

JUAS 2014



LINACS

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BE/ABP – CERN

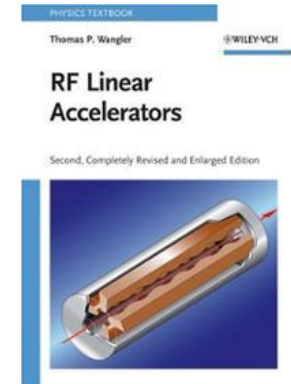
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<http://jlalleme.web.cern.ch/jlalleme/Juas2014/>

Credits

Much material is taken from:

- Thomas Wangler, RF linear accelerators
- Nicolas Pichoff – from previous CAS school
- Maurizio Vretenar – from previous CAS school
<http://cas.web.cern.ch/cas/>
- Alessandra Lombardi – from previous JUAS school



Before starting

- Please, ask questions.....
 - During the lecture.
 - During the tutorial.
 - Feel free to contact me later.
- We will put together many concepts already seen : Relativity, Electromagnetism, RF, Transverse and Longitudinal beam dynamics...

Organization of the Lecture

- 4 hours + 3 hours tutorial

	Monday Jan 20 th	Tuesday Jan 21 st	Wednesday Jan 22 nd	Thursday Jan 23 rd	Friday Jan 24 th	
09:00	Transverse Dynamics lecture <i>A. Latina</i>	Linear imperfections lecture <i>Y. Papaphilippou</i>	Linear imperfections lecture <i>Y. Papaphilippou</i>	Exercises in computer room	Instabilities lecture <i>M. Migliorati</i>	09:00
10:00	Coffee Break	Coffee Break	Coffee Break	Coffee Break	Coffee Break	10:00
10:15	Transverse Dynamics tutorial <i>A. Latina</i>	Linear imperfections lecture <i>Y. Papaphilippou</i>	Non-linear effects lecture <i>Y. Papaphilippou</i>	Space charge lecture <i>M. Migliorati</i>	Instabilities lecture <i>M. Migliorati</i>	10:15
11:15	Linacs lecture <i>J-B. Lallement</i>	Linear imperfections lecture <i>Y. Papaphilippou</i>	Non-linear effects lecture <i>Y. Papaphilippou</i>	Space charge lecture <i>M. Migliorati</i>	Instabilities tutorial <i>M. Migliorati</i>	11:15
12:15	LUNCH	LUNCH	LUNCH	LUNCH	LUNCH	12:15
14:00	Linacs lecture <i>J-B. Lallement</i>	Injection / extraction lecture <i>T. Perron</i>	Linacs lecture <i>J-B. Lallement</i>	Space charge tutorial <i>M. Migliorati</i>	Non-linear effects lecture <i>Y. Papaphilippou</i>	14:00
15:00	Linacs lecture <i>J-B. Lallement</i>	Injection / extraction lecture <i>T. Perron</i>	Linacs tutorial <i>J-B. Lallement</i>	Space charge lecture <i>M. Migliorati</i>	Non-linear effects lecture <i>Y. Papaphilippou</i>	15:00
16:00	Coffee Break	Coffee Break	Coffee Break	Coffee Break	Coffee Break	16:00
16:15	Linacs tutorial <i>J-B. Lallement</i>	Linear imperfections lecture <i>Y. Papaphilippou</i>	Linacs tutorial <i>J-B. Lallement</i>	Space charge lecture <i>M. Migliorati</i>	Non-linear effects tutorial <i>Y. Papaphilippou</i>	16:15
17:15						17:15

Organization of the Lecture

- 4 hours + 3 hours tutorial
- Lecture
 - Part1: Introduction to Linacs.
 - Part2: Cavities and structures.
 - Part3: Beam dynamics.
 - Part4: Bonus
- Tutorial
 - Several problems to better understand and put in practice the different concepts.

Part1: Introduction

- What is a LINAC
- A bit of history
- Why a LINAC
- Principle of RF LINACs



What is a LINAC

- **LIN**ear **AC**celerator : A device where charged particles acquire energy moving on a linear path.

$$m \cdot \frac{d^2 \vec{z}}{dt^2} = q \cdot \left(\vec{E} + \frac{d\vec{z}}{dt} \times \vec{B} \right)$$

Acceleration related to the sum of the forces

$$\frac{d\vec{p}}{dt} = q \cdot \left(\vec{E} + \frac{d\vec{x}}{dt} \times \vec{B} \right)$$

Momentum

$$\frac{dW}{dt} = \frac{d\vec{z}}{dt} \cdot \frac{d\vec{p}}{dt} = q \cdot \frac{d\vec{z}}{dt} \cdot \left(\vec{E} + \frac{d\vec{z}}{dt} \times \vec{B} \right)$$

Energy gain !

Energy gain thanks to the electric field.

What is a LINAC

- **L**INear **A**Ccelerator : A device where charged particles acquire energy moving on a linear path.

$$\frac{d^2\vec{z}}{dt^2} = \underbrace{\left(\frac{q}{m} \cdot \left(\vec{E} + \frac{d\vec{z}}{dt} \times \vec{B} \right) \right)}$$

