Generalized N=0 vacua

Fernando Marchesano



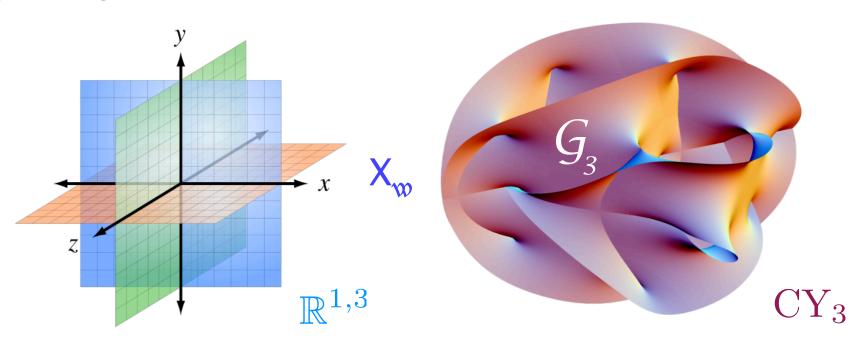
Generalized N=0 vacua

Fernando Marchesano

In collaboration with Dieter Lüst, Luca Martucci, Dimitrios Tsimpis



- Some significant progress in string phenomenology has been based in exploring new and more general string vacua
- Classical example: type IIB on a warped Calabi-Yau, threaded by background fluxes



- Some significant progress in string phenomenology has been based in exploring new and more general string vacua
- Classical example: type IIB on a warped Calabi-Yau, threaded by background fluxes
 - Moduli stabilization
 - ◆ Randall-Sundrum scenario
 - SUSY-breaking
 - ♦ de Sitter vacua
 - Inflationary scenarios

Dasgupta, Rajesh, Sethi'99 Kachru, Schulz, Trivedy'02

Giddings, Kachru, Polchinski '01

Kachru, Kallosh, Linde, Trivedi'03

Balasubramanian, Berglund, Conlon, Zuevedo'05

Kachru, Kallosh, Linde, Maldacena, McGreevy, Trivedi'03

- In this setup, at the 10D supergravity level
 - ♦ $\mathcal{N}=1$ and $\mathcal{N}=0$ vacua share the same geometry

$$ds^2 = e^{2A} ds_{\mathbb{R}^{1,3}}^2 + e^{-2A+\Phi} ds_{X_6}^2$$

- ◆ The flux introduces a new scale m_{flux}
- ♦ The SUSY-breaking parameter is a geom. quantity $G_3^{(0,3)}$
- ***** By considering $\mathcal{N}=0$ vacua and some stringy effects
 - ♦ D-instantons
 - α' corrections
 - anti-D3-branes

- If we neglect the warp factor
 - ◆ We can understand 4D physics in terms of the CY light fields, Kähler potential, and a flux-induced superpotential

$$W=\int_{X_6} \mathcal{G}_3 \wedge \Omega$$
 Gukov, Vafa, Witten'99

- lacktriangle SUSY-breaking is modulus dominated $\langle F^T \rangle \neq 0$
- lacktriangle The scalar pot. does not depend on $\langle F^T \rangle \Rightarrow$ no-scale vacuum
- On the other hand the warp factor can have important effects
 - ♦ It will modify the spectrum of light fields
 - ♦ It will modify the Kähler potential

see Shiu's talk

♦ It is essential to create hierarchies, suppress soft terms and to uplift to de Sitter via anti-D3-branes

Questions:

Can we find similar families of N=0 vacua?

Are they all no-scale?

Which new features can we obtain?

- These questions are hard to answer even in supergravity:
 - ♦ We need to solve e.o.m. which are 2nd order
 - ♦ We need to check stability

- Main strategy in the literature:
 - → Minimize a flux-inspired D=4 effective potential V_{flux}
 - ◆ Guess the 10D geometry from its minima and K, W_{flux}

see Camara's talk

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 - → Minimize a flux-inspired D=4 effective potential V_{flux}
 - ◆ Guess the 10D geometry from its minima and K, W_{flux}

see Camara's talk

- However:
 - ♦ We are neglecting all kinds of warp factor effects
 - ◆ We do not know if W_{flux} captures all the light degrees of freedom of the theory
 - ⇒ We could be missing important 4D physics!!!

