

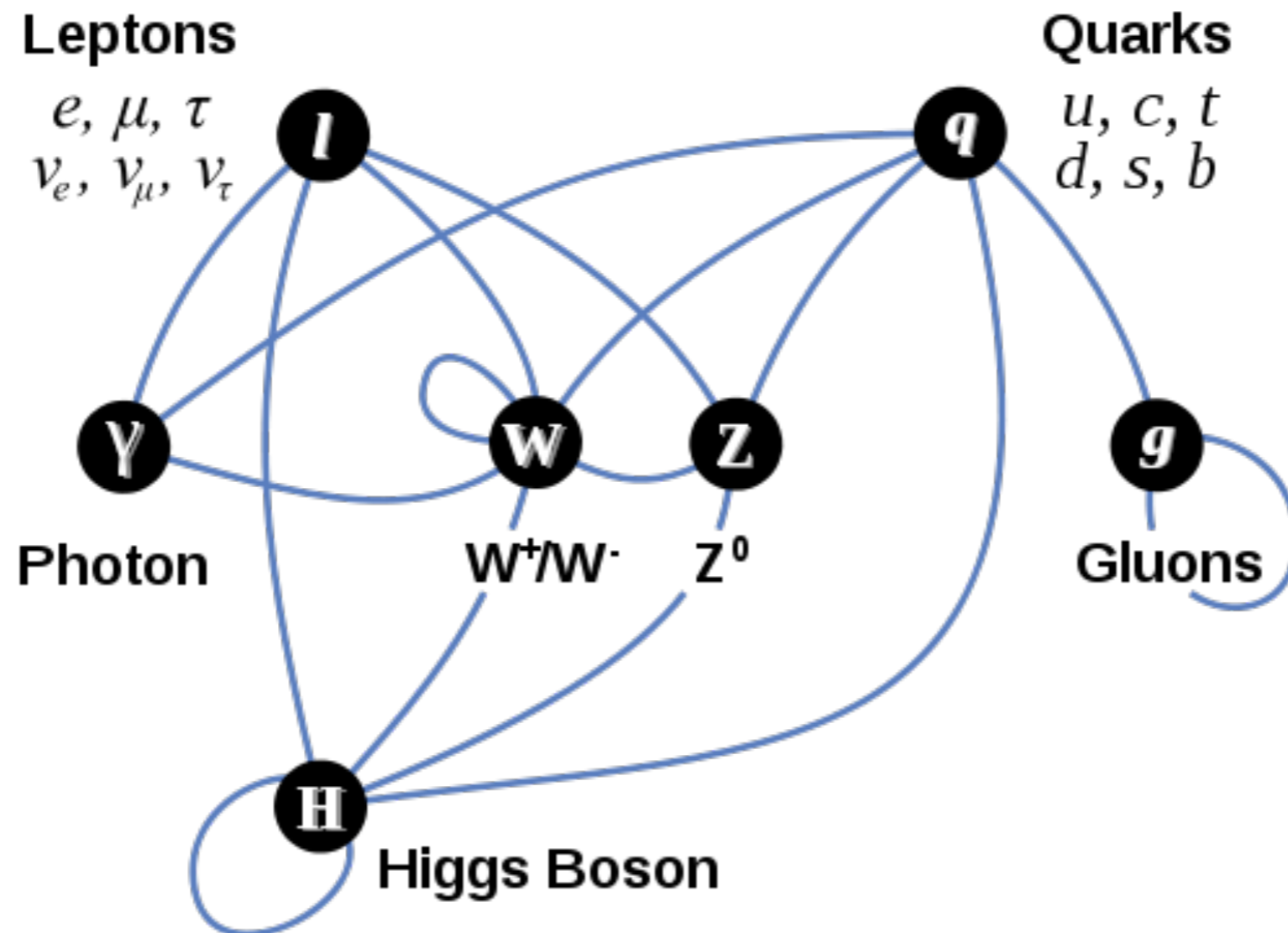
Beyond the Standard Model

Andreas Weiler
(DESY&CERN)

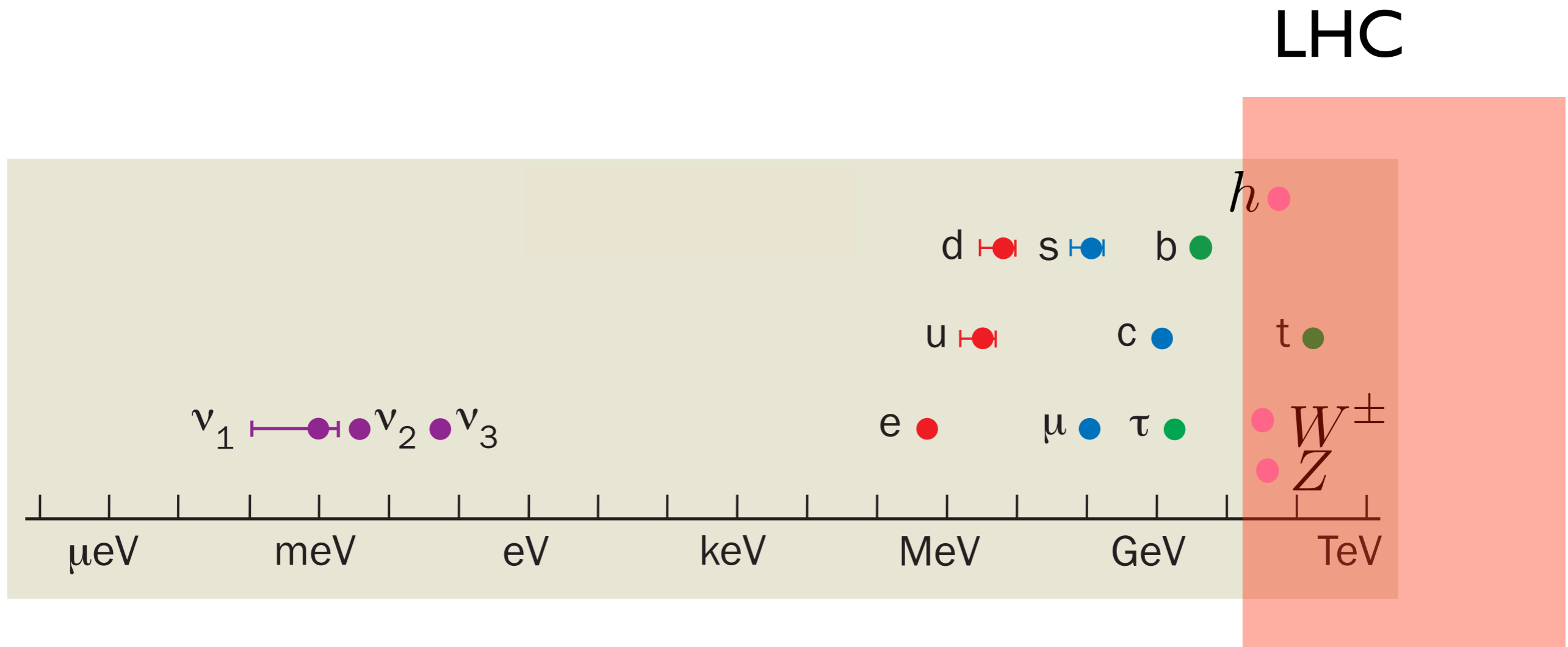


CERN school
2014/6/29

The SM



The energy frontier



What can we expect to discover?

Before LHC_{7/8}

theorists' statements

Susy is right around
the corner

Dark matter is a WIMP
and we'll produce it at LHC

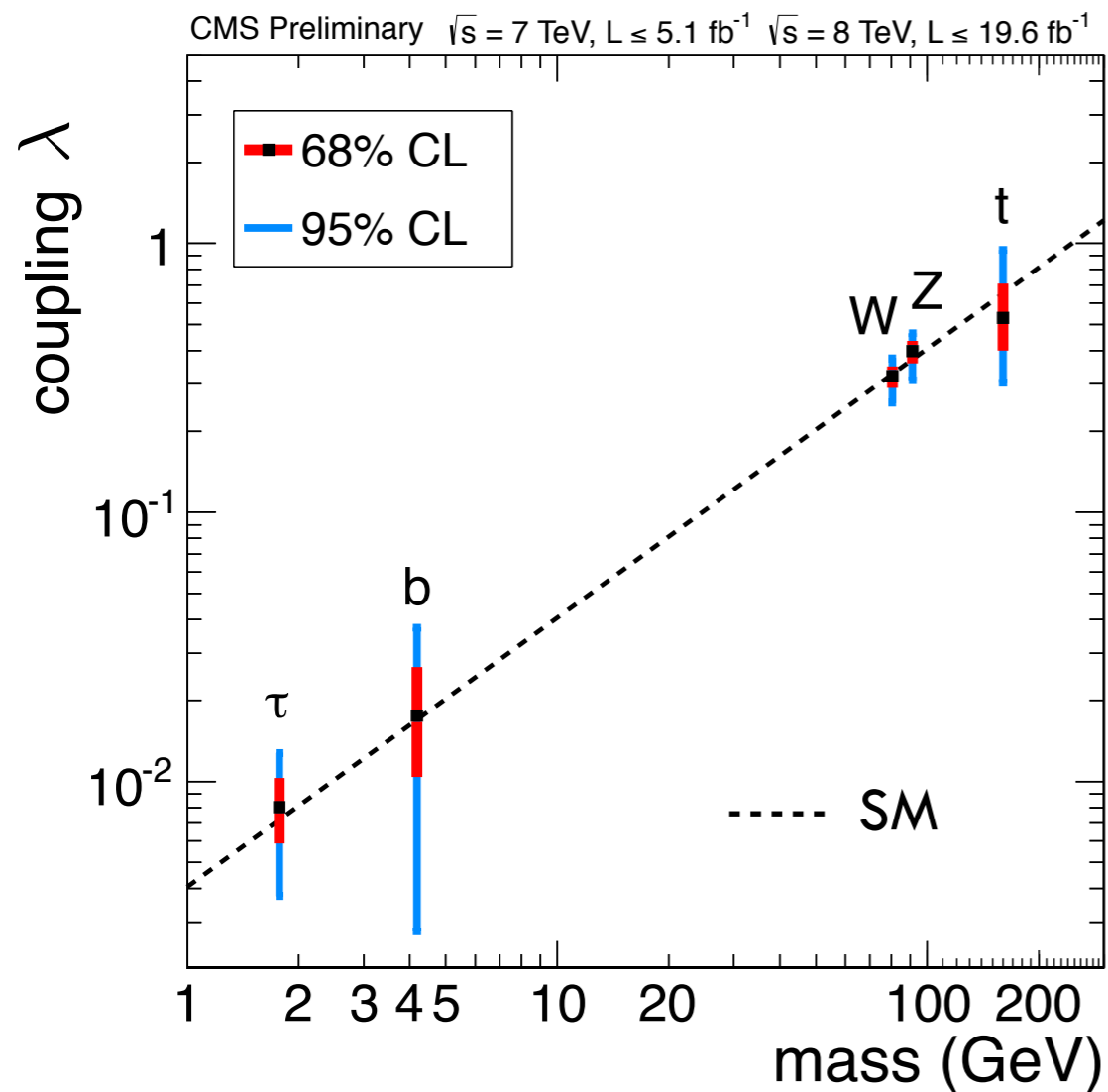
We'll see non-SM CP and
flavor violation

Extra-dimensions will
manifest itself through KK-states

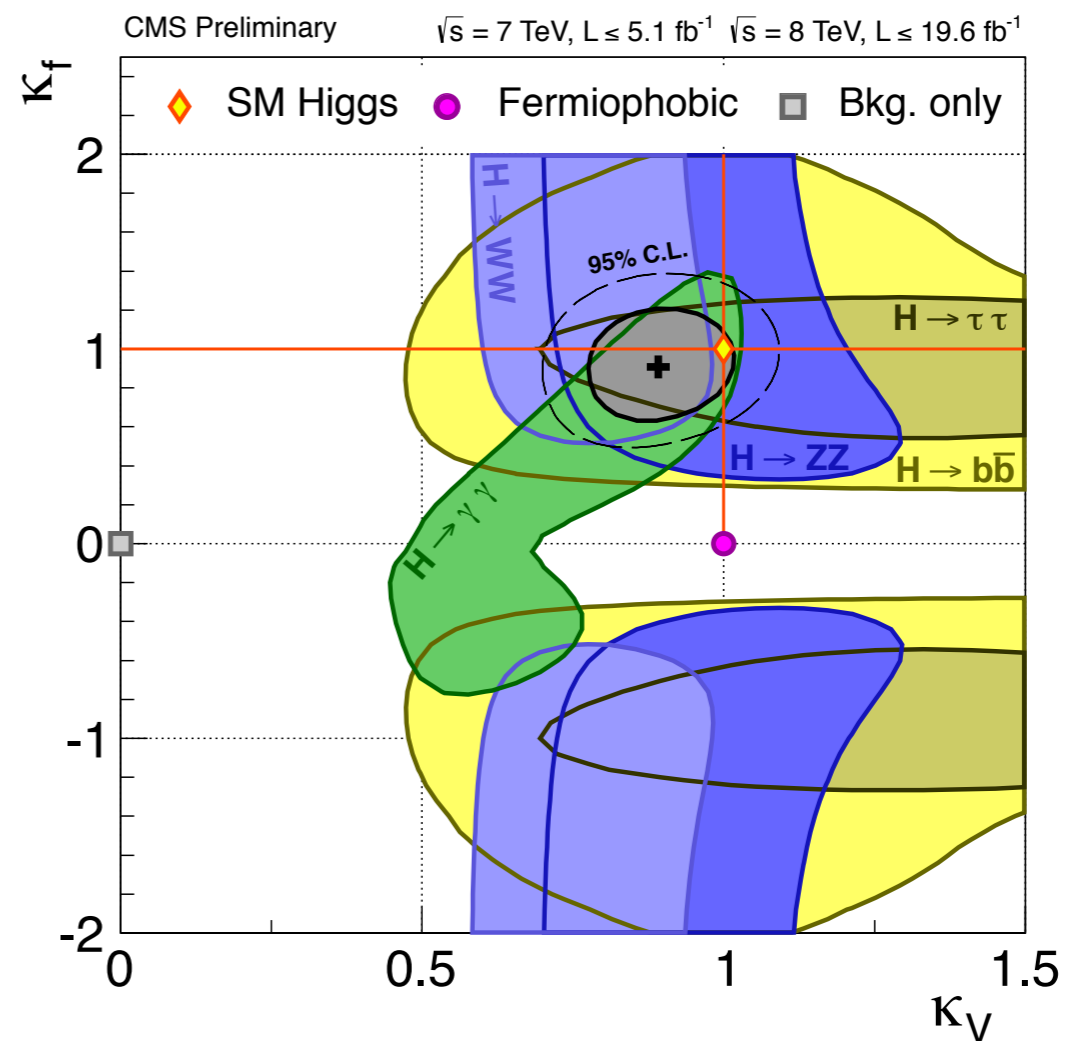
We'll have a portal
to hidden sectors

Higgs

Related to EWSB



overall compatible w/ SM



$$\lambda_\psi \propto \frac{m_\psi}{v}, \quad \lambda_V^2 \equiv \frac{g_{VVh}}{2v} \propto \frac{m_V^2}{v^2}$$

Good time for BSM?

- Fundamental scalars abound (Higgs, inflation)
- Are we done?

DM is an axion?

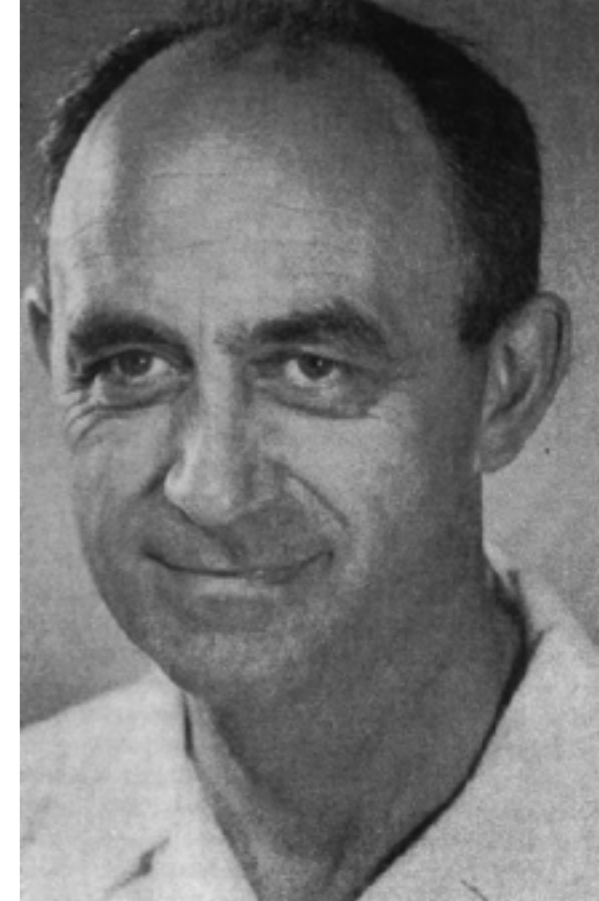
Susy at 100 TeV?



Why still expect new physics at the LHC?



Fermi theory



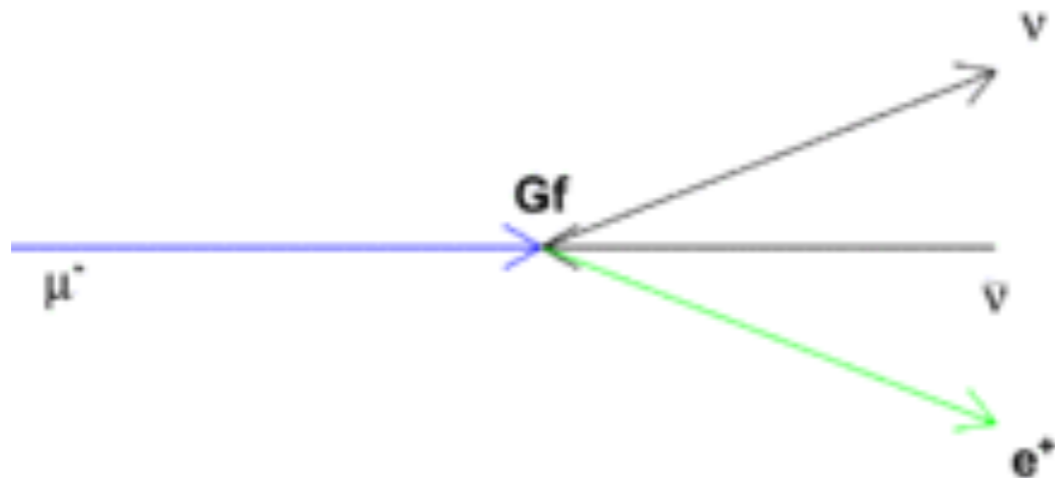
G_F

$$\frac{g^2}{M_W^2} (\bar{\nu}_\mu \gamma_L^\alpha \mu) (\bar{e} \gamma_L^\alpha \nu_e)$$

scale!

dimensional analysis

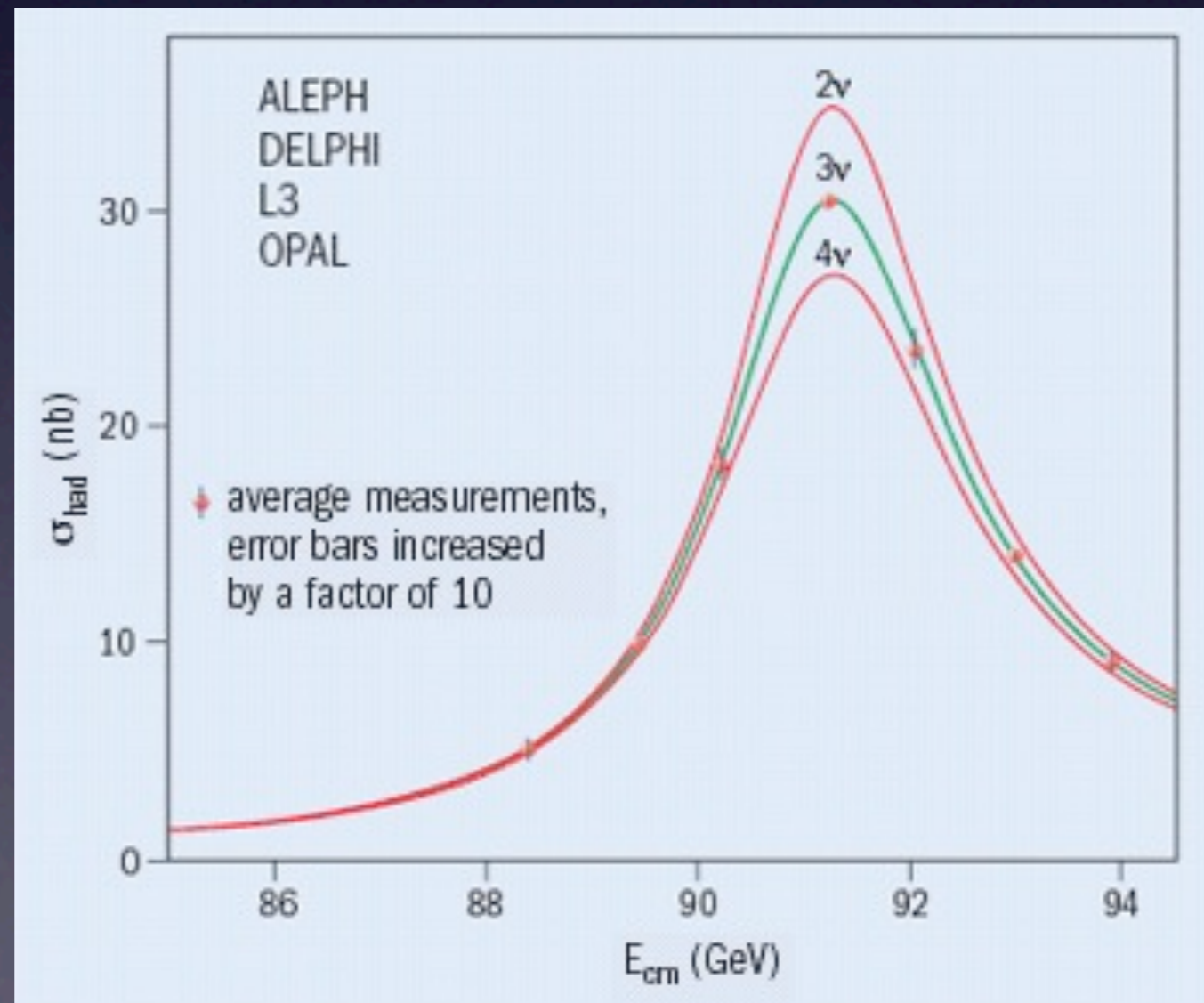
$$\sigma \propto \frac{g^4}{M_W^4} E^2$$