Type of the accelerated Particles

- Charge
- Mass

Type of the accelerating sturcture

- Electric field for acceleration
- Magnetic field for focusing/bending

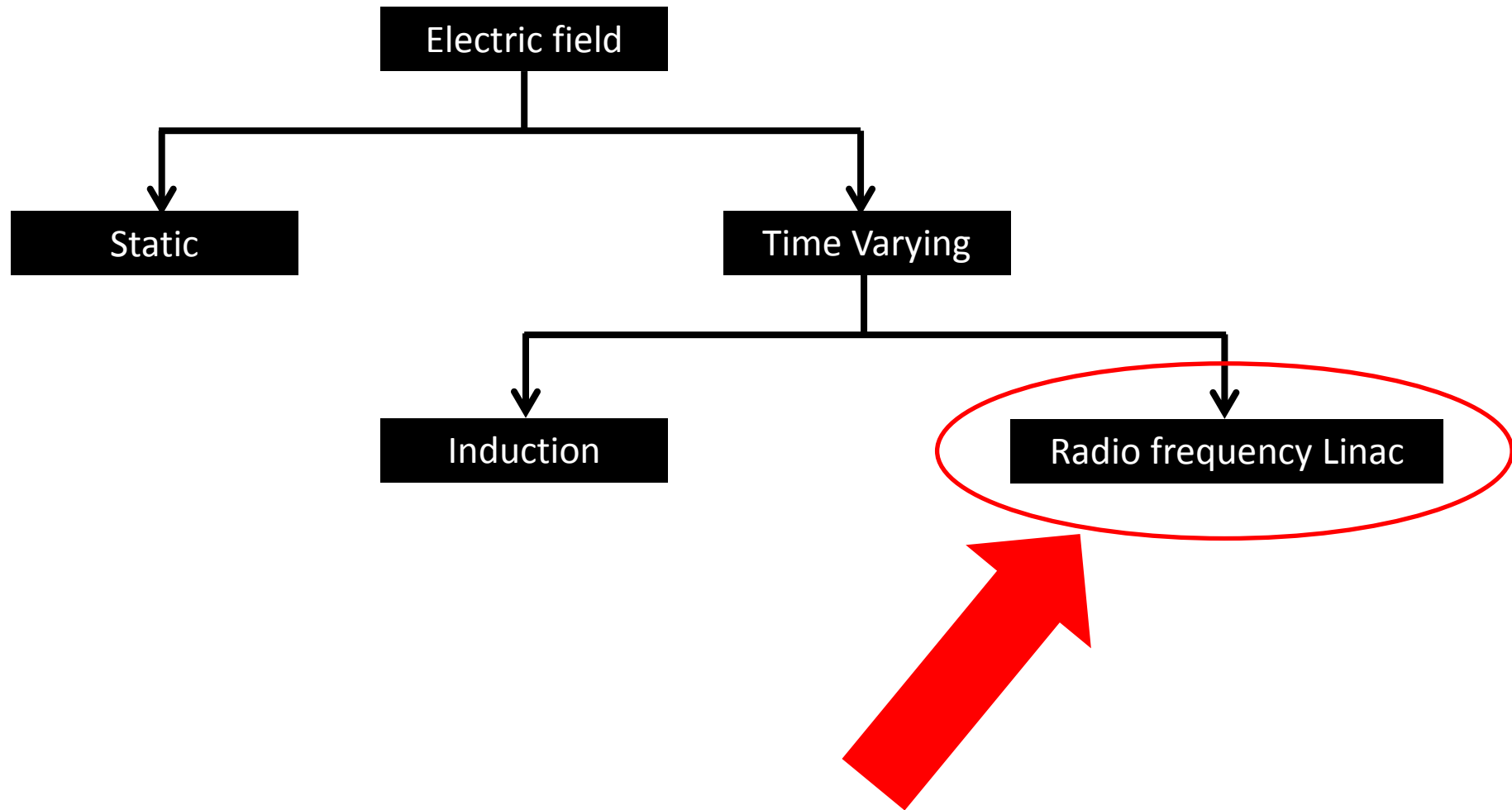
Mainly:

Electrons

Protons and light ions

Heavy ions

Different type of LINACs



What we will discuss during 4 hours !!!

Example of a static Linac



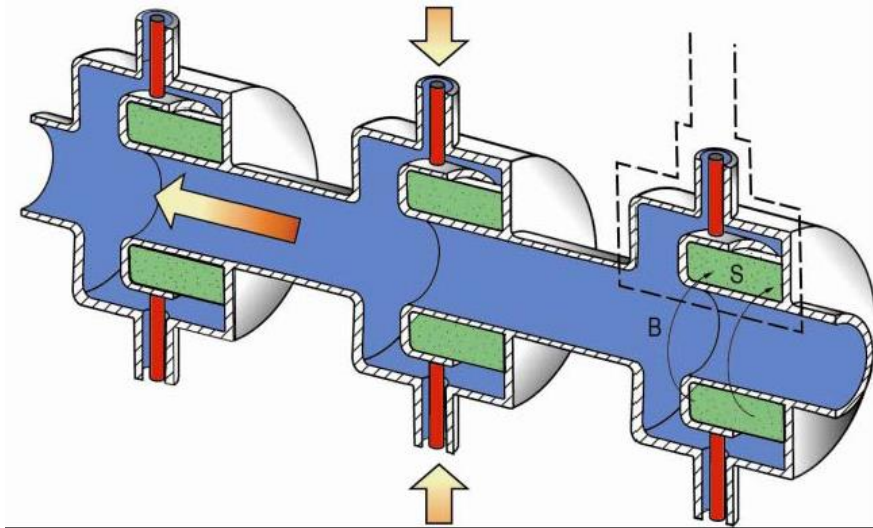
Constant potential difference (electric field)
Energy gain in [eV]

Acceleration limited to few MeV (electric field breakdown)

Still used in very first stage of acceleration

Picture : 750 kV Cockcroft-Walton
Linac2 injector at CERN from 1978 to 1992.

Principle of the induction linac



A varying magnetic field can generate an electric field.

$$V_0 = \oint \vec{E} \cdot d\vec{l} = \iint_S \frac{d\vec{B}}{dt} \cdot d\vec{S}$$

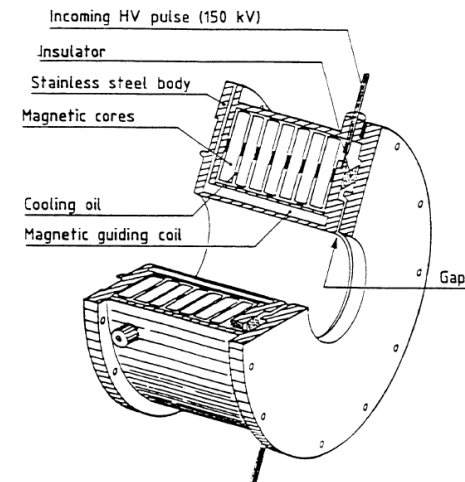
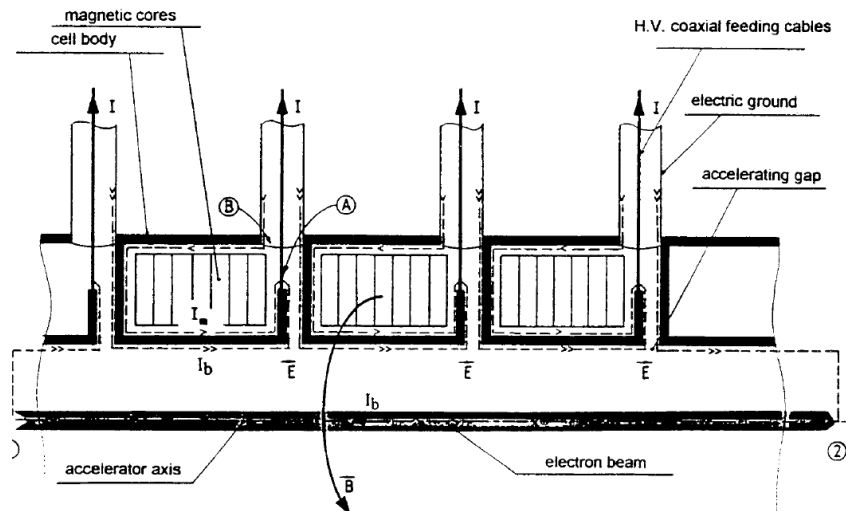


