

Modeling Hadronic Interactions in Cosmic Ray MC generators

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Outline

Hadronic interaction models for air showers

Cross-section and Multiplicity

air shower maximum

Particle spectra

number of muons

Constraints from air showers

LHC (accelerator) data : constrain hadronic models used for EAS simulations.

<u>Cosmic ray (EAS) data</u> : additional constraints on models leading to better predictive power.

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Models for Air Shower Simulation



- Hadronic models for Simulations
 - mainly soft (low p_t (< 2 GeV/c)) physics + diffraction (forward region)
 - should handle p-, π-Air, K-Air and A-Air interactions
 - should be able to run at 10⁶ GeV center-of-mass (cms) energy
 - Single set of parameters
 - models used for EAS analysis :
 - QGSJET01/II
 - SIBYLL 2.1
 - EPOS
 - DPMJET, ...

Main source of uncertainties in EAS analysis !

Hadronic Interaction Models in CORSIKA



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Cosmic Ray Hadronic Interaction Models

- Theoretical basis :
 - ➡ pQCD (large p_t)
 - Gribov-Regge (cross section with multiple scattering)
 - energy conservation
- Phenomenology (models) :
 - hadronization
 - string fragmentation
 - EPOS : high density effects (statistical hadronization and flow)
 - diffraction (Good-Walker, ...)
 - higher order effects (multi-Pomeron interactions)
 - remnants
- Comparison with data to fix parameters
 - one set of parameter for all systems/energies

Data for Hadronic Interaction Models

- Theoretical basis :
 - pQCD : PDF and jets
 - Gribov-Regge : All cross-sections and particle multiplicities
 - energy conservation : Correlations (various triggers, proton tagging, multiplicity windows or dependence)
- Phenomenology :
 - hadronization : Particle identification and pt and multiplicity dep.
 - diffraction : Energy loss, rapidity gaps
 - higher order effects : Nuclear modification factor
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- Comparison with data to fix parameters
 - all type of min bias data are welcome to constrain hadronic interaction models for air showers
 - specific interest in forward measurement to check extrapolation for air showers

New Models

- QGSJETII-03 to QGSJETII-04 :
 - Ioop diagrams
 - rho0 forward production in pion interaction
 - re-tuning some parameters for LHC and lower energies
- EPOS 1.99 to EPOS LHC
 - tune cross section to TOTEM value
 - change old flow calculation to a more realistic one
 - introduce central diffraction
 - keep compatibility with lower energies
- Both models used in (some) LHC analysis



Direct influence of collective effects on EAS simulations has to be shown but important to compare to LHC and set parameters properly (<pt>, ...).

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Cross Section Calculation : SIBYLL / QGSJET

Interaction amplitude given by parameterization (soft) or pQCD (hard) and Gribov-Regge for multiple scattering :

- \rightarrow elastic amplitude : -2 χ (s,b)
- sum n interactions :
 - optical theorem :

 $s = (cms energy)^2$ b = impact parameter

...
$$\rightarrow -2\chi(s,b)$$
 $\sigma \sim 1 - \exp(-2\chi) \leftarrow Not the same \chi in QGSJET01, QGSJET11 and SIBYLL$

 $\frac{-2\chi)''}{2} \rightarrow \exp(-2\chi)$

 $\rightarrow \chi(s,b)$ parameters for a given model fixed by pp cross-section

- SIBYLL: pQCD mini-jet with energy dependent cut-off
- QGSJETII: pQCD + infinite re-summation of (soft) triple Pomeron coupling
- pp to pA or AA cross section from Glauber
- energy conservation not taken into account at this level

Cross Section Calculation : EPOS



Different approach in EPOS :

- Gribov-Regge but with energy sharing at parton level : MPI with energy conservation !
- amplitude parameters fixed from QCD and pp cross section
- cross section calculation take into account interference term

$$\Phi_{\rm pp}\left(x^+, x^-, s, b\right) = \sum_{l=0}^{\infty} \int dx_1^+ dx_1^- \dots dx_l^+ dx_l^- \left\{ \frac{1}{l!} \prod_{\lambda=1}^l -G(x_\lambda^+, x_\lambda^-, s, b) \right\}$$

$$\times F_{\rm proj}\left(x^+ - \sum x_\lambda^+\right) F_{\rm targ}\left(x^- - \sum x_\lambda^-\right).$$