Idea:

Construct N=0, 10D backgrounds similar to the warped Calabí-Yau case

Analyze later on their 4D physics

Generalized geometry

* What is the right way to generalize $\mathcal{N}=0$ warped Calabi-Yau?

Idea: use generalized complex geometry

see Louis' talk

♣ Basically, this amounts to take the background "Killing" spinor € and express it in terms of polyforms

$$\epsilon = \begin{pmatrix} \epsilon_1 \\ \epsilon_2 \end{pmatrix} \qquad \epsilon_i = \zeta_i \otimes \eta_i + \zeta_i^* \otimes \eta_i^*$$

$$\{\eta_1, \eta_2\} \quad \leftrightarrow \quad \{\Psi_1, \Psi_2\} \qquad \begin{cases} \Psi_1 & = \psi_0 + \psi_2 + \psi_4 + \psi_6 \\ \Psi_2 & = \psi_1 + \psi_3 + \psi_5 \end{cases}$$

Generalized geometry

❖ What is the right way to generalize $\mathcal{N}=0$ warped Calabi-Yau? ↓

Idea: use generalized complex geometry

- ♣ Basically, this amounts to take the background "Killing" spinor € and express it in terms of polyforms
- * This can be done in $\mathcal{N}=1$ backgrounds and in backgrounds with approximate SUSY, like in $\mathcal{N}=0$ wCY/F-theory compactifications

The e.o.m. constraints found by GKP are

see also Graña and Polchinski'00

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These can be rewritten as:

$$d_H \left[e^{4A - \Phi} \operatorname{Re} \left(e^{iJ} \right) \right] = e^{4A} \tilde{*}_6 F_{RR}$$

$$J = e^{\Phi - 2A} J^{X_6}$$

 $F_{RR} = F_1 + F_3 + F_5^{int}$

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$$\downarrow \qquad \qquad F$$

$$d_{H}\left[e^{4A-\Phi}\operatorname{Re}\Psi_{1}\right] = e^{4A}\tilde{*}_{6}F_{RR}$$

$$J = e^{\Phi - 2A} J^{X_6}$$

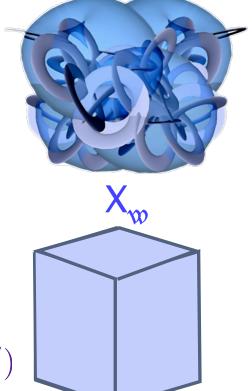
 $F_{RR} = F_1 + F_3 + F_5^{int}$

$$\Psi_1^{ ext{wCY}} = e^{iJ}$$

- $lacktriangledown d_H \left[e^{4A-\Phi} \mathrm{Re} \, \Psi_1
 ight] = e^{4A} \tilde{*}_6 F_{\mathrm{RR}}$ is a differential condition satisfied by general $\mathcal{N}=1$ type II vacua

 Graña, Minasian, Petrini, Tomasiello '05
- ♣ It has also a nice D=4 interpretation
 - ◆ e^{4A-Φ} Re Ψ₁ is a generalized calibration for space-time filling probe D-branes
 - ◆ This calibration is "closed" when the condition above is satisfied
 - → A calibrated D-brane minimizes its energy with respect to any continuous deformation
 - \Rightarrow BPS lower bound $V(\Sigma, \mathcal{F})_{BPS} \leq V(\Sigma', \mathcal{F}')$