Fig. 2 Induction cell

The first Radio Frequency Linac

Acceleration by time varying electromagnetic field overcome the limitation of static fields.

First RF linac design and experiment – Wideroe Linac in 1928

K beam – $2 \times 25 \text{ kV} = 50 \text{ keV}$

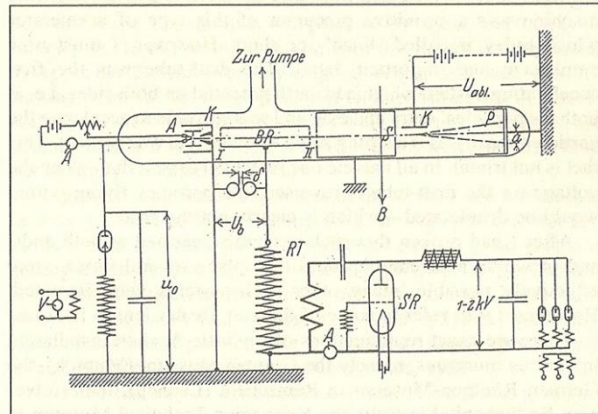
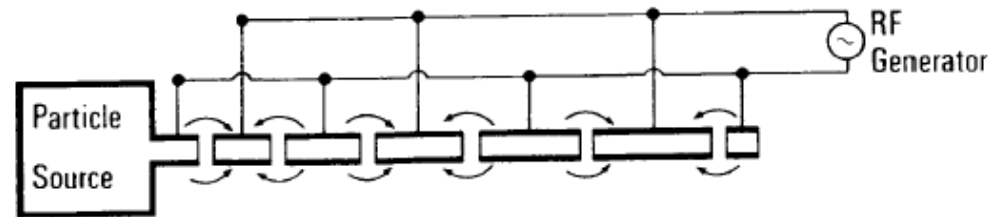
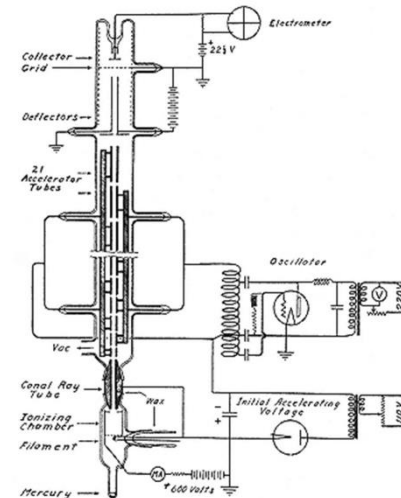


Fig. 3.6: Acceleration tube and switching circuits [Wi28].



First working Linac – Berkeley in 1931

Hg beam – $30 \times 42 \text{ kV} = 1.26 \text{ MeV}$



Big Jump in RF technology – 40's

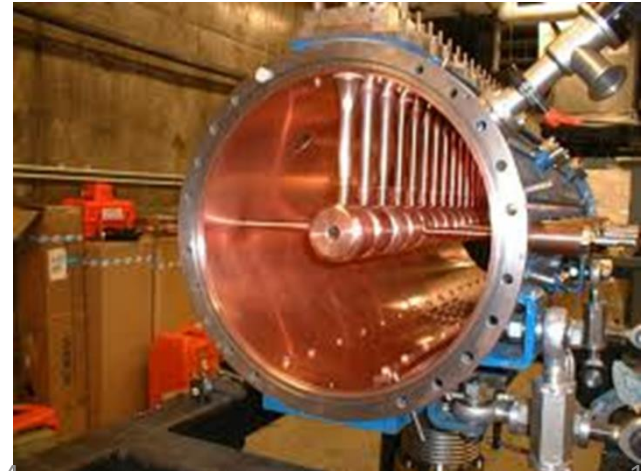
- Development of Radar technology during the WW II.
- Competences and components in the MHz-GHz range.

From Wideroe to Alvarez

- Drift tubes inside a cavity resonator
- After WW II, 2.000 transmitters at 202.56 MHz from US army stocks
- First Drift Tube Linac in 1955 from 4 to 32 MeV.



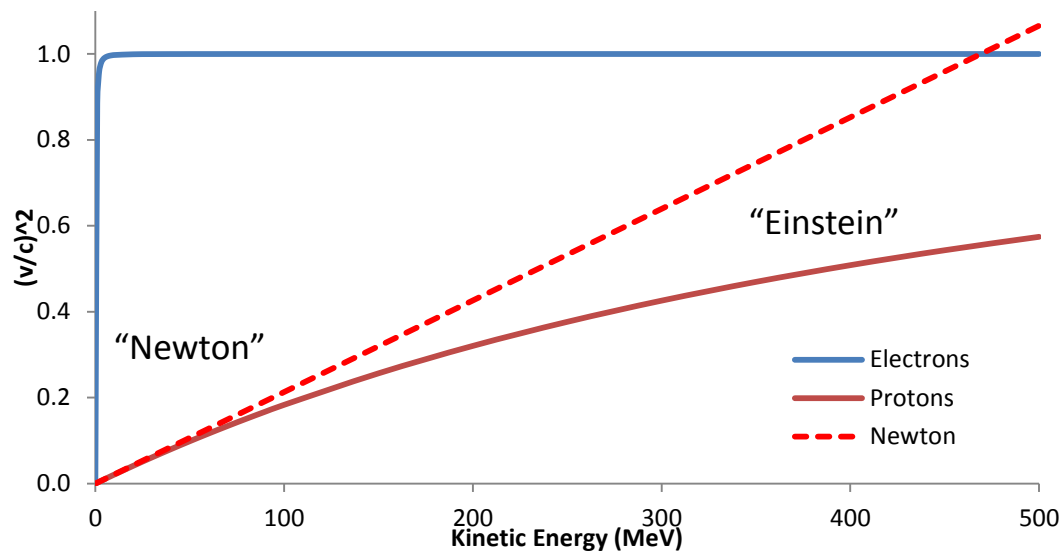
Basement of modern RF linac technology !!!



