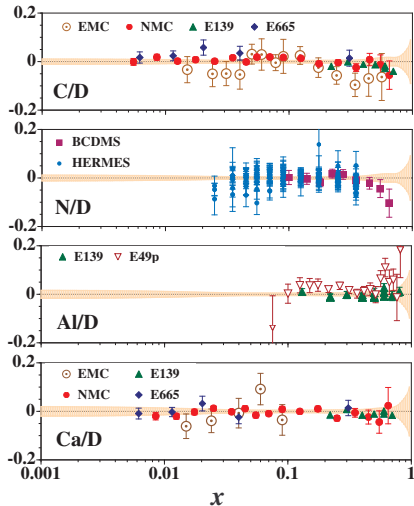
$$f_i^{P/A}(x_N, Q_0) = R_i^A(x_N, Q_0) f_i^P(x_N, Q_0), \quad i = u_v, d_v, g, \text{sea}$$

$$R_i(x, Q_0, A) = 1 + \left(1 - \frac{1}{A^\alpha}\right) \frac{a_i + b_i x + c_i x^2 + d_i x^3}{(1-x)^{\beta_i}}$$

- ▶ MRST 1998 free proton baseline
- ▶ Neglects $x_N > 1$
- ▶ Data: DIS & DY

HKN framework [PRC 76, 065207 (2007), arXiv:0709.3038]

► NLO fit: $\chi^2/dof = 1.21$



- ▶ LO & NLO PDFs with errors
- ▶ Error PDFs produced with *Hessian method*
- ▶ Parametrization ($Q_0=1.3\text{GeV}$)

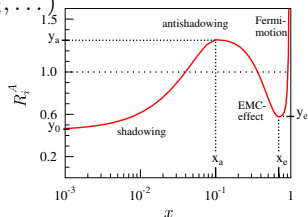
$$f_i^{p/A}(x_N, \mu_0) = R_i(x_N, \mu_0, A, Z) f_i(x_N, \mu_0), \quad i = \text{valence}, s, g$$

$$R_i(x, A, Z) = \begin{cases} a_0 + (a_1 + a_2 x)(e^{-x} - e^{-x_a}) & x \leq x_a \\ b_0 + b_1 x + b_2 x^2 + b_3 x^3 & x_a \leq x \leq x_e \\ c_0 + (c_1 - c_2 x)(1 - x)^{-\beta} & x_e \leq x \leq 1 \end{cases}$$

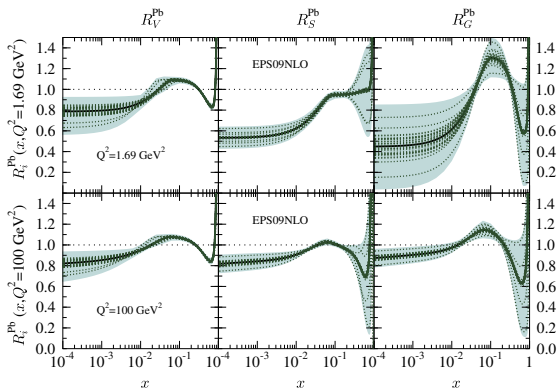
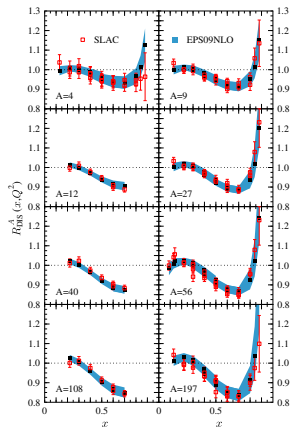
A-dependence of fitting parameters ($d_i = a_i, b_i, \dots$)

$$d_i^A = d_i^{A_{ref}} \left(\frac{A}{A_{ref}} \right)^{p_{d_i}}$$

- ▶ CTEQ6.1M free proton baseline
- ▶ Neglects $x_N > 1$
- ▶ Data: DIS, DY, π^0 @ RHIC



► NLO fit: $\chi^2/dof = 0.79$



DSSZ framework [PRD 85, 074028 (2012), arXiv:1112.6324]

- ▶ NLO PDFs with errors
- ▶ Error PDFs produced with *Hessian method*
- ▶ Parametrization ($Q_0=1\text{GeV}$)

$$f_i^{p/A}(x_N, Q_0) = R_i^A(x_N, Q_0) f_i^p(x_N, Q_0), \quad i = \text{valence, } s, g$$

$$R_v^A(x, Q_0) = \epsilon_1 x^{\alpha_1} (1-x)^{\beta_1} \left[1 + \epsilon_2 (1-x)^{\beta_2} \right] \left[1 + a_v (1-x)^{\beta_3} \right]$$

$$R_s^A(x, Q_0) = R_v^A(x, Q_0) \frac{\epsilon_s}{\epsilon_1} \frac{1 + a_s x^{\alpha_s}}{1 + a_s}$$

$$R_g^A(x, Q_0) = R_v^A(x, Q_0) \frac{\epsilon_g}{\epsilon_1} \frac{1 + a_g x^{\alpha_g}}{1 + a_g}$$