Martucci'06

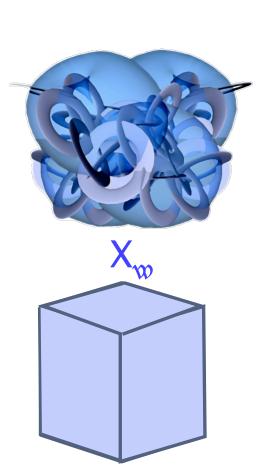


BPS bounds

- **BPS** bounds for D-branes are usual in $\mathcal{N}=1$ backgrounds, but they can also appear in absence of bulk supersymmetry
- In the present context

BPS bound \Leftrightarrow \exists gen. calibration ω

- ♣ If the latter is true everything works like in $\mathcal{N}=1$ backgrounds \Rightarrow same BPS conditions
- In the GKP case $\omega^{sf} = \text{Re } e^{iJ}$, so the BPS D-branes are
 - D3-branes
 - ♦ D7-branes with $\mathcal{F}^{SD} = 0$



More GKP from GCG

- What about other kinds of D-branes?
- The wCY/F-theory construction implies that

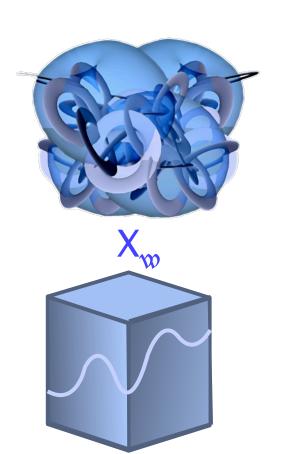
$$→$$
 dJ^X₆ = d(e^{2A-Φ} J) = 0

$$ightharpoonup H$$
 harm. $+ b_1(X_6) = 0 \Rightarrow H \land J = 0$

$$d_{H}\left[e^{2A-\Phi}\operatorname{Im}\left(e^{iJ}\right)\right] = 0$$

$$d_{H}\left[e^{2A-\Phi}\operatorname{Im}\Psi_{1}\right] \equiv d_{H}\omega^{\operatorname{st}} = 0$$

⇒ 4D strings also develop a BPS lower bound



More GKP from GCG

♣ There is a last kind of calibrated D-brane in N=1 vacua:
4D domain walls
Martucci '06

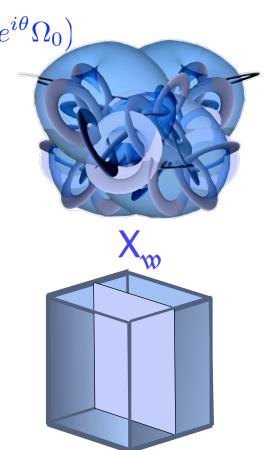
The gen. calibration in this case is

 $\omega^{DW} = e^{3A-\Phi} \operatorname{Re}\left(e^{i\theta}\Psi_{2}\right) = e^{-\Phi/2} \operatorname{Re}\left(e^{i\theta}\Omega_{X_{6}}\right) \equiv \operatorname{Re}\left(e^{i\theta}\Omega_{0}\right)$

where Ω_0 is a closed, holomorphic (3,0)-form

Is $d_H\omega^{DW}=0$?

- ♦ d $\Omega_0 = 0$ ⇒ D5-branes wrapping SL's are BPS like in $\mathcal{N}=1$ vacua
- ♦ H ∧ $\Omega_0 = 0 \Leftrightarrow H^{(0,3)} = 0 \Leftrightarrow G_3^{(0,3)} = 0 !!$ ⇒ D7-branes in coisotropic 5-cycles are not BPS for $\mathcal{N}=0$ vacua
- ⇒ BPSness breaks down for 4D DW



♣ For general N=1 backgrounds we have

Graña, Minasian, Petrini, Tomasiello'05

Martucci'06

Equation	D=4 interpretation
$d_H \left(e^{4A - \phi} \operatorname{Re} \Psi_1 \right) = e^{4A} F_{RR}$	gauge BPSness
$d_H\left(e^{2A-\phi}\mathrm{Im}\Psi_1\right) = 0$	D-string BPSness
$d_H\left(e^{3A-\phi}\Psi_2\right) = 0$	Domain Wall BPSness