Why LINACs

	LINACS		SYNCHROTRON
	Low Energy	High Energy	High Energy
Protons, Ions	<p>Injector to synchrotrons, stand alone applications.</p> <p>Synchronicity with the RF fields in the range where velocity increase with energy.</p>	<p>Production of secondary beams (n, ν, RIB, ...)</p> <p>Higher cost/ MeV than synchrotrons</p> <p>High average beam current (repetition rate, less resonances, easier beam loss)</p>	<p>Very efficient when velocity is constant (multiple crossing of RF gaps).</p> <p>Limited current (repetition frequency, instabilities)</p>
Electrons	<p>Conventional e- linac</p> <p>Simple and compact</p>	<p>Linear colliders</p> <p>No energy loss due to synchrotron radiation – smaller beam size. Only option for high energy.</p>	<p>Light sources</p> <p>Can accumulate high beam intensities.</p>

Why LINACs



Electrons mass 511 keV

Proton mass 938.27 MeV (1836 time e- mass)

At 3 MeV, $\beta_{e^-} = 0.99$, $\beta_{p^+} = 0.08$

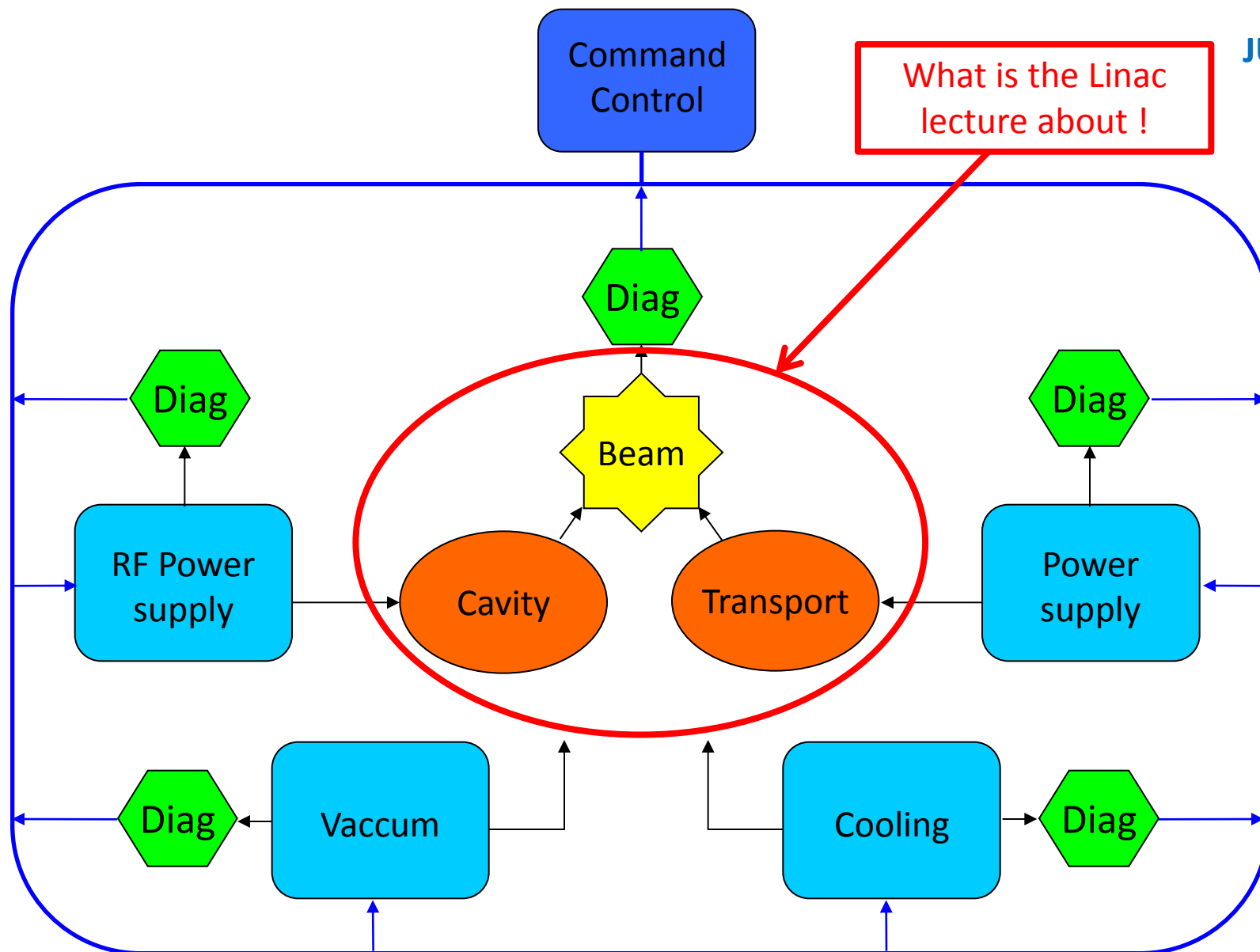
At 500 MeV, $\beta_{p^+} = 0.76$

A Linac is a perfect structure to adapt to non-relativistic particles

Accelerator components