 $\sigma_{\text{ine}}(s) = \int d^2b \left(1 - \Phi_{\text{pp}}(1, 1, s, b)\right) \Rightarrow \text{can not use complex diagram like QII}$ with energy sharing

non linear effects taken into account as correction of single amplitude G

Cross Sections

- Same cross sections at pp level up to LHC
 - weak energy dependence : no room for large change beyond LHC
- other LHC measurements of inelastic cross-section (ALICE, ATLAS, CMS) test the difference between models (diffraction)



Particle Production in SIBYLL and QGSJET

Number n of exchanged elementary interaction per event fixed from elastic amplitude (cross section) :

n from (Poisson distribution):

$$P(n) = \frac{(2\chi)^n}{n!} \cdot \exp(-2\chi)$$

- no energy sharing accounted for (interference term)
- ✤ 2n strings formed from the n elementary interactions
 - In QGSJET II, n is increased by the sub-diagrams
 - energy conservation : energy shared between the 2n strings
 - particles from string fragmentation

 \blacksquare inconsistency : energy sharing should be taken into account when fixing n

EPOS approach

Particle Production in EPOS

m number of exchanged elementary interaction per event fixed from elastic amplitude taking into account energy sharing :

➡ m from :

$$\Omega_{AB}^{(s,b)}(m,X^+,X^-) = \prod_{k=1}^{AB} \left\{ \frac{1}{m_k!} \prod_{\mu=1}^{m_k} G(x_{k,\mu}^+, x_{k,\mu}^-, s, b_k) \right\} \Phi_{AB} \left(x^{\text{proj}}, x^{\text{targ}}, s, b \right)$$

m and X fixed together by a complex Metropolis (Markov Chain)

➡ 2m strings formed from the m elementary interactions

energy conservation : energy fraction of the 2m strings given by X

- consistent scheme : energy sharing reduce the probability to have large m
- modified hadronization due to high density effect
 - statistical hadronization instead of string fragmentation

✤ larger Pt (flow)

Number of cut Pomerons

Fluctuations reduced by energy sharing (mean can be changed by parameters)



Multiplicity

- Consistent results
 - Better mean after corrections
 - difference remains in shape
 - Better tail of multiplicity distributions
 - corrections in EPOS LHC (flow) and QGSJETII-04 (minimum string size) Pre - LHC
 Post - LHC



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Pseudorapidity Distributions



Low Energy Data



EAS with Old CR Models : X_{max}



EAS with Re-tuned CR Models : X_{max}



EAS with Re-tuned CR Models : X_{max}

- Cross section and multiplicity fixed at 7 TeV
 - smaller slope for EPOS and larger for QGSJETII
 - re-tuned model converge to old Sibyll 2.1 predictions
 - reduced uncertainty from ~50 g/cm² to ~20 g/cm²
 (difference proton/iron is about 100 g/cm²)



Particle Spectra



Particle production from string (minijets) and remnants:

SIBYLL

- No remnant except for diffraction
- Leading particle from string ends
- Lund string fragmentation
- QGSJET
 - Low mass remnants
 - Leading particle similar to proj.
 - Simplified string fragmentation

EPOS

- Low and high mass remnants
- Any type of leading particle (from resonance, string, cluster)
- Corona: string fragm. from area law
- Core: micro-canonical decay+flow

Identified particles



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Identified Particle Spectra

- Detailed description can be achieved
 - identified spectra
 - \rightarrow p_t behavior driven by collective effects (in EPOS statistical hadronization + flow)



Pion Leading Particle Effect

- Rho meson production added in QGSJETII to take into account leading particle effect in pion-Air interaction
 - same effect as baryon production : forward π⁰ replaced by charged pions (reduced leading π⁰)
 - increase muon production



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EAS with Re-tuned CR Models : Muons

Effect of LHC hidden by other changes

- Corrections at mid-rapidity only for EPOS
- Changes in QGSJET motivated by pion induced data
- EPOS LHC ~ EPOS 1.99 and only -7% for QGSJETII-04



EAS constraints on Models

- A model used for EAS simulation can be highly constrain from low energy data
 - predicted mass between p and Fe
 - at low energy link with direct measurements
 - KASCADE measured correlations between hadrons, electrons and muons



Constraints from EAS

Muon Production Depth

- Independent SD mass composition measurement
 - geometric delay of arriving muons

$$c \cdot t_{g} = \frac{l}{l} - (z - \Delta)$$
$$= \sqrt{r^{2} + (z - \Delta)^{2}} - (z - \Delta)$$

mapped to muon production distance

 $z = \frac{1}{2} \left(\frac{r^2}{ct_{\rm g}} - ct_{\rm g} \right) + \Delta$

decent resolution and no bias





MPD and Models

- 2 independent mass composition measurements
 - both results should be between p and Fe
 - both results should give the same mean logarithmic mass for the same model
 - problem with EPOS appears after corrections motivated by LHC data

Iower diffractive mass motivated by rapidity gap cross-section !