something interesting will happen around $E \sim M_W!$

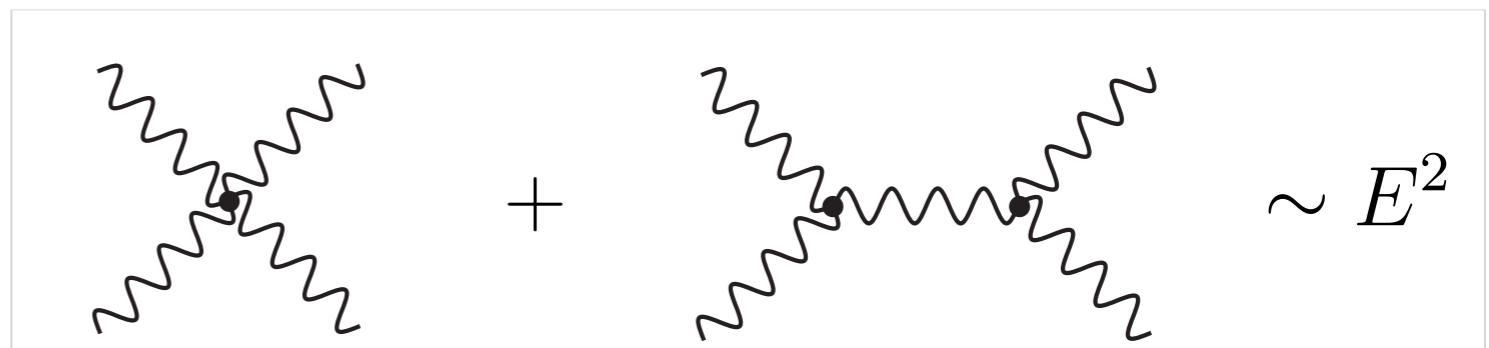
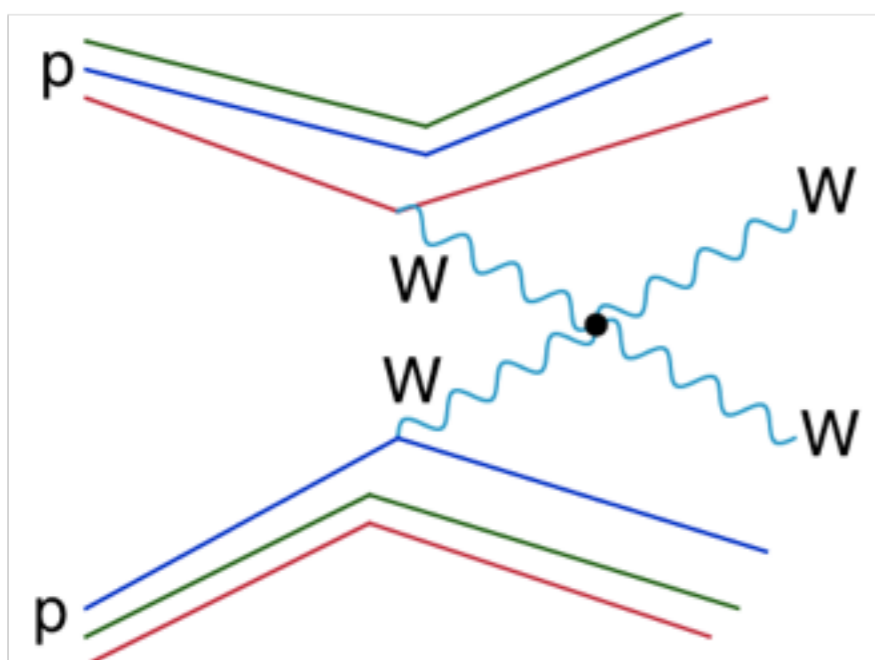
LEP

M_Z

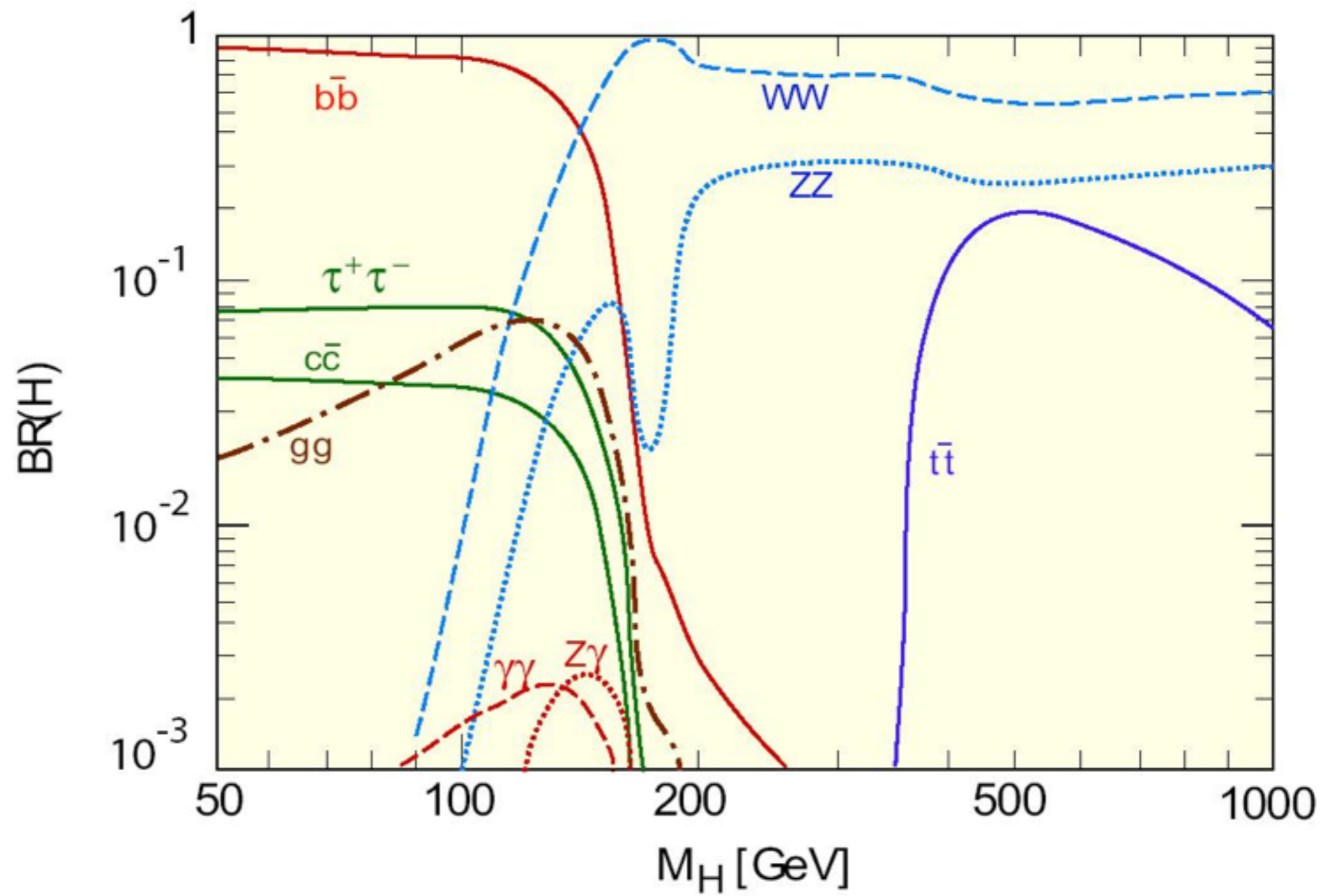


SM without the Higgs

$$\mathcal{L}_{\text{eff}} = \mathcal{L}_{\text{SM}}(\cancel{H^0}, A_\mu, W_\mu^\pm, Z_\mu, G_\mu, q, \ell) \quad (\text{unitary gauge})$$

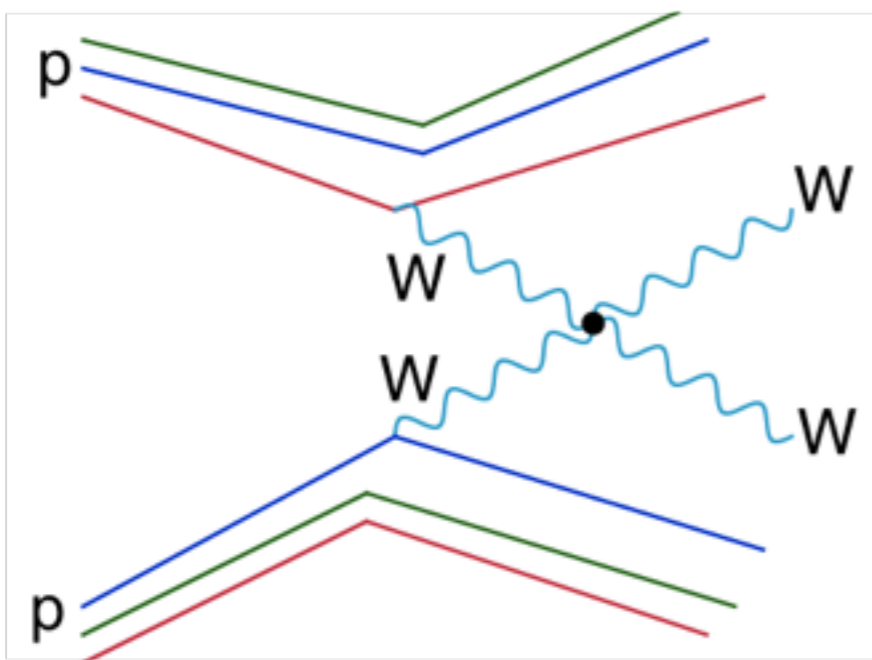


$$\sim \cancel{E^4} + E^2 + \dots \quad \sim \cancel{E^4} + E^2 + \dots$$



SM without the Higgs

$$\mathcal{L}_{\text{eff}} = \mathcal{L}_{\text{SM}}(\cancel{H^0}, A_\mu, W_\mu^\pm, Z_\mu, G_\mu, q, \ell) \quad (\text{unitary gauge})$$

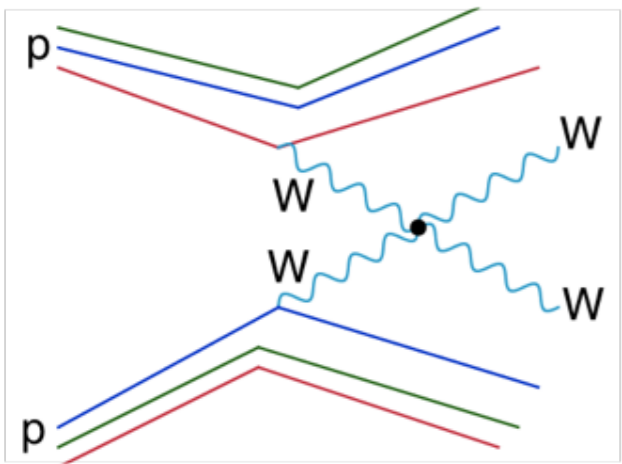


$$\text{Diagram 1} + \text{Diagram 2} \sim E^2$$

$$\sim \cancel{E^4} + E^2 + \dots \quad \sim \cancel{E^4} + E^2 + \dots$$

$$\Lambda \approx 4\pi v \approx 3 \text{ TeV}$$

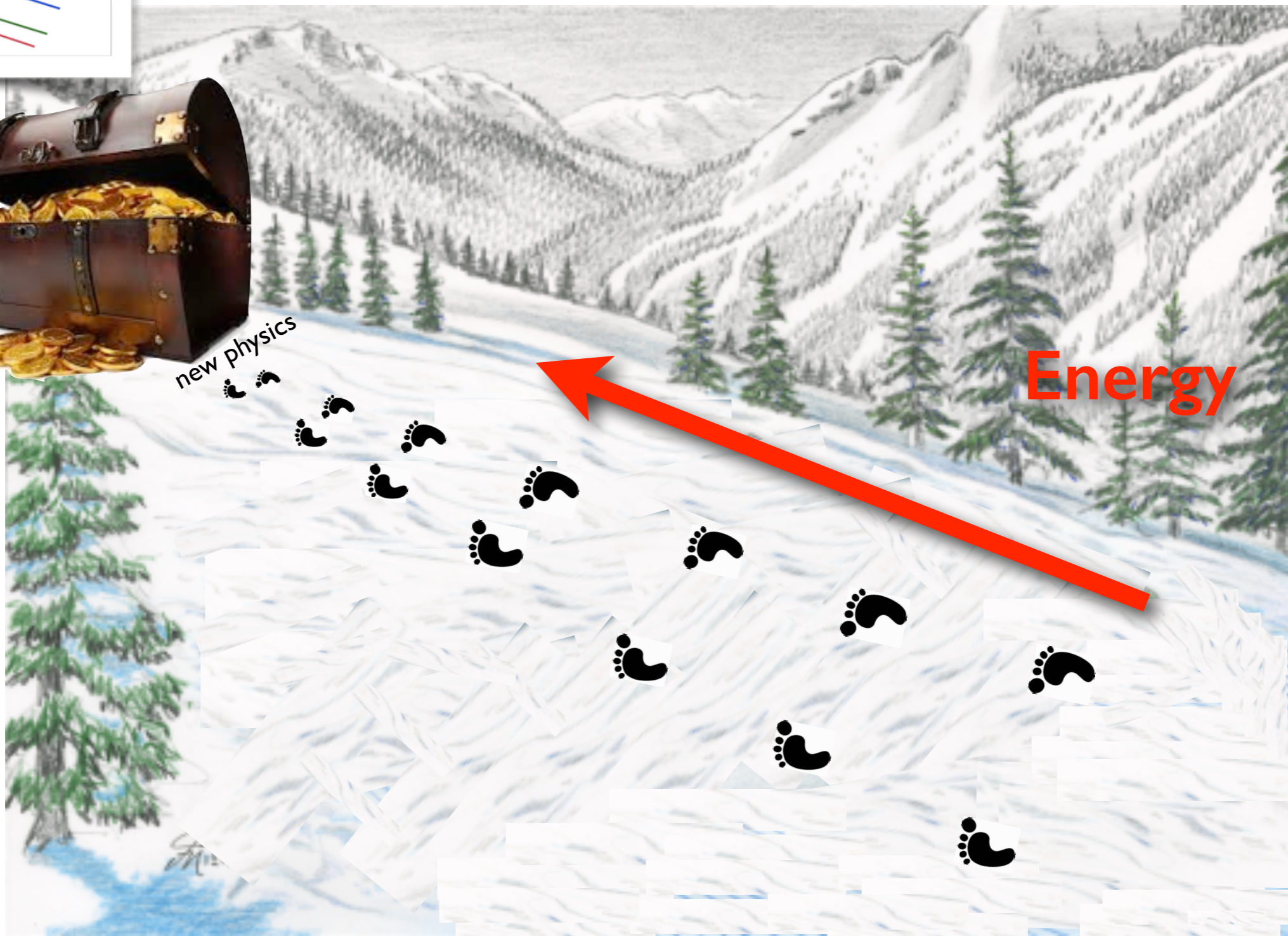
New physics to show
up below this scale

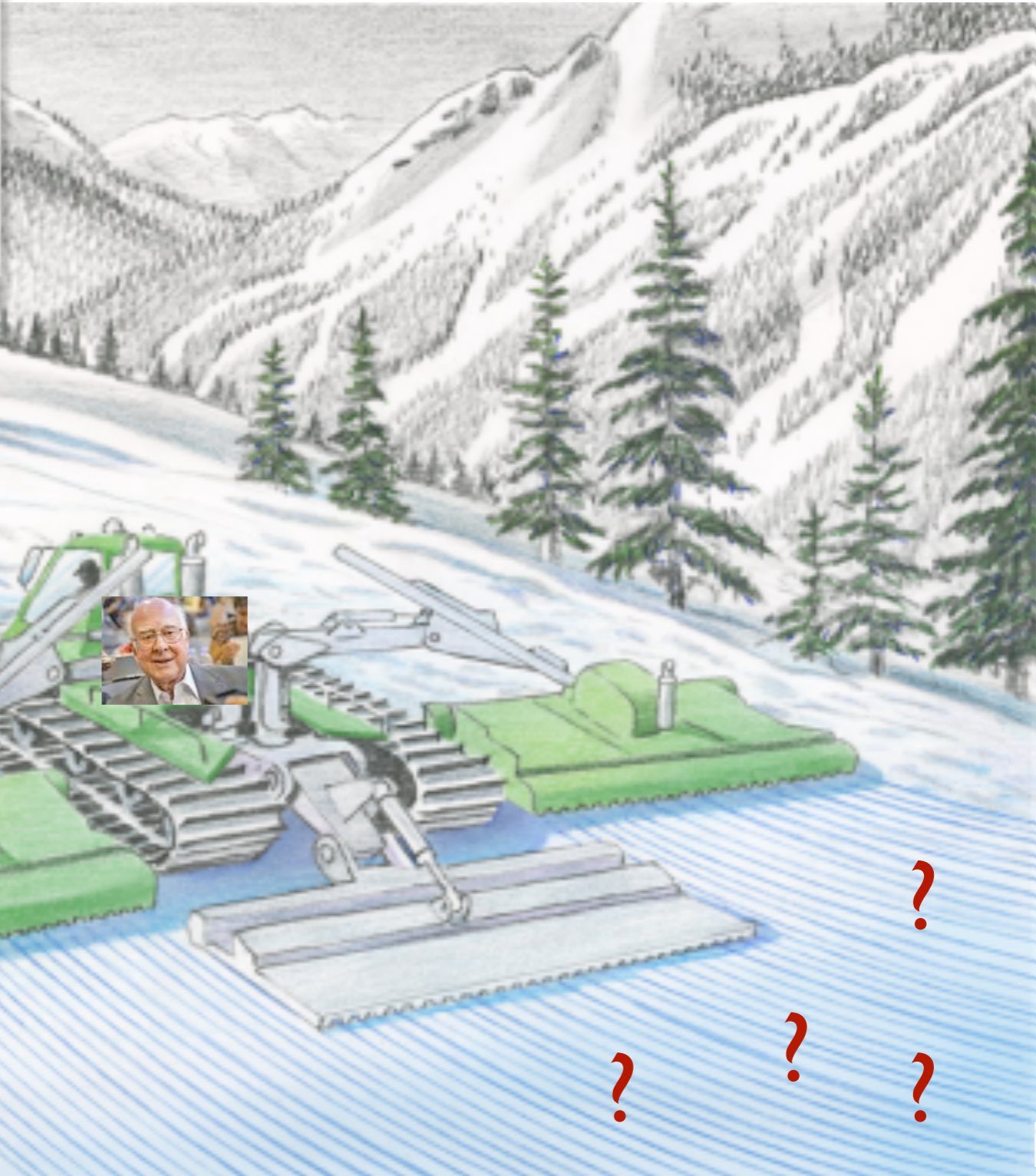
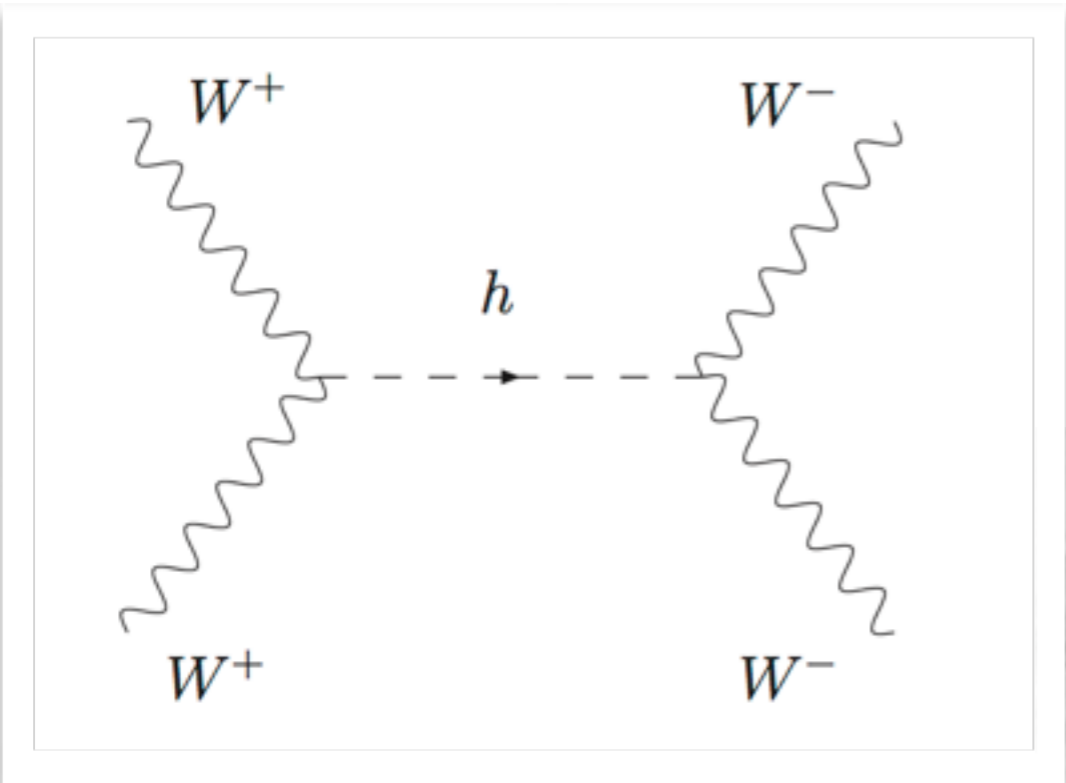


new physics



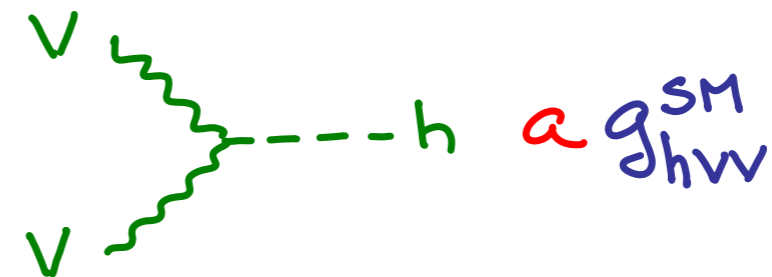
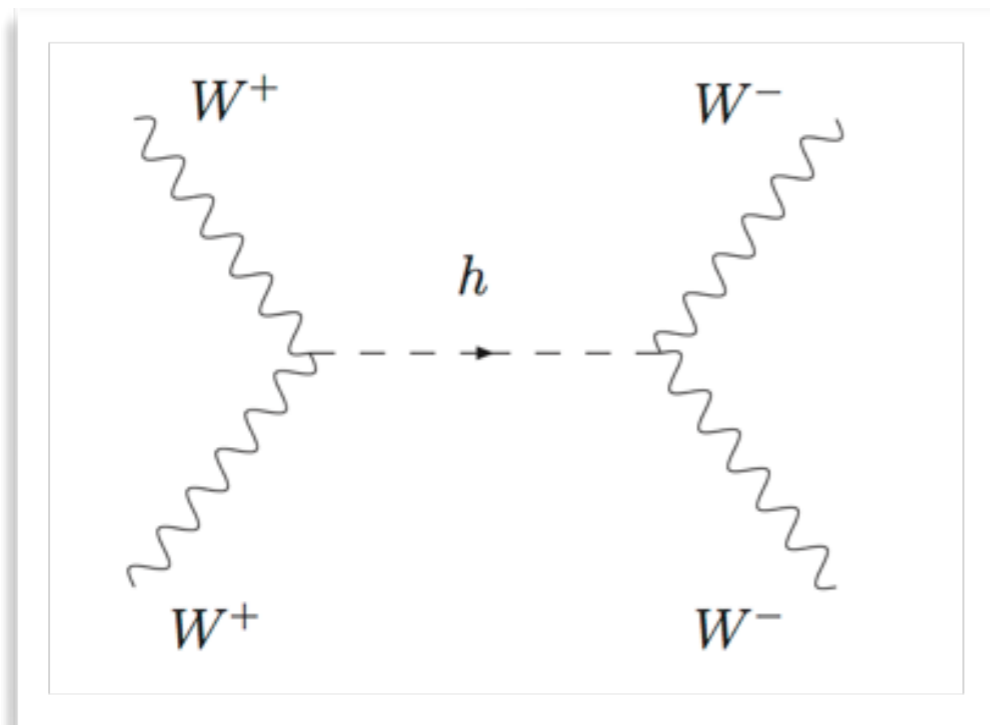
Energy





SM-like Higgs

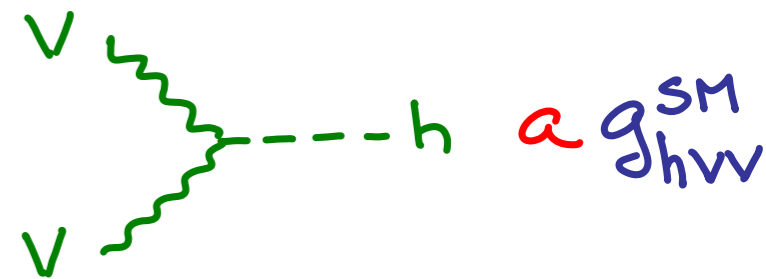
What if it couples only approximately like the SM?



$$\Lambda \approx 4\pi v \longrightarrow \frac{4\pi v}{\sqrt{1 - a^2}}$$

$W_L W_L \rightarrow W_L W_L$
fully unitarized?

$$\Lambda \approx 4\pi v \longrightarrow \frac{4\pi v}{\sqrt{1 - a^2}}$$



Even if we measure $a < 1$, current limits do not guarantee new physics in reach of LHC.