In a warped Calabi-Yau

$$\Psi_1^{\text{wCY}} = e^{iJ} \qquad \Psi_2^{\text{wCY}} = \Omega_0$$

♣ For an N=0 warped Calabi-Yau

Equation	D=4 interpretation
$d_H \left(e^{4A - \phi} \operatorname{Re} \Psi_1 \right) = e^{4A} F_{RR}$	gauge BPSness
$d_H\left(e^{2A-\phi}\mathrm{Im}\Psi_1\right) = 0$	D-string BPSness
$d_H\left(e^{3A-\phi}\Psi_2\right) \neq 0$	DW non-BPSness

In a warped Calabi-Yau

$$\Psi_1^{\text{wCY}} = e^{iJ} \qquad \Psi_2^{\text{wCY}} = \Omega_0$$

• We will focus on $\mathcal{N}=0$ backgrounds that fulfill the gauge and D-string BPSness conditions but not the DW BPSness cond.

DWSB backgrounds



❖ We will focus on N=0 backgrounds that fulfill the gauge and D-string BPSness conditions but not the DW BPSness cond.

DWSB backgrounds

- If such background leads to a D=4 effective theory the BPSness conditions will imply
 - → gauge BPSness ⇒ stable gauge theories, no tachyons
 - → string BPSness
 → no D-terms generated by fluxes

DWSB

In terms of gravitino and dilatino var. DWSB gives a constrained, but still complicated, SUSY-breaking ansatz. We can consider the subansatz

$$\delta\psi_{\mu} = r \Gamma_{\mu} \zeta \otimes \begin{pmatrix} \eta_{1}^{*} \\ \eta_{2}^{*} \end{pmatrix} + cc.$$

$$\delta\psi_{m} = -r \zeta \otimes \begin{pmatrix} \Lambda_{mn} \Gamma^{n} \eta_{1}^{*} \\ \Lambda_{nm} \Gamma^{n} \eta_{2}^{*} \end{pmatrix} + cc.$$

$$\delta\lambda' = -2r \zeta \otimes \begin{pmatrix} \eta_{1}^{*} \\ \eta_{2}^{*} \end{pmatrix} + cc.$$

where Λ^{m}_{n} is a local O(6) transformation that, in the spinorial rep. satisfies $\eta_{1} = i\Lambda\eta_{2}$

The DW non-BPSness condition then reads

$$d_H \left(e^{3A - \phi} \Psi_2 \right) = i r e^{3A - \phi} \left[\operatorname{Im} \Psi_1 + \frac{1}{2} \Lambda_{mn} \Gamma^m (\operatorname{Im} \Psi_1) \Gamma^n \right]$$

DWSB

♦ We can further simplify things by assuming that Λ has the form of a certain "D-brane rotation"

The DWSB condition then reads

$$d_H(e^{3A-\Phi}\Psi_2) = 4i \, r \, (-)^{|\Psi_2|} e^{3A-\Phi} \frac{\sqrt{\det g|_{\Pi}}}{\sqrt{\det(g|_{\Pi}+R)}} e^{-R} \wedge \sigma(d\text{Vol}_{\perp})$$

- ♦ T_{Π} is integrable and $dR = H|_{\Pi} \Rightarrow$ generalized foliation
- ♦ A gauge D-brane wrapping Π and with $\mathcal{F} = R$ is BPS (aligned)
- ◆ Because of d_H-exactness r cannot be any function

GKP as DWSB

This subansatz contains the warped Calabi-Yau case

$$\Psi_1^{\text{wCY}} = e^{iJ} \qquad \Psi_2^{\text{wCY}} = \Omega_0$$

$$\mathcal{G}^{(0,3)} = -\frac{i}{2} r e^{-3A} \bar{\Omega}_0 \qquad \Lambda_{mn} = g_{mn}$$

- ♣ And $d_H(e^{3A-\Phi} \Psi_2) = six-form \Rightarrow \Pi = point \Rightarrow aligned D3-branes$
- ♣ In this case, r and \(\Lambda \) are related to 4D quantities
 - r e^{-3A} ≈ W₀ ≈ F_T (T : overall Kähler modulus)
 - ↑ A_{mn} structure of soft terms on D7-branes
- Does this apply to more general DWSB vacua?