- Inelasticity linked to diffraction (cross-section and mass distribution)
 weak influence on EM X_{max} since only 1st interaction really matters
 - \bullet cumulative effect for X^µ_{max} since muons produced at the end of hadr. subcase



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 - \rightarrow harder mass spec. for pions reduce X^{μ}_{max} and increase muon for same X_{max} !



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Summary

- LHC data not usable directly to analyze air showers but important to constrain hadronic models used to analyze data !
 - any min-bias measurement is useful and correlation with forward emission are even more constraining
- LHC and models for air showers :
 - strong constrains on energy evolution of particle production and crosssection
 - results converge between models for both air shower observable X_{max} and number of muons at ground (differences reduced by a factor of 2)
 - ➡ further improvements by taking into account all new important results
 - saturation effects, collective effects, forward/mid-rapidity correlations, ...
- EAS :
 - Models can be tested using EAS data by checking consistency of mass composition with different methods

high sensitivity on hadronic interactions of MPD

more direct tests : cross-section measurement, muon number, ...

Particle Spectra

Constraints from EAS

Final Conclusions



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Particle Spectra

Constraints from EAS

Final Conclusions



Constraints from EAS

Backup

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Is X^{μ}_{max} Important for Muons at Ground ?

- For EM particles : shift in $X_{max} \approx$ change in EM at ground
 - strong atmospheric absorption
- For muons : shift in $X^{\mu}_{max} \approx$ change in muons at ground
 - weak atmospheric absorption
 - model dependent energy spectra
 - distance to core dependence





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Extrapolation and LHC Results

- Source of uncertainties : extrapolation
 - to higher energies
 - strong constraints by current LHC data
 - from p-p to p-Air and pi-Air
 - current main source of uncertainty
- Needs to better take into account last LHC results :
- hard scale saturation
- collective effects in small system
 dotailed diffractive
- detailed diffractive measurements
- particle correlations
 - EPOS 3
 - QGSJETxxx







Effects of Parameters



Inelasticity



Difference in diffraction

Iow mass / high mass / central diffraction





- Pierre Auger Observable (Cazon and Garcia-Gomez)
 - Depth of maximum muon production rate
 - link to hadronic shower core
 - very sensitive to inelasticity





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rapidity gap measurement (diffraction)



Constraints from EAS

Multiplicity

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 - Better mean after corrections
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Inelasticity



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Identified particles

- Large improvement at mid-rapidity
 - very similar results for particle ratios
 - overestimation of baryon production before due to wrong interpretation of Tevatron data



Pre - LHC

Post - LHC

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Identified particles

- Large improvement at mid-rapidity
 - very similar results for particle ratios
 - overestimation of baryon production before due to wrong interpretation of Tevatron data
- Only small changes very forward

no try to tune LHCf data yet (difficult)



EAS with Re-tuned CR Models : Muons



EAS with Re-tuned CR Models : Muons



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Cross Section and Multiplicity in Models



Gribov-Regge and optical theorem

- Basis of all models (multiple scattering) but
 - Classical approach for QGSJET and SIBYLL (no energy conservation for cross section calculation)
 - Parton based Gribov-Regge theory for EPOS (energy conservation at amplitude level)
- pQCD



- Minijets with cutoff in SIBYLL
- Same hard Pomeron (DGLAP convoluted with soft part : no cutoff) in QGS and EPOS but
 - No enhanced diagram in Q01
 - Generalized enhanced diagram in QII
 - Simplified non linear effect in EPOS
 - Phenomenological approach

EAS Energy Deposit

Increase of muons in QII04

larger correction factor from missing energy



EAS Energy Deposit

Increase of muons in QII04

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Muon Energy Spectra

- Total number of muons in QGSJETII-04 (@60°) closer to EPOS BUT
 - muons with different energy (hadronic energy stored in mesons or baryons ?)
 - different zenith angle dependence (attenuation length depends on muon energy spectrum)
 - effect of low energy hadronic interaction models (Gheisha, Fluka, UrQMD) ?
 - muon production dominated by last hadronic interaction(s) !