Example: composite pseudo-Goldstone Higgs:

$$a = \sqrt{1 - (v/f)^2} \approx 0.8 \dots 0.9$$

$$\Lambda > 6 \dots 8 \text{ TeV}$$

Where is the next scale?

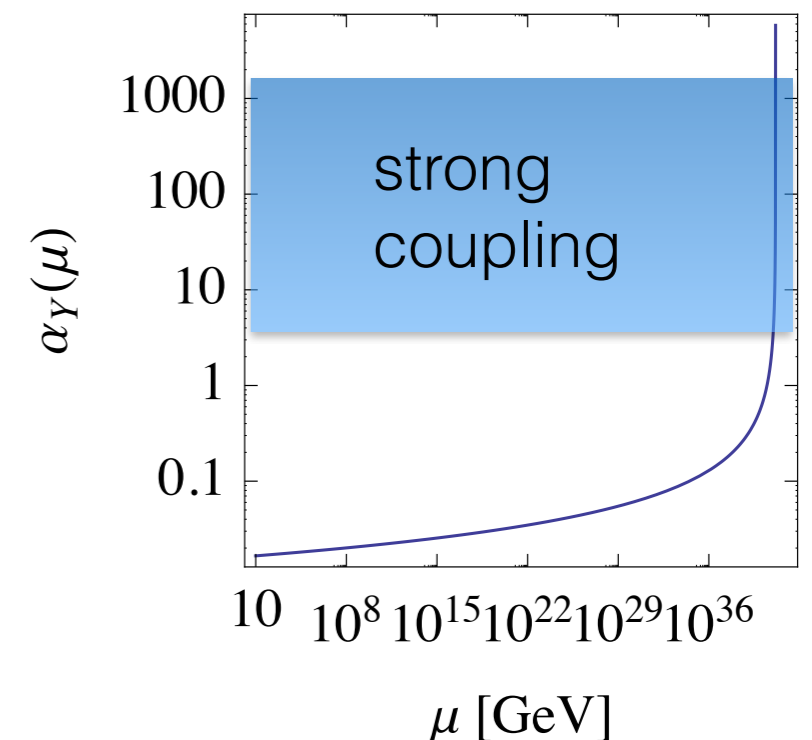
- 13/14 TeV enough to reveal fundamental physics?
- First time in history **without nearby new scale**: all couplings dimensionless (marginal) or of positive mass dimension (relevant)
- Remaining hopes?
 - Landau pole of hyper charge $U(1)_Y$
 - **Gravity** scale (M_{Planck})

SM Hyper-charge

Hyper-charge is **not asymptotically free**, will blow up at (very) high energies — **Landau Pole**

$$1/\alpha_Y(M_Z) = 1/\alpha_Y(\Lambda) + \frac{b_Y}{2\pi} \ln \frac{\Lambda}{M_Z} \quad b_Y = \frac{41}{10}$$

$$\Lambda \sim M_Z e^{2\pi/\alpha_Y b_Y} \sim 10^{41} \text{ GeV}$$



Gravity

- Strong coupling problem, e.g. graviton-graviton scattering

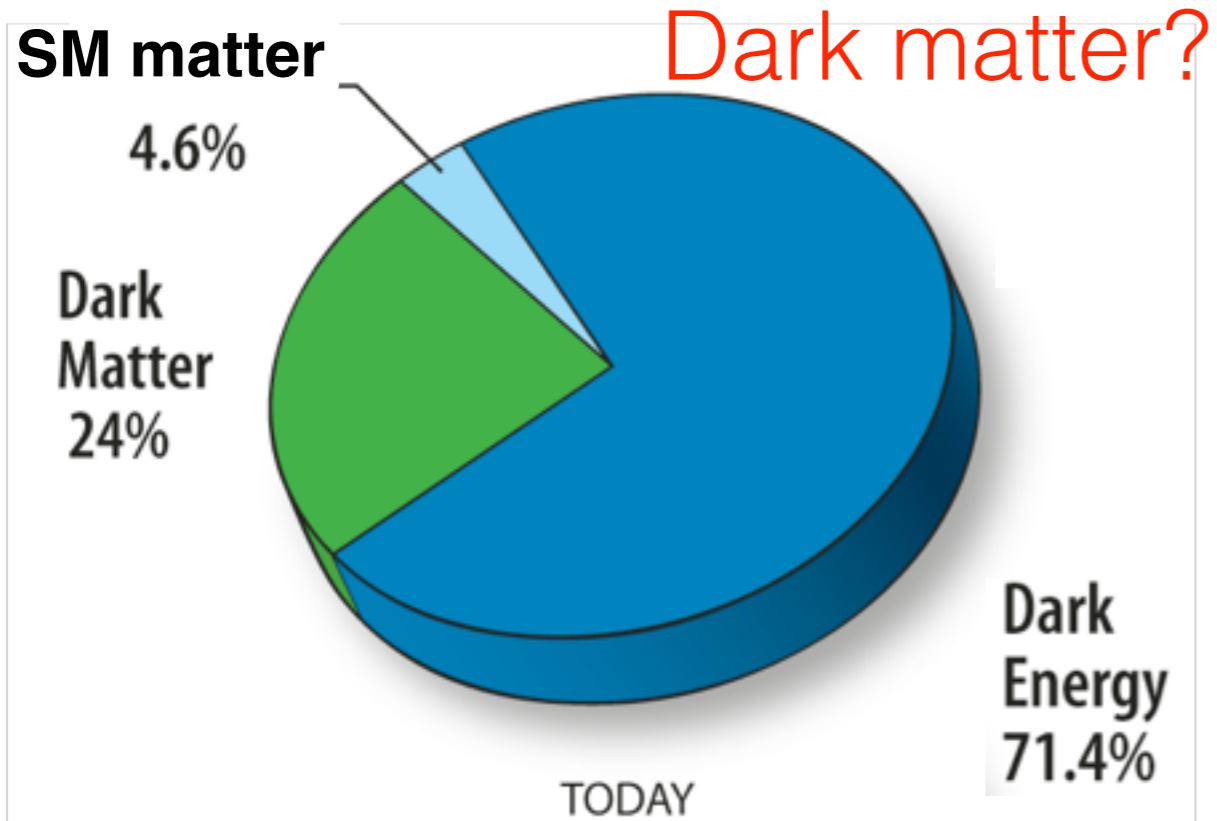
$$\sigma \sim \frac{E^n}{M_{pl}^{n+2}}$$

$$M_{pl} \simeq 10^{19} \text{ GeV}$$

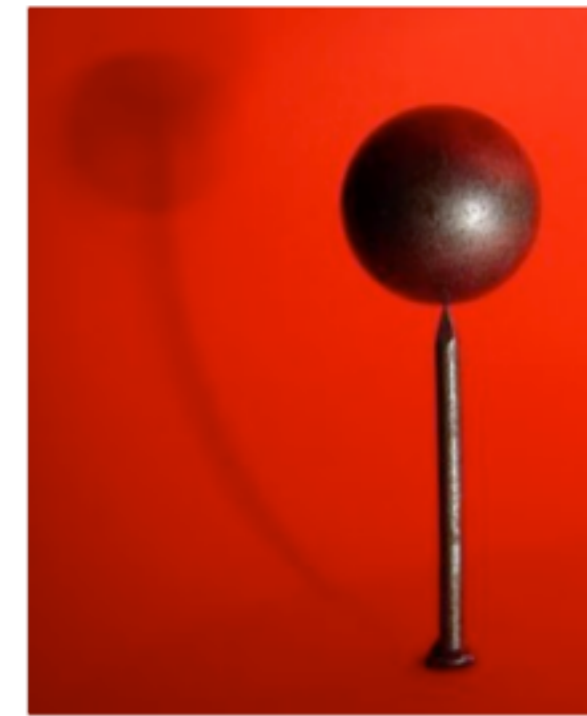
Open questions of the SM



The SM is incomplete



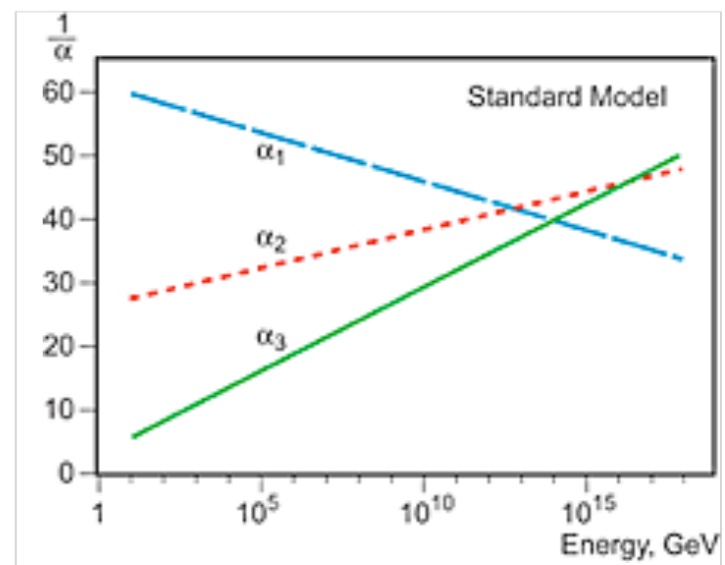
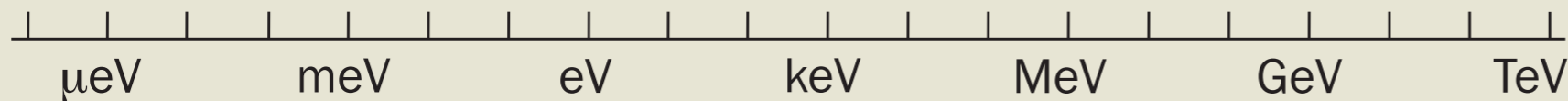
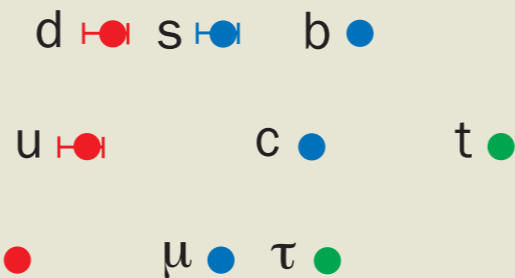
Fine-tuning?



Origin of SM flavor and mass hierarchies?

Unity of forces?

$$Y_U \approx \begin{pmatrix} 10^{-5} & -0.002 & 0.007 + 0.004i \\ 10^{-6} & 0.007 & -0.04 + 0.0008i \\ 10^{-8} + 10^{-7}i & 0.0003 & 0.92 \end{pmatrix}$$

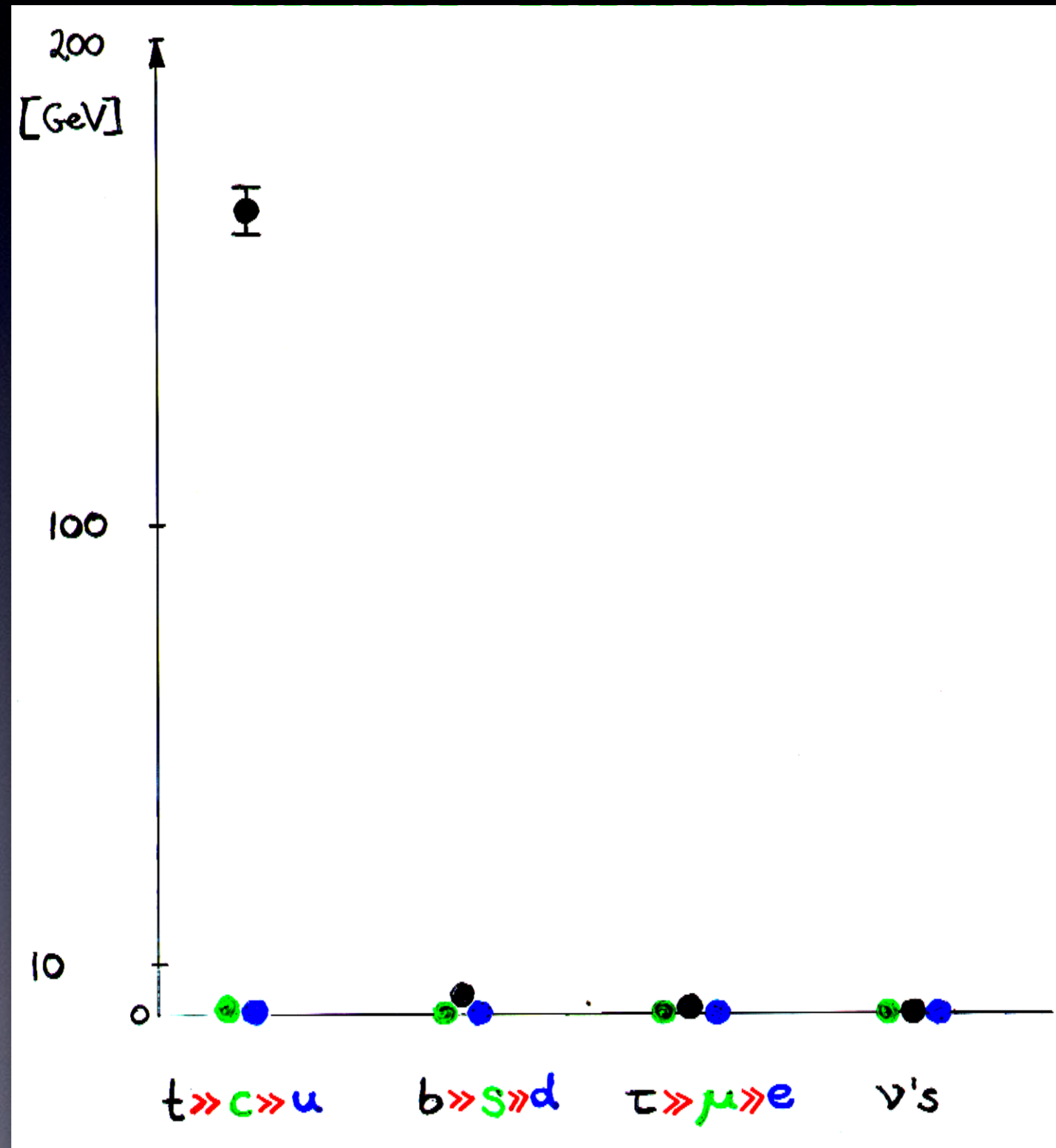


The SM

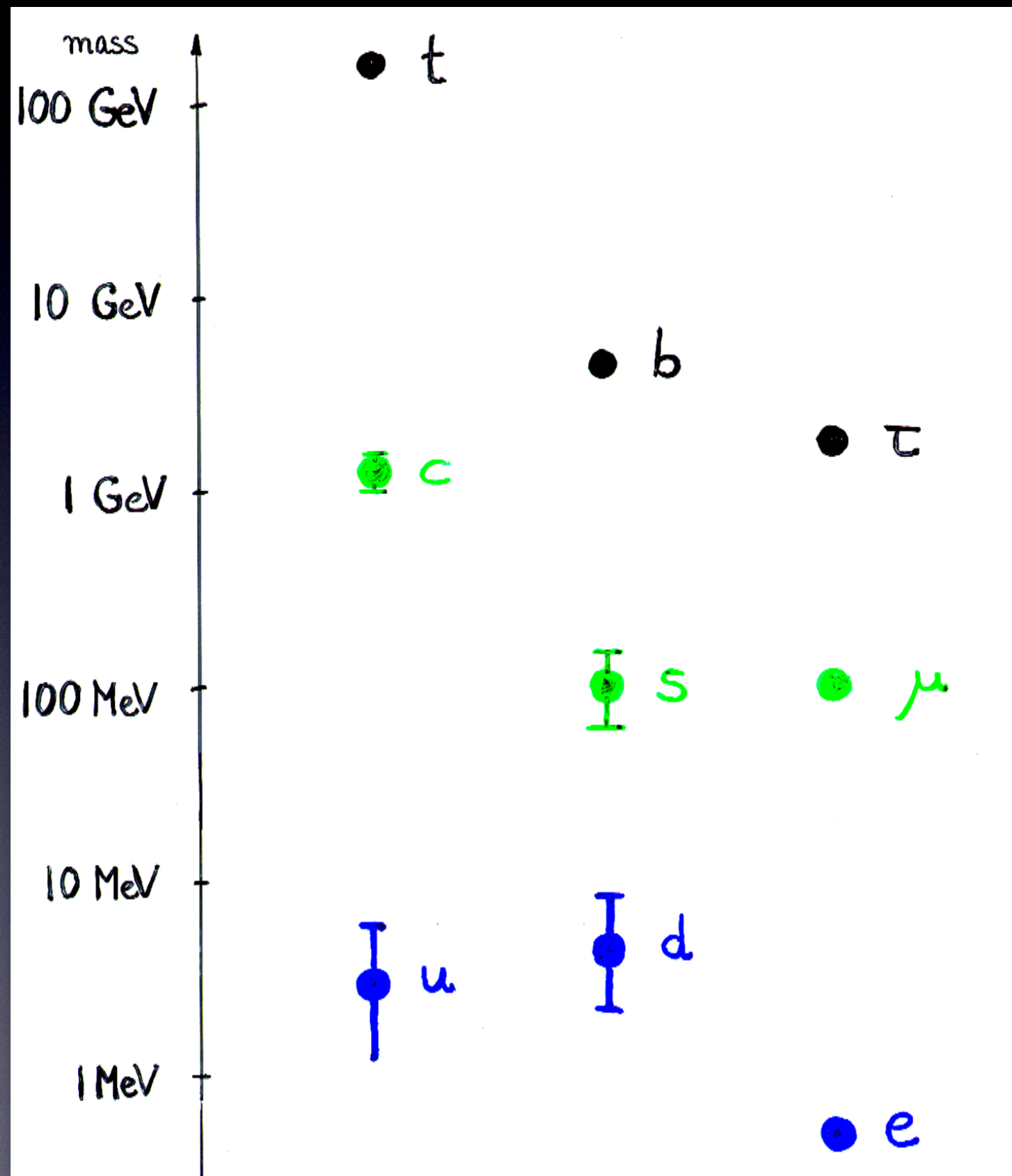
$$\begin{aligned}\mathcal{L} = & -\frac{1}{4} F_{\mu\nu} F^{\mu\nu} \\ & + i\bar{\psi} \not{D} \psi + \text{h.c.} \\ & + \bar{\psi}_i y_{ij} \psi_j \phi + \text{h.c.} \\ & + |D_\mu \phi|^2 - V(\phi)\end{aligned}$$

fermion
masses
& mixings

Quark and Lepton mass hierarchy



Masses on a Log-scale



$$Y_D = (m_d, m_s, m_b)/v$$

$$Y_U = V_{\text{CKM}}^\dagger (m_u, m_c, m_t)/v$$

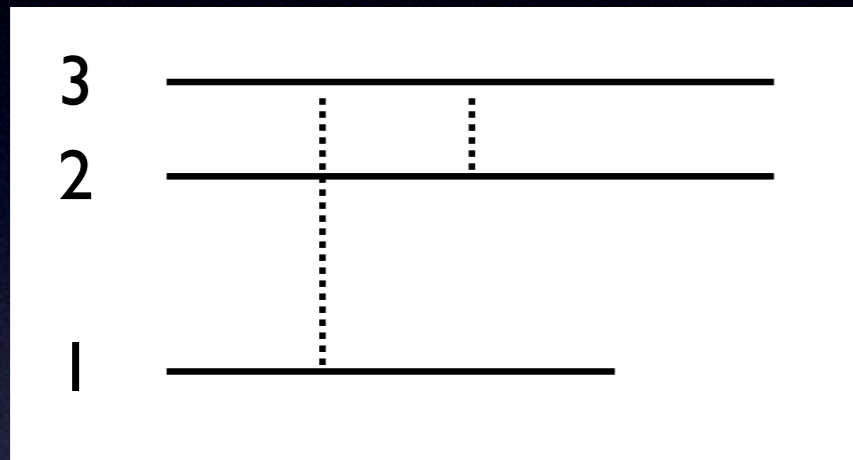
$$Y_D \approx (10^{-5}, 0.0005, 0.026)$$

$$Y_U \approx \begin{pmatrix} 10^{-5} & -0.002 & 0.007 + 0.004i \\ 10^{-6} & 0.007 & -0.04 + 0.0008i \\ 10^{-8} + 10^{-7}i & 0.0003 & 0.96 \end{pmatrix}$$

SM quark masses: mostly **small & hierarchical**.
Origin of this structure?