Effective potential

- But... are these backgrounds actually vacua?
- At the supergravity level, one can check if the 10D e.o.m.'s are satisfied by extremizing the effective 4D action

$$S_{
m eff}=\int_{X_4} d^4x \sqrt{-g_4} \Big(rac{1}{2}\,{\cal N} \widetilde{R_4-2\pi {\cal V}_{
m eff}}\Big)$$
 4D curvature

$$\mathcal{V}_{\mathrm{eff}} = \int_{X_6} d\mathrm{Vol}_6 \, e^{4A} \Big\{ e^{-2\Phi} \big[-R_6 + \frac{1}{2} H^2 - 4(d\Phi)^2 + 8\nabla^2 A + 20(dA)^2 \big] - \frac{1}{2} F_{\mathrm{RR}}^2 \Big\} \quad \text{closed strings} \\ + \sum_{i \in \mathrm{loc. \ sources}} \tau_i \Big(\int_{\Sigma_i} e^{4A - \Phi} \sqrt{\det(g|_{\Sigma_i} + \mathcal{F}_i)} - \int_{\Sigma_i} C^{\mathrm{el}}|_{\Sigma_i} \wedge e^{\mathcal{F}_i} \Big) \quad \quad \text{open strings} \\ + \text{O-planes}$$

Effective potential

Extremizing Seff one obtains the full set of e.o.m.'s to be imposed on a type II flux compactification to 4D of the form

$$ds_{10}^2 = e^{2A(y)} ds_{X_4}^2 + g_{mn} dy^m dy^n$$

- For instance, one can derive that the external 4D space must be Einstein, with $R_4 = 8 \pi V_{\text{eff}}/\mathcal{N}$
- One can also rewrite V_{eff} in terms of Ψ_1 and Ψ_2 , and check that SUSY backgrounds automatically satisfy the e.o.m.'s

see also Koerber and Tsimpis'07

For our DWSB subansatz to Minkowski, only the variation of the B-field and internal metric give non-trivial constraints, which however are automatically satisfied in simple examples

- This effective potential is also useful to exclude the presence of tree-level closed string tachyons
- For the DWSB subansatz above two conditions need to be imposed to make $V_{\rm eff}$ semi-definite positive
- Namely, when going off-shell
 - ♦ No vectors under SU(3) x SU(3) must appear in $\delta \lambda'$
 - ★ X₆ must still be a generalized foliation

$$d_H(e^{3A-\Phi}\Psi_2) = ir\tilde{\jmath}_{(\Pi,R)}$$

$$\mathcal{V}_{\text{eff}}^{\text{DWSB}} = \frac{1}{2} \int_{X_6} d\text{Vol}_6 \, e^{4A} \big[F_{\text{RR}} - e^{-4A} d_H (e^{4A - \Phi} \text{Re} \Psi_1) \big]^2$$

$$+ \frac{1}{2} \int_{X_6} d\text{Vol}_6 \, \big[d_H (e^{2A - \Phi} \text{Im} \Psi_1) \big]^2$$

$$+ \frac{1}{2} \int_{X_6} e^{-2A} |r|^2 \Big[\langle \tilde{*}_6 \tilde{\jmath}_{(\Pi,R)}, \tilde{\jmath}_{(\Pi,R)} \rangle - \frac{|\langle \Psi_1, \tilde{\jmath}_{(\Pi,R)} \rangle|^2}{d\text{Vol}_6} \Big]$$