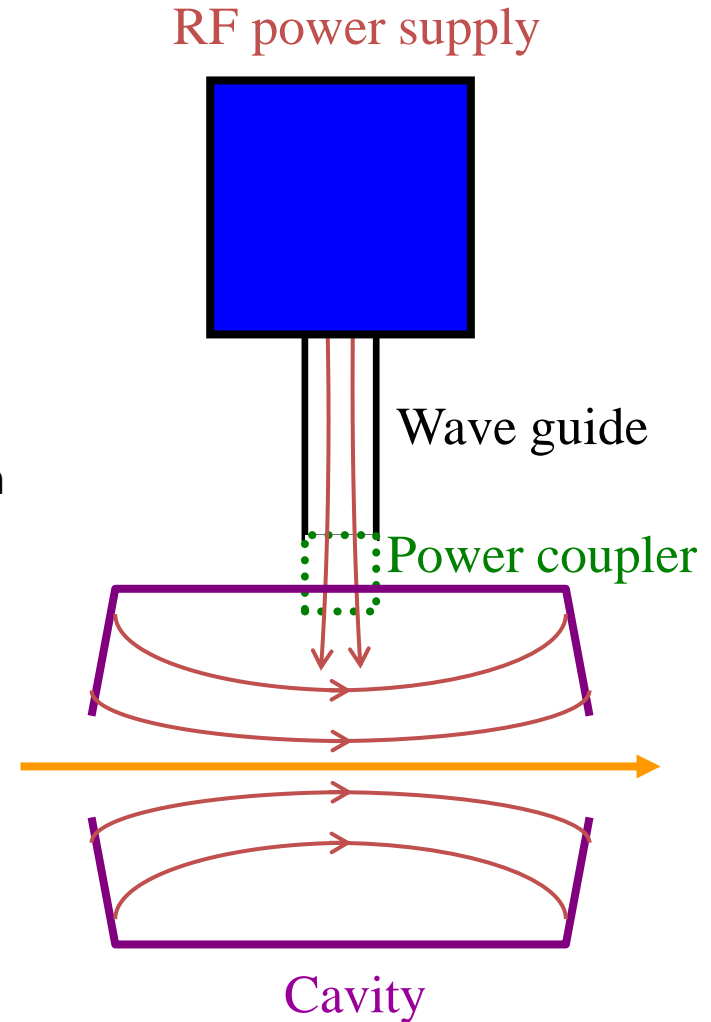


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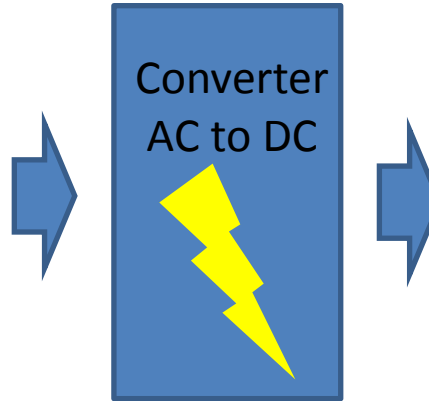


RF acceleration

1. RF power source
Generator of electromagnetic wave of a specified frequency
2. Cavity
Space enclosed in a metallic boundary which resonates with the wave frequency and tailors the field pattern
3. Beam
Flux of particles going thru the cavity.
4. Energy gain
Field and phase is adjusted to accelerate the beam.



RF acceleration



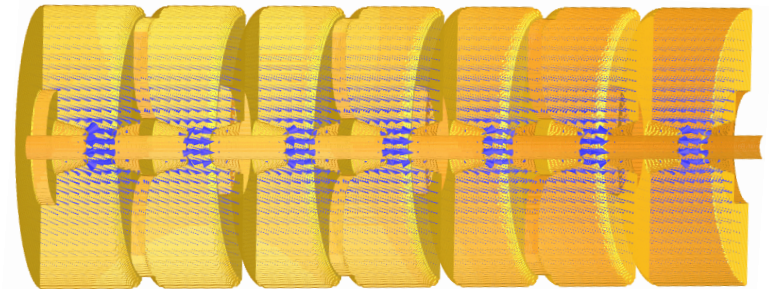
Linac JB.Lallement- JUAS 2014



Designing an RF LINAC

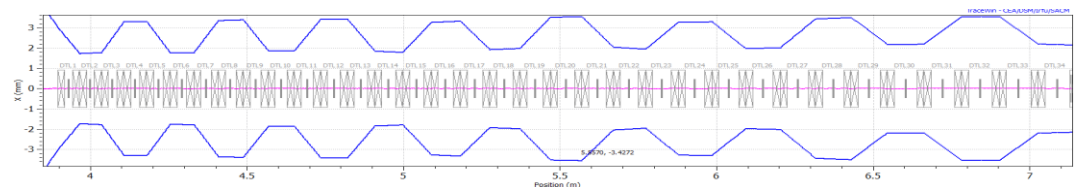
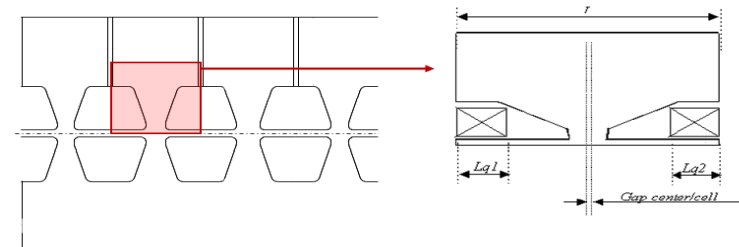
1. Cavity design

- Control the field pattern inside the cavity
- Minimize the Ohmic losses on the walls/maximize the stored energy



2. Beam dynamics design

- Control the timing btw field and particles
- Insure that the beam is kept in the smallest possible volume during acceleration



Electric field in a cavity

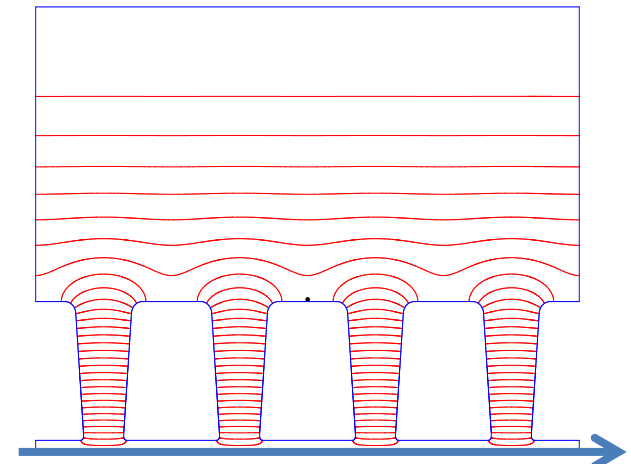
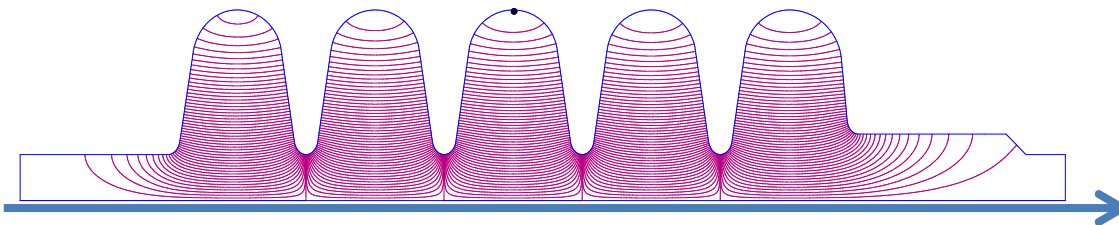
- Assuming that the solution of the wave equation in a bounded medium can be written as