Compare to: $g_s \sim 1$, $g \sim 0.6$, $g' \sim 0.3$, $\lambda_{\text{Higgs}} \sim 1$

Analog to mysterious spectral lines before QM



$$\nu = \left(\frac{1}{n^2} - \frac{1}{m^2} \right) R$$

Explained by Bohr

$$E_n = -\frac{2\pi^2 e^4 m_e}{h^2 n^2}$$

Is there an analogue to the Bohr atom, we might discover at the LHC?

Flavor dynamics @ LHC ?

Possible, but ...

1) Lack of scale

$$\mathcal{L}_{\text{flavor}} = [Y^U]_{ij} \bar{Q}_i H_c u_j + \dots$$

$$\text{dim} \quad 0 + 3/2 + 1 + 3/2 = 4$$

→ Jernej's lecture

2) Very strong constraints from flavor physics:

Generic flavor dynamics $\gg 100 \text{ TeV}$

TeV? 10^3 TeV ? 10^{16} GeV ?

The SM

$$\begin{aligned}\mathcal{L} = & -\frac{1}{4} F_{\mu\nu} F^{\mu\nu} \\ & + i\bar{\psi} \not{D} \psi + \text{h.c.} \\ & + \sum_i \bar{\psi}_i \gamma_{ij} \psi_j \phi + \text{h.c.} \\ & + |D_\mu \phi|^2 - V(\phi)\end{aligned}$$

Higgs
potential

Top as a destabilizing
agent

Stability and meta-stability

Cabibbo, Maiani, Parisi, Petronzio, '79;
Hung '79; Lindner 86; Sher '89; ...

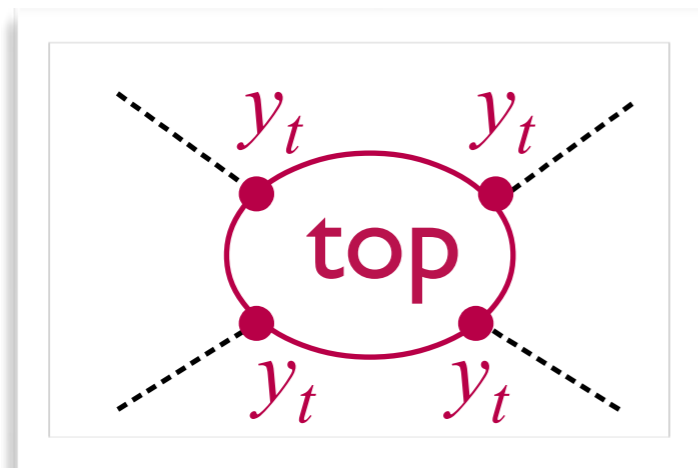
Tree-level

$$V(\phi) = -\mu^2 |\phi|^2 + \lambda |\phi|^4$$

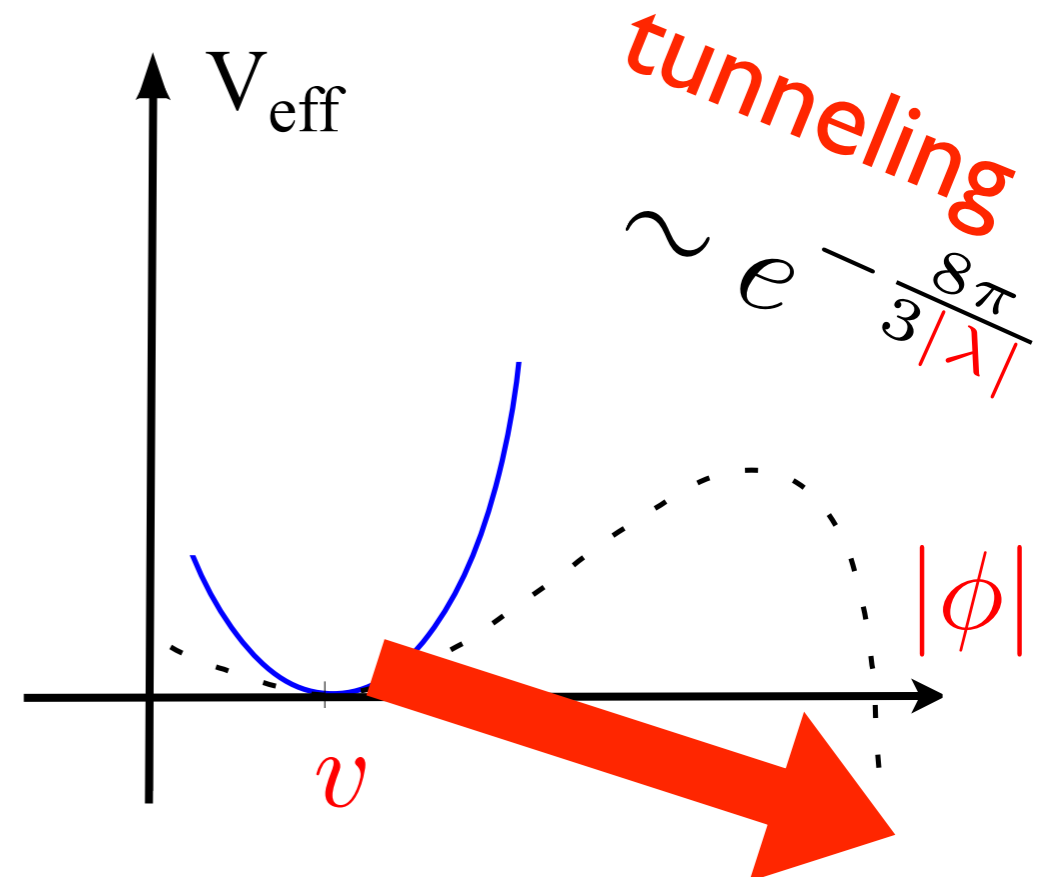
What happens at $|\phi| \gg v$? Focus on λ , $\mu^2 \ll |\phi|^2$

Quantum fluctuations change potential

$$V \simeq \lambda(|\phi|) |\phi|^4$$



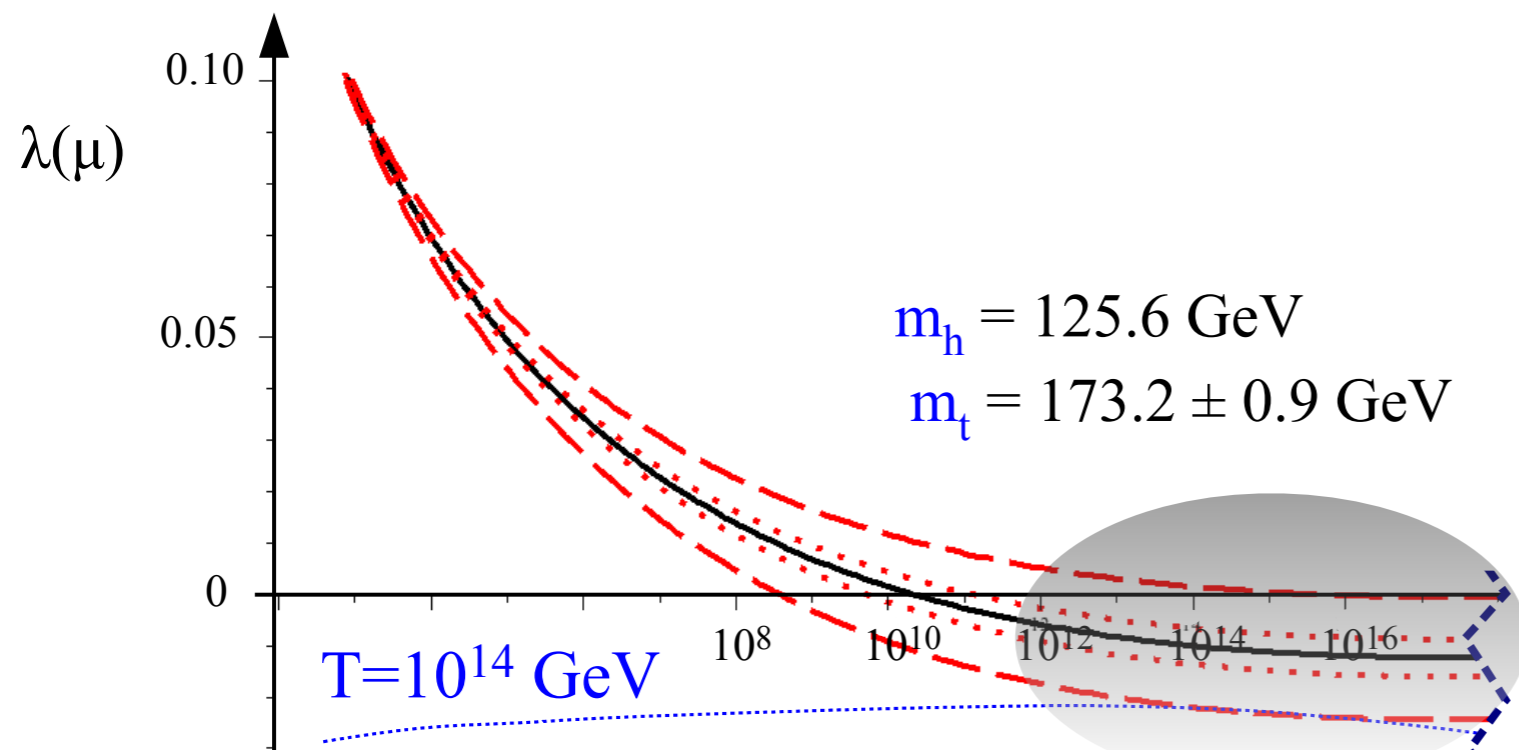
decreasing
at large
Energies
 \Rightarrow



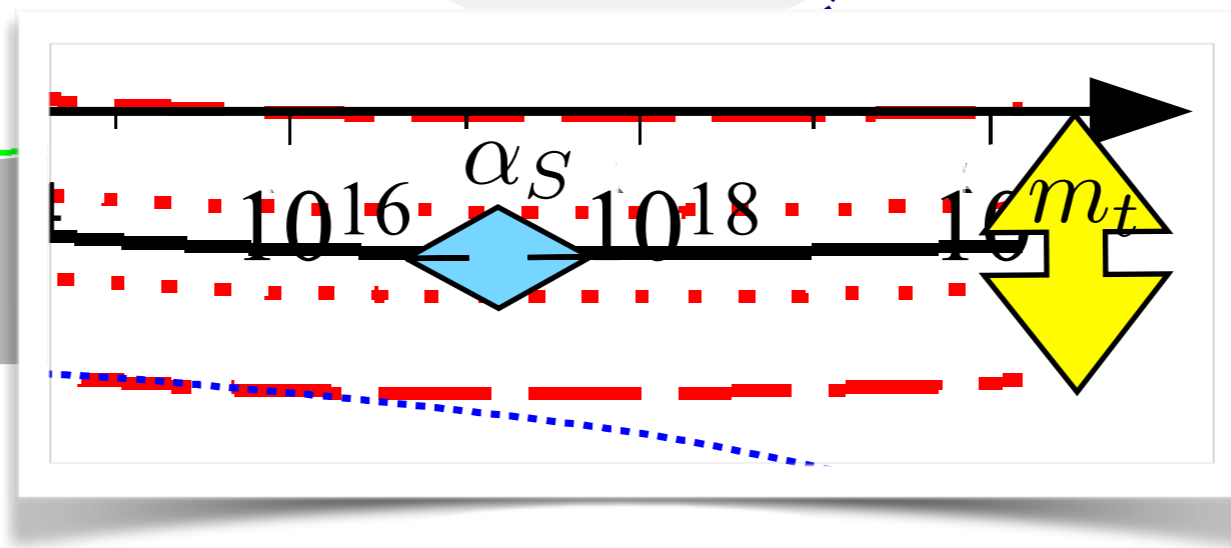
Stability and meta-stability

SM vacuum is **unstable but sufficiently long-lived**,
 (depends on m_{top} , m_{Higgs})

cf Elias-Miro et al. '12
 Degraasi et al. '12
 Buttazzo et al. '12

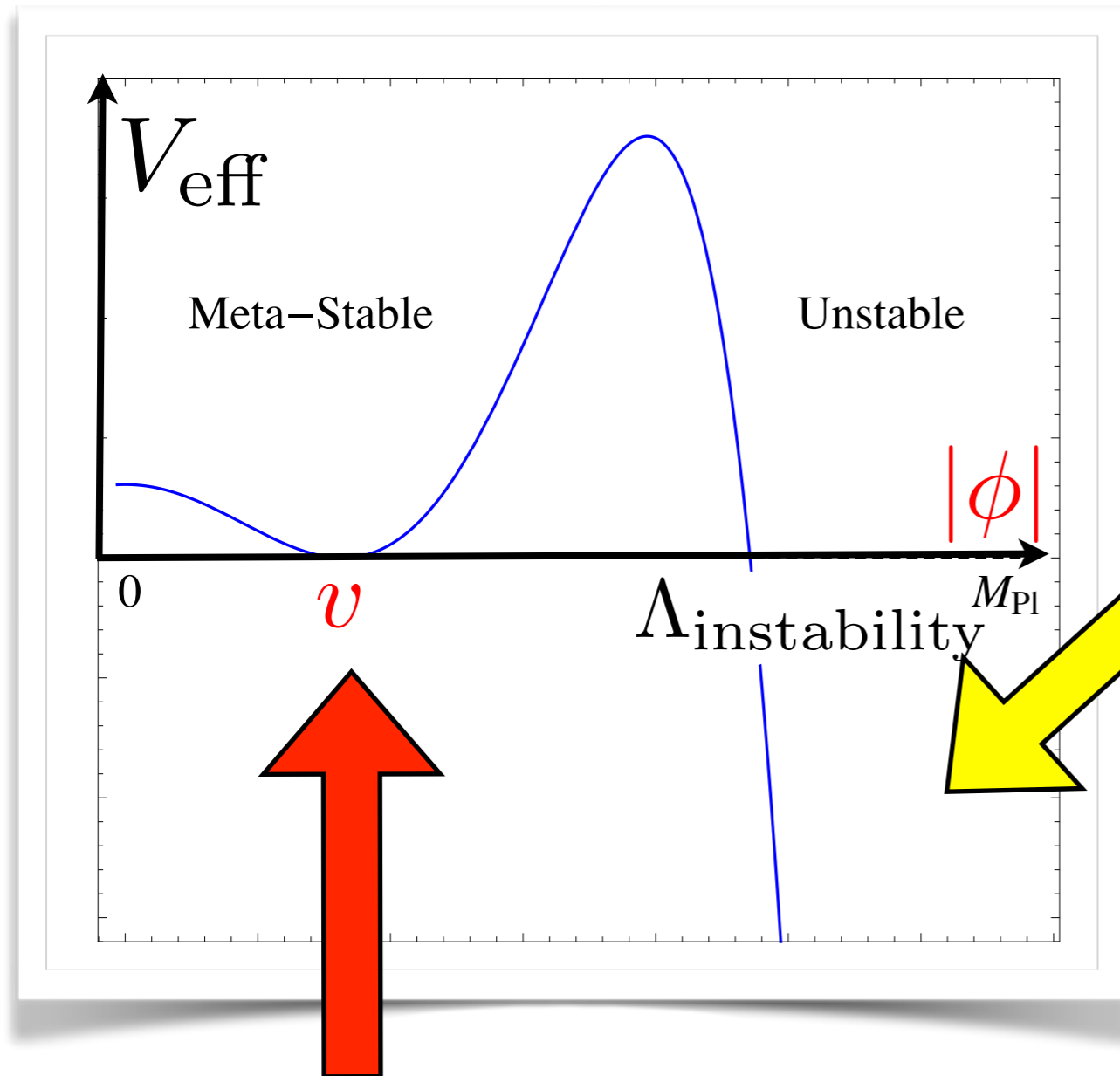


Unlikely the full story,
 assumes nothing but
 SM up to the Planck
 scale ...



decisive
 uncertainty
 m_{top}

If metastable: How did we end up in the energetically disfavoured vacuum?



Universe is overwhelmingly likely to evolve to wrong minimum

Fine-tuning of initial conditions?

$$\sim \Lambda_{\text{instability}} / M_{\text{Planck}}$$

You are here?!

For $\Lambda_{\text{instability}} \sim 10^{10} \text{ GeV} \rightarrow 10^{-8}$ tuning

Higgs potential

$$V(\phi) = -\mu^2|\phi|^2 + \lambda|\phi|^4$$

quantum fluctuations

destabilise Higgs mass²

Effective Field Theory

An approximate field theory which works up to a certain energy scale (Λ), using only degrees of freedom with $m \ll \Lambda$.

Example: QED (e, γ), for $E \ll M_W$

Is the SM an EFT?

Yes! Breaks down latest at the gravity scale (details unknown).

Principle: UV insensitivity

Naturalness : absence of special conspiracies between phenomena occurring at very different length scales.



Planets do not care about QED.



QED at $E \sim m_e$ does not care about the Higgs.

Hierarchy problem

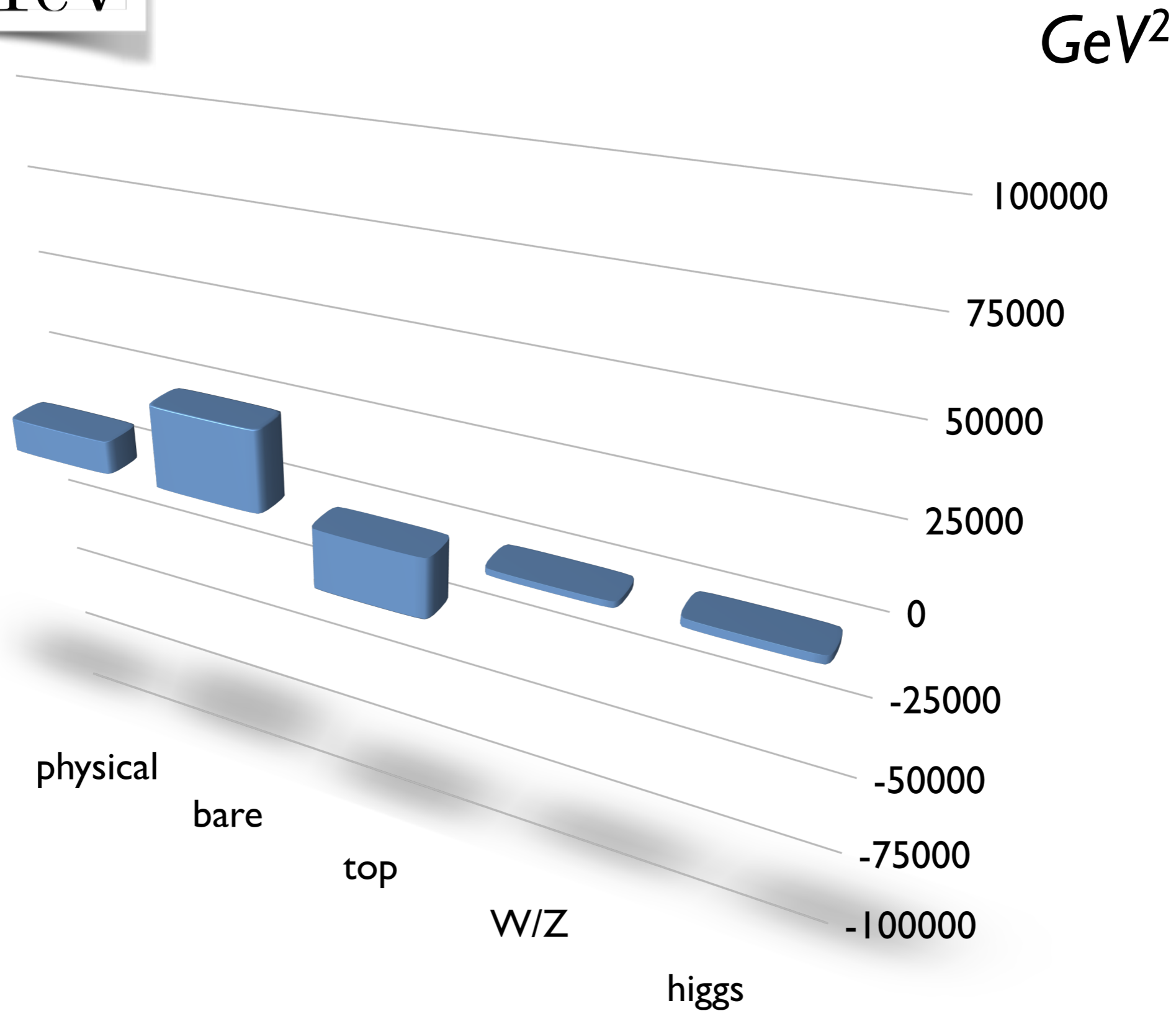
- Higgs mass sensitive to thresholds (GUT, gravity)
- Enormous quantum corrections $\mathcal{O}(\text{highest scale})$ exceed Higgs mass physical value, need to **fine-tune** parameters

The diagram shows the Higgs mass correction structure. It starts with a dashed line representing the bare Higgs mass, which has a cross through it. This is followed by a plus sign and three loop diagrams: a top quark loop (circle labeled 'top'), a W/Z/gamma loop (cloud labeled 'W,Z,γ'), and a Higgs loop (dashed circle labeled 'higgs'). Below each diagram is its corresponding mathematical expression.