Muon Signal at 1000m for PAO

Different zenith angle dependence

 probably better description of muon number for PAO using heavy composition consistent with X_{max}



Constraints from EAS

EAS with Re-tuned CR Models : Correlations



EAS with Re-tuned CR Models : Correlations



EAS with Re-tuned CR Models : Correlations

- QGSJETII-04 and EPOS LHC similar to EPOS 1.99
 - More muons AND more electrons with EPOS LHC compared to QGSJETII-04
 - More muons and less electrons with QGSJETII-04 compared to QGSJETII-03
 - Same correlations with EPOS LHC and QGSJETII-04
 - Lighter composition compared to QGSJETII-03



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Constraints from EAS

No big difference @ LHC but larger uncertainty in

- Source of uncertainties : extrapolation
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 - strong constraints by current LHC data
 - from p-p to p-Air
 - current main source of uncertainty



Constraints from EAS



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 - ➡ to higher energies
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 - from p-p to p-Air
 - current main source of uncertainty
- Needs for new data : p-O







Extensive Air Shower Observables



Longitudinal Development
 number of particles vs depth

$$X = \int_{h}^{\infty} dz \rho(z)$$

Larger number of particles at X_{max}

For many showers

♦ mean : <X_{max}>

- fluctuations : RMS X_{max}
- Lateral distribution function (LDF)
 - particle density at ground vs distance to the impact point (core)
 - can be muons or electrons/gammas or a mixture of all.

Simplified Shower Development

Using generalized Heitler model and superposition model :

$$X_{max} \sim \lambda_e \ln \left((1-k) \cdot E_0 / (2 \cdot N_{tot} \cdot A) \right) + \lambda_{ine}$$

Model independent parameters :

- \blacksquare E₀ = primary energy
- A = primary mass
- λ_{a} = electromagnetic mean free path
- Model dependent parameters :

N_{tot} = total multiplicity

k = elasticity

- First hadronic generation only !
- λ_{ine} = hadronic mean free path (cross section)

$$N_{tot} = N_{had} + N_{em}$$

J. Matthews, Astropart.Phys. 22 (2005) 387-397

Muon Number

From Heitler

$$N_{\mu} = \left(\frac{E_0}{E_{dec}}\right)^{\alpha}, \quad \alpha = \frac{\ln N_{\pi^{ch}}}{\ln (N_{\pi^{ch}} + N_{\pi^0})}$$

 \rightarrow after n generations

- In real shower, not only pions : Kaons and (anti)Baryons (but 10 times less ...)
- \blacksquare Baryons do not produce leading π^0
- With leading baryon, energy kept in hadronic channel = muon production
- Cumulative effect for low energy muons
- High energy muons
 - important effect of first interactions
 and baryon spectrum (LHC energy range) o



Muon number depends on the number of (anti)B in p- or π -Air interactions at all energies

More fast (anti)baryons = more muons

T. Pierog et al., Phys. Rev. Lett. 101 (2008) 171101

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Ideal Measurements for CR



add tracking in ZDC ?

Example : Inclusive Muon Spectra

Energy spectrum of all muons arriving at ground

- convolution of CR spectrum, composition of primary and hadronic interactions
- important for neutrino experiment like Ice-Cube (atmospheric neutrino flux is the background of astrophysical neutrinos)
- Can be calculated if muon weighted spectra is known :

$$|\mathbf{x}_{\mathrm{F}}|^{1.7} \mathrm{dn/dx}_{\mathrm{F}}$$

• dn/dx_{F} should be known for $\pi^{+},\pi^{-},K^{+},K^{-},D^{+},D^{-}...$

Example : Inclusive Muon Spectra (2)



In the range of LHCf ... but charged particles not seen by LHCf !

extrapolation needed

- Hadronic models are needed even for incl. flux.

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 - ➡ diffraction (Good-Walker, ...)

 - remnants
- Comparison with data to fix parameters

Better predictive power than HEP models thanks to link between total cross section and particle production (GRT) tested on a broad energy range (including EAS)

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EPOS 1.99/LHC QGSJet01/II-03/II-04 Sibyll 2.1

Oll and EPOS modif. for LHC