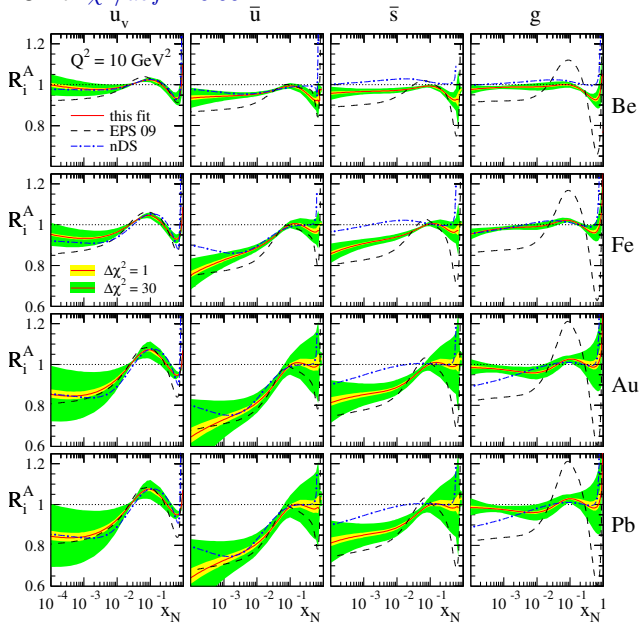
A-dependence of fitting parameters ($\xi = \alpha_v, \alpha_s, \dots$)

$$\xi = \gamma_\xi + \lambda_\xi A^{\delta_\xi}$$

- ▶ MSTW 2008 free proton baseline
- ▶ Neglects $x_N > 1$
- ▶ Data: DIS, DY, π^0 @ RHIC, Neutrino DIS

DSSZ framework [PRD 85, 074028 (2012), arXiv:1112.6324]

► NLO fit: $\chi^2/dof = 0.99$



- ▶ Functional form of the **bound proton PDF** same as for the free proton (CTEQ6M, x restricted to $0 < x < 1$)

$$x f_i^{p/A}(x, Q_0) = c_0 x^{c_1} (1-x)^{c_2} e^{c_3 x} (1 + e^{c_4 x})^{c_5}, \quad i = u_v, d_v, g, \dots$$
$$\bar{d}(x, Q_0)/\bar{u}(x, Q_0) = c_0 x^{c_1} (1-x)^{c_2} + (1 + c_3 x)(1-x)^{c_4}$$

- ▶ A -dependent fit parameters (reduces to free proton for $A = 1$)

$$c_k \rightarrow c_k(A) \equiv c_{k,0} + c_{k,1} (1 - A^{-c_{k,2}}), \quad k = \{1, \dots, 5\}$$

- ▶ PDFs for nucleus (A, Z)

$$f_i^{(A,Z)}(x, Q) = \frac{Z}{A} f_i^{p/A}(x, Q) + \frac{A-Z}{A} f_i^{n/A}(x, Q)$$

(bound neutron PDF $f_i^{n/A}$ by isospin symmetry)

Data sets

▶ NC DIS & DY

CERN BCDMS & EMC & NMC

N = (D, Al, Be, C, Ca, Cu, Fe, Li, Pb, Sn, W)

FNAL E-665

N = (D, C, Ca, Pb, Xe)

DESY Hermes

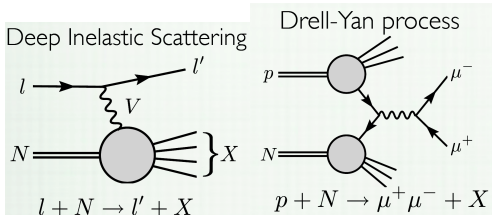
N = (D, He, N, Kr)

SLAC E-139 & E-049

N = (D, Ag, Al, Au, Be, C, Ca, Fe, He)

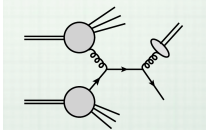
FNAL E-772 & E-886

N = (D, C, Ca, Fe, W)



▶ Single pion production (not yet included)

Single pion production

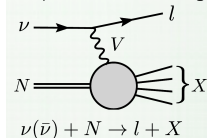


RHIC - PHENIX & STAR

N = Au

▶ Neutrino (to be included later)

Deep Inelastic Scattering



CHORUS CCFR & NuTeV

N = Pb N = Fe

nCTEQ fits

Fit properties:

- ▶ fit @NLO
- ▶ $Q_0 = 1\text{GeV}$
- ▶ using ACOT heavy quark scheme
- ▶ kinematical cuts: $Q > 2\text{GeV}$,
 $W > 3.5\text{GeV}$
- ▶ 708 (1233) data points after
(before) cuts
- ▶ 17 free parameters
 - ▶ 7 gluon
 - ▶ 8 valence
 - ▶ 2 sea
- ▶ $\chi^2/\text{dof} = 0.87$

Error analysis:

- ▶ use Hessian method

$$\chi^2 = \chi_0^2 + \frac{1}{2} H_{ij} (a_i - a_i^0)(a_j - a_j^0)$$

$$H_{ij} = \frac{\partial^2 \chi^2}{\partial a_i \partial a_j}$$

- ▶ tolerance $\Delta\chi^2 = 35$ (every nuclear target within 90% C.L.)
- ▶ eigenvalues span 10 orders of magnitude \rightarrow require numerical precision
- ▶ use noise reducing derivatives

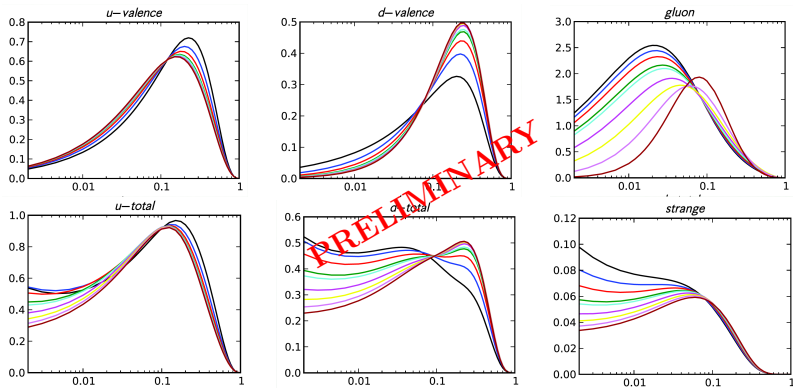
nCTEQ RESULTS

(preliminary)

A-dependence of bound proton PDFs

$$x f_i^A(x, Q)$$

$$A = (1, 2, 4, 9, 12, 27, 56, 108, 207)$$

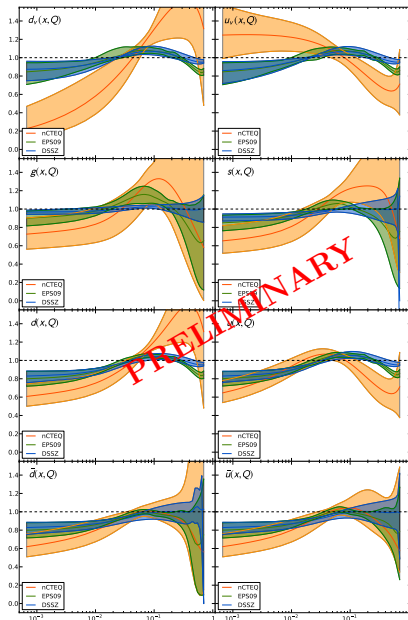


nCTEQ results

Nuclear correction factors
($Q = 10\text{GeV}$)

$$R_i(Pb) = \frac{f_i^{Pb}(x, Q)}{f_i^p(x, Q)}$$

- ▶ different solution for d -valence & u -valence compared to EPS09 & DSSZ
- ▶ sea quark nuclear correction factors similar to EPS09
- ▶ nuclear correction factors depend largely on underlying proton baseline

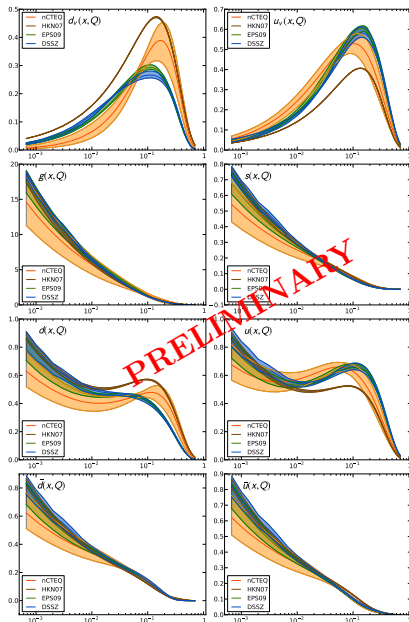


nCTEQ results

Nuclear PDFs ($Q = 10\text{GeV}$)

$$x f_i^{Pb}(x, Q)$$

- ▶ nCTEQ d -valence & u -valence solution between HKN07 & EPS09
- ▶ nCTEQ features larger uncertainties than previous nPDFs
- ▶ better agreement between different groups (nPDFs don't depend on proton baseline)