$$E(x, y, z, t) = E(x, y, z) \cdot e^{-j\omega t}$$

Function of space

Function of time
Oscillating at freq. $\omega/2\pi$

- First step in cavity design: Concentrating the RF power on the beam path in the most efficient way. Tailor $E(x, y, z)$ by choosing the appropriate cavity geometry



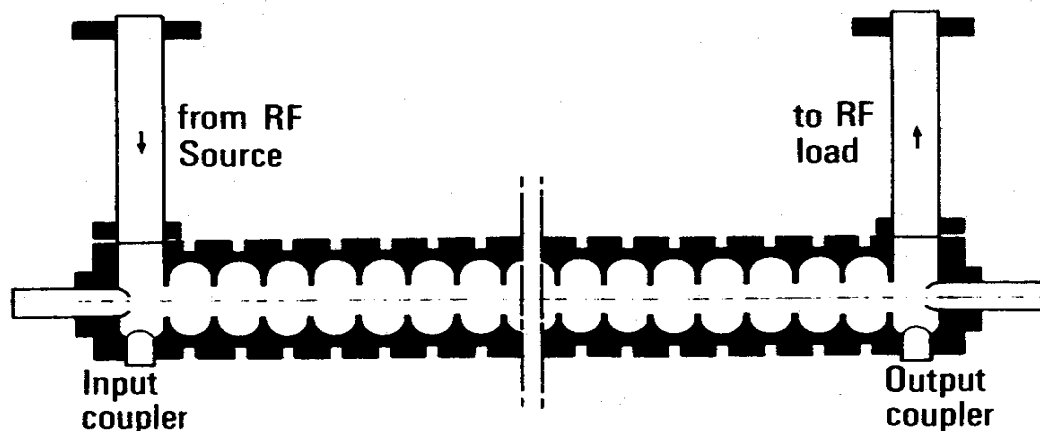
One word on travelling wave cavities

These cavities are essentially used for acceleration of ultra-relativistic particles.
The longitudinal field component is:

$$E_z(r, z, t) = \sum E_n(r) \cdot e^{j(\omega t - k_n z)}$$

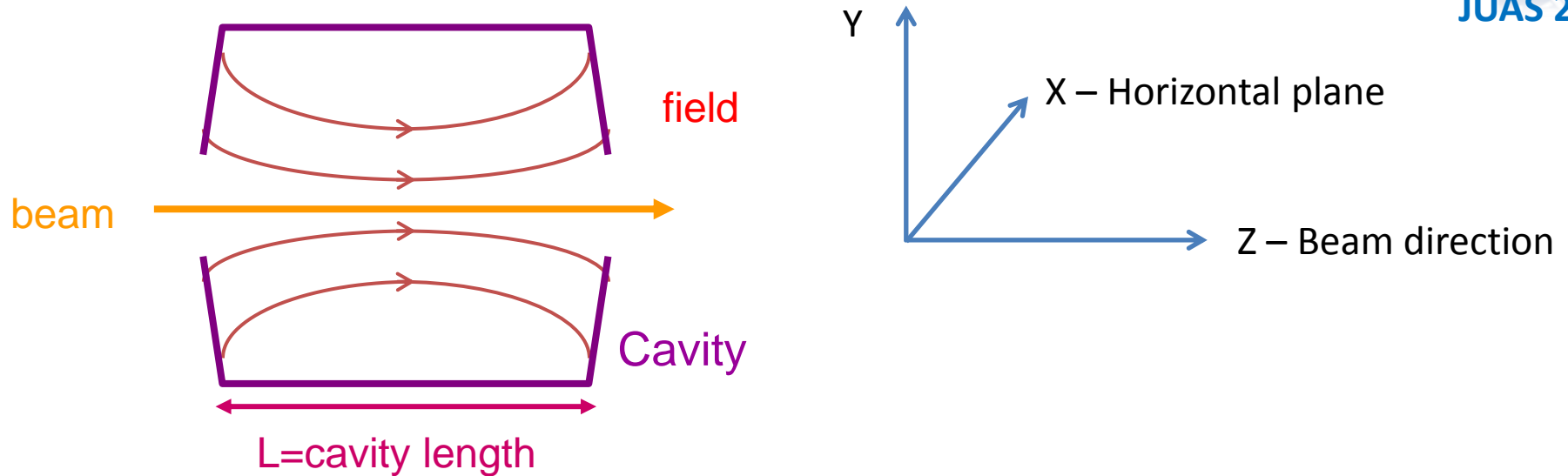
$E_n(r) \cdot e^{j(\omega t - k_n z)}$ is a space harmonic of the field, given by the cavity periodicity

Particle whose velocity is close to the phase velocity of the space harmonic exchanges energy with it. Otherwise, mean effect is null.



Constant cell length does not allow synchronism
Structures are long without space for transverse focusing

Cavity parameters



1. Average electric field
2. Shunt impedance
3. Quality factor
4. Filling time
5. Transit time factor
6. Effective shunt impedance

1. Average electric field
2. Shunt impedance
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Average electric field

Average electric field: E_0 measured in V/m.

Average electric field on beam axis in the direction of the beam propagation at a given moment in time when E(t) is maximum.

$$E(x, y, z, t) = E(x, y, z) \cdot e^{-j\omega t}$$

$x=0, y=0, z$ from 0 to L (cavity length)

$$E_0 = \frac{1}{L} \int_0^L E(0,0,z) dz$$

Measure how much field is available for acceleration

Depends on the cavity shape, resonating mode and frequency

1. Average electric field
2. **Shunt impedance**
3. Quality factor
4. Filling time
5. Transit time factor
6. Effective shunt impedance

Shunt impedance

Shunt impedance (per unit of length): **Z** measured in Ω/m .