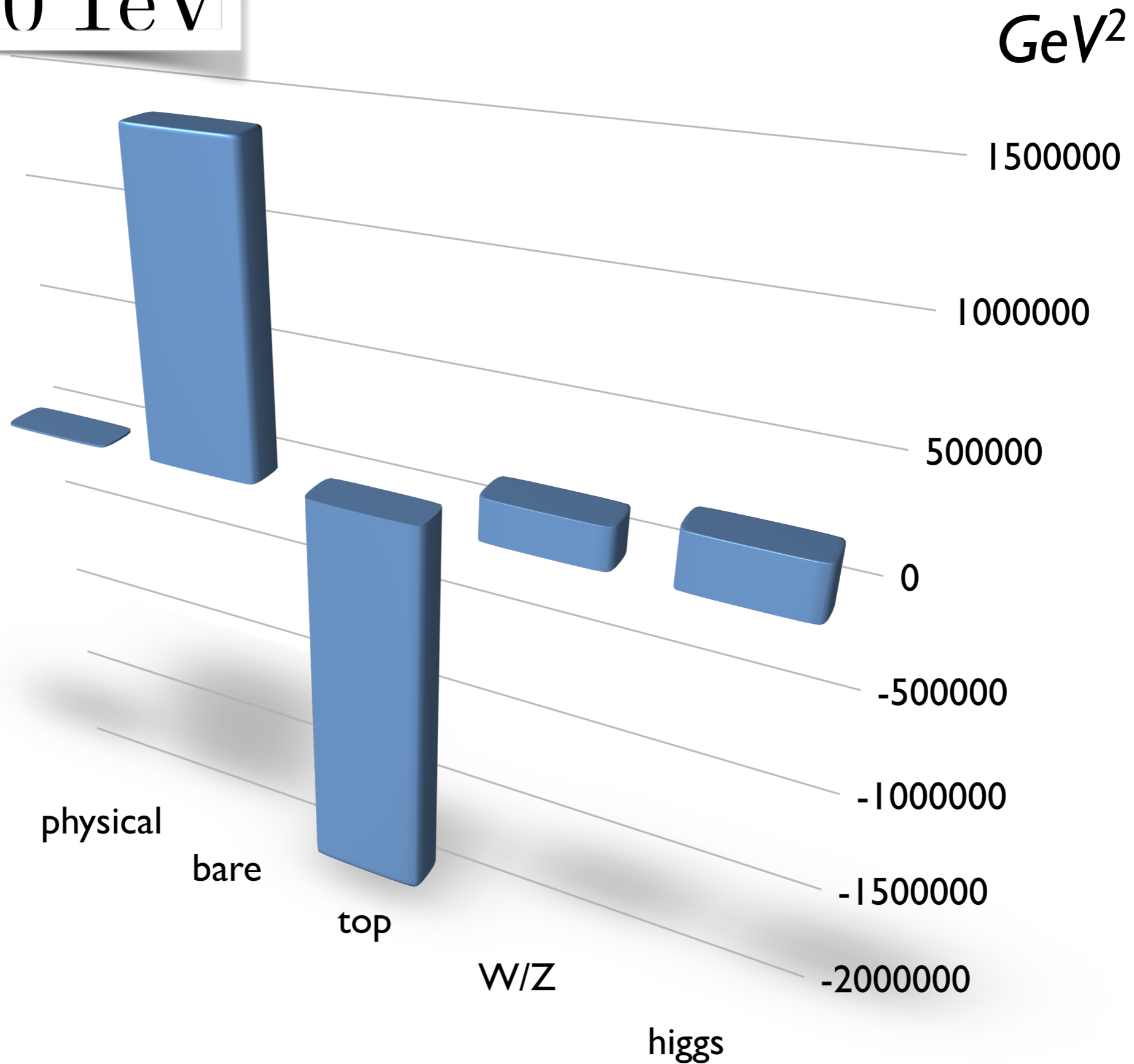
$$\begin{array}{c}
 \text{---} \times \text{---} + \text{---} \text{---} \text{---} \text{---} + \text{---} \text{---} \text{---} \text{---} + \text{---} \text{---} \text{---} \text{---} \\
 \text{bare} \qquad \text{top} \qquad \text{W,Z,}\gamma \qquad \text{higgs} \\
 \\
 -\frac{3}{8\pi^2} \lambda_t^2 \Lambda^2 \qquad \frac{9}{64\pi^2} g^2 \Lambda^2 \qquad \frac{1}{16\pi^2} \lambda^2 \Lambda^2
 \end{array}$$

$$m_h^2(\text{physical}) = m_h^2(\text{bare}) + \sum_i a_i \Lambda^2$$

$\Lambda = 1 \text{ TeV}$

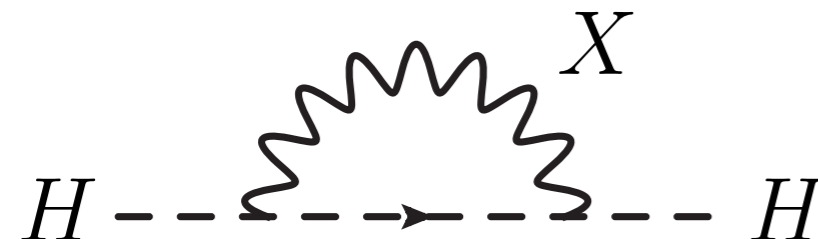


$$\Lambda = 10 \text{ TeV}$$



Comments

- The ‘**cancelation of divergencies**’ is not the question
- Rather: parameters in the **effective** theory are strongly **sensitive to fundamental** ones

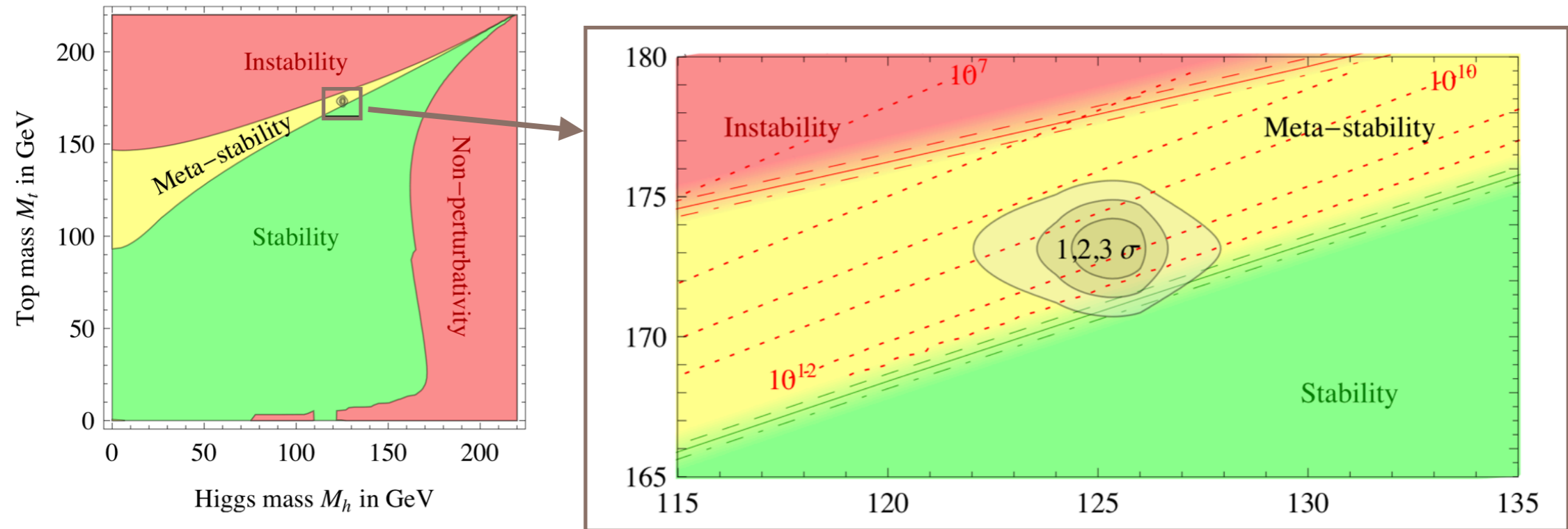


The diagram shows two external dashed lines labeled 'H' connected by a loop of a particle labeled 'X'. The loop is represented by a wavy line with a zigzag pattern. An arrow on the loop points clockwise.

$$\Rightarrow \Delta m_H^2 \sim \frac{g_{\text{GUT}}^2}{16\pi^2} M_X^2 \sim (10^{15} \text{ GeV})^2 \quad \text{e.g. GUT}$$

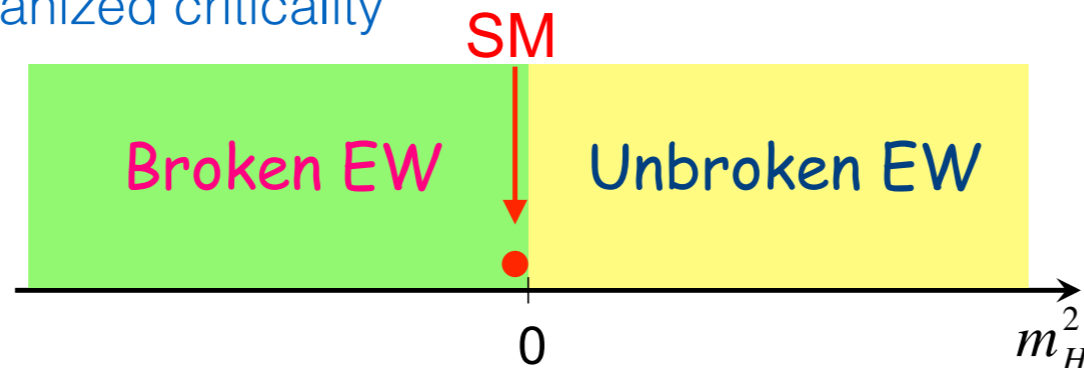
- The hierarchy problem needs a ‘hierarchy of scales’. The SM alone (no gravity, nothing else) if fine → **no hierarchy, no problem!**

Only the SM?



We seem to be living close to a critical condition, similar to Planck-Weak hierarchy ...

Giudice, Rattazzi, 'Self-organized criticality'

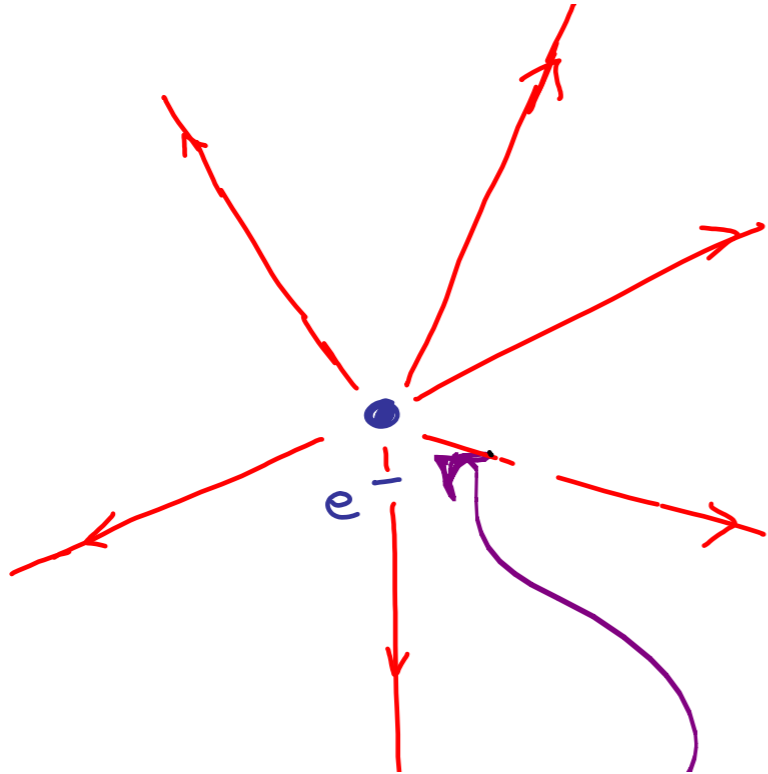


Fine-tuning not an inconsistency of physics since we can always cancel bare vs. quantum. However, it might help us understand where new physics could set in.



Example: Electron Mass

Ex I : divergent self energy of electric field



New physics expected
at

$$\Lambda \sim m_e/\alpha$$

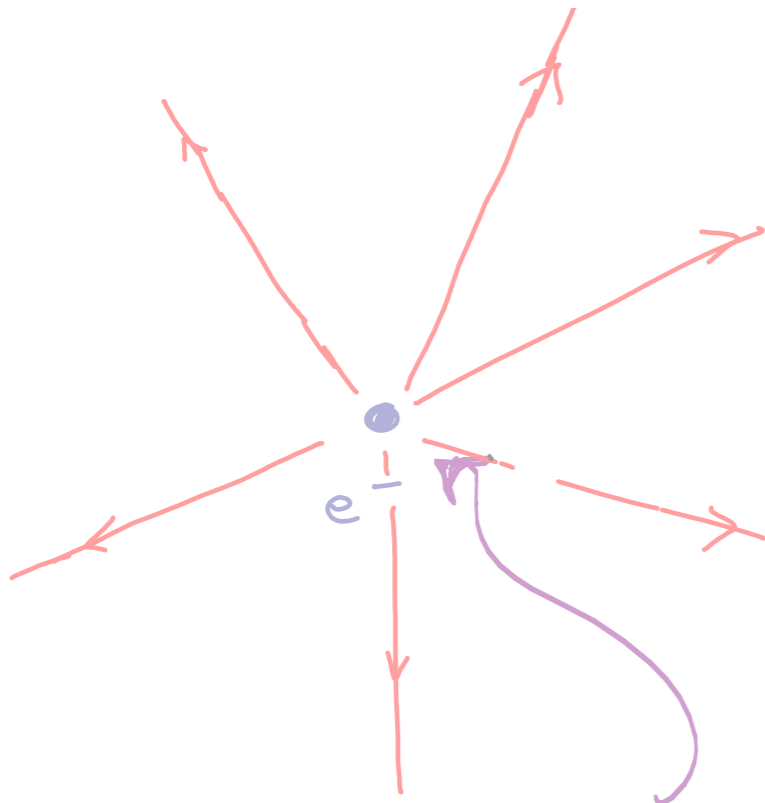
Classically:

$$\int_{r=\Lambda^{-1}} d^3r \vec{E}^2 \simeq \alpha\Lambda \quad \text{vs.} \quad m_e$$

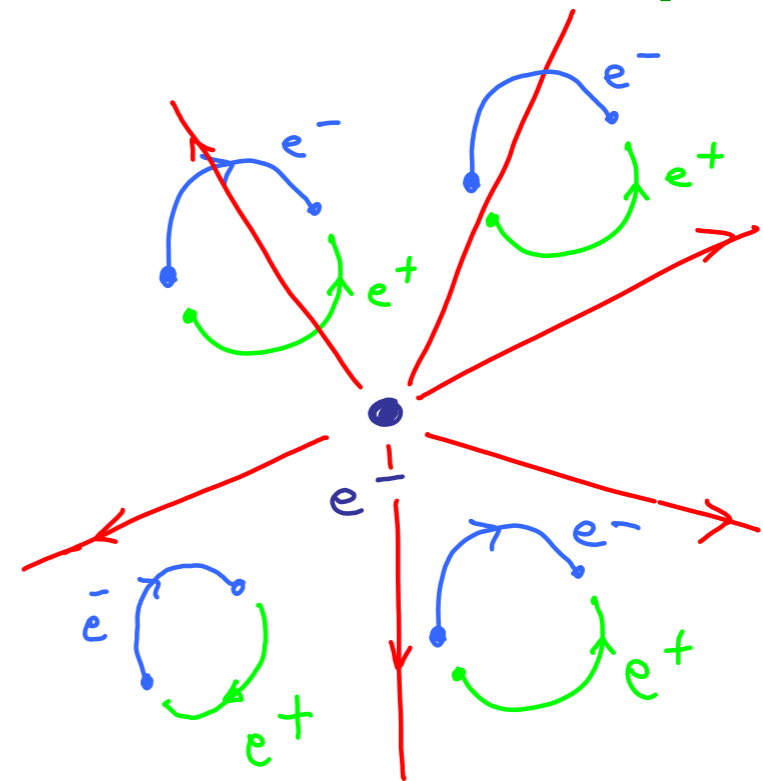
$$\vec{E} \sim \vec{n}/r^2 \quad \text{Coulomb}$$

Electron Mass

Ex I : divergent energy of electric field



+positron



Classically:

$$\int_{r=\Lambda^{-1}} d^3 r \vec{E}^2 \simeq \alpha \Lambda$$

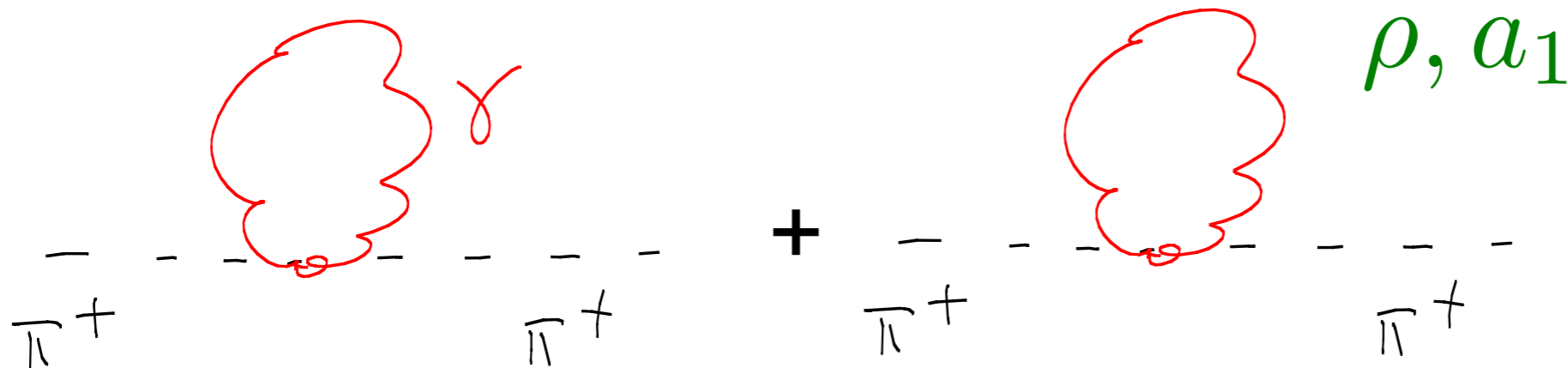
Extend space-time symmetry, relativity + QM: predict positron

$$\delta m_e \simeq \frac{\alpha}{\pi} m_e \log \left(\frac{\Lambda}{m_e} \right)$$

→ natural electron mass.

Another example: Pion mass

Ex2 Neutral-charged pion mass difference



$$\delta m_{\pi^+}^2 \sim \frac{3\alpha}{4\pi} \Lambda^2 < (m_{\pi^+}^2 - m_{\pi^0}^2)_{\text{exp}} \approx (4 \text{ MeV})^2$$

Expect $\rightarrow \Lambda < 850 \text{ MeV}$

‘New physics’: comes in at $m_\rho = 770 \text{ MeV}$

$$m_{\pi^\pm}^2 - m_{\pi^0}^2 \simeq \frac{3\alpha_{em}}{4\pi} \frac{m_\rho^2 m_{a_1}^2}{m_{a_1}^2 - m_\rho^2} \log \left(\frac{m_{a_1}^2}{m_\rho^2} \right)$$

Das et al '67

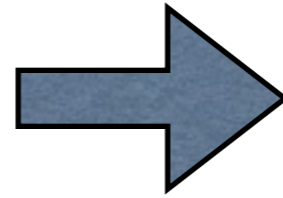
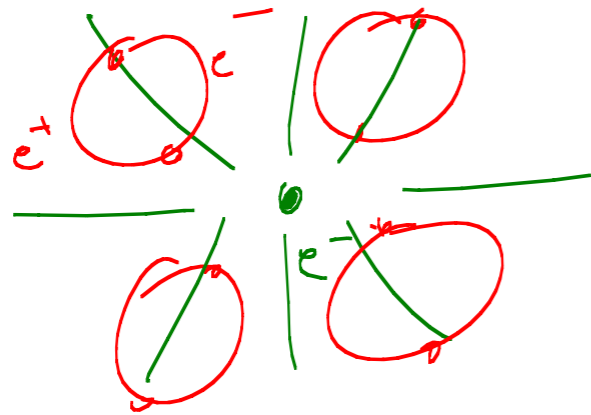
$$(m_{\pi^\pm} - m_{\pi^0})|_{\text{TH}} \simeq 5.8 \text{ MeV} !$$

Famous naturalness disaster

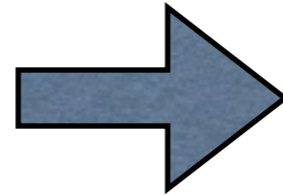
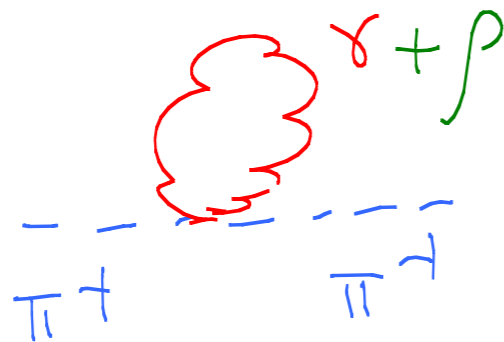
- We don't understand the cosmological constant $CC = \Lambda_0 \approx (10^{-3} \text{ eV})^4$

$$S = \frac{1}{16\pi G} \int d^4x \sqrt{-g} (R - \Lambda_0)$$

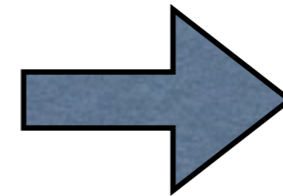
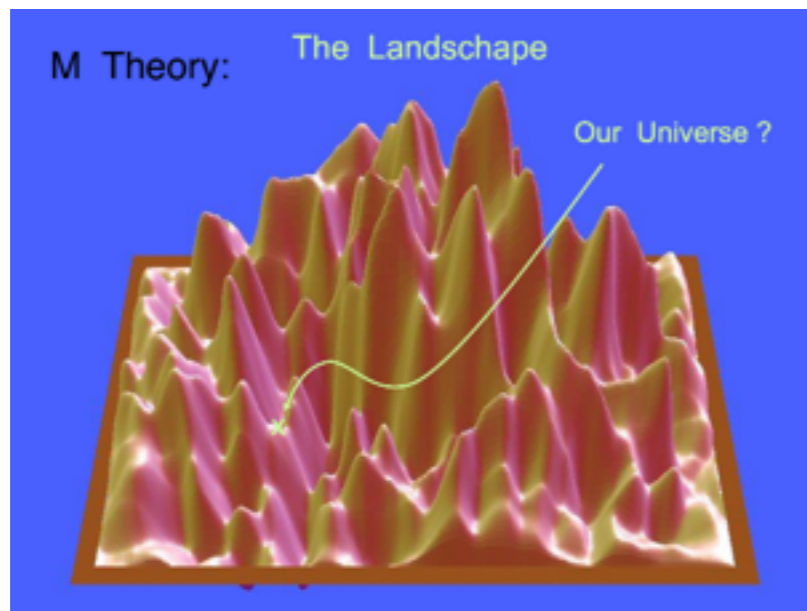
$\delta\Lambda_0 \approx \Lambda^4 \rightarrow$ new physics at 10^{-3} eV or
 \sim few mm !?!



Supersymmetry
(new space-time
symmetry)



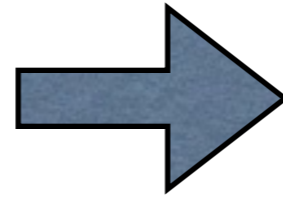
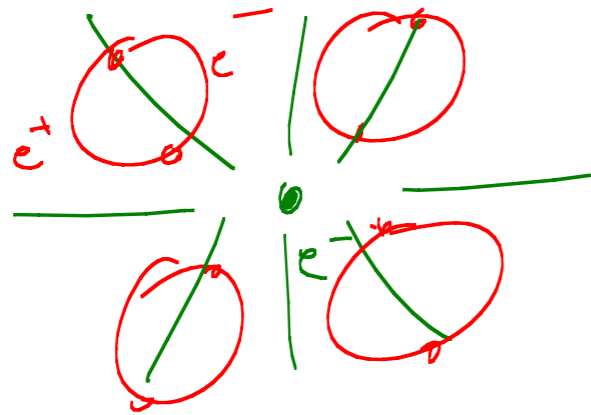
Composite Higgs



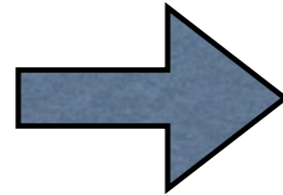
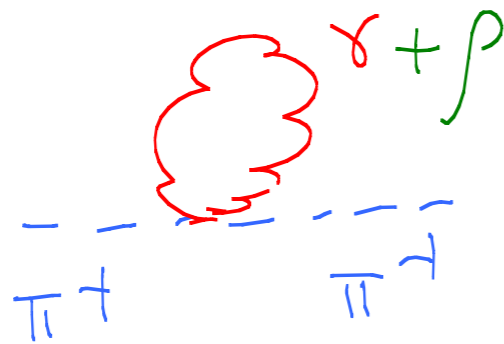
Multiverse

anthropic principle?