nCTEQ vs. EPS09

nCTEQ

$$x u_v^{p/A}(Q_0) = x c_1^u (1-x) c_2^u e^{c_3^u x} (1 + e^{c_4^u x}) c_5^u$$

$$x d_v^{p/A}(Q_0) = x c_1^d (1-x) c_2^d e^{c_3^d x} (1 + e^{c_4^d x}) c_5^d$$

$$c_k^{uv} = c_{k,0}^{uv} + c_{k,1}^{uv} (1 - A^{-c_{k,2}^{uv}})$$

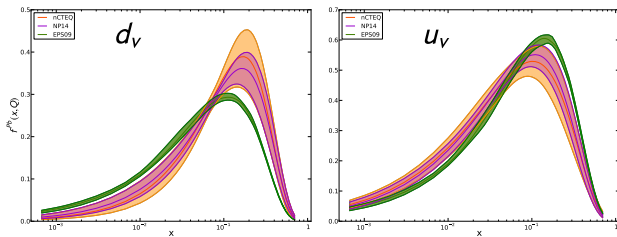
$$c_k^{dv} = c_{k,0}^{dv} + c_{k,1}^{dv} (1 - A^{-c_{k,2}^{dv}})$$

EPS09

$$u_v^{p/A}(Q_0) = R_v(x, A, Z) u(x, Q_0)$$

$$d_v^{p/A}(Q_0) = R_v(x, A, Z) d(x, Q_0)$$

$$R_v = \begin{cases} a_0 + (a_1 + a_2 x)(e^{-x} - e^{-x a}) & x \leq x_a \\ b_0 + b_1 x + b_2 x^2 + b_3 x^3 & x_a \leq x \leq x_e \\ c_0 + (c_1 - c_2 x)(1-x)^{-\beta} & x_e \leq x \leq 1 \end{cases}$$



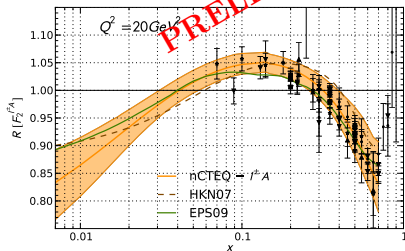
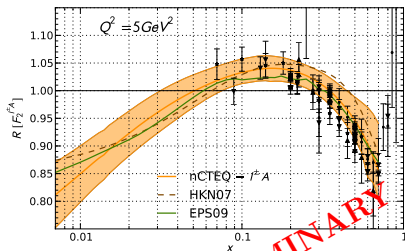
we set:

$$\begin{cases} c_1^{dv} = c_1^{uv} \\ c_2^{dv} = c_2^{uv} \end{cases}$$

Structure function ratio

$$R = \frac{F_2^{Fe}(x, Q)}{F_2^D(x, Q)}$$

- ▶ good data description
- ▶ despite different u -valence & d -valence ratios are similar to EPS09

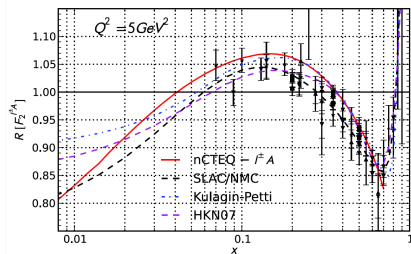


Compatibility of nuclear corrections for νA and $l^\pm A$ DIS

PRL106, 122301 (2011), arXiv:1012.0286
PRD80, 094004 (2009), arXiv:0907.2357

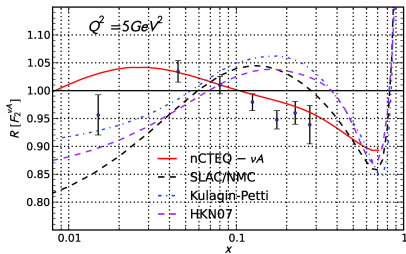
Fit to $l^\pm A$ DIS and DY data

$$\chi^2/\text{dof} = 0.89$$



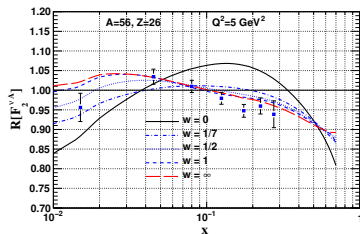
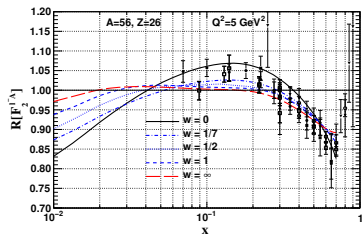
Fit to νA DIS data only

$$\chi^2/\text{dof} = 1.33$$



Compatibility of nuclear corrections for νA and $l^\pm A$ DIS

PRL106, 122301 (2011), arXiv:1012.0286
 PRD80, 094004 (2009), arXiv:0907.2357



w	$l^\pm A$	χ^2 (/pt)	νA	χ^2 (/pt)	total χ^2 (/pt)
0	708	638 (0.90)	-	-	638 (0.90)
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$$\chi^2 = \sum_{l^\pm A \text{ data}} \chi_i^2 + \sum_{\nu A \text{ data}} w \chi_i^2,$$