Defines the ratio of the average electric field squared (E_0^2) to the power (P) per unit of length (L) dissipated on the walls surface.

$$Z = E_0^2 \cdot \frac{L}{P} \quad \text{or} \quad Z = E_0^2 \cdot \frac{dL}{dP}$$

Measure how well we concentrate the RF power in the useful region.

Independent on the field level and cavity length. Depends on cavity mode and geometry.

1. Average electric field
2. Shunt impedance
3. **Quality factor**
4. Filling time
5. Transit time factor
6. Effective shunt impedance

Quality factor

Quality factor: **Q** dimension-less.

Defines the ratio of the stored energy (U) to the power lost on the wall (P) in one RF cycle (f = frequency).

$$Q = \frac{2\pi \cdot f}{P} \cdot U$$

Q is a function of the geometry and of the surface resistance of the cavity material.

Examples at 700 MHz

Superconducting (niobium): $Q=10^{10}$ (depends on temperature)

Normal conducting (copper): $Q=10^4$ (depends on cavity mode)

1. Average electric field
2. Shunt impedance
3. Quality factor
4. **Filling time**
5. Transit time factor
6. Effective shunt impedance

Filling time

Filling time: t_F measured in sec.

Two different definition for traveling or standing wave.

- For TW: Time needed for the electromagnetic energy to fill the cavity of length L

$$t_F = \int_0^L \frac{dz}{v_g(z)}$$

Velocity at which the energy propagate thru the cavity

- For SW: Time it takes for the field to decrease by 1/e after the cavity has beam filled.

$$t_F = \frac{2Q}{\omega}$$

How fast the stored energy is dissipated to the wall

1. Average electric field
2. Shunt impedance
3. Quality factor
4. Filling time
5. **Transit time factor**
6. Effective shunt impedance

Transit time factor

Transit time factor: **T** dimension-less.

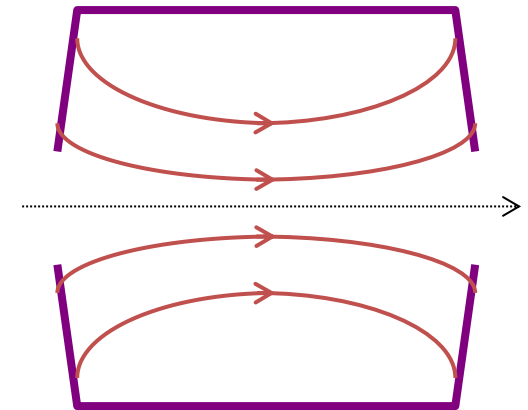
Defines the ratio of the energy gained in the time varying RF field to that in a DC field.

T is a measure of the reduction in energy gain caused by the sinusoidal time variation of the field in the gap.

$$E(x, y, z, t) = E(x, y, z) \cdot e^{-j\omega t}$$

Energy gain of a particle with charge q on axis at phase ϕ .

$$\Delta W = \int_0^L q E_z(0,0,z) \cdot e^{-j(\omega t + \phi)} dz$$



1. Average electric field
2. Shunt impedance
3. Quality factor
4. Filling time
5. **Transit time factor**
6. Effective shunt impedance

Transit time factor

Assuming a constant velocity thru the cavity (approximation!!!), we can relate position and time via

$$Z = v \cdot t = \beta c \cdot t$$

We can write the energy gain as

$$\Delta W = q \cdot E_0 \cdot L \cdot T \cdot \cos(\phi)$$

And define transit time factor as

$$T = \frac{\int_{-L/2}^{L/2} E_z(z) \cdot e^{-j\left(\frac{\omega z}{\beta c}\right)} dz}{\int_{-L/2}^{L/2} E_z(z) \cdot dz} = \frac{\int_{-L/2}^{L/2} E_z(z) \cdot e^{-j\left(\frac{\omega z}{\beta c}\right)} dz}{E_0}$$

T depends on the particle velocity and on the gap length.
It does not depend on the field.

1. Average electric field
2. Shunt impedance
3. Quality factor
4. Filling time
5. **Transit time factor**
6. Effective shunt impedance

Transit time factor

NB: TTF depends on x and y (distance for the beam axis in cylindrical symmetry).
By default, TTF is on axis!

Exercise:

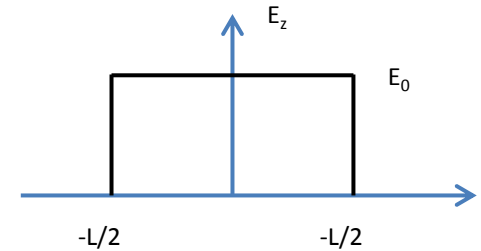
Calculate the TTF for a pillbox cavity where $E_z = E_0$