-> Yael's lectures

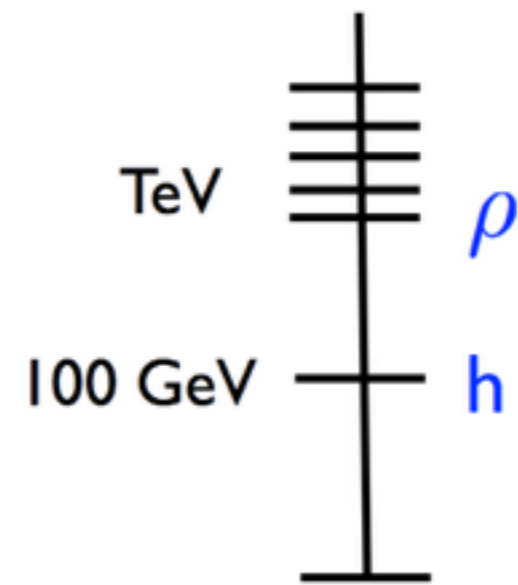
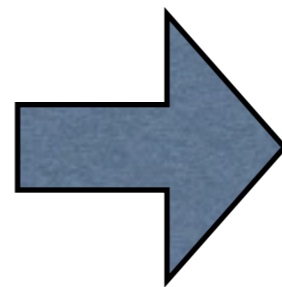
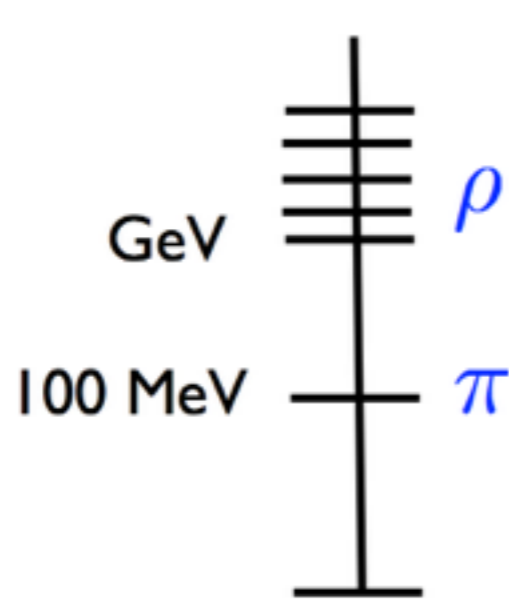


Supersymmetry
(new space-time symmetry)



Composite Higgs

Strong EWSB (Composite Higgs)



QCD

Higgs as a pGB

Why is the Higgs light?

Kaplan; Agashe et. al

Inspired by QCD: (pseudo) scalar pion is the lightest state

Shift symmetry...

$$\pi \rightarrow \pi + c$$

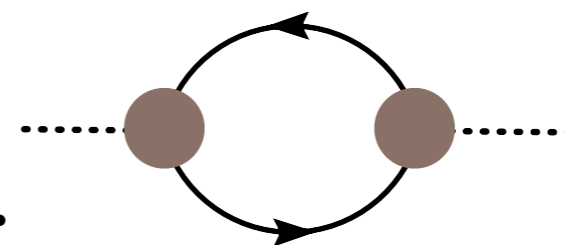
... protects its mass.

Interactions are perturbative for $E \ll 4\pi f$

No pure composite effects due to Goldstone symmetry


$$= 0$$

Shift symmetry broken by elementary-composite couplings:



$$m_h^2 \sim \frac{\lambda^2}{16\pi^2} \Lambda_{comp}^2$$

$$\lambda \ll 4\pi$$

Supersymmetry is a **weakly coupled** solution to the hierarchy problem. We can extrapolate physics to the Planck scale, complete the MSSM in a GUT.

There is another way and it's already in use. Nature already employs a **strongly coupled** mechanism to explain why

$$\Lambda_{\text{QCD}} \ll M_{\text{Planck}}$$
$$\sim 1 \text{ GeV} \quad 10^{19} \text{ GeV}$$

QCD



David J. Gross



H. David Politzer



Frank Wilczek

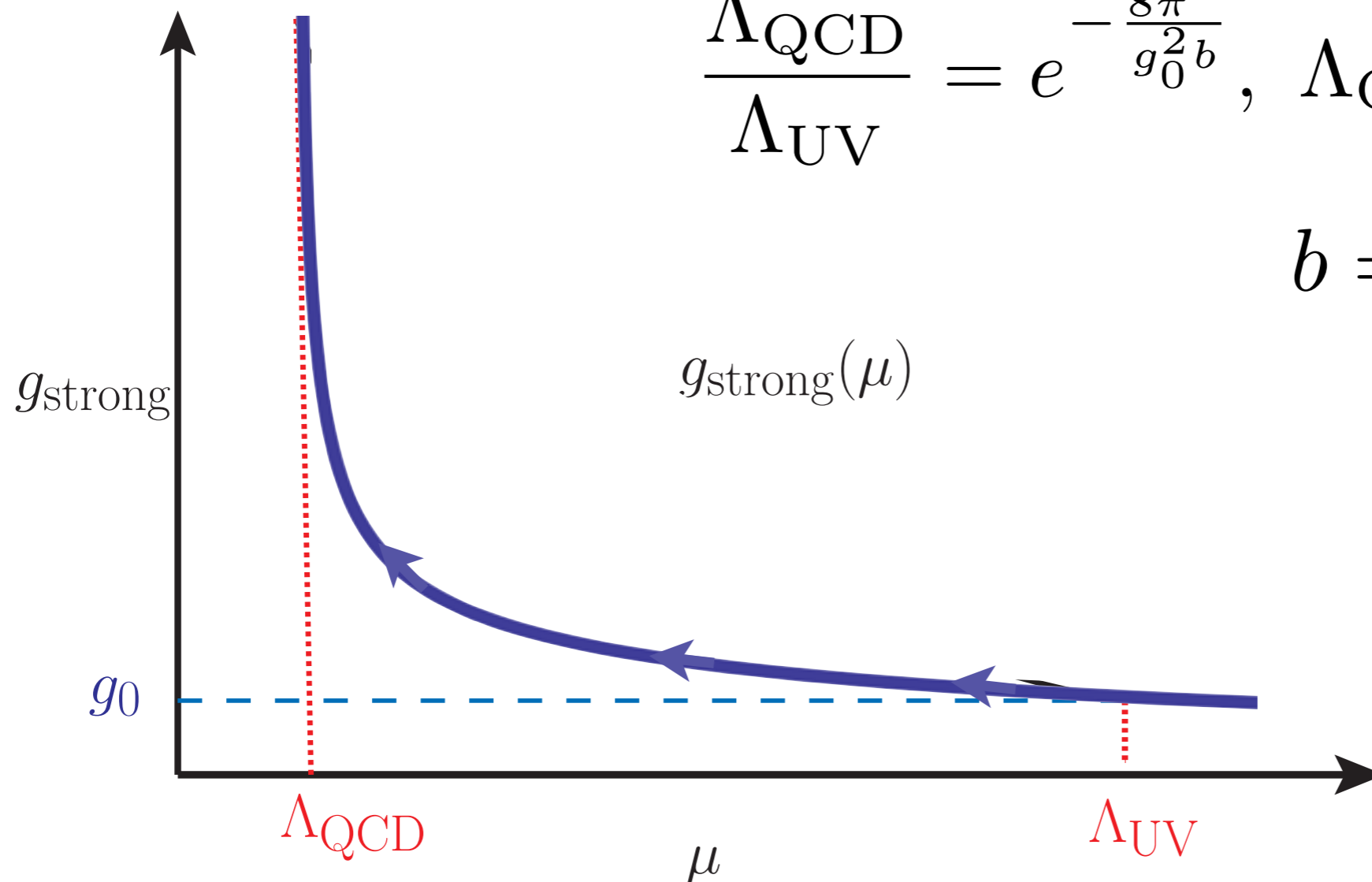
Fix QCD coupling at some high scale

→ exponential hierarchy generated dynamically



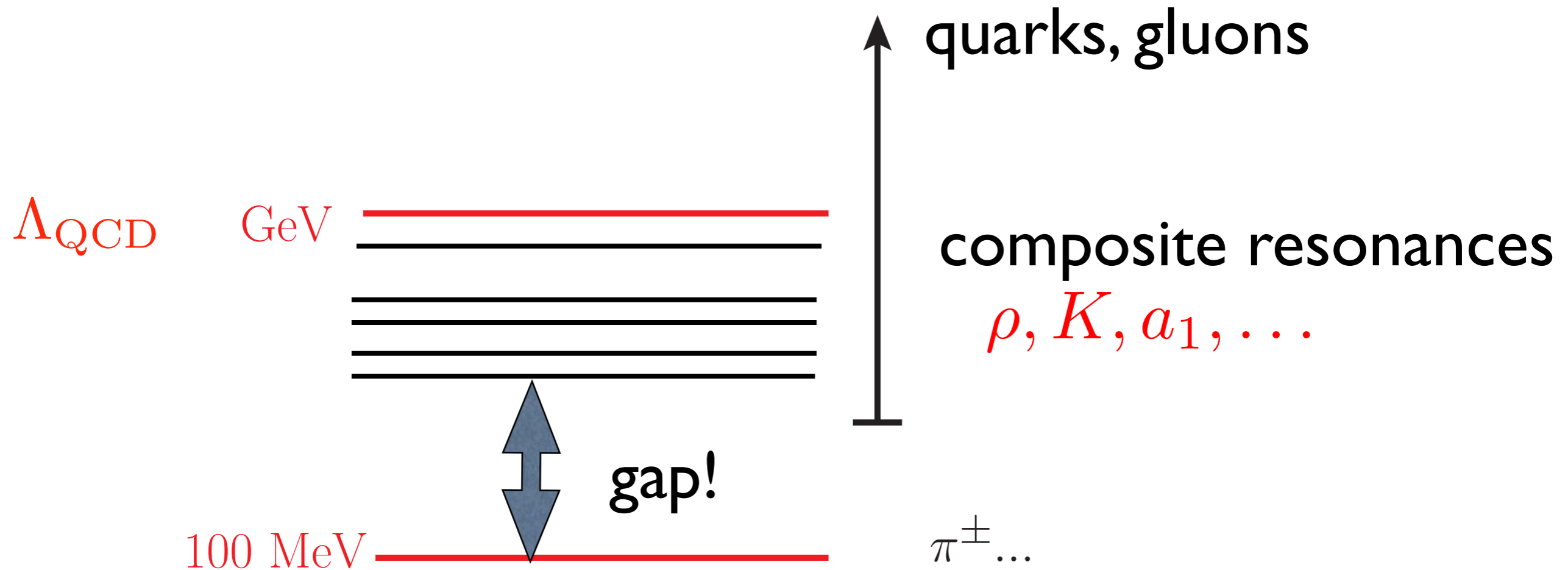
$$\frac{\Lambda_{\text{QCD}}}{\Lambda_{\text{UV}}} = e^{-\frac{8\pi^2}{g_0^2 b}}, \quad \Lambda_{\text{QCD}} \leq \text{GeV}$$

$$b = 7$$



Asymptotic
freedom

QCD: composite bound states



At strong coupling, new resonances are generated

QCD vs. EWSB

QCD dynamically breaks SM gauge symmetry

$$SU(2)_L \times SU(2)_R \rightarrow SU(2)_V$$

$$\langle \bar{q}_L q_R \rangle \simeq \Lambda_{\text{QCD}}^3 \sim (\text{GeV})^3$$

The QCD masses of W/Z are small

$$m_{W,Z} \sim \frac{g}{4\pi} \Lambda_{\text{QCD}} \sim 100 \text{ MeV}$$

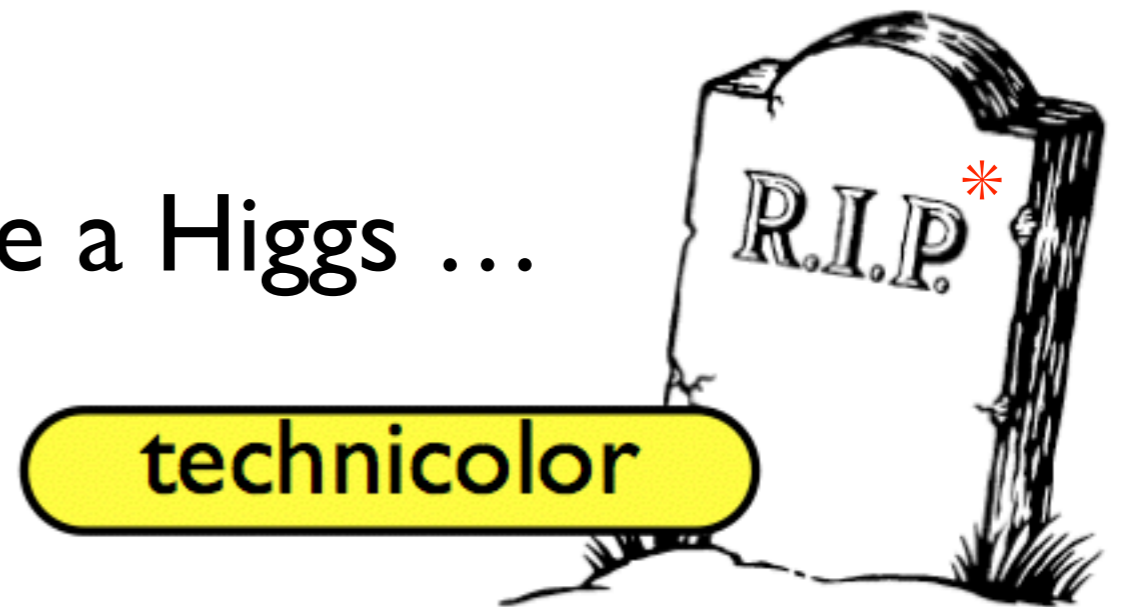
Longitudinal components of W & Z have tiny admixture of pions...

Technicolor

Scaled up version of QCD mechanism

$$\langle \bar{q}'_L q'_R \rangle \sim \Lambda_{\text{TC}}^3, \quad \Lambda_{\text{TC}} \sim \text{TeV}$$

Technicolor, doesn't have a Higgs ...

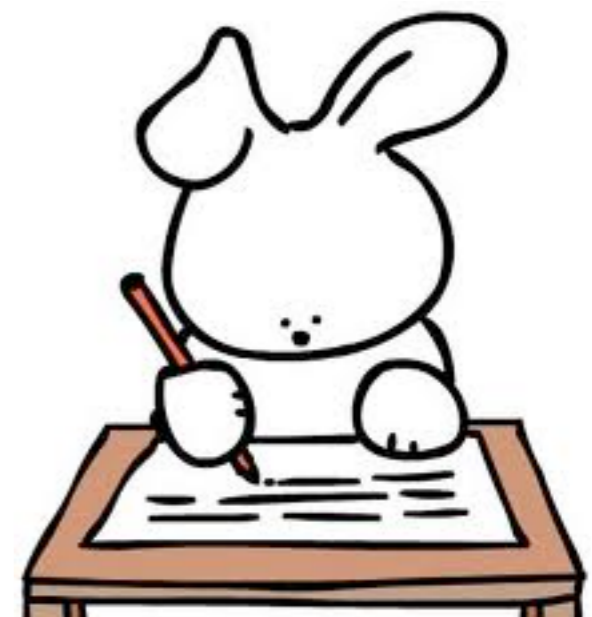


* the Higgs as the dilaton
as the last bastion ...

Composite Higgs

- Want to copy QCD, but extend pion sector (QCD: π^0, π^\pm)
- Higgs as a (pseudo) Goldstone boson

Need to learn about
goldstone bosons...



Quantum Protection

Symmetries can soften quantum behaviour

$$\mathcal{L} = |\partial_\mu \phi|^2 + \mu^2 |\phi|^2 - \lambda |\phi|^4 + \dots$$

breaks susy \rightarrow corrections must be
proportional to susy breaking

Shift symmetry

Higgs mass term can be forbidden

$$\mathcal{L} = |\partial_\mu \phi|^2 + \mu^2 |\phi|^2 - \lambda |\phi|^4 + \dots$$

$$\phi \rightarrow e^{i\alpha} \phi$$

does not forbid the mass²

$$\phi \rightarrow \phi + \alpha$$

works!

Can we make the Higgs transform this way?

Spontaneous breaking of U(1)

$$\langle \Phi \rangle = \frac{f}{\sqrt{2}}$$

$$\mathcal{L} = |\partial_\mu \phi|^2 + \mu^2 |\phi|^2 - \lambda |\phi|^4 + \dots$$

Instead using complex field

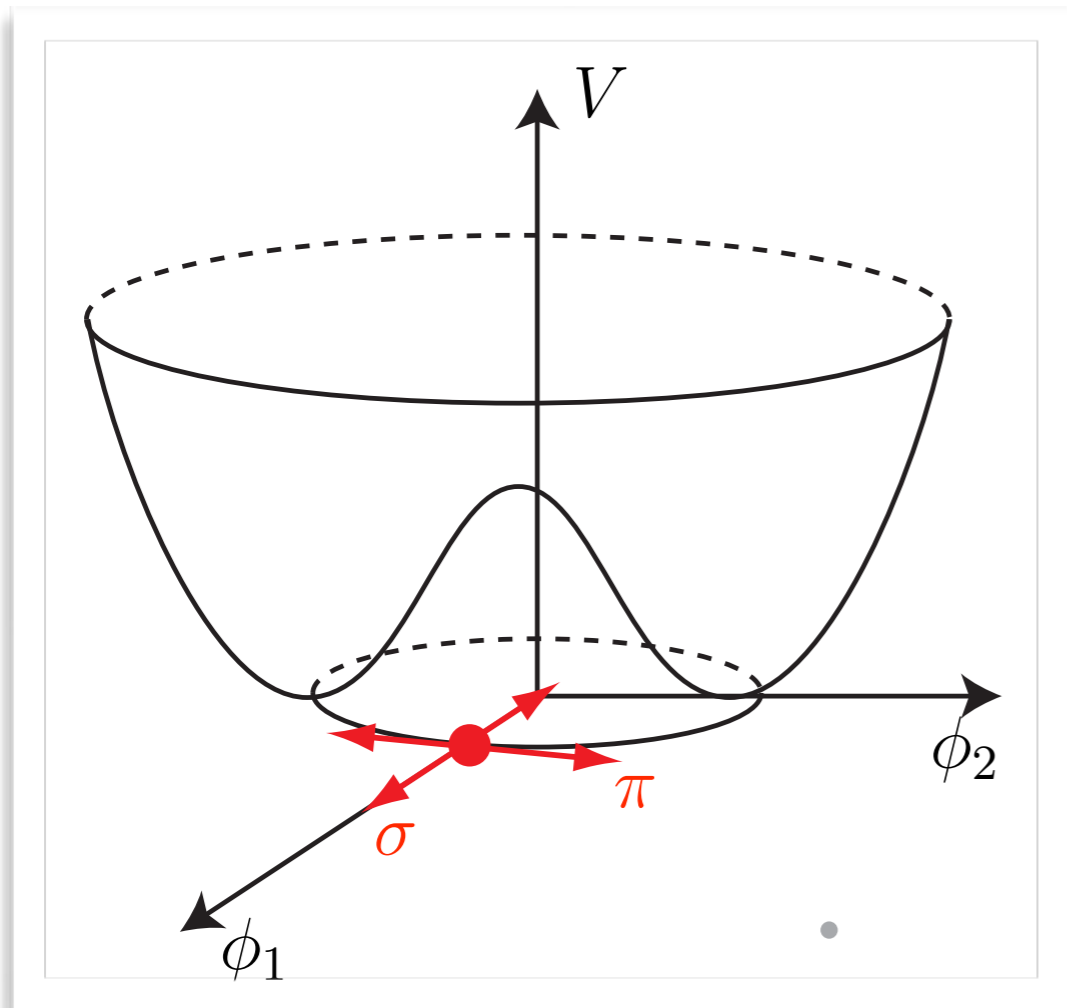
$$\phi = \phi_1 + i\phi_2$$

use real parametrisation

$$\phi(x) = \frac{1}{2} e^{i\pi(x)/f} (f + \sigma(x))$$

'phase'

'modulos'



$$\mathcal{L} = |\partial_\mu \phi|^2 + \mu^2 |\phi|^2 - \lambda |\phi|^4 + \dots \quad V(|\phi(x)|^2)$$

use $\phi(x) = \frac{1}{2} e^{i\pi(x)/f} (f + \sigma(x))$

$$\partial^\mu \phi^\dagger \partial_\mu \phi = \frac{1}{2} \partial^\mu \sigma \partial_\mu \sigma + \frac{1}{2} (1 + \sigma/f)^2 \frac{1}{2} \partial^\mu \pi \partial_\mu \pi$$

$$V(|\phi(x)|^2) = V(\sigma(x)) \quad \text{no mass term}$$

no dependence on $\pi(x)$

$$\frac{1}{2} \left(1 + \sigma(x)/f\right)^2 \frac{1}{2} \partial^\mu \pi \partial_\mu \pi + \frac{1}{2} \partial^\mu \sigma \partial_\mu \sigma - V(\sigma(x))$$

Using this parameterization a new symmetry is visible:

$$\pi(x) \rightarrow \pi(x) + \alpha$$

because $\pi(x)$ has only 'derivative interactions'

$$\partial_\mu (\pi(x) + \alpha) = \partial_\mu \pi(x)$$

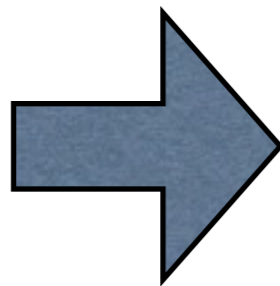
But what happened to the U(1) symmetry ?

$\pi(x), \sigma(x)$ are real...