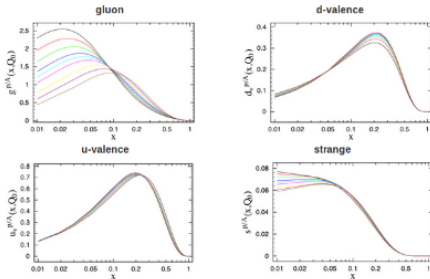
$$w = \{0, \frac{1}{7}, \frac{1}{2}, 1, \infty\}$$

nCTEQ

nuclear parton distribution functions

- Home
- PDF grids & code
- Papers & Talks
- Subversion
- Tracker
- Wiki

nCTEQ project is an extension of the CTEQ collaborative effort to determine parton distribution functions inside of a free proton. It generalizes the free-proton PDF framework to determine densities of partons in bound protons (hence nCTEQ which stands for nuclear CTEQ). More details on the framework and the first results can be found in [arXiv:09072357](https://arxiv.org/abs/09072357) [[hep-ph](#)]. The effects of the nuclear environment on the parton densities can be shown as modified parton densities



where all black curves stand for free proton PDF and red, green, blue, cyan, pink, yellow, magenta and brown curves show PDF in protons bound in nuclei - from deuterium (red) to lead (brown).

An alternative way how effects of nuclear environment can be displayed is in ratios of Deep Inelastic Scattering (DIS) structure functions e.g. ratios of the structure function F_2 for a neutral current DIS as in the figure below on the left or ratios of the same structure function F_2 but for a charged current DIS.

Summary

- ▶ We have first nCTEQ error PDFs (still preliminary)
- ▶ nCTEQ PDFs features larger (more realistic) uncertainties.
- ▶ LHC $p Pb$ data will allow to further constrain nPDFs (first need a proton baseline with LHC data).
- ▶ Nuclear component important not only for heavy ion collisions, but also for flavor differentiation, especially for s -quark distribution (which is important for LHC W/Z benchmark processes).

Summary

- ▶ Plans for future:
 - ▶ finish current analysis;
 - ▶ redo analysis of neutrino nuclear corrections;
 - ▶ include new data (LHC, JLAB, Minerva, ???);
 - ▶ high x region, deuterium nuclear corrections, higher twist effects – CJ collaboration in JLAB;
 - ▶ unified framework to fit both free proton and nuclear PDFs;
 - ▶ different methods for minimizing and estimating errors;

BACKUP SLIDES

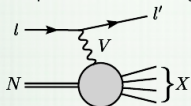
NEUTRINO DIS

K. Kovařík, DIS2013

- Experiments included in the analysis

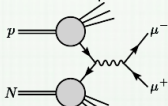
Charged lepton

Deep Inelastic Scattering



$$l + N \rightarrow l' + X$$

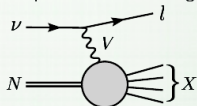
Drell-Yan process



$$p + N \rightarrow \mu^+ \mu^- + X$$

Neutrino

Deep Inelastic Scattering



$$\nu(\bar{\nu}) + N \rightarrow l + X$$

CERN BCDMS & EMC & NMC

$N = (\text{D, Al, Be, C, Ca, Cu, Fe, Li, Pb, Sn, W})$

FNAL E-665

$N = (\text{D, C, Ca, Pb, Xe})$

DESY Hermes

$N = (\text{D, He, N, Kr})$

SLAC E-139 & E-049

$N = (\text{D, Ag, Al, Au, Be, C, Ca, Fe, He})$

FNAL E-772 & E-886

$N = (\text{D, C, Ca, Fe, W})$

CHORUS

$N = \text{Pb}$

CCFR & NuTeV

$N = \text{Fe}$

1233 data points (708 after cuts)

3832 data points (3134 after cuts)

- NPDF fit properties:

- we fit nuclear data with NLO QCD predictions
- we include heavy quark effects (ACOT)
- applied standard CTEQ kinematical cuts $Q > 2\text{GeV}$ & $W > 3.5\text{GeV}$

- NPDF fit results:

- 708 (1233) data points after (before) cuts
- 17 free parameters - 691 degrees of freedom
- overall $\chi^2/\text{dof} = 0.87$
- individually for different data subsets
 - for F_2^A/F_2^D $\chi^2/\text{pt} = 0.80$
 - for $F_2^A/F_2^{A'}$ $\chi^2/\text{pt} = 0.51$
 - for $\sigma_{DY}^{pA}/\sigma_{DY}^{pA'}$ $\chi^2/\text{pt} = 0.85$

F_2^A/F_2^A : Observable	Experiment	# data
Be/C	NMC-96	15
Al/C	NMC-96	15
Ca/C	NMC-95	20
	NMC-96	15
Fe/C	NMC-95	15
Sn/C	NMC-96	144
Pb/C	NMC-96	15
C/Li	NMC-95	20
Ca/Li	NMC-95	20
Total:		279

$\sigma_{DY}^{pA}/\sigma_{DY}^{pA'}$: Observable	Experiment	# data
C/D	FNAL-E772-90	9
Ca/D	FNAL-E772-90	9
Fe/D	FNAL-E772-90	9
W/D	FNAL-E772-90	9
Fe/Be	FNAL-E866-99	28
W/Be	FNAL-E866-99	28
Total:		92

F_2^A/F_2^D : Observable	Experiment	# data
D	NMC-97	275
He/D	SLAC-E139	18
	NMC-95,re	16
	Hermes	92
Li/D	NMC-95	15
	SLAC-E139	17
Be/D	EMC-88	9
	EMC-90	2
C/D	SLAC-E139	7
	NMC-95,re	16
	NMC-95	15
	FNAL-E665-95	4
	BCDMS-85	6
N/D	BCDMS-85	9
	Hermes	92
	SLAC-E049	18
Al/D	SLAC-E139	17
	EMC-90	2
Ca/D	SLAC-E139	7
	NMC-95,re	15
	FNAL-E665-95	4
Fe/D	BCDMS-85	6
	BCDMS-87	10
	SLAC-E049	14
	SLAC-E139	23
Cu/D	SLAC-E140	6
	EMC-88	9
	EMC-93(addendum)	10
Kr/D	EMC-93(chariot)	9
	Hermes	84
Ag/D	SLAC-E139	7
	Sn/D	8
Xe/D	EMC-88	8
	FNAL-E665-92	4
Au/D	SLAC-E139	18
	FNAL-E665-95	4
Pb/D		
Total:	Total:	862

- NPDF Hessian analysis:

$$\chi^2 = \chi_0^2 + \frac{1}{2} H_{ij} (a_i - a_i^0)(a_j - a_j^0) \quad H_{ij} = \frac{\partial^2 \chi^2}{\partial a_i \partial a_j}$$

- 17 free parameters - 7 gluon parameters
 - 8 valence parameters
 - 2 sea parameters
- Eigenvalues span 10 orders of magnitude \rightarrow numerical precision required
- Use improved derivatives - less sensitive to noise

$$\frac{\partial f}{\partial x} = \frac{f_1 - f_{-1}}{2h}$$

\uparrow
 central differences

$$\begin{aligned} & \nearrow \frac{f_1 - f_{-1} + 2(f_2 - f_{-2}) + 3(f_3 - f_{-3})}{28h} \\ & \searrow \frac{f_1 - f_{-1} + 2(f_2 - f_{-2}) + 3(f_3 - f_{-3}) + 4(f_4 - f_{-4}) + 5(f_5 - f_{-5})}{110h} \end{aligned}$$

\nwarrow
 noise robust Lanczos 3, 5-point derivative

- $\Delta \chi^2 = 35$ determined so that every nuclear target is described within 90% C.L.