$$+ \sum_{i \in \text{D-branes}} \tau_i \int_{X_6} e^{4A - 2\Phi} \Big(d\text{Vol}_6 \, \rho_i^{\text{loc}} - \langle \text{Re} \Psi_1, j_i \rangle \Big)$$

$$\begin{split} \mathcal{V}_{\text{eff}}^{\text{DWSB}} &= \frac{1}{2} \int_{X_6} d \text{Vol}_6 \, e^{4A} \big[F_{\text{RR}} - e^{-4A} d_H (e^{4A-\Phi} \text{Re} \Psi_1) \big]^2 \text{gauge } \\ &+ \frac{1}{2} \int_{X_6} d \text{Vol}_6 \, \big[d_H (e^{2A-\Phi} \text{Im} \Psi_1) \big]^2 \\ &+ \frac{1}{2} \int_{X_6} e^{-2A} |r|^2 \Big[\langle \tilde{*}_6 \tilde{\jmath}_{(\Pi,R)}, \tilde{\jmath}_{(\Pi,R)} \rangle - \frac{|\langle \Psi_1, \tilde{\jmath}_{(\Pi,R)} \rangle|^2}{d \text{Vol}_6} \Big] \\ &+ \sum_{i \in \text{D-branes}} \tau_i \int_{X_6} e^{4A-2\Phi} \Big(d \text{Vol}_6 \, \rho_i^{\text{loc}} - \langle \text{Re} \Psi_1, j_i \rangle \Big) \end{split}$$

$$\begin{split} \mathcal{V}_{\text{eff}}^{\text{DWSB}} &= \frac{1}{2} \int_{X_6} d \text{Vol}_6 \, e^{4A} \big[F_{\text{RR}} - e^{-4A} d_H (e^{4A - \Phi} \text{Re} \Psi_1) \big]^2 \\ &+ \frac{1}{2} \int_{X_6} d \text{Vol}_6 \, \big[d_H (e^{2A - \Phi} \text{Im} \Psi_1) \big]^2 \quad \text{string BPS ness} \\ &+ \frac{1}{2} \int_{X_6} e^{-2A} |r|^2 \Big[\langle \tilde{*}_6 \tilde{\jmath}_{(\Pi,R)}, \tilde{\jmath}_{(\Pi,R)} \rangle - \frac{|\langle \Psi_1, \tilde{\jmath}_{(\Pi,R)} \rangle|^2}{d \text{Vol}_6} \Big] \\ &+ \sum_{i \in \text{D-branes}} \tau_i \int_{X_6} e^{4A - 2\Phi} \Big(d \text{Vol}_6 \, \rho_i^{\text{loc}} - \langle \text{Re} \Psi_1, j_i \rangle \Big) \end{split}$$

We then obtain:
$$\mathcal{V}_{\text{eff}}^{\text{GKP}} = \frac{1}{4} \int_{X_6} d\text{Vol}_6 \, e^{4A} \big| (1 + i *_6) \mathcal{G}_3 \big|^2$$

$$\mathcal{V}_{\text{eff}}^{\text{DWSB}} = \frac{1}{2} \int_{X_6} d\text{Vol}_6 \, e^{4A} \big[F_{\text{RR}} - e^{-4A} d_H (e^{4A - \Phi} \text{Re} \Psi_1) \big]^2$$

$$+ \frac{1}{2} \int_{X_6} d\text{Vol}_6 \, \big[d_H (e^{2A - \Phi} \text{Im} \Psi_1) \big]^2$$

$$+ \frac{1}{2} \int_{X_6} e^{-2A} |r|^2 \left[\langle \tilde{*}_6 \tilde{\jmath}_{(\Pi,R)}, \tilde{\jmath}_{(\Pi,R)} \rangle - \frac{|\langle \Psi, \tilde{\jmath}_{(\Pi,R)} \rangle|^2}{d\text{Vol}_6} \right]$$