But what happened to the U(1) symmetry ?

$$\phi \rightarrow e^{i\alpha} \phi$$

$$e^{i\pi(x)/f} (f + \sigma(x)) \rightarrow e^{i\alpha} e^{i\pi(x)/f} (f + \sigma(x))$$



$$\sigma(x) \rightarrow \sigma(x)$$

$$\pi(x) \rightarrow \pi(x) + \alpha$$

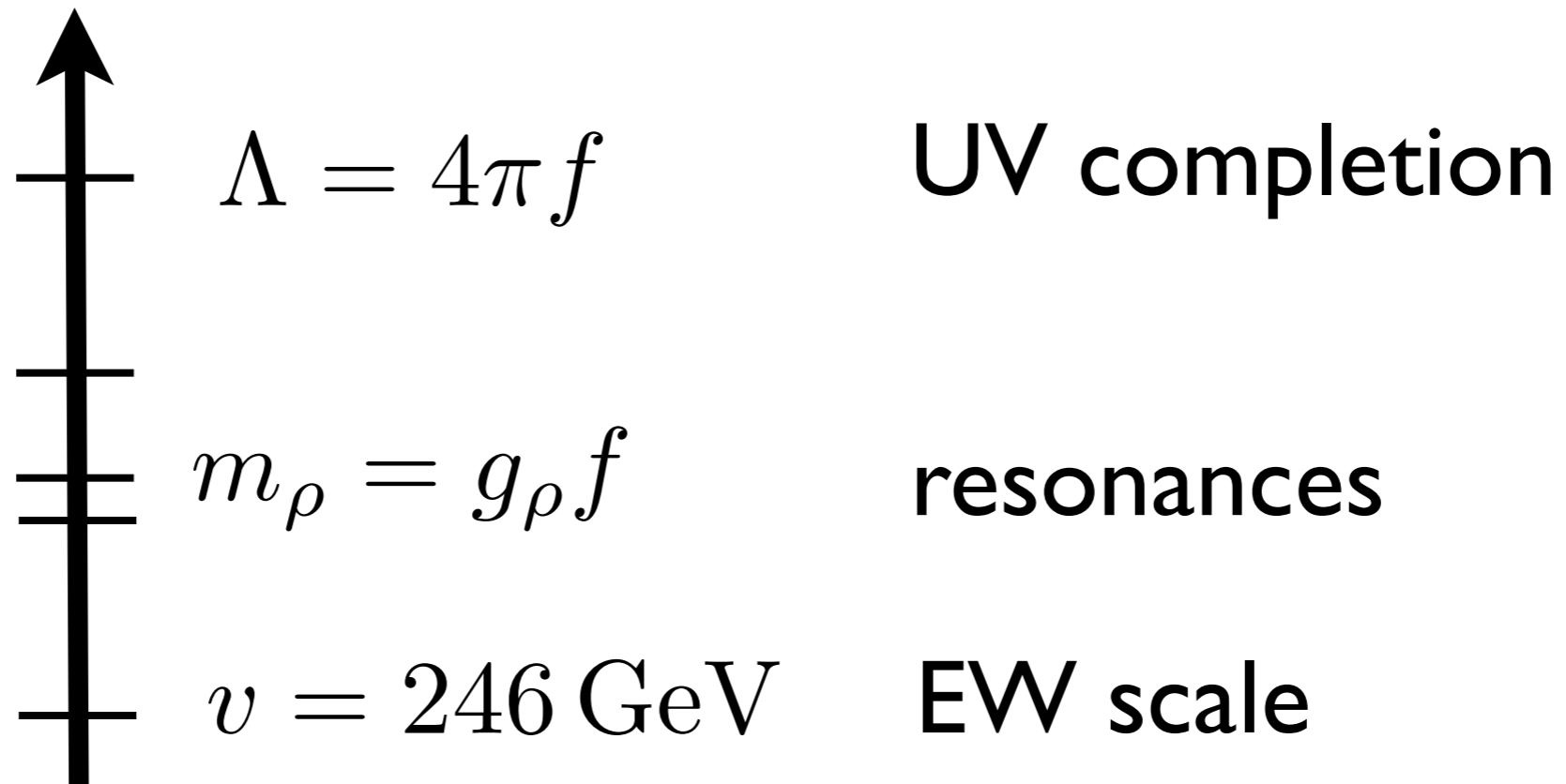
Phase rotation becomes shift symmetry

$\pi(x)$ is **massless** but also no

- gauge couplings
- potential
- yukawas

Semi-realistic model





pGB Higgs

$$SU(3) \rightarrow SU(2)$$

Break symmetry using

$$\langle \Phi \rangle = \begin{pmatrix} 0 \\ 0 \\ f \end{pmatrix}$$

Goldstone bosons = # broken generators

$$\Phi = \frac{1}{\sqrt{2}} e^{i\Pi/f} \begin{pmatrix} 0 \\ 0 \\ f + \sigma \end{pmatrix} \quad \Pi = \frac{1}{\sqrt{2}} \begin{pmatrix} \eta/\sqrt{3} & 0 & H_1 \\ 0 & \eta/\sqrt{3} & H_2 \\ H_1^* & H_2^* & -2\eta/\sqrt{3} \end{pmatrix}$$

$$\Phi = \frac{1}{\sqrt{2}} e^{i\Pi/f} \begin{pmatrix} 0 \\ 0 \\ f + \sigma \end{pmatrix} \quad \Pi = \frac{1}{\sqrt{2}} \begin{pmatrix} \eta/\sqrt{3} & 0 & H_1 \\ 0 & \eta/\sqrt{3} & H_2 \\ H_1^* & H_2^* & -2\eta/\sqrt{3} \end{pmatrix}$$

Expand

$$\Phi(x) = \begin{pmatrix} H_1(x) \\ H_2(x) \\ -\frac{2}{\sqrt{2}}\eta(x) \end{pmatrix} + \dots$$

Contains a Higgs: $H = \begin{pmatrix} H_1 \\ H_2 \end{pmatrix} = SU(2) \text{ doublet}$

$$SU(3) \rightarrow SU(2)$$

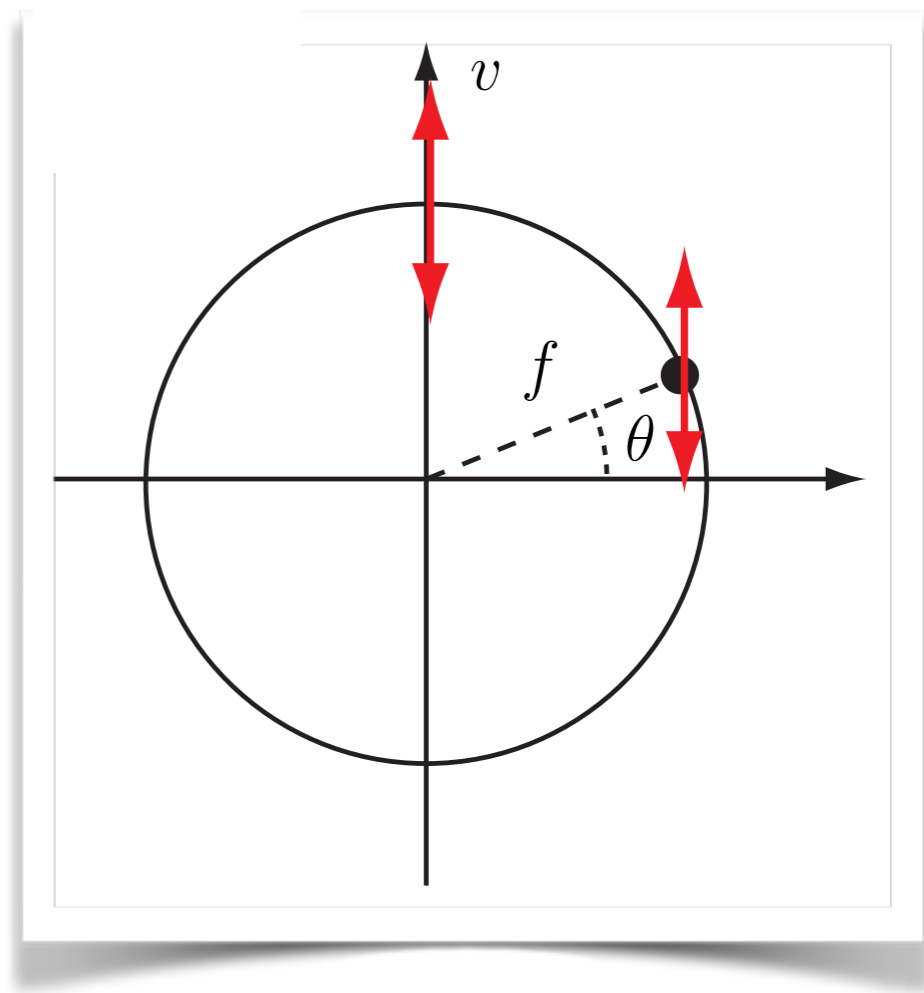
pGB Higgs

Unbroken gauge symmetry in global $SU(2)$,
dynamics generates ‘**vacuum misalignment**’

$SU(2)_L$ vs. $SU(2)$

$$\langle \Phi \rangle = \frac{f}{\sqrt{2}} \begin{pmatrix} 0 \\ \sin \theta \\ \cos \theta \end{pmatrix} \quad SU(2)_L$$

EW symmetry broken





vacuum misalignment

pGB Higgs

$$\langle \Phi \rangle = \frac{f}{\sqrt{2}} \begin{pmatrix} 0 \\ \sin \theta \\ \cos \theta \end{pmatrix} \text{SU}(2)_L$$

Electro-weak scale $v = f \sin \theta$

$f \sim$ scale of new physics

$\sin \theta \ll 1 \Leftrightarrow f \gg v$ (SM limit)

$$\Rightarrow \langle H \rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v \end{pmatrix}$$

Collective Breaking

We now want to add a yukawa coupling to give mass to the top quark

$$\lambda_t \bar{Q}_i H_i^c t_R \quad i: \text{sum over SU(2)}$$

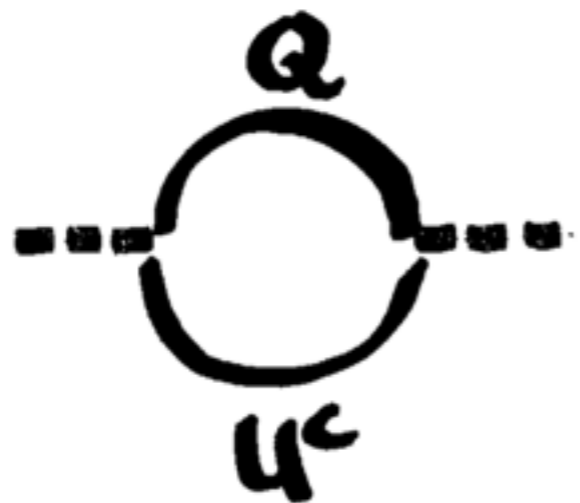
Fundamental field is a triplet

$$\phi = \exp \left\{ i \begin{pmatrix} h_1 \\ h_2 \\ h_1^* & h_2^* \end{pmatrix} \right\} \begin{pmatrix} \\ \\ f \end{pmatrix}$$

Top yukawa: 1st try

$$\sum_i^2 \lambda_t \phi_i^c \bar{Q}_i t_R \quad \text{works, gives mass to the top}$$

... but breaks **SU(3)** structure explicitly, does not respect Goldstone symmetry protecting the Higgs mass:



A Feynman diagram showing a top quark loop. The top quark line is labeled 'Q' at the top and 't^c' at the bottom. A Higgs boson line, represented by a dashed line, enters from the left and exits to the right, connecting to the top quark loop. The diagram is followed by an approximation symbol and the expression $\frac{\lambda_t^2}{16\pi^2} \Lambda_{UV}^2$.

$$\sim \frac{\lambda_t^2}{16\pi^2} \Lambda_{UV}^2$$

we've accomplished nothing---

2nd try: Collective breaking

Example: $SU(3) \rightarrow SU(2)$ (ignore $U(1)_Y$ again)

$$\langle \Phi_1 \rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ 0 \\ f_1 \end{pmatrix} \quad \langle \Phi_2 \rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ 0 \\ 2 \end{pmatrix}$$

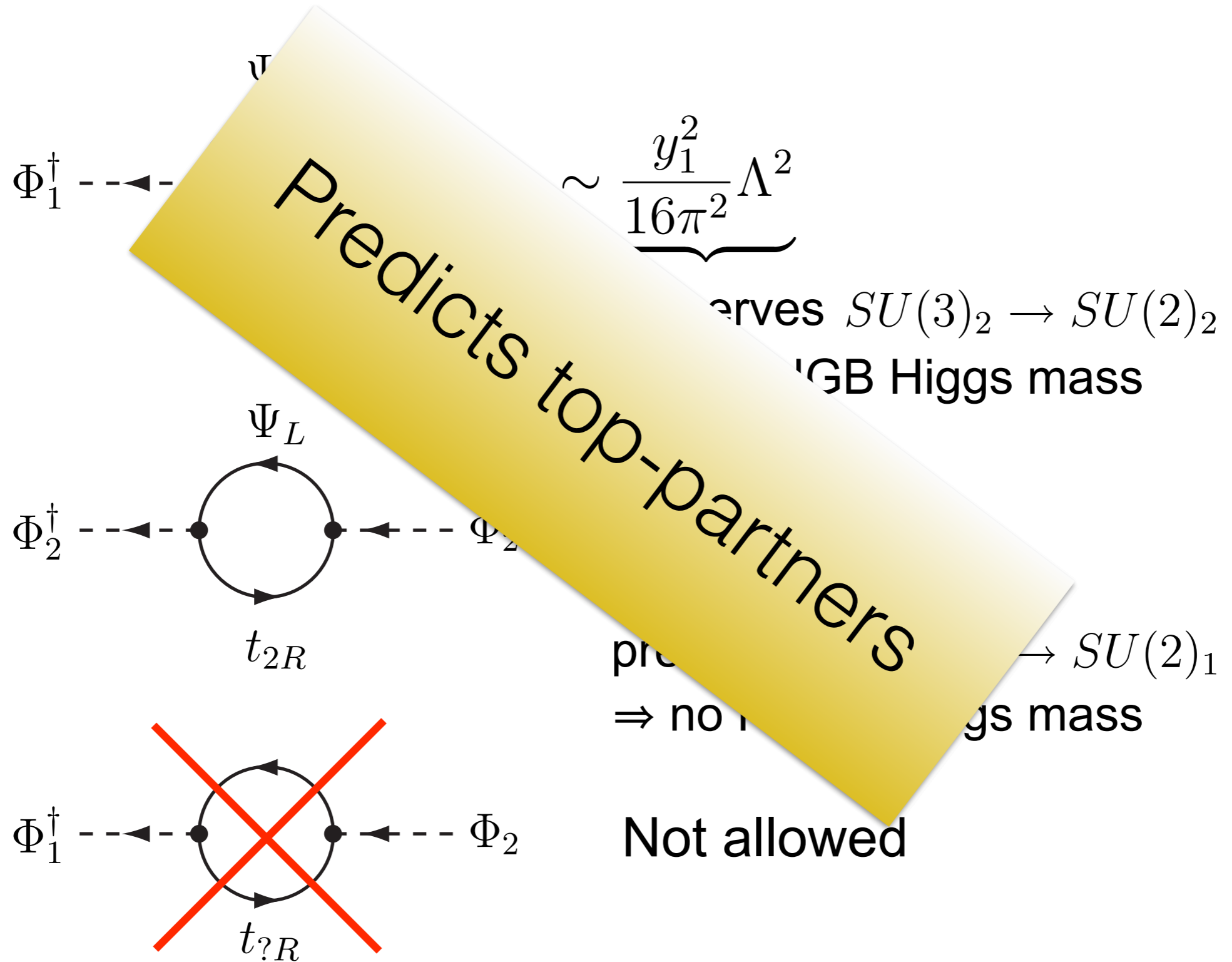
Gauge full $SU(3) \Rightarrow$ exact symmetry

$$\Psi_L = \begin{pmatrix} t_L \\ b_L \\ T_L \end{pmatrix} \quad t_{1R}, t_{2R}, b_R$$

$$\mathcal{L}_{\text{Yukawa}} = y_1 \bar{\Psi}_L \Phi_1 t_{1R} + y_2 \bar{\Psi}_L \Phi_2 t_{2R}$$

$y_1 \rightarrow 0 \Rightarrow$ exact $SU(3)_2 \rightarrow SU(2)_2$ and vice versa

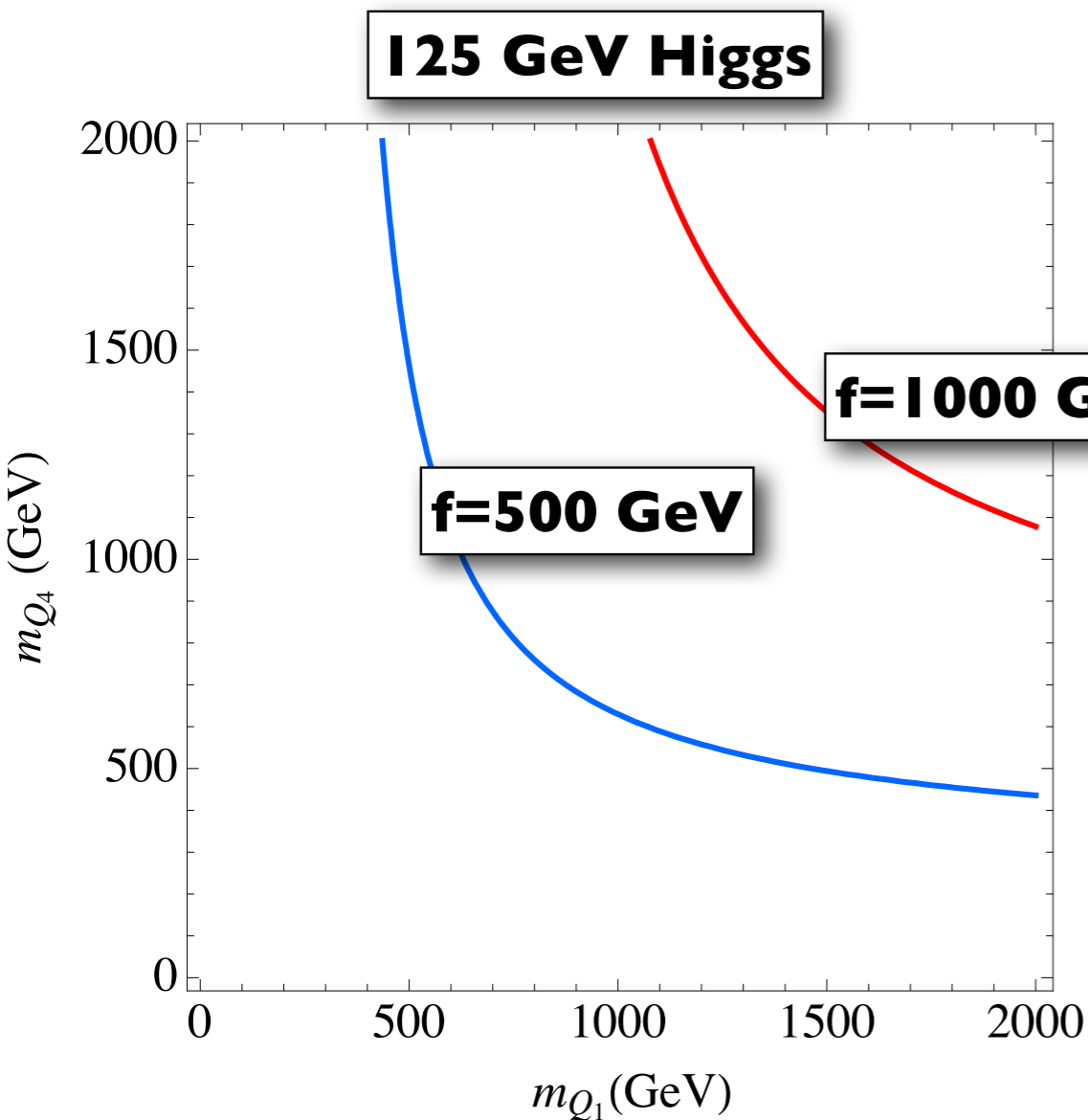
Both $y_1, y_2 \neq 0$ required for non-derivative couplings
of PNGB Higgs



Light Higgs implies light fermionic top partners

$$m_h^2 \simeq \frac{N_c}{\pi^2} \left[\frac{m_t^2}{f^2} \frac{m_{Q_4}^2 m_{Q_1}^2}{m_{Q_1}^2 - m_{Q_4}^2} \log \left(\frac{m_{Q_1}^2}{m_{Q_4}^2} \right) \right]$$

Pomarol et al; Marzocca



$$5 = 4 + 1$$

$Q_4 \quad Q_1$

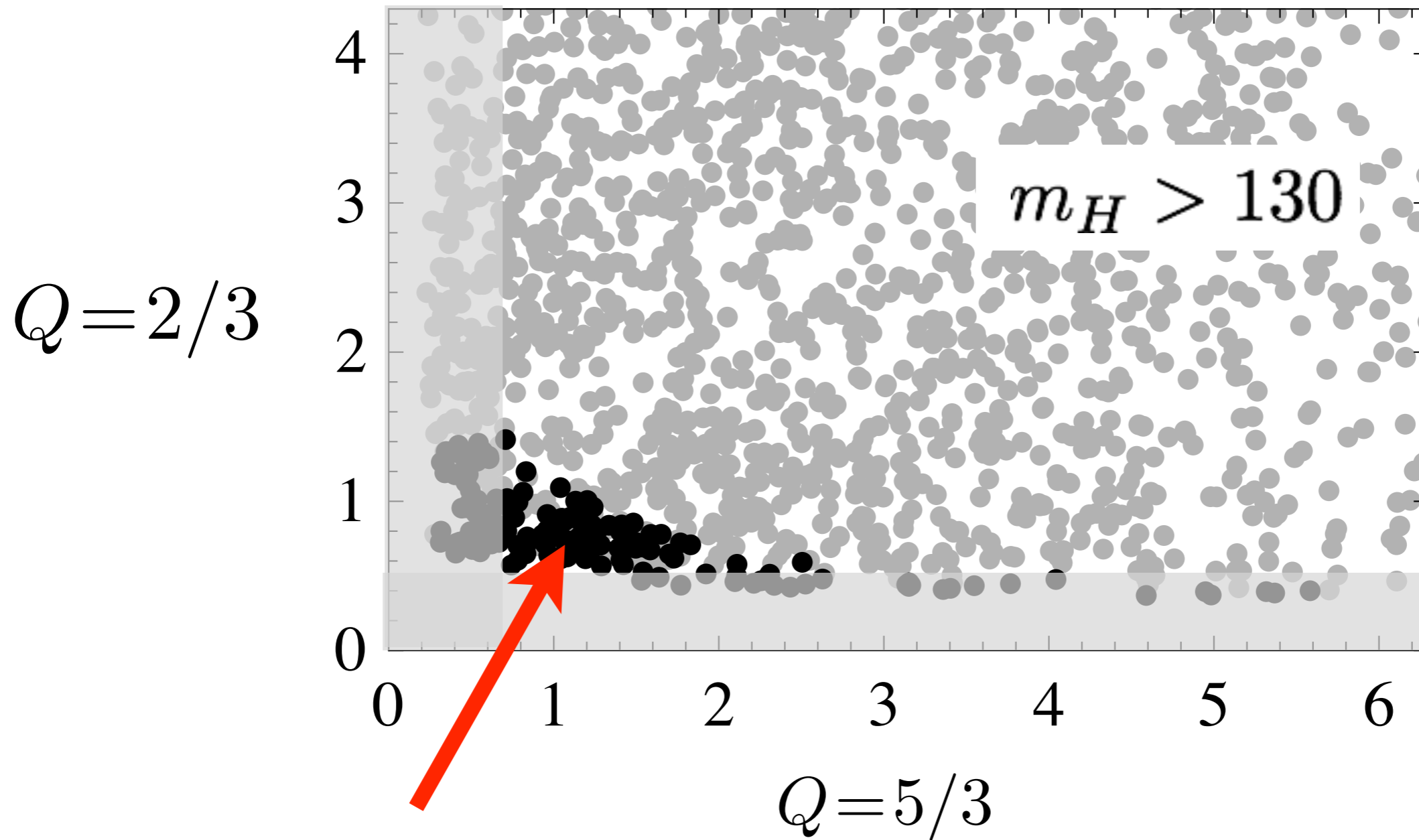
with EM charges $5/3, 2/3, -1/3$

Contino et al; Pomarol, Riva;
Matsedonskyi, Panico, Wulzer; Redi, Tesi;
Marzocca, Serone, Shu;