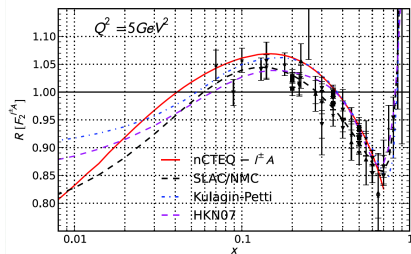
K. Kovarik, DIS2013

Compatibility of nuclear corrections for νA and $l^\pm A$ DIS

PRL106, 122301 (2011), arXiv:1012.0286
PRD80, 094004 (2009), arXiv:0907.2357

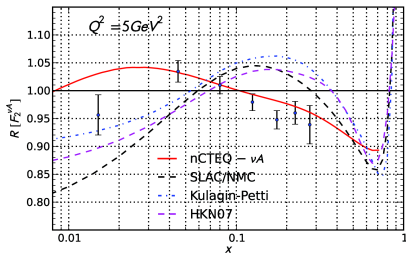
Fit to $l^\pm A$ DIS and DY data

$$\chi^2/\text{dof} = 0.89$$



Fit to νA DIS data only

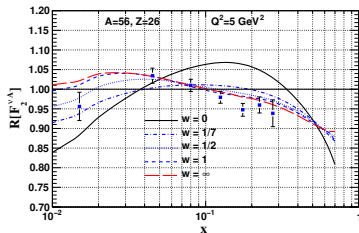
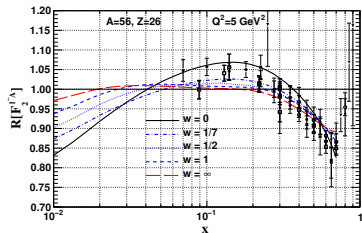
$$\chi^2/\text{dof} = 1.33$$



Compatibility of nuclear corrections for νA and $l^\pm A$ DIS

PRL106, 122301 (2011), arXiv:1012.0286

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$$w = \{0, \frac{1}{7}, \frac{1}{2}, 1, \infty\}$$

Compatibility of nuclear corrections for νA and $l^\pm A$ DIS

- ▶ It was argued in the literature that νA DIS data is compatible with $l^\pm A$ data:

Paukkunen, Salgado, JHEP **07**, 32 2010, [arXiv:1004.3140](#)

de Florian, Sassot, Stratmann, Zurita, PRD85, 074028 (2012),

[arXiv:1112.6324](#)

- ▶ However these results were obtained using **uncorrelated errors** for NuTeV experiment, which were crucial for the nCTEQ conclusions [PRL106, 122301 \(2011\)](#).

w	$l^\pm A$	$\chi^2(/pt)$	νA	$\chi^2(/pt)$	total $\chi^2(/pt)$
1-corr	708	736 (1.04)	3134	4246 (1.36)	4983 (1.30)
1-uncorr	708	809 (1.14)	3110	3115 (1.00)	3924 (1.02)

Compatibility of nuclear corrections for νA and $l^\pm A$ DIS

- ▶ Recent paper

Paukkunen, Salgado, PRL110, 212301 (2013), [arXiv:1302.2001](#)

suggests a method to renormalize the NuTeV data so that the tension between νA and $l^\pm A$ data sets are removed

Instead of looking at the ratio of cross-sections $R^\nu(x, y, E) \equiv \frac{\sigma_{\text{exp}}^\nu(x, y, E)}{\sigma_{\text{CTEQ6.6}}^\nu(x, y, E)}$

they suggest considering

$$\bar{R}^\nu(x, y, E) \equiv \frac{\sigma_{\text{exp}}^\nu(x, y, E)/I_{\text{exp}}^\nu(E)}{\sigma_{\text{CTEQ6.6}}^\nu(x, y, E)/I_{\text{CTEQ6.6}}^\nu(E)}$$

where

$$I_{\text{exp}}^\nu(E) \equiv \sum_{i \in \text{fixed } E} \sigma_{\text{exp}, i}(x, y, E) \times B_i(x, y)$$

$B_i(x, y)$ is size of the experimental (x, y) -bin

- ▶ However this analysis still **do not** take into account correlated errors provided by NuTeV collaboration.

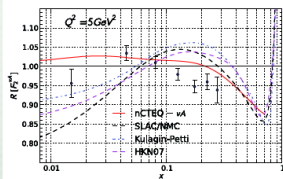
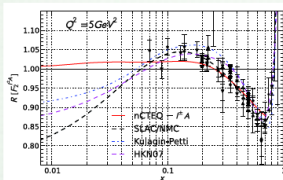
NEUTRINO DIS

K. Kovařík, DIS2013

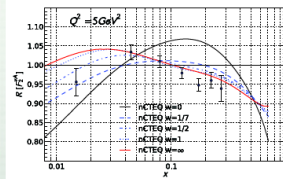
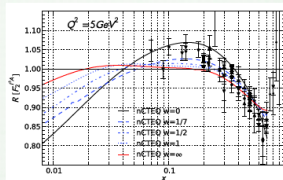
- Analysis of fits with neutrino DIS (uncorrelated errors)