$$+ \sum_{i \in \text{D-branes}} \tau_i \int_{X_6} e^{4A - 2\Phi} \big(d\text{Vol}_6 \, \rho_i^{\text{loc}} - \langle \text{Re} \Psi_1, j_i \rangle \big)$$

$$= dib^{ration} \quad cond.$$

$$\begin{split} \mathcal{V}_{\text{eff}}^{\text{DWSB}} &= \frac{1}{2} \int_{X_6} d \text{Vol}_6 \, e^{4A} \big[F_{\text{RR}} - e^{-4A} d_H (e^{4A-\Phi} \text{Re} \, \Psi_1) \big]_{\textit{gauge}}^2 \, \textit{BPSne55} \\ &+ \frac{1}{2} \int_{X_6} d \text{Vol}_6 \, \big[d_H (e^{2A-\Phi} \text{Im} \, \Psi_1) \big]^2 \quad \textit{string} \, \, \textit{BPSne55} \\ &+ \frac{1}{2} \int_{X_6} e^{-2A} |r|^2 \Big[\langle \tilde{*}_6 \tilde{\jmath}_{(\Pi,R)}, \tilde{\jmath}_{(\Pi,R)} \rangle - \frac{|\langle \Psi_1, \tilde{\jmath}_{(\Pi,R)} \rangle|^2}{d \text{Vol}_6} \Big] \\ &+ \sum_{i \in \text{D-branes}} \tau_i \int_{X_6} e^{4A-2\Phi} \Big(d \text{Vol}_6 \, \rho_i^{\text{loc}} - \langle \text{Re} \, \Psi_1, j_i \rangle \Big) \\ &\quad \textit{cdibration cond.} \end{split}$$

- lacktriangle Notice that on-shell $\mathcal{V}_{ ext{eff}}$ does not depend on r
 - ⇒ No-scale structure

4D Interpretation

Without truncating the theory, one may give a 4D interpretation of these vacua by using a 4D Weyl invariant formalism

Koerber and Martucci'07

One then finds a 4D gravitino mass of the form

$$\mathcal{N}m_{3/2} = \int_{X_6} r \, e^{3A - 2\Phi} d\text{Vol}_6$$

- \bullet An F-term proportional to r for a field \triangle ["orthogonal" to $\Delta^{\perp} \sim d_H(e^{3A-\Phi} \Psi_2)$]
 - \rightarrow A superpot. W independent of $\Delta \Rightarrow$ no-scale structure
 - Non-vanishing gaugino masses for all but aligned D-branes whose gauge kinetic function depends on Δ^{\perp}
 - \rightarrow An F-term pattern that can be understood as \triangle -dominated, quaternionic SUSY breaking in the constant warp factor limit

What else is in the book?

- The DWSB subansatz contains many classes of vacua beyond the GKP class. One can describe their 10D geometry and provide explicit examples based on twisted-tori and β-deformed bkgs.
- One can compute moduli mediated soft-term masses microscopically, by using the fermionic D-brane action
- One can include anti-D-branes into these backgrounds and compute their effective potential
- One can generalize the DWSB ansatz to AdS₄ compactifications
- ❖ One can follow a complementary approach to construct N=0 vacua, based on integrability techniques, and construct novel classes of AdS₄ vacua in this way

Conclusions

- We have discussed a very particular class of $\mathcal{N}=0$ backgrounds, where the 4D BPS bounds of $\mathcal{N}=1$ vacua are partially present
- We have considered backgrounds which contain the BPS bounds for gauge D-branes, with model-building applications in mind
- ❖ We have also imposed D-flatness in our backgrounds, aiming to reproduce the features of warped Calabi-Yau/F-theory \mathcal{N} =0 vacua
- We have achieved this by considering a very particular subansatz, but this is clearly only the tip of the iceberg. Many more vacua with different features are out there
- ❖ Our discussion has remained in the supergravity limit of type II theories, but the main idea of classifying vacua via their 4D BPS bounds is general. It could be applied to other 𝒩=0 vacua!!