L = gap length

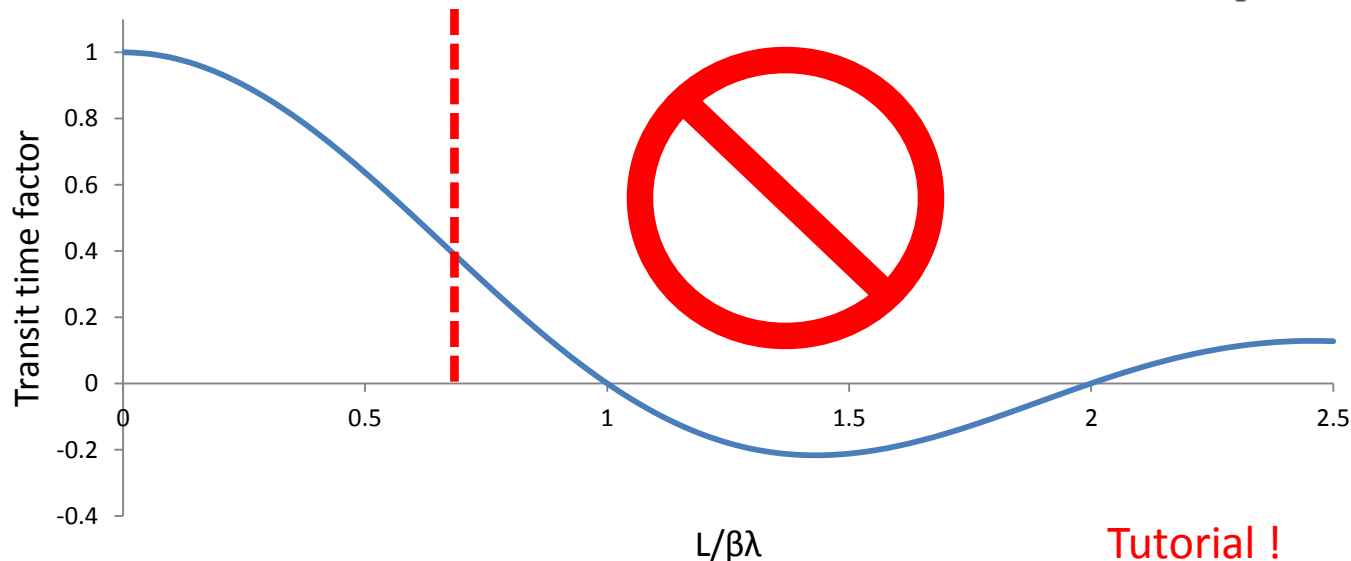
β = reduced velocity

λ = RF wavelength

Distance travelled during one RF period: $\beta c / f = \beta \lambda$



$$T = \frac{\sin \frac{\pi L}{\beta \lambda}}{\frac{\pi L}{\beta \lambda}}$$



Tutorial !

1. Average electric field
2. Shunt impedance
3. Quality factor
4. Filling time
5. Transit time factor
6. **Effective shunt impedance**

Effective shunt impedance

Effective shunt impedance: **ZT^2** .

More practical for accelerator designers who want to maximize the particle energy gain per unit power dissipation.

$$ZTT = (E_0 T)^2 \cdot \frac{L}{P}$$

While the shunt impedance measures if the structure design is optimized, the effective shunt impedance measures if the structure is optimized and adapted to the velocity of the particle to be accelerated.

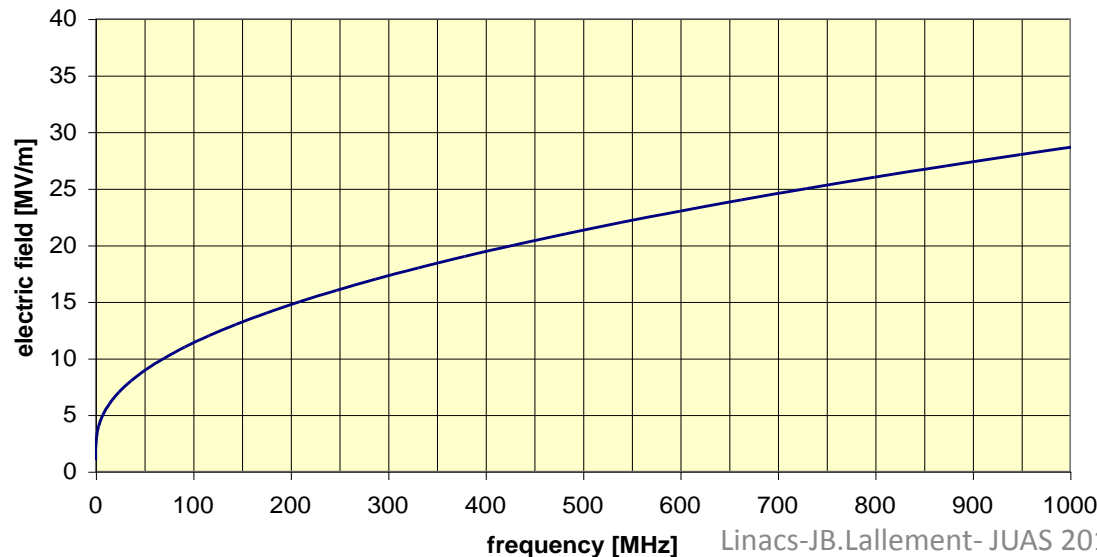
Limit to the field in a cavity

- Normal conducting
 - Heating
 - **Electrical peak** surface field (sparking)
- Super conducting
 - Quenching
 - **Magnetic field** on the surface (in Niobium max 200 mT)

The Kilpatrick sparking criterion

Normal conducting – Large gap

Kilpatrick field



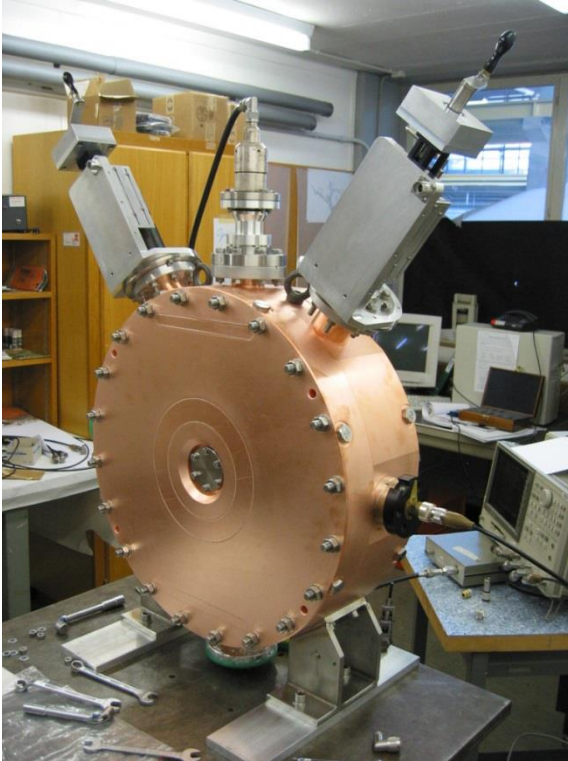
$$f = 1.64 * E^2 * \exp\left(\frac{-8.5}{E}\right)$$

W.D. Kilpatrick in the 50's

Nowadays, the peak surface field up to 2 Kilpatrick

Tutorial !

Example of cavities



Summary of Part1

First step to accelerating is to fill a cavity with electromagnetic energy to build a resonant field. In order to be the most efficient, one should:

- Concentrate the field in the beam area
- Minimize losses of RF power
- Control the limiting factors to put energy into the cavity

This is achieved by **shaping the cavity** in the appropriate way