Scan over composite Higgs parameter space

$$\xi = 0.2$$

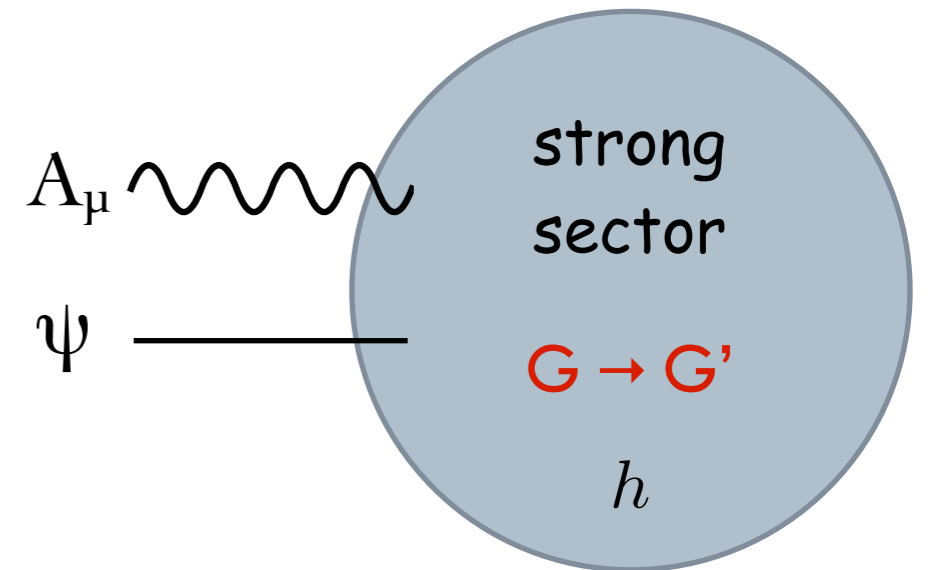
from 1204.6333



$m_H = 115 \dots 130$ GeV

Minimal composite Higgs

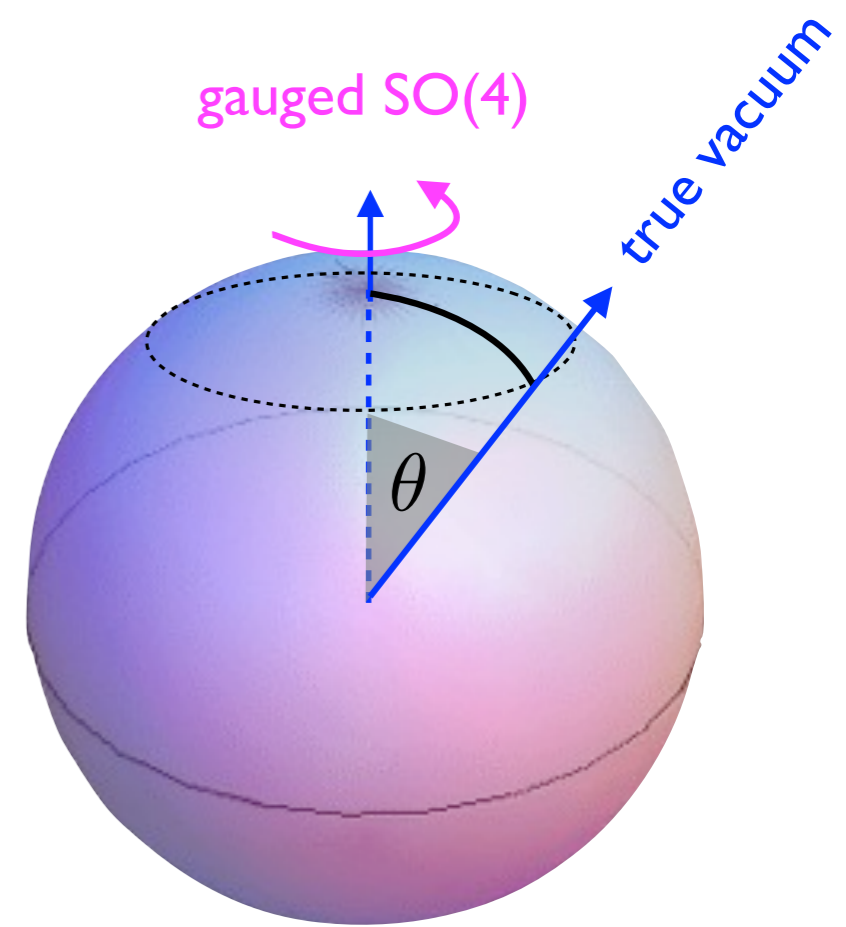
Agashe et. al



Minimal bottom up construction

$$SO(5) \rightarrow SO(4) \sim SU(2)_L \times SU(2)_R$$

$SO(5)/SO(4)$



Tree level: gauge $SO(4)$ aligned

Higgs

$$\phi = e^{i\pi \hat{a} T^{\hat{a}} / f} \begin{pmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 1 \end{pmatrix} = \begin{pmatrix} \sin(\pi/f) \times \begin{pmatrix} \hat{\pi}^1 \\ \hat{\pi}^2 \\ \hat{\pi}^3 \\ \hat{\pi}^4 \end{pmatrix} \\ \cos(\pi/f) \end{pmatrix} \stackrel{\text{I-loop } \langle \phi(x) \rangle = \theta \cdot f}{=} \begin{pmatrix} \sin(\theta + h(x)/f) e^{i\chi^i(x) A^i / v} \begin{pmatrix} 0 \\ 0 \\ 0 \\ 1 \end{pmatrix} \\ \cos(\theta + h(x)/f) \end{pmatrix}$$

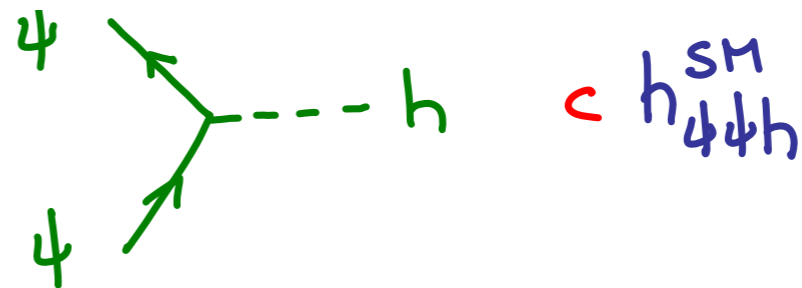
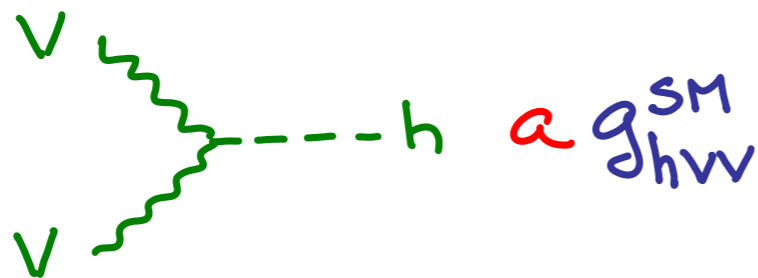
eaten by W_L, Z_L

Deviations from SM Higgs

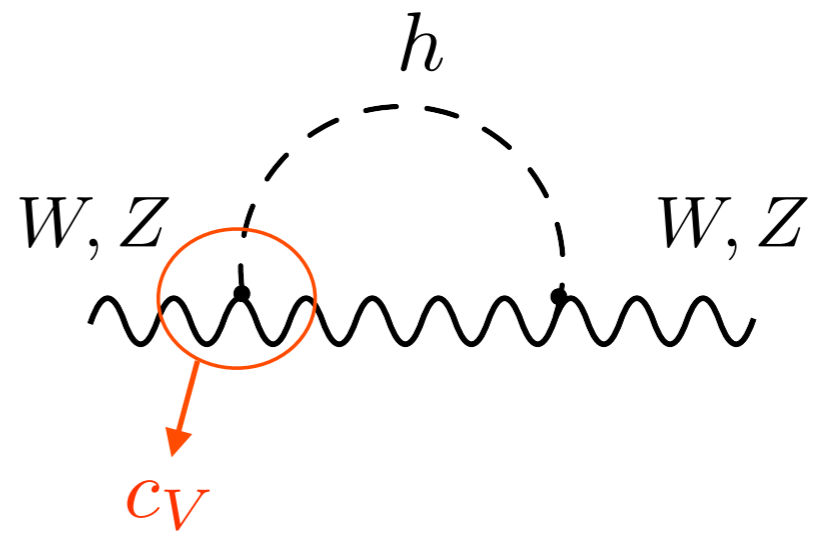
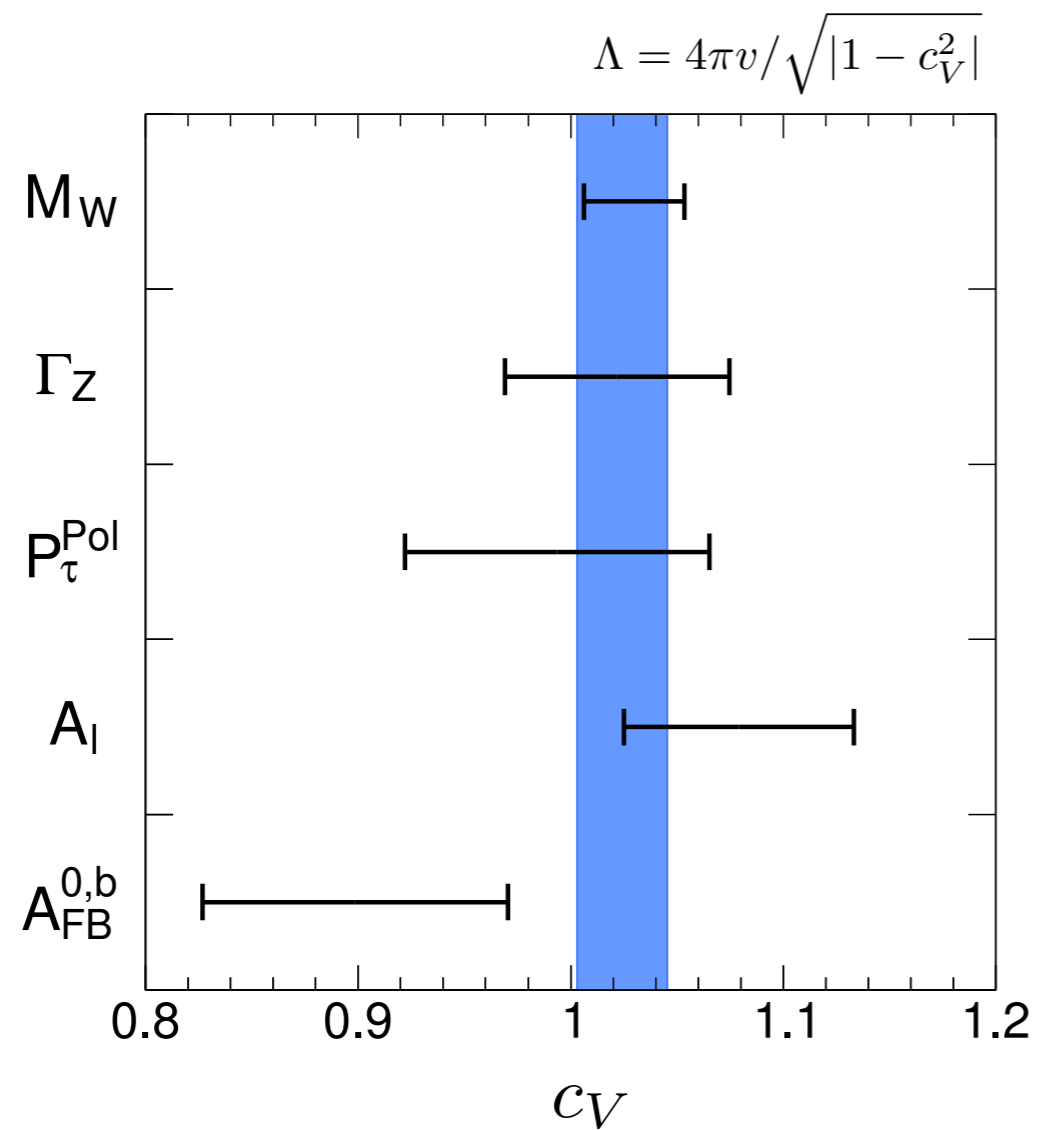
Goldstone boson nature

$$f^2 \left| \partial_\mu e^{i\pi/f} \right|^2 = |D_\mu H|^2 + \frac{c_H}{2f^2} [\partial_\mu (H^\dagger H)]^2 + \frac{c'_H}{2f^4} (H^\dagger H) [\partial_\mu (H^\dagger H)]^2 + \dots$$

Giudice et al. JHEP 0706 (2007) 045

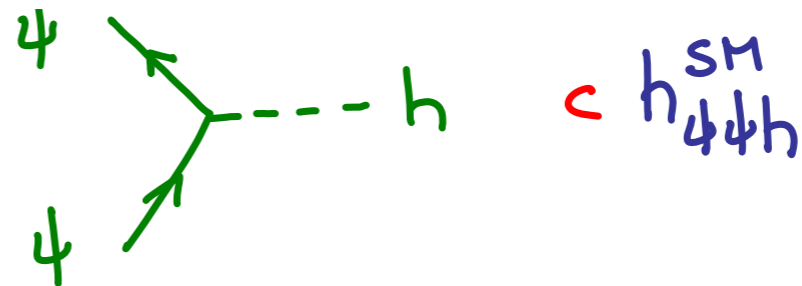
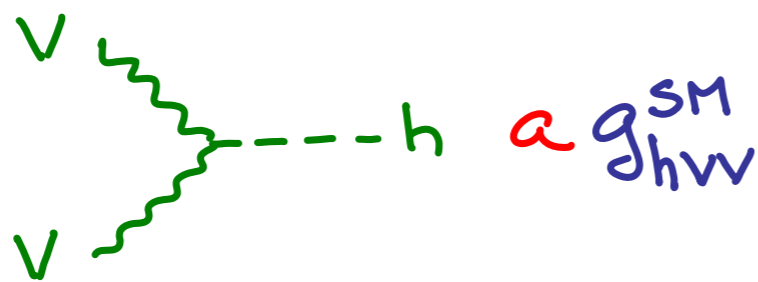


EW precision tests



Higgs couplings

Have been measured to 20-30% precision



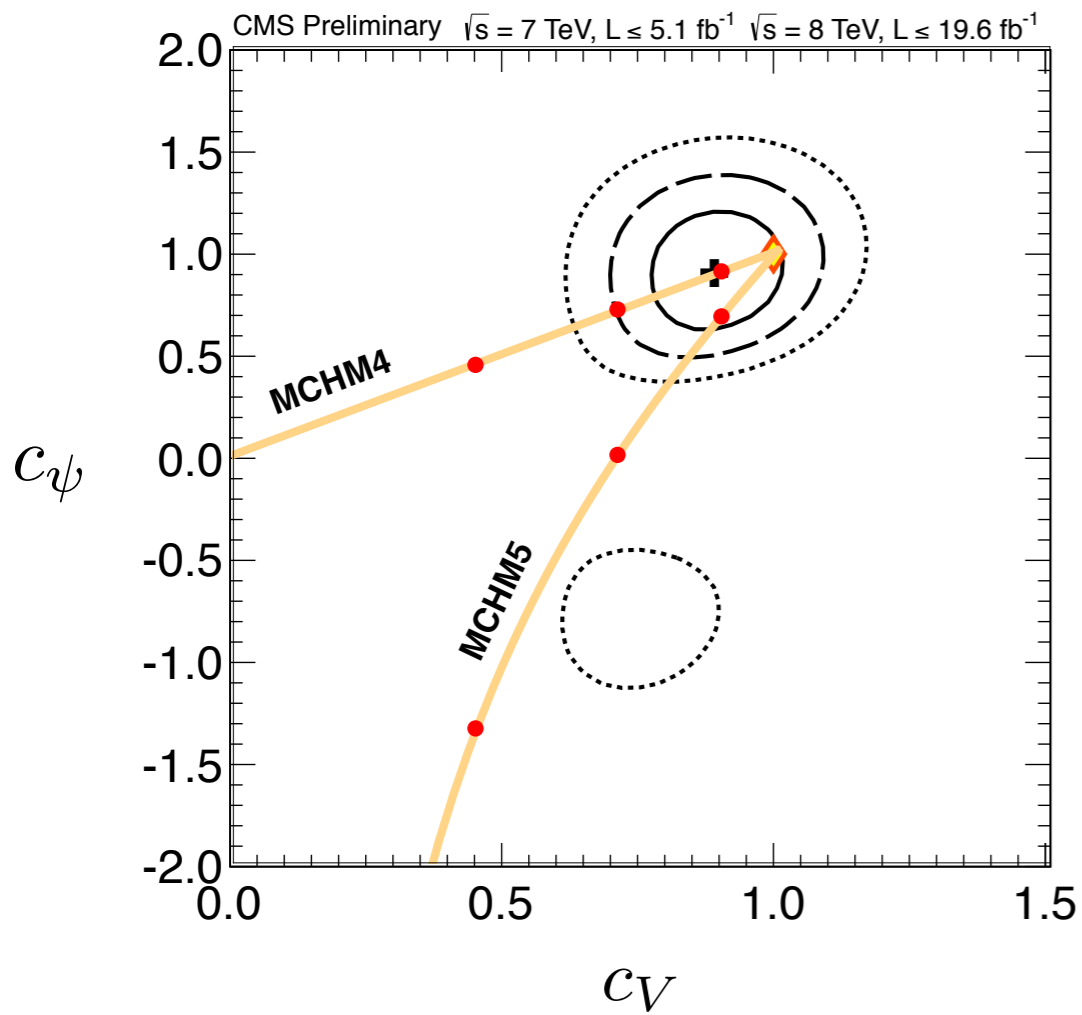
Expect deviations $\sim (v/f)^2$

$$\xi \equiv \frac{v^2}{f^2}$$

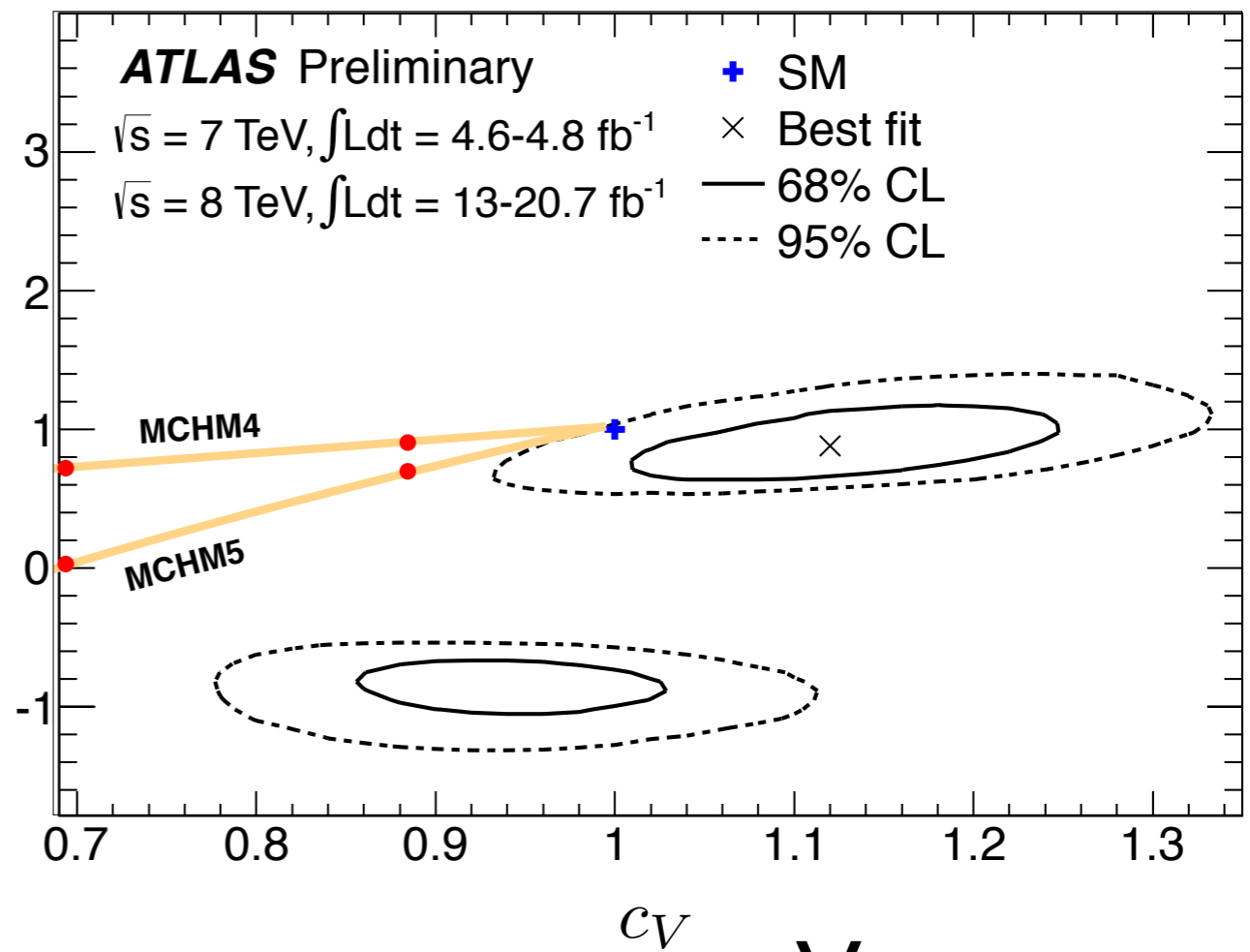
$$a = \sqrt{1 - \xi}$$

$$c_f = \frac{1 - (1 + n)\xi}{1 - \xi}$$

Higgs couplings



Fermion



Red points at $\xi \equiv (v/f)^2 = 0.2, 0.5, 0.8$

Vector