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uncorrelated errors



correlated errors



- ▶ Parametrization (GRV98 baseline, FFNS, $Q_0^2 = 0.4\text{GeV}^2$)

$$f_i^{p/A}(x_N, Q_0^2) = \int_{x_N}^A \frac{dy}{y} W_i(y, A, Z) f_i\left(\frac{x_N}{y}, Q_0^2\right).$$

allows for $0 < x_N < A$

- ▶ Weight functions W_i parameterize nuclear effects for *valence*, *sea* and *gluon*

$$W_v(y, A, Z) = A [a_v \delta(1 - \epsilon_v - y) + (1 - a_v) \delta(1 - \epsilon_v' - y)] \\ + n_v \left(\frac{y}{A}\right)^{\alpha_v} \left(1 - \frac{y}{A}\right)^{\beta_v} + n_s \left(\frac{y}{A}\right)^{\alpha_s} \left(1 - \frac{y}{A}\right)^{\beta_s}$$

$$W_s(y, A, Z) = A \delta(1 - y) + \frac{a_s}{N_s} \left(\frac{y}{A}\right)^{\alpha_s} \left(1 - \frac{y}{A}\right)^{\beta_s}$$

$$W_g(y, A, Z) = A \delta(1 - y) + \frac{a_g}{N_g} \left(\frac{y}{A}\right)^{\alpha_g} \left(1 - \frac{y}{A}\right)^{\beta_g}$$

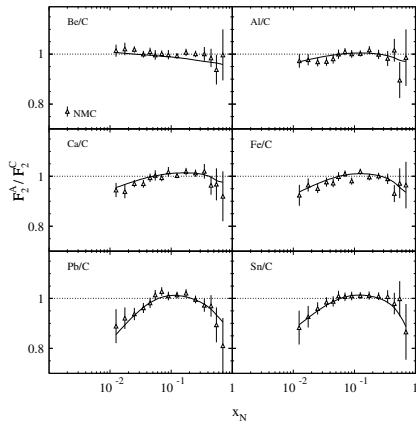
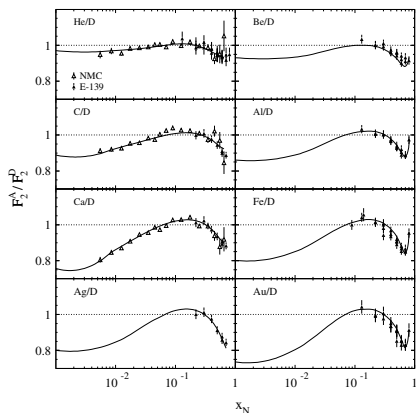
- ▶ Nuclear structure functions are defined as usual

$$A F_2^A(x, Q^2) = Z F_2^{p/A}(x, Q^2) + (A - Z) F_2^{n/A}(x, Q^2)$$

- ✓ *In principle* takes into account $x > 1$ region.
- ✓ Convenient for working in Mellin space.
- ? Unfortunately in the actual grids $0 < x < 1$, and sum rules are consistent with $(0, 1)$ range.

DS04 framework

DS04 feature very good data description (DIS, DY, 420 data points)
with $\chi^2/ndof = 0.76$



ATLAS strange measurement

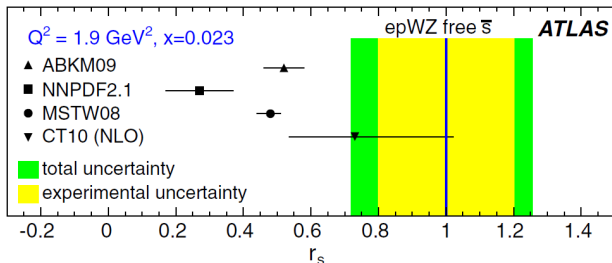
ATLAS has used W/Z production to infer constraints on the strange quark distribution (2010 data, 35pb^{-1})

G. Aad et al. (ATLAS Collaboration) Phys. Rev. Lett. 109, 012001 (2012),

arXiv:1203.4051

for $Q^2 = 1.9 \text{ GeV}^2$ and $x = 0.023$:

$$r_s = 0.5(s + \bar{s})/\bar{d} = 1.00^{+0.25}_{-0.28}$$



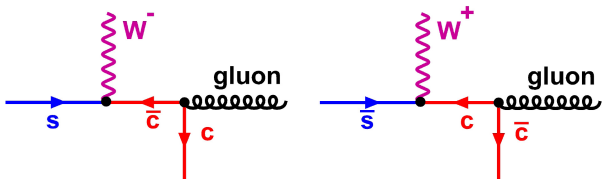
CMS W_c final states measurement

CMS measured ratios of cross-sections using 36pb^{-1} of data

CMS-PAS-EWK-11-013

arXiv:1310.1138

$$R_c^\pm = \frac{\sigma(W^+\bar{c})}{\sigma(W^-c)} = 0.92 \pm 0.19(\text{stat.}) \pm 0.04(\text{sys.})$$



see also:

W. J. Stirling, E. Vryonidou, Phys. Rev. Lett. 109, 082002 (2012),

arXiv:1203.6781

Motivations: proton Strange PDF

- ▶ large proton s -quark PDF uncertainty:
- ▶ much more important in LHC than in Tevatron
 - ▶ heavy quarks contributions more important
 - ▶ larger rapidity range
 - ▶ high energy \rightarrow probes PDFs at small